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LAB REPORT
on
Artificial Intelligence (23CS5PCAIN)

Submitted by

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in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING
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**B.M.S. College of Engineering,
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CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Navanidhi D J(1BM23CS204)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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Github Link:

https://github.com/NavanidhiDJ/Artificial_intelligence-

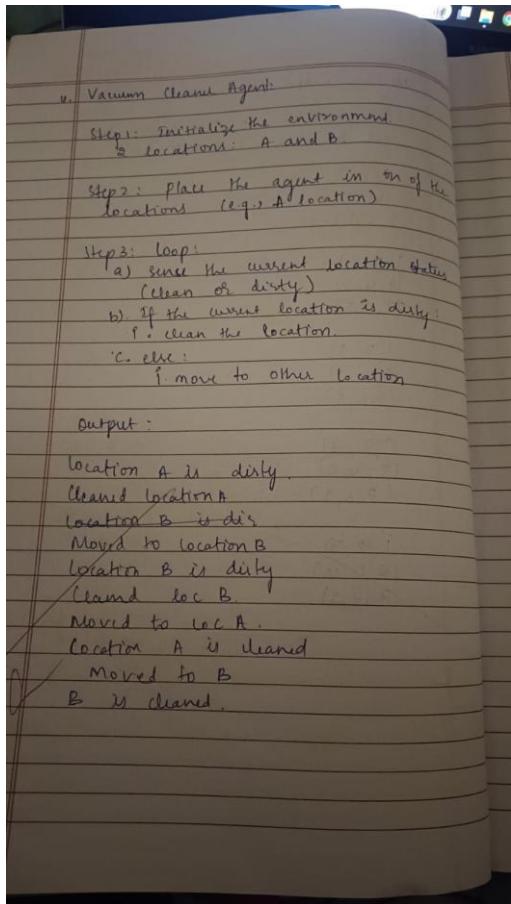
Program 1

Implement Tic - Tac - Toe Game
Implement vacuum cleaner agent

Algorithm:

The image shows two pages of handwritten notes. The left page is dated 29/9/25 and titled "Tic-tac-toe Algorithm". It lists six steps: 1. Initialize with an empty board. 2. Define a function to print the 3x3 board. 3. Define a function to check for a win (diagonals, rows, columns). 4. Define a function to check if it's a draw (all positions filled with 'X' or 'O'). 5. Define a function to place a letter ('X' or 'O') at a free space. 6. Define a function for the player's move. The right page is dated 30/9/25 and titled "Minimax". It discusses the minimax function and provides three examples of a 3x3 board state:

- Example 1: A board where 'X' has won vertically. The board is labeled "winning".
- Example 2: A board where 'O' has won vertically. The board is labeled "winning".
- Example 3: A board where the game is a draw. The board is labeled "draw".



CODE:

Tic Tac Toe:

```

def print_board(board):
    for row in board:
        print(" | ".join(row))
        print("-" * 5)

def check_winner(board, player):
    for row in board:
        if all(cell == player for cell in row):
            return True
    for col in range(3):
        if all(board[row][col] == player for row in range(3)):
            return True
    if all(board[i][i] == player for i in range(3)):
        return True
    if all(board[i][2 - i] == player for i in range(3)):
        return True
    return False
  
```

```

def is_draw(board):
    return all(cell != " " for row in board for cell in row)

def play_game():
    board = [[" " for _ in range(3)] for _ in range(3)]
    current_player = "X"
    while True:
        print_board(board)
        print(f"Player {current_player}'s turn.")
        try:
            row = int(input("Enter row (0, 1, 2): "))
            col = int(input("Enter col (0, 1, 2): "))
        except ValueError:
            print("Invalid input. Please enter numbers 0, 1, or 2.")
            continue
        if row not in [0, 1, 2] or col not in [0, 1, 2] or board[row][col] != " ":
            print("Invalid move. Try again.")
            continue
        board[row][col] = current_player
        if check_winner(board, current_player):
            print_board(board)
            print(f"🎉 Player {current_player} wins!")
            break
        if is_draw(board):
            print_board(board)
            print("It's a draw!")
            break
        current_player = "O" if current_player == "X" else "X"

if __name__ == "__main__":
    play_game()

```

```

VACUUM CLEANER AGENT :
class VacuumCleanerAgent:
    def __init__(self):
        self.location = 'A'

    def perceive_and_act(self, environment):
        current_status = environment[self.location]

        if current_status == 'Dirty':
            action = 'Suck'
            environment[self.location] = 'Clean'
        else:
            action = 'Move Right' if self.location == 'A' else 'Move Left'
            self.location = 'B' if self.location == 'A' else 'A'

```

```

    return action

def run_vacuum_agent(environment):
    agent = VacuumCleanerAgent()
    steps = 0

    print(f'Initial environment: {environment}')
    while 'Dirty' in environment.values():
        action = agent.perceive_and_act(environment)
        print(f'Step {steps}: Agent at {agent.location}, Action: {action}, Environment: {environment}')
        steps += 1

    print("Environment is clean!")

if __name__ == "__main__":
    env = {'A': 'Dirty', 'B': 'Dirty'}
    run_vacuum_agent(env)

```

```

Welcome to Tic Tac Toe!
You are X, computer is O.

| |
| |
| |

Enter your move (1-9): 1
X | |
| |
| |

Computer's turn...
X | O |
| |
| |

Enter your move (1-9): 5
X | O |
| X |
| |

Computer's turn...
X | O |
| X |
O | |

Enter your move (1-9): 9
X | O |
| X |
O | | X

you win!

```

```

Initial State:
Room A: Dirty, Room B: Dirty, Agent at: A

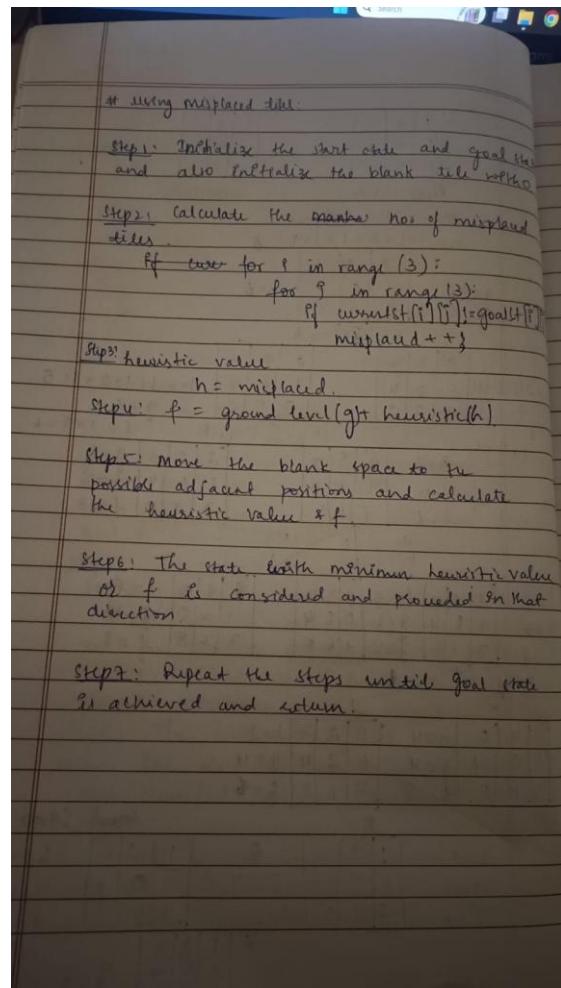
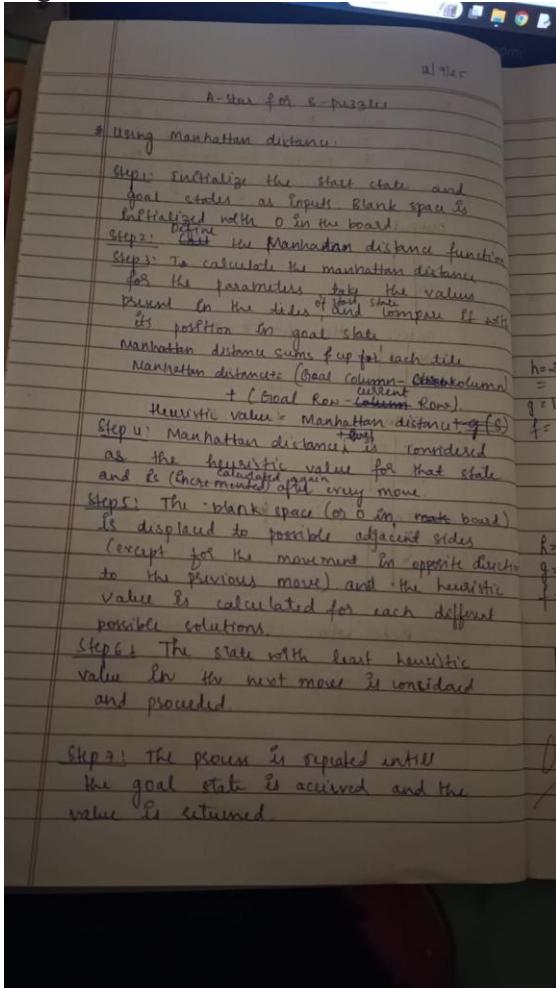
Vacuum Cleaner Starting!
Action: Suck (cleaning Room A)
Room A: Clean, Room B: Dirty, Agent at: A
Action: Move Right
Room A: Clean, Room B: Dirty, Agent at: B
Action: Suck (cleaning Room B)
Room A: Clean, Room B: Clean, Agent at: B
Task Completed! Both Room Are Clean

