

UNIT-2 STACKS AND QUEUES

Stacks:- Stack is a linear data structure in which all the operations (such as insertion, deletion) takes place at only one end called "TOP". Thus it is also called Restrictive Data Structure.

* In this stack the insertion operation is called PUSH operation & Deletion operation is called POP operation.

* This follows a principle FILO [First in last out] (or) LIFO [Last in, first out].

* Examples:- The common examples of stack are

1. Placing the books in the shelf.

2. Bread slices.

3. Moving out of the bench.

4.

Basic Operations of Stack are :-

1. PUSH operation

2. POP operation

3. Stack top Operation (or) Display operation.

3. Stack top Operation (or) Display operation.

PUSH Operation:

Code :-

```
if (top == max-1)
```

```
{ printf("overflow"); top=0 }
```

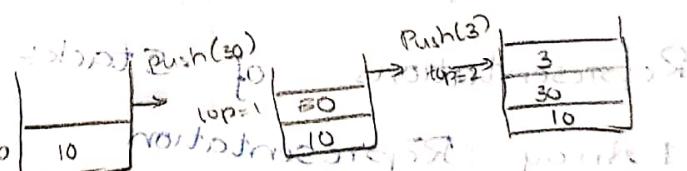
```
}
```

```
{
```

```
top++;
```

```
st[top]=x;
```

```
}
```

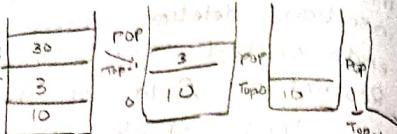


* At a time only one element can be inserted (or) deleted from the stack.

POP Operations

```

code :- if (top == -1)
{
    printf("under flow");
}
else
{
    temp = st[top];
    top--;
}
cout << temp;
    
```



* Stack TOP / Display Operations

```

code :- if (top == -1)
{
    if (stack is empty)
        printf("stack is empty");
    else
        for(i=top; i>=0; i--)
            printf("%d", st[i]);
}
    
```

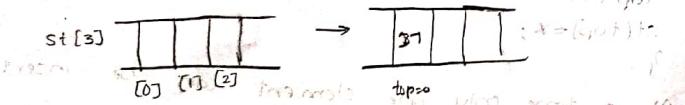
Stack Top is used to display all the data from Top to bottom.

Representations of Stack:

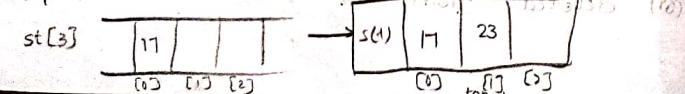
1. Array Representation

Set [17, 23, 9, 5]
maximum size is 3

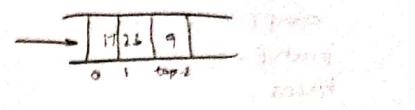
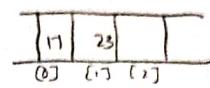
Step-1: PUSH - 17



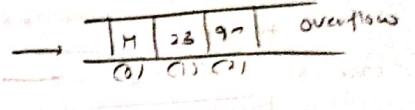
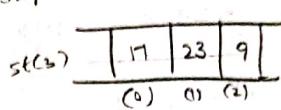
Step-2: PUSH - 23



Step-3: PUSH - 9

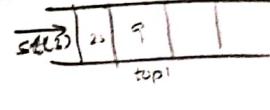
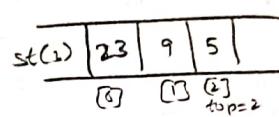


Step-4: PUSH - 5

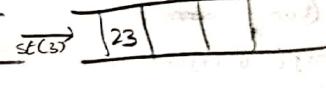


For Deletion

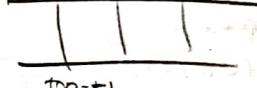
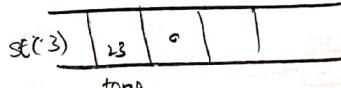
Step-1: POP - 5



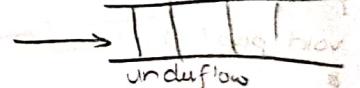
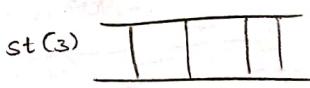
Step-2: POP - 9



