

Intro to Cryptography

CSE 405 July 2023
Lecture 2

The clouds come and go,
providing a rest for all
the moon viewers.

— Matsuo Bashō —



What is cryptography?

Textbook Chapter 5.1

What is cryptography?

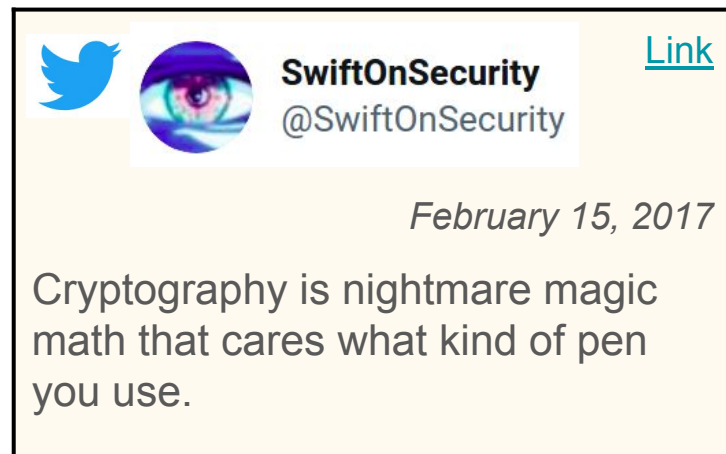
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- Older definition: The study of secure communication over insecure channels
- Newer definition: Provide rigorous guarantees on the security of data and computation in the presence of an attacker
 - Not just *confidentiality* but also *integrity* and *authenticity* (we'll see these definitions today)
- Modern cryptography involves a lot of math
 - Finite field theory
 - Number theory

Don't try this at home (Except for Assignment 1)!

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- We will teach you the basic building blocks of cryptography, but you should never try to write your own cryptographic algorithms
- It's very easy to make a mistake that makes your code insecure
 - Lots of tricky edge cases that we won't cover
 - One small bug could compromise the security of your code
- Instead, use existing well-vetted cryptographic libraries
 - This portion of the class is as much about making you a good *consumer* of cryptography



Don't try this at home!

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- In summer 2020, CS 61A wrote a program to distribute online exams
- However, when writing cryptographic code, they used a secure algorithm in an insecure way
- Because of their mistake, it was possible to see exam questions before they were released!
 - Later in the semester, you'll get to try and break their insecure scheme yourself
 - Exam leakage was reported, but we never found out if anyone actually attacked the insecure scheme
- The TAs who wrote this code were former CS 161 students!
- **Takeaway:** Do not write your own crypto code!

Definitions

Textbook Chapter 5.3–5.9

Meet Alice, Bob, Eve, and Mallory

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- Alice and Bob: The main characters trying to send messages to each other over an insecure communication channel
 - Carol and Dave can also join the party later
- Eve: An **eavesdropper** who can read any data sent over the channel
- Mallory: A **manipulator** who can read and modify any data sent over the channel



Meet Alice, Bob, Eve, and Mallory

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<https://cryptocouple.com/>



Meet Alice, Bob, Eve, and Mallory

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- We often describe cryptographic problems using a common cast of characters
- One scenario:
 - Alice wants to send a message to Bob.
 - However, Eve is going to *eavesdrop* on the communication channel.
 - How does Alice send the message to Bob without Eve learning about the message?
- Another scenario:
 - Bob wants to send a message to Alice.
 - However, Mallory is going to *tamper* with the communication channel.
 - How does Bob send the message to Alice without Mallory changing the message?

Three Goals of Cryptography (CIA)

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- In cryptography, there are three main properties that we want on our data
- **Confidentiality**: An adversary cannot *read* our messages.
- **Integrity**: An adversary cannot *change* our messages without being detected.
- **Authenticity**: I can prove that this message came from the person who claims to have written it.
 - Integrity and authenticity are closely related properties...
 - Before I can prove that a message came from a certain person, I have to prove that the message wasn't changed!
 - ... but they're not identical properties
 - Later we'll see some edge cases

Keys

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- The most basic building block of any cryptographic scheme: The **key**
- We can use the key in our algorithms to secure messages
- Two models of keys:
 - **Symmetric key model:** Alice and Bob both know the value of the same secret key.
 - **Asymmetric key model:** Everybody has two keys, a secret key and a public key.
 - Example: The famous RSA encryption algorithm



Security Principle: Kerckhoff's Principle

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- This principle is closely related to Shannon's Maxim
 - Don't use security through obscurity. Assume the attacker knows the system.
- Kerckhoff's principle says:
 - Cryptosystems should remain secure even when the attacker knows all internal details of the system. The security of a cryptographic system shouldn't rely on the secrecy of the algorithm
 - The key should be the only thing that must be kept secret
 - The system should be designed to make it easy to change keys that are leaked (or suspected to be leaked)
 - If your secrets are leaked, it is usually a lot easier to change the key than to replace every instance of the running software
- Our assumption: The attacker knows all the algorithms we use. The only information the attacker is missing is the secret key(s).

Effective Key Management

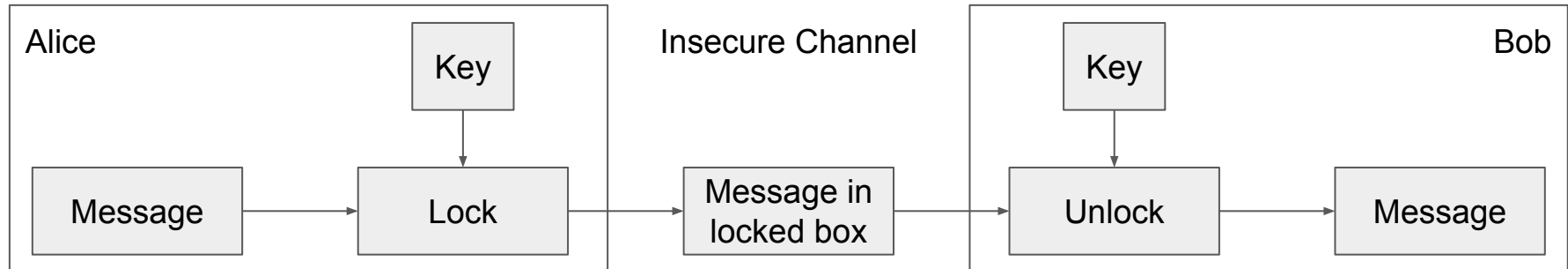
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- The secret key must be stored and transmitted in a secure manner because disclosure of the secret key makes the data unsecured.
- The longer the same key is in use, the easier it becomes to crack the key. Thus, the key must be changed from time to time.
- The key must be generated randomly, so that it is hard for any attacker to guess it. The higher the randomness of the key is, higher will be the quality of the key, making it progressively more difficult to guess it.
- If the length of the key is short, its lifetime must also be short. That is, a short key must not be used for a longer period of time.
- The key must be destroyed properly after its use.