```

2. 8 Puzzle using A star(Manhattan)

8 Puzzle using A star(Misplaced Tiles)

Algorithm:



Code:

```
import heapq
```

```
def misplaced_tiles(state, goal):
    return sum(1 for i in range(9) if state[i] != 0 and state[i] != goal[i])
```

```
def get_neighbors(state):
    neighbors = []
    zero_pos = state.index(0)
    x, y = divmod(zero_pos, 3)
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]
```

for dx, dy in directions:
nx, ny = x + dx, y + dy

```

if 0 <= nx < 3 and 0 <= ny < 3:
    new_pos = nx * 3 + ny
    new_state = list(state)
    new_state[zero_pos], new_state[new_pos] = new_state[new_pos], new_state[zero_pos]
    neighbors.append(tuple(new_state))
return neighbors

def a_star(start, goal):
    open_set = []
    heapq.heappush(open_set, (0 + misplaced_tiles(start, goal), 0, start, []))
    closed_set = set()

    while open_set:
        f, g, current, path = heapq.heappop(open_set)

        if current == goal:
            return path + [current]

        if current in closed_set:
            continue
        closed_set.add(current)

        for neighbor in get_neighbors(current):
            if neighbor in closed_set:
                continue
            new_g = g + 1
            new_f = new_g + misplaced_tiles(neighbor, goal)
            heapq.heappush(open_set, (new_f, new_g, neighbor, path + [current]))

    return None

def print_puzzle(state):
    for i in range(0, 9, 3):
        print(state[i:i+3])
    print()

def input_state(prompt):
    while True:
        try:
            s = input(prompt)
            lst = tuple(int(x) for x in s.strip().split())
            if len(lst) != 9 or set(lst) != set(range(9)):
                raise ValueError
            return lst
        except ValueError:
            print("Invalid input! Please enter 9 numbers from 0 to 8 separated by spaces, no repeats.")

```

```

def main():
    print("Enter the start state (0 represents the blank):")
    start = input_state("Start state: ")
    print("Enter the goal state (0 represents the blank):")
    goal = input_state("Goal state: ")

    print("\nSolving...")
    path = a_star(start, goal)

    if path is None:
        print("No solution found.")
    else:
        print(f"Solution found in {len(path) - 1} moves:")
        for step in path:
            print_puzzle(step)

if __name__ == "__main__":
    main()

import heapq

def manhattan_distance(state, goal):
    distance = 0
    for num in range(1, 9):
        x1, y1 = divmod(state.index(num), 3)
        x2, y2 = divmod(goal.index(num), 3)
        distance += abs(x1 - x2) + abs(y1 - y2)
    return distance

def get_neighbors(state):
    neighbors = []
    zero_pos = state.index(0)
    x, y = divmod(zero_pos, 3)
    directions = [(-1,0), (1,0), (0,-1), (0,1)]

    for dx, dy in directions:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_pos = nx * 3 + ny
            new_state = list(state)
            new_state[zero_pos], new_state[new_pos] = new_state[new_pos], new_state[zero_pos]
            neighbors.append(tuple(new_state))
    return neighbors

def a_star(start, goal):
    open_set = []

```

```

heapq.heappush(open_set, (0 + manhattan_distance(start, goal), 0, start, []))
closed_set = set()

while open_set:
    f, g, current, path = heapq.heappop(open_set)

    if current == goal:
        return path + [current]

    if current in closed_set:
        continue
    closed_set.add(current)

    for neighbor in get_neighbors(current):
        if neighbor in closed_set:
            continue
        new_g = g + 1
        new_f = new_g + manhattan_distance(neighbor, goal)
        heapq.heappush(open_set, (new_f, new_g, neighbor, path + [current]))

return None

def print_puzzle(state):
    for i in range(0, 9, 3):
        print(state[i:i+3])
    print()

def input_state(prompt):
    while True:
        try:
            s = input(prompt)
            lst = tuple(int(x) for x in s.strip().split())
            if len(lst) != 9 or set(lst) != set(range(9)):
                raise ValueError
            return lst
        except ValueError:
            print("Invalid input! Please enter 9 numbers from 0 to 8 separated by spaces, no repeats.")

def main():
    print("Enter the start state (0 represents the blank):")
    start = input_state("Start state: ")
    print("Enter the goal state (0 represents the blank):")
    goal = input_state("Goal state: ")

    print("\nSolving...")
    path = a_star(start, goal)

```

```

if path is None:
    print("No solution found.")
else:
    print(f"Solution found in {len(path) - 1} moves:")
    for step in path:
        print_puzzle(step)

if __name__ == "__main__":
    main()

```

```

--- Manhattan Distance Heuristic ---
[2, 8, 3]
[1, 6, 4]
[7, 0, 5]

[2, 8, 3]
[1, 0, 4]
[7, 6, 5]

[2, 0, 3]
[1, 8, 4]
[7, 6, 5]

[0, 2, 3]
[1, 8, 4]
[7, 6, 5]

[1, 2, 3]
[0, 8, 4]
[7, 6, 5]

[1, 2, 3]
[8, 0, 4]
[7, 6, 5]

[Done] exited with code=0 in 0.104 seconds

```

```

--- Misplaced Tiles Heuristic ---
[2, 8, 3]
[1, 6, 4]
[7, 0, 5]

[2, 8, 3]
[1, 0, 4]
[7, 6, 5]

[2, 0, 3]
[1, 8, 4]
[7, 6, 5]

[0, 2, 3]
[1, 8, 4]
[7, 6, 5]

[1, 2, 3]
[0, 8, 4]
[7, 6, 5]

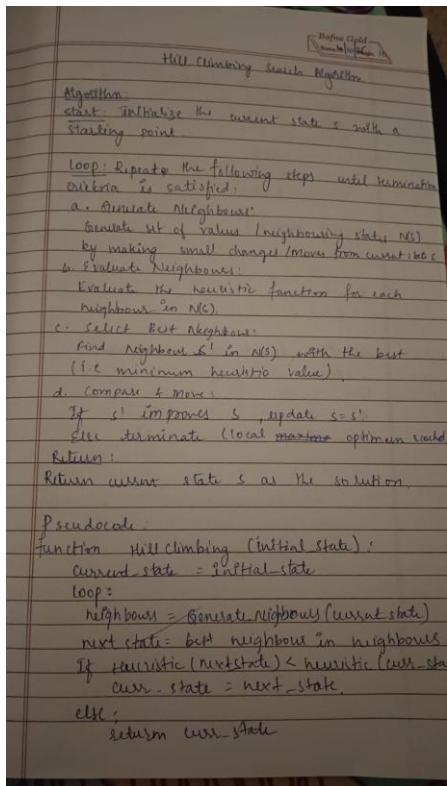
[1, 2, 3]
[8, 0, 4]
[7, 6, 5]

[Done] exited with code=0 in 0.106 seconds

```

3. Hill Climbing Search Algorithm

Algorithm:



```
import random
```

```
def heuristic(state):  
    h = 0  
    n = len(state)  
    for i in range(n):  
        for j in range(i + 1, n):  
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):  
                h += 1  
    return h  
  
def get_neighbors(state):  
    neighbors = []  
    n = len(state)  
    for col in range(n):  
        for row in range(n):  
            if state[col] != row:  
                neighbor = list(state)  
                neighbor[col] = row  
                neighbors.append(neighbor)  
    return neighbors
```

```

def hill_climbing(initial_state):
    current = list(initial_state)
    current_h = heuristic(current)

    while True:
        neighbors = get_neighbors(current)
        neighbor_h = [(heuristic(neighbor), neighbor) for neighbor in neighbors]

        neighbor_h.sort(key=lambda x: x[0])
        best_h, best_neighbor = neighbor_h[0]

        if best_h >= current_h:
            break # No improvement

        current, current_h = best_neighbor, best_h

    return current, current_h

def random_restart_hill_climbing(initial_state, max_restarts=1000):
    n = len(initial_state)
    current_state = list(initial_state)

    for restart in range(max_restarts):
        solution, h = hill_climbing(current_state)
        if h == 0:
            return solution, h, restart

        current_state = [random.randint(0, n - 1) for _ in range(n)]
    return solution, h, max_restarts

def print_board(state):
    n = len(state)
    for row in range(n):
        line = ""
        for col in range(n):
            line += " Q " if state[col] == row else ". "
        print(line)
    print()

if __name__ == "__main__":
    while True:
        try:
            N = int(input("Enter the number of queens (N): "))
            if N > 3:
                break
            else:

```

```

        print("N must be at least 4.")
    except ValueError:
        print("Invalid input. Please enter an integer.")

print(f"Enter the initial row positions for each of the {N} columns (0 to {N-1}):")
initial_state = []
for col in range(N):
    while True:
        try:
            row = int(input(f"Column {col}: "))
            if 0 <= row < N:
                initial_state.append(row)
                break
            else:
                print(f"Please enter a number between 0 and {N-1}.")
        except ValueError:
            print("Invalid input. Enter an integer.")

print("\nInitial board:")
print_board(initial_state)

solution, h, restarts = random_restart_hill_climbing(initial_state, max_restarts=1000)

if h == 0:
    print(f"Solution found after {restarts} restarts:")
    print_board(solution)
else:
    print(f"No solution found after {restarts} restarts. Local optimum with heuristic {h}:")
    print_board(solution)

```

```

Initial State: [3, 1, 2, 0] with 2 attacks
-----
| .. | .. | .. | Q |
-----
| .. | Q | .. | .. |
-----
| .. | .. | Q | .. |
-----
| Q | .. | .. | .. |
-----

== Running Hill Climbing with Random Restarts ==
Solution found after 2 restart(s)!
Final State: [1, 3, 0, 2] with 0 attacks
-----
| .. | .. | Q | .. |
-----
| Q | .. | .. | .. |
-----
| .. | .. | .. | Q |
-----
| .. | Q | .. | .. |
-----
```

4. Iterative deepening search algorithm

Algorithm:

Bafna Gold
Date: 19/11/2023

Iterative Deepening Search (IDS)

```
function IDS (start, goal):
    depth = 0
    loop:
        result = DLS (start, goal, depth)
        if result ≠ failure:
            return result
        depth = depth + 1

function DLS (state, goal, limit):
    if state == goal:
        return path
    if limit == 0:
        return failure
    for each neighbour in next-neighbours (state):
        if neighbour not in visited:
            result = DLS (neighbour, goal, limit - 1)
            if result ≠ failure:
                return result
    return failure

function Get-neighbours (state):
    blank-pos = find 0 in state
    for each valid move (up, down, right, left),
        swap 0 with neighbour to create
        new-state
        add new-state to neighbours.
    return neighbours.
```

Code:

```
from collections import deque

# Define the goal state
GOAL_STATE = ((1, 2, 3),
              (4, 5, 6),
              (7, 8, 0))

# Moves (up, down, left, right)
MOVES = [(-1, 0), (1, 0), (0, -1), (0, 1)]
```

```

def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j
    return None

def swap_positions(state, pos1, pos2):
    state_list = [list(row) for row in state]
    x1, y1 = pos1
    x2, y2 = pos2
    state_list[x1][y1], state_list[x2][y2] = state_list[x2][y2], state_list[x1][y1]
    return tuple(tuple(row) for row in state_list)

def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
    for dx, dy in MOVES:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_state = swap_positions(state, (x, y), (nx, ny))
            neighbors.append(new_state)
    return neighbors

def depth_limited_search(state, goal, limit, path, visited):
    if state == goal:
        return path
    if limit <= 0:
        return None
    visited.add(state)

    for neighbor in get_neighbors(state):
        if neighbor not in visited:
            result = depth_limited_search(neighbor, goal, limit - 1, path + [neighbor], visited)
            if result is not None:
                return result

    visited.remove(state)
    return None

def iterative_deepening_search(start, goal):
    depth = 0

```

```

while True:
    visited = set()
    print(f"Searching at depth: {depth}")
    result = depth_limited_search(start, goal, depth, [start], visited)
    if result is not None:
        return result
    depth += 1

def print_state(state):
    for row in state:
        print(''.join(str(x) if x != 0 else ' ' for x in row))
    print()

if __name__ == "__main__":
    # Example start state
    start_state = ((1, 2, 3),
                   (4, 0, 6),
                   (7, 5, 8))

    solution_path = iterative_deepening_search(start_state, GOAL_STATE)

    print(f"Solution found in {len(solution_path) - 1} moves:\n")
    for step in solution_path:
        print_state(step)

import heapq
import copy

# Goal state
GOAL_STATE = [[1, 2, 3],
              [4, 5, 6],
              [7, 8, 0]]

DIRECTIONS = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right

def manhattan_distance(state):
    distance = 0
    for i in range(3):
        for j in range(3):
            val = state[i][j]
            if val != 0:
                goal_x = (val - 1) // 3
                goal_y = (val - 1) % 3

```

```

        distance += abs(i - goal_x) + abs(j - goal_y)
    return distance

def misplaced_tiles(state):
    count = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0 and state[i][j] != GOAL_STATE[i][j]:
                count += 1
    return count

def get_blank_pos(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def is_goal(state):
    return state == GOAL_STATE

def valid(x, y):
    return 0 <= x < 3 and 0 <= y < 3

def heuristic_fn(state, heuristic):
    if heuristic == "manhattan":
        return manhattan_distance(state)
    elif heuristic == "misplaced":
        return misplaced_tiles(state)
    else:
        raise ValueError("Unknown heuristic: choose 'manhattan' or 'misplaced'")

def a_star(start_state, heuristic="manhattan"):
    visited = set()
    heap = []

    g = 0
    h = heuristic_fn(start_state, heuristic)
    f = g + h

    heapq.heappush(heap, (f, g, start_state, [])) # (f, g, state, path)

```

```

while heap:
    f, g, state, path = heapq.heappop(heap)

    state_tuple = tuple(tuple(row) for row in state)
    if state_tuple in visited:
        continue

    visited.add(state_tuple)

    if is_goal(state):
        return path + [state]

    x, y = get_blank_pos(state)

    for dx, dy in DIRECTIONS:
        nx, ny = x + dx, y + dy
        if valid(nx, ny):
            new_state = copy.deepcopy(state)
            new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
            new_state_tuple = tuple(tuple(row) for row in new_state)
            if new_state_tuple not in visited:
                new_g = g + 1
                new_h = heuristic_fn(new_state, heuristic)
                new_f = new_g + new_h
                heapq.heappush(heap, (new_f, new_g, new_state, path + [state]))

return None

```

```

def print_path(path):
    for step, state in enumerate(path):
        print(f"Step {step}:")
        for row in state:
            print(row)
        print("")

# Example usage:
if __name__ == "__main__":
    # Change this to test different starting positions
    start_state = [[1, 2, 3],
                   [4, 0, 6],
                   [7, 5, 8]]

    print("Using Manhattan Distance Heuristic:")
    path_manhattan = a_star(start_state, heuristic="manhattan")
    if path_manhattan:

```

```

print_path(path_manhattan)
print(f"Total steps (Manhattan): {len(path_manhattan) - 1}")
else:
    print("No solution found with Manhattan.")

print("\nUsing Misplaced Tiles Heuristic:")
path_misplaced = a_star(start_state, heuristic="misplaced")
if path_misplaced:
    print_path(path_misplaced)
    print(f"Total steps (Misplaced Tiles): {len(path_misplaced) - 1}")
else:
    print("No solution found with Misplaced Tiles.")

