# Graphlopedia

# **Washington Experimental Mathematics Laboratory**

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December 1, 2017

Welcome to Graphlopedia, a database for graphs! We are a small team of undergraduate students (with mentors Sara Billey and Riley Casper) at the University of Washington. For the last five months we have been building a database of graphs for the use of mathematicians and other graph lovers. We have a limited number of entries right now, but it will soon grow exponentially as we start implementing graph recognition and user input.

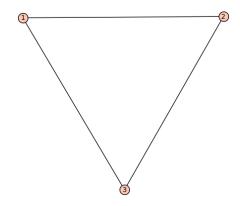
Please use "ctrl + F" to search our database. The graphs are ordered by degree sequence. A more involved website is in the works; for now please enjoy our static PDF version.

Title: Triangle

Degree Sequence: [2, 2, 2]

Vertices: 3

**Edges**: [[1, 2], [1, 3], [2, 3]]



#### **Comments:**

- 1. Complete graph on 3 vertices,  $K_3$ ,
- 2. Coxeter graph of type affine  $A_2$ ,
- 3. Cycle on 3 vertices,  $C_3$ ,

# Links:

- http://mathworld.wolfram.com/TriangleGraph.html,
- 2. https://en.wikipedia.org/wiki/Triangle\_graph,

#### **References**:

1. J. E. Humphreys, Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 34.,

**Title**: 2-Path,  $P_2$ 

**Degree Sequence**: [1, 1]

Vertices: 2 Edges: [[1, 2]]



#### **Comments:**

1. Coxeter graph of type  $A_2$ ,

#### Links:

https://en.wikipedia.org/wiki/Path\_graph,

#### **References**:

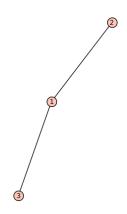
1. J. E. Humphreys, Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 32.,

**Title**: 3-Path,  $P_3$ 

**Degree Sequence**: [2, 1, 1]

Vertices: 3

**Edges**: [[1, 2], [1, 3]]



# **Comments:**

1. Coxeter graph of type  $A_3$ ,

# Links:

https://en.wikipedia.org/wiki/Path\_graph,

# **References**:

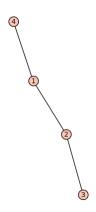
1. J. E. Humphreys, Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 32.,

**Title**: 4-Path,  $P_4$ 

**Degree Sequence**: [2, 2, 1, 1]

Vertices: 4

**Edges**: [[1, 2], [1, 4], [2, 3]]



# **Comments:**

1. Coxeter graph of type  $A_4$ ,

# Links:

https://en.wikipedia.org/wiki/Path\_graph,

# **References**:

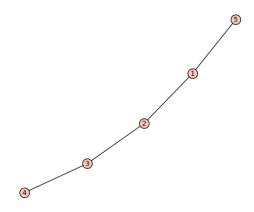
1. J. E. Humphreys, Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 32.,

**Title**: 5-Path,  $P_5$ 

**Degree Sequence**: [2, 2, 2, 1, 1]

Vertices: 5

**Edges**: [[1, 2], [1, 5], [2, 3], [3, 4]]



# **Comments:**

1. Coxeter graph of type  $A_5$ ,

# Links:

https://en.wikipedia.org/wiki/Path\_graph,

# **References**:

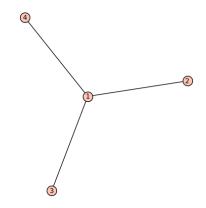
1. J. E. Humphreys, Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 32.,

Title: Claw

**Degree Sequence**: [3, 1, 1, 1]

Vertices: 4

**Edges**: [[1, 2], [1, 3], [1, 4]]



#### **Comments:**

- 1. star graph of type (1,3),
- 2. complete bipartite graph  $K_{1,3}$ ,
- 3. Coxeter graph of type  $D_4$ ,

#### Links:

http://mathworld.wolfram.com/ClawGraph.html,

#### **References**:

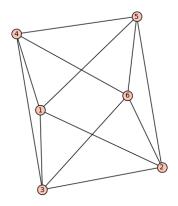
- 1. Horton, J. D. and Bouwer, I. Z. Symmetric Y-Graphs and H-Graphs. J. Combin. Th. Ser. B 53, (1991). Page 116.,
- 2. Humphreys J., Reflection Groups and Coxeter Groups, Cambridge Studies in Advanced Math, Volume 29, 1990. Page 32.,
- 3. Dahlberg, S., Foley, A., and van Willigenburg, S. Resolving Stanley's e-positivity of claw contractible free graphs. Preprint arXiv:1703.05770, (2017), Page 5.,
- 4. Gasharov V., On Stanley's chromatic symmetric function and clawfree graphs, Discrete Math. 205, 229-234 (1999).,

