> LIBRARY SETTINGS

```
[ ] Ļ 2 cells hidden
```

2 Prelimiaries

2.1 DATA MANIPULATION

```
x = torch.arange(12, dtype=torch.float32)
Х
\rightarrow tensor([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9., 10., 11.])
x.numel()
→ 12
x.shape
\rightarrow torch.Size([12])
X = x.reshape(3, 4)
Χ
→ tensor([[ 0., 1., 2., 3.],
            [4., 5., 6., 7.],
             [8., 9., 10., 11.]])
torch.zeros((2, 3, 4))
→ tensor([[[0., 0., 0., 0.],
             [0., 0., 0., 0.],
             [0., 0., 0., 0.]
             [[0., 0., 0., 0.],
             [0., 0., 0., 0.]
             [0., 0., 0., 0.]]
torch.ones((2, 3, 4))
```

```
\rightarrow tensor([[[1., 1., 1., 1.],
             [1., 1., 1., 1.],
             [1., 1., 1., 1.]],
             [[1., 1., 1., 1.],
             [1., 1., 1., 1.],
             [1., 1., 1., 1.]]
torch.randn(3, 4)
→ tensor([[-2.5244, -0.0730, -0.7310, 0.6800],
             [0.0626, 1.0085, -1.0283, 0.2288],
             [-0.8688, -0.6578, -0.1008, -1.4014]])
torch.tensor([[2, 1, 4, 3], [1, 2, 3, 4], [4, 3, 2, 1]])
→ tensor([[2, 1, 4, 3],
            [1, 2, 3, 4],
             [4, 3, 2, 1]])
X[-1], X[1:3]
→ (tensor([ 8., 9., 10., 11.]),
      tensor([[ 4., 5., 6., 7.],
             [8., 9., 10., 11.]]))
X[1, 2] = 17
Χ
→ tensor([[ 0., 1., 2., 3.],
             [4., 5., 17., 7.],
             [8., 9., 10., 11.]])
X[:2, :] = 12
Χ
→ tensor([[12., 12., 12., 12.],
             [12., 12., 12., 12.],
             [ 8., 9., 10., 11.]])
torch.exp(x)
→ tensor([162754.7969, 162754.7969, 162754.7969, 162754.7969, 162754.7969,
             162754.7969, 162754.7969, 162754.7969,
                                                     2980.9580, 8103.0840,
              22026.4648, 59874.1406])
x = torch.tensor([1.0, 2, 4, 8])
y = torch.tensor([2, 2, 2, 2])
```

```
x + y, x - y, x * y, x / y, x ** y
→ (tensor([ 3., 4., 6., 10.]),
      tensor([-1., 0., 2., 6.]),
      tensor([ 2., 4., 8., 16.]),
      tensor([0.5000, 1.0000, 2.0000, 4.0000]),
      tensor([ 1., 4., 16., 64.]))
X = torch.arange(12, dtype=torch.float32).reshape((3,4))
Y = torch.tensor([[2.0, 1, 4, 3], [1, 2, 3, 4], [4, 3, 2, 1]])
torch.cat((X, Y), dim=0), torch.cat((X, Y), dim=1)
\rightarrow (tensor([[ 0., 1., 2., 3.],
             [ 4.,
                    5., 6., 7.],
             [8., 9., 10., 11.],
             [ 2., 1., 4., 3.],
             [1., 2., 3., 4.],
             [4., 3., 2., 1.]
     tensor([[ 0., 1., 2., 3., 2., 1., 4., 3.],
             [4., 5., 6., 7., 1., 2., 3., 4.],
             [8., 9., 10., 11., 4., 3., 2., 1.]]))
X == Y
→ tensor([[False, True, False, True],
            [False, False, False],
             [False, False, False, False]])
X.sum()
\rightarrow tensor(66.)
a = torch.arange(3).reshape((3, 1))
b = torch.arange(2).reshape((1, 2))
a, b
→ (tensor([[0],
             [1],
             [2]]),
     tensor([[0, 1]]))
a + b
\rightarrow tensor([[0, 1],
            [1, 2],
             [2, 3]])
```

```
before = id(Y)
Y = Y + X
id(Y) == before
```

→ False

```
Z = torch.zeros_like(Y)
print('id(Z):', id(Z))
Z[:] = X + Y
print('id(Z):', id(Z))
```

id(Z): 139868415165760 id(Z): 139868415165760

```
before = id(X)
X += Y
id(X) == before
```

→ True

```
A = X.numpy()
B = torch.from_numpy(A)
type(A), type(B)
```

(numpy.ndarray, torch.Tensor)

```
a = torch.tensor([3.5])
a, a.item(), float(a), int(a)
```

```
(tensor([3.5000]), 3.5, 3.5, 3)
```

Key Takeaways:

- 1. ndarray is essential for managing multi-dimensional data efficiently.
- 2. Basic operations include slicing, reshaping, and broadcasting.
- 3. ndarrays allow for fast mathematical operations and efficient memory use.

