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## Linear Regression Algorithm:

$$h_0(x) = \theta_0 + \theta_1 x \quad h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \dots + \theta_n x_n$$

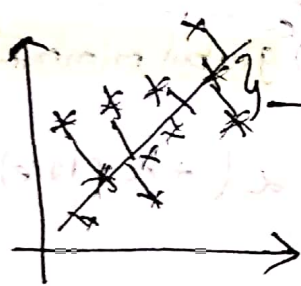
## Convergence Algorithm:

$$J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_0(x^{(i)}) - y^{(i)})^2$$

MSE  $\leftarrow$  cost function

Every observation

Loss function vs cost function



$$\text{Loss function} = (h_0(x^{(i)}) - y^{(i)})^2$$

loss function

$$\hookrightarrow (y_0 - y_{(1)})^2$$

Predicted

Actual

loss function is about <sup>every</sup> single point different.

## derivative:

$$\frac{\partial}{\partial x} (x^2) = 2x$$

$$\frac{\partial}{\partial x} (x)^n = n x^{n-1} (1)$$

$$\frac{\partial}{\partial x} (x+1)^2 = 2x(x+1) \times (1+0) = 2(x+1)$$

$$\frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) = \frac{\partial}{\partial \theta_0} \left[ \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x)^{(i)} - y^{(i)})^2 \right]$$

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

$$j=0 \quad = \frac{\partial}{\partial \theta_0} \left[ \frac{1}{2m} \sum_{i=1}^m \left[ (\theta_0 + \theta_1 x)^{(i)} - y^{(i)} \right]^2 \right]$$

$$= \frac{2}{m} \sum_{i=1}^m \left[ (\theta_0 + \theta_1 x) - y^{(i)} \right] \times (1 + 0)$$

$$j=1 \quad = \frac{\partial}{\partial \theta_1} \left[ \frac{1}{2m} \sum_{i=1}^m \left( \theta_0 + \theta_1 x \right)^{(i)} - y^{(i)} \right]^2$$

$$\frac{2}{m} \sum_{i=1}^m \left[ (\theta_0 + \theta_1 x)^{(i)} - y^{(i)} \right] \times [x]$$

Repeat until convergence:

$$\left\{ \begin{aligned} \theta_0 &:= \theta_0 - L \frac{1}{n} \sum_{i=1}^n (h_\theta(x^{(i)}) - y^{(i)}) \\ \theta_1 &:= \theta_1 - L \frac{1}{n} \sum_{i=1}^n [h_\theta(x^{(i)}) - y^{(i)}] x^{(i)} \end{aligned} \right\}$$

Cost function:

① MSE :- Mean Squared Error

② MAE :- Mean Absolute Error

③ RMSE :- Root Mean Square Error

④ MSE :- Mean Squared Error

$$MSE = \frac{1}{n} \sum_{i=1}^n (y - \hat{y})^2$$

$$\hat{y} = \theta_0 + \theta_1 x$$

↳ predicted value

↓  
quadratic equation

Equation of straight line =  $y = mx + c$

$$ax^2 + by + c = 0$$

↳ quadratic equation

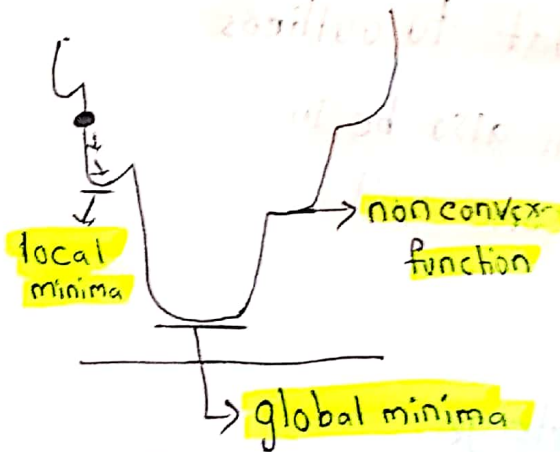
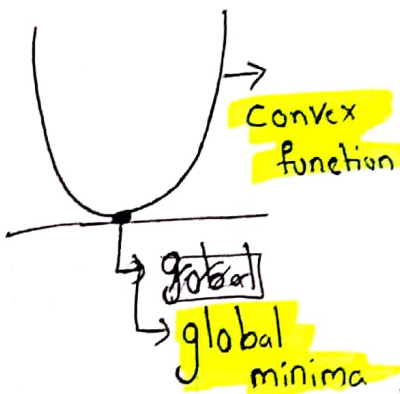


