UNIVERSITÄT DES SAARLANDES Prof. Dr.-Ing. Philipp Slusallek Computer Graphics Group Arsène Pérard-Gayot (perard@cg.uni-saarland.de)



Use this in the practical e

25. November 2019

Introduction to Computer Graphics Assignment 5

Submission deadline for the exercises: 2. December 2019

The paper copies for the theoretical parts of the assignments will be collected at the beginning of the lecture on the due date. The programming parts must instead be marked as release before the beginning of the lecture on the due date. The code submitted for the programming part of the assignments is required to reproduce the provided reference images. The submission ought to tag the respective commit in your group's git repository as well as attach the mandatory generated images to the release. The submission should also contain a creative image show-casing all extra-credit features that have been implemented.

The projects are expected to compile and work out of the box. A successful build by Drone CI is a good indicator. If it fails to do so on our Windows or Linux computers, we will try to do so on the CIP-pool students' lab as a "fallback".

To pass the course you need for every assignment at least 50% of the points.

5.1 Normalization of the Phong BRDF (10 + 20 Points)

The *Phong* BRDF has the following form:

$$f(\omega_i, \omega_o) = k_d + k_s \cos^n(\omega_r, \omega_o)$$

where ω_r is the result of the reflection of the incoming direction ω_i along the surface normal N. The goal of this exercise is to find the possible values of k_d and k_s so that f is energy conserving. In order to do this, we define ρ_s and ρ_d such that:

$$k_d = \frac{\rho_d}{C_d}$$

$$k_s = \frac{\rho_s}{C_s}$$

$$\rho_d + \rho_s \le 1$$

$$\rho_s, \rho_d \ge 0$$

 C_s and C_d are the normalization factors needed to make the BRDF energy conserving.

- a) Assume that $k_s = 0$ (this means $\rho_s = 0$ and $\rho_d \in [0,1]$). Derive the expression of C_d so that f is energy conserving.
- **b)** Assume that $k_d = 0$ (this means $\rho_d = 0$ and $\rho_s \in [0, 1]$). Derive the expression of C_s so that f is energy conserving.

1

Hint: we are interested in the maximum of the reflected energy, which happens when the outgoing direction is parallel to the normal $(\omega_o = N)$. The cosine term becomes $cos(\omega_r, \omega_o) = cos(\omega_r, N) = cos(\omega_i, N)$.

5.2 Analytical solution of the rendering equation in 2D (20 Points)

The Figure 1 shows a simple 2D scene with a linear light source L of uniform radiance 1 for each point and direction. Assume that the light source absorbs all light hitting it. Located at the y = 0 line is a Lambertian material with the following BRDF:

$$f_r(\omega, (p, 0), \omega_o) = \frac{1}{\pi}$$

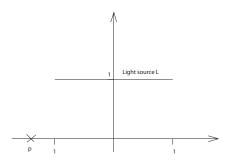


Figure 1: The linear light source reaches from -1 to 1 at y-position 1 with a uniform radiance of 1 for each point on the light source and each direction.

a) The standard rendering equation in 2D is given by:

$$L(x,\omega_o) = L_e(x,\omega_o) + \int_0^{\pi} f_r(\omega, x, \omega_o) \cdot L(x,\omega) \cdot \cos\phi \cdot d\omega$$

Solve the rendering equation analytically for each point x = (p, 0) and direction ω_o . As the rendering equation shows, you have to integrate over the hemicircle for each point x.

b) Let S be the set of all points on the light source (the y = 0 plane can be ignored here) then the point form of the rendering equation in 2D is given by:

$$L(x,\omega_o) = L_e(x,\omega_o) + \int_{y \in S} f_r(\omega_i, x, \omega_o) \cdot L(y, -\omega_i(x, y)) \cdot \frac{\cos\phi_i \cos\phi_y}{|x - y|} \cdot dA_y$$

Note that the denominator |x - y| is really the distance not the squared distance as in the 3D version. Again solve the equation analytically, but now by integrating over the light source.