2.2 DATA PREPROCESSING

```
os.makedirs(os.path.join('..', 'data'), exist_ok=True)
data_file = os.path.join('..', 'data', 'house_tiny.csv')
with open(data_file, 'w') as f:
    f.write('''NumRooms,RoofType,Price
NA,NA,127500
2,NA,106000
```

```
4, Slate, 178100
NA,NA,140000''')
data = pd.read_csv(data_file)
print(data)
\rightarrow
        NumRooms RoofType
                              Price
              NaN
                       NaN
                            127500
     1
              2.0
                       NaN 106000
     2
              4.0
                     Slate 178100
     3
              NaN
                       NaN 140000
inputs, targets = data.iloc[:, 0:2], data.iloc[:, 2]
inputs = pd.get_dummies(inputs, dummy_na=True)
print(inputs)
\overline{\longrightarrow}
        NumRooms
                   RoofType_Slate RoofType_nan
             NaN
                            False
                                             True
     1
              2.0
                             False
                                             True
                                            False
     2
              4.0
                             True
              NaN
                             False
                                             True
inputs = inputs.fillna(inputs.mean())
print(inputs)
                   RoofType_Slate RoofType_nan
        NumRooms
     0
              3.0
                             False
                                             True
              2.0
                             False
                                             True
     1
     2
              4.0
                             True
                                            False
     3
              3.0
                             False
                                             True
X = torch.tensor(inputs.to_numpy(dtype=float))
y = torch.tensor(targets.to_numpy(dtype=float))
Х, у
→ (tensor([[3., 0., 1.],
               [2., 0., 1.],
               [4., 1., 0.],
               [3., 0., 1.]], dtype=torch.float64),
      tensor([127500., 106000., 178100., 140000.], dtype=torch.float64))
```

- 1. Pandas is essential for efficient data preprocessing and manipulation.
- 2. It helps handle missing data, perform filtering, and convert data types.
- Pandas' DataFrames and Series provide powerful structures for working with large datasets.

2.3 LINEAR ALGEBRA

```
x = torch.tensor(3.0)
y = torch.tensor(2.0)
x + y, x * y, x / y, x**y
\rightarrow (tensor(5.), tensor(6.), tensor(1.5000), tensor(9.))
x = torch.arange(3)
Х
\rightarrow tensor([0, 1, 2])
print(x[2])
print(len(x))
x.shape
\rightarrow tensor(2)
     torch.Size([3])
A = torch.arange(6).reshape(3, 2)
print(A)
A.T
\rightarrow tensor([[0, 1],
             [2, 3],
             [4, 5]])
     tensor([[0, 2, 4],
             [1, 3, 5]])
A = torch.tensor([[1, 2, 3], [2, 0, 4], [3, 4, 5]])
A == A.T
→ tensor([[True, True, True],
              [True, True, True],
              [True, True, True]])
torch.arange(24).reshape(2, 3, 4)
→ tensor([[[ 0, 1, 2, 3],
              [4, 5, 6, 7],
              [8, 9, 10, 11]],
              [[12, 13, 14, 15],
              [16, 17, 18, 19],
              [20, 21, 22, 23]]])
```

```
A = torch.arange(6, dtype=torch.float32).reshape(2, 3)
B = A.clone()
print(A, A + B)
print(A*B)
→ tensor([[0., 1., 2.],
             [3., 4., 5.]]) tensor([[ 0., 2., 4.],
             [ 6., 8., 10.]])
     tensor([[ 0., 1., 4.],
            [ 9., 16., 25.]])
a = 2
X = torch.arange(24).reshape(2, 3, 4)
a + X, (a * X).shape
→ (tensor([[[ 2, 3, 4, 5],
               [6, 7, 8, 9],
               [10, 11, 12, 13]],
              [[14, 15, 16, 17],
               [18, 19, 20, 21],
               [22, 23, 24, 25]]]),
      torch.Size([2, 3, 4]))
x = torch.arange(3, dtype=torch.float32)
print(x, x.sum())
print(A.shape, A.sum())
print(A.shape, A.sum(axis=0).shape)
print(A.shape, A.sum(axis=1).shape)
print(A.sum(axis=[0, 1]) == A.sum() )
print(A.mean(), A.sum() / A.numel())
print(A.mean(axis=0), A.sum(axis=0) / A.shape[0])
\rightarrow tensor([0., 1., 2.]) tensor(3.)
     torch.Size([2, 3]) tensor(15.)
     torch.Size([2, 3]) torch.Size([3])
     torch.Size([2, 3]) torch.Size([2])
     tensor(True)
     tensor(2.5000) tensor(2.5000)
     tensor([1.5000, 2.5000, 3.5000]) tensor([1.5000, 2.5000, 3.5000])
sum_A = A.sum(axis=1, keepdims=True)
print(sum_A)
print(sum_A.shape)
print(A / sum_A)
print(A.cumsum(axis=0))
→ tensor([[ 3.],
             [12.]])
     torch.Size([2, 1])
```

```
y = torch.ones(3, dtype = torch.float32)
print(x, y, torch.dot(x, y))
print(torch.sum(x * y))
print(A.shape, x.shape, torch.mv(A, x), A@x)

B = torch.ones(3, 4)
torch.mm(A, B), A@B
```

```
u = torch.tensor([3.0, -4.0])
print(torch.norm(u))
print(torch.abs(u).sum())
torch.norm(torch.ones((4, 9)))
```

```
tensor(5.)
tensor(7.)
tensor(6.)
```

