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Introduction

In the volatile world of financial markets, accurately predicting future price movements and understanding market behavior are critical for investors, traders, and financial analysts. The primary challenge lies in dealing with the inherent unpredictability and fluctuations in financial data. This project focuses on leveraging advanced time series analysis techniques to forecast financial data, specifically examining returns and volatility. By doing so, I aim to provide a robust framework for better decision-making and risk management.

The significance of this project is based in its ability to enhance forecasting accuracy by combining ARMA (AutoRegressive Moving Average) models with GARCH (Generalized Autoregressive Conditional Heteroskedasticity) models. ARMA models are capable at capturing the linear patterns in time series data, while GARCH models excel at modeling volatility clustering in financial markets. By integrating these models, we can achieve a more comprehensive understanding of market dynamics which offers valuable insights that can aid in strategic planning, risk assessment, and optimizing investment strategies.

Non-Seasonal Data

• Non-seasonal data does not show periodic patterns. Fluctuations in such data are not tied to a specific season or time of year and can arise from a variety of non-cyclical factors.

Seasonal Data

 Seasonal data exhibits patterns or behaviors that repeat over a specific period, such as monthly or quarterly. This cyclical nature often corresponds to external factors like weather or holidays.

ADF Test for Stationarity

 The Augmented Dickey-Fuller (ADF) test is a statistical test used to determine the stationarity of a time series. It tests the null hypothesis that a unit root is present, where its absence (p-value <0.05) indicates stationarity.

Differencing for Stationarity

Differencing is a method to make a time series stationary by subtracting the current observation from the
previous one. This process, often repeated, removes trends and cycles, making the data more suitable for
ARIMA modeling.

ARIMA Models

• ARIMA (AutoRegressive Integrated Moving Average) models are used for forecasting nonseasonal time series data. It combines autoregressive (AR) terms, differencing for stationarity (I), and moving average (MA) terms, represented as ARIMA(p, d, q), where p, d, and q are nonnegative integers.

GARCH Models

GARCH (Generalized AutoRegressive Conditional Heteroskedasticity) models describe the variance of the
current error term or innovation as a function of the past squared error terms. Primarily used in financial time
series, it captures volatility clustering, where high volatility tends to follow high volatility.

SARIMA Models

SARIMA (Seasonal AutoRegressive Integrated Moving Average) extends the ARIMA model by incorporating

seasonal elements. It's defined as SARIMA(p, d, q)(P, D, Q)s, where (p, d, q) are non-seasonal orders, (P, D, Q) are seasonal orders, and s is the seasonality period.

Ljung-Box Test

 The Ljung-Box test assesses whether any of a group of autocorrelations of a time series are different from zero. It tests the null hypothesis that the data are independently distributed. Low p-values (typically < 0.05) indicate significant autocorrelation.

Shapiro Wilk Test

• The Shapiro-Wilk test is a statistical test that checks whether a dataset is normally distributed. It calculates a p-value; if this value is small (less than 0.05), it suggests the data does not follow a normal distribution.

Dataset

https://finance.yahoo.com/quote/DABUR.NS/history/?guccounter=1&period1=1325376000&period2=1672531200

```
In [1]:
```

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
from statsmodels.tsa.stattools import adfuller
from statsmodels.graphics.tsaplots import plot_acf
from statsmodels.graphics.tsaplots import plot_pacf
from statsmodels.tsa.arima.model import ARIMA
import statsmodels.api as sm
import scipy
import warnings
import arch
warnings.filterwarnings('ignore')
```

```
In [2]:
```

```
df = pd.read_csv('DABUR.csv')
df.head()
```

Out[2]:

_	Date	Open	High	Low	Close	Adj Close	Volume
(2012-01-02	99.300003	101.400002	99.050003	100.449997	89.762779	289745.0
	1 2012-01-03	101.000000	101.500000	98.449997	100.900002	90.164902	369216.0
:	2 2012-01-04	101.199997	102.849998	100.599998	101.099998	90.343620	354686.0
;	3 2012-01-05	101.199997	101.849998	99.449997	100.050003	89.405334	444672.0
4	4 2012-01-06	101.199997	101.199997	98.500000	98.800003	88.288345	924778.0

```
In [3]:
```

```
df.describe()
```

Out[3]:

	Open	High	Low	Close	Adj Close	Volume
count	2713.000000	2713.000000	2713.000000	2713.000000	2713.000000	2.713000e+03
mean	340.821231	344.689219	336.640435	340.496572	324.676184	1.856691e+06
std	151.732568	153.116946	150.038014	151.497707	152.087223	1.560272e+06
min	93.800003	94.900002	92.000000	92.500000	82.658607	0.000000e+00

```
225.000000
Open
                            221.250000
Low
 25%
                  226.850006
High
                                       223.699997
Close
                                                           8.797650e+05
Volume
       307.799988
                                       307.600006
                                                  287.562988 1.422545e+06
 50%
                  311.000000
                            303.500000
 75%
       477.700012
                  483.649994
                            471.049988
                                       477.549988
                                                  458.896515 2.312806e+06
 max 654.849976
                  658.950012
                            649.000000
                                       653.950012 638.903931 2.079605e+07
In [4]:
df.isna().sum()
Out[4]:
Date
              0
Open
              6
High
              6
Low
Close
              6
Adj Close
Volume
dtype: int64
Found some unexpected values. Need to remove them
In [5]:
df.dropna(inplace=True)
In [6]:
df.isna().sum()
Out[6]:
Date
              0
Open
              0
High
              0
Low
              0
Close
              Ω
Adj Close
Volume
dtype: int64
In [7]:
# Check the time range of the dataset
print("Min Date:", df['Date'].min())
print("Max Date:", df['Date'].max())
Min Date: 2012-01-02
Max Date: 2022-12-30
My data ranges form 2012 to 2022. We will be using 6 years of data for our analysis.
In [8]:
df = df[df['Date'] >= '2017-01-01']
In [9]:
```

import matplotlib.dates as mdates

plt.plot(df['Date'], df['Close'])
plt.title('DABUR Prices Over Time')

plt.figure(figsize=(10, 5))

plt.ylabel('Closing Price')

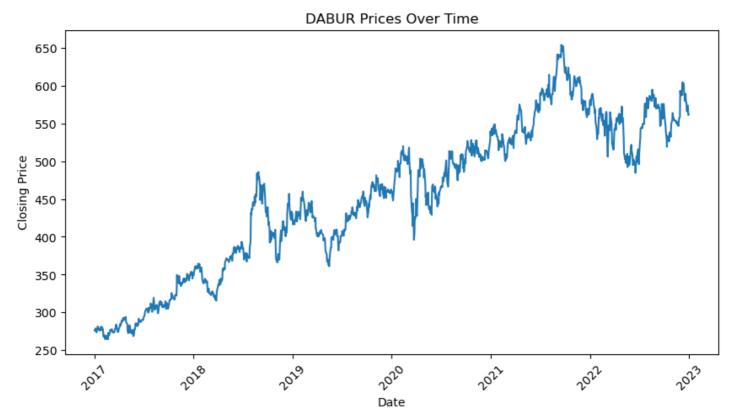
plt.xlabel('Date')

Converting 'Date' column to datetime format

Plotting the closing prices over time with proper date formatting

df['Date'] = pd.to_datetime(df['Date'])

```
# Using YearLocator to set ticks at the start of each year
plt.gca().xaxis.set_major_locator(mdates.YearLocator(base=1))
plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
plt.xticks(rotation=45)
plt.show()
```

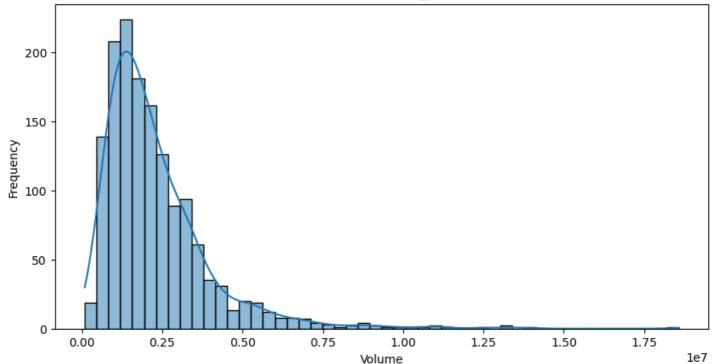


Visualizing the price of DABUR over a period of 6 years

In [10]:

```
plt.figure(figsize=(10, 5))
sns.histplot(df['Volume'], bins=50, kde=True)
plt.title('Distribution of Trading Volumes')
plt.xlabel('Volume')
plt.ylabel('Frequency')
plt.show()
```





The graph depicts the frequency distribution of trading volumes, which is right-skewed rather than normally distributed. This indicates that most trading volumes are relatively low, with a few exceptionally high volumes. The distribution clusters around the lower end, with a long tail extending towards higher volumes which highlights that very large trades are less frequent.