**Title**: 3-Antiprism

**Degree Sequence**: [4, 4, 4, 4, 4, 4]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 5], [2, 6], [3, 4], [3, 6], [4, 5], [4, 6], [5, 6]]



# **Comments:**

1. planar,

# Links:

- http://mathworld.wolfram.com/AntiprismGraph.html,
- 2. https://en.wikipedia.org/wiki/Antiprism\_graph,

#### **References**:

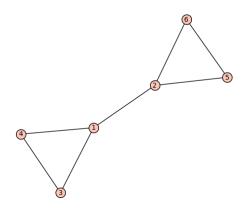
1. Alekseyev, M.; Michon, G. Making Walks Count: From Silent Circles to Hamiltonian Cycles. eprint arXiv:1602.01396. (2016),

Title: 3-Barbell

**Degree Sequence**: [3, 3, 2, 2, 2, 2]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 5], [2, 6], [3, 4], [5, 6]]



# **Comments:**

1. planar,

# Links:

- http://mathworld.wolfram.com/BarbellGraph.html,
- 2. https://en.wikipedia.org/wiki/Barbell\_graph,

#### **References**:

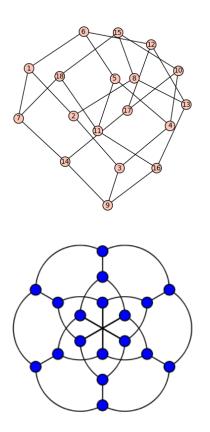
1. Wilf, H. The editor's corner: the white screen problem. Amer. Math. Monthly 96 (1989), no. 8, 704-707.

Title: Pappus Graph

**Vertices**: 18

**Edges**: [[1, 2], [1, 6], [1, 7], [2, 3], [2, 8], [3, 4], [3, 9], [4, 5], [4, 10], [5, 6], [5, 11], [6, 12], [7, 14], [7, 18], [8, 13], [8, 15], [9, 14], [9, 16], [10, 15], [10, 17], [11, 16], [11, 18], [12, 13], [12, 17], [13, 16],

[14, 17], [15, 18]]



#### **Comments:**

1. The Pappus graph is formed as the Levi graph of the Pappus configuration.,

#### Links:

- https://en.wikipedia.org/wiki/Pappus\_graph,
- 2. http://mathworld.wolfram.com/PappusGraph.html,

#### **References**:

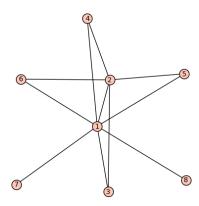
1. Coxeter, H. S. M. Self-Dual Configurations and Regular Graphs. Bull. Amer. Math. Soc. 56, 413-455, 1950. Page 434.,

**Graphlopedia ID**: G000010 **Title**: 8-Vertex Threshold Graph

**Degree Sequence**: [7, 5, 2, 2, 2, 2, 1, 1]

Vertices: 8

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [1, 7], [1, 8], [2, 3], [2, 4], [2, 5], [2, 6]]



#### **Comments:**

1. threshold, planar, and trivially perfect.,

# Links:

https://en.wikipedia.org/wiki/Threshold\_graph,

#### **References**:

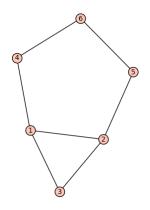
1. Heggernes, P.; Kratsch, D. Linear-time certifying recognition algorithms and forbidden induced subgraphs, Nordic Journal of Computing, 14 (1-2): 87-108 (2008),

**Graphlopedia ID**: G000011 **Title**: 6-Vertex Circular-Arc

**Degree Sequence**: [3, 3, 2, 2, 2, 2]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 3], [2, 5], [4, 6], [5, 6]]



# **Comments:**

- 1. circular-arc graph,
- 2. intersection graph,
- 3. arc,

# Links:

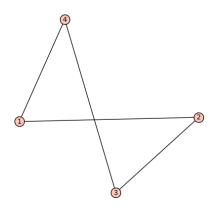
https://en.wikipedia.org/wiki/Circular-arc\_graph,

Title: 4-Cycle

**Degree Sequence**: [2, 2, 2, 2]

Vertices: 4

**Edges**: [[1, 2], [1, 4], [2, 3], [3, 4]]



#### **Comments:**

1. minimal non-trivially-perfect graph,

# Links:

https://en.wikipedia.org/wiki/Trivially\_perfect\_graph,

#### **References**:

1. Martin Charles Golumbic, Trivially perfect graphs, Discrete Mathematics, Volume 24, Issue 1, 1978, Pages 105-107.,

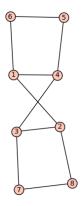
Author(s): Katrina Warner, Sara Billey.