Confidentiality

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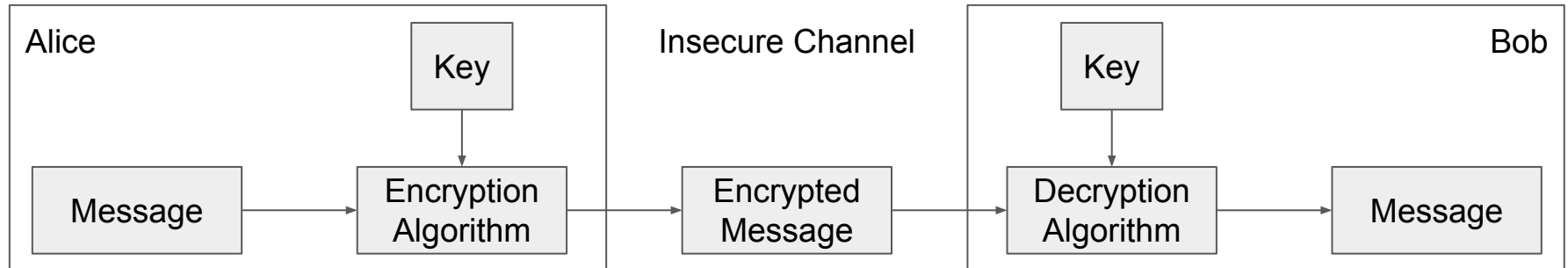
- **Confidentiality:** An adversary cannot *read* our messages.
- **Analogy:** Locking and unlocking the message
 - Alice uses the key to lock the message in a box
 - Alice sends the message (locked in the box) over the insecure channel
 - Eve sees the locked box, but cannot access the message without the key
 - Bob receives the message (locked in the box) and uses the key to unlock the message



Confidentiality

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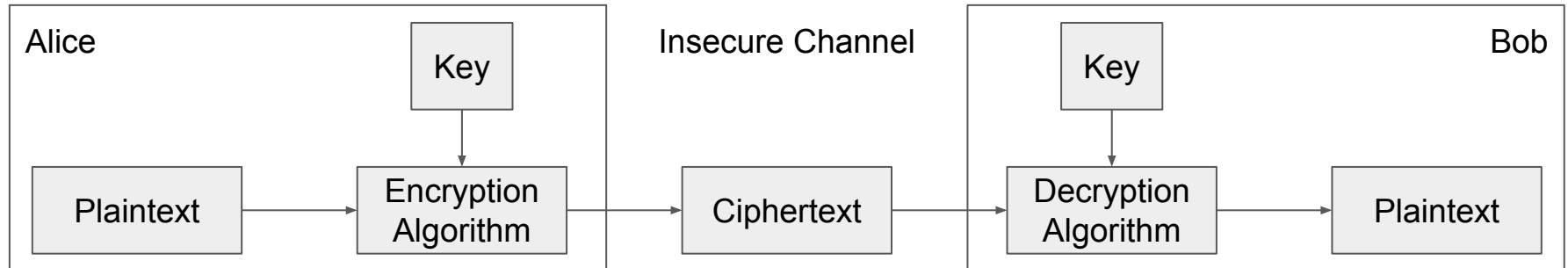
- Schemes provide confidentiality by **encrypting** messages
 - Alice uses the key to **encrypt** the message: Change the message into a scrambled form
 - Alice sends the encrypted message over the insecure channel
 - Eve sees the encrypted message, but cannot figure out the original message without the key
 - Bob receives the encrypted message and uses the key to **decrypt** the message back into its original form



Confidentiality

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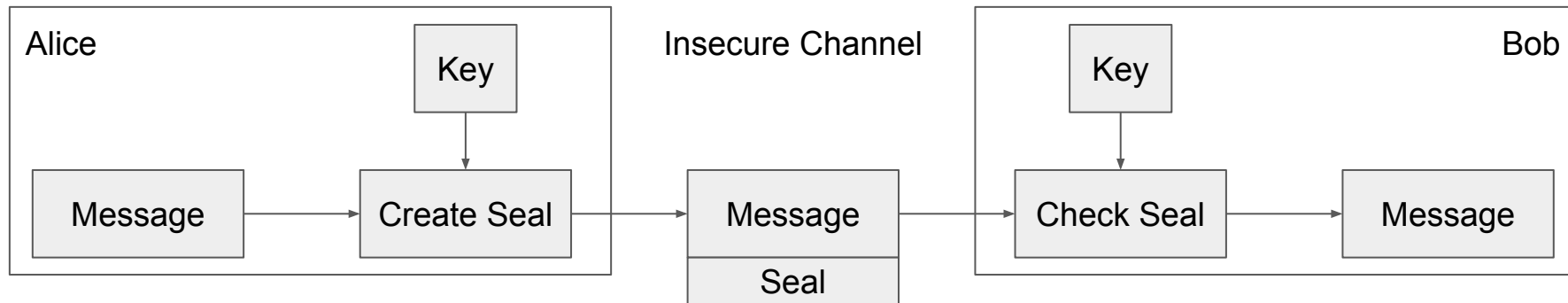
- **Plaintext:** The original message
- **Ciphertext:** The encrypted message



Integrity (and Authenticity)

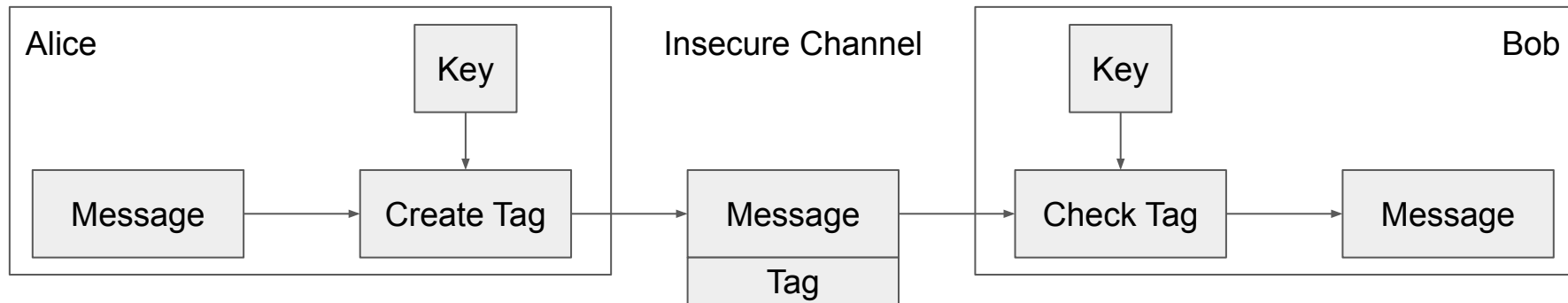
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- **Integrity:** An adversary cannot *change* our messages without being detected.
- **Analogy:** Adding a seal on the message
 - Alice uses the key to add a special seal on the message (e.g. puts tape on the envelope)
 - Alice sends the message and the seal over the insecure channel
 - If Mallory tampers with the message, she'll break the seal (e.g. break the tape on the envelope)
 - Without the key, Mallory cannot create her own seal
 - Bob receives the message and the seal and checks that the seal has not been broken



Integrity (and Authenticity)