Step-3: POP - 23



Step-4: POP - 17



Stacks using Arrays st

```

#define size 3
void push(int);
void pop();
void display();
int st[size], top=-1;
void main()
{
    int x, ch;
    printf("1. Push 2. Pop 3. display\n4. Exit");
    printf("Enter your choice");
    scanf("%d", &ch);
    switch(ch)
    {
        case 1:
            push();
            break;
        case 2:
            pop();
            break;
        case 3:
            display();
            break;
        case 4:
            exit(0);
        default:
            printf("Wrong choice");
    }
}
    
```

```
case1: printf("enter element");
        scanf("%d", &x);
        push(x);
        break;
case -2: pop();
        break;
case -3: display();
        break;
case -4: exit(0);
default: printf("wrong choice");
        }
```

```
void push(int x)
{
    if (top == max-1);
        printf("overflow");
    else
    {
        top++;
        st[top] = x;
    }
}
```

```
void pop()
{
    if (top == -1)
        printf("underflow");
    else
    {
        temp = st[top]
        top--;
    }
}
```

```
void display()
{
    if (top == -1)
        printf("stack is empty");
}
```

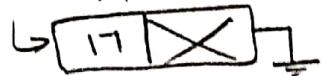
```

else
{
    for(l=top; l>=0; l--)
        printf("%d ", st[top]);
}

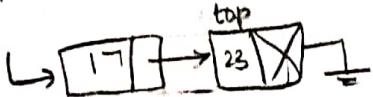
```

3. Below is the Linked list Representation of stack

Step-1 : Push(17)



Step-2 : Push(23)



Step-3 : Push(9)



Step-4 : Push(5)

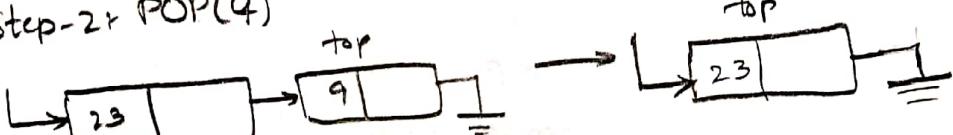


For Deletion

Step-1 : POP(5)



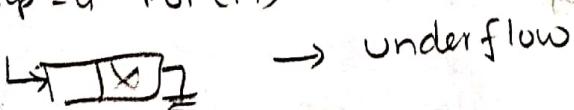
Step-2 : POP(9)



Step-3 : POP(23)



Step-4 : POP(17)

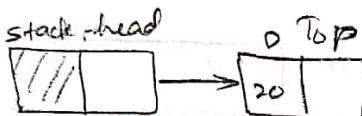


Algorithm for PUSH operation using linked list:

This can be represented using single linked list where insertion and deletion process takes place at only at end of the linked list.

Code:-

```
new = get node(node)
new → data = item
new → link = TOP
TOP = new
stack - Head → Link = TOP
stop
```



If (`top == NULL`) // This indicates to check whether the top value of the linked list is `NULL` or not. If `NULL`, then create a new node and attach it to the header.

```
{  
    top = (struct node*) malloc  
        (sizeof (struct node));  
    top → ptr = NULL;
```

}

else

{

```
    temp = (struct node*) malloc (sizeof  
        (struct node));
```

```
    temp → ptr = top;
```

```
    temp → info = data;
```

```
    count + 1;
```

}

Algorithm for POP operation:

This is used to delete the elements from the end of the linked list

```

code:
    POPC)
    {
        if (top == -1)
            printf("empty");
        else
            {
                printf("not empty");
                temp = top;
                top = top->link;
                temp->link = NULL;
                return node (temp);
            }
    }
}

```

After popping out the top, make the pointer of the top to be assigned to temp. Then top = top->link. Finally, temp->link = NULL; and return node (temp);

Display Operation: To display all the values present in the stack.

```

code:
display()
{
    if (top == -1)
        printf("empty");
    else
        {
            temp = top;
            while (temp != NULL)
            {
                printf("temp->data");
                temp = temp->link;
            }
        }
}

```

Applications of Stacks:

1. Converting the infix expression into the postfix expression.

Steps:

- (1) Scan the infix string from left to right one character at a time.

