

Asymptotic Notations

These are the expressions used to calculate the complexity of an algorithm.

- * There are 3 types of Analysis that we perform for any algorithm.

1. Best Case

2. Worst Case

3. Average Case

Best Case: It is a case in which further input given and space. the algorithm takes less time

Worst Case: It is a case in which further input given and space. the algorithm takes more time

Average Case: This lies between Best Case & Worst Case.

Asymptotic Notations

- * There are 3 types

(1) Big-oh (O) Notation

(2) Theta (Θ) Notation

(3) Omega (Ω) Notation

Big- O Notation

This defines

an algorithm.

This describes the worst case scenario as it takes maximum values than the input

This takes data.

Ex: Consider function $f(n) = 2n^2 + 3n + 5$

Condition: $f(n) \leq c * g(n)$

(1) Under taken as $f(n) \leq c * g(n)$

Condition:

$c = 5$

$n = 10$

$g(n) = n^2$

$n = 10$

$c = 5$

$n = 10$

$g(n) = n^2$

$n = 10$

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$g(n) = n^2$

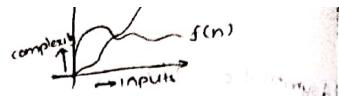
$n = 10$

$c = 5$

$n = 10$

Soln Let $x=1$

$$f(1) = 2(1) + 3(1) + 5$$

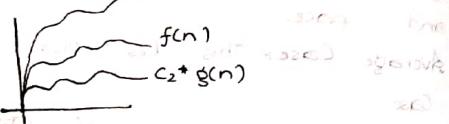


≈ 10 is considered as the existing value such that $C=10$ & $n \leq 1$

Theta Notation: The theta notation describes the bounded value in b/w the lower bound & upper bound.

* The condition with which the theta notation is applicable can be given as

$$C_1 * g(n) \leq f(n) \leq C_2 * g(n)$$



* As the value of theta notation lies in b/w upper bound and the lower bound, it resembles the average case.

Ex: $C_1 \leq \frac{1}{2} - 3/n \leq C_2$, n will be $n \leq 7$

$$C_1 = \frac{1}{2} - 3/7 \text{ and } n \leq 7 \text{ so } 0.5$$

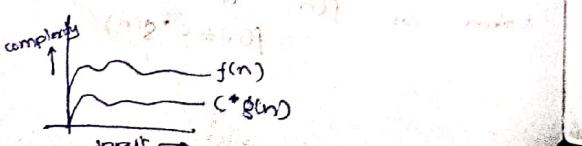
$$C_1 = \frac{1}{14} \text{ when } n=7$$

$$C_2 = \frac{1}{2} - 3/10 = \frac{1}{2} - 0.3 = 0.4$$

$$\text{so } C_1 = 0.14 \text{ and } C_2 = 0.4$$

Omega Notation / Big-Omega Notation (Ω)

Omega notation is used to define the lower bound of $f(n)$.



* This omega notation includes the condition $f(n) \geq C * g(n)$

* It will be under best case analysed from many of the algorithm.

Ex: Consider the equations $f(n) = (n^3 + n^2 + n + 1)$ & $g(n) = 3n^2 + 2n + 1$

$$g(n) = 3n^2 + 2n + 1$$

Let $n = 3$

$$40 \geq 34$$

$\therefore n \geq 3$

Algorithm: It is a step-by-step procedure used to describe the program execution.

Ex: To perform add operation,

Start

↓

Read a and b values

↓

Declare $c = a + b$

↓

Perform add operation → Print c

↓

Stop

Arrays: An array is a collection of the similar data items held at ~~one~~ more adjacent cells

Syntax: `<datatype> <name of array> [size];`

* Arrays are static elements in nature.

* Arrays have the static memory allocation.

Ex: `int a[5];`

`int marks[10];`

* The array memory allocation will always starts with zero [0].

Types of Arrays:

1. 1-dimensional Array

2. 2-dimensional Array

3. Multi-dimensional Array

One-dimensional Array

* It is also known as single dimensional linear array.

Declaration

Syntax: <datatype> <arrayname> [size];

Ex: int marks[10];

Initialization

Ex: int marks[5] = {10, 20, 30, 40, 50};

char name[5] = {'a', 'b', 'c', 'd', 'e'};

Write a program to illustrate the declaration, initialization and accessing elements of an array.

```
<stdio.h>
<conio.h>
void main()
{
    int marks[5] = {10, 20, 30, 40, 50};
    int i;
    for(i=0; i<5; i++)
        printf("%d", marks[i]);
    getch();
}
```

Write a program for declaring, reading and printing the array elements.

```
<stdio.h>
<conio.h>
void main()
{
    int marks[5];
    int i;
    printf("enter array element");
    for(i=0; i<5; i++)
        scanf("%d", &marks[i]);
    for(i=0; i<5; i++)
        printf("%d", marks[i]);
    getch();
}
```

Two-dimensional Arrays

A two-dimensional arrays includes a number of indices which represent the row & the column data.

