

## Offline Problem | CSE 208 | MST

### Instructions:

- (1) \* Please DO NOT COPY solutions from anywhere (your friends, seniors, internet etc.). Any form of plagiarism (irrespective of source or destination), will result in getting -100% marks in the online/offline.
- (2) Deadline: 4th December 11:59 PM
- (3) Rename all the problem solutions according to your rule. If your rule is 2005XXX, then create a folder named 2005XXX. Afterward, rename problem 1 as 2005XXX\_problem1.cpp, and similarly, rename the others. Next, move all the solutions inside the folder. Create a zip file of that folder. Lastly, submit the zip file.
- (4) You get 10 marks for each right answer. A viva will also be conducted. If the teacher finds that you don't know how to implement it, you'll get a score of 0.

### Offline Problem 1:

Find all possible MST of a given graph.

### Input

The first line contains two integers  $n$  and  $m$  — the number of the graph's vertices and edges, correspondingly. Then follow  $m$  lines, each of them contains three integers — the description of the graph's edges as " $a_i b_i w_i$ " where  $a_i$  and  $b_i$  are the numbers of vertices connected by the  $i$ -th edge,  $w_i$  is the edge's weight. It is guaranteed that the graph is connected and doesn't contain loops or multiple edges.

### Output

Print All the edges for each possible MST.

### Examples

| Input  | Output  |
|--|---|
| 5 10<br>0 1 1<br>2 4 1<br>1 2 2<br>0 4 2<br>3 4 3<br>0 3 5<br>1 4 6<br>2 3 8<br>0 2 9<br>1 3 9 | MSTs:<br>1 : [[0, 1, 1], [2, 4, 1], [1, 2, 2], [3, 4, 3]]<br>2 : [[0, 1, 1], [2, 4, 1], [0, 4, 2], [3, 4, 3]] |

|  |  |
|--|--|
| 1 3 9  |  |
| 7 12<br>3 4 1<br>1 5 1<br>1 4 1<br>0 6 4<br>2 3 8<br>4 5 8<br>2 6 10<br>0 5 10<br>3 6 10<br>1 6 10<br>1 3 12<br>3 5 12 | <b>MSTs:</b><br><b>1</b> : [[3, 4, 1], [1, 5, 1], [1, 4, 1], [0, 6, 4], [2, 3, 8], [2, 6, 10]]<br><b>2</b> : [[3, 4, 1], [1, 5, 1], [1, 4, 1], [0, 6, 4], [2, 3, 8], [0, 5, 10]]<br><b>3</b> : [[3, 4, 1], [1, 5, 1], [1, 4, 1], [0, 6, 4], [2, 3, 8], [3, 6, 10]]<br><b>4</b> : [[3, 4, 1], [1, 5, 1], [1, 4, 1], [0, 6, 4], [2, 3, 8], [1, 6, 10]] |

## Offline Problem 2:

You are given a connected weighted undirected graph without any loops and multiple edges. Your task is to determine the following for each edge of the given graph: whether it is either included in all possible MST(s), or included at least in one MST, or not included in any MST.

## Input

The first line contains two integers  $n$  and  $m$  — the number of the graph's vertices and edges, correspondingly. Then follow  $m$  lines, each of them contains three integers — the description of the graph's edges as " $a_i b_i w_i$ " where  $a_i$  and  $b_i$  are the numbers of vertices connected by the  $i$ -th edge,  $w_i$  is the edge's weight. It is guaranteed that the graph is connected and doesn't contain loops or multiple edges.

## Output

Print  $m$  lines — the answers for all edges. If the  $i$ -th edge is included in any MST, print "any"; if the  $i$ -th edge is included at least in one MST, print "at least one"; if the  $i$ -th edge isn't included in any MST, print "none". Print the answers for the edges in the order in which the edges are specified in the input.

## Examples

| Input  | Output   |
|--|--|
| 4 5<br>1 2 101<br>1 3 100<br>2 3 2<br>2 4 2<br>3 4 1 | none<br>any<br>at least one<br>at least one<br>any |
| 3 3<br>1 2 1<br>2 3 1<br>1 3 2                       | any<br>any<br>none                                 |

### Offline Problem 3:

Given a weighted undirected connected graph with  $n$  vertices numbered from 0 to  $n - 1$ , and an array of edges where  $\text{edges}[i] = [a_i, b_i, \text{weight}_i]$  represents a bidirectional and weighted edge between nodes  $a_i$  and  $b_i$ . A minimum spanning tree (MST) is a subset of the graph's edges that connects all vertices without cycles and with the minimum possible total edge weight.

Find all the critical and pseudo-critical edges in the given graph's minimum spanning tree (MST). An MST edge whose deletion from the graph would cause the MST weight to increase is called a **critical edge**. On the other hand, a pseudo-critical edge is that which can appear in some MSTs but not all.

### Input

The first line contains two integers  $n$  and  $m$  — the number of the graph's vertices and edges, correspondingly. Then follow  $m$  lines, each of them contains three integers — the description of the graph's edges as " $a_i b_i w_i$ " where  $a_i$  and  $b_i$  are the numbers of vertices connected by the  $i$ -th edge,  $w_i$  is the edge's weight. It is guaranteed that the graph is connected and doesn't contain loops or multiple edges.

### Output

Print  $m$  lines — all the critical and pseudo-critical edges

### Examples

| Input  | Output  |
|--|---|
| 5 7<br>0 1 1<br>1 2 1<br>2 3 2<br>0 3 2<br>0 4 3<br>3 4 3<br>1 4 6 | Critical edges: [0,1],<br>Pseudo critical edges: [2,3,4,5]<br><br><b>#NB: Here edge 0 means edge (0, 1 ,1)</b><br><b>Edge 1 means (1,2,1) look inputs</b> |