- Schemes provide integrity by adding a **tag** or **signature** on messages
 - Alice uses the key to generate a special tag for the message
 - Alice sends the message and the tag over the insecure channel
 - If Mallory tampers with the message, the tag will no longer be valid
 - Bob receives the message and the tag and checks that the tag is still valid
- More on integrity in a future lecture



Integrity Real Life Example

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- Cryptographic hash functions are like digital signatures – they ensure data hasn't been tampered with



Threat Models

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- What if Eve can do more than eavesdrop?
- Real-world schemes are often vulnerable to more sophisticated attackers, so cryptographers have created more sophisticated threat models too
- Some threat models for analyzing confidentiality:

	Can Eve trick Alice into encrypting messages of Eve's choosing?	Can Eve trick Bob into decrypting messages of Eve's choosing?
Ciphertext-only	No	No
Chosen-plaintext	Yes	No
Chosen-ciphertext	No	Yes
Chosen plaintext-ciphertext	Yes	Yes

Threat Models

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- In this class, we'll use the chosen plaintext attack model
- In practice, cryptographers use the chosen plaintext-ciphertext model
 - It's the most powerful
 - It can actually be defended against

	Can Eve trick Alice into encrypting messages of Eve's choosing?	Can Eve trick Bob into decrypting messages of Eve's choosing?
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Cryptography Roadmap

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	Symmetric-key	Asymmetric-key
Confidentiality	<ul style="list-style-type: none">• One-time pads• Block ciphers with chaining modes (e.g. AES-CBC)• Stream ciphers	<ul style="list-style-type: none">• RSA encryption• ElGamal encryption• ECC
Integrity, Authentication	<ul style="list-style-type: none">• MACs (e.g. HMAC)	<ul style="list-style-type: none">• Digital signatures (e.g. RSA signatures)

- Hash functions
- Pseudorandom number generators
- Public key exchange (e.g. Diffie-Hellman)
- Key management (certificates)
- Password management

Symmetric-Key Encryption



Textbook Chapter 6.1

Cryptography Roadmap

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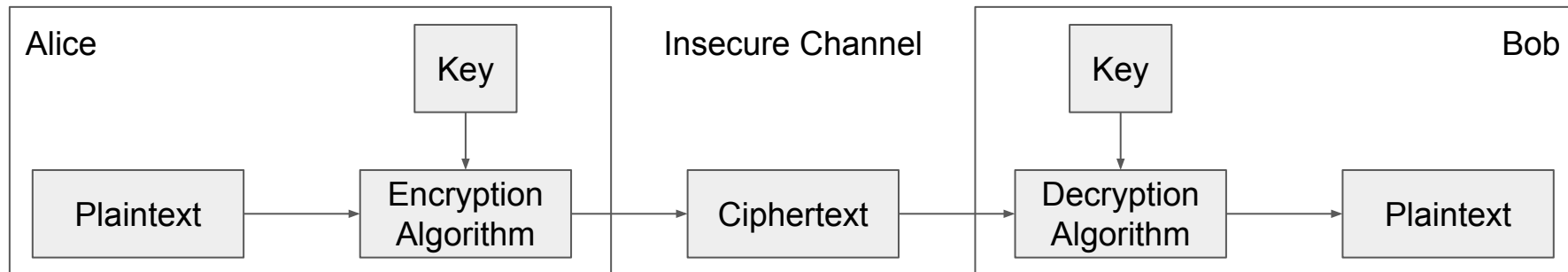
Symmetric-Key Encryption

- The next few schemes are symmetric-key encryption schemes
 - **Encryption schemes** aim to provide *confidentiality* (but not integrity or authentication)
 - **Symmetric-key** means Alice and Bob share the same secret key that the attacker doesn't know
 - Don't worry about how Alice and Bob share the key for now
- For modern schemes, we're going to assume that messages are *bitstrings*
 - **Bitstring**: A sequence of bits (0 or 1), e.g. 11010101001001010
 - Text, images, etc. can usually be converted into bitstrings before encryption, so bitstrings are a useful abstraction. After all, everything in a computer is just a sequence of bits!

Symmetric-Key Encryption: Definition

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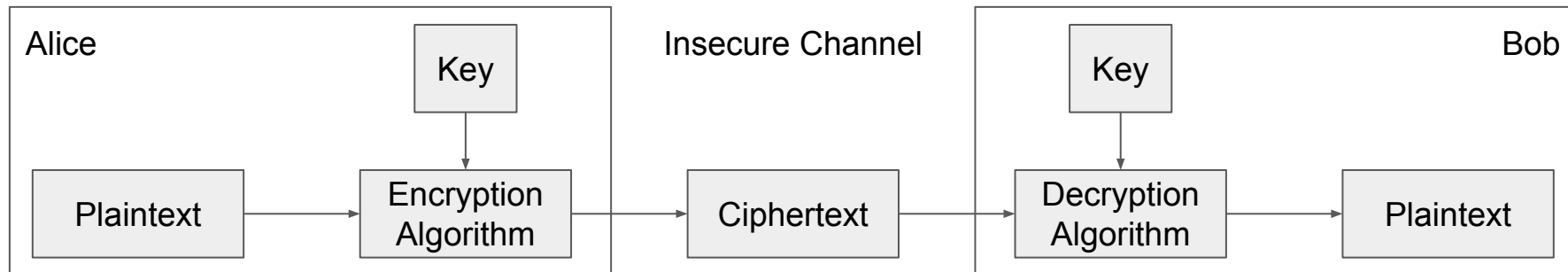
- A symmetric-key encryption scheme has three algorithms:
 - $\text{KeyGen}() \rightarrow K$: Generate a key K
 - $\text{Enc}(K, M) \rightarrow C$: Encrypt a **plaintext** M using the key K to produce **ciphertext** C
 - $\text{Dec}(K, C) \rightarrow M$: Decrypt a ciphertext C using the key K



Symmetric-Key Encryption: Definition

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- What properties do we want from a symmetric encryption scheme?
 - **Correctness:** Decrypting a ciphertext should result in the message that was originally encrypted
 - $\text{Dec}(K, \text{Enc}(K, M)) = M$ for all $K \leftarrow \text{KeyGen}()$ and M
 - **Efficiency:** Encryption/decryption algorithms should be fast: >1 Gbps on a standard computer
 - **Security:** Confidentiality



Defining Confidentiality

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- Recall our definition of confidentiality from earlier: “An adversary cannot read our messages”
 - This definition isn’t very specific
 - What if Eve can read the first half of Alice’s message, but not the second half?
 - What if Eve figures out that Alice’s message starts with “Dear Bob”?
 - This definition doesn’t account for prior knowledge
 - What if Eve already knew that Alice’s message ends in “Sincerely, Alice”?
 - What if Eve knows that Alice’s message is “BUY!” or “SELL” but doesn’t know which?



Defining Confidentiality

- A better definition of confidentiality: The ciphertext should not give the attacker *any additional information* about the plaintext.
- Let's design an experiment/security game to test our definition:
 - Eve chooses two messages M_0 and M_1 of the same length
 - Alice chooses one message at random M_b , encrypts it, and sends the ciphertext
 - Eve knows either M_0 or M_1 was sent, but doesn't know which
 - Eve reads the ciphertext and tries to guess which message was sent
 - If the probability that Eve correctly guesses which message was sent is $1/2$, then the encryption scheme is confidential
- Intuition
 - If the scheme is confidential, Eve can only guess with probability $1/2$, which is no different than if Eve hadn't sent the ciphertext at all
 - In other words: the ciphertext gave Eve no *additional* information about which plaintext was sent!