The basic application of the two-dimensional arrays is matrix representation syntax for declaration of 2-dimensional arrays:

Syntax: <datatype> <arrayname> [row][column];

Ex: int a[3][3];

Syntax for initialization of 2-dimensional array:

Syntax: <datatype> <arrayname> [row][column] = {values};

int a[3][3] = {1, 2, 3, 4, 5, 6, 7, 8, 9};

Write a program to illustrate the declaration, initialization and accessing of elements from 2-dimensional array.

```
<stdio.h>
<conio.h>
void main()
{
    int a[3][3] = {1, 2, 3, 4, 5, 6, 7, 8, 9};
    int i, j;
    for(i=0; i<3; i++)
        for(j=0; j<3; j++)
            printf("%d", a[i][j]);
    getch();
}
```

Write a C-program to illustrate, declaring, reading & printing the array elements of 2-dimensional array

```
<stdio.h>
<conio.h>
void main()
{
    int a[3][3];
    int i, j;
    scanf("%d", &a[i][j]);
    printf("%d", a[i][j]);
    getch();
}
```

Write the program to find product of 2 matrices.

```
#include<stdio.h>
#include<conio.h>
void main()
{
    int a[2][2], b[2][2], c[2][2], i, j, k;
    clrscr();
    printf("enter 2*2 matrix elements:");
    for(i=1; i<=2; i++)
    {
        for(j=1; j<=2; j++)
            scanf("%d", &a[i][j]);
    }
    printf("\n enter 2*2 matrix elements:");
    for(i=1; i<=2; i++)
    {
        for(j=1; j<=2; j++)
            scanf("%d", &b[i][j]);
    }
    printf("the 2*2 matrix elements of a:");
    for(i=1; i<=2; i++)
    {
        printf("\n");
        for(j=1; j<=2; j++)
            printf("%d\t", a[i][j]);
    }
    printf("\n the 2*2 matrix elements of b:");
    for(i=1; i<=2; i++)
    {
        printf("\n");
        for(j=1; j<=2; j++)
            printf("%d\t", b[i][j]);
    }
    for(i=1; i<=2; i++)
    {
        printf("\n");
        for(j=1; j<=2; j++)
        {
            c[i][j]=0;
            for(k=1; k<=2; k++)

```

```

    {
        c[i][j] = c[i][j] + a[i][k] * b[k][j];
    }
}

printf("The product of two matrices:"),
for(i=1; i<=2; i++)
{
    printf("\n");
    for(j=1; j<=2; j++)
        printf("%d", c[i][j]);
}
getch();
}

```

```

void main()
{
    int a[10][10], b[10][10], c[10][10], r, c, i, j, k;
    printf("enter no. of rows");
    scanf("%d", &r);
    printf("enter no. of columns");
    scanf("%d", &c);
    printf("enter the values of matrix x:");
    for(i=0; i<r; i++)
    {
        for(j=0; j<c; j++)
        {
            scanf("%d", &a[i][j]);
        }
    }
    printf("enter the values of matrix y:");
    for(i=0; i<r; i++)
    {
        for(j=0; j<c; j++)
        {
            scanf("%d", &b[i][j]);
        }
    }
}

```

```

printf("multiplication of matrix a & b");
for(i=0; i<r; i++)
{
    for(j=0; j<c; j++)
    {
        c[i][j]=0; // here the initial value of c[i][j] is considered
        as zero(0).
        for(k=0; k<C; k++)
        {
            c[i][j] = c[i][j] + a[i][k] * b[k][j];
        }
    }
}

```

Multi-dimensional Arrays -

Multi-dimensional Arrays-
 The arrays with 2 or many dimensions can be called as multi-dimensional arrays.

Syntax of Multi-dimensional Arrays :- `arrayname [size1][size2] ... [sizeN];`

Syntax :- <datatype> <arrayname> [size];

Ex :- int arr a[2][2];
int arr a[2][3][2];
the first index

In 3-dimensional matrix where α_{ij} as $i=1, 2, 3$
 represents the dimension where $j=1, 2, 3$
 represents the rows & columns.
 indices represents the rows & columns.

Ex :- For the statement obtained as

output can be
written as
 $\begin{bmatrix} 1 & 2 \\ 1 & 3 \\ 1 & 4 \end{bmatrix}$ and
 $\begin{bmatrix} 2 & 3 \\ 2 & 4 \\ 2 & 6 \end{bmatrix}$
no. of matrices.

Here dimensions means without any boundaries.

Pointer Arrays:
 These are the collection of addresses. The address of one array pointer varies from other elements address. The representation of arrays will always be unique, i.e. the addresses are in nature.

The pointers can be represented by the symbol "*" .

Ex: int *a[3];
 The syntax of pointer Arrays is

Syntax: <datatype> *<arrayname>[size];

```
Ex:- int *a[3];
* int *a[3];
int i=10, j=20, k=30, y;
a[0]=&i;
a[1]=&j;
a[2]=&k;
for(y=0; y<3; y++)
printf("%d", *a[y]);
```

Dynamic Memory Allocation:

This covers all the disadvantages of arrays concept by allowing the memory to be allocated Dynamically.

There are 4 Dynamic Memory Allocation functions:

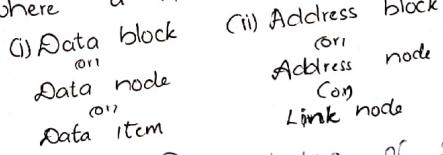
- * malloc()
- * calloc()
- * realloc()
- * free()

These are used to allocate and de-allocate the memory of a variable.

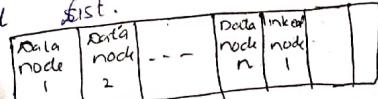
malloc() is used to dynamically allocate single large block of memory with a fixed size.
 Syntax of malloc() is:
 Syntax: ptr = (datatype *) malloc(byte-size);
 Ex:- ptr = (int *) malloc(100 * sizeof(int));
 This allocates 100 (or) 400 bytes of memory all together when taken as int (or) long-int.
 calloc() :- [contiguous memory allocation]
 It is used to allocate specified memory block memory for the exact type
 Syntax: ptr = (datatype *) calloc(n, element size);
 Syntax: ptr = (datatype *) calloc(25, * size of (float));
 Ex:- ptr = (float *) calloc(25, * size of (float));
 realloc() :- [Reallocation]
 Reallocation is used to change the memory allocated by either malloc() or calloc()
 such that it enables the new size to a variable
 Syntax: ptr = realloc(ptr, newsize);
 new size indicates the size given for reallocation.
 Ex:- ptr = realloc(10 * sizeof(float));

free(): It is used to de-allocate the given size of a variable
 Syntax: free(ptr);