```

```

--- Manhattan Distance Heuristic ---
[2, 8, 3]
[1, 6, 4]
[7, 0, 5]

[2, 8, 3]
[1, 0, 4]
[7, 6, 5]

[0, 2, 3]
[1, 8, 4]
[7, 6, 5]

[1, 2, 3]
[0, 8, 4]
[7, 6, 5]

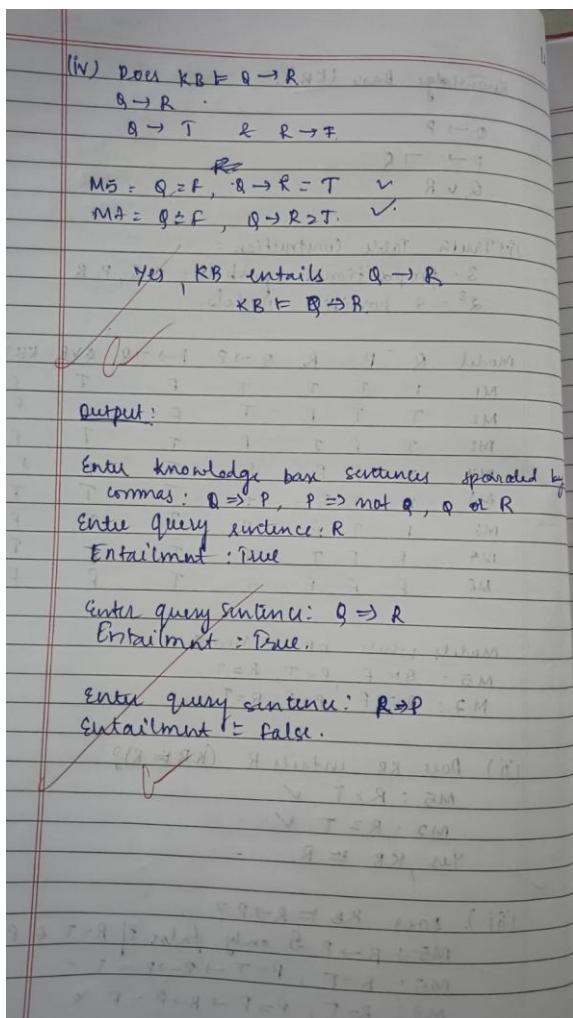
[1, 2, 3]
[8, 0, 4]
[7, 6, 5]

[Done] exited with code=0 in 0.104 seconds

```

5. Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm:



Knowledge Base (KB):

$Q \rightarrow P$
 $P \rightarrow \neg Q$
 $Q \vee R$

(i) Truth Table Construction:
3 propositional symbols: $\rightarrow, \neg, \wedge, \vee$
 $2^3 = 8$ possible models.

Model	Q	P	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	$KB \text{ True?}$
M1	T	T	T	T	F	T	F
M2	T	T	F	T	F	T	F
M3	T	F	T	F	T	T	F
M4	T	F	F	F	T	T	F
M5	F	T	T	T	T	T	T
M6	F	T	F	T	T	F	F
M7	F	F	T	T	F	T	F
M8	F	F	F	T	F	P	P

Models where KB is True:
M5: $Q=F, P=T, R=T$
M7: $Q=F, P=F, R=T$

(ii) Does KB entail R ($KB \models R$)?
M5: $R=T$ ✓
M7: $R=T$ ✓
Yes, $KB \models R$.

(iii). Does $KB \models R \rightarrow P$?
M5: $R \rightarrow P$ is only false if $R=T \wedge P=F$.
M5: $R=T, P=T \rightarrow R \rightarrow P=T$
M7: $R=T, P=F \rightarrow R \rightarrow P=F$ ✗
No $KB \models R \rightarrow P$.

1+1/15 | 25

8. Propositional Logic

```

function TT-ENTAILS ?(KB,  $\alpha$ ) return true or false
Inputs : KB , the knowledgebase, a sentence
         in propositional logic.  $\alpha$ , the query
         sentence in propositional logic
symbols  $\leftarrow$  a list of the proposition symbols
         in KB and  $\alpha$ .
return TT-CHECK-ALL (KB,  $\alpha$ , symbols, +)

```

```

function TT-CHECK-ALL (KB,  $\alpha$ , symbols, model)
returns true or false.
if Empty? (symbols) then
  if PL-true? (KB, model) then return true
  else return false // when KB is false, always
                     returns false
else do
  p  $\leftarrow$  first (symbols)
  rest  $\leftarrow$  Rest (symbols)
  return (TT-CHECK-ALL (KB,  $\alpha$ , rest, Model V
                         $\wedge$  p = True?))
  and
  TT-CHECK-ALL (KB,  $\alpha$ , rest, Model V
                  $\wedge$  p = False?))

```

Code:

```
import itertools
```

```

def pl_true(expr, model):
    if expr == 'True': return True
    if expr == 'False': return False
    if expr in model: return model[expr]
    if expr.startswith('not '): return not pl_true(expr[4:], model)
    if 'and' in expr:
        a, b = expr.split(' and ', 1)
        return pl_true(a, model) and pl_true(b, model)
    if 'or' in expr:

```

```

a, b = expr.split(' or ', 1)
return pl_true(a, model) or pl_true(b, model)
if '=>' in expr:
    a, b = expr.split('=>', 1)
    return (not pl_true(a, model)) or pl_true(b, model)
if '<=>' in expr:
    a, b = expr.split('<=>', 1)
    return pl_true(a, model) == pl_true(b, model)
return False

def tt_check_all(kb, alpha, symbols, model):
    if not symbols:
        if all(pl_true(s, model) for s in kb):
            return pl_true(alpha, model)
        else:
            return True
    rest = symbols[1:]
    p = symbols[0]
    model_true = model.copy()
    model_true[p] = True
    model_false = model.copy()
    model_false[p] = False
    return tt_check_all(kb, alpha, rest, model_true) and tt_check_all(kb, alpha, rest, model_false)

def tt_entails(kb, alpha):
    symbols = sorted({s for sentence in kb + [alpha] for s in sentence.replace('not',
        '').replace('(','').replace(')','').replace('and','').replace('or','').replace('=>','').replace('<=>','').split() if s
        not in ['and','or','=>','<=>','not','True','False']})
    return tt_check_all(kb, alpha, symbols, {})

kb = input("Enter knowledge base sentences separated by commas: ").split(',')
alpha = input("Enter query sentence: ")
print("Entailment:", tt_entails([s.strip() for s in kb], alpha.strip()))

```

```

Evaluating Query: R
Truth Table Evaluation:
P | Q | R | KB | Query | KB ⊨ Query
-----
T | T | T | F | T | T
T | T | F | F | F | T
T | F | T | T | T | T
T | F | F | F | F | T
F | T | T | F | T | T
F | T | F | F | F | T
F | F | T | T | T | T
F | F | F | F | F | T

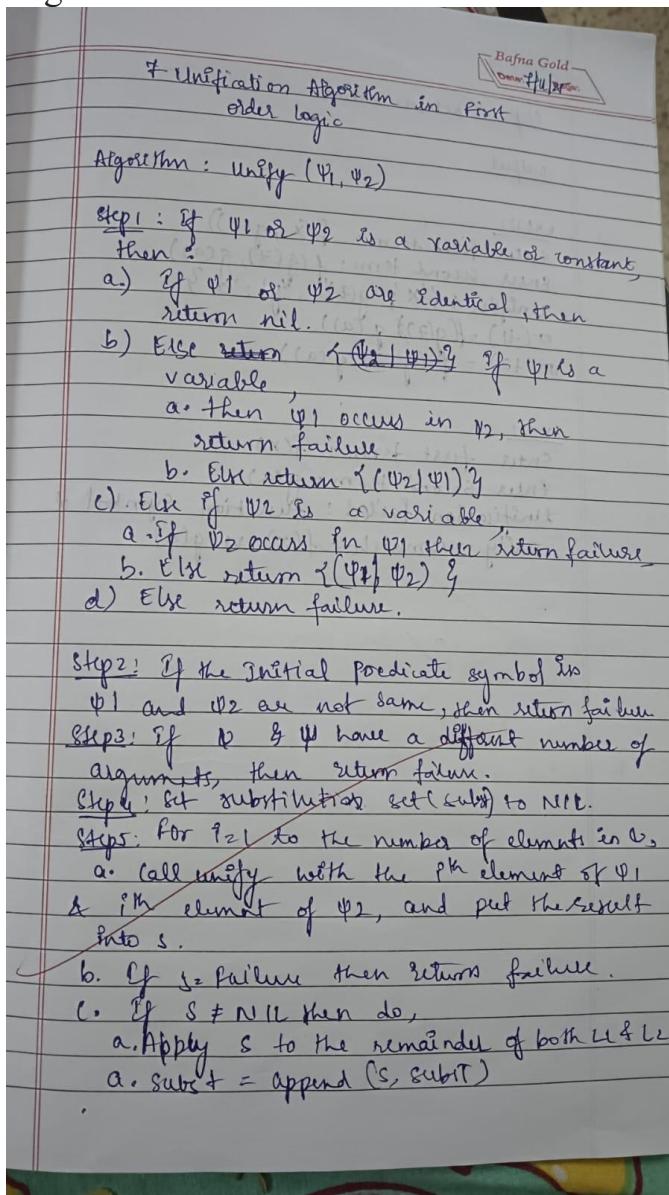
Result:
The Knowledge Base entails the Query (KB ⊨ Query)
=====

Evaluating Query: R -> P
Truth Table Evaluation:
P | Q | R | KB | Query | KB ⊨ Query
-----
T | T | T | F | T | T
T | T | F | F | T | T
T | F | T | T | T | T
T | F | F | F | T | T
F | T | T | F | F | T
F | T | F | F | T | T
F | F | T | T | F | F
F | F | F | F | T | T

Result:
The Knowledge Base does NOT entail the Query (KB ⊨ Query)
=====
```