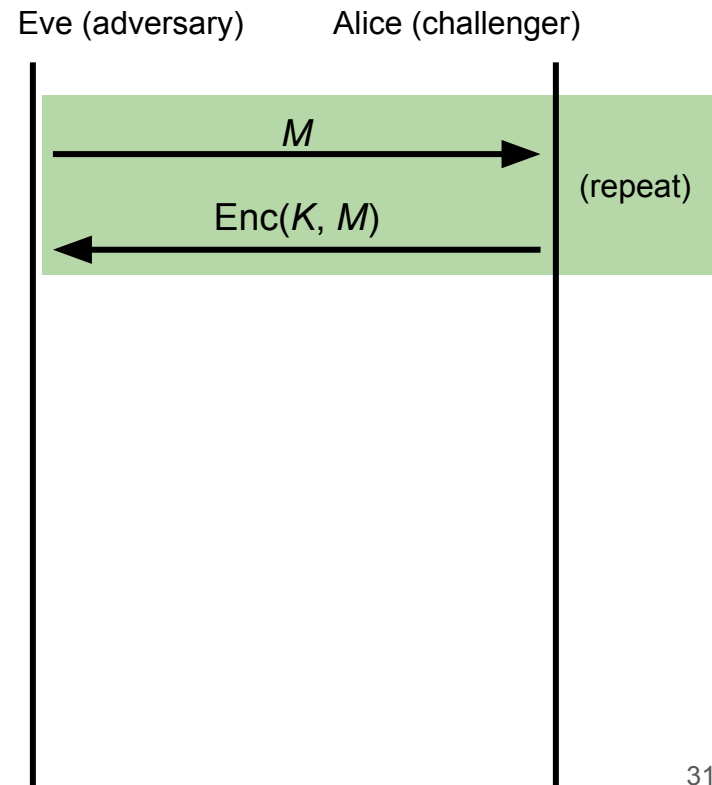
Defining Confidentiality: IND-CPA

- Recall our threat model: Eve can also perform a **chosen plaintext attack**
 - Eve can trick Alice into encrypting arbitrary messages of Eve's choice
 - We can adapt our experiment to account for this threat model
- A better definition of confidentiality: Even if Eve is able to trick Alice into encrypting messages, Eve can still only guess what message Alice sent with probability $1/2$.
 - This definition is called **IND-CPA** (indistinguishability under chosen plaintext attack)
- Cryptographic properties are often defined in terms of “games” that an adversary can either “win” or “lose”
 - We will use one to define confidentiality precisely

Defining Confidentiality: IND-CPA

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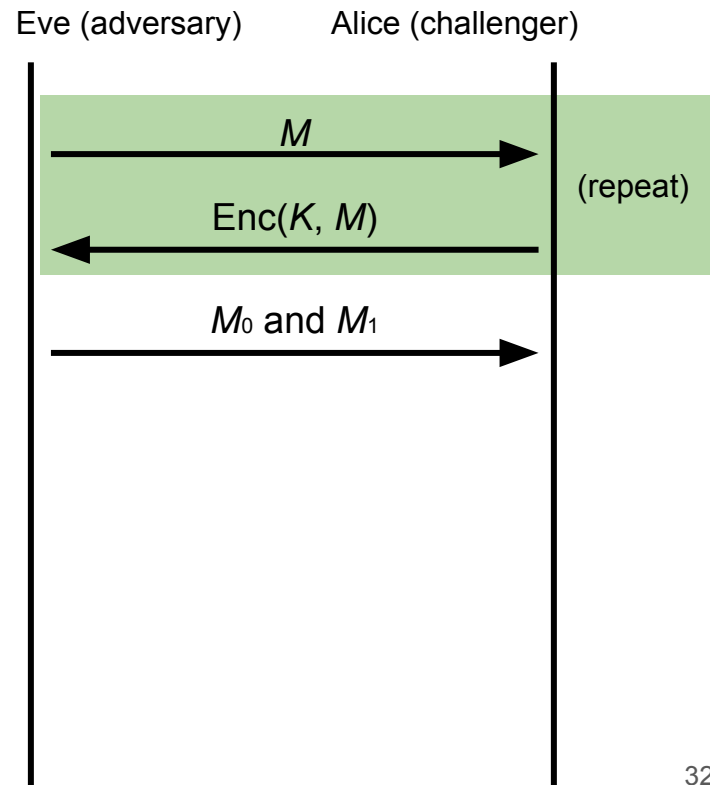
1. Eve may choose plaintexts to send to Alice and receives their ciphertexts



Defining Confidentiality: IND-CPA

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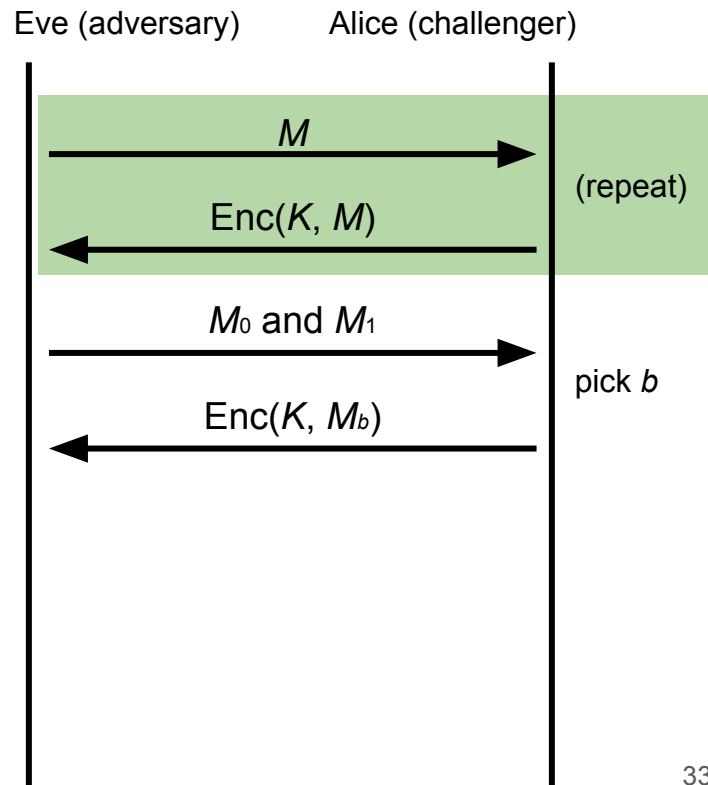
1. Eve may choose plaintexts to send to Alice and receives their ciphertexts
2. Eve issues a pair of plaintexts M_0 and M_1 to Alice



