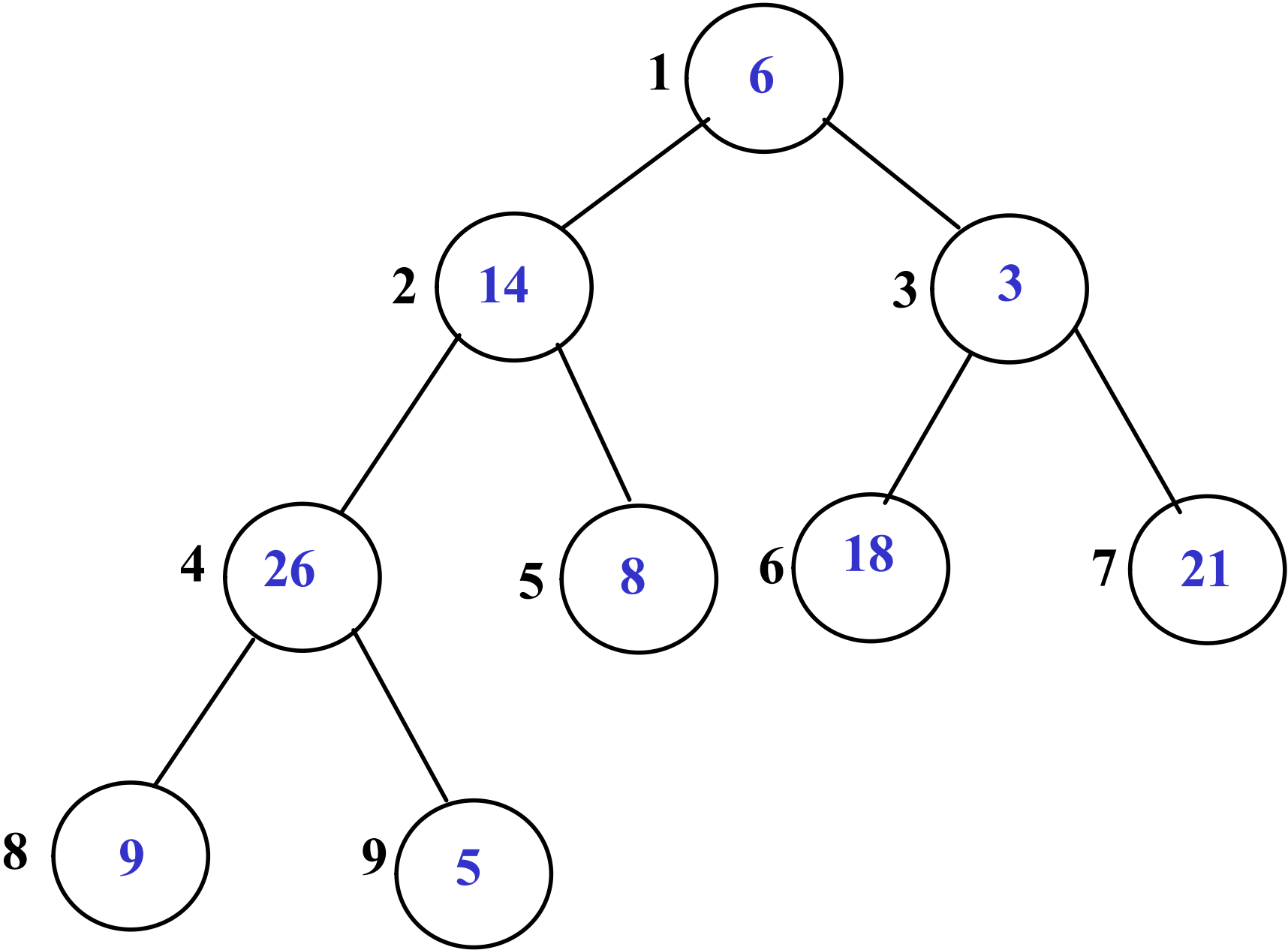


**Almost Complete Binary Tree**



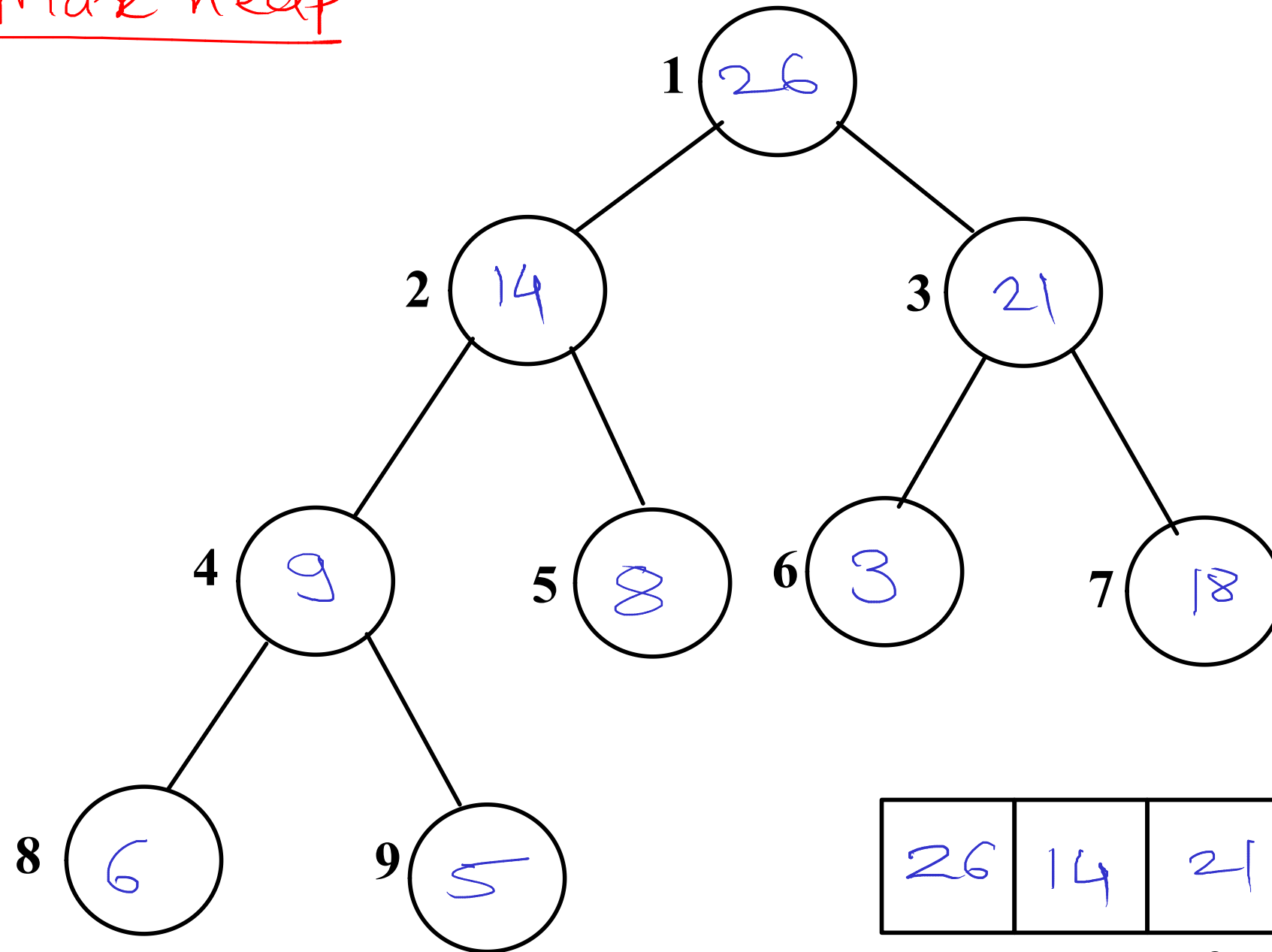
6	14	3	26	8	18	21	9	5
1	2	3	4	5	6	7	8	9

## Create Max Heap

6 14 3 26 8 18 21 9 5

Max heap

Time Complexity =  $O(h)$   
=  $O(\log n)$