```
In [11]:

df['Date'] = pd.to_datetime(df['Date'])
```

```
In [12]:
```

```
df['Returns'] = 100 * df['Close'].pct_change()
df.iloc[0, 7] = 0
df.head()
```

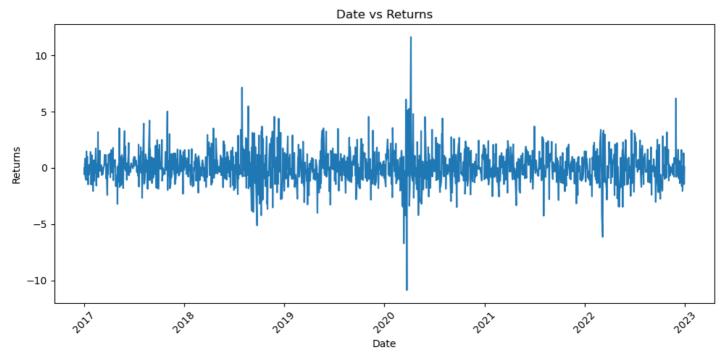
Out[12]:

	Date	Open	High	Low	Close	Adj Close	Volume	Returns
1235	2017-01-02	278.000000	278.399994	274.399994	277.149994	259.739594	265516.0	0.000000
1236	2017-01-03	277.500000	278.000000	274.399994	275.500000	258.193268	450185.0	-0.595343
1237	2017-01-04	275.100006	278.200012	272.899994	276.549988	259.177338	2110365.0	0.381121
1238	2017-01-05	278.149994	279.950012	276.950012	278.850006	261.332886	508994.0	0.831683
1239	2017-01-06	279.250000	280.500000	275.500000	276.600006	259.224152	782100.0	-0.806885

In []:

In [13]:

```
plt.figure(figsize=(10, 5))
plt.plot(df['Date'].values, df['Returns'].values)
plt.title('Date vs Returns')
plt.xlabel('Date')
plt.ylabel('Returns')
plt.xticks(rotation=45)
plt.tight_layout()
plt.show()
```



Stationary Test

```
In [14]:
def test stationarity(ts):
    result = adfuller(ts)
    print(f'ADF Statistic: {result[0]:.4f}')
    print(f'p-value: {result[1]:.4f}')
    print('Critical Values:')
    for key, value in result[4].items():
        print(f'\t{key}: {value:.4f}')
    # Interpretation of the ADF test
    print('\nHypothesis:')
    print('Null Hypothesis (H0): The series has a unit root (non-stationary).')
    print('Alternative Hypothesis (H1): The series has no unit root (stationary).')
    if result[1] > 0.05:
       print("\nFailed to reject the null hypothesis (H0), the data has a unit root and
is non-stationary.")
       print("\nReject the null hypothesis (H0), the data does not have a unit root and
is stationary.")
ts = df.set index('Date')['Returns']
test stationarity(ts)
ADF Statistic: -12.8142
p-value: 0.0000
Critical Values:
 1%: -3.4348
 5%: -2.8635
 10%: -2.5678
Hypothesis:
Null Hypothesis (H0): The series has a unit root (non-stationary).
Alternative Hypothesis (H1): The series has no unit root (stationary).
Reject the null hypothesis (H0), the data does not have a unit root and is stationary.
```

The highly negative ADF statistic of -12.8142, coupled with a practically zero p-value, solidly supports rejecting the null hypothesis. This tells us that the time series data is stationary, meaning it does not have a unit root and shows consistent statistical properties over time.

```
In [15]:

ts = pd.DataFrame(ts)
ts.head()

Out[15]:
```

Returns

Date 2017-01-02 0.000000 2017-01-03 -0.595343 2017-01-04 0.381121 2017-01-05 0.831683 2017-01-06 -0.806885

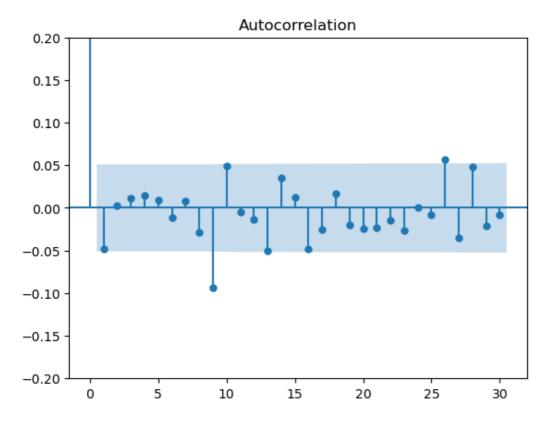
ACF and PACF

In [16]:

```
plot_acf(ts['Returns'], lags = 30);
plt.ylim(-0.2,0.2)
```

Out[16]:

(-0.2, 0.2)

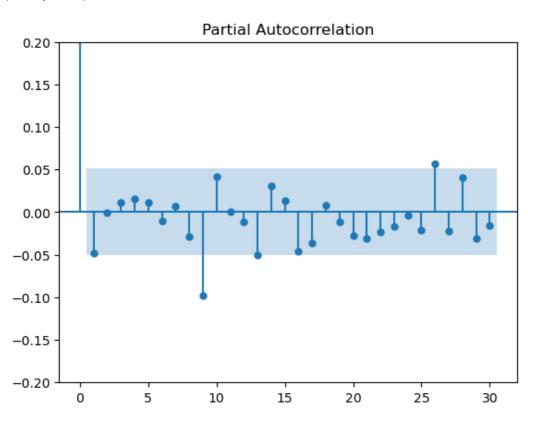


In [17]:

```
plot_pacf(ts['Returns'], lags = 30);
plt.ylim(-0.2,0.2)
```

Out[17]:

(-0.2, 0.2)



Based on the ACF and PACF plots I can see the major significant lag is at 9th lag so based on that I will try some models

ARMA (6,1)

```
In [18]:
```

```
from statsmodels.tsa.arima.model import ARIMA

# Fit an ARIMA model

model = ARIMA(ts['Returns'], order=(6,0,1))
model_fit = model.fit()

# Summary of the model
print(model_fit.summary())

# Perform residual checks
residuals = model_fit.resid
```

SARIMAX Results

Dep. Variable:	Returns	No. Observations:	1484
Model:	ARIMA(6, 0, 1)	Log Likelihood	-2696.950
Date:	Thu, 02 May 2024	AIC	5411.901
Time:	03:05:00	BIC	5459.623
Sample:	0	HQIC	5429.689
	- 1484		

Covariance Type: opg

coef	std err	Z	P> z	[0.025	0.975]
0.0587	0.039	1.490	0.136	-0.019	0.136
-0.0243	2.088	-0.012	0.991	-4.118	4.069
0.0016	0.101	0.016	0.987	-0.197	0.200
0.0122	0.019	0.628	0.530	-0.026	0.050
0.0163	0.031	0.523	0.601	-0.045	0.077
0.0100	0.040	0.253	0.800	-0.068	0.088
-0.0104	0.031	-0.341	0.733	-0.070	0.049
-0.0240	2.091	-0.011	0.991	-4.123	4.075
2.2185	0.049	45.016	0.000	2.122	2.315
========= (L1) (Q):	=======	0.00	Jarque-Bera	========= (JB):	
Prob(Q):			Prob(JB):		0.0
Heteroskedasticity (H):			Skew:		0.2
wo-sided):		0.04	Kurtosis:		8.
	0.0587 -0.0243 0.0016 0.0122 0.0163 0.0100 -0.0104 -0.0240 2.2185	0.0587 0.039 -0.0243 2.088 0.0016 0.101 0.0122 0.019 0.0163 0.031 0.0100 0.040 -0.0104 0.031 -0.0240 2.091 2.2185 0.049 (L1) (Q):	0.0587 0.039 1.490 -0.0243 2.088 -0.012 0.0016 0.101 0.016 0.0122 0.019 0.628 0.0163 0.031 0.523 0.0100 0.040 0.253 -0.0104 0.031 -0.341 -0.0240 2.091 -0.011 2.2185 0.049 45.016 (L1) (Q): 0.00 asticity (H): 0.83	0.0587 0.039 1.490 0.136 -0.0243 2.088 -0.012 0.991 0.0016 0.101 0.016 0.987 0.0122 0.019 0.628 0.530 0.0163 0.031 0.523 0.601 0.0100 0.040 0.253 0.800 -0.0104 0.031 -0.341 0.733 -0.0240 2.091 -0.011 0.991 2.2185 0.049 45.016 0.000 (L1) (Q): 0.00 Jarque-Bera 1.00 Prob(JB): asticity (H): 0.83 Skew:	0.0587 0.039 1.490 0.136 -0.019 -0.0243 2.088 -0.012 0.991 -4.118 0.0016 0.101 0.016 0.987 -0.197 0.0122 0.019 0.628 0.530 -0.026 0.0163 0.031 0.523 0.601 -0.045 0.0100 0.040 0.253 0.800 -0.068 -0.0104 0.031 -0.341 0.733 -0.070 -0.0240 2.091 -0.011 0.991 -4.123 2.2185 0.049 45.016 0.000 2.122 (L1) (Q): 0.00 Jarque-Bera (JB): 1.00 Prob(JB): asticity (H): 0.83 Skew:

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

ARMA(6,2)

In [19]:

```
from statsmodels.tsa.arima.model import ARIMA

# Fit an ARIMA model

model = ARIMA(ts['Returns'], order=(6,0,2))
model_fit = model.fit()

# Summary of the model
print(model_fit.summary())

# Perform residual checks
residuals = model_fit.resid
```

SALTMAV VESATCS

Dep. Varial Model: Date: Time: Sample: Covariance	Th	Return Re	2) Log 024 AIC :05 BIC 0 HQIC	Observations Likelihood	:	1484 -2691.386 5402.772 5455.797 5422.537
	coef	std err		P> z	[0.025	0.975]
ar.L2 ar.L3 ar.L4 ar.L5 ar.L6 ma.L1 ma.L2	1.2719 -0.2732 -0.0046 0.0009 -0.0066 -0.0181 -1.3278 0.3402	0.561	2.101 -0.487 -0.095 0.028 -0.177 -0.483 -2.197 0.572	0.036 0.626 0.924 0.978 0.859 0.629 0.028 0.567	-0.100 -0.061 -0.080 -0.091 -2.512 -0.825	2.458 0.826 0.091 0.063 0.067 0.055
Ljung-Box Prob(Q): Heteroskeda Prob(H) (tr	asticity (H):		0.00 1.00 0.84 0.05	Jarque-Bera Prob(JB): Skew: Kurtosis:	(JB):	1739.5 0.0 0.2 8.2

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

ARMA(6,5)

In [20]:

```
from statsmodels.tsa.arima.model import ARIMA

# Fit an ARIMA model

model = ARIMA(ts['Returns'], order=(6,0,5))
model_fit = model.fit()

# Summary of the model
print(model_fit.summary())

# Perform residual checks
residuals = model_fit.resid
```

SARIMAX Results

Dep. Variable:	Returns	No. Observations:	1484
Model:	ARIMA(6, 0, 5)	Log Likelihood	-2690.823
Date:	Thu, 02 May 2024	AIC	5407.646
Time:	03:05:09	BIC	5476.578
Sample:	0	HQIC	5433.339
	_ 1/0/		

- 1484

Covariance Type: opg

========						
	coef	std err	Z	P> z	[0.025	0.975]
const	0.0585	0.038	1.552	0.121	-0.015	0.132
ar.L1	0.2726	0.095	2.880	0.004	0.087	0.458
ar.L2	0.0394	0.076	0.516	0.606	-0.110	0.189
ar.L3	-0.0054	0.068	-0.079	0.937	-0.139	0.129
ar.L4	0.4194	0.065	6.454	0.000	0.292	0.547
ar.L5	-0.8463	0.082	-10.302	0.000	-1.007	-0.685
ar.L6	-0.0536	0.025	-2.128	0.033	-0.103	-0.004
ma.L1	-0.3173	0.093	-3.399	0.001	-0.500	-0.134
ma.L2	-0.0128	0.079	-0.162	0.871	-0.168	0.142
ma.T.3	0.0330	0.072	0.460	0.646	-0.108	0.174

	· • · · · ·	· • · · <u>-</u>	· • • · ·	· • · · ·	· · · ·	· · · ·
ma.L4	-0.4022	0.071	-5.688	0.000	-0.541	-0.264
ma.L5	0.8416	0.083	10.109	0.000	0.678	1.005
sigma2	2.1501	0.048	44.348	0.000	2.055	2.245
		=======				
Ljung-Box	(L1) (Q):		0.02	Jarque-Bera	(JB):	1779.88
Prob(Q):			0.90	Prob(JB):		0.00
Heterosked	dasticity (H):		0.84	Skew:		0.21
Prob(H) (t	two-sided):		0.06	Kurtosis:		8.35

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

ARMA(7,2)

In [21]:

```
from statsmodels.tsa.arima.model import ARIMA

# Fit an ARIMA model

model = ARIMA(ts['Returns'], order=(7,0,2))
model_fit = model.fit()

# Summary of the model
print(model_fit.summary())

# Perform residual checks
residuals = model_fit.resid
```

SARIMAX Results

Dep. Variable:	Returns	No. Observations:	1484
Model:	ARIMA(7, 0, 2)	Log Likelihood	-2689.510
Date:	Thu, 02 May 2024	AIC	5401.020
Time:	03:05:13	BIC	5459.348
Sample:	0	HQIC	5422.761
	1 1 0 1		

- 1484

Covariance Type: opg

Covariance Type:			opg				
	coef	std err	z	P> z	[0.025	0.975]	
const	0.0585	0.040	1.447	0.148	-0.021	0.138	
ar.L1	-0.1683	0.060	-2.810	0.005	-0.286	-0.051	
ar.L2	-0.8721	0.063	-13.905	0.000	-0.995	-0.749	
ar.L3	-0.0307	0.029	-1.063	0.288	-0.087	0.026	
ar.L4	0.0176	0.028	0.627	0.531	-0.037	0.073	
ar.L5	0.0238	0.030	0.786	0.432	-0.036	0.083	
ar.L6	0.0287	0.022	1.281	0.200	-0.015	0.073	
ar.L7	0.0581	0.025	2.282	0.022	0.008	0.108	
ma.L1	0.1201	0.055	2.172	0.030	0.012	0.228	
ma.L2	0.8747	0.058	15.034	0.000	0.761	0.989	
sigma2	2.1961	0.053	41.209	0.000	2.092	2.301	
Ljung-Box	========= (L1) (Q):		0.00	Jarque-Bera	======================================	1370.8	
Prob(Q):			0.96	Prob(JB):		0.0	
Heteroskedasticity (H):			0.84	Skew:		0.2	
Prob(H) (to			0.06	Kurtosis:		7.6	

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

In [22]:

```
# Initialize an empty list to store results
results = []
```

```
for p in range (1, 15):
    for q in range (1, 15):
        try:
            # Fit the ARIMA model with the current p and q values
            model = ARIMA(ts['Returns'], order=(p, 0, q))
            model fit = model.fit()
            # Store p, q, and AIC values
            results.append((p, q, model fit.aic))
        except:
            # In case the model does not converge or other errors occur
            results.append((p, q, float('inf')))
# Print results
for p, q, aic in results:
    print(f'ARIMA({p}, 0, {q}) : AIC = {aic}')
ARIMA(1, 0, 1) : AIC = 5402.80234389899
ARIMA(1, 0, 2) : AIC = 5396.750865652479
ARIMA(1, 0, 3) : AIC = 5406.299832751347
ARIMA(1, 0, 4) : AIC = 5408.058980352547
ARIMA(1, 0, 5) : AIC = 5409.824994143258
ARIMA(1, 0, 6) : AIC = 5411.744783045005
ARIMA(1, 0, 7) : AIC = 5413.710019457894
ARIMA(1, 0, 8) : AIC = 5403.5864188165215
ARIMA(1, 0, 9) : AIC = 5400.591160948659
ARIMA(1, 0, 10) : AIC = 5402.271164369802
ARIMA(1, 0, 11) : AIC = 5395.173963708938
ARIMA(1, 0, 12) : AIC = 5397.011635015501
ARIMA(1, 0, 13) : AIC = 5403.347645193009
ARIMA(1, 0, 14) : AIC = 5404.7715348949205
ARIMA(2, 0, 1) : AIC = 5404.802334538377
ARIMA(2, 0, 2) : AIC = 5402.248045532302
ARIMA(2, 0, 3) : AIC = 5400.750577730124
ARIMA(2, 0, 4) : AIC = 5410.0347890804915
ARIMA(2, 0, 5) : AIC = 5404.667604331093
ARIMA(2, 0, 6) : AIC = 5406.408887022455
ARIMA(2, 0, 7) : AIC = 5400.835026748442
ARIMA(2, 0, 8) : AIC = 5401.945957885089
ARIMA(2, 0, 9) : AIC = 5398.49044484905
ARIMA(2, 0, 10) : AIC = 5400.489794372526
ARIMA(2, 0, 11) : AIC = 5400.488083602455
ARIMA(2, 0, 12) : AIC = 5402.351071754423
ARIMA(2, 0, 13) : AIC = 5400.325036864477
ARIMA(2, 0, 14) : AIC = 5402.309374017914
ARIMA(3, 0, 1) : AIC = 5406.377378871495
ARIMA(3, 0, 2) : AIC = 5402.855379323296
ARIMA(3, 0, 3) : AIC = 5403.481320146682
ARIMA(3, 0, 4) : AIC = 5405.988754466959
ARIMA(3, 0, 5) : AIC = 5410.151030802785
ARIMA(3, 0, 6) : AIC = 5403.621597457739
ARIMA(3, 0, 7) : AIC = 5402.535448530778
ARIMA(3, 0, 8) : AIC = 5393.061968070756
ARIMA(3, 0, 9) : AIC = 5398.697622743374
ARIMA(3, 0, 10) : AIC = 5397.122560664024
ARIMA(3, 0, 11) : AIC = 5399.086430930097
ARIMA(3, 0, 12) : AIC = 5403.742351728029
ARIMA(3, 0, 13) : AIC = 5400.850600780092
ARIMA(3, 0, 14) : AIC = 5399.483414550699
ARIMA(4, 0, 1) : AIC = 5408.1589023750175
ARIMA(4, 0, 2) : AIC = 5404.9153932984955
ARIMA(4, 0, 3) : AIC = 5405.310444903649
ARIMA(4, 0, 4) : AIC = 5400.748370931749
ARIMA(4, 0, 5) : AIC = 5397.642180173287
```

ARIMA(4, 0, 6): AIC = 5402.802126106476

ARIMA(4, 0, 7): AIC = 5404.1377752551925

ARIMA(4, 0, 8): AIC = 5402.1898831714025

ARIMA(4, 0, 9): AIC = 5390.388205356368

ARIMA(4, 0, 10): AIC = 5391.681500111064

ARIMA(4, 0, 11): AIC = 5393.389583070554

ARIMA(4, 0, 12): AIC = 5395.581397340809

ARIMA(4, 0, 13): AIC = 5397.12843165296

ARIMA(4, 0, 14): AIC = 5399.007912655397