- 1. Vectors and matrices are fundamental structures for storing and computing data.
- 2. Matrix operations like inversion and multiplication are vital for model calculations.

2.5 Automatic Differentiation

```
x = torch.arange(4.0)
print(x)

x.requires_grad_(True)
x.grad

y = 2 * torch.dot(x, x)
print(y)

y.backward()
```

```
print(x.grad)
print(x.grad == 4 * x)
x.grad.zero_()
y = x.sum()
y.backward()
print(x.grad)
\rightarrow tensor([0., 1., 2., 3.])
     tensor(28., grad_fn=<MulBackward0>)
     tensor([ 0., 4., 8., 12.])
     tensor([True, True, True, True])
     tensor([1., 1., 1., 1.])
x.grad.zero_()
y = x * x
u = y.detach()
z = u * x
z.sum().backward()
print(x.grad == u)
x.grad.zero_()
y.sum().backward()
x.grad == 2 * x
tensor([True, True, True, True])
     tensor([True, True, True])
def f(a):
    b = a * 2
    while b.norm() < 1000:
        b = b * 2
    if b.sum() > 0:
        c = b
    else:
        c = 100 * b
    return c
a = torch.randn(size=(), requires_grad=True)
d = f(a)
d.backward()
a.grad == d / a
→ tensor(True)
```

- Autograd automates derivative computation, simplifying model training and it's critical for backpropagation in neural networks.
- 2. It also tracks operations to create a computation graph for efficient optimization.

3 Linear Neural Networks for Regression

3.1 Linear Regression

→ 3.1.2. Vectorization for Speed

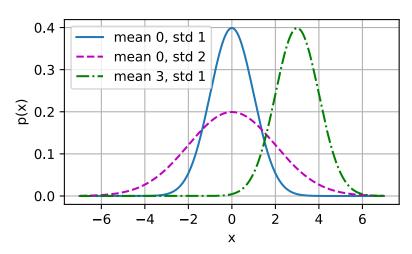
```
n = 10000
a = torch.ones(n)
b = torch.ones(n)

c = torch.zeros(n)
t = time.time()
for i in range(n):
    c[i] = a[i] + b[i]
print(f'{time.time() - t:.5f} sec')

t = time.time()
d = a + b
f'{time.time() - t:.5f} sec'
```

3.1.3. The Normal Distribution and Squared Loss





- 1. Linear regression can predict continuous outcomes.
- 2. Techniques like gradient descent are crucial for finding the optimal parameters in linear regression, and they are also applicable to other machine learning algorithms.
- 3. Linear regression assumes a linear relationship between variables. In real-world scenarios, this may not always be the case, and more complex models may be needed.

