

## Traverse till Position (DLLL)

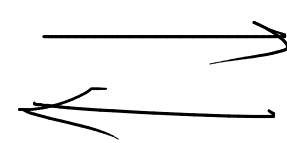
head  
↓

tail  
↓

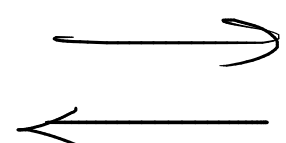
\*

\*

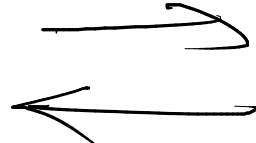
10



20



30



40

①

②

③

trav

pos = 3

Node trav = head;

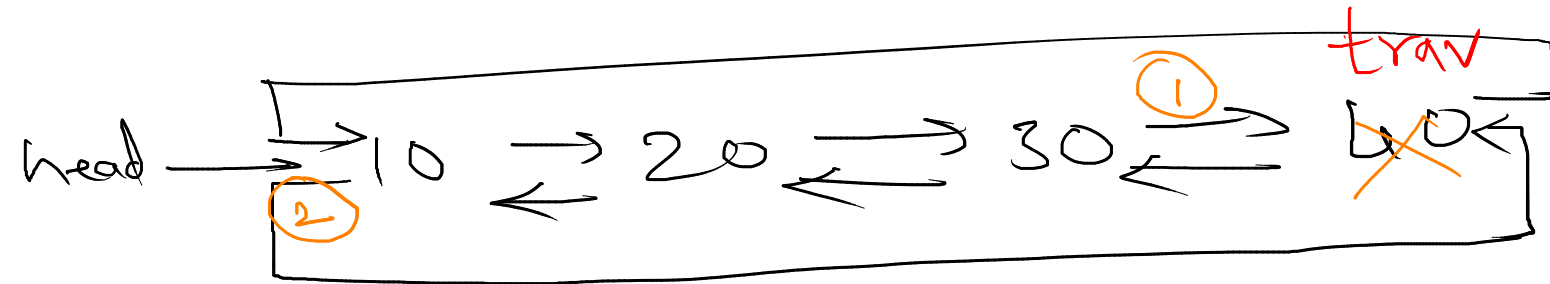
for (int i = 1; i < <sup>3-1 = ②</sup> pos; i++)

trav = trav->next;