26	14	21	9	8	3	18	6	5
1	2	3	4	5	6	7	8	9

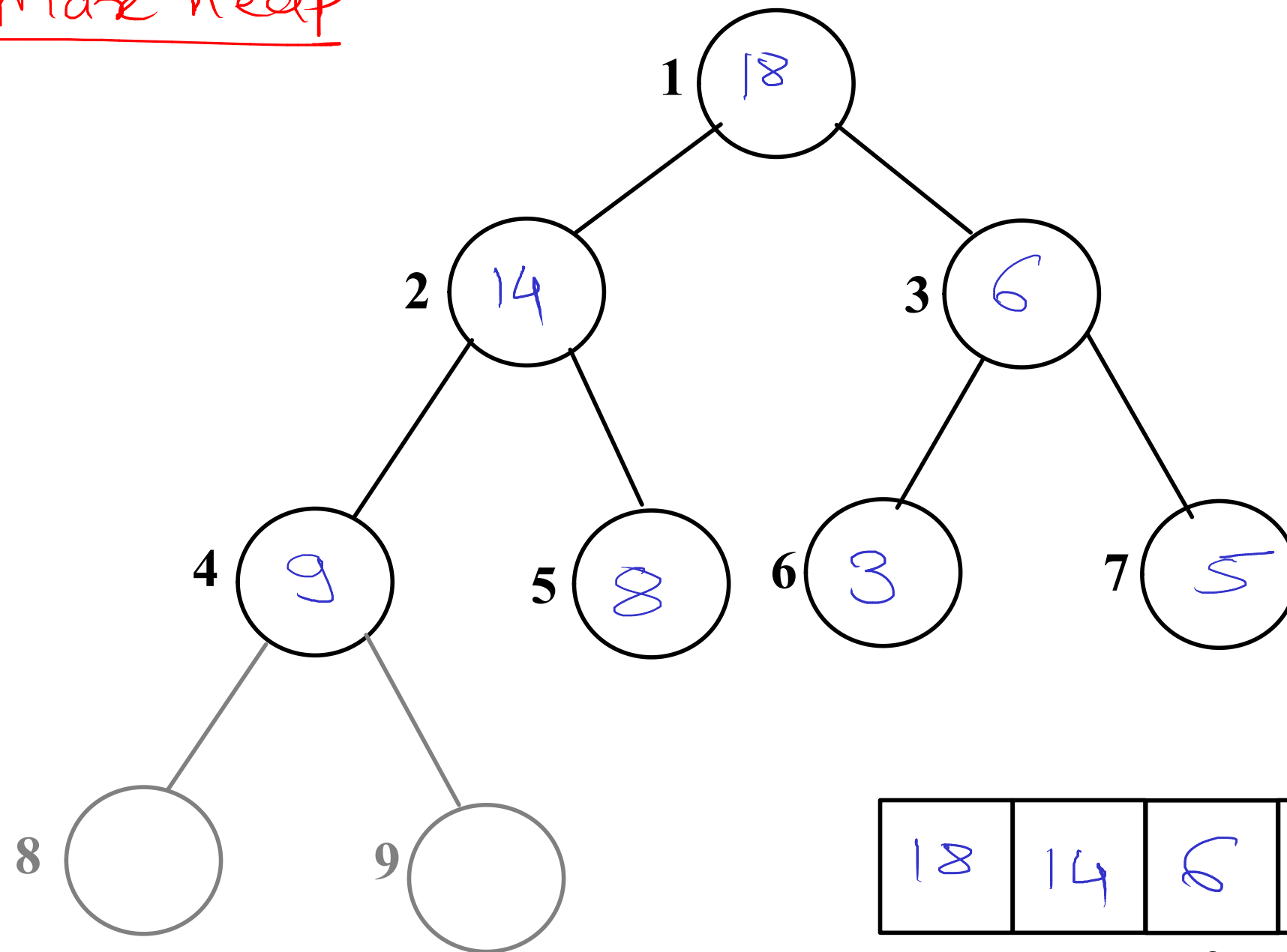
## delete Max Heap

Max heap

Max = 26

Max = 21

Time Complexity =  $O(h)$   
=  $O(\log n)$



18	14	6	9	8	3	5	21	26
1	2	3	4	5	6	7	8	9

# Merge Sort

## Divide and Conquer

//1. divide collection(array) into two partitions (parts)

//2. sort individual partition separately

//3. merge sorted partitions in single array to get sorted array

<del>6</del>	<del>3</del>	<del>9</del>	<del>1</del>	<del>7</del>	2	8	4	5
0	1	2	3	4	5	6	7	8