→ 3.2. Object-Oriented Design for Implementation

→ 3.2.1 Utilities

```
def add_to_class(Class):
    """Register functions as methods in created class."""
    def wrapper(obj):
        setattr(Class, obj.__name__, obj)
    return wrapper

class A:
    def __init__(self):
        self.b = 1

a = A()

@add_to_class(A)
def do(self):
    print('Class attribute "b" is', self.b)

a.do()
```

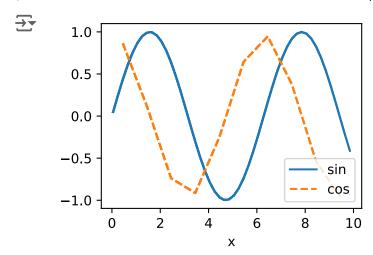
→ Class attribute "b" is 1

```
class HyperParameters:
    """The base class of hyperparameters."""
    def save_hyperparameters(self, ignore=[]):
        raise NotImplemented

class B(d21.HyperParameters):
    def __init__(self, a, b, c):
        self.save_hyperparameters(ignore=['c'])
        print('self.a =', self.a, 'self.b =', self.b)
        print('There is no self.c =', not hasattr(self, 'c'))

b = B(a=1, b=2, c=3)
```

self.a = 1 self.b = 2 There is no self.c = True




```
class Module(nn.Module, d21.HyperParameters):
   def __init__(self, plot_train_per_epoch=2, plot_valid_per_epoch=1):
       super().__init__()
        self.save_hyperparameters()
        self.board = ProgressBoard()
   def loss(self, y_hat, y):
       raise NotImplementedError
   def forward(self, X):
       assert hasattr(self, 'net'), 'Neural network is defined'
       return self.net(X)
   def plot(self, key, value, train):
        assert hasattr(self, 'trainer'), 'Trainer is not inited'
        self.board.xlabel = 'epoch'
       if train:
           x = self.trainer.train_batch_idx / \
                self.trainer.num_train_batches
            n = self.trainer.num_train_batches / \
                self.plot_train_per_epoch
       else:
           x = self.trainer.epoch + 1
            n = self.trainer.num_val_batches / \
                self.plot_valid_per_epoch
        self.board.draw(x, value.to(d21.cpu()).detach().numpy(),
                        ('train_' if train else 'val_') + key,
                        every_n=int(n))
   def training_step(self, batch):
       1 = self.loss(self(*batch[:-1]), batch[-1])
        self.plot('loss', 1, train=True)
```

```
return 1

def validation_step(self, batch):
    l = self.loss(self(*batch[:-1]), batch[-1])
    self.plot('loss', l, train=False)

def configure_optimizers(self):
    raise NotImplementedError
```

3.2.3 Data

```
class DataModule(d21.HyperParameters):
    def __init__(self, root='../data', num_workers=4):
        self.save_hyperparameters()

def get_dataloader(self, train):
        raise NotImplementedError

def train_dataloader(self):
        return self.get_dataloader(train=True)

def val_dataloader(self):
    return self.get_dataloader(train=False)
```

→ 3.2.4 Training

```
class Trainer(d21.HyperParameters):
   def init__(self, max_epochs, num_gpus=0, gradient_clip_val=0):
       self.save_hyperparameters()
        assert num_gpus == 0, 'No GPU support yet'
   def prepare_data(self, data):
        self.train_dataloader = data.train_dataloader()
        self.val_dataloader = data.val_dataloader()
        self.num_train_batches = len(self.train_dataloader)
        self.num_val_batches = (len(self.val_dataloader)
                                if self.val_dataloader is not None else 0)
   def prepare_model(self, model):
       model.trainer = self
       model.board.xlim = [0, self.max_epochs]
        self.model = model
   def fit(self, model, data):
        self.prepare data(data)
        self.prepare_model(model)
        self.optim = model.configure_optimizers()
```

```
self.epoch = 0
self.train_batch_idx = 0
self.val_batch_idx = 0
for self.epoch in range(self.max_epochs):
    self.fit_epoch()

def fit_epoch(self):
    raise NotImplementedError
```

- 1. Object-oriented design promotes modularity by encapsulating the model's functionality within a class which stored in d2l library. This makes the code easier to understand, maintain, and extend.
- 2. The class-based design makes it easier to extend the model to include more features or functionalities. For example, you could add regularization methods or support for different types of regression.
- 3. Different aspects of the model like forward pass, loss calculation, and training are handled by separate methods. This separation helps in maintaining and debugging the code.