trav	i
10	1
20	2

# DCLL

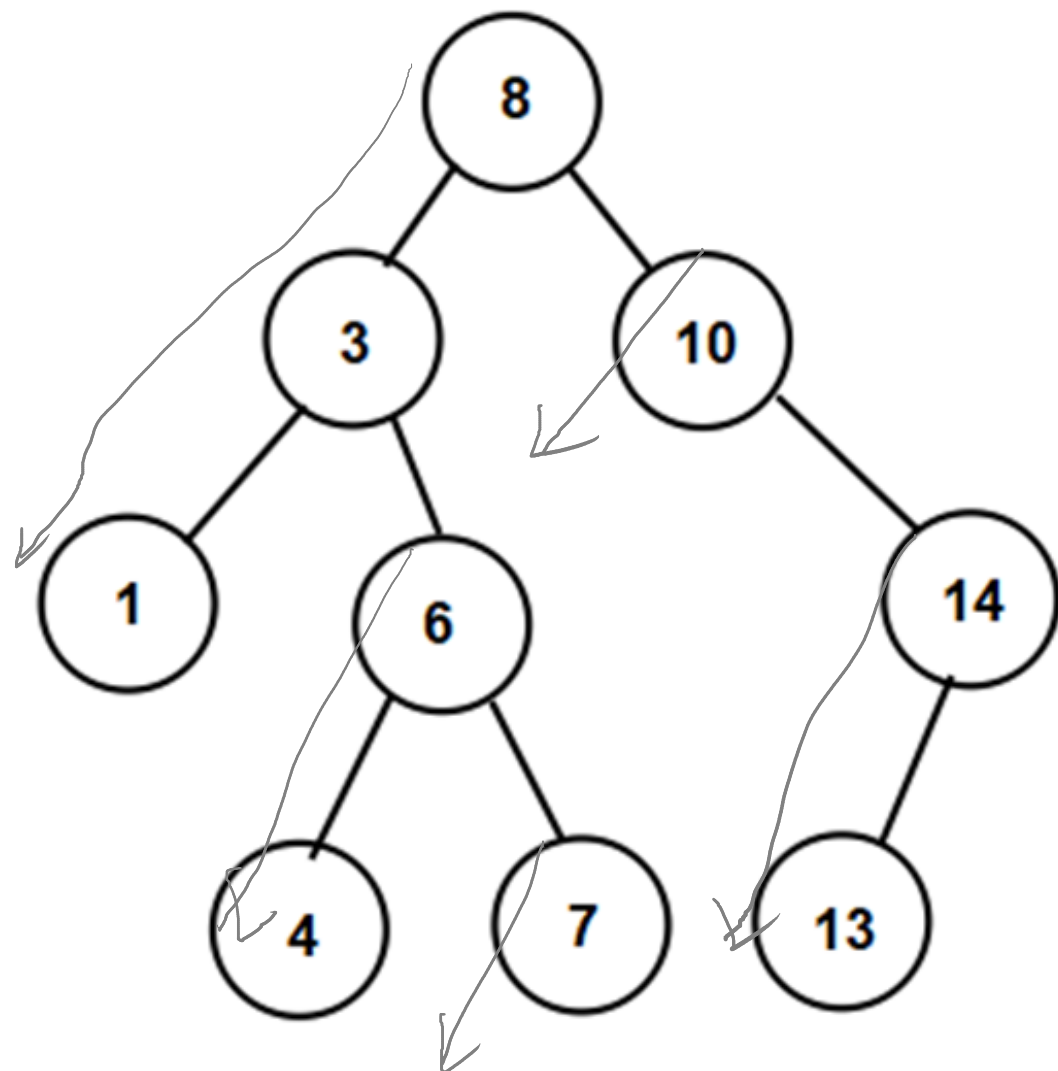
## Delete from Last Position



①  $pos - 1 \rightarrow next = pos + 1$

②  $pos + 1 \rightarrow prev = pos - 1$

## BST - DFS (Depth First Traversal)



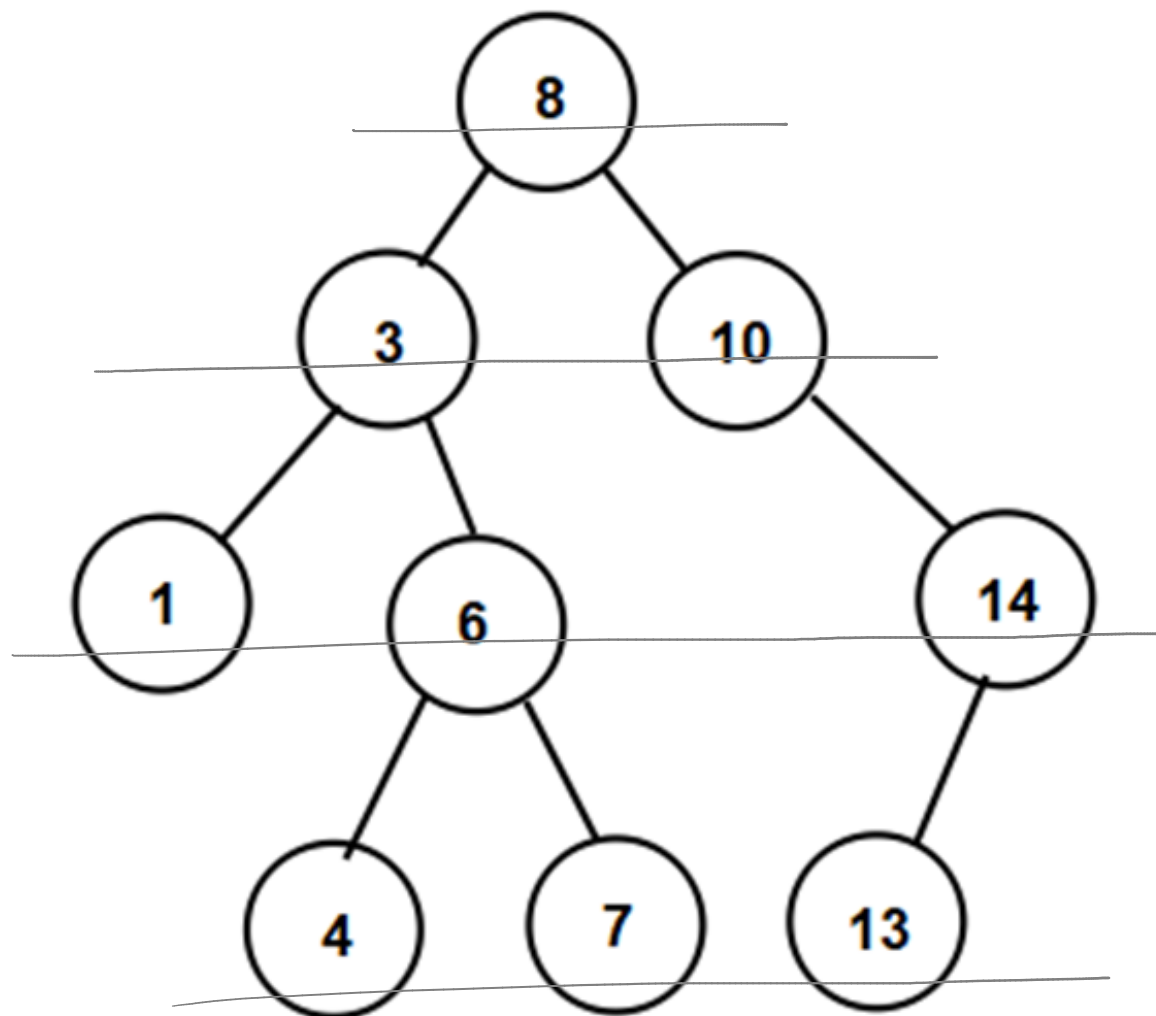
Stack

<del>13</del>
<del>14</del>
<del>4</del>
<del>7</del>
<del>6</del>
<del>3</del>
<del>10</del>
<del>8</del>

- //1. push root on stack
- //2. pop one node from stack
- //3. visit(print) node
- //4. if right exist, push it on stack
- //5. if left exist, push it on stack
- //6. while stack is not empty  
//repeat ste 2 to 5

DFS Traversal = 8, 3, 1, 6, 4, 7, 10, 14, 13

## BST - BFS (Bredth First Search)



Queue

<del>13</del>
<del>7</del>
<del>4</del>
<del>14</del>
<del>6</del>
<del>1</del>
<del>10</del>
<del>3</del>
<del>8</del>

