

Reflections:

Binomial coefficient

Formula:

$$C(n,k) = C(n-1,k-1) + C(n-1,k)$$

1. dynamic programming version-1:

1. Involves two comparisons.
2. Creates 2-D array representation.
3. Doesn't compute the result which are already computed.
4. Calculates value using previously stored values.
5. The second for loop runs from $j=0$ to $\min(i,k)$ this is because in case where k reaches $k+1$ iteration in n side, it should return the value k only.
6. Doesn't compute the entire 2-D.
7. Time complexity: $O(n*k)$
8. Space complexity: $O(n*k)$

2. Recursive:

1. Each recursive call is going to create spaces for variables created during computation.
2. Computes the same subproblem again and again i.e overlapping subproblem.
3. Space used: $O(2^n - 1) * 8$ (bytes)
4. Time complexity $O(2^n - 1)$.

3. Dynamic programming version-2 (using 1-D array):

1. Display only the final array elements as intermediate results are used to generate final result.
2. Computes next row of pascal triangle using the previous row.
3. Every loop on i builds i 'th row of pascal triangle using $(i-1)$ th row therefore, 2-D representation is reduced to 1-D.
4. Time complexity: $O(n*k)$
5. Space complexity: $O(k)$