```
ARIMA(5, 0, 1) : AIC = 5409.940242156227
ARIMA(5, 0, 2) : AIC = 5404.551390209662
ARIMA(5, 0, 3) : AIC = 5406.199406234916
ARIMA(5, 0, 4) : AIC = 5403.203374298048
ARIMA(5, 0, 5) : AIC = 5402.629861531252
ARIMA(5, 0, 6) : AIC = 5404.36840773771
ARIMA(5, 0, 7) : AIC = 5408.119822953384
ARIMA(5, 0, 8) : AIC = 5404.284291880551
ARIMA(5, 0, 9) : AIC = 5392.5192072128675
ARIMA(5, 0, 10) : AIC = 5393.961313107182
ARIMA(5, 0, 11) : AIC = 5395.149904617383
ARIMA(5, 0, 12) : AIC = 5397.598601195038
ARIMA(5, 0, 13) : AIC = 5399.123981301581
ARIMA(5, 0, 14) : AIC = 5398.533569119739
ARIMA(6, 0, 1) : AIC = 5411.900797821638
ARIMA(6, 0, 2) : AIC = 5402.772287403706
ARIMA(6, 0, 3) : AIC = 5403.3235112440925
ARIMA(6, 0, 4) : AIC = 5407.836240948345
ARIMA(6, 0, 5) : AIC = 5407.645866007526
ARIMA(6, 0, 6) : AIC = 5406.092646966501
ARIMA(6, 0, 7) : AIC = 5410.668540076749
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ARIMA(6, 0, 9) : AIC = 5393.502109978785
ARIMA(6, 0, 10) : AIC = 5395.226844255676
ARIMA(6, 0, 11) : AIC = 5397.985779449053
ARIMA(6, 0, 12) : AIC = 5399.183703554676
ARIMA(6, 0, 13) : AIC = 5394.949630898898
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ARIMA(7, 0, 2) : AIC = 5401.020212336962
ARIMA(7, 0, 3) : AIC = 5401.370877779882
ARIMA(7, 0, 4) : AIC = 5414.752772768743
ARIMA(7, 0, 5) : AIC = 5404.280382496303
ARIMA(7, 0, 6) : AIC = 5403.461414978077
ARIMA(7, 0, 7) : AIC = 5408.947474066128
ARIMA(7, 0, 8) : AIC = 5402.756994394405
ARIMA(7, 0, 9) : AIC = 5388.684198923897
ARIMA(7, 0, 10) : AIC = 5390.750203209266
ARIMA(7, 0, 11) : AIC = 5395.169902889234
ARIMA(7, 0, 12) : AIC = 5396.503524972659
ARIMA(7, 0, 13) : AIC = 5394.565911554795
ARIMA(7, 0, 14) : AIC = 5395.355678805094
ARIMA(8, 0, 1) : AIC = 5403.893728890186
ARIMA(8, 0, 2) : AIC = 5401.816761218195
ARIMA(8, 0, 3) : AIC = 5392.835001380319
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ARIMA(8, 0, 5) : AIC = 5407.5883622452275
ARIMA(8, 0, 6) : AIC = 5413.8806516615605
ARIMA(8, 0, 7) : AIC = 5405.717104003339
ARIMA(8, 0, 8) : AIC = 5404.459638363558
ARIMA(8, 0, 9) : AIC = 5396.9470350476195
ARIMA(8, 0, 10) : AIC = 5390.817023426845
ARIMA(8, 0, 11) : AIC = 5394.146624665469
ARIMA(8, 0, 12) : AIC = 5397.604061110516
ARIMA(8, 0, 13) : AIC = 5402.86963343356
ARIMA(8, 0, 14) : AIC = 5398.26828553105
ARIMA(9, 0, 1) : AIC = 5400.293735111799
ARIMA(9, 0, 2) : AIC = 5398.549009715448
ARIMA(9, 0, 3) : AIC = 5397.2667209587735
ARIMA(9, 0, 4) : AIC = 5391.027809960479
ARIMA(9, 0, 5) : AIC = 5393.179272745818
ARIMA(9, 0, 6) : AIC = 5396.223343965018
ARIMA(9, 0, 7) : AIC = 5390.866465419775
ARIMA(9, 0, 8) : AIC = 5396.633763682458
ARIMA(9, 0, 9) : AIC = 5398.4814382524455
ARIMA(9, 0, 10) : AIC = 5391.636900062089
ARIMA(9, 0, 11) : AIC = 5395.811560903115
ARIMA(9, 0, 12) : AIC = 5397.04035670869
ARIMA(9, 0, 13) : AIC = 5396.304868756625
ARIMA(9, 0, 14) : AIC = 5397.202459144968
ARIMA(10, 0, 1) : AIC = 5402.080377265192
ARIMA(10, 0, 2) : AIC = 5400.444867568017
```

ARIMA(10,	0,	3) : AIC = 5398.374464575117
ARIMA(10,	Ο,	4) : AIC = 5390.829398326914
ARIMA(10,	0,	5) : AIC = 5393.408421374298
ARIMA(10,	0,	6) : AIC = 5398.436256174442
ARIMA(10,	Ο,	7) : AIC = 5393.86791008232
ARIMA(10,	0,	8) : AIC = 5398.716093066838
ARIMA(10,	Ο,	9) : AIC = 5400.682441467256
ARIMA(10,	0,	10) : AIC = 5401.7544151966185
ARIMA(10,	0,	11) : AIC = 5404.7996917978035
ARIMA(10,	Ο,	12) : AIC = 5405.061742544686
ARIMA(10,	Ο,	13) : AIC = 5396.902239550642
ARIMA(10,	Ο,	14) : AIC = 5399.826581722281
ARIMA(11,		1) : AIC = 5404.079173596253
ARIMA(11,	0,	2) : AIC = 5399.870689617061
ARIMA(11,	Ο,	3) : AIC = 5399.979936451011
ARIMA(11,	Ο,	4) : AIC = 5392.676654943945
ARIMA(11,	Ο,	5) : AIC = 5395.2017435721955
ARIMA(11,	Ο,	6) : AIC = 5397.897032776667
ARIMA(11,	Ο,	7) : AIC = 5397.960135470588
ARIMA(11,	Ο,	8) : AIC = 5401.14267563801
ARIMA(11,	Ο,	9) : AIC = 5404.120865181905
ARIMA(11,	Ο,	10) : AIC = 5404.649489205936
ARIMA(11,	Ο,	11) : AIC = 5419.8356786522045
ARIMA(11,	Ο,	12) : AIC = 5406.149346825049
ARIMA(11,	Ο,	13) : AIC = 5411.243895880277
ARIMA(11,	Ο,	14) : AIC = 5400.840581201006
ARIMA(12,	Ο,	1) : AIC = 5396.879784635505
ARIMA(12,	Ο,	2) : AIC = 5401.868274305048
ARIMA(12,	Ο,	3) : AIC = 5401.493622139562
ARIMA(12,	0,	4) : AIC = 5395.257109020221
ARIMA(12,	0,	5) : AIC = 5397.082365723956
ARIMA (12,	0,	6) : AIC = 5401.706640794462
ARIMA (12,	0,	7) : AIC = 5396.091895418908
ARIMA (12,	0,	8) : AIC = 5415.354451530724 9) : AIC = 5403.964852502593
ARIMA(12, ARIMA(12,	0, 0,	9) : AIC = 5403.964852502593 10) : AIC = 5404.899922601615
ARIMA(12,		
ARIMA(12, ARIMA(12,		·
ARIMA(12,		
ARIMA(12,		
ARIMA(13,		1) : AIC = 5403.545844438279
ARIMA(13,		2) : AIC = 5401.49906971969
	Ο,	3) : AIC = 5399.446363427149
ARIMA(13,	Ο,	4) : AIC = 5397.06682176508
ARIMA(13,	Ο,	5) : AIC = 5399.635837241296
ARIMA(13,	Ο,	6) : AIC = 5402.126102380351
ARIMA(13,	Ο,	7) : AIC = 5397.296602427205
ARIMA(13,		8) : AIC = 5402.559013827829
ARIMA(13,		9) : AIC = 5405.924457814676
ARIMA(13,		10) : AIC = 5407.582702050658
ARIMA (13,		11) : AIC = 5409.518720616096
ARIMA (13,		
ARIMA (13,		
ARIMA (13,		14) : AIC = 5404.84766351795
ARIMA(14,	0,	1): AIC = 5404.780132348459 2): AIC = 5402.81819110992
	0,	
	0, 0,	3) : AIC = 5404.742052922873 4) : AIC = 5400.973832916306
	0,	5) : AIC = 5400.7325787648715
ARIMA(14,		6) : AIC = 5405.922767816388
ARIMA (14,		7) : AIC = 5401.361873813972
ARIMA(14,		8) : AIC = 5404.632041836703
ARIMA(14,		
ARIMA(14,		
ARIMA(14,		
	,	
		12) : AIC = 5412.483109112428
ARIMA(14,	0, 0,	12) : AIC = 5412.483109112428 13) : AIC = 5413.2632928699195
ARIMA(14,	0, 0,	12) : AIC = 5412.483109112428

