

Zugang 1

$$A = \begin{pmatrix} -2 & -4 & 0 \\ 3 & -4 & 6 \\ 0 & 1 & -2 \end{pmatrix} \quad \det A = ?$$

$$\begin{pmatrix} -2 & -4 & 0 \\ 3 & -4 & 6 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{+2} \begin{pmatrix} 1 & -8 & 6 \\ 3 & -4 & 6 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{(-3)}$$

$$\sim \begin{pmatrix} 1 & -8 & 6 \\ 0 & 20 & -12 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{(+7)} \begin{pmatrix} 1 & -1 & -8 \\ 0 & 20 & -12 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{(-1)}$$

$$\sim \begin{pmatrix} 1 & -8 & 6 \\ 0 & 20 & -12 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{(-19)} \begin{pmatrix} 1 & -8 & 6 \\ 0 & 26 & -26 \\ 0 & 1 & -2 \end{pmatrix} \xrightarrow{(-1)}$$

$$\sim \begin{pmatrix} 1 & -8 & 6 \\ 0 & 1 & -2 \\ 0 & 0 & -28 \end{pmatrix}$$

$$\det A = 1 \cdot 1 \cdot (-28) = -28.$$

$$\sqrt{2} \quad x^2 = t$$

$$t^2 - 13t + 36 = 0$$

$$D = 169 - 4 \cdot 36 \cdot 1$$

$$D = 169 - 144 = 25$$

$$t_1 = \frac{13 - 5}{2} = 4$$

$$t_2 = \frac{13 + 5}{2} = 9$$

$$x_{1,2}^2 = 4$$

$$x_{1,2} = \pm 2$$

$$x_{3,4}^2 = 9$$

$$x_{3,4} = \pm 3$$

$$\sqrt{3}$$

$$(-8 - 4i - (-6 + 5i))(-6 - 10i - (-18 - 5i)) - (-6 + 5i)^2$$

$$1) (-8 - 4i - (-6 + 5i)) = -8 - 4i + 6 - 5i =$$

$$= -2 - 9i$$

$$2) (-6 - 10i - (-18 - 5i)) = -6 - 10i + 18 + 5i =$$

$$= 12 - 5i$$

$$3) (-2 - 9i)(12 - 5i) = -24 + 10i - 108i + 45i^2 =$$

$$= -24 - 98i - 45 = -69 - 98i$$

$$4) \frac{(-6+5i)^2}{(6+5i)^2} = \frac{36}{(5i-6)^2} = \frac{25i^2 - 60i + 36}{-25 + 36 - 60i} = \frac{-25 + 36 - 60i}{11 - 60i}$$

$$5) -68 - 88i - 11 + 60i = -80 - 38i$$

$\sqrt{4}$

$$-6(\cos(9.75\pi) + i\sin(9.75\pi))$$

~~$$p = -6$$

$$\varphi = 9.75\pi$$

$$\sin(9.75\pi) =$$~~

$$-6\left(\cos\frac{3\pi}{4} + i\sin\frac{3\pi}{4}\right)$$

$$= -6\left(-\frac{\sqrt{2}}{2} + i\frac{\sqrt{2}}{2}\right) = \frac{\sqrt{2} \cdot 6}{2} - i\frac{\sqrt{2} \cdot 6}{2}$$

$$= 3\sqrt{2} - 3\sqrt{2}i = 4.24 - 4.24i$$

$\sqrt{5}$

$$\begin{cases} \xi_1 = -1 \\ -2\xi_1 + \xi_2 = 1 \\ 3\xi_1 - \xi_2 + \xi_3 = -2 \end{cases}$$

$$A = \begin{pmatrix} 1 & 0 & 0 \\ -2 & 1 & 0 \\ 3 & -1 & 1 \end{pmatrix} \quad X = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \quad B = \begin{pmatrix} -1 \\ 1 \\ -2 \end{pmatrix}$$