3.4 Linear Regression Implementation from Scratch

→ 3.4.1. Defining the Model

```
class LinearRegressionScratch(d21.Module):
    """The linear regression model implemented from scratch."""
    def __init__(self, num_inputs, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
        self.w = torch.normal(0, sigma, (num_inputs, 1), requires_grad=True)
        self.b = torch.zeros(1, requires_grad=True)
```

```
@d21.add_to_class(LinearRegressionScratch)
def forward(self, X):
    return torch.matmul(X, self.w) + self.b
```

3.4.2 Defining the Loss Function

```
@d21.add_to_class(LinearRegressionScratch)
def loss(self, y_hat, y):
    1 = (y_hat - y) ** 2 / 2
    return 1.mean()
```

3.4.3 Defining the Optimization Algorithm

```
class SGD(d21.HyperParameters):
    def __init__(self, params, lr):
        self.save_hyperparameters()

def step(self):
        for param in self.params:
            param -= self.lr * param.grad

def zero_grad(self):
        for param in self.params:
            if param.grad is not None:
                param.grad.zero_()

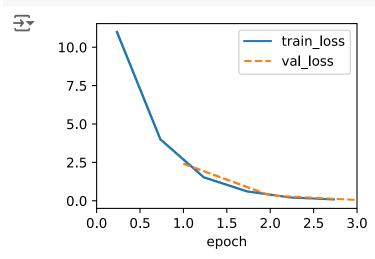
@d21.add_to_class(LinearRegressionScratch)
def configure_optimizers(self):
    return SGD([self.w, self.b], self.lr)
```

→ 3.4.4 Training

```
@d21.add to class(d21.Trainer)
def prepare_batch(self, batch):
    return batch
@d21.add_to_class(d21.Trainer)
def fit_epoch(self):
    self.model.train()
    for batch in self.train_dataloader:
        loss = self.model.training_step(self.prepare_batch(batch))
        self.optim.zero_grad()
        with torch.no_grad():
            loss.backward()
            if self.gradient clip val > 0:
                self.clip_gradients(self.gradient_clip_val, self.model)
            self.optim.step()
        self.train_batch_idx += 1
    if self.val_dataloader is None:
        return
    self.model.eval()
    for batch in self.val_dataloader:
```

```
with torch.no_grad():
    self.model.validation_step(self.prepare_batch(batch))
self.val_batch_idx += 1
```

```
model = LinearRegressionScratch(2, 1r=0.03)
data = d21.SyntheticRegressionData(w=torch.tensor([2, -3.4]), b=4.2)
trainer = d21.Trainer(max_epochs=3)
trainer.fit(model, data)
```



- 1. While frameworks like PyTorch automate these steps, implementing it from scratch reveals how the core components work together and gives more control over the learning process.
- 2. During optimization, careful tuning of the learning rate is necessary to ensure the model converges to a good solution. If the learning rate is too high, the model may overshoot the optimal values.

4 Linear Neural Networks for Classification

4.1 Softmax Regression

- Softmax function converts model outputs into probabilities, allowing the model to predict
 which class an input belongs to. It's essential for classification tasks with more than two
 classes
- 2. Softmax regression is an extended version of binary logistic regression to handle multiple classes. This makes it suitable for tasks like image classification or text classification with multiple categories.
- 3. In Softmax regression, we rely on Maximum Likelihood Estimation, the same method when working on Mean Squared Error Loss

4.2 The Image Classification Dataset

4.2.1 Loading the Dataset

```
data = FashionMNIST(resize=(32, 32))
len(data.train), len(data.val)
```

```
Downloading <a href="http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-images-idx2">http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-images-idx2</a>
100% 26421880/26421880 [00:02<00:00, 12928721.90it/s]
Extracting ../data/FashionMNIST/raw/train-images-idx3-ubyte.gz to ../data/FashionMNIST/r

Downloading <a href="http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-labels-idx1">http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-labels-idx1</a>
100% 29515/29515 [00:00<00:00, 210352.35it/s]
Extracting ../data/FashionMNIST/raw/train-labels-idx1-ubyte.gz to ../data/FashionMNIST/r

Downloading <a href="http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10k-images-idx3-bownloading">http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10k-images-idx3-bownloading</a> http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10k-images-idx3-bownloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t
```

Extracting .../data/FashionMNIST/raw/t10k-images-idx3-ubyte.gz to .../data/FashionMNIST/ra

4422102/4422102 [00:01<00:00, 3916938.53it/s]