//1. push root on queue

//2. pop one node from queue

//3. visit(print) node

//4. if left exist, push it on queue

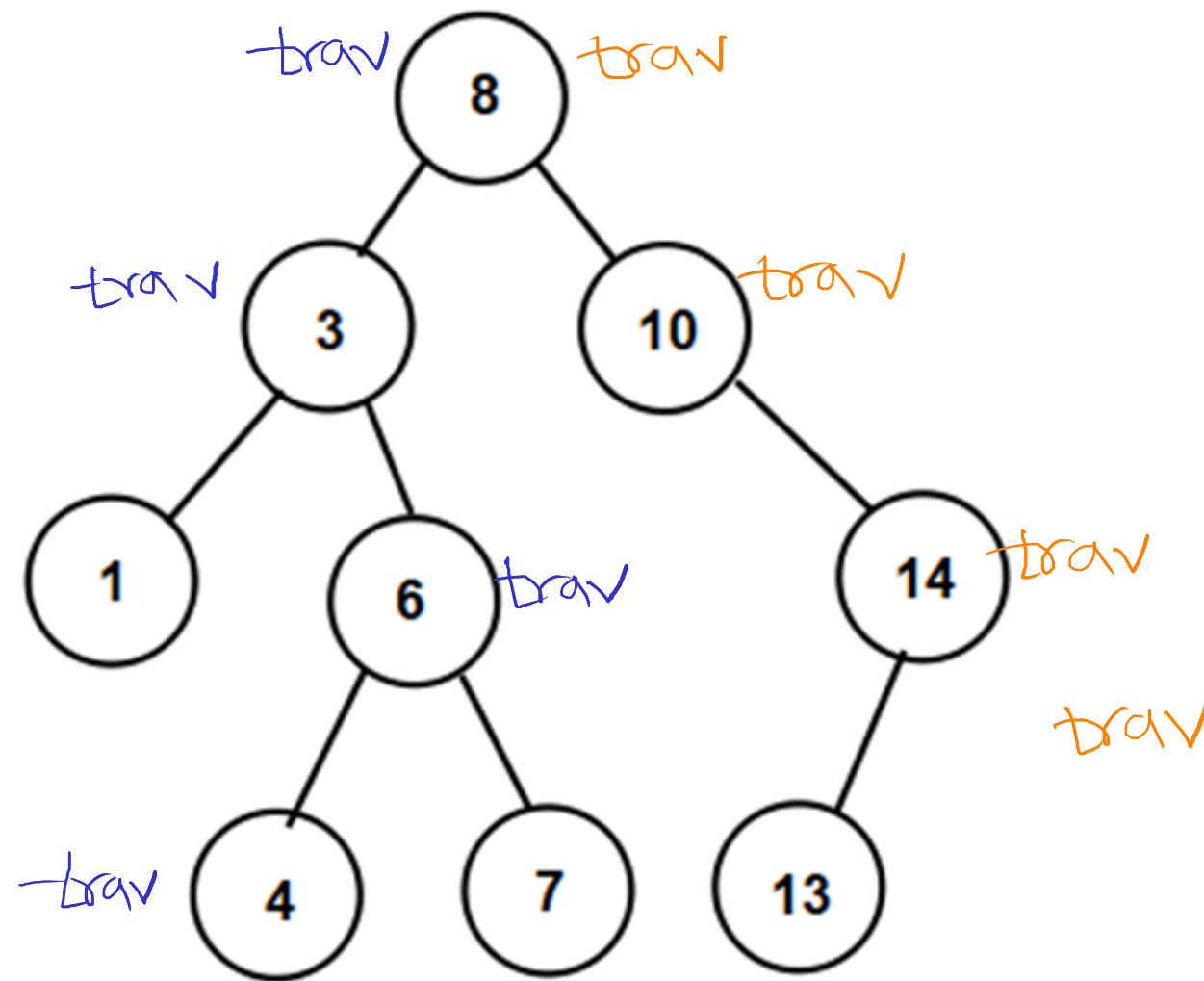
//5. if right exist, push it on queue

//6. while queue is not empty

//repeat ste 2 to 5

BFS Traversal : 8, 3, 10, 1, 6, 14, 4, 7, 13

## BST - Binary Search



**//1. start from root**

**//2. if key is equal to current data  
//return current node**

**//3. if key is less than current data  
// search key into left of current node**

**//4. if key is greater than current data  
// search key into right of current node**

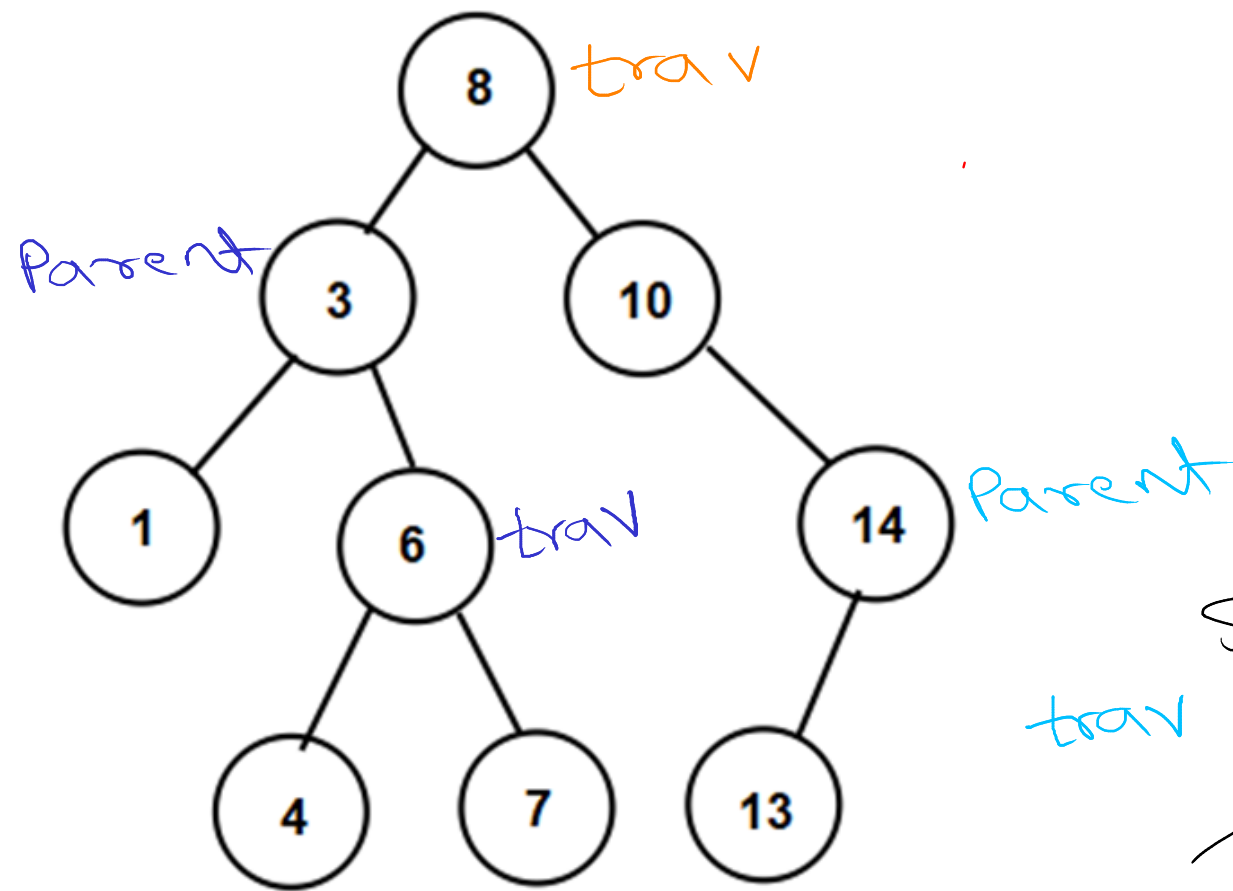
**//5. repeat step 2 to 4 till leaf nodes**