2. * While the characters are left switch on to the particular character.
- (i) If it is a letter then place it in the postfix string.
 - (ii) If it is an operator check its precedence of top of the stack whether it is higher than the scanned character. Then pop all the top of the stack and add to postfix.
 - (iii) If it is the left parenthesis then push into the stack.
 - (iv) If it is a right parenthesis then pop out from stack till the left parenthesis is encountered.
3. Pop out the stack contents until the stack is empty and add to the postfix expression.
- PRECEDENCE AND ASSOCIATIVITY

PRECEDENCE AND ASSOCIATIVITY

Precedence

	Operator	Associativity
1.	$++$ (period operator)	Left to Right
	$-- \rightarrow$	
	$() []$	
2.	$! \sim * \& \&$ size of (pointers) address	Right to Left
	$\& \&$ size of	
3.	Multiplication*, Division / Modulus%, remainder	Left to Right
	*	*
	/	/
	%	%
4.	$+ -, +d, -d$	Left to Right
	$* -, +$	
5.	$<<, >>d$	Left to Right
	$- +$	
6.	$< > + <= >=$	Left to Right
7.	$= = , !=$	Left to Right
8.	$\& \&$ [Bitwise AND]	Left to Right
9.	\wedge [Bitwise Exclusive OR]	Left to Right
10.	$\vee \vee$ [Bitwise Inclusive OR]	Left to Right
11.	$\& \&$ [Logical AND]	Left to Right
12.	$\ \ $ [Logical OR]	Left to Right
13.	? :	right to left
14.	$= =$	right to left
	$\& =$	
	$\% =$	
	$\wedge =$	
	$<< =$	
15.	comma operator	left to right

end

empty

ABC * +

Application - 2 :-

Evaluation of postfix expression.

Character Scanned	Stack content	Explanation
2		Push 2 in to stack.
3		Push 3 in to stack.
5		Push 5 in to the stack.
*		5, 3 is pop out and perform $3 * 5$ we get 15. Push result 15 into stack
+		15 & 2 is popped out and perform $15 + 2$ we get 17. Push 17 in to stack
		17 is the output

~~A+(B*C)~~~~A+[B*C-(D/E-F)*G]*H~~

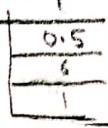
Character scanned	Stack content	Postfix Expression
A	+	A
+		A
(+ C	A B
B	+ C	A B
*	+ (*	A B C
C	+ (*)	A B C
-	+ (* -	

	+ C -	A B C *
C	+ C - C	A B C * D
D	+ C - C	A B C * D E
/	+ C - C /	A B C * D E F
E	+ C - C / -	A B C * D E F G
-	+ C - C / -	A B C * D E F G H
F	+ C - C / -	A B C * D E F G H I
G	+ C - C / -	A B C * D E F G H I J
H	empty	A B C * D E F G H I J K

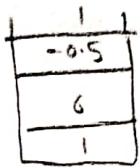
Character scanned	Stack content	Explanation
1	[]	Push 1 into the stack
2	[1]	Push 2 into the stack
*	[1]	Push 3 into the stack
*	[1]	3 * 2 is popped out and perform $2 * (3 * \text{wc})$ getting 6
1	[]	Push 1 to the stack
2	[1]	Push 2 into the stack



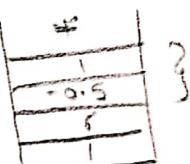
2 & 1 is popped out & perform $1/2$
we get $0.5 + 1$ push
 0.5 in to stack
13 & 1 is popped out &
perform $13 - 1$ we get
 12 push it in to stack



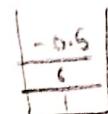
Put 6 into the stack.
0.5 & 1 is popped out
and perform $0.5 - 1$
we get -0.5 and
push it in to the stack



Push 6 into the stack.

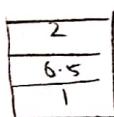


1 & -0.5 is popped out and perform 1×-0.5 and push in to the stack.



6 & -0.5 is popped out and perform $6 - (-0.5)$
we get 6.5

Push 2 into the stack



2 & 6.5 is popped out & perform $2 + 6.5$ we get
13. Push it in to the stack.