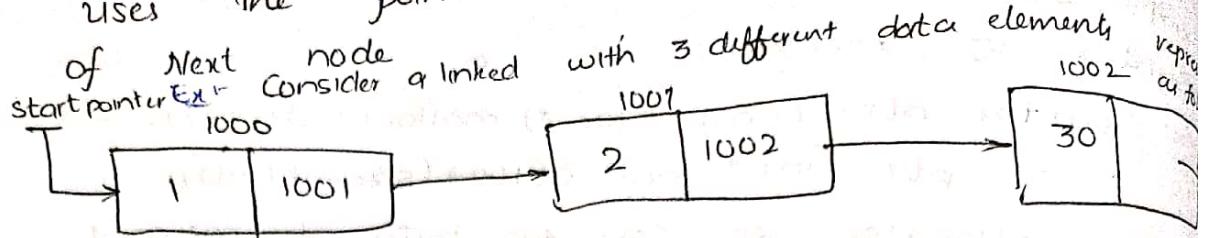
Linked Lists:
 It is a data structure that contains sequence of records stored at nodes blocks.
 where a node is a combination of



Syntax (or) Representation of node structure in linked list.



Linked list is the series of nodes used to store the address of the pointer node.



Advantages of Linked List:

- * It allocates the memory dynamically.
- * In these linked list the insertion & deletion of data can be done easily.

The linked

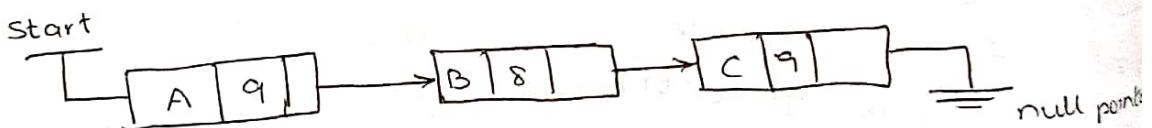
C. Types of Linked Lists:

There are different types of linked lists.

1. Single Linked list:

This is the data item where each node can have one (or) many data nodes but only one link node.

* The single linked list has only one link per node as given below



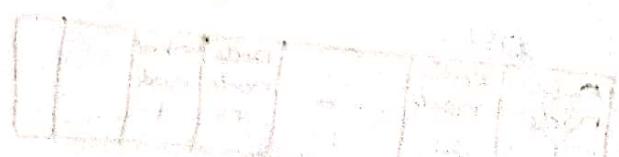
Operations on Single Linked list:

(1) Insertion

(2) Deletion

(3) Traversal

C.



Single linked list Operations

Creating of linked list :-

steps for creating a new node of single linked list :-

(1) Allocate the node

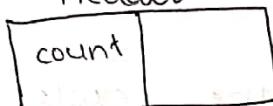
(2) Use the "getnode()" of function as

call getnode(x)

(3) Then set the head link i.e. of the particular list to null and also the list count to zero(0).

Header

(4)



Here the count is used to store the no. of elements or no. of nodes in the single linked list.

(5) The second part of header x is head which is used to create the new nodes.

(6) Insertion of Data :-

Insertion of Data can be done in three ways.

1. Inserting at Beginning
2. Inserting at Ending
3. Inserting at Middle.

Inserting at Beginning:-

This is used to insert the node at the beginning of the linked list such that by creating the very first node attached to the header node created

Input :- Here header is the pointer to the header node and the x is considered as the data of the node which is used to be inserted.

Steps :-

```

new = getnode(node)
if (new = null) then
printf("memory underflow")
exit
else
new → link = header → link;
new → data = x;
header → link = new;
end if;

```

Insert the value 15 at the beginning of the node

Insertion at Ending :-

This is used to insert the node at end of linked list.

Input :- Header is the pointer to the head node & x is the node we need to insert at the end

Steps :-

- 1) ptr = header; // move the position of cursor (or) pointer get executed from starting of the node.
- 2) while (ptr → link ≠ NULL) // it checks whether the pointer link is null or not.
- 3) ptr = ptr → link // change the pointer to the next node
- 4) end while
- 5) ptr → link = new; // change the link field of a last node as a pointer.
- 6) new → data = x; // change the content x into a new node
- 7) end;

Ex:-

Insertion at Middle :-

Always the insertion at the middle is done just based on the key element

[i.e. the element after which the node to be inserted]

Algorithm :-

```

new = Getnode(node)
if (new = null) then
printf("Memory insufficient")
exit

```

```

new = getnode(node)
if (new = null) then
printf("Memory insufficient")
exit
else
new → link = header → link;
newdata = x;
header → link = new;
end if.

```



```

else
ptr = header
while (ptr → data ≠ key) and (ptr → link ≠ null) do
    ptr → ptr → link
end while
if (ptr → link = null) then
    printf("key is not available in list");
exit
else
new → link = ptr → link
new → data =>
ptr → link = new
end if
stop

```

Deletion of Nodes from the Single Linked List

List :- The deletion can be made by 3 ways

- (1) Delete at Beginning
- (2) Delete at End
- (3) Delete at any position from the linked list.

Delete at Beginning :- Here the input includes the header node.