Defining Confidentiality: IND-CPA

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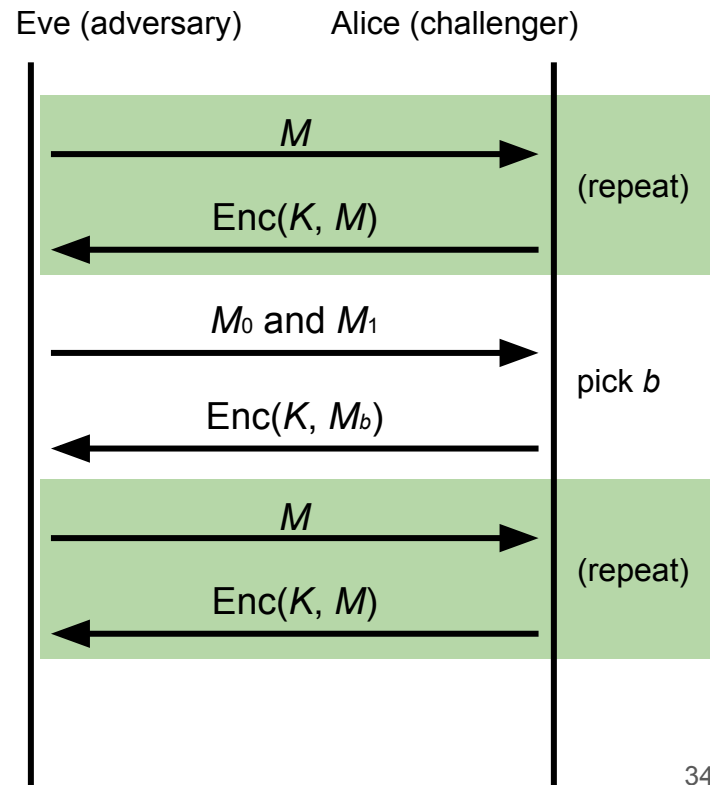
1. Eve may choose plaintexts to send to Alice and receives their ciphertexts
2. Eve issues a pair of plaintexts M_0 and M_1 to Alice
3. Alice randomly chooses either M_0 or M_1 to encrypt and sends the encryption back
 - a. Alice does not tell Eve which one was encrypted!



Defining Confidentiality: IND-CPA

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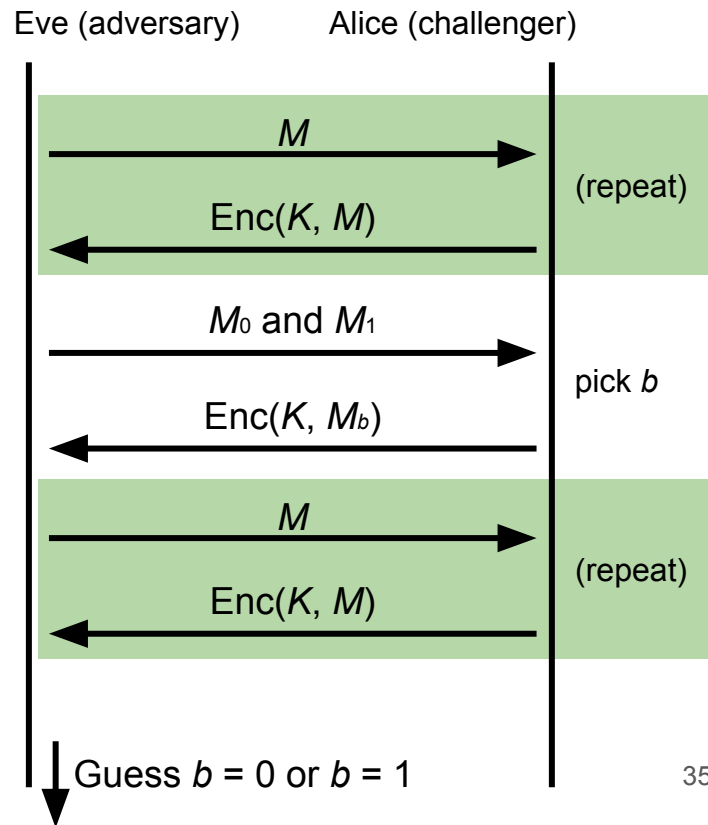
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3. Alice randomly chooses either M_0 or M_1 to encrypt and sends the encryption back
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4. Eve may again choose plaintexts to send to Alice and receives their ciphertexts



Defining Confidentiality: IND-CPA

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1. Eve may choose plaintexts to send to Alice and receives their ciphertexts
2. Eve issues a pair of plaintexts M_0 and M_1 to Alice
3. Alice randomly chooses either M_0 or M_1 to encrypt and sends the encryption back
 - a. Alice does not tell Eve which one was encrypted!
4. Eve may again choose plaintexts to send to Alice and receives their ciphertexts
5. Eventually, Eve outputs a guess as to whether Alice encrypted M_0 or M_1



Defining Confidentiality: IND-CPA

- If Eve correctly guesses which message Alice encrypted, then Eve wins. Otherwise, she loses.
- How does Eve guess whether M_0 or M_1 was encrypted? What strategy does she use?
 - We don't *assume* she uses a particular strategy; Eve represents all possible strategies
- Proving insecurity: There exists at least *one* strategy that can win the IND-CPA game with probability $> 1/2$
 - $1/2$ is the probability of winning by random guessing
 - If you can be better than random, then the ciphertext has leaked information, and Eve is able to learn it and use it to gain an advantage!
- Proving security: For *all* attackers/Eve-s, the probability of winning the IND-CPA game is at most $1/2$

Edge Cases: Length

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- Cryptographic schemes are (usually) allowed to leak the length of the message
 - To hide length: All messages must always be the same length
 - 16-byte messages: We can't encrypt large messages (images, videos, etc.)!
 - 1-GB messages: Sending small messages (text, Tweets, etc.) needs 1 GB of bandwidth!
 - This is impractical
 - Applications that which to hide length must choose to *pad* their own messages to the maximum possible length before encrypting
- In the IND-CPA game: M_0 and M_1 must be the same length
 - To break IND-CPA, Eve must learn something other than message length



Edge Cases: Attacker Runtime

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- Some schemes are theoretically vulnerable, but secure in any real-world setting
 - If an attack takes longer than the life of the solar system to complete, it probably won't happen!
 - Or if it would require a computer made out of a literal galaxy worth of science-fiction nanotech
- In the IND-CPA game: Eve is limited to a practical runtime
 - One common practical limit: Eve is limited to polynomial runtime algorithms (no exponential-time algorithms)



Edge Cases: Negligible Advantage

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- Sometimes it's possible for Eve to win with probability $1/2 + 1/2^{128}$
 - This probability is greater than $1/2$, but it's so close to $1/2$ that it's as good as $1/2$.
 - Eve's advantage is so small that she can't use it for any practical attacks
- In the IND-CPA game: The scheme is secure even if Eve can win with probability $\leq 1/2 + \epsilon$, where ϵ is *negligible*
 - The actual mathematical definition of negligible is out of scope
 - Example: $1/2 + 1/2^{128}$: Negligible advantage
 - Example: $2/3$: Non-negligible advantage



Edge Cases: Negligible Advantage

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- Defining negligibility mathematically:
 - Advantage of the adversary should be exponentially small, based on the security parameters of the algorithm
 - Example: For an encryption scheme with a k -bit key, the advantage should be $O(1/2^k)$
- Defining negligibility practically:
 - A $1/2^{128}$ probability is completely inconceivable
 - A $1/2^{20}$ probability is fairly likely
 - “One in a million events happen every day in New York City”
 - In between these extremes, it can be messy
 - Different algorithms run faster or slower and have their own security parameters
 - Computers get more powerful over time
 - Recall: Know your threat model!
- **Takeaway:** For now, 2^{80} is a reasonable threshold, but this will change over time!