```
lowest_aic = min(results, key=lambda x: x[2])
# Print the result
lowest_aic_p, lowest_aic_q, lowest_aic_value = lowest_aic
print(f"Lowest AIC is {lowest_aic_value} for ARMA({lowest_aic_p}, {lowest_aic_q})")
```

Lowest AIC is 5388.684198923897 for ARMA(7, 9)

After some hassle I got the best ARMA model as ARMA(7,9) based on the lowest AIC.

```
In [24]:
```

Covariance Type:

```
# ARMA model with lowest aic
order = (lowest_aic_p,0, lowest_aic_q)
model_arma_lowest_aic = ARIMA(ts, order=order)
results_arma_lowest_aic = model_arma_lowest_aic.fit()
# Print results
print(results_arma_lowest_aic.summary())
```

SARIMAX Results

Dep. Variable:	Returns	No. Observations:	1484
Model:	ARIMA(7, 0, 9)	Log Likelihood	-2676.342
Date:	Thu, 02 May 2024	AIC	5388.684
Time:	03:29:25	BIC	5484.129
Sample:	0	HQIC	5424.260

- 1484 opa

Covariance	Type:		opg			
	coef	std err		P> z	[0.025	0.975]
const	0.0612	0.016	3.788	0.000	0.030	0.093
ar.L1	-0.2166	0.205	-1.059	0.290	-0.617	0.184
ar.L2	-0.0020	0.187	-0.011	0.992	-0.369	0.365
ar.L3	-0.1051	0.176	-0.598	0.550	-0.450	0.240
ar.L4	0.5497	0.098	5.633	0.000	0.358	0.741
ar.L5	0.2036	0.172	1.186	0.236	-0.133	0.540
ar.L6	-0.1629	0.176	-0.928	0.354	-0.507	0.181
ar.L7	0.4698	0.176	2.664	0.008	0.124	0.815
ma.L1	0.1667	0.205	0.813	0.416	-0.235	0.569
ma.L2	-0.0113	0.181	-0.062	0.950	-0.367	0.344
ma.L3	0.1160	0.172	0.673	0.501	-0.222	0.454
ma.L4	-0.5512	0.089	-6.186	0.000	-0.726	-0.377
ma.L5	-0.1791	0.170	-1.051	0.293	-0.513	0.155
ma.L6	0.1851	0.174	1.065	0.287	-0.156	0.526
ma.L7	-0.5086	0.179	-2.845	0.004	-0.859	-0.158
ma.L8	-0.0173	0.028	-0.617	0.537	-0.072	0.038
ma.L9	-0.0976	0.027	-3.626	0.000	-0.150	-0.045
sigma2	2.1566	0.050	43.224	0.000	2.059	2.254
Ljung-Box	========= (L1) (Q):		0.02	Jarque-Bera	======================================	1360.

=======================================		=======================================	=======
Ljung-Box (L1) (Q):	0.02	Jarque-Bera (JB):	1360.09
Prob(Q):	0.90	Prob(JB):	0.00
Heteroskedasticity (H):	0.86	Skew:	0.10
<pre>Prob(H) (two-sided):</pre>	0.09	Kurtosis:	7.69

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

Residual Analysis

```
In [25]:
```

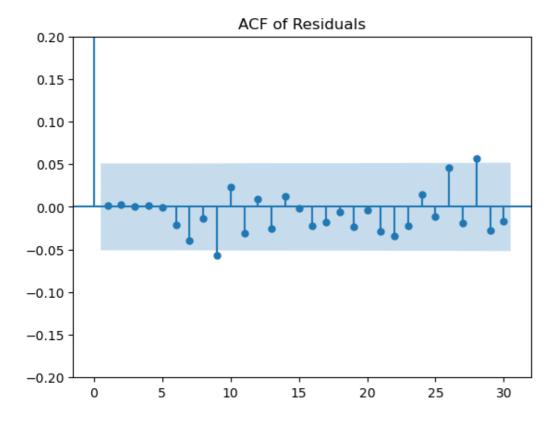
```
# ACF and PACF plots for the residuals
plot_acf(residuals, lags = 30);
plt.ylim(-0.2,0.2)
plt.title('ACF of Residuals')

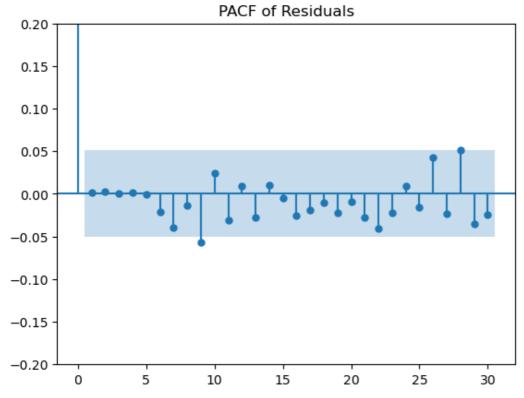
plot_pacf(residuals, lags=30);
```

```
plt.ylim(-0.2,0.2)
plt.title('PACF of Residuals')
```

Out[25]:

Text(0.5, 1.0, 'PACF of Residuals')





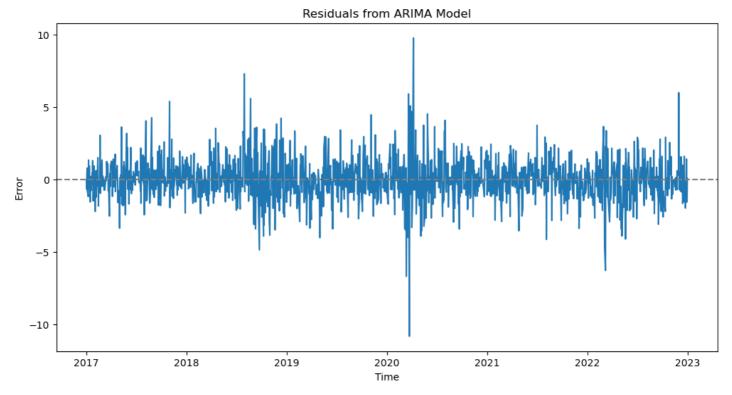
Almost all lags are inside confidence interval

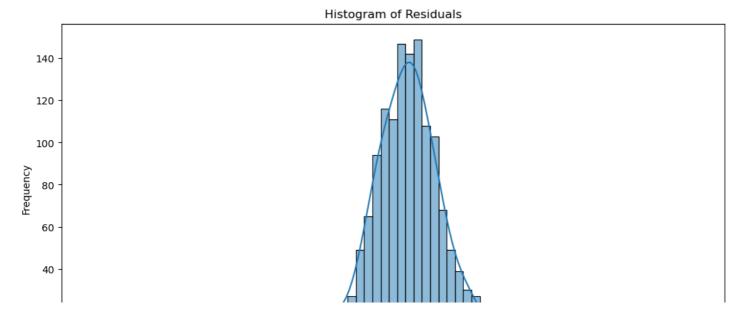
```
In [26]:
```

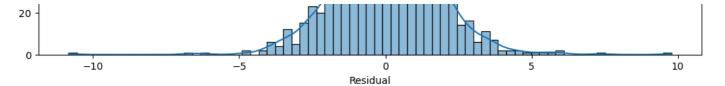
```
import statsmodels.api as sm
from scipy import stats
import matplotlib.pyplot as plt