## MSE (Advantages)

this equation is differentiable

This equation also has one global minima

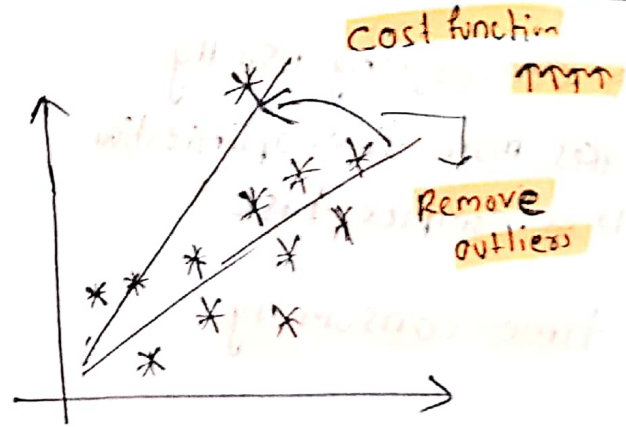
Penalizing  $\Rightarrow$  increasing



## MSE (disadvantage)

this equation is not robust to outliers

Penalizing the error changing the size



$$(y - y^A)^2$$

Exp Salary (lacks) (INR) dependent independent

lacks lacks  
Salary - Predicted Salary)<sup>2</sup>  
Error (lacks)<sup>2</sup>  
unit changing

$$MSE \Rightarrow \sum_{i=1}^n (y - y^A)^2$$

$$(y - y^A)^2 \Rightarrow \text{lacks}$$

Error  $\rightarrow$  squared  $\rightarrow$  Error  
increasing (penalized)

cost function should

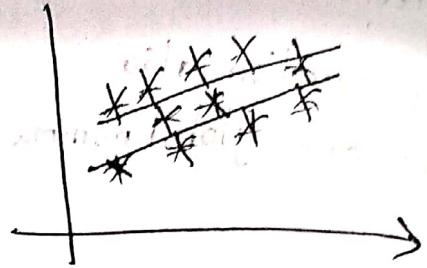
## ② Mean Absolute Error :- (MAE)

$$MAE = \frac{1}{n} \sum_{i=1}^n |y - \hat{y}|$$

### Advantage:

⇒ Robust to outliers

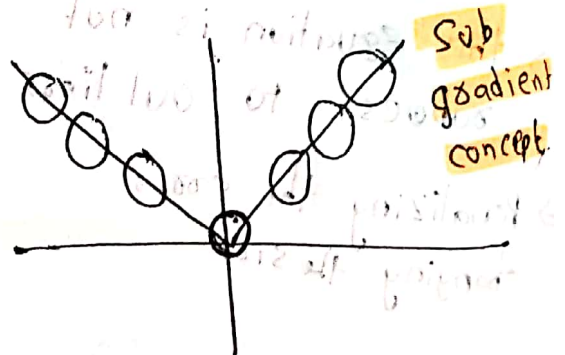
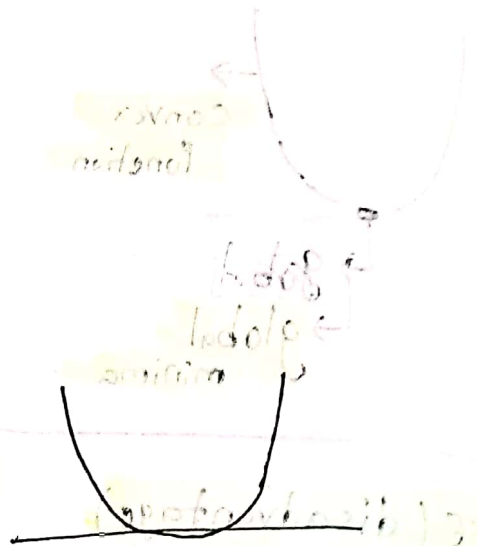
⇒ It will also be in the same unit.