key=4, key found

key=15, key not found

# BST - Delete Node

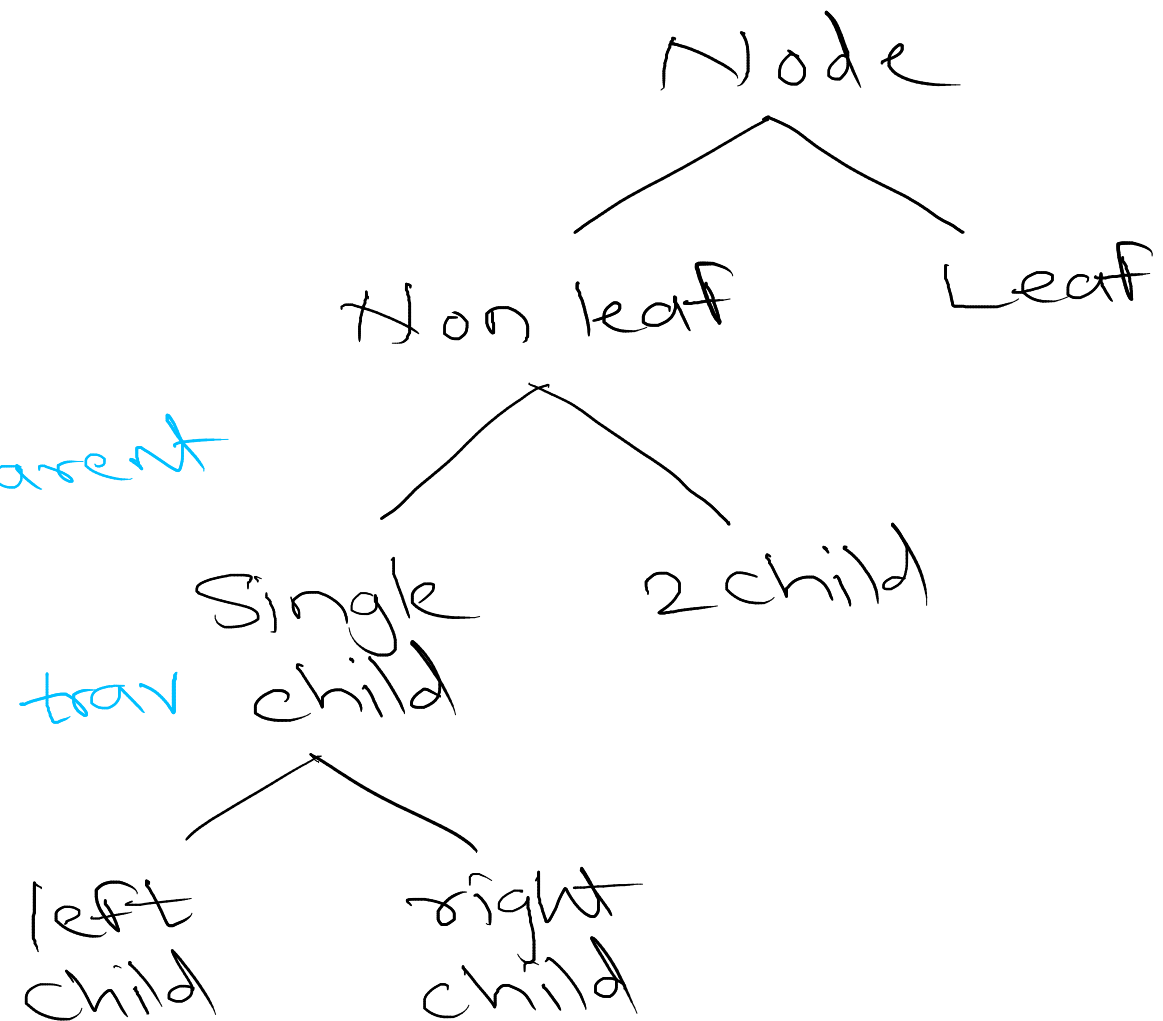
Parent = null



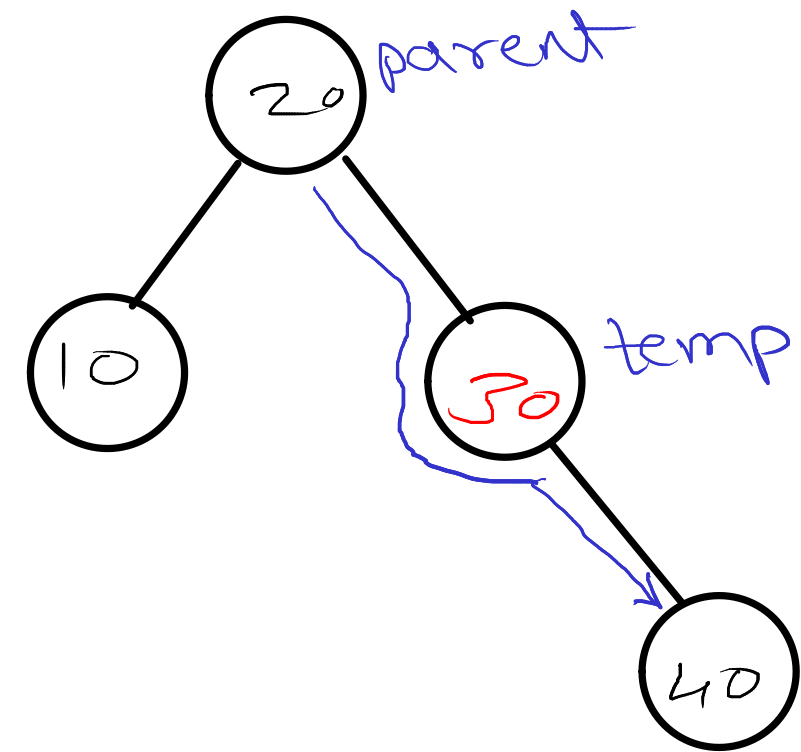
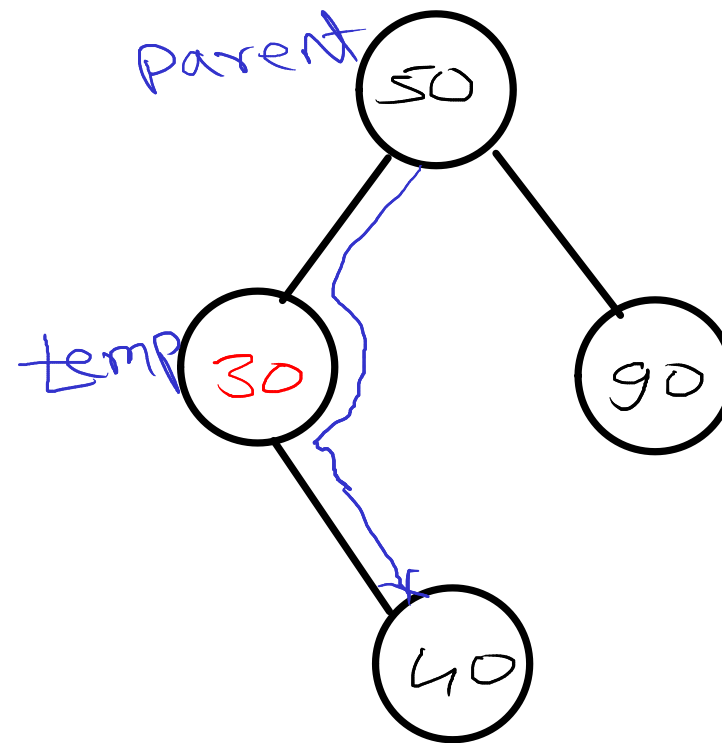
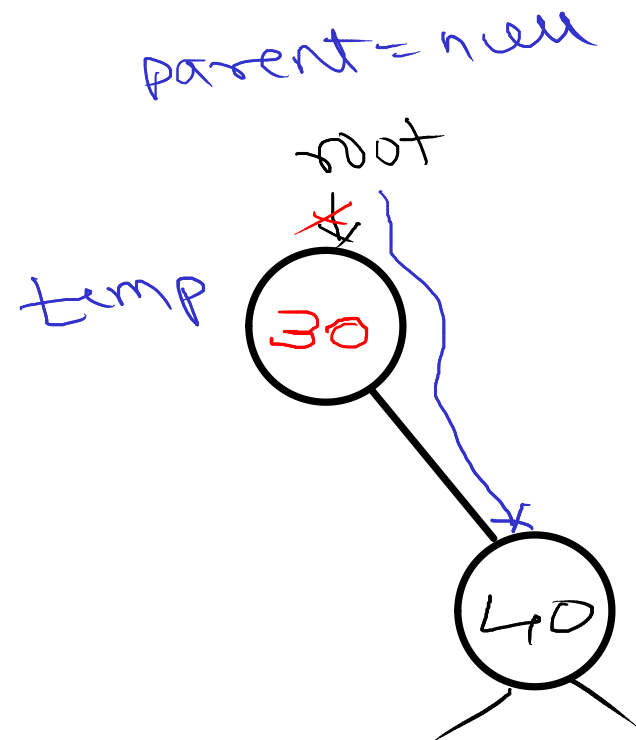
key = 6

key = 8

key = 15

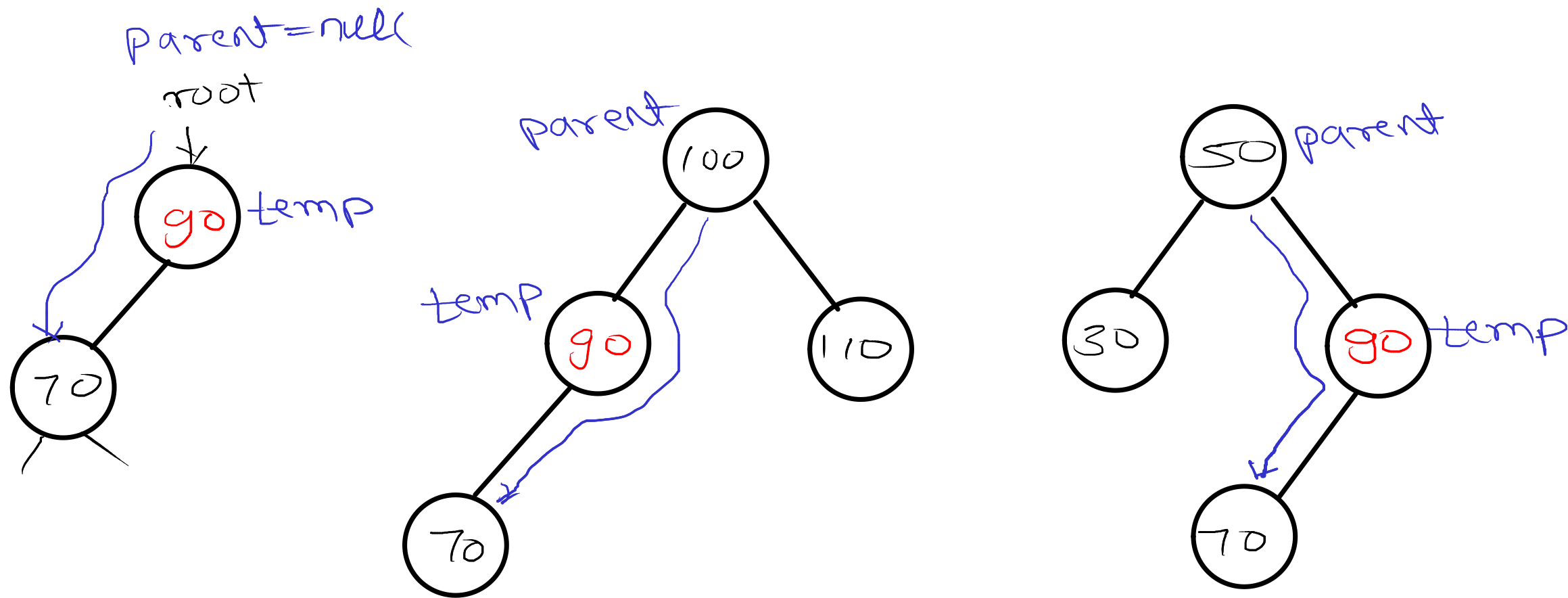


## BST - Delete node which has single child (right child)



```
if(temp.left == null){  
    if(temp == root)  
        root = temp.right;  
    else if(temp == parent.left)  
        parent.left = temp.right;  
    else //if(temp == parent.right)  
        parent.right = temp.right;  
}
```