13 & 1 is popped out & perform $13 + 1$ we get 14
Push it in to the stack



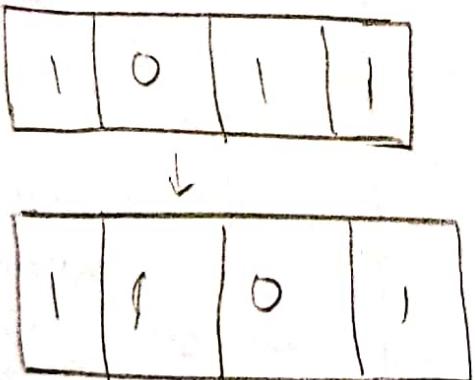
14 is the result



Other applications of stacks :-

- * It is used for viewing the page history visited in any browser.
- * It is used in reversing the array elements of the given order.
- * It is also used in number conversion. This can be converted into binary number by the use of stack data structure and can display the obtained output.

```
while (num >= 0)
{
    digit = num % 2;
    push(digit);
    num = num / 2;
}
```



PART-B
QUEUES

* Queue is also a linear data structure where the insertion and deletion takes place at two different ends.

They are 1. Rear End or FIFO
2. Front End

* Insertion Operation of Queue

Algorithm :-

```
if (rear == max-1)
{
    printf("full");
    printf("queue is full");
}
else
{
    rear++;
    rear=rear+1;
    qu[rear] = x;
}
```

* Deletion Operation

Algorithm :-

```
if (front == -1)
{
    printf("queue is empty");
}
else
{
    front++;
    front=front+1;
    qu[front]=x; (or) x=qu[front];
}
```

* Display Operation

Algorithm :-

```
if (front == rear);
{
    printf("queue is empty");
}
else
{
    for(i=front, i <= rear, i++);
    printf("%d", qu[front]);
}
```

```
if (front == rear)
{
    printf("queue is empty");
}
else
{
    for(i=front, i <= rear, i++);
    printf("%d", qu[front]);
}
```

Types of queues

Circular Queue is called as Ring Buffer.
* It can also perform insertion and deletion
* Here both insertion and deletion takes place in circular fashion.
i.e. in a clockwise direction.

Algorithm

Note: The insertion process in the queue is called "enqueue".
The deletion process is called "dequeue".

Algorithm for Insertion:

```
void enqueue(int x)
{
    if(front == 0 && rear == size - 1)
        printf("Queue is full");
    else
    {
        if(rear == size - 1)
            rear = 0;
        else
            rear = rear + 1;
        cq[rear] = x;
        if(front == -1)
            front = 0;
    }
}
```

Algorithm for Deletion:

```
void dequeue(int x)
```

```
{
    if(front == -1)
```

```
    printf("queue is empty"),
```

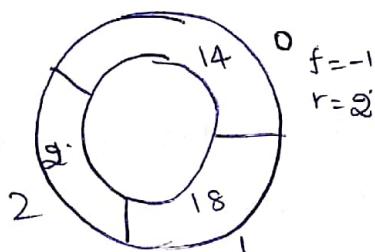
etc

```

printf("%d", cq(front));
if(front == rear);
{
    front=rear=-1;
}
else
{
    if(front == size-1);
        front=0;
    }
    else
        front = front+1;
}

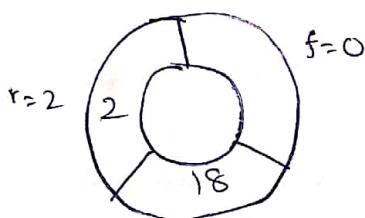
```