6. Implement unification in first order logic

Algorithm:



Code:

```
from dataclasses import dataclass
from typing import Tuple, Dict, Union, List, Optional

@dataclass(frozen=True)
class Var:
    name: str
    def __repr__(self):
        return self.name
```

```

@dataclass(frozen=True)
class Func:
    name: str
    args: Tuple['Term', ...]
    def __repr__(self):
        if not self.args:
            return self.name
        return f'{self.name}({", ".join(map(str, self.args))})'

Term = Union[Var, Func]
Subst = Dict[Var, Term]

def is_variable(t: Term) -> bool:
    return isinstance(t, Var)

def apply_subst(subst: Subst, term: Term) -> Term:
    if is_variable(term):
        while term in subst:
            term = subst[term]
        return term
    return Func(term.name, tuple(apply_subst(subst, a) for a in term.args))

def occurs_in(var: Var, term: Term, subst: Subst) -> bool:
    term = apply_subst(subst, term)
    if term == var:
        return True
    if isinstance(term, Func):
        return any(occurs_in(var, a, subst) for a in term.args)
    return False

class UnificationFailure(Exception):
    pass

def unify_var(var: Var, x: Term, subst: Subst) -> Subst:
    x = apply_subst(subst, x)
    if var == x:
        return subst
    if occurs_in(var, x, subst):
        raise UnificationFailure(f'Occurs-check failed: {var} occurs in {x}')
    new_subst = {v: apply_subst({var: x}, t) for v, t in subst.items()}
    new_subst[var] = x
    return new_subst

def unify(t1: Term, t2: Term, subst: Optional[Subst] = None) -> Subst:
    if subst is None:
        subst = {}

```

```

t1 = apply_subst(subst, t1)
t2 = apply_subst(subst, t2)
if t1 == t2:
    return subst
if is_variable(t1):
    return unify_var(t1, t2, subst)
if is_variable(t2):
    return unify_var(t2, t1, subst)
if isinstance(t1, Func) and isinstance(t2, Func):
    if t1.name != t2.name or len(t1.args) != len(t2.args):
        raise UnificationFailure(f"Function symbol or arity mismatch: {t1} vs {t2}")
    for a1, a2 in zip(t1.args, t2.args):
        subst = unify(a1, a2, subst)
    return subst
    raise UnificationFailure(f"Cannot unify {t1} and {t2}")

def parse_term(s: str) -> Term:
    s = s.strip()
    if '(' not in s:
        if s[0].islower():
            return Func(s, ())
        else:
            return Var(s)
    name, rest = s.split('(', 1)
    rest = rest[:-1]
    args = split_args(rest)
    return Func(name, tuple(parse_term(arg) for arg in args))

def split_args(s: str) -> List[str]:
    args, depth, current = [], 0, ""
    for c in s:
        if c == ',' and depth == 0:
            args.append(current.strip())
            current = ""
        else:
            if c == '(':
                depth += 1
            elif c == ')':
                depth -= 1
            current += c
    if current:
        args.append(current.strip())
    return args

if __name__ == "__main__":
    expr1 = input("Enter first term: ").strip()
    expr2 = input("Enter second term: ").strip()

```

```

try:
    t1 = parse_term(expr1)
    t2 = parse_term(expr2)
    sigma = unify(t1, t2)
    print("Unifier:", {str(k): str(v) for k, v in sigma.items()})
    print("σ(t1) =", apply_subst(sigma, t1))
    print("σ(t2) =", apply_subst(sigma, t2))
except UnificationFailure as e:
    print("Unification failed:", e)
except Exception as e:
    print("Error:", e)

```

```

Starting Unification:

Unify(['f', 'X', ['g', 'Y']], ['f', 'a', ['g', 'b']]) with subst = {}
  Unify(f, f) with subst = {}
    Terms are identical, no change.
  Unify(X, a) with subst = {}
    Add a -> X to subst
  Unify(['g', 'Y'], ['g', 'b']) with subst = {'a': 'X'}
    Unify(g, g) with subst = {'a': 'X'}
      Terms are identical, no change.
    Unify(Y, b) with subst = {'a': 'X'}
      Add b -> Y to subst

Final Unification Result: {'a': 'X', 'b': 'Y'}

```

7. Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:

```

First order logic: Forward Chaining
function FOL-FC-ASK(KB, α) returns a
    substitution or false
    Inputs : KB , the KnowledgeBase , a set of
    first order definite clauses .
    local variables : new , the new sentences
    inferred on each iteration
repeat until new is empty
    new ← []
    for each rule in KB do
        ( $p_1 \wedge \dots \wedge p_n \Rightarrow q$ ) & Standard variable
        (rule)
        for each  $\sigma$  such that  $SUBST(\sigma, p_1 \wedge \dots \wedge p_n)$ 
        =  $q'$ 
        for some  $p'_1, \dots, p'_n$  in KB
         $q' \leftarrow \text{Subst}(\sigma, q)$ 
        if  $q'$  does not unify some sentence
        already in KB or have then
        add  $q'$  to new
         $\phi \leftarrow \text{unify}(q', \alpha)$ 
        if  $\phi$  is not fail then return  $\phi$ 
    add new to KB
return false

```

Code:

```

import re

def parse_predicate(pred):
    pred = pred.strip()
    if "(" not in pred:
        # Treat constant symbols or atomic facts with no arguments

```

```

        return pred, []
name, args = pred.split("(", 1)
args = args.strip(")").split(",")
return name.strip(), [a.strip() for a in args]

def is_variable(x):
    return x[0].islower() # lowercase = variable

def unify(x, y, theta=None):
    if theta is None:
        theta = {}
    if x == y:
        return theta
    if is_variable(x):
        return unify_var(x, y, theta)
    if is_variable(y):
        return unify_var(y, x, theta)
    if isinstance(x, tuple) and isinstance(y, tuple):
        if x[0] != y[0] or len(x[1]) != len(y[1]):
            return None
        for a, b in zip(x[1], y[1]):
            theta = unify(a, b, theta)
        if theta is None:
            return None
        return theta
    return None

def unify_var(var, x, theta):
    if var in theta:
        return unify(theta[var], x, theta)
    if x in theta:
        return unify(var, theta[x], theta)
    if occurs_check(var, x, theta):
        return None
    theta[var] = x
    return theta

def occurs_check(var, x, theta):
    if var == x:
        return True
    if isinstance(x, tuple):
        return any(occurs_check(var, arg, theta) for arg in x[1])
    if x in theta:
        return occurs_check(var, theta[x], theta)
    return False

def substitute(pred, theta):

```

```

name, args = pred
new_args = [theta.get(a, a) for a in args]
return (name, new_args)

def parse_clause(clause):
    if "=>" in clause:
        premises, conclusion = clause.split("=>")
        premises = [parse_predicate(p.strip()) for p in premises.split("&")]
        conclusion = parse_predicate(conclusion.strip())
    else:
        premises = []
        conclusion = parse_predicate(clause.strip())
    return premises, conclusion

def forward_chaining(kb, facts, query):
    query = parse_predicate(query)
    known_facts = [parse_predicate(f) for f in facts]
    added = True
    while added:
        added = False
        for premises, conclusion in kb:
            possible_subs = [{}]
            for prem in premises:
                new_subs = []
                for f in known_facts:
                    theta = unify(prem, f)
                    if theta is not None:
                        for ps in possible_subs:
                            merged = {**ps, **theta}
                            new_subs.append(merged)
                possible_subs = new_subs
            for s in possible_subs:
                new_fact = substitute(conclusion, s)
                if new_fact not in known_facts:
                    known_facts.append(new_fact)
                    added = True
                    if unify(new_fact, query) is not None:
                        return True
    return False

n = int(input("Enter number of rules in Knowledge Base:\n"))
kb = []
print("\nEnter rules (use format: A & B => C or single fact):")
for _ in range(n):
    clause = input().strip()
    kb.append(parse_clause(clause))

```

```

# Fix: Use re.findall to correctly parse facts that might contain commas in arguments
facts_input_string = input("\nEnter initial known facts (comma separated):\n").strip()
facts = re.findall(r'[A-Za-z_]+(.+?)', facts_input_string)
query = input("\nEnter query to prove:\n").strip()

result = forward_chaining(kb, facts, query)

print("\n-----")
print("Knowledge Base:")
for p, c in kb:
    print(f'{p} & {c} => {c}' if p else
          f'{c}')
print("\nInitial Facts:", facts)
print("Query:", query)
print("-----")
print("Query can be proven!" if result else "Query cannot be proven.")