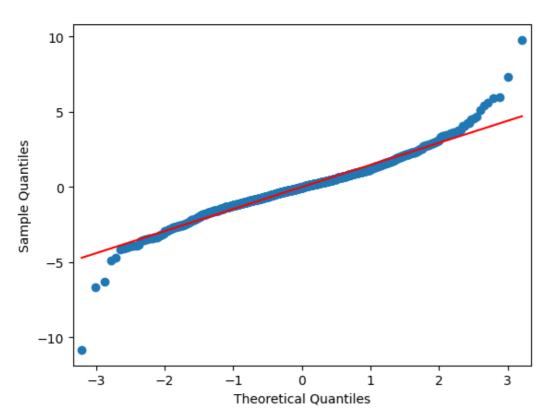
new_order = (7, 0, 9)
```

```
model refined = ARIMA(ts, order=new order)
results_refined = model_refined.fit()
# Model Diagnostics
residuals = results refined.resid
# Plot residual errors
plt.figure(figsize=(12, 6))
plt.plot(residuals)
plt.title('Residuals from ARIMA Model')
plt.xlabel('Time')
plt.ylabel('Error')
plt.axhline(0, linestyle='--', color='grey')
plt.show()
# Histogram of the residuals
plt.figure(figsize=(12, 6))
sns.histplot(residuals, kde=True)
plt.title('Histogram of Residuals')
plt.xlabel('Residual')
plt.ylabel('Frequency')
plt.show()
# Q-Q plot
sm.qqplot(residuals, line='s')
plt.show()
```









From the residual plot I can say that there are some periods where the residuals exhibit clustering, indicating phases of higher or lower volatility and also there are a few noticeable spikes, particularly around 2020 indicating outliers.

The Histogram almost looks normaly distributed.

For the Q-Q plot the residuals roughly follow the red line in the middle range but deviate at the tails. This indicates that the residuals are not perfectly normally distributed especially in the low and high values. The points deviate significantly from the line at both ends which means the presence of fat tails.

```
In [27]:
```

```
from statsmodels.stats.diagnostic import acorr_ljungbox
import matplotlib.pyplot as plt

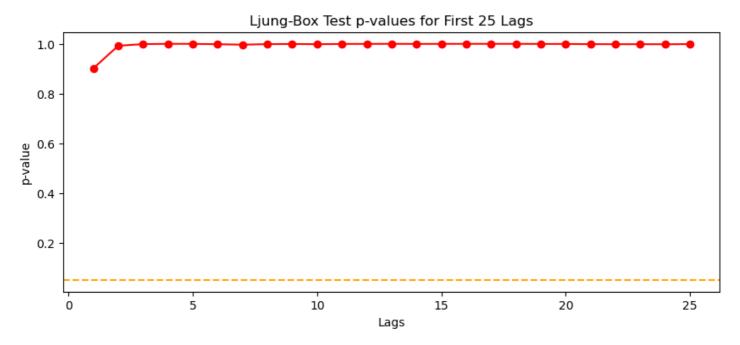
ljung_box_results = acorr_ljungbox(residuals, lags=25, return_df=True)

# Print the results
print(ljung_box_results)

# Plotting the Ljung-Box test p-values
plt.figure(figsize=(10, 4))
plt.plot(ljung_box_results['lb_pvalue'], marker='o', linestyle='-', color='red')
plt.title('Ljung-Box Test p-values for First 25 Lags')
plt.xlabel('Lags')
plt.ylabel('p-value')
plt.axhline(y=0.05, color='orange', linestyle='--') # significance line at p = 0.05
plt.show()
```

```
lb stat
               lb pvalue
1
    0.015407
                0.901216
2
    0.015550
                0.992255
3
    0.026794
                0.998843
    0.027181
                0.999908
5
    0.104061
                0.999821
```

```
6
    0.445925
                0.998436
7
    0.881197
                0.996524
8
    0.908812
                0.998761
9
    1.008531
                0.999418
10
    1.637731
                0.998438
11
    1.641909
                0.999410
12
                0.999703
    1.750939
13
    1.756485
                0.999892
14
    2.663878
                0.999535
15
    2.792380
                0.999743
16
    2.836102
                0.999884
17
    3.186230
                0.999893
18
    3.695923
                0.999867
19
    4.876459
                0.999526
20
   5.566965
                0.999369
   6.641558
                0.998746
21
22
    7.389885
                0.998444
23
    7.880760
                0.998556
24
   8.676179
                0.998210
25
   8.682269
                0.998967
```



The Ljung-Box test results show that all the p-values are well above the 0.05 significance level across all 25 lags, indicating that there is no autocorrelation that can be seen amongst the residuals.

```
In [28]:
```

```
from scipy import stats
# Shapiro-Wilk test for normality
shapiro test = stats.shapiro(residuals)
# Print results and hypothesis information
print(f'Shapiro-Wilk test statistic: {shapiro test[0]:.4f}, p-value: {shapiro test[1]:.4f
}')
# Hypotheses
print("\nHypotheses:")
print("Null Hypothesis (H0): The data is normally distributed.")
print("Alternative Hypothesis (Ha): The data is not normally distributed.")
# Interpretation
if shapiro test[1] < 0.05:</pre>
    print("\nReject the null hypothesis (H0), suggesting the data is not normally distrib
uted.")
else:
   print("\nFailed to reject the null hypothesis (HO), suggesting the data is normally d
```

```
istributed.")
Shapiro-Wilk test statistic: 0.9601, p-value: 0.0000
```

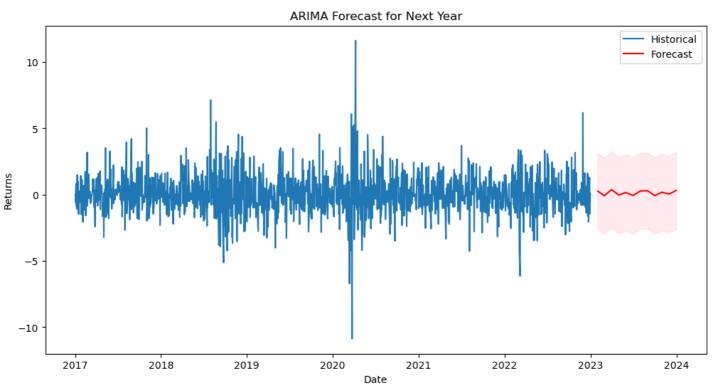
Hypotheses: Null Hypothesis (H0): The data is normally distributed. Alternative Hypothesis (Ha): The data is not normally distributed.

Reject the null hypothesis (H0), suggesting the data is not normally distributed.

Forecasting

In [29]:

```
# Forecast the next 12 periods ahead in the future
forecast_steps = 12
forecast = results refined.get forecast(steps=forecast steps)
forecast mean = forecast.predicted mean
forecast conf int = forecast.conf int()
last date = ts.index[-1]
forecast dates = pd.date range(start=last date, periods=forecast steps + 1, freq='M')[1:
# Assign the new date range as the index of the forecasted data
forecast_mean.index = forecast dates
forecast conf int.index = forecast dates
# Plot the forecast alongside the historical data
plt.figure(figsize=(12, 6))
plt.plot(ts.index, ts['Returns'], label='Historical')
plt.plot(forecast mean.index, forecast mean, color='red', label='Forecast')
plt.fill between (forecast conf int.index,
                 forecast conf int.iloc[:, 0],
                 forecast conf int.iloc[:, 1], color='pink', alpha=0.3)
plt.title('ARIMA Forecast for Next Year')
plt.xlabel('Date')
plt.ylabel('Returns')
plt.legend()
plt.show()
```



After performing forecasts using the ARIMA model, I plan to further enhance our analysis by applying a GARCH model to the residuals. This approach will allow us to investigate any potential volatility clustering in the time series data, providing a more nuanced understanding of variability in the model's errors over time.

GARCH model