## BST - Delete node which has single child (left child)

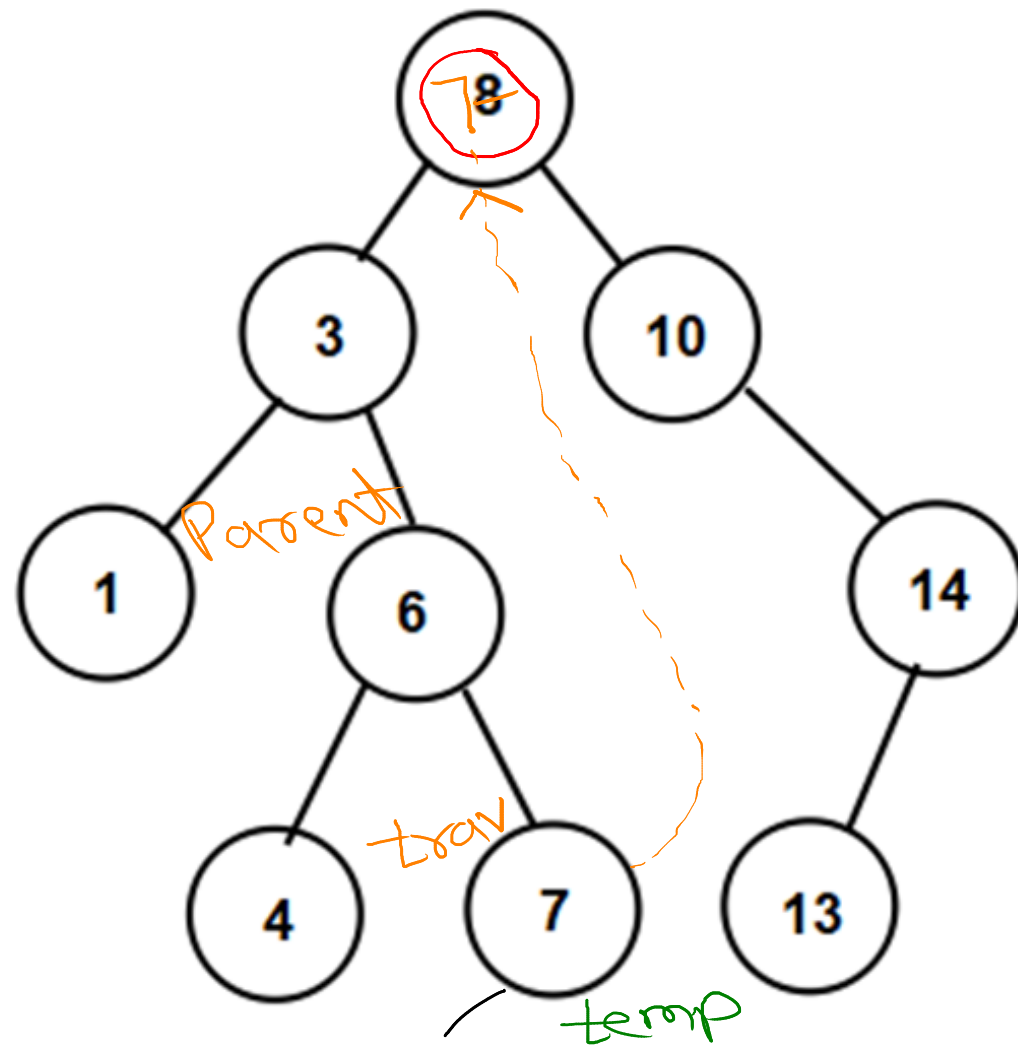


```
if(temp.right == null){  
    if(temp == root)  
        root = temp.left;  
    else if(temp == parent.left)  
        parent.left = temp.left  
    else //if(temp == parent.right)  
        parent.right = temp.left;  
}
```



## BST - Delete node which has two childs

```
if(temp.left != null && temp.right != null){  
    //1. find inorder predecessor  
    Node trav = temp.left;  
    parent = temp;  
    while(trav.right != null){  
        parent = trav;  
        trav = trav.right;  
    }  
    //2. update data by data of predecessor  
    temp.data = trav.data;  
    //3. mark trav to be deleted  
    temp = trav;  
}
```