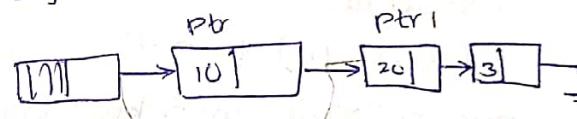
Code :-

```

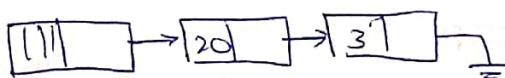
ptr = header → link
if (ptr = null) then
    printf("no deletion");
exit
else
    ptr1 = ptr → link
    header → link = ptr1
    return node (ptr)
end if
exit / stop

```

Before Deletion



After Deletion



Deletion at Ending :-

This is used to delete last node of list & makes the previous node as last node

Steps :-

- * Move from the header node
- * Move to the last node to store the previous pointer & then move to the next node

Code :-

```

ptr = header → link
if (ptr → link = null) then
    printf("list is empty");
exit
else
    while (ptr → link ≠ null) do

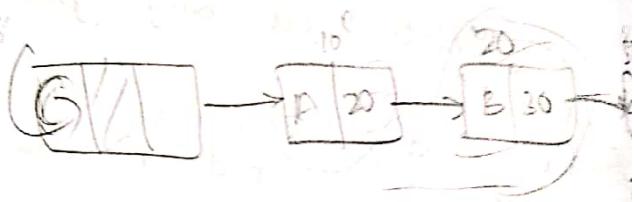
```

```
ptr = ptr;  
ptr = ptr → link  
end while  
ptr → link = NULL  
return node (ptr)
```

Deletion at any position from the linked list:

Code :-

```
while (ptr ≠ NULL) do  
    if (ptr → data ≠ key) then  
        ptr1 = ptr  
        ptr = ptr → link  
    else  
        ptr1 → link = ptr → link  
    return node (ptr)  
    exit  
end if  
end while  
if (ptr = NULL) then  
    printf("Node with key doesn't Exist");  
end if  
stop
```



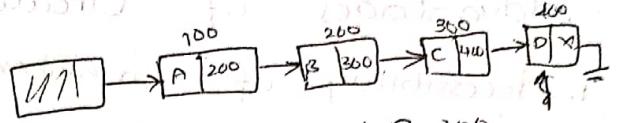
- * Key element is the one after which the element is ~~inserted.~~ deleted
- * In deletion the element which we need to delete is called Key Element, and the element before that is known as

Traversal

Traversal is used to display the elements or the data fields that are present in the given linked list from the beginning of the node till it detects the null link.

Code :-

```
struct node *P
P = start
while (P != NULL)
{
    printf(" P->data");
    P = P->link;
}
```



$P = 100$	$100 \neq \text{NULL(T)}$	$P = 300$	$300 \neq \text{NULL(T)}$
A		C	
$P = 200$	$200 \neq \text{NULL(T)}$	$P = 400$	$400 \neq \text{NULL(T)}$
B	$200 \neq \text{NULL(T)}$	D	$400 \neq \text{NULL(T)}$
$P = 300$	$300 \neq \text{NULL(T)}$	$P = \text{NULL}$	$\text{NULL} \neq \text{NULL(T)}$

Merging Two Different Linked list :-

* Combining of two lists as one can be done by the use of merging process.

* In this consider two header nodes which are the pointers of both the header nodes of separate lists merging the nodes such that node such that will exists.

only one header node

Code:-

```
ptr = Header
while (ptr = ptr->link) do
```

ptr =

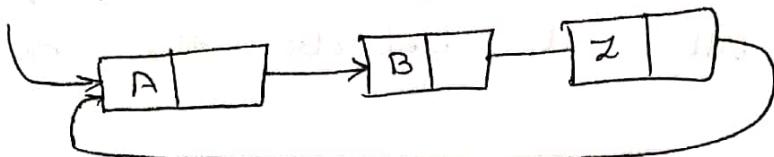
Disadvantages of single linked list:-

In single list the last nodes link field is left with the null link without storing any data also

* Also the starting nodes address will not be stored at any link field of the nodes. So circular linked list is used in order to overcome these disadvantages.

```
ptr = Header
while (ptr->link != NULL) do
    ptr = ptr->link
end while
ptr->link = Header2->link
return node(Header2)
Header = Header2
stop.
```

Circular linked list :-
General representation of circular linked list
is as follows :-



Advantages of Circular linked list :-

1. Accessibility of member nodes in the list is done efficiently.
2. All the nodes here acts as member nodes and can be access from the any node using Chaining Method.

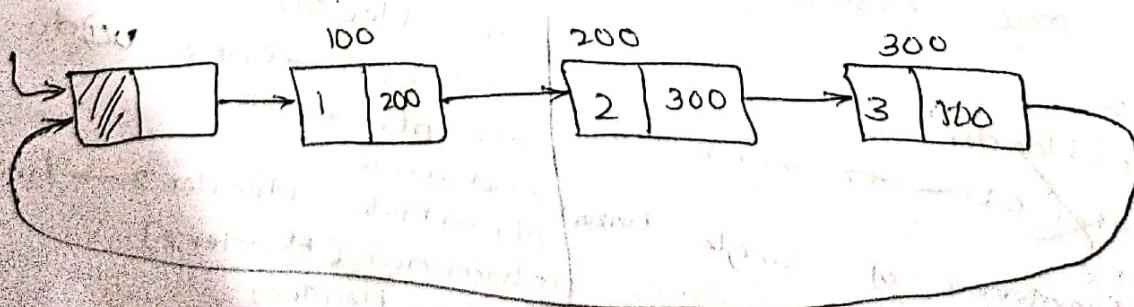
2. NULL-link Problem

No NULL nodes are detected in the circular linked list

3. It is easy to operate the different operations on this linked list.

Disadvantages of Circular linked list
This results in infinite loop problem because we do not have a null link in the circular linked list

Ex:-



Concatenation of two circular linked lists :-
 Consider two circular linked list and make those to be combined as a single circular linked list.