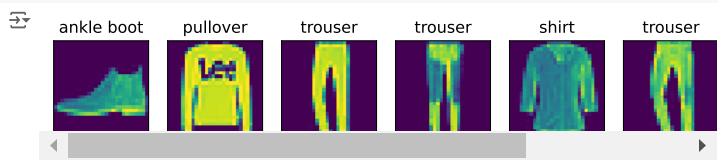
4.2.2 Reading a Minibatch

4.2.3 Visualization

'13.09 sec'

```
def show_images(imgs, num_rows, num_cols, titles=None, scale=1.5):
    raise NotImplementedErrors

@d21.add_to_class(FashionMNIST)
def visualize(self, batch, nrows=1, ncols=8, labels=[]):
    X, y = batch
    if not labels:
        labels = self.text_labels(y)
        d21.show_images(X.squeeze(1), nrows, ncols, titles=labels)
batch = next(iter(data.val_dataloader()))
data.visualize(batch)
```



- 1. During Pre-processing, images will be resized to a uniform size and the pixels will be normalized to help the model to process them in more efficient and consistent way.
- 2. Enhancing the dataset with variations through augmentation helps the model generalize better by exposing it to a broader range of scenarios.
- 3. Splitting the dataset into training, validation, and test sets is important for assessing model performance and avoiding overfitting.

4.3 The Base Classification Model

→ 4.3.1 The Classifier Class

```
class Classifier(d21.Module):
    """The base class of classification models."""
    def validation_step(self, batch):
        Y_hat = self(*batch[:-1])
        self.plot('loss', self.loss(Y_hat, batch[-1]), train=False)
        self.plot('acc', self.accuracy(Y_hat, batch[-1]), train=False)
```

```
@d21.add_to_class(d21.Module)
def configure_optimizers(self):
    return torch.optim.SGD(self.parameters(), lr=self.lr)
```

4.3.2 Accuracy

```
@d21.add_to_class(Classifier)
def accuracy(self, Y_hat, Y, averaged=True):

Y_hat = Y_hat.reshape((-1, Y_hat.shape[-1]))
preds = Y_hat.argmax(axis=1).type(Y.dtype)
compare = (preds == Y.reshape(-1)).type(torch.float32)
return compare.mean() if averaged else compare
```

Key Takeaways:

- 1. It is often the performance measure that we care about the most.
- 2. Although there will be probabilities estimated for one input, at the end, it will need to be chosen to be categorized among the classes given.

4.4 Softmax Regression Implementation from Scratch

4.4.1 The Softmax

tensor([1.0000, 1.0000]))

4.4.2 The Model

```
class SoftmaxRegressionScratch(d21.Classifier):
    def __init__(self, num_inputs, num_outputs, lr, sigma=0.01):
        super().__init__()
        self.save hyperparameters()
        self.W = torch.normal(0, sigma, size=(num_inputs, num_outputs),
                              requires grad=True)
        self.b = torch.zeros(num_outputs, requires_grad=True)
    def parameters(self):
        return [self.W, self.b]
@d21.add_to_class(SoftmaxRegressionScratch)
def forward(self, X):
    X = X.reshape((-1, self.W.shape[0]))
    return softmax(torch.matmul(X, self.W) + self.b)
y = torch.tensor([0, 2])
y_hat = torch.tensor([[0.1, 0.3, 0.6], [0.3, 0.2, 0.5]])
y_hat[[0, 1], y]
→ tensor([0.1000, 0.5000])
def cross_entropy(y_hat, y):
    return -torch.log(y_hat[list(range(len(y_hat))), y]).mean()
print(cross_entropy(y_hat, y))
@d21.add_to_class(SoftmaxRegressionScratch)
def loss(self, y_hat, y):
    return cross_entropy(y_hat, y)
→ tensor(1.4979)
```

4.4.3 The Cross Entropy Loss

```
y = torch.tensor([0, 2])
y_hat = torch.tensor([[0.1, 0.3, 0.6], [0.3, 0.2, 0.5]])
y_hat[[0, 1], y]

tensor([0.1000, 0.5000])
```

```
def cross_entropy(y_hat, y):
    return -torch.log(y_hat[list(range(len(y_hat))), y]).mean()

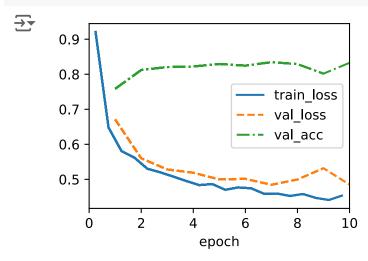
cross_entropy(y_hat, y)

tensor(1.4979)

@d21.add_to_class(SoftmaxRegressionScratch)
def loss(self, y_hat, y):
    return cross_entropy(y_hat, y)
```

