

Name _____ StudentID _____

In this lab, write a program of FindGCD1, FindGCD2 and FindGCD3. Identify the basic operation of each step, and add instructions to count the number of times the operation that are executed.

FindGCD1(m,n)

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Step 1  Assign the value of  $\min\{m,n\}$  to  $t$ 
Step 2  Divide  $m$  by  $t$ . If the remainder is 0, go to Step 3;
        otherwise, go to Step 4
Step 3  Divide  $n$  by  $t$ . If the remainder is 0, return  $t$  and stop;
        otherwise, go to Step 4
Step 4  Decrease  $t$  by 1 and go to Step 2
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FindGCD2(m,n)

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Step 1  Find the prime factorization of  $m$ 
Step 2  Find the prime factorization of  $n$ 
Step 3  Find all the common prime factors
Step 4  Compute the product of all the common prime factors
        and return it as  $\gcd(m,n)$ 
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FindGCD3(m,n)

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if  $m > n$ , then  $\text{GCD}(m, n) = \text{GCD}(m - n, n) = \text{GCD}(m, m - n)$ 
if  $m = n$ , then  $\text{GCD}(m, n) = m = n$ 
if  $m < n$ , then  $\text{GCD}(m, n) = \text{GCD}(m, n - m) = \text{GCD}(n - m, n)$ 
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