```

```

--- Forward Chaining (FOL-FC-ASK) ---

Initial known facts:
Missile(T1)
Owns(A, T1)
Enemy(A, America)
American(Robert)

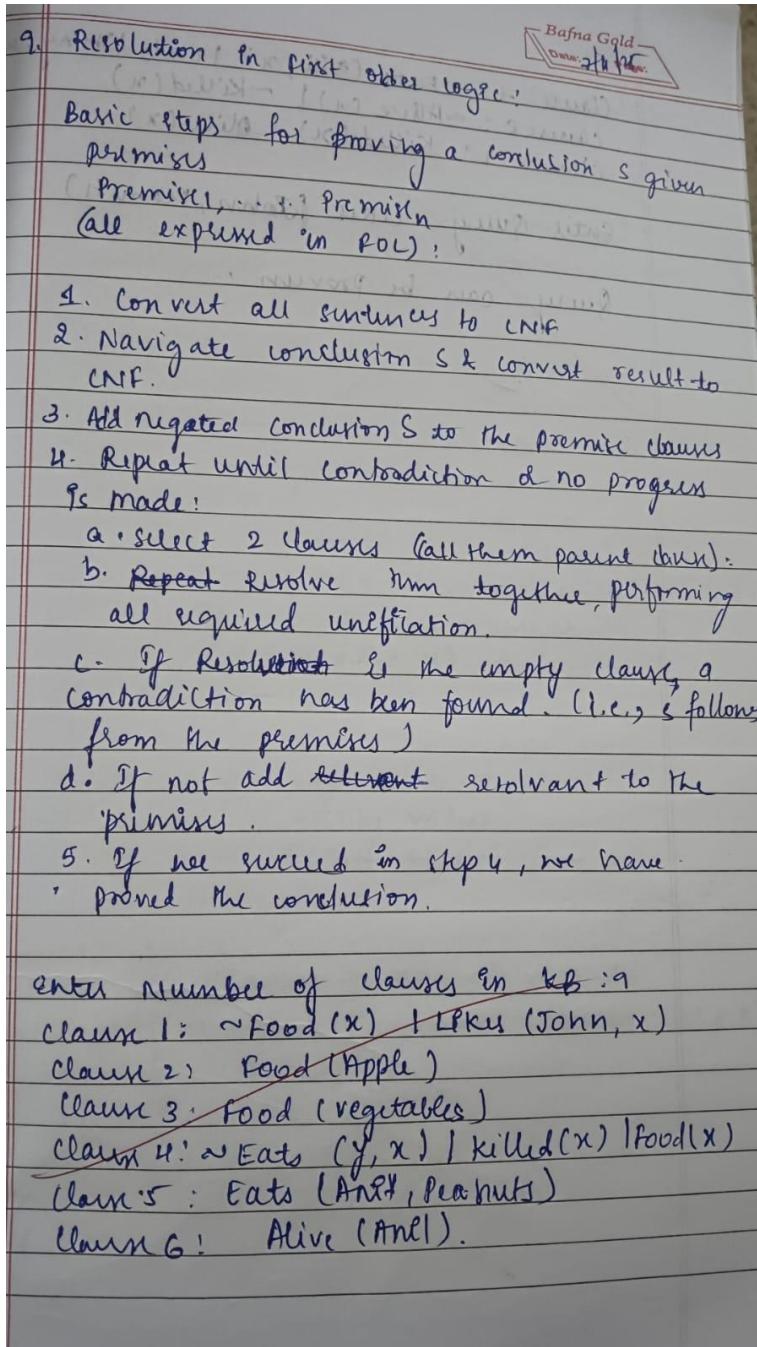
Inferred: Weapon(T1)
Inferred: Hostile(A)
Inferred: Sells(Robert, T1, A)
Inferred: Criminal(Robert)

Query satisfied: Criminal(Robert)

```

8. Resolution in First order logic:

Algorithm:



Code:

import re

```
def standardize_variables(clause, index):
```

```
    vars_in_clause = re.findall(r'[a-zA-Z]\w*', clause)
```

```

for v in vars_in_clause:
    clause = re.sub(r'\b' + v + r'\b', v + str(index), clause)
return clause

def negate_literal(literal):
    if literal.startswith('~'):
        return literal[1:]
    else:
        return '~' + literal

def parse_clause(clause):
    return [lit.strip() for lit in clause.split('|')]

def unify(x, y, subs):
    if subs is None:
        return None
    elif x == y:
        return subs
    elif isinstance(x, str) and x[0].islower():
        return unify_var(x, y, subs)
    elif isinstance(y, str) and y[0].islower():
        return unify_var(y, x, subs)
    elif '(' in x and '(' in y:
        fx, argsx = x.split('(', 1)
        fy, argsy = y.split('(', 1)
        if fx != fy:
            return None
        argsx = argsx[:-1].split(',')
        argsy = argsy[:-1].split(',')
        for a, b in zip(argsx, argsy):
            subs = unify(a.strip(), b.strip(), subs)
    return subs
    else:
        return None

def unify_var(var, x, subs):
    if var in subs:
        return unify(subs[var], x, subs)
    elif x in subs:
        return unify(var, subs[x], subs)
    else:
        subs[var] = x
    return subs

def apply_subs(literal, subs):
    for var, val in subs.items():
        literal = re.sub(r'\b' + var + r'\b', val, literal)

```

```

return literal

def resolve(ci, cj):
    for di in ci:
        for dj in cj:
            if di == negate_literal(dj):
                new_clause = list(set(ci + cj))
                new_clause.remove(di)
                new_clause.remove(dj)
                return new_clause
    return None

n = int(input("Enter number of clauses in KB: "))
kb = []
for i in range(n):
    kb.append(standardize_variables(input(f'Clause {i+1}: ').strip(), i))

query = input("Enter query: ").strip()
negated_query = negate_literal(query)
kb.append(negated_query)

new = set()
resolved = False

while True:
    pairs = [(kb[i], kb[j]) for i in range(len(kb)) for j in range(i + 1, len(kb))]
    for (ci, cj) in pairs:
        resolvent = resolve(parse_clause(ci), parse_clause(cj))
        if resolvent == []:
            resolved = True
            break
        if resolvent:
            new.add(' | '.join(resolvent))
    if resolved:
        print("\nQuery can be proven by resolution.")
        break
    if new.issubset(set(kb)):
        print("\nQuery can be proven.")
        break
    for c in new:
        if c not in kb:
            kb.append(c)

```

```

FIRST-ORDER LOGIC RESOLUTION PROOF
Proving: John likes peanuts
=====
=====

FIRST-ORDER LOGIC REPRESENTATIONS:
=====
1. John likes all kinds of food
   ForAll x {Food(x) -> Likes(John, x))
2. Apple is food
   Food(Apple)
3. Vegetables are food
   Food(Vegetables)
4. Anything anyone eats and is not killed is food
   ForAll y ForAll z {((Eats(y,z) AND -Killed(y)) -> Food(z))
5. Anil eats peanuts
   Eats(Anil, Peanuts)
6. Anil is alive
   Alive(Anil)
7. Harry eats everything that Anil eats
   ForAll x {Eats(Anil,x) -> Eats(Harry,x))
8. Anyone who is alive is not killed
   ForAll x {Alive(x) -> -Killed(x))
9. Anyone who is not killed is alive
   ForAll x {-Killed(x) -> Alive(x))

Query: Likes(John, Peanuts)
Negated Query (for refutation): -Likes(John, Peanuts)

=====
CNF CLAUSES (after conversion):
=====
C1: {Likes(John, x)} V {-Food(x)}
C2: {Food(Apple)}
C3: {Food(Vegetables)}
C4: {Food(z)} V Killed(y) V -Eats(y, z)
C5: {Eats(Anil, Peanuts)}
C6: {Alive(Anil)}
C7: {Eats(Harry, x)} V {-Eats(Anil, x)}
C8: {-Alive(x)} V {-killed(x)}
C9: {Alive(x)} V Killed(x)
C10: {-Likes(John, Peanuts)}

=====
RESOLUTION PROOF:
=====

```

9. Implement Alpha-Beta Pruning:

Algorithm:

Bafna Gold Date: 10/12/23

```

11. Alpha - Beta Pruning (cut off) Search Algorithm:
function Alpha-Beta-Search (state) returns an
action
    v ← MAX_Value (state, -∞, +∞)
    return the action in Action(state) with
    value v.

function Alpha-Beta-Max-Value (state, α, β)
    returns a utility value.
    if Terminal-Test (state) then return
        Utility (state)
    v ← -∞
    for each a in Actions (state) do
        v ← Max (v, Min-Value (Result(s, a), α, β))
        if v ≥ β then return v
        α ← Max (α, v)
    return v

function Min-Value (state, α, β)
    return a utility value.
    if terminal-Test (state) then return
        Utility (state)
    v ← +∞
    for each a in Action (state) do
        v ← Min (v, Max-Value (Result (s, a), α, β))
        if v ≤ α then return v
        β ← min (β, v)
    return v.

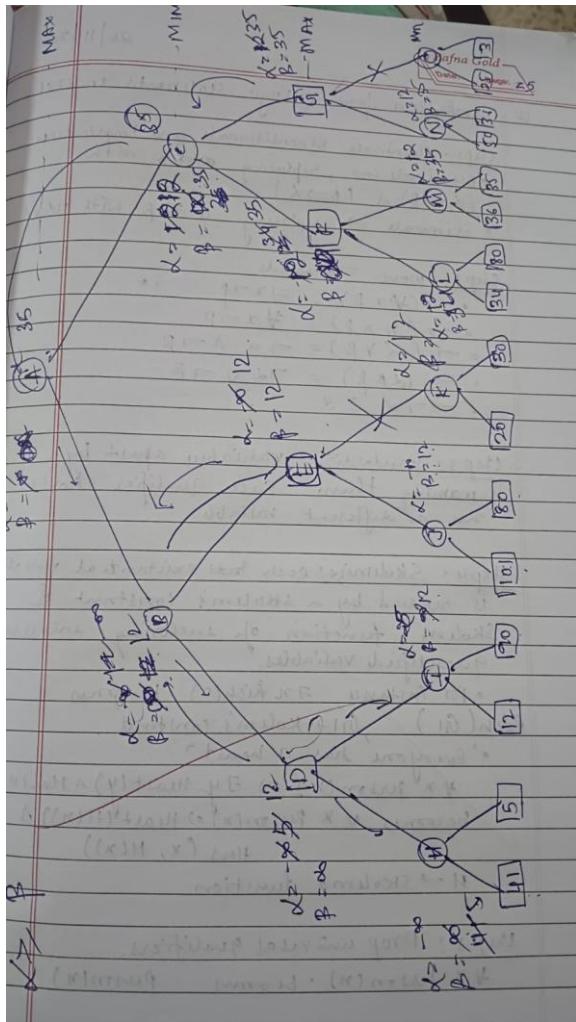
```

Output:

Enter node:
A B C
B D E
C F G
D H I
E J K
F L M
G N O
H U I
I 12 90
J 101 20
K 80 30
L 34 80
M 36 25
N 50 36
O 25 3
done

Enter root node: A
Value of root (A) = 35
Chosen Path:
A → C → F → M → 35

Pruned Branches:
Pruned : child R of node E
Pruned : child O of node G.



Code:

```

import math

pruned = [] # store pruned branches

def alphabeta(node, isMax, alpha, beta, tree):
    global pruned

    # Leaf node (integer)
    if isinstance(node, int):
        return node

    children = tree[node]

    if isMax:      # MAX NODE
        value = -math.inf
        for child in children:
            value = max(value, alphabeta(child, False, alpha, beta, tree))
            if value >= beta:
                pruned.append(node)
                break
            alpha = max(alpha, value)
    else:
        value = math.inf
        for child in children:
            value = min(value, alphabeta(child, True, alpha, beta, tree))
            if value <= alpha:
                pruned.append(node)
                break
            beta = min(beta, value)

    return value

```

```

if value >= beta:
    pruned.append((node, child))
    break
val = alphabeta(child, False, alpha, beta, tree)
value = max(value, val)
alpha = max(alpha, value)
return value

else:      # MIN NODE
    value = math.inf
    for child in children:
        if value <= alpha:
            pruned.append((node, child))
            break
        val = alphabeta(child, True, alpha, beta, tree)
        value = min(value, val)
        beta = min(beta, value)
    return value

def compute_value(node, isMax, tree):
    """Compute subtree value without pruning."""
    if isinstance(node, int):
        return node
    if isMax:
        return max(compute_value(c, False, tree) for c in tree[node])
    else:
        return min(compute_value(c, True, tree) for c in tree[node])

def find_path(node, target, isMax, tree):
    if isinstance(node, int):
        return [node]

    children = tree[node]

    if isMax:
        for c in children:
            if compute_value(c, False, tree) == target:
                return [node] + find_path(c, target, False, tree)
    else:
        for c in children:
            if compute_value(c, True, tree) == target:
                return [node] + find_path(c, target, True, tree)

    return [node]

print("\nEnter your game tree.")

```

```

print("Format for each line:")
print(" Parent Child1 Child2 Child3 ...")
print("Use integers for leaves.")
print("Example:")
print(" A B C")
print(" B D E")
print(" D 41 5")
print("Type 'done' to stop\n")

tree = {}

while True:
    line = input("Enter node: ")
    if line.lower().strip() == "done":
        break

    parts = line.split()
    parent = parts[0]
    children = []

    for ch in parts[1:]:
        # convert leaf to int
        try:
            children.append(int(ch))
        except:
            children.append(ch)

    tree[parent] = children

root = input("\nEnter root node: ").strip()

pruned = []
root_value = alphabeta(root, True, -math.inf, math.inf, tree)
path = find_path(root, root_value, True, tree)

print("\n=====")
print("  ALPHA-BETA RESULT")
print("=====\n")

print(f"Value of Root ({root}) = {root_value}\n")

print("Chosen Path:")
print(" → ".join(map(str, path)), "\n")

print("Pruned Branches:")
if pruned:
    for p in pruned:

```

```

    print(f" Pruned: child {p[1]} of node {p[0]}")
else:
    print(" No branches pruned.")

```

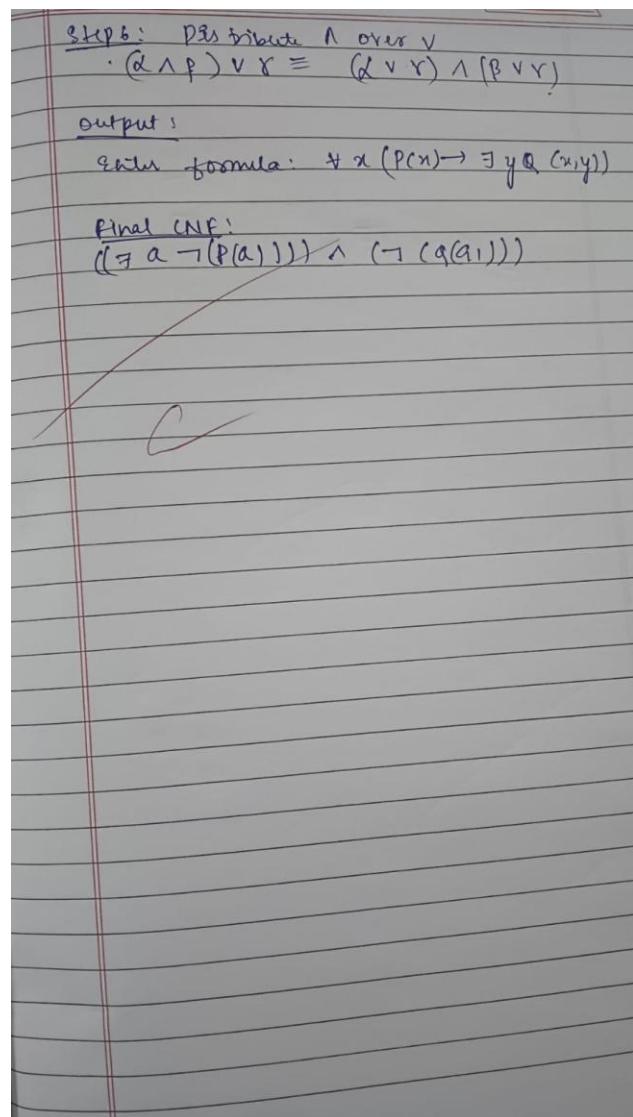
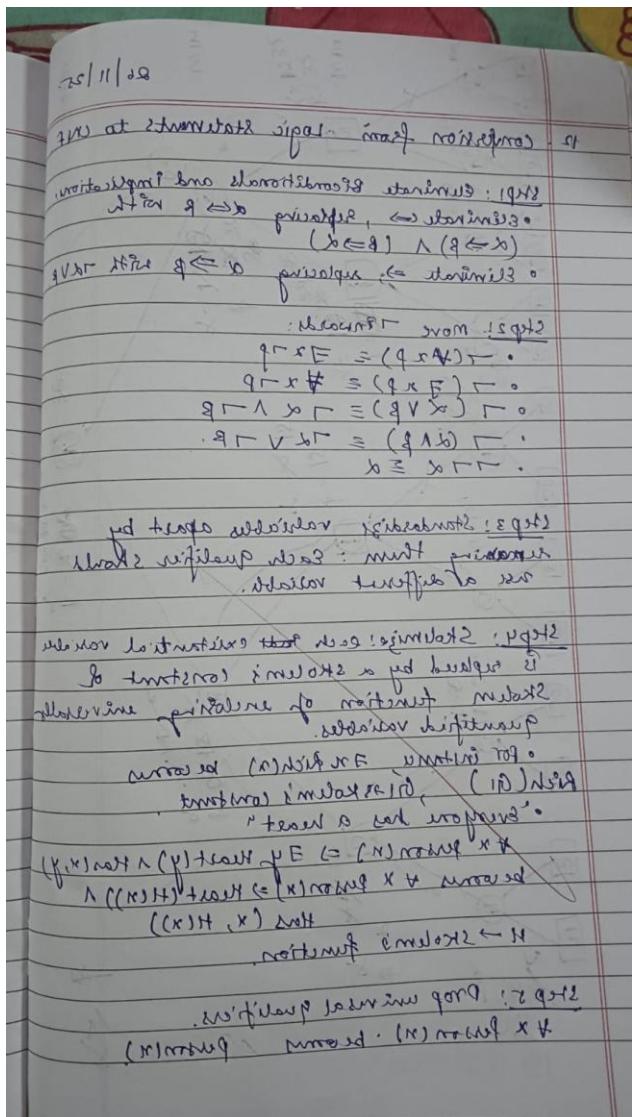
```

Game Tree Structure:
      A (MAX)
     /   \
  B (MIN)   C (MIN)
 /   \   /   \
D (MAX) E (MAX) F (MAX) G (MAX)
/   \   /   \   /   \
10   9   14  18   5   4   50   3
=====
Starting Alpha-Beta Pruning...
=====
Exploring MAX node A (depth=0), alpha=-inf, beta=-inf
--> Exploring child B of A
Exploring MIN node B (depth=1), alpha=-inf, beta=-inf
--> Exploring child D of B
Exploring MAX node D (depth=2), alpha=-inf, beta=-inf
--> Exploring child L1 of D
| Reached leaf L1 with value 10
Updated MAX node D: value=10, alpha=10, beta=-inf
--> Exploring child L2 of D
| Reached leaf L2 with value 9
Updated MAX node D: value=10, alpha=10, beta=-inf
Updated MIN node B: value=10, alpha=-inf, beta=10
--> Exploring child E of B
Exploring MAX node E (depth=2), alpha=-inf, beta=10
--> Exploring child L3 of E
| Reached leaf L3 with value 14
Updated MAX node E: value=14, alpha=14, beta=10
!!! PRUNING at MAX node E (beta=10 <= alpha=14)
Updated MIN node B: value=10, alpha=-inf, beta=10
Updated MAX node A: value=10, alpha=10, beta=-inf
--> Exploring child C of A
Exploring MIN node C (depth=1), alpha=10, beta=-inf
--> Exploring child F of C
Exploring MAX node F (depth=2), alpha=10, beta=-inf
--> Exploring child L5 of F
| Reached leaf L5 with value 5
Updated MAX node F: value=5, alpha=10, beta=-inf
--> Exploring child L6 of F
| Reached leaf L6 with value 4
Updated MAX node F: value=5, alpha=10, beta=-inf
Updated MIN node C: value=5, alpha=10, beta=5