Code:-

```
if L1 ≠ NULL
```

```
{
```

```
if L2 ≠ NULL
```

```
{ temp = Link(L1)
```

```
Link(L1) = Link(L2)
```

```
Link(L2) = Temp
```

```
L1 = L2
```

```
Header1 = Header2
```

```
Header = Header1
```

```
}
```

```
if L1 ≠ NULL
```

```
{
```

```
if L2 ≠ NULL
```

```
{ temp = Link(L1)
```

```
Link(LL1) = Link(L2)
```

```
Link(LL2) = temp
```

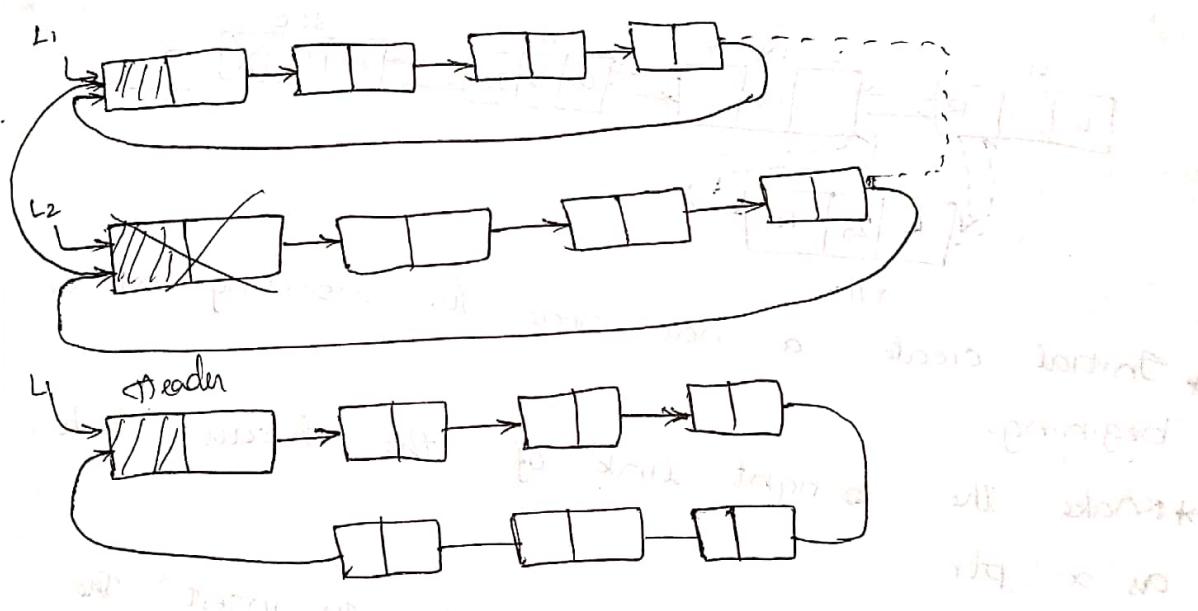
```
L1 = L2
```

```
Header1 = Header2
```

```
Header2 = Header1
```

```
}
```

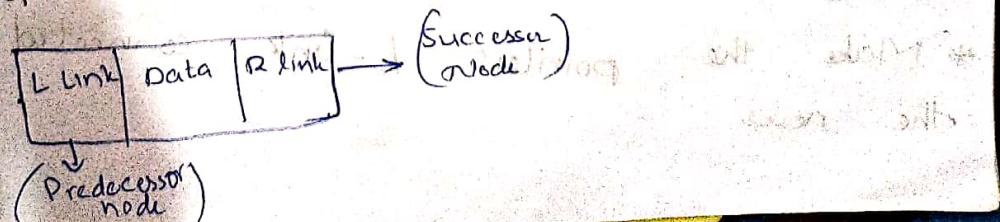
```
}
```

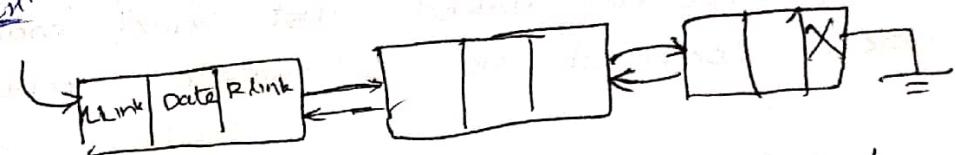


Double linked List:-

In the single linked list the nodes will be processed from left to right, and hence it is called One Way list, and in this single linked list we will have only one link field connected towards the successive nodes.

The representation of Double linked list is:





The operations of Double linked lists are

(i) Insertion

(2) Deletion &

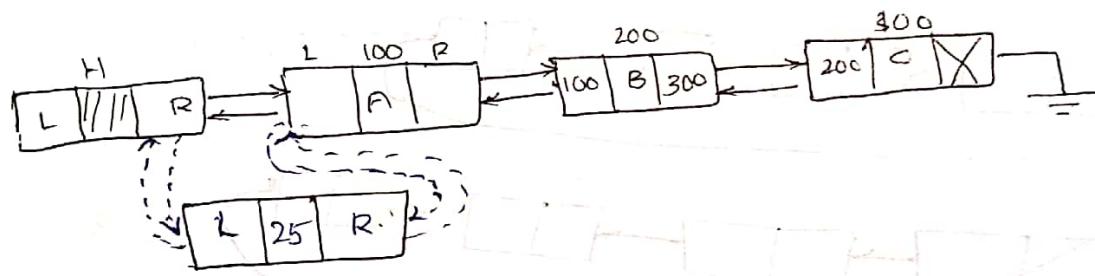
(3) Traversal Mainly

Where as both the insertions & Deletions can done in 3 ways as at the begining, and at any position of the list.

Insertion of Elements in Double linked list.

Inserting at Beginning

Let New be the node to be inserted.



* Initial create a new node for inserting at the beginning.

* Make the right link of the header to be as a ptr

* Then user create the new node to insert the data.

* Header is connected to the L-link of new node

* The new node is assigned to the R-link of the header.

