P1:

Let X be a d.r.v. with p.m.f given by

$$p(x) = \begin{cases} \frac{1}{3}, x = 0 \\ \frac{2}{3}, x = 2 \end{cases}$$

Find the mean and variance of X.

Solution:

Here
$$p(0) = \frac{1}{3}$$
 and $p(2) = \frac{2}{3}$

Then

$$E(X) = \sum_{x} x p(x) = 0 \times \frac{1}{3} + 2 \times \frac{2}{3} = \frac{4}{3}$$

and

$$E(X^2) = \sum_{x} x^2 p(x) = 0^2 \times \frac{1}{3} + 2^2 \times \frac{2}{3} = \frac{8}{3}$$

$$\therefore V(X) = E(X^2) - (E(X))^2 = \frac{8}{3} - \frac{16}{9} = \frac{8}{9}$$

Thus, mean is equal to $\frac{4}{3}$ and variance is equal to $\frac{8}{9}$.