Ex:- To insert 3 - element

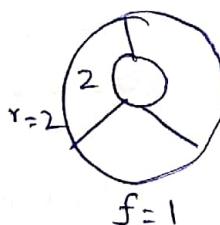


14, 18, 2, 3,

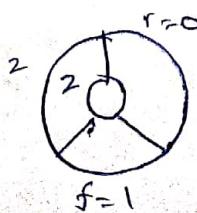
→ Now delete 14



→ Now delete 18

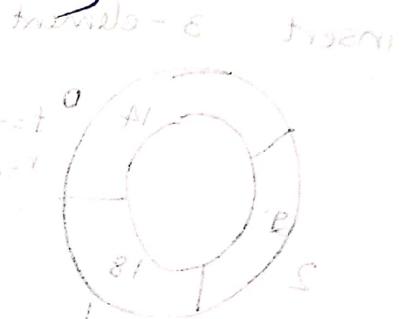


→ Now enter 3



Display : Algorithm for Display

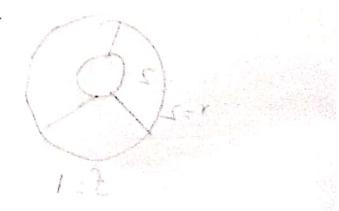
```
void display( )  
{  
    if(front == -1)  
    {  
        printf(" Queue is empty");  
    }  
    else if(front <= r) if(front <= rear);  
    while(front <= r), while(front <= r);  
    {  
        printf(" cq[front]"),  
        front++;  
    }  
    else  
    {  
        while(front = max - 1)  
        {  
            printf(" cq[front]"),  
            front++;  
        }  
        front = 0;  
        while(front <= rear);  
        {  
            printf(" cq[front]");  
            front++;  
        }  
    }  
}
```



41 delete and



81 delete and



5 return and

Double Ended Queue

Double Ended Queue is a linear data structure where insertions and deletions are done at the ends but not in the middle.

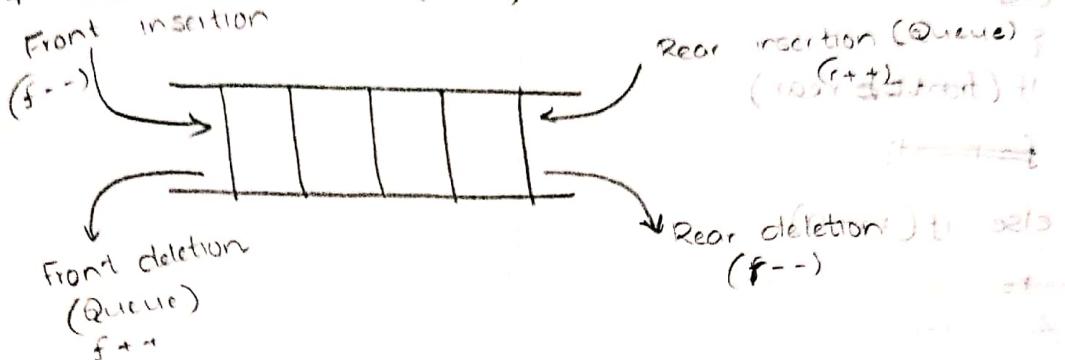
There are 4 types of operations such as

1. Front insertion ($f++$)

2. Front deletion ($f--$)

3. Rear insertion ($r++$)

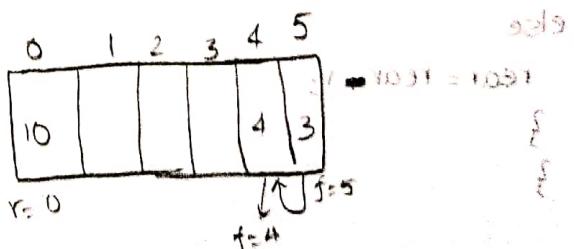
4. Rear deletion ($r--$)



* Here rear insertion & front deletion follows
are as same as in the linear queue

Front Insertion :-

```
void dq_insert_front(int x)
{
    if(front == -1 && rear == size - 1)
        printf(" deque is full");
    else
        if(front == -1)
            front = rear = 0;
        else
            if(front == 0)
                front = size - 1;
            else
                front = front - 1;
    dq[front] = x;
}
```



Deletion at Rear

While deleting out of the rear, the rear value by order. sometimes the above will do a swap.