* Connect the pointer to the new \$ nodes

R link

* Make the pointer's L-link connected to the new

Code :-

```
ptr = Header → R link  
new = Get node(node)  
if (new ≠ NULL) then  
① new → l-link = header  
② header → R link = new  
③ new → R link = ptr  
④ ptr → L link = new  
new → data = x
```

Insertion at End :-

- To insert an element
- * First make down the Header then check pointer's R-link is equal to NULL (or) not
 - * If true then insert the element at the position. (or) else make move from one node to the next node.

Code :-

```
ptr = Header  
while (ptr → R link ≠ NULL) do  
ptr = ptr → R link  
end while  
new = Get node(node)  
if (new ≠ null) do then  
① new → l-link = ptr  
② ptr → R-link = new  
③ new → R-link = NULL  
new → data = x
```

Insertion at Middle :-

To insert at the middle make the data to be inserted as x and pointer be the predecessor node where you want to insert and ptr1 be the successor node of the newly inserted data node.

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
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ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
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ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

if (new ≠ NULL) then
for

ptr = Header → R link
new = Get node(node)

```

code:
    while (ptr → data ≠ key) and (ptr → R-link ≠ Null)
        ptr = ptr → R-link
    end while.
    new = GetNode (Node)
    if (new = null) then
        printf("memory not available");
        exit
    end if
    if (ptr → R-link = null) then
        new → L-link = ptr
        ptr → R-link = new
        new → R-link = null
        new → data = x
    else
        ptr1 = ptr → R-link
        new → L-link = ptr
        new → R-link = ptr1
        ptr → R-link = new
        ptr1 → L-link = new
        ptr = new
        new → data = x
    end if
stop

```

* Even the key node can also consider after which you want to insert in the data for that check whether the key node is present in the list or not.

```
{ while (ptr → data ≠ key)
```

```
    and (ptr → R-link ≠ Null)
```

```
    ptr = ptr → R-link
```

```
end while
```

Note: If the key element is not found in the double linked list during the process of inserting at the middle then the elements gets to be inserted at the end of the list.

Deletion of Elements from Double linked list

Deleting at Beginning:

Deleting at the front front ~~not~~ includes a pointer node given as right links of the header node.

ptr = Header \rightarrow R link

If (ptr = NULL) then

print("it is empty")

exit

else

ptr1 = ptr \rightarrow R link

Header \rightarrow R link = ptr1

If (ptr1 \neq NULL)

ptr1 \rightarrow L link = Header

end if

returnnode (ptr)

stop

Deleting at End:

To delete at the end we find the last node to be pointed to a null node such that the null node will be connected to the new node created

ptr = Header

while (ptr \rightarrow R link \neq NULL) do

ptr = ptr \rightarrow R link

end while

If (ptr = header) then

printf("list is empty");

exit

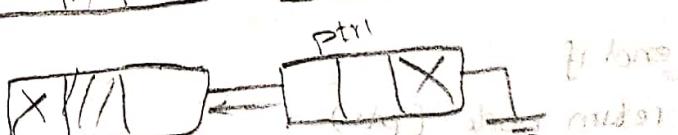
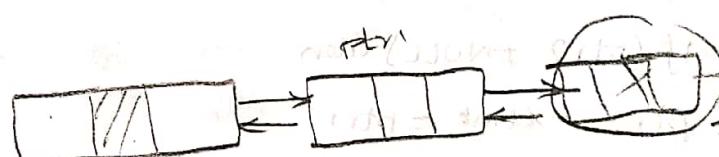
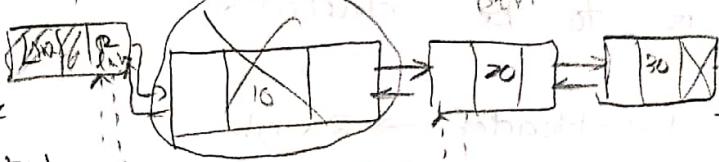
else

ptr1 = ptr \rightarrow L link;

ptr1 \rightarrow R link = NULL;

returnnode (ptr)

end if



Deleting at any position of the Double linked list

In this case of deleting the data from any where of the list we make the search from the begining of the list i.e. from header and we make the use of key or value regarding the element which is to be deleted.

`ptr=Header → Rlink`

`if (ptr=NULL) then`

`print (empty)`

`exit`

`end if`

`while (ptr→Data ≠ key)`

`ptr = ptr → Rlink`
and `(ptr → Rlink ≠ NULL)`

`end while`

④ `if (ptr → Data = key) then`

`ptr1 = ptr → Llink`

`ptr2 = ptr → Rlink`

`ptr1 → Rlink = ptr2`

`if (ptr2 ≠ NULL) then`

`ptr2 → Llink = ptr1`

`end if`

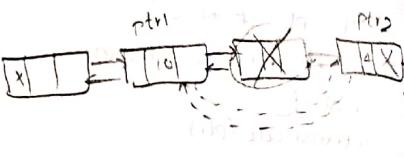
`return node (ptr)`

`else`

`print "node not found"`

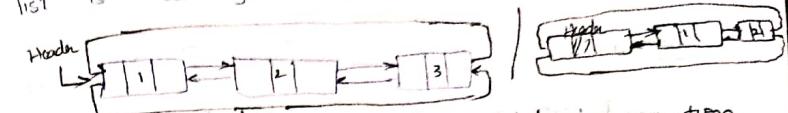
⑤ `end if`

`stop`



* It is a combination of circular linked list and double linked list.

Basic Representation of Circular Double linked list is as given below:



This also performs insertion, deletion, insertion and Traversal operations as that of the circular double linked list.