### Disadvantage:

⇒ Converging usually takes more time. Optimization is a complex task

⇒ time consuming



We cannot find the

derivative when it is

0

We can find derivative

by using sub gradient

Sub-gradient means

you have to take a region of a part and divide that region and find



## Performance matrices:

- R Squared
- Adjusted R Squared

## Loss function

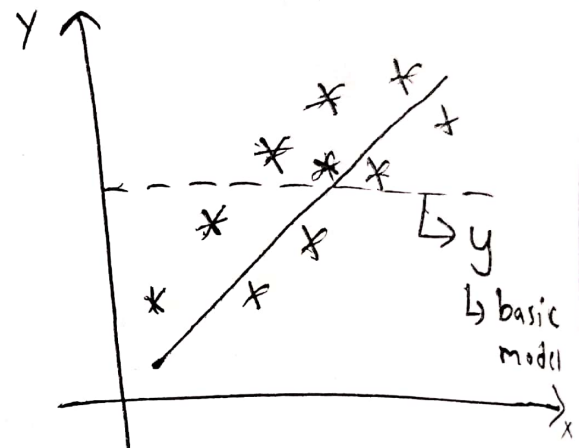
- MAE
- MSE
- RMSE
- Huber loss

## R-Squared:

$$R\text{-Squared} = \frac{1 - SS_{\text{res}}}{1 - SS_{\text{total}}}$$

$SS_{\text{res}}$  = Sum of square residuals

$SS_{\text{total}}$  = Sum of square Average



$\bar{y}$  = Average of y

$$= 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2 \rightarrow \text{low value}}{\sum_{i=1}^n (y_i - \bar{y})^2 \rightarrow \text{high value}}$$

$$R\text{-Squared} = 1 - \left\{ \frac{\text{Small number}}{\text{Bigger number}} \right\} \rightarrow \text{Small number}$$

$$= 0.85$$

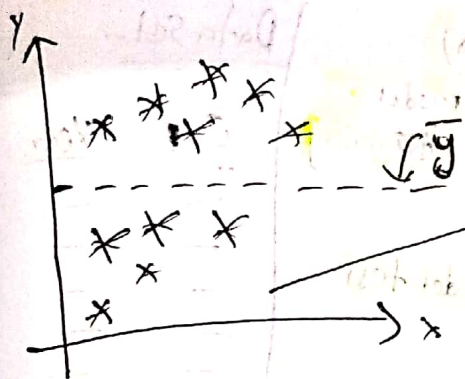
→ 85% accuracy

$$= 0.75 \rightarrow$$

Perf

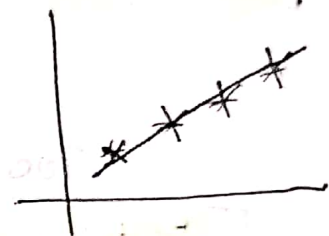
# Performance of the model that you have created

$R^2$  squared (-ve)



$R^2 = -ve$

$R^2 = 1$



$\bar{y}$  = average of y  
y Point

⇒ Adjusted R-squared:

{over fitting & under fitting}

Size of house

city location

No. of bedroom

Gender

Price

$$\text{Adjusted } R^2 = 1 - \frac{(1 - R^2)(N - 1)}{N - P - 1}$$

[2.1.1.1]

[N - P - 1]

$R^2$  65%

$R^2$  75%

$R^2$  88%

$R^2$  90%

⇒ No

$N$  = NO of data Point

$P$  = NO of Independent feature

We use adjusted R-squared.