```

10. Conversion of logic statement to CNF

Algorithm:



Code:

```
import re  
import itertools
```

```

def remove_implications(expr):
    """Eliminate  $\leftrightarrow$  and  $\rightarrow$  using logical equivalences."""
    # Eliminate  $\leftrightarrow$ :  $(A \leftrightarrow B) = (A \rightarrow B) \wedge (B \rightarrow A)$ 
    while " $\leftrightarrow$ " in expr:
        expr = re.sub(r"(.*?)(\leftrightarrow)(.*?)" , r"\1 \rightarrow \3) \wedge (\3 \rightarrow \1", expr)

```

```

# Eliminate → : (A → B) = ¬A ∨ B
expr = re.sub(r"(.*?)→(.*)", r"¬(\1) ∨ (\2)", expr)
return expr

def push_negation(expr):
    """Move negations inward using De Morgan rules & quantifier rules."""
    # Double negation
    expr = re.sub(r"¬¬", "", expr)

    # ¬(A ∧ B) = (¬A ∨ ¬B)
    expr = re.sub(r"¬((.*?) ∧ (.*)\)", r"¬\1 ∨ (¬\2)", expr)

    # ¬(A ∨ B) = (¬A ∧ ¬B)
    expr = re.sub(r"¬((.*?) ∨ (.*)\)", r"¬\1 ∧ (¬\2)", expr)

    # Quantifiers:
    expr = re.sub(r"¬∀([a-z])", r"∃\1¬", expr)
    expr = re.sub(r"¬∃([a-z])", r"∀\1¬", expr)

    return expr

def standardize_variables(expr):
    """Rename variables so all quantifiers use different names."""
    variables = "abcdefghijklmnopqrstuvwxyz"
    mapping = {}
    new_expr = ""

    counter = 0
    for ch in expr:
        if ch in variables:
            if ch not in mapping:
                mapping[ch] = variables[counter]
                counter += 1
            new_expr += mapping[ch]
        else:
            new_expr += ch
    return new_expr

skolem_counter = 1

def skolemize(expr):
    """Remove existential quantifiers replacing them with Skolem constants/functions."""
    global skolem_counter

```

```

# Replace  $\exists x P(x)$  with  $P(G1)$ 
pattern = r"\(\exists([a-zA-Z])\s*\(\w+\)\((.*?)\))"
match = re.search(pattern, expr)

while match:
    var = match.group(1)
    pred = match.group(2)
    args = match.group(3)

    new_const = f"G{skolem_counter}"
    skolem_counter += 1

    expr = re.sub(pattern, f'{pred}({{new_const}})', expr)
    match = re.search(pattern, expr)

return expr


def drop_universal(expr):
    """Remove  $\forall$  quantifiers (they are implicit in CNF)."""
    expr = expr.replace("\\"", "")
    return expr


def distribute_and_over_or(expr):
    """Distribute  $\wedge$  over  $\vee$  (very simplified CNF converter)."""
    # This function is intentionally simple and works for standard textbook examples.

    #  $(A \wedge B) \vee C \rightarrow (A \vee C) \wedge (B \vee C)$ 
    pattern = r"\((.*?) \wedge (.*?)\)\vee (.*?)" 
    if re.search(pattern, expr):
        A, B, C = re.findall(pattern, expr)[0]
        return f'({{A}} \vee {{C}}) \wedge ({ {B}} \vee {{C}})"

    return expr


def convert_to_cnf(expr):
    print("\n---- Step 1: Remove  $\leftrightarrow$  and  $\rightarrow$  ----")
    expr = remove_implications(expr)
    print(expr)

    print("\n---- Step 2: Push  $\neg$  inward ----")
    expr = push_negation(expr)
    print(expr)

    print("\n---- Step 3: Standardize variables ----")

```

```

expr = standardize_variables(expr)
print(expr)

print("\n---- Step 4: Skolemize ----")
expr = skolemize(expr)
print(expr)

print("\n---- Step 5: Drop universal quantifier ----")
expr = drop_universal(expr)
print(expr)

print("\n---- Step 6: Distribute ∧ over ∨ ----")
expr = distribute_and_over_or(expr)
print(expr)

return expr

print("Enter a First-Order Logic Statement to Convert to CNF:")
print("Example input:")
print("  ∀x (P(x) → ∃y Q(x,y))")
print("  (A ↔ B)")
print("-----")

expr = input("\nEnter formula: ")

print("\n====")
print("      CNF CONVERSION STEPS")
print("====")

cnf = convert_to_cnf(expr)

print("\n====")
print("Final CNF:")
print(cnf)
print("====")

```

Output:

Enter a First-Order Logic Statement to Convert to CNF:

Example input:

$\forall x \ (P(x) \rightarrow \exists y \ Q(x,y))$
 $(A \leftrightarrow B)$

Enter formula: $\forall x \ (P(x) \rightarrow \exists y \ Q(x,y))$

=====
CNF CONVERSION STEPS
=====

---- Step 1: Remove \leftrightarrow and \rightarrow ----

$(\neg(\forall x \ (P(x))) \vee (\exists y \ Q(x,y)))$

---- Step 2: Push \neg inward ----

$((\exists x \neg (P(x))) \wedge (\neg(\exists y \ Q(x,y))))$

---- Step 3: Standardize variables ----

$((\exists a \neg (P(a))) \wedge (\neg(\exists b \ Q(a,b))))$

---- Step 4: Skolemize ----

$((\exists a \neg (P(a))) \wedge (\neg(Q(G1))))$

---- Step 5: Drop universal quantifier ----

$((\exists a \neg (P(a))) \wedge (\neg(Q(G1))))$

---- Step 6: Distribute \wedge over \vee ----

$((\exists a \neg (P(a))) \wedge (\neg(Q(G1))))$

=====

Final CNF:

$((\exists a \neg (P(a))) \wedge (\neg(Q(G1))))$