```
In [30]:
```

```
from statsmodels.graphics.tsaplots import plot_acf

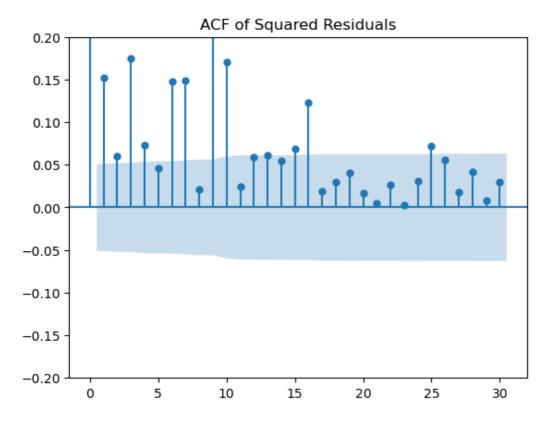
squared_residuals = residuals**2

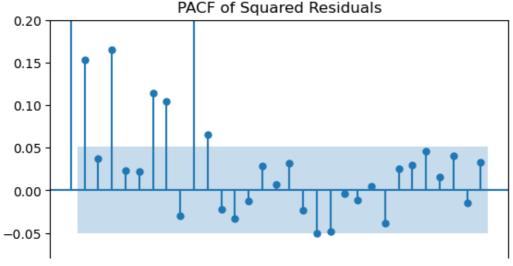
plot_acf(squared_residuals, alpha=0.05, lags = 30);
plt.ylim(-0.2,0.2)
plt.title('ACF of Squared Residuals')

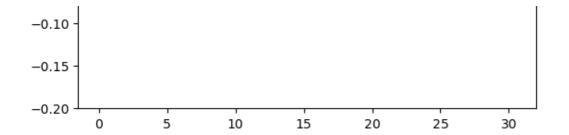
plot_pacf(squared_residuals, alpha=0.05, lags = 30);
plt.ylim(-0.2,0.2)
plt.title('PACF of Squared Residuals')
```

Out[30]:

Text(0.5, 1.0, 'PACF of Squared Residuals')







Best GARCH model

GARCH(3,3): AIC = 8375.547143550306

```
In [31]:
```

```
from arch import arch model
import numpy as np
squared residuals = residuals ** 2 # Using squared residuals
# Define the range of p and q values to explore
p_range = range(1, 6)
q_range = range(1, 6)
best aic = np.inf
best order = None
best model = None
                # List to store AIC values and corresponding orders
aic values = []
# Grid search over different combinations of p and q for the GARCH model
for p in p range:
    for q in q range:
        try:
            # Specify the GARCH model using the squared residuals
            model = arch model(squared residuals, mean='Zero', vol='GARCH', p=p, q=q)
            # Fit the model
            model fit = model.fit(disp='off', show warning=False)
            # Save the AIC and order
            aic values.append((p, q, model fit.aic))
            # Compare AIC
            if model fit.aic < best aic:</pre>
                best aic = model fit.aic
                best order = (p, q)
                best model = model fit
        except Exception as e:
            print(f'Error fitting GARCH({p}, {q}):', str(e))
# Output all AIC values with their corresponding models
for order in aic values:
    print(f'GARCH({order[0]}, {order[1]}) : AIC = {order[2]}')
# Output the results of the grid search
if best order:
   print(f'\nBest GARCH model order: p={best order[0]}, q={best order[1]} with AIC: {bes
t aic}')
   print(best model.summary())
else:
   print("\nNo suitable GARCH model was found.")
GARCH(1,1): AIC = 8406.712273976093
GARCH(1,2): AIC = 8408.71219033534
GARCH(1,3) : AIC = 8409.012994147526
GARCH(1,4) : AIC = 8402.184983991296
GARCH(1,5) : AIC = 8397.95020857262
GARCH(2,1) : AIC = 8408.712273423294
GARCH(2,2): AIC = 8410.662853402247
GARCH(2,3) : AIC = 8406.185959364768
GARCH(2,4) : AIC = 8390.969075917903
GARCH(2,5) : AIC = 8392.27674980971
GARCH(3,1) : AIC = 8410.712273486826
GARCH(3,2): AIC = 8373.673070934725
```

```
GARCH(3,4) : AIC = 8382.546269503458
GARCH(3,5) : AIC = 8384.546269424083
GARCH(4,1) : AIC = 8373.67307104133
GARCH(4,2) : AIC = 8375.67307063462
GARCH(4,3) : AIC = 8377.547143435753
GARCH(4,4) : AIC = 8384.54626913178
GARCH(4,5) : AIC = 8381.547145275976
GARCH(5,1) : AIC = 8414.71227355095
GARCH(5,2) : AIC = 8377.673070525067
GARCH(5,3) : AIC = 8379.439969170055
GARCH(5,4): AIC = 8382.624636696317
GARCH(5,5) : AIC = 8384.624638253168
Best GARCH model order: p=3, q=2 with AIC: 8373.673070934725
                Zero Mean - GARCH Model Results
______
Dep. Variable:
                        None
                             R-squared:
                    Zero Mean Adj. R-squared:
GARCH Log-Likelihood:
Mean Model:
                                                       0.001
Vol Model:
                                                    -4180.84
Distribution: Normal AIC: Method: Maximum Likelihood BIC:
                                                     8373.67
                                                     8405.49
                              No. Observations:
                                                        1484
Date:
              Thu, May 02 2024 Df Residuals:
                                                        1484
                03:30:00 Df Model:
Time:
                      Volatility Model
_____
            coef std err t P>|t| 95.0% Conf. Int.
______
          9.2001 1.661 5.537 3.070e-08 [ 5.944, 12.457]
alpha[1]
          0.2724
                   0.129
                            2.116 3.432e-02
                                           [2.012e-02, 0.525]
        alpha[2]
alpha[3]
beta[1] 2.1844e-10 4.794e-02 4.557e-09 1.000 [-9.395e-02,9.395e-02]
beta[2] 2.1370e-10 6.082e-02 3.514e-09 1.000 [-0.119, 0.119]
_____
```

Covariance estimator: robust

Residual Analysis using GARCH

```
In [43]:
```

```
import matplotlib.pyplot as plt
from statsmodels.graphics.tsaplots import plot acf
# Get standardized residuals from the GARCH model
std resid = best model.resid / best model.conditional volatility
# Get squared standardized residuals
squared std resid = std resid**2
# Plot standardized residuals
plt.figure(figsize=(10, 4))
plt.plot(std resid, color='blue')
plt.title('Standardized Residuals from GARCH Model')
plt.axhline(0, linestyle='--', color='black')
plt.show()
# Plot ACF of standardized residuals
plot acf(std resid, alpha=0.05, title='ACF of Standardized Residuals')
plt.ylim(-0.2, 0.2)
plt.show()
# Plot ACF of squared standardized residuals
plot acf(squared std resid, alpha=0.05, title='ACF of Squared Standardized Residuals')
plt.\overline{y}lim(-0.2, 0.\overline{2})
plt.show()
# Perform Shapiro-Wilk test of normality on the standardized residuals
from scipy import stats
```

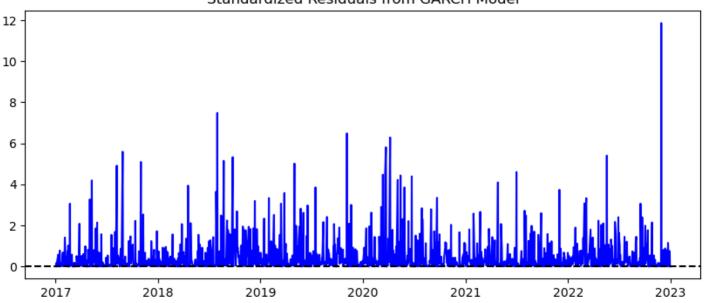
```
# Shapiro-Wilk test for normality
shapiro_test = stats.shapiro(std_resid)

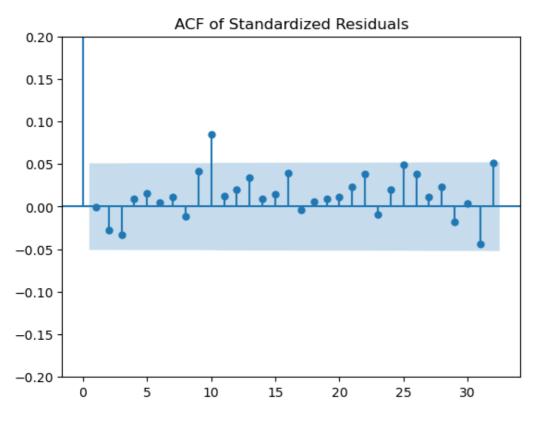
# Print results and hypothesis information
print(f'Shapiro-Wilk test statistic: {shapiro_test[0]:.4f}, p-value: {shapiro_test[1]:.4f}
}')

# Hypotheses
print("\nHypotheses:")
print("Null Hypothesis (H0): The data is normally distributed.")
print("Alternative Hypothesis (Ha): The data is not normally distributed.")