* Here insertion and the deletion operations can be done in 3 ways as

* at beginning

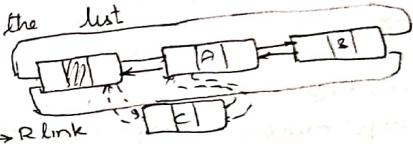
* At ending

* Any where at the list

At beginning :

code:-

```
ptr=Header → Rlink
new=Getnode (node)
if (new≠NULL) then
new→Llink = header
header → Rlink = new
new → Rlink = ptr
ptr → Llink = new
new → data = x
```



At End :

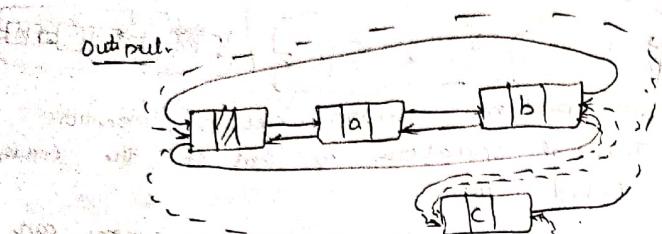
While inserting at the end the last node connected to the very node to the list will be modified and re-connected to the newly added node.

code:-

```
ptr=Header → if (ptr → rlink ≠ Header)
{ptr=ptr → rlink
ptr → rlink = header}
header → Llink = ptr
while (ptr → Rlink != null)
{
ptr = ptr → rlink;
```

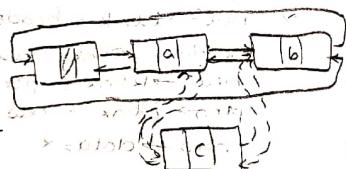
$\text{new} \rightarrow \text{l-link} = \text{ptr}$,
 $\text{new} \rightarrow \text{r-link} = \text{header}$,
 $\text{header} \rightarrow \text{l-link} = \text{new}$,
 $\text{new} \rightarrow \text{data} = \text{x}$.

Output



Insertion at Any Position:

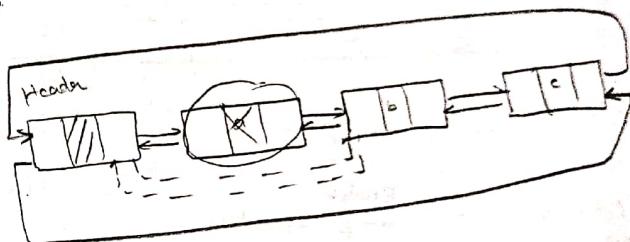
code:-
 while($\text{ptr} \rightarrow \text{data} \neq \text{key}$) and ($\text{ptr} \rightarrow \text{r-link} \neq \text{NULL}$)
 $\text{ptr} = \text{ptr} \rightarrow \text{r-link}$
 end while
 $\text{new} = \text{Get node}(\text{node})$
 if($\text{new} = \text{null}$) then
 $\text{printf(" memory not available")};$
 exit
 end if
 if($\text{ptr} \rightarrow \text{R-link} = \text{NULL}$) then
 $\text{new} \rightarrow \text{l-link} = \text{ptr}$
 $\text{ptr} \rightarrow \text{R-link} = \text{new}$
 $\text{new} \rightarrow \text{R-link} = \text{NULL Header}$
 $\text{new} \rightarrow \text{data} = \text{x}$
 else
 $\text{ptr} = \text{ptr} \rightarrow \text{R-link}$,
 $\text{new} \rightarrow \text{l-link} = \text{ptr}$
 $\text{new} \rightarrow \text{R-link} = \text{ptr}$,
 $\text{ptr} \rightarrow \text{R-link} = \text{ptr} \rightarrow \text{new}$
 $\text{ptr} \rightarrow \text{R-link} = \text{new}$
 $\text{ptr} = \text{new}$
 $\text{new} \rightarrow \text{Data} = \text{x}$
 end if
 STOP



Deletion at Beginning:

```

ptr = Header → R-link
if(ptr = Header) then
  printf(" It is empty");
  exit
else
  ptr1 = ptr → R-link
  Header → R-link = ptr1
  if(ptr1 ≠ Header)
    ptr1 → L-link = Header
  end if
  return node(ptr)
  stop
  
```



Deleting at End & Any Position of the Circular Double linked list:

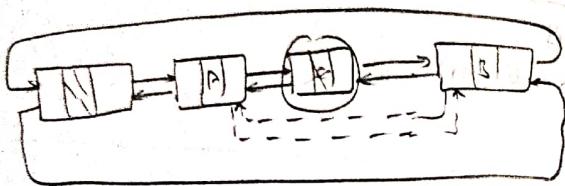
```

ptr = Header → R-link
if(ptr = Header) then
  print("empty")
  exit
end if
while( $\text{ptr} \rightarrow \text{Data} \neq \text{key}$ ) and ( $\text{ptr} \rightarrow \text{R-link} \neq \text{Header}$ ) do
  ptr = ptr → R-link
end while
if ptr1 = ptr → L-link
  ptr2 = ptr → R-link
  ptr1 → R-link = ptr2
  
```

```

if (ptr2 != Header) then
ptr2 → l-link = ptr1
end if
return node(ptr)
else
print("node not found")
end if
stop

```

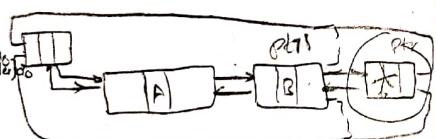


Deleting at ~~any position~~ End +

```

ptr = Header
while(ptr → r-link != Header) do
ptr = ptr → R-link
end while
if (ptr == header) then
printf("list is empty");
exit
else
ptr1 = ptr → l-link;
ptr1 → R-link = header;
header → l-link = ptr1;
return node(ptr);
end if

```



Applications of linked lists
* The linked lists can be used in various applications such as