Inorder Traversal : 1   3   4   5   7   8   10   13   14

**Inorder  
predecessor**

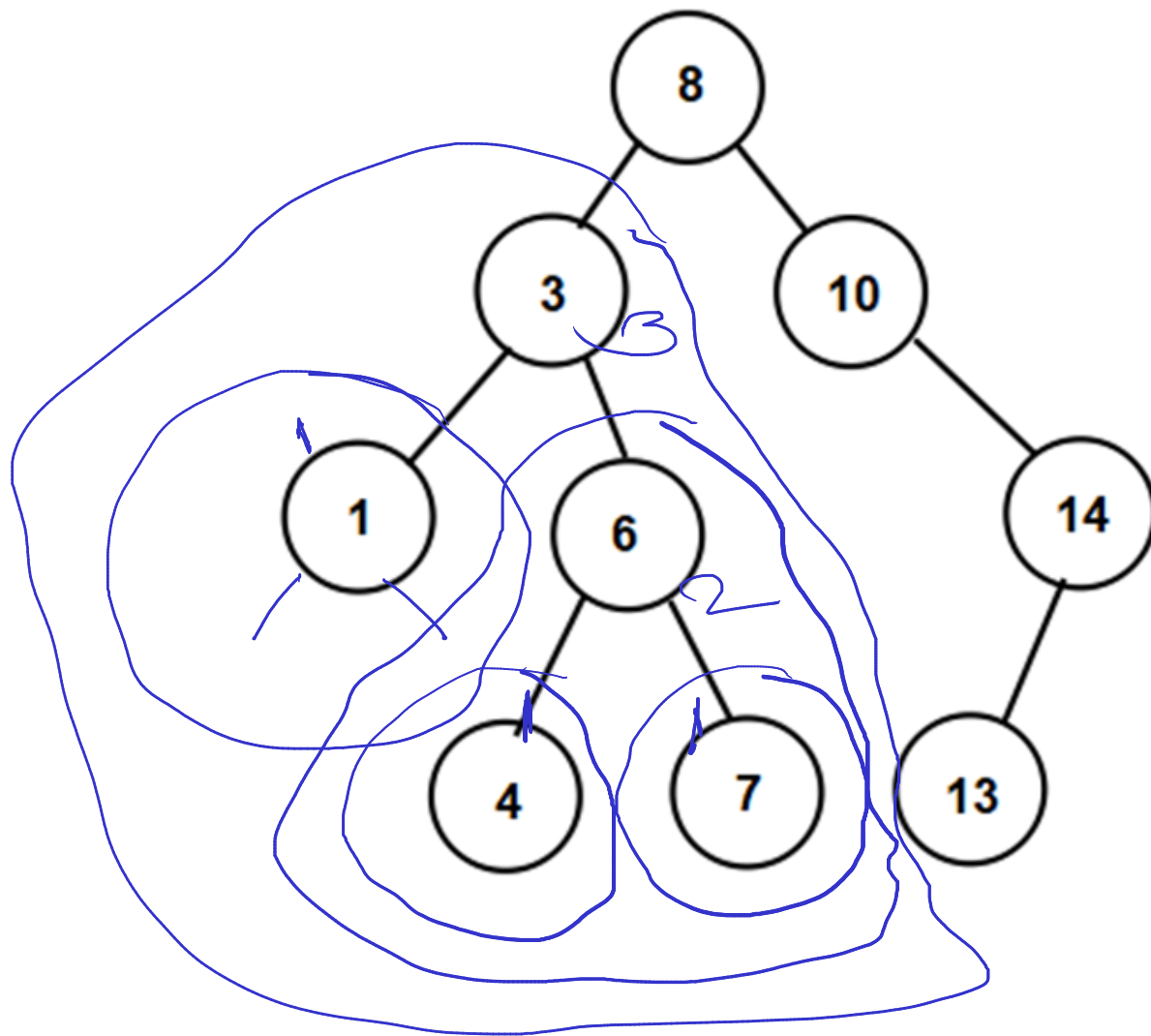
left  
extreme right

**Inorder  
successor**

right  
extreme left

## BST - Height

**Height of tree = MAX(Height(left sub tree), Height(right sub tree)) + 1**



**//0. if left or right sub tree is absent**

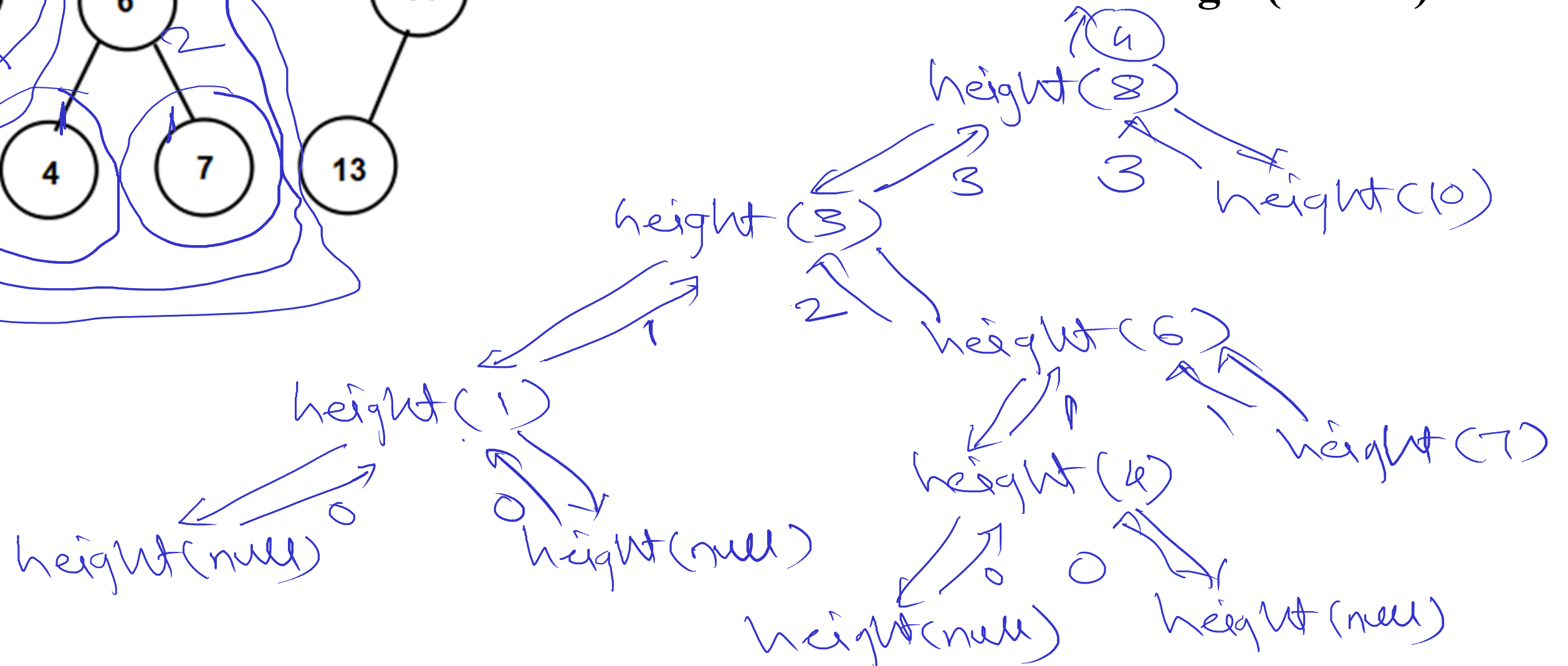
**//then return 0**

**//1. find height of left subtree**

**//2. find height of right subtree**

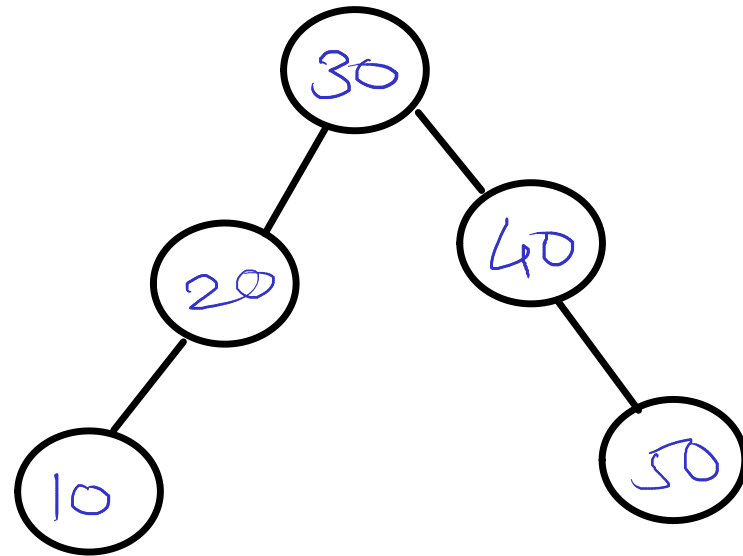
**//3. find max height**

**//4. add one into max height(return)**



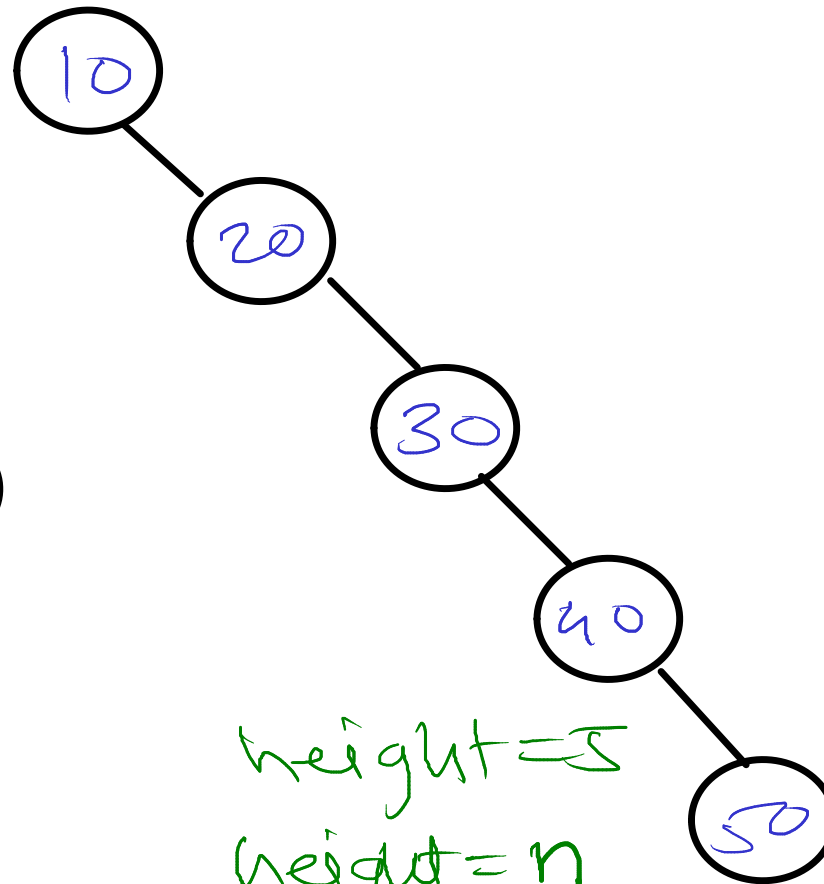
## Skewed BST

Keys : 30, 40, 20, 50, 10



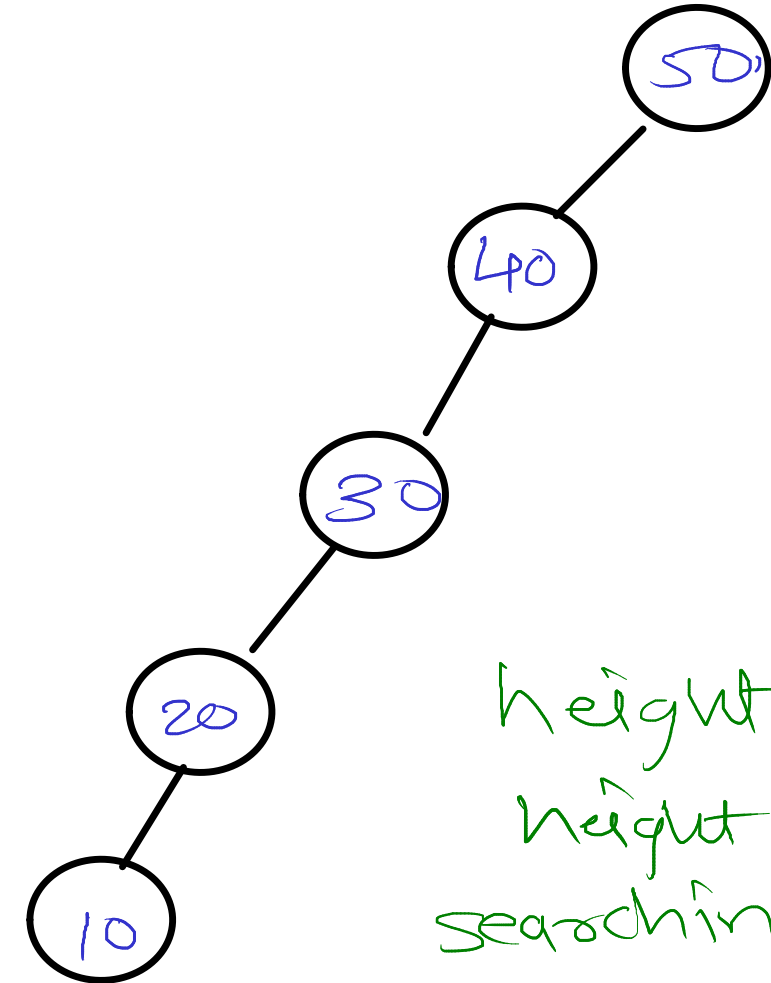
height = 3  
height =  $\log n$   
