

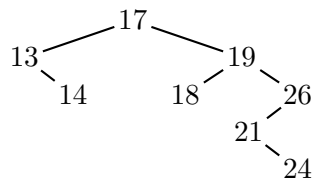
**School of Computing and Information Systems**  
**COMP90038 Algorithms and Complexity Tutorial Week 9**

**Sample answers**

Have you made a start on the assignment questions?

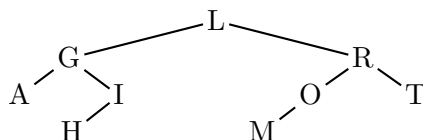
1. Construct a binary search tree (BST) by starting from an empty tree and inserting these keys, in the given order: 17, 19, 13, 26, 14, 18, 21, 24.

**Answer:**



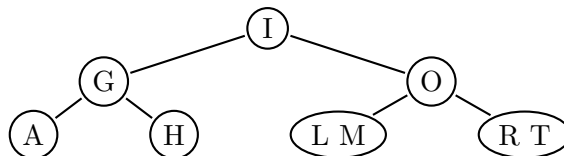
2. Construct an AVL tree from the empty tree by inserting the following keys in the given order: A, L, G, O, R, I, T, H, M.

**Answer:**



3. Construct a 2-3 tree from the empty tree by inserting the following keys in the given order: A, L, G, O, R, I, T, H, M.

**Answer:**



4. Consider the set of five keys (let us say they are positive integers)  $\{k_1, k_2, k_3, k_4, k_5\}$ , satisfying  $k_1 < k_2 < k_3 < k_4 < k_5$ . There are 120 different permutations of these five keys. For exactly two of the 120 permutations, the following happens, when the keys are inserted one by one, in the order given by the permutation, into an initially empty AVL tree: First an LR-rotation takes place, then an RL-rotation takes place. Which two permutations generate that behaviour?

**Answer:** Without loss of generality, assume the set of keys is  $\{1, 2, 3, 4, 5\}$ . After the first three keys are inserted to make an AVL tree, that tree must be perfectly balanced. Hence the first three keys inserted must cause the  $\swarrow$  zigzag path that requires an LR-rotation. After that, insertion of the two remaining keys must cause the  $\searrow$  zigzag path that requires an RL-rotation. The only permutations that will achieve this are 3, 1, 2, 5, 4 and 5, 1, 4, 3, 2.

5. ... if time permits

Use Horspool's algorithm to search for the pattern GORE in the string ALGORITHM.

**Answer:**

See Week 10 solutions