Algorithm:

```
Void dq_delete_rear()
{
    If (front == -1)
    {
        printf("Queue is empty");
    }
    else
    {
        If (front == rear)
        {
            f = -1;
        }
        else if (r == 0)
        {
            r = size - 1;
        }
    }
}
```

Algorithm:

```
Void dq_delete_rear()
{
    rear = -1;
    If (front == -1)
    {
        printf("Queue is empty");
    }
    else
    {
        If (front == rear)
        {
            front = rear = -1;
        }
        else if (rear == 0)
        {
            rear = size - 1;
        }
        else
        {
            rear = rear - 1;
        }
    }
}
```

1	2	3	4	5
10	20	30	40	50

Front deletion :

```
void dq front delete(int x)
{
    if (front == -1) & rear_size == 0;
    printf("double queue is empty");
}
else
{
    front++;
    dq[front] = x;
}
```

Rear insertion :

```
void dq rear insert()
{
    if (rear == max) then msg or it dq isn't
    {
        printf("dq is full");
    }
    else
    {
        rear++;
        dq[rear] = x;
    }
}
```

both modified with

front ++
rear ++

performed in step 7

[0,1] = (0) phone

[1,2] = (1) option

[2,3] = (2) phone

option

phone

Priority Queue: It is a queue where insertions and deletions are done from any position based on the priority.

* In a priority queue element with highest priority will be deleted first. Such we can store highest priority element at the front.

Example: Executing the jobs.

$J_1(2)$	$J_2(1)$	$J_3(1)$
f ↑		r ↑

* The job J_1 is given with highest priority.

To insert $J_4(0)$

$$\text{Priority } (2) = \boxed{J_1(2)}$$

$$\text{Priority } (1) = \boxed{J_2(1) \quad J_3(1)}$$

$$\text{Priority } (0) = \boxed{J_4(0)}$$

$J_2(2)$	$J_2(1)$	$J_3(1)$	$J_4(0)$
f ↑			r ↑

To insert $J_5(2)$

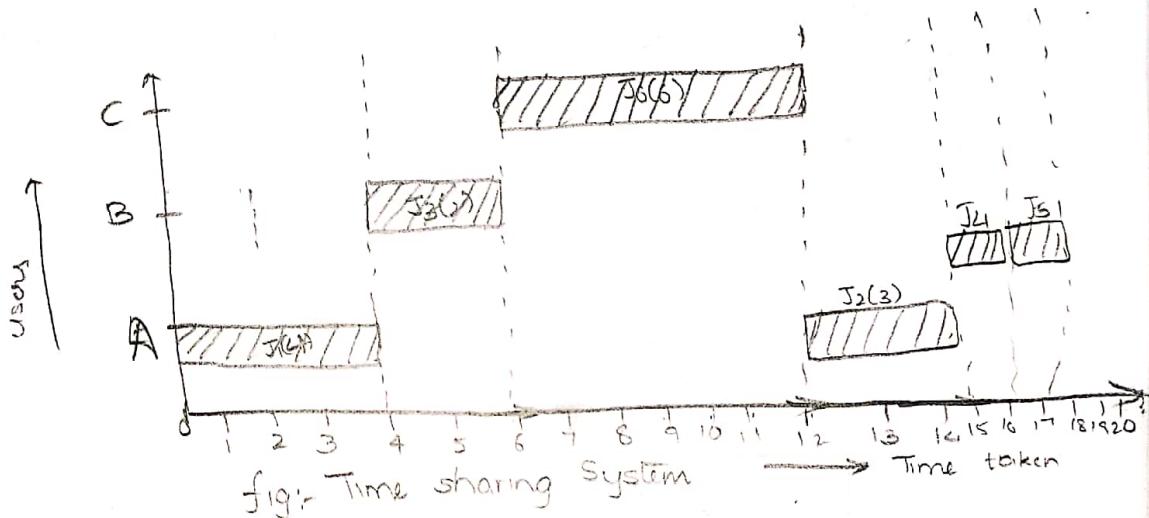
By following linear queue principle
FIFO / LIFO

$J_2(2)$	$J_5(2)$	$J_2(1)$	$J_3(1)$	$J_4(0)$
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Applications of Questions

- (1) CPU Job scheduling; FCFS CPU scheduling system.
OR
 - ~~Job~~ Time sharing System
 - (2) Round Robin CPU scheduling Algorithm.
 - (3) Priority CPU scheduling Algorithm.
 - (1) ~~Job~~ CPU Job Scheduling; [Linear Queue];

Users	Jobs
A	J ₁ (4), J ₂ (3)
B	J ₃ (2), J ₄ (1), J ₅ (1)
C	J ₆ (6)

