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Prova 2

19.2.4007

Questão 2.

$$\begin{cases} T(n) = 2T(n/2) + 2 \\ T(1) = 1 \end{cases}$$

$$T(n) = 2T(n/2) + 2$$

$$T(n) = 2(2T(n/4) + 2) + 2 \Rightarrow 4T(n/4) + 6$$

$$T(n) = 4(2T(n/8) + 2) + 6 \Rightarrow 8T(n/8) + 14$$

$$T(n) = 8(2T(n/16) + 2) + 14 \Rightarrow 16T(n/16) + 30$$

⋮

⋮

$$T(n) = 2^k T(n/2^k) + 2^{k+1} - 2 \quad \text{para } n > 1$$

$$\bullet \text{ Para } T(1) = 1. \text{ logo } n/2^k = 1 \Rightarrow k = \log_2 n$$

Substituindo

para $n = 1$

$$T(n) = 2^{\log_2 n} T(n/2^{\log_2 n}) + 2^{\log_2 n + 1} - 2$$

$$T(n) = n T(1) + 2n - 2$$

$$T(n) = n T(1) + 2n - 2$$

$$T(n) = 3n - 2 //$$