$ms(arr, 0, 8) \quad m=4$

$ms(arr, 0, 4) \quad m=2$

1	3	6	7	9
0	1	2	3	4

$ms(arr, 3, 4) \quad m=3$

1	7
0	1

$ms(arr, 3, 3)$

$ms(arr, 4, 4)$

$ms(arr, 0, 2) \quad m=1$

3	6	9
0	1	2

$ms(arr, 2, 2)$

$ms(arr, 0, 1) \quad m=0$

3	6
0	1

$ms(arr, 0, 0)$

$ms(arr, 1, 1)$

levels of division =  $\log n$

comparisons =  $n$   
per level

total comp =  $n \log n$   
 $T(n) = O(n \log n)$

# Quick Sort

## Divide and Conquer

//1. select one reference/axis/pivot element from array

//i. pivot = leftmost element

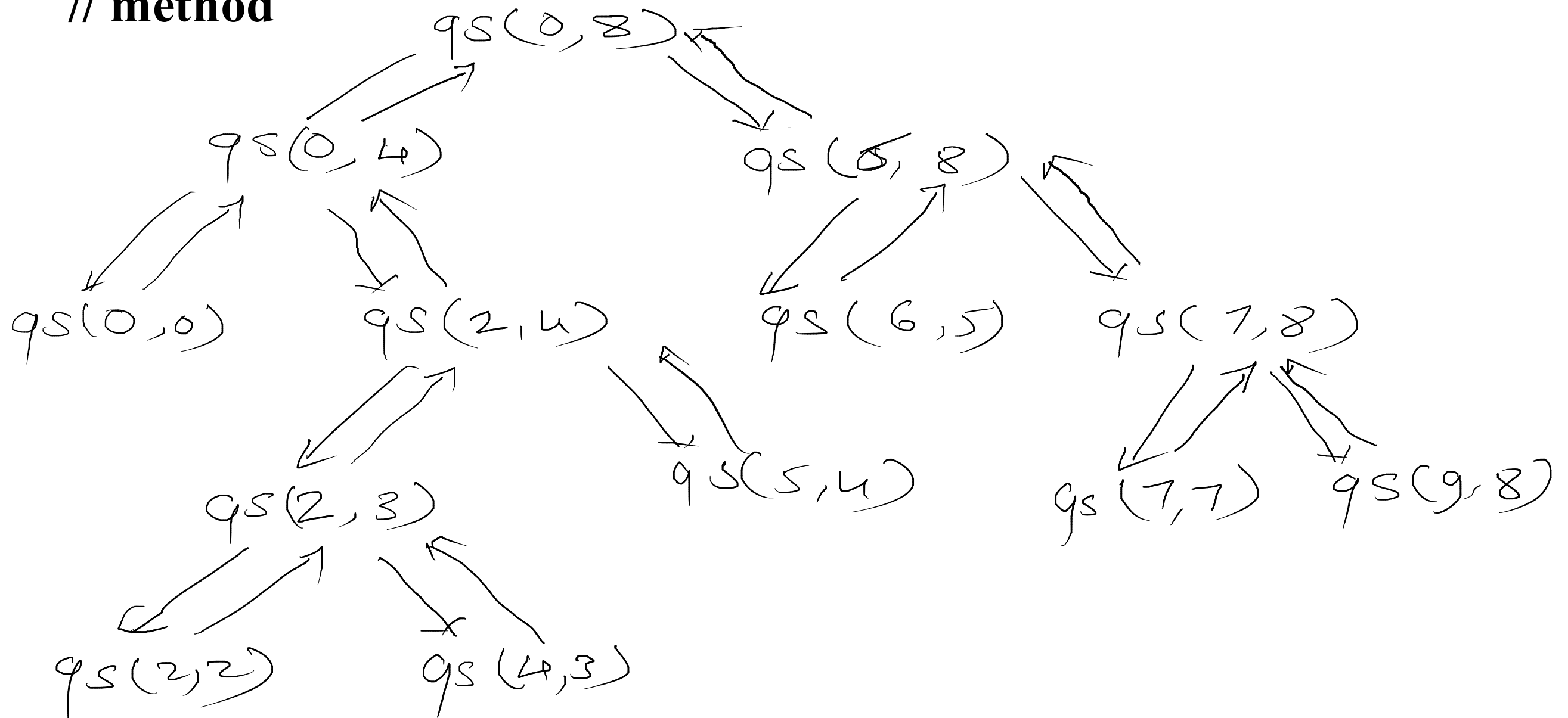
//ii. pivot = rightmost element

//iii. pivot = middle element

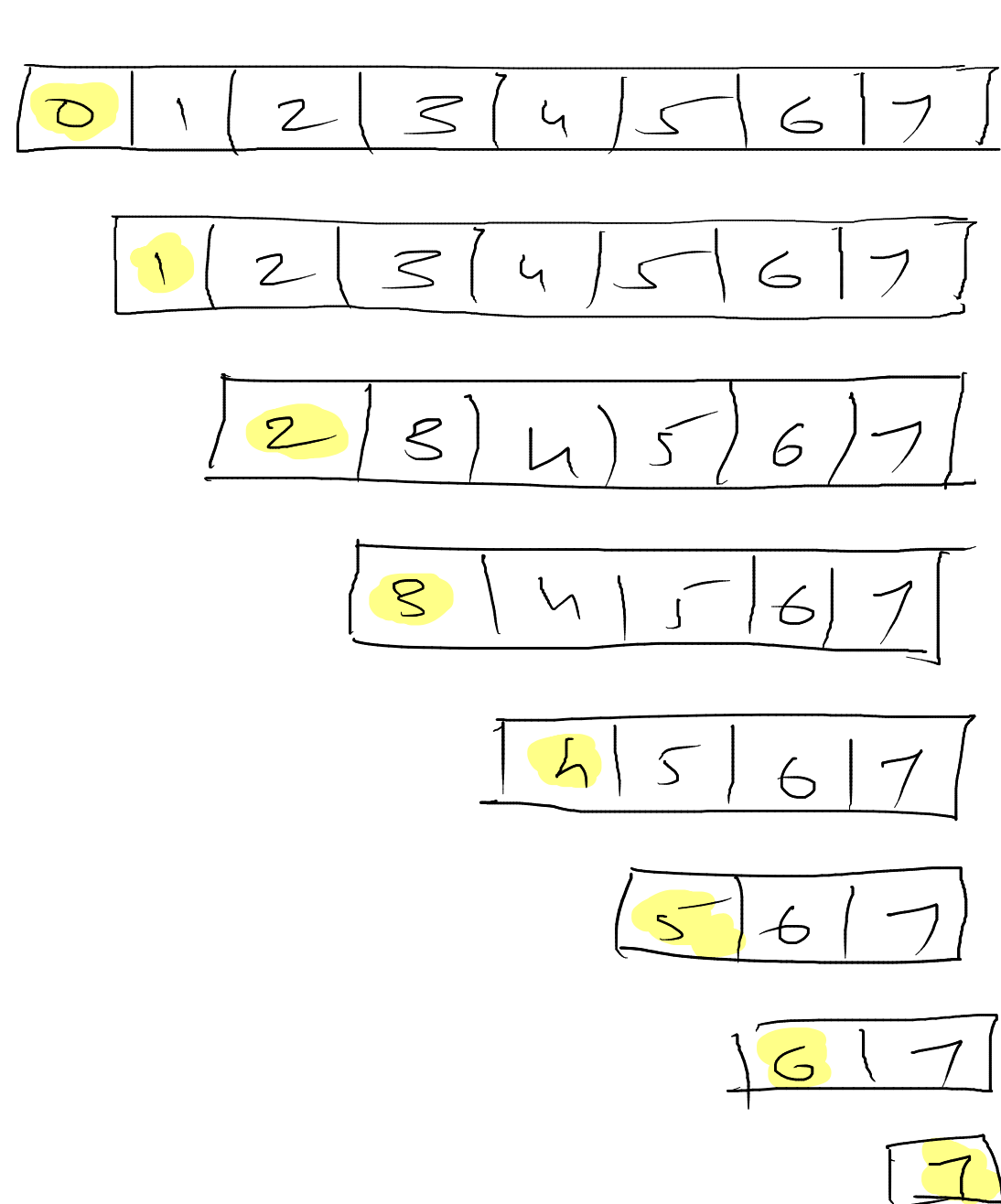
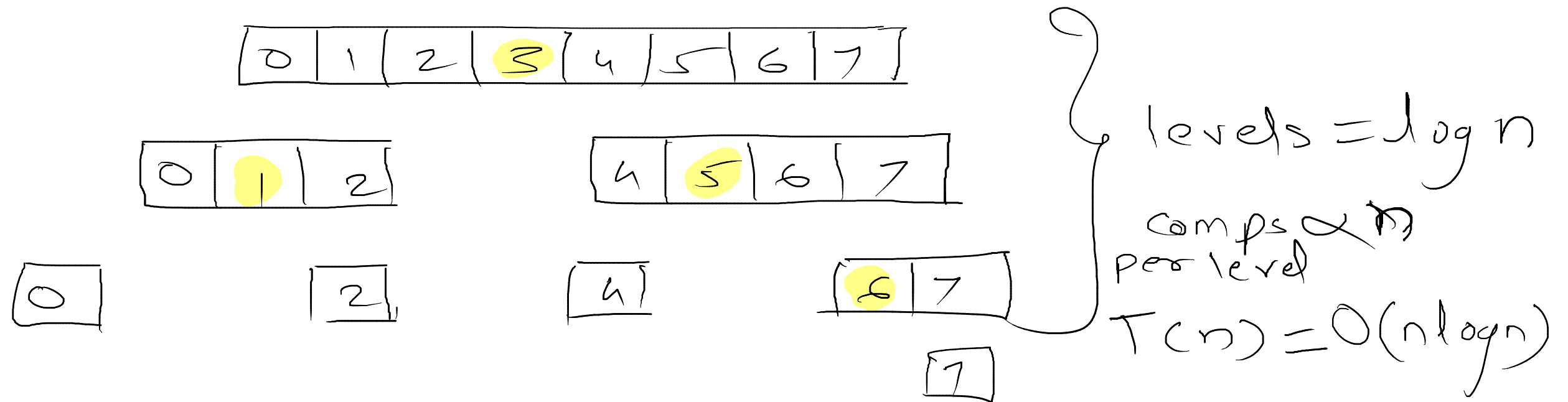
//2. arrange all lesser elements than pivot on left side of pivot

//3. arrange all greater elements than pivot on right side of pivot

//4. sort left and right partition of pivot individually by applying same  
// method



# Quick Sort



Time complexity of quick sort also depends on selection of pivot.

levels =  $n$   
comp  $\propto n$  per level

$$T(n) = O(n^2)$$

Pivot selection —  
to improve performance  
— dual pivot quick sort  
— median of 3