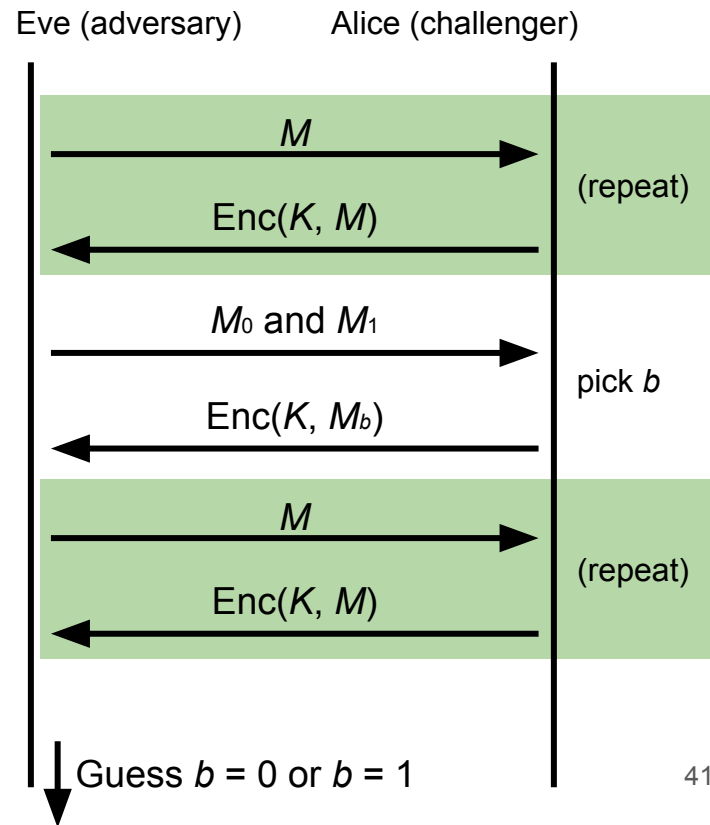
IND-CPA: Putting it together

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1. Eve may choose plaintexts to send to Alice and receives their ciphertexts
2. Eve issues a pair of plaintexts M_0 and M_1 to Alice
3. Alice randomly chooses either M_0 or M_1 to encrypt and sends the encryption back
 - Alice does not tell Eve which one was encrypted!
4. Eve may again choose plaintexts to send to Alice and receives their ciphertexts
5. Eventually, Eve outputs a guess as to whether Alice encrypted M_0 or M_1



- An encryption scheme is IND-CPA secure if for all polynomial time attackers Eve:
 - Eve can win with probability $\leq 1/2 + \epsilon$, where ϵ is *negligible*.



A Brief History of Cryptography



Textbook Chapter 5.2

Cryptography by Hand: Caesar Cipher

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- One of the earliest cryptographic schemes was the **Caesar cipher**
 - Used by Julius Caesar over 2,000 years ago
- **KeyGen():**
 - Choose a key K randomly between 0 and 25
- **Enc(K, M):**
 - Replace each letter in M with the letter K positions later in the alphabet
 - If $K = 3$, plaintext DOG becomes GRJ
- **Dec(K, C):**
 - Replace each letter in C with the letter K positions earlier in the alphabet
 - If $K = 3$, ciphertext GRJ becomes DOG

$K = 3$			
M	C	M	C
A	D	N	Q
B	E	O	R
C	F	P	S
D	G	Q	T
E	H	R	U
F	I	S	V
G	J	T	W
H	K	U	X
I	L	V	Y
J	M	W	Z
K	N	X	A
L	O	Y	B
M	P	Z	C

Cryptography by Hand: Attacks on the Caesar Cipher

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- Eve sees the ciphertext JCKN ECGUCT, but doesn't know the key K
- If you were Eve, how would you try to break this algorithm?
- Brute-force attack: Try all 26 possible keys!
- Use existing knowledge: Assume that the message is in English

+1 IBJM DBFTBS

+2 HAIL CAESAR

+3 GZHK BZDRZQ

+4 FYGJ AYCQYP

+5 EXFI ZXBPXO

+6 DWEH YWAOWN

+7 CVDG XVZNVN

+8 BUCF WUYMUL

+9 ATBE VTXLTK

+10 ZSAD USWKSJ

+11 YRZC TRVJRI

+12 XQYB SQUIQH

+13 WPXA RPTHPG

+14 VOWZ QOSGOF

+15 UNVY PNRFNE

+16 TMUX OMQEMD

+17 SLTW NLPDLC

+18 RKSV MKOCKB

+19 QJRU LJNBJA

+20 PIQT KIMAIZ

+21 OHPS JHLZHY

+22 NGOR IGKYGX

+23 MFNQ HFJXFW

+24 LEMP GEIWEV

+25 KDLO FDHVDU

Cryptography by Hand: Attacks on the Caesar Cipher

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- Eve sees the ciphertext JCKN ECGUCT, but doesn't know the key K
- Chosen-plaintext attack: Eve tricks Alice into encrypting plaintext of her choice
 - Eve sends a message $M = \text{AAA}$ and receives $C = \text{CCC}$
 - Eve can deduce the key: C is 2 letters after A, so $K = 2$
 - Eve has the key, so she can decrypt the ciphertext

Cryptography by Hand: Substitution Cipher

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- A better cipher: create a mapping of each character to another character.
 - Example: $A = N$, $B = Q$, $C = L$, $D = Z$, etc.
 - Unlike the Caesar cipher, the shift is no longer constant!
- **KeyGen():**
 - Generate a random, one-to-one mapping of characters
- **Enc(K, M):**
 - Map each letter in M to the output according to the mapping K
- **Dec(K, C):**
 - Map each letter in C to the output according to the *reverse* of the mapping K

K			
M	C	M	C
A	N	N	G
B	Q	O	P
C	L	P	T
D	Z	Q	A
E	K	R	J
F	R	S	O
G	V	T	D
H	U	U	I
I	E	V	C
J	S	W	F
K	B	X	M
L	W	Y	X
M	Y	Z	H

Cryptography by Hand: Attacks on Substitution Ciphers

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- Does the brute-force attack still work?
 - There are $26! \approx 2^{88}$ possible mappings to try
 - Too much for most modern computers... for now
- How about the chosen-plaintext attack?
 - Trick Alice into encrypting ABCDEFGHIJKLMNOPQRSTUVWXYZ, and you'll get the whole mapping!
- Another strategy: *cryptanalysis*
 - The most common english letters in text are E, T, A, O, I, N