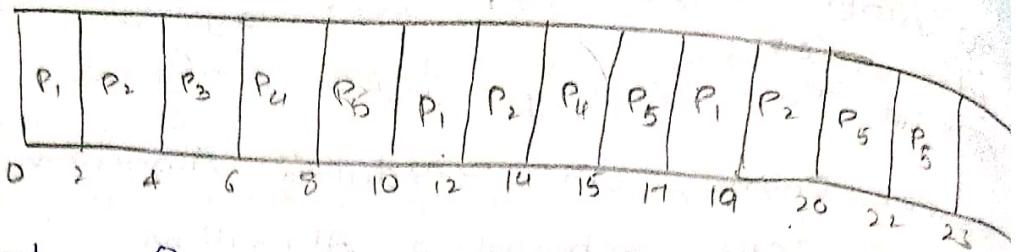


- (2) Round Robin CPU scheduling algorithm :-
In this round robin algorithm the process has been scheduled based on their time quantum allotted between them.

Process	Time Taken
P ₁	6400
P ₂	5300
P ₃	70
P ₄	300
P ₅	1800

Time quantum
i.e. the time which
is limited

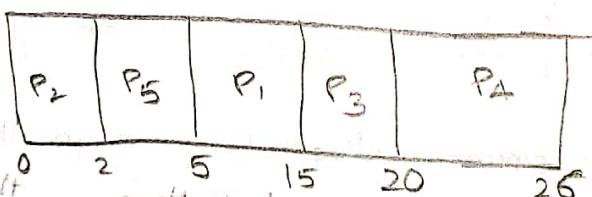
Time quantum = 2



Priority Queue :-

Priority CPU scheduling algorithms

Process	Time taken/ burst time	Priority
P ₁	10	3
P ₂	2	1
P ₃	5	4
P ₄	6	5
P ₅	3	2



Applications based on Queues

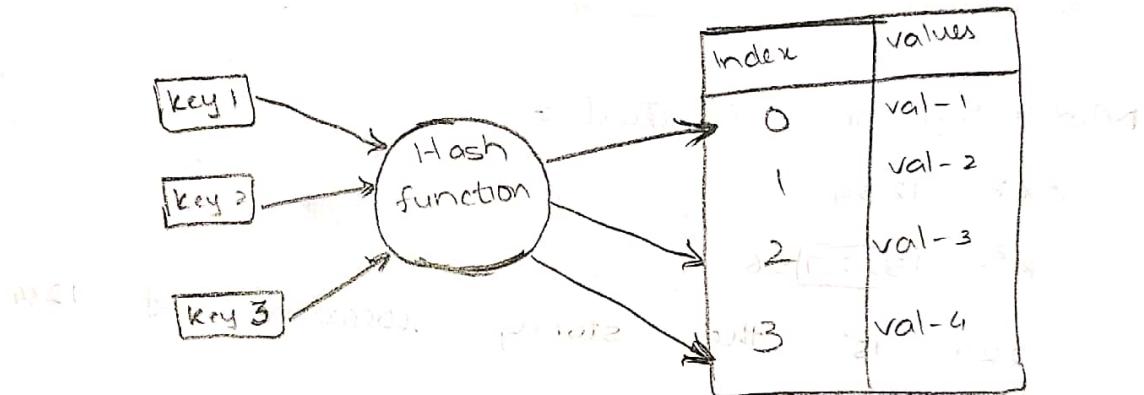
- * Statements executed by ~~microprocessor~~ microprocessor
- * OS task scheduling.
- * Print lines of a document
- * Printer sharing between computers
- * Recognizing Palindromes
- * Queues used in Simulation applications.

TABLES

Hash Table :-

Hash table is a kind of data structure used to store the data in the form of arrays using its own unique indexing value.