4.4.4 Training

```
data = d21.FashionMNIST(batch_size=256)
model = SoftmaxRegressionScratch(num_inputs=784, num_outputs=10, lr=0.1)
trainer = d21.Trainer(max_epochs=10)
trainer.fit(model, data)
```



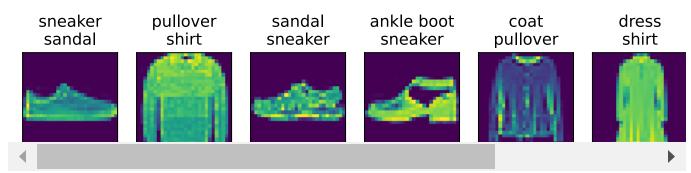
4.4.5 Prediction

```
X, y = next(iter(data.val_dataloader()))
preds = model(X).argmax(axis=1)
preds.shape
```

→ torch.Size([256])

```
wrong = preds.type(y.dtype) != y
X, y, preds = X[wrong], y[wrong], preds[wrong]
labels = [a+'\n'+b for a, b in zip(
    data.text_labels(y), data.text_labels(preds))]
data.visualize([X, y], labels=labels)
```





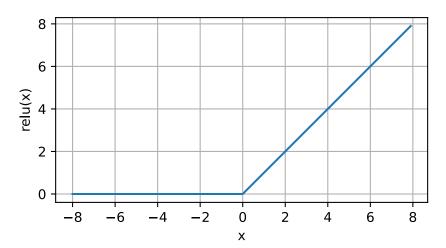
- 1. The softmax function converts raw scores (logits) into probabilities. For each class, it calculates the probability that an input belongs to that class. The probabilities are normalized so they sum up to 1.
- 2. The loss function used in softmax regression is cross-entropy loss.
- 3. The process involves multiple steps including initialization, forward pass, loss calculation, backward pass, and parameter updates.

5. Multilayer Perceptrons

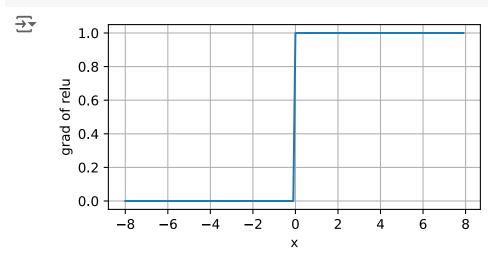
- → 5.1.2 Hidden Layers
- ✓ 5.1.2.1 ReLU Function

```
x = torch.arange(-8.0, 8.0, 0.1, requires_grad=True)
y = torch.relu(x)
d2l.plot(x.detach(), y.detach(), 'x', 'relu(x)', figsize=(5, 2.5))
```





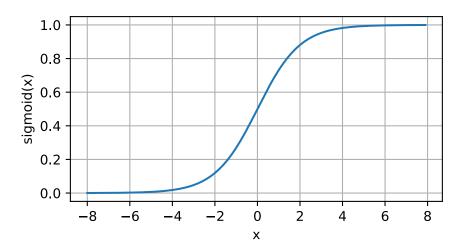
y.backward(torch.ones_like(x), retain_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of relu', figsize=(5, 2.5))



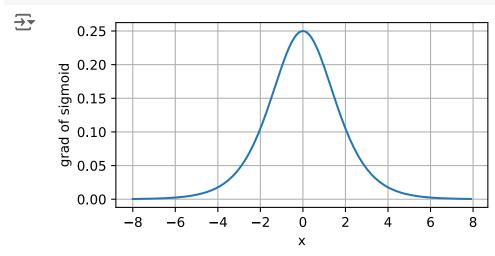
→ 5.1.2.2 Sigmoid Function

```
y = torch.sigmoid(x)
d21.plot(x.detach(), y.detach(), 'x', 'sigmoid(x)', figsize=(5, 2.5))
```