K			
M	C	M	C
A	N	N	G
B	Q	O	P
C	L	P	T
D	Z	Q	A
E	K	R	J
F	R	S	O
G	V	T	D
H	U	U	I
I	E	V	C
J	S	W	F
K	B	X	M
L	W	Y	X
M	Y	Z	H

Takeaways

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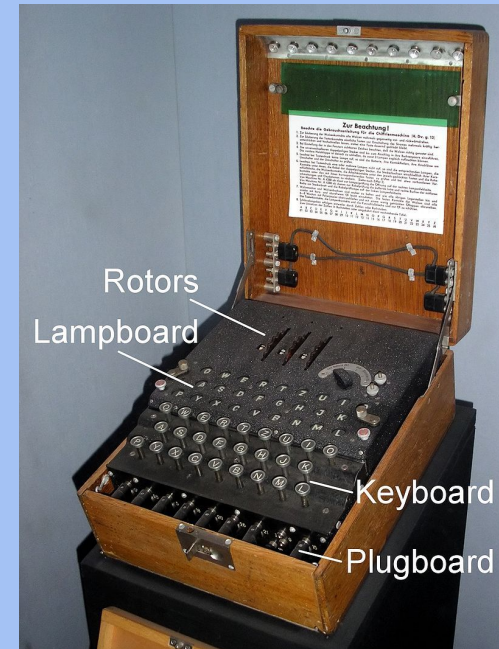
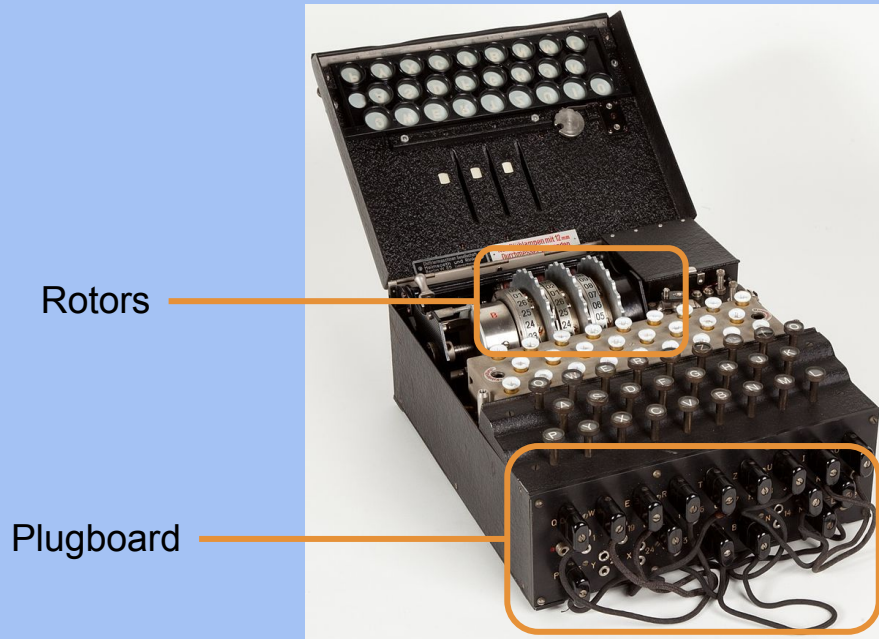
- Cryptography started with paper-and-pencil algorithms (Caesar cipher)
- Then cryptography moved to machines (Enigma)
- Finally, cryptography moved to computers (which we're about to study)
- Hopefully you gained some intuition for some of the cryptographic definitions



Cryptography by Machines: Enigma [\(View Here\)](#)

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- A mechanical encryption machine used by the Germans in WWII



Enigma Operating Principle: Rotor Machine

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- The encryption core was composed of 3 or 4 rotors
 - Each rotor was a fixed permutation (e.g. A maps to F, B maps to Q...)
 - And the end was a "reflector", a rotor that sent things backwards
 - Plus a fixed-permutation plugboard
- A series of rotors were arranged in a sequence
 - Each keypress would generate a current from the input to one light for the output
 - Each keypress also advanced the first rotor
 - When the first rotor makes a full rotation, the second rotor advances one step
 - When the second rotor makes a full rotation, the third rotor advances once step

Cryptography by Machines: Enigma

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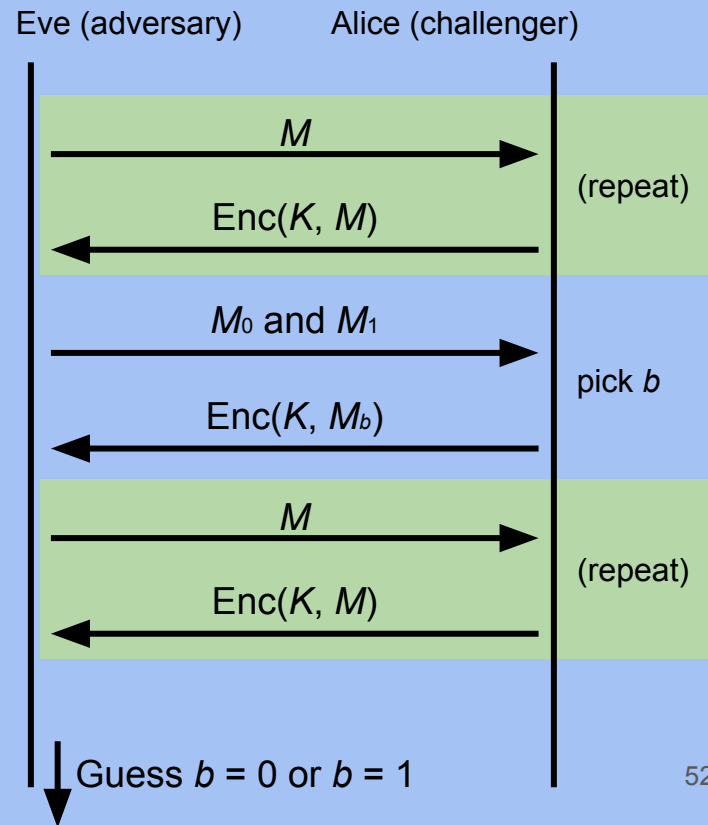
- **KeyGen():**
 - Choose rotors, rotor orders, rotor positions, and plugboard settings
 - 158,962,555,217,826,360,000 possible keys
- **Enc(K , M) and Dec(K , C):**
 - Input the rotor settings K into the Enigma machine
 - Press each letter in the input, and the lampboard will light up the corresponding output letter
 - Encryption and decryption are the same algorithm!
- Germans believed that Enigma was an “unbreakable code”



Cryptography by Machines: Enigma

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- Enigma has a significant weakness: a letter never maps to itself
 - No rotor maps a letter to itself
 - The reflector never maps a letter to itself
 - This property is necessary for Enigma's mechanical system to work
- What pair of messages should Eve send to Alice in the challenge phase?
 - Send $M_0 = A^k$, $M_1 = B^k$
 - M_0 is a string of k 'A' characters, M_1 is a string of k 'B' characters
- How can Eve probably know which message Alice encrypted?
 - If there are no 'A' characters, it was M_0
 - If there are no 'B' characters, it was M_1