* This can be obtained by Hash function which is used for calculating the addressing values (or) hash codes



The hash index can be calculated as
 (key \% size) $H(\text{key}) = \text{Key \% size}$

Methods used in Hash tables:-

* To generate the address or to store the key value at any position in the hash table we can have different types of methods

1. Division Method

2. Mid Square Method

3. Folding Method

4. Digital analysis Method

Division Method

It is a method

This method is followed by using the formula

$$h(\text{key}) = \text{key \% size}$$

Ex:- 20, 25, 33, 46, 50 size 10

$$h(20) = 20 \% 10 = 0$$

$$h(25) = 25 \% 10 = 5 \text{ or stored at index } 5$$

$$h(33) = 33 \% 10 = 3 \text{ or stored at index } 3$$

$$h(46) = 46 \% 10 = 6 \text{ or stored at index } 6$$

$$h(50) = 50 \% 10 = 0 \text{ or stored at index } 0$$

Here collision occurs, so we follows

1. Closed hashing
2. Open hashing methods

to overcome this collision.

0	20
1	
2	33
3	
4	
5	25
6	46
7	
8	
9	

Mid Square Method :-

Ex:- 1234

$$K^2 = 1522756$$

227 is the storing location of 1234

Folding Method's

In this folding Method the given key is chopped into 'n' no. of subkeys and then at the sum of all the keys the final key will be stored.

* Even in this method there are 3 different types of Techniques as

1. Pure Folding Method

2. Fold shifting Method

3. Fold Boundary Method

Pure Folding Method

This is used to store at the location where the sum of all the partitioned keys is obtained.

Fold Shifting Method

In this method consider odd numbered positions of Partition keys & reverse those positions values and then add those values together.

Fold Boundary Method

Consider the first and last partitioned keys and reverse them then add together.

Ex: $K = \underline{15} \underline{22} \underline{27} \underline{56}$

chopping = 01 52 27 56
= 136th position \rightarrow Pure folding Method

Fold shifting method

$$\begin{aligned} &= \overbrace{01} \quad \underline{52} \quad \overbrace{27} \quad \underline{56} \\ &= 10 \quad 52 \quad 27 \quad 56 \\ &= 190^{\text{th}} \text{ position} \end{aligned}$$

Fold Boundary method

$$\begin{aligned} &= \overbrace{01} \quad 52 \quad 27 \quad \overbrace{56} \\ &= 10 \quad 52 \quad 27 \quad 65 \\ &= 154^{\text{th}} \text{ position} \end{aligned}$$

Digital Analysis Method:

In this method the hash address is formed by extracting even no. of digit positions and reversing them.

Ex: $15 \underline{22} \underline{27} \underline{48} \underline{6}$

Reversing
 825^{th} position

* Among all these method is used for allocating the key in the hash tables for major applications

Types of Hashing:

There are 2 types of Hashing Technique

(1) Closed Hashing

(2) Open Hashing

These Techniques are used for resolving the collision problems.

Closed Hashing :

(1) Linear Probing Technique

(2) Quadratic Probing Technique

Linear Probing Technique

Ex:- 11, 10, 20, 23, 25, 22

Size = 10

$$H(11) = 11 \% 10 = 1$$

$$H(10) = 10 \% 10 = 0$$

$$H(20) = 20 \% 10 = 0$$

* '0' is filled & next higher address will be checked

* 1 is also filled & next higher address will be checked

* if this is empty so will be stored at

0	10
1	11
2	20
3	23
4	22
5	25
6	
7	
8	
9	

Quadratic Probing Technique:

In this Technique the key elements are stored by the process of probing

1. Assign $J=0$

2. Get the hash values by $(K+j^2) \bmod \text{size}$

$$H(K) = (K+j^2) \% \text{size}$$

Ex: Insert the elements 76, 40, 48, 5, 20 with maximum size as 7.

$$H(76) = (76 + 0) \% 7 \\ = 6$$

$$H(40) = (40 + 0) \% 7 \\ = 5$$

$$H(48) = (48 + 0) \% 7 \\ = 6$$

$$H(48) = (48 + 1) \% 7 \\ = 0$$

$$H(5) = (5 + 4) \% 7 \\ = 02 \\ = (5 + 3) \% 7 \\ = 81$$

$$H(20) = 20 \% 7 \\ = 6 \neq \\ = 21 \% 7 \\ = 0$$

$$= (20 + 4) \% 7 \\ = 24 \% 7 \\ = 3$$

~~* Open Hashing :-~~ [Chaining Process]
 * Chaining of elements will be taken
 place by using linked list concept

Ex: 10, 20, 33, 43, 54

$$H(k) = k \% 10$$