searching =  $O(\log n)$

Keys : 10, 20, 30, 40, 50



height = 5  
height =  $n$   
searching =  $O(n)$

Key : 50, 40, 30, 20, 10



height = 5  
height =  $n$   
searching =  $O(n)$

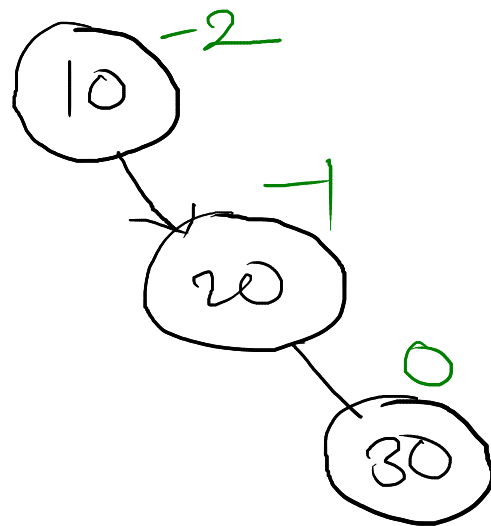
- if tree is growing in only one direction, such tree is known as skewed BST
- if tree is growing in only right direction, such tree is known as right skewed BST
- if tree is growing in only left direction, such tree is known as left skewed BST

## Balanced BST

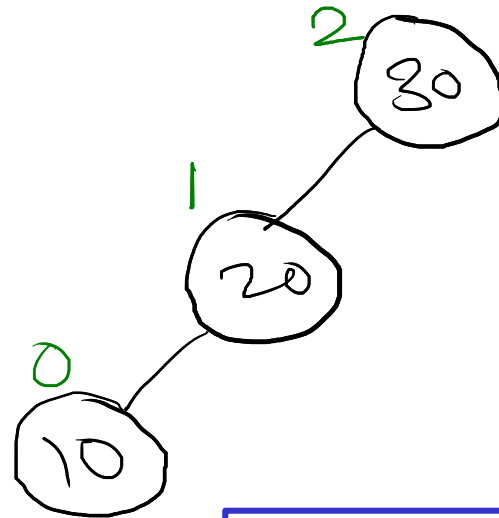
$$\text{Balance Factor} = \text{height}(\text{left sub tree}) - \text{height}(\text{right sub tree})$$

- tree is balanced if balance factor of all the nodes is either -1, 0 or +1
- balance factor = {-1, 0, +1}