5.3 Basic Materials (10 Points)

When a ray intersects a solid object, lighting at the hit point has to be computed. This depends on:

- The light sources around the hit point
- The material of which the solid is made

A Material is defined by:

- The reflectance (getReflectance) computes the amount of light that is reflected on a material surface. It depends on the following parameters:
 - inDir the direction vector (in world coordinate space) from which the light is incoming
 - outDir the direction to the viewer, where the light is reflected to
 - normal the surface normal vector at the hit point
 - texPoint the local coordinate of the hit point. Currently it should be simply Intersection::local(), in the future we will compute some texture coordinates to supply this function.



Figure 2: Final image using the colored point light sources. In the code we ask to create two images of the same scene with different scale, but the output should be identical.

• The emission (getEmission) of the material itself towards given direction. Similarly to reflectance, it requires outDir, normal and texPoint.

Note that reflectance denotes only the percentage of that light that is being reflected. It does *not* compute the actual amount of light. For that reason you never need to trace any additional rays from within the material. Shooting rays is the job of the Integrator.

In some cases it is convenient for computational purposes to include the cosine term from the rendering equation into the material itself, and that is why the getReflectance function should account for the cosine term as well.

While these two functions can fully describe the material, they are sometimes insufficient for practical reasons. Only the material "knows" which combination of the above parameters yield significant results. For that reason a Material provides additional functionality - sampling - which we will discuss in the future. At the moment however the sampling-related functions may be left unimplemented.

Your task is to implement a very simple material (DummyMaterial) which should emit no light, and have reflectance fr = 1. (multiplied by the cosine term from the rendering equation)

You should also update all Primitive classes to now support setMaterial. Calling this function on a single Solid should set the material of that solid, while calling it on a Group should change the material of all the contained objects.

5.4 Lighting (5 + 30 Points)

In order to compute lighting we need light sources in the scene. A Light is an object that lights the scene and as such is being queried only in relation to some hit point between a ray and a solid. It is defined by two functions:

• getLightHit — provides a direction vector from the intersection point p towards the light source, and a distance along this vector.

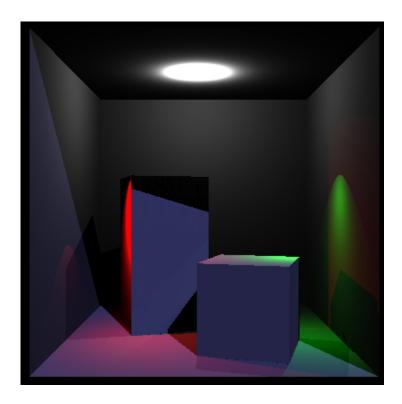


Figure 3: Final image using the colored spot lights (red and green) and a directional light (blue).

• getIntensity — computes the amount of light reaching the intersection point (defined by the result of getLightHit) assuming no obstacles in between.

Note that these functions define only the light itself. We do not care about the scene, shadows, etc... that will be the task of the Integrator.

As a simple realization of a light source, implement a PointLight source. A point light is defined by a position in space and its intensity. The effective irradiance dissipates proportionally to the square distance from the source to the hit point.

Implement a new RayTracingIntegrator. When a hit point is found, it should compute the lighting:

- Iterate over all light sources in the World.
- For each light source compute the shadow ray.

for a light that is infinitely faraway, incoming ray

- Confirm that the shadow ray and the primary ray leave the surface on the same side.
- Trace a shadow ray into the world to detect any obstacles between the light source and the hit point.
- If no obstacle is found, query the light for the intensity.
- Use the irradiance intensity and the material properties to compute the amount of reflected light.
- In addition add the emitted light of the material.

5.5 Light Sources (8 + 12 Points)

Implement the following light sources:

• DirectionalLight — a light that illuminates the whole scene from a single direction. The distance to the light source is always infinity (use FLT_MAX) and the intensity is constant.

• SpotLight — clipped Warn spot light. It is similar to point light, except that it illuminates only in a cone. The irradiance is nonzero only along those directions that form an angle lower than angle with a specified direction vector, with intensity proportional to the cosine lobe raised to the exponent exp.

5.6 More Light Sources (15 Points)*

Implement a ProjectiveLightSource that behaves similarly to PointLight but emits a different light color depending on the direction vector. Use the Julia function as the projection pattern.