Adj  $R^2$  = 63%  $P=1$

Adj  $R^2$  = 73%  $P=2$

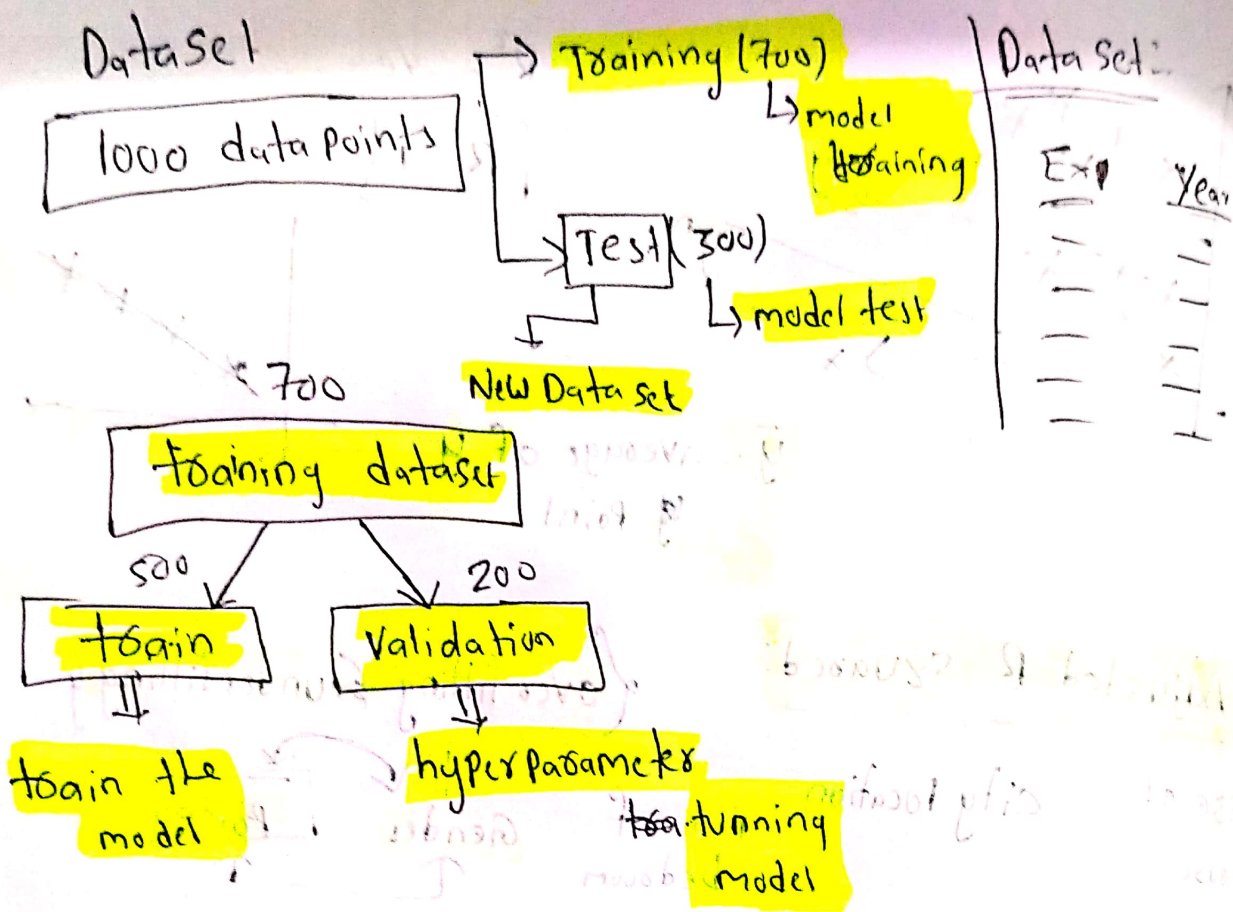
Adj  $R^2$  = 88%  $P=3$

Adj  $R^2$  = 85%





# Overfitting & Underfitting: (Bias and Variance)



model

Train Data | Very good Accuracy (90%) [Low Bias]

Test Data | Very good Accuracy (85%) [Low Variance]

→ Generalized model

Training data | Very good accuracy [90%] [Low Bias]

Test Data | Bad Accuracy (50%) [High Variance]

⇓  
Overfitting

to fix it  
we need from  
hyperparameter  
tuning





Model accuracy is low [High bias]

Model Accuracy is low/high [low or high Variance]

⇓  
model is under fitting