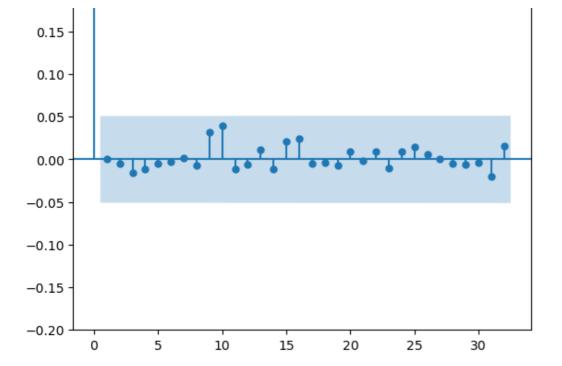
# Interpretation
if shapiro_test[1] < 0.05:
    print("\nReject the null hypothesis (H0), suggesting the data is not normally distributed.")
else:
    print("\nFailed to reject the null hypothesis (H0), suggesting the data is normally distributed.")</pre>
```

Standardized Residuals from GARCH Model





ACF of Squared Standardized Residuals



Shapiro-Wilk test statistic: 0.5532, p-value: 0.0000

Hypotheses:

Null Hypothesis (H0): The data is normally distributed. Alternative Hypothesis (Ha): The data is not normally distributed.

Reject the null hypothesis (HO), suggesting the data is not normally distributed.

In [44]:

```
from statsmodels.stats.diagnostic import acorr_ljungbox
import matplotlib.pyplot as plt

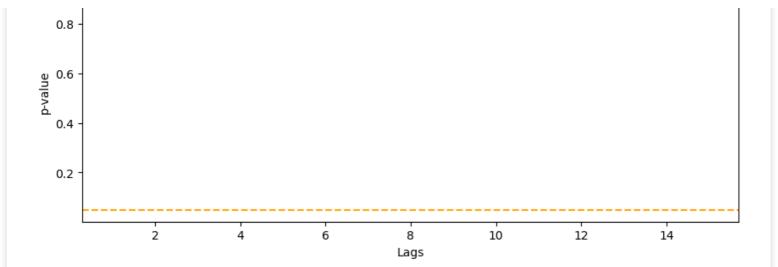
ljung_box_results = acorr_ljungbox(squared_std_resid, lags=15, return_df=True)

# Print the results
print(ljung_box_results)

# Plotting the Ljung-Box test p-values
plt.figure(figsize=(10, 4))
plt.plot(ljung_box_results['lb_pvalue'], marker='o', linestyle='-', color='red')
plt.title('Ljung-Box Test p-values for First 15 Lags')
plt.xlabel('Lags')
plt.ylabel('p-value')
plt.axhline(y=0.05, color='orange', linestyle='--') # significance line at p = 0.05
plt.show()
```

```
lb stat
              lb_pvalue
1
    0.000921
               0.975785
2
    0.036925
               0.981707
3
    0.392294
               0.941830
4
    0.592917
               0.963848
5
    0.624372
               0.986860
    0.633985
               0.995806
7
    0.639435
               0.998759
8
               0.999470
    0.721465
9
    2.226329
               0.987362
               0.921528
   4.508122
10
    4.696556
11
               0.944967
12
    4.757892
               0.965580
13
    4.964263
               0.975971
14
   5.166501
                0.983358
15
   5.826536
                0.982516
```

Ljung-Box Test p-values for First 15 Lags



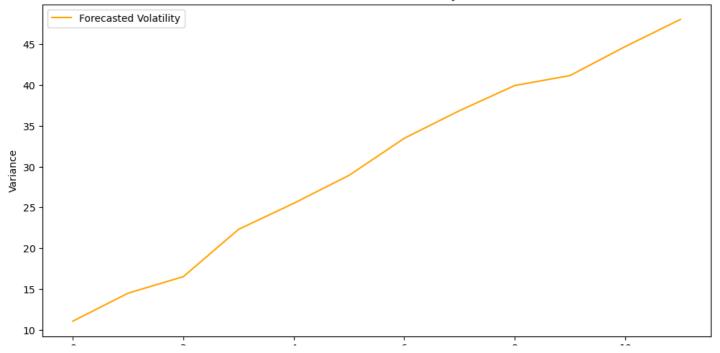
The Ljung-Box test results above suggest that there is no significant autocorrelation in the squared standardized residuals for the first 15 lags, as all p-values are well above the 0.05 significance level.

Forecasting the Volatility

```
In [37]:
```

```
# Forecast future volatility
forecasts = best model.forecast(horizon=forecast steps, start=None, method='simulation',
simulations=1000)
# Extract the forecasted variance
future volatility = forecasts.variance[-1:]
# Plot the forecasted volatility
plt.figure(figsize=(12, 6))
plt.plot(future volatility.values.flatten(), color='orange', label='Forecasted Volatility
plt.title('Forecasted Future Volatility')
plt.xlabel('Time')
plt.ylabel('Variance')
plt.legend()
plt.show()
# Display the last forecasted variance
print("Forecasted Variance:")
print(future volatility)
```

Forecasted Future Volatility



10

The forecast shows that the expected future changes or volatility in the data are likely to increase over time. This means we might see bigger ups and downs in the future. Understanding this helps us prepare for more unpredictable changes and manage risks better.

Forecating using ARIMA-GARCH

```
In [38]:
```

```
from arch import arch model
import pandas as pd
import matplotlib.pyplot as plt
# Fit the ARIMA model
arima model = ARIMA(ts, order=(7,0,9))
arima results = arima model.fit()
# Forecast future values with ARIMA
arima forecast = arima results.get forecast(steps=forecast steps)
forecast mean = arima forecast.predicted mean
forecast std = arima forecast.se mean
# Fit the GARCH model
garch model = arch model(arima results.resid, p=3, q=2)
garch results = garch model.fit(update freq=10)
# Forecast future volatility with GARCH
garch forecast = garch results.forecast(horizon=forecast steps)
forecast var = garch forecast.variance.values[-1]
# Combine the ARIMA and GARCH forecasts
forecast combined var = forecast std**2 + forecast var
# Now, forecast combined var contains the forecasted variance for the ARIMA-GARCH model
lower_bound = forecast_mean - 1.96 * np.sqrt(forecast_combined_var)
upper_bound = forecast_mean + 1.96 * np.sqrt(forecast_combined_var)
# Generate future dates
future dates = pd.date range(start=ts.index[-1], periods=forecast steps, freq='M')
# Plot the historical returns
plt.plot(ts.index, ts, label='Historical Returns')
# Plot the forecasted returns
plt.plot(future dates, forecast mean, color='red', label='Forecasted Returns')
# Plot the forecasted volatility (95% prediction interval)
plt.fill between (future dates, lower bound, upper bound, color='pink', alpha=0.3, label=
'95% Prediction Interval')
# Show the plot
plt.legend()
plt.title('ARIMA-GARCH Forecast of Returns')
plt.xlabel('Date')
plt.ylabel('Returns')
plt.show()
```

Iteration: 10, Func. Count: 93, Neg. LLF: 2591.1412996279223 Iteration: 20, Func. Count: 178, Neg. LLF: 2591.0733425361486

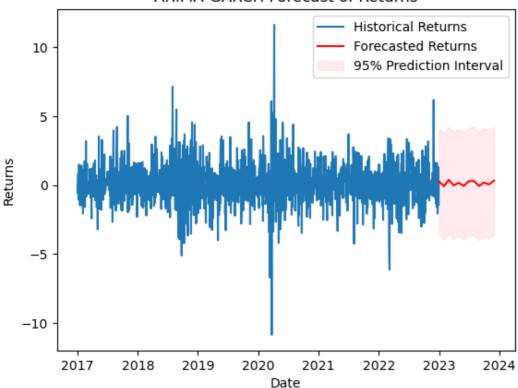
Optimization terminated successfully (Exit mode 0)

Current function value: 2590.949167266409

Iterations: 25

Function evaluations: 221 Gradient evaluations: 25

ARIMA-GARCH Forecast of Returns



Conclusion

In this project, we utilized advanced forecasting techniques to analyze financial data, identifying the best GARCH model with parameters (3,2) for predicting future volatility. Simultaneously, we selected an ARMA model with parameters (7,9) for the returns data. By integrating these models into an ARIMA-GARCH framework, we effectively captured both the trends and variability in the data, offering a comprehensive view of the market dvnamics.

This combined approach allowed us to generate detailed predictions that included confidence intervals, illustrating the potential future values and the associated uncertainties. The successful application of these techniques provides valuable insights for financial planning and risk management, demonstrating the critical role of appropriate model selection in understanding complex financial behaviors.