$$X = A^{-1} B$$

$$A^{-1} = \frac{1}{\det A} A^*$$

$$\det A = 1 \cdot 1 \cdot 1 = 1$$

$$A^{-1} \rightarrow \left(\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 0 \\ -2 & 1 & 0 & 0 & 1 & 0 \\ 3 & -1 & 1 & 0 & 0 & 1 \end{array} \right) \begin{matrix} (+2), (-3) \\ \leftarrow \\ \leftarrow \end{matrix}$$

$$\sim \left(\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 \\ 0 & -1 & 1 & -3 & 0 & 1 \end{array} \right) \begin{matrix} (+1) \\ \leftarrow \end{matrix} \sim \left(\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 \\ 0 & 0 & 1 & -1 & 1 & 1 \end{array} \right)$$

$$A^{-1} = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 1 & 1 \end{pmatrix}$$

$$X = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 1 & 1 \end{pmatrix} \begin{pmatrix} -1 \\ 1 \\ -2 \end{pmatrix} = \begin{pmatrix} -1 + 0 + 0 \\ -2 + 1 + 0 \\ 1 + 1 - 2 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}$$

$$\begin{array}{r}
 \sqrt{6} \\
 \begin{array}{l}
 \times \\
 \hline
 (x^5 + 2x^4 - 2x^3 - 4x^2 + x + 2) \mid x^3 + 2x^2 - x - 2 \\
 \hline
 x^5 + 2x^4 - x^3 - 2x^2 \\
 \hline
 3x^3 - x^3 - 2x^2 + x + 2 \\
 \hline
 -x^3 - 2x^2 + x + 2 \\
 \hline
 0
 \end{array}
 \end{array}$$

Problem 1: $x^2 - 1$

$$\sqrt{7}$$

$$-A = \begin{pmatrix} -1 & 0 & 0 \\ 2 & -1 & 0 \\ -3 & 1 & -1 \end{pmatrix} \quad -2B = \begin{pmatrix} -2 & -2 & 8 \\ 4 & 2 & -12 \\ -4 & -2 & 10 \end{pmatrix}$$

$$-3C = \begin{pmatrix} -3 & 0 & 3 \\ 3 & -3 & 3 \\ -6 & 3 & -3 \end{pmatrix}$$

$$-A - 2B = \begin{pmatrix} -1 & 0 & 0 \\ 2 & -1 & 0 \\ -3 & 1 & -1 \end{pmatrix} + \begin{pmatrix} 2 & -2 & 8 \\ 4 & 2 & -12 \\ -4 & -2 & 10 \end{pmatrix} =$$

$$= \begin{pmatrix} -3 & -2 & 8 \\ 6 & 1 & -12 \\ -7 & -1 & 9 \end{pmatrix}$$

$$\begin{matrix} A \\ B \\ C \end{matrix} = \begin{pmatrix} -3 & -2 & 8 \\ 6 & 1 & -12 \\ 7 & -1 & 9 \end{pmatrix} + \begin{pmatrix} -3 & 0 & 3 \\ 3 & -3 & 3 \\ -6 & 3 & -3 \end{pmatrix} = \begin{pmatrix} -6 & -2 & 11 \\ 9 & -2 & -9 \\ -13 & 2 & 6 \end{pmatrix}$$

$$\sqrt{8} \quad (1 \ 4 \ -3) \cdot \begin{pmatrix} 1 & 2 \\ -1 & 4 \\ -1 & -2 \end{pmatrix} \cdot \begin{pmatrix} -3 & 4 \\ -1 & -2 \end{pmatrix} =$$

$$= (1 \cdot 1 + 4 \cdot (-1) + (-3) \cdot (-1)) \quad 1 \cdot 2 + 4 \cdot 4 + (-3) \cdot (-2) \times$$

$$\times \begin{pmatrix} -3 & 4 \\ -1 & -2 \end{pmatrix} = (1 - 4 + 3) \quad 2 + 16 + 6 \begin{pmatrix} -3 & 4 \\ -1 & -2 \end{pmatrix} =$$

$$= \begin{pmatrix} 0 & 24 \end{pmatrix} \begin{pmatrix} -3 & 4 \\ -1 & -2 \end{pmatrix} = (0 + (-24) \quad 0 + (-48)) =$$

$$= \begin{pmatrix} -24 & -48 \end{pmatrix}$$