Cryptography by Machines: Attack on Enigma

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- Polish and British cryptographers built BOMBE, a machine to brute-force Enigma keys
- Why was Enigma breakable?
 - Kerckhoff's principle: The Allies stole Enigma machines, so they knew the algorithm
 - Known plaintext attacks: the Germans often sent predictable messages (e.g. the weather report every morning)
 - Chosen plaintext attacks: the Allies could trick the Germans into sending a message (e.g. "newly deployed minefield")
 - Brute-force: BOMBE would try many keys until the correct one was found
 - Plus a weakness: You'd be able to try multiple keys with the same hardware configuration

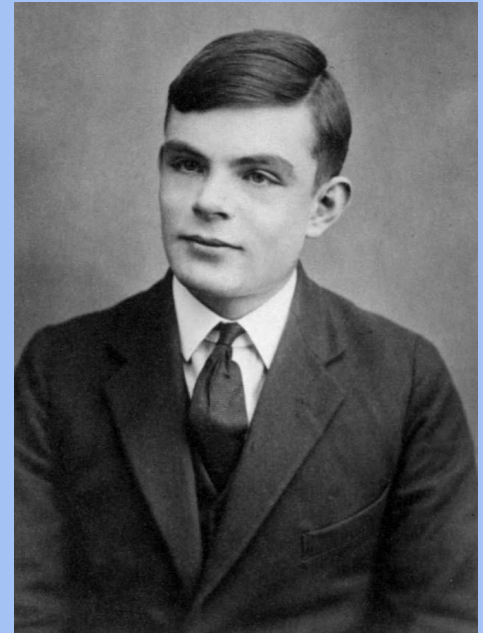


BOMBE machine

Cryptography by Machines: Legacy of Enigma

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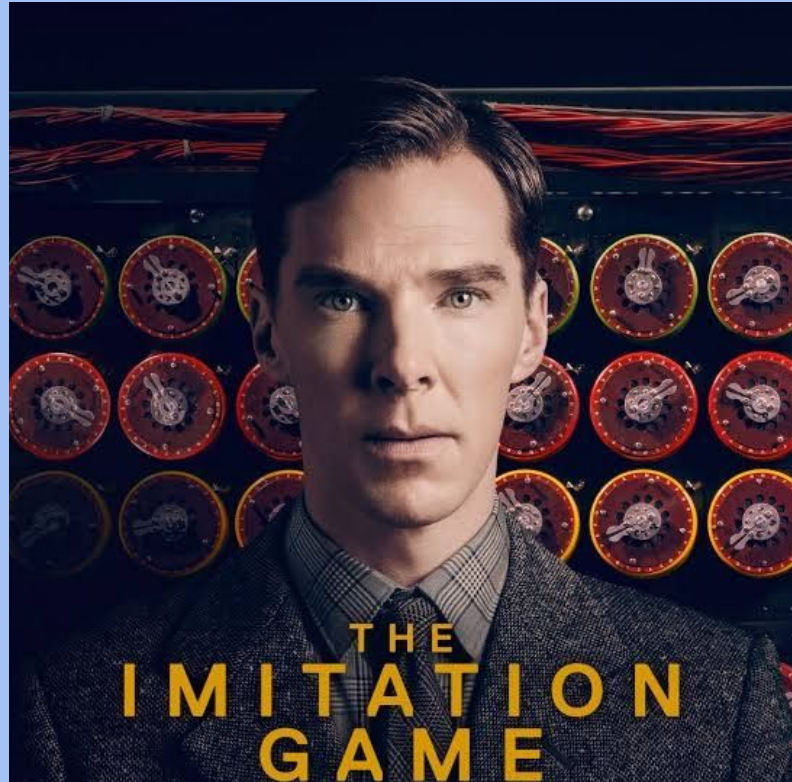
- Alan Turing, one of the cryptographers who broke Enigma, would go on to become one of the founding fathers of computer science
- Most experts agree that the Allies breaking Enigma shortened the war in Europe by about a year



Alan Turing

Cryptography by Machines: Legacy of Enigma

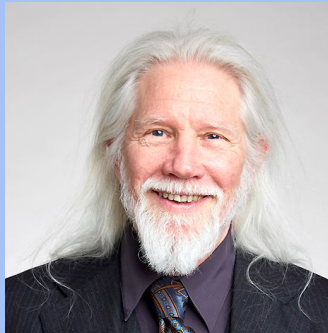
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Cryptography by Computers

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- The modern era of cryptography started after WWII, with the work of Claude Shannon
- “New Directions in Cryptography” (1976) showed how number theory can be used in cryptography
 - Its authors, Whitfield Diffie and Martin Hellman, won the Turing Award in 2015 for this paper
- This is the era of cryptography we’ll be focusing on



One of these is Diffie, and
the other one is Hellman.



Diffusion

- The theory of diffusion and confusion was proposed by Claude Shannon in attempt to thwart cryptanalysis based on statistical analysis.
- Both diffusion and confusion are the essential properties of block ciphers.
- *Diffusion* is based on the idea of hiding the relationship between the ciphertext and plaintext.
 - This will frustrate a cryptanalyst who examines the ciphertext statistics in order to determine the plaintext.
 - To achieve diffusion, a ciphertext symbol must depend on some or all symbols in the plaintext.
 - That is, a change in a single symbol in the plaintext causes change in several or all symbols in the ciphertext.

Confusion

- On the other hand, *confusion* is based on the idea of hiding the relationship between the ciphertext and the key.
 - This will frustrate a cryptanalyst who attempts to determine the key using the ciphertext.
 - To prevent intruders from discovering the key, confusion attempts to make the relationship between the value of encryption key and the statistics of ciphertext as complex as possible.
 - This can be achieved by making sure that a ciphertext symbol depends on some or all symbols of the key used.
 - That is, a change in a single bit of the key causes changes in several or all symbols in the ciphertext.

Unicity Distance

- The minimum number of characters in ciphertext Eve needs to collect to be reasonably sure she can figure out the decryption key or the original plaintext message.
 - If the ciphertext is less than the unicity distance, multiple keys might still make sense.
 - If it's more, only one key fits — so the cipher is cracked.

Summary

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- What's cryptography?
 - Communicating securely over insecure channels
 - You should never write your own crypto! Use existing libraries instead.
- Definitions
 - Alice and Bob want to send messages over an insecure channel. Eve can read anything sent over the insecure channel. Mallory can read or modify anything sent over the insecure channel.
 - We want to ensure confidentiality (adversary can't read message), integrity (adversary can't modify message), and authenticity (prove message came from sender)
 - Crypto uses secret keys. Kerckhoff's principle says to assume the attacker knows the entire system, except the secret keys.
 - There are several different threat models. We'll focus on the chosen plaintext attack, where Eve tricks Alice into encrypting some messages.

Summary

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- IND-CPA security
 - Even if Eve can trick Alice into encrypting some messages of Eve's choosing, given the encryption of either M_0 or M_1 , Eve cannot distinguish which message was sent with probability greater than $1/2$.
 - We can use the IND-CPA game to test for IND-CPA security
 - Edge cases: IND-CPA secure schemes can leak length. Eve is limited to polynomial-time algorithms, and must have a non-negligible advantage to win.