(i) Polynomial expression

(ii) Addition of Polynomial Expression

* Sparse Matrix representation

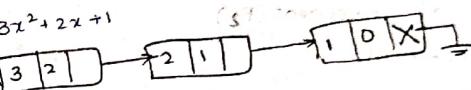
{Addition of } Polynomial Expression

The representation of the polynomial expression used by list is given by

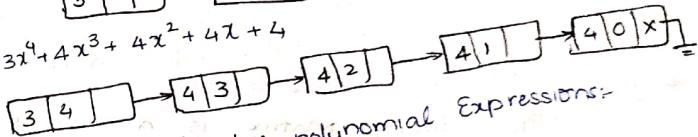
Syntax:

co-efficient	Exponent	link
--------------	----------	------

Ex:-



$3x^4 + 4x^3 + 4x^2 + 4x + 4$



The Addition of two polynomial Expressions:

Add code:
input → co-efficient & exponent values of given polynomial expressions

i.e Let P_1 & P_2 be the polynomial expressions
output The resultant polynomial expression
P [the addition of the two polynomial expressions P_1 & P_2]

code:

```

if ((exponent( $P_1$ )) = ((exponent( $P_2$ ))) {
    if ((co-eff( $P_1$ ) + coeff( $P_2$ )) ≠ 0 then
        call Getnode(x);
        coeffs(x) = coeff( $P_1$ ) + coeff( $P_2$ );
        exponent(x) = exponent( $P_1$ );
        link(x) = null;
}

```

```

if (exponent(P1) > exponent(P2))
{
    call get node(x),
    coeff(x) = coeff(P1)
    exponent(x) = exponent(P1)
    link(x) = null
}
else if (exponent(P1) < exponent(P2))
{
    call get node(x),
    coeff(x) = coeff(P2)
    exponent(x) = exponent(P2)
    link(x) = null
}

```

* Sparse Matrix Representation
The Sparse Matrix is a matrix which contains maximum no. of zero elements.

Ex:- 4x5

$$\begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 0 & 0 & 2 & 0 & 0 \\ 2 & 0 & 0 & 0 & 3 \\ 0 & 5 & 0 & 0 & 1 \\ 0 & 0 & 4 & 0 & 0 \end{bmatrix}$$

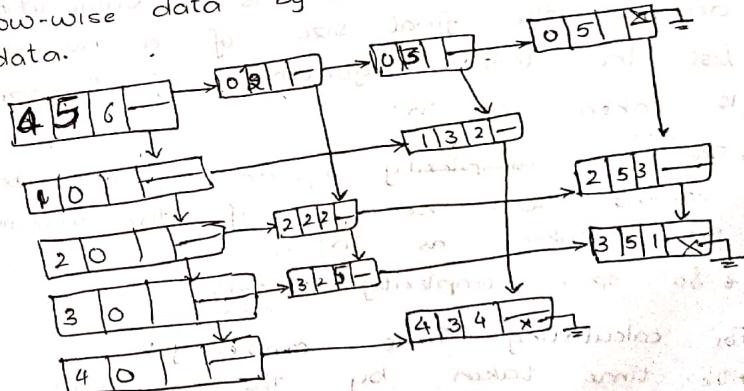
0	0	0	0	0
0	2	0	0	3
2	0	0	0	0
0	5	0	0	1
0	0	4	0	0

* For representing the Sparse matrix we use array representation of elements.
* Here multiple linked list is used for the representation of Sparse matrix.
* The node structure of linked list used for representing the sparse matrix.

Diagram showing the relationship between exponent and coefficient fields of a node:

* From the right link we store the next non-zero elements of the field is connected with each other in the form of a linked list.

* Procedure:-
* The very start node is taken as total no. of rows, columns, data and down link and the right link.
* Then mark the column wise data by disabling the row data.
* Then mark the right link of the start node from here by disabling the row link by disabling the down link mark the data.



Conditions :-
1. If all elements are zero then there will be no linked list.
2. If all elements are non-zero then there will be one linked list.

Calculating Time complexity and space complexity for example algorithm.

Algorithm for sum of

Algorithm sum(number, size)

```
{
    result = 0.0;
    for count = 1 to size do
        result = result + number [count];
    return result;
}
```

To calculate space complexity find 2 different components fixed component and variable component

- * The fixed components are the components (or) the variables given in front of the program.

- * In this algorithm result, count and size are the three different fixed components

- * The variable component is a value which decides the final size of a numbers list. In this algorithm if the size is taken as "n"

- * The space complexity required by a number variable will be "n" if the maximum size is taken as "n".

- * So space complexity = "3+n"

For calculating Time complexity :-

- * The time taken by the program totally for compiling & execution is given as time complexity. So time = fixed time + instance time

statement	Execution	frequency	TT
1. Algorithm sum(number, size)	0	=	0
2. { result = 0.0;	0	=	0
3. for count = 1 to size do,	1	1	1
{ for the statement becomes false & it also includes the statement for number [count];	size	size	size
result = result + number [count];	1	1	1
} return result;	1	-	0
3. }	0	-	0

Frequency is the total no. of times that each statement repeats

∴ The time complexity = $2 \cdot size + 3$

* Code for Searching a key

```

while (head != NULL)
{
    if (head → current == key)
        printf("key found");
    else
        head = head → next;
}
printf("key not found");
}
```

UNIT 2 STACKS AND QUEUES

Stacks:- Stack is a linear data structure in which all the operations (such as insertion, deletion) takes place at only one end called "TOP". Thus it is also called Restricted Data Structure.

* In this stack the insertion operation is called PUSH operation & Deletion operation is called POP operation.

* This follows a principle FIFO [First In Last Out] or LIFO [Last In, First Out].

* Examples:- The common examples of stack are

1. Placing the books in the shelf.
2. Bread Slicer.
3. Moving out of the bench.

4. Stack are :-

Basic Operations

1. PUSH operation
2. POP operation
3. Stack top

PUSH Operation :-

```
Code :-  
if (top == max-1)  
{  
    cout << "Stack Overflow";  
    return;  
}  
else  
{  
    top++;  
    stack[top] = x;  
}
```

Diagram :-

* At a time only one element can be inserted
(or) deleted from the stack.