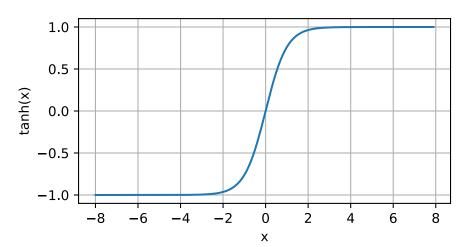
```
x.grad.data.zero_()
y.backward(torch.ones_like(x),retain_graph=True)
d21.plot(x.detach(), x.grad, 'x', 'grad of sigmoid', figsize=(5, 2.5))
```



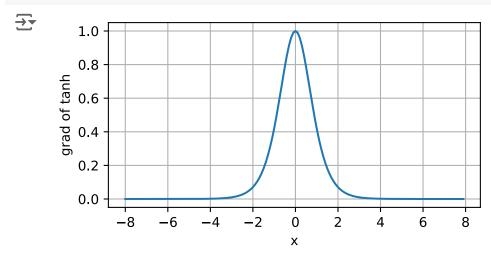
→ 5.1.2.3 Tanh Function

```
y = torch.tanh(x)
d2l.plot(x.detach(), y.detach(), 'x', 'tanh(x)', figsize=(5, 2.5))
```





```
# Clear out previous gradients
x.grad.data.zero_()
y.backward(torch.ones_like(x),retain_graph=True)
d21.plot(x.detach(), x.grad, 'x', 'grad of tanh', figsize=(5, 2.5))
```



- 1. Training an MLP involves iterating through many epochs, adjusting weights to minimize the loss. Effective training requires careful tuning of hyperparameters like learning rate, batch size, and number of epochs.
- 2. Neurons in hidden layers use activation functions to introduce non-linearity into the model.

5.2 Implementation of Multilayer Perceptrons

▼ 5.2.1 Implementation from Scratch

▼ 5.2.1.1. Initializing Model Parameters

```
class MLPScratch(d21.Classifier):
    def __init__(self, num_inputs, num_outputs, num_hiddens, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
        self.W1 = nn.Parameter(torch.randn(num_inputs, num_hiddens) * sigma)
        self.b1 = nn.Parameter(torch.zeros(num_hiddens))
        self.W2 = nn.Parameter(torch.randn(num_hiddens, num_outputs) * sigma)
        self.b2 = nn.Parameter(torch.zeros(num_outputs))
```

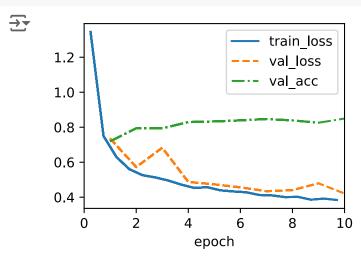
✓ 5.2.1.2 Model

```
def relu(X):
    a = torch.zeros_like(X)
    return torch.max(X, a)

@d21.add_to_class(MLPScratch)
def forward(self, X):
    X = X.reshape((-1, self.num_inputs))
    H = relu(torch.matmul(X, self.W1) + self.b1)
    return torch.matmul(H, self.W2) + self.b2
```

✓ 5.2.1.3 Training

```
model = MLPScratch(num_inputs=784, num_outputs=10, num_hiddens=256, lr=0.1)
data = d2l.FashionMNIST(batch_size=256)
trainer = d2l.Trainer(max_epochs=10)
trainer.fit(model, data)
```

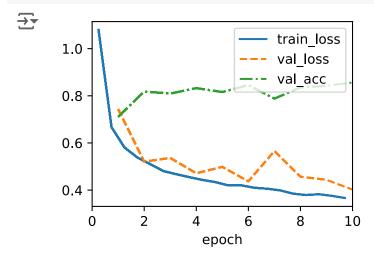


5.2.2 Concise Implementation

√ 5.2.2.1 Model

√ 5.2.2.2 Training

```
model = MLP(num_outputs=10, num_hiddens=256, lr=0.1)
trainer.fit(model, data)
```



Key Takeaways:

- 1. The training loop for MLP is exactly the same as for Softmax Regression.
- 2. Process of training includes: Define mode, data, trainer, then invoke the fitting method on model and data.
- 3. No forward method is defined, instead is now defined as a sequence of transformations via Sequential class.

5.3. Forward Propagation, Backward Propagation, and

Key Takeaways:

1.	. When it comes to calculate the gradients, we just invoke backpropagation function pro	ovided in
	framework.	

2.	Forward	propagat	ion and	back	oropaga	ation	are i	interd	lepend	lent, a	nd	training	requi	res
	significa	intly more	memor	y thai	n predic	tion.								