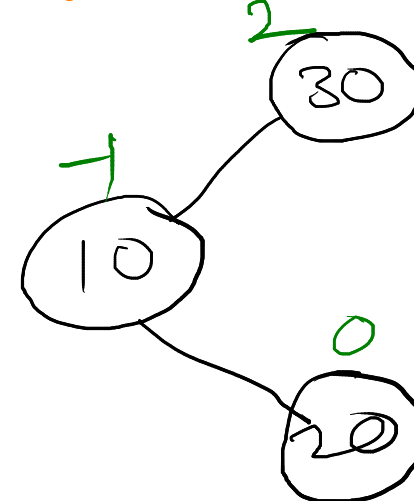
Keys : 10, 20, 30



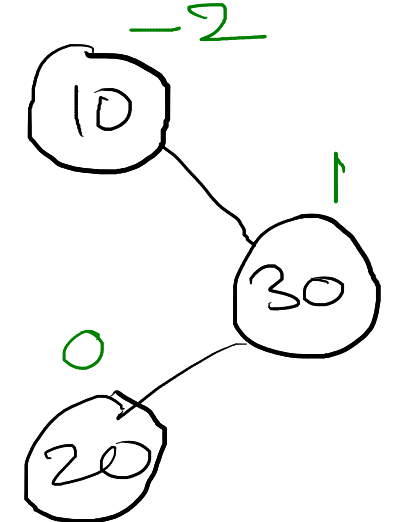
Keys : 30, 20, 10



Keys : 30, 10, 20

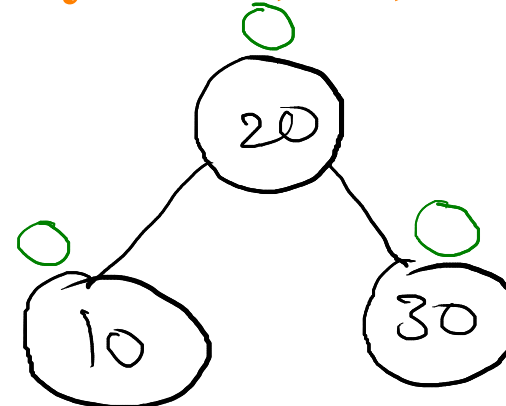


Keys : 10, 30, 20



Keys : 20, 10, 30

Keys : 20, 30, 10

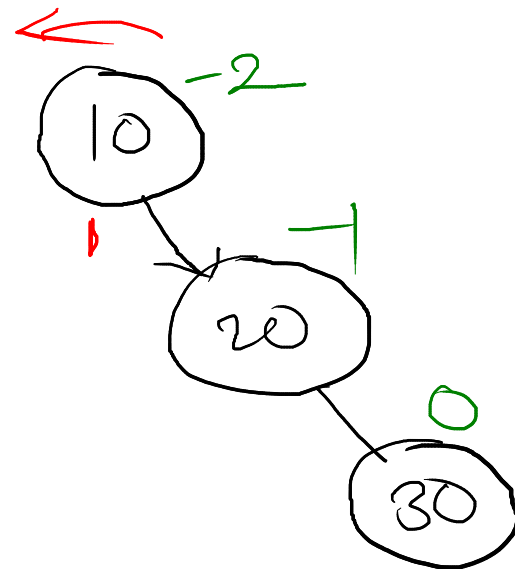


Balanced BST

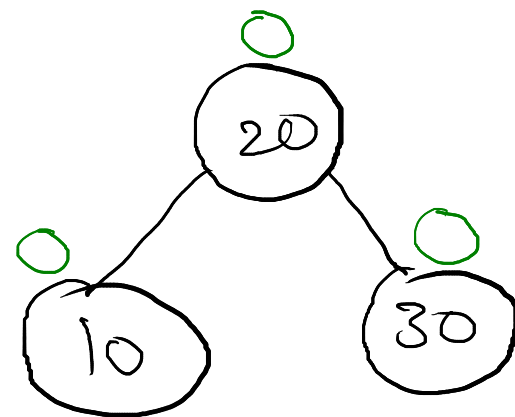
# Rotations

## RR Imbalance

Keys : 10, 20, 30



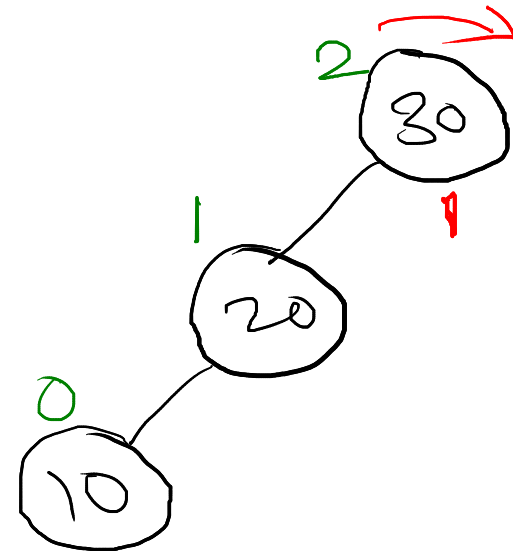
Left Rotation



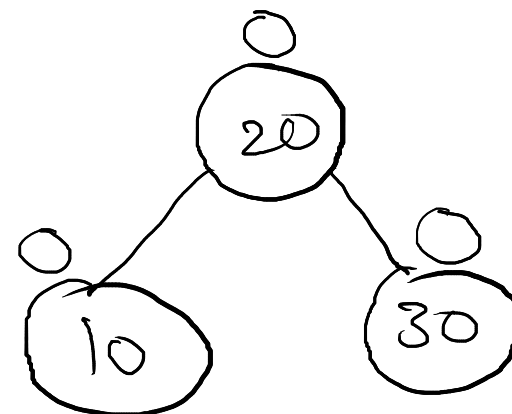
Single Rotation

## LL Imbalance

Keys : 30, 20, 10

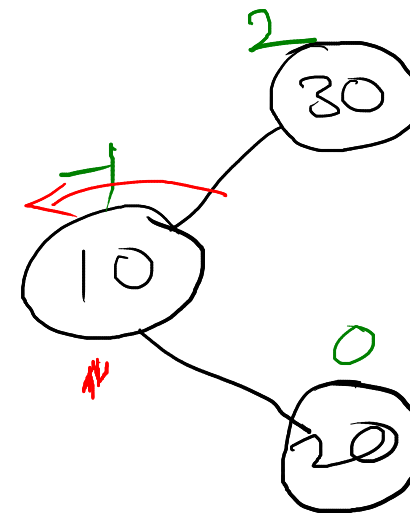


Right Rotation

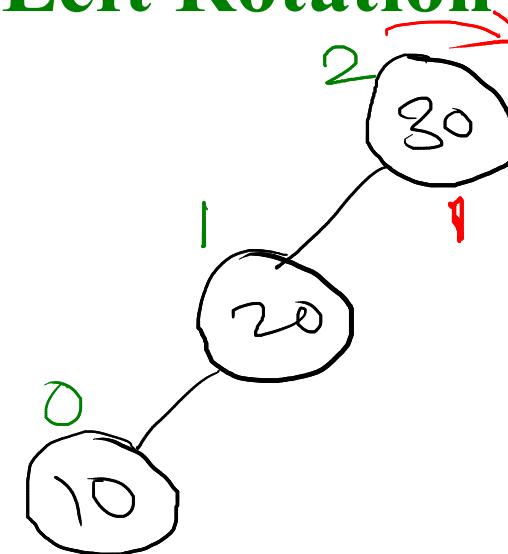


## LR Imbalance

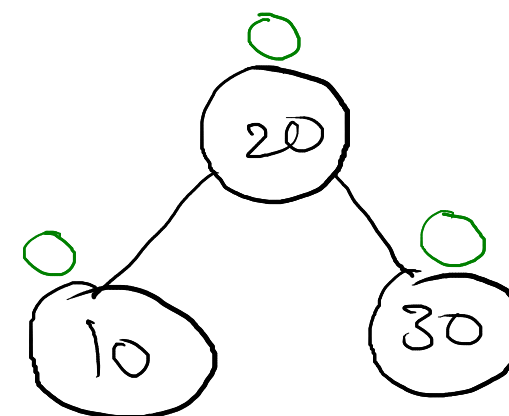
Keys : 10, 30, 20



Left Rotation



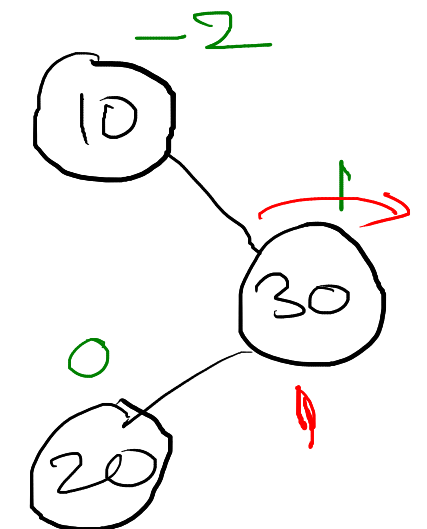
Right Rotation



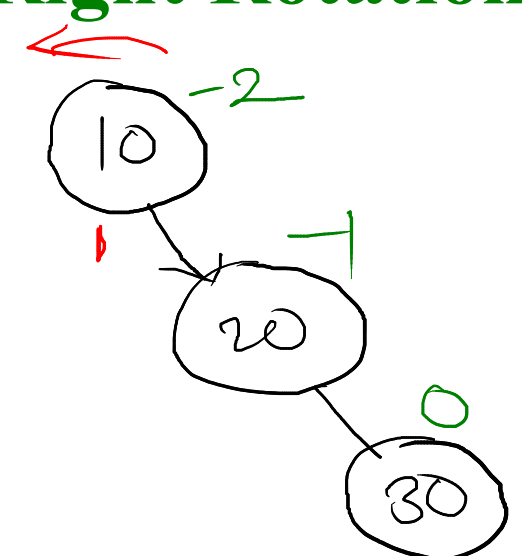
Double Rotation

## RL Imbalance

Keys : 30, 10, 20



Right Rotation



Left Rotation