Title: ladder graph

**Degree Sequence**: [3, 3, 3, 3, 2, 2, 2, 2]

Vertices: 8

**Edges**: [[1, 2], [1, 4], [1, 6], [2, 3], [2, 8], [3, 4], [3, 7], [4, 5], [5, 6], [7, 8]]



# **Comments:**

1. ladder graph,

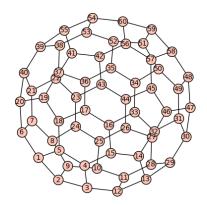
# Links:

https://en.wikipedia.org/wiki/Ladder\_graph,

Title: Truncated Icosahedral Graph

Vertices: 60

**Edges**: [[1, 2], [1, 6], [2, 3], [2, 9], [3, 4], [3, 12], [4, 5], [4, 15], [5, 1], [5, 18], [6, 7], [6, 20], [7, 8], [7, 21], [8, 9], [8, 24], [9, 10], [10, 11], [10, 25], [11, 12], [11, 28], [12, 13], [13, 14], [13, 29], [14, 15], [14, 32], [15, 16], [16, 17], [16, 33], [17, 18], [17, 36], [18, 19], [19, 20], [19, 37], [20, 40], [21, 22], [21, 40], [22, 23], [22, 41], [23, 24], [23, 43], [24, 25], [25, 26], [26, 27], [26, 44], [27, 28], [27, 46], [28, 29], [29, 30], [30, 31], [30, 47], [31, 32], [31, 49], [32, 33], [33, 34], [34, 35], [34, 50], [35, 36], [35, 52], [36, 37], [37, 38], [38, 39], [38, 53], [39, 40], [39, 55], [41, 42], [41, 55], [42, 43], [42, 56], [43, 44], [44, 45], [45, 46], [45, 57], [46, 47], [47, 48], [48, 49], [48, 58], [49, 50], [50, 51], [51, 52], [51, 59], [52, 53], [53, 54], [54, 55], [54, 60], [56, 57], [56, 60], [57, 58], [58, 59], [59, 60]]



#### **Comments:**

- 1. buckyball graph,
- 2. cayley,
- 3. 60-fullerene,

#### Links:

1. http://m.wolframalpha.com/input/?i=buckyball+graph,

#### **References:**

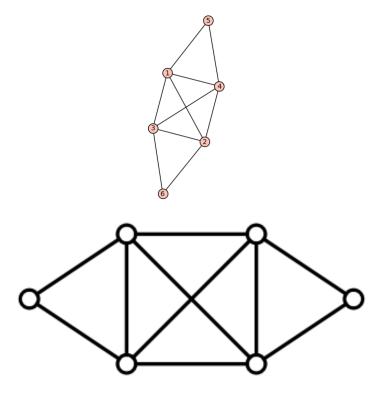
1. "Truncated Icosahedral Graph." Buckyball Graph – from Wolfram MathWorld, m.wolframalpha.com/input/?ibuckyball + graph.

Title:  $F_2$ 

**Degree Sequence**: [4, 4, 4, 4, 2, 2]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 6], [3, 4], [3, 6], [4, 5]]



#### **Comments:**

1. canonical example of a graph with an Eulerian cycle,

# **References**:

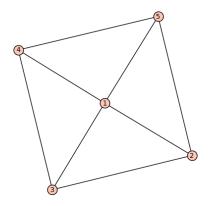
1. N. Chiarelli, Martin Milanic, A threshold approach to connected domination, University of Primorska, 2016. Page 4.,

Title: 5-Wheel Graph

**Degree Sequence**: [4, 3, 3, 3, 3]

Vertices: 5

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 5], [3, 4], [4, 5]]



# **Comments:**

1. wheel graph  $W_5$ ,

# Links:

http://mathworld.wolfram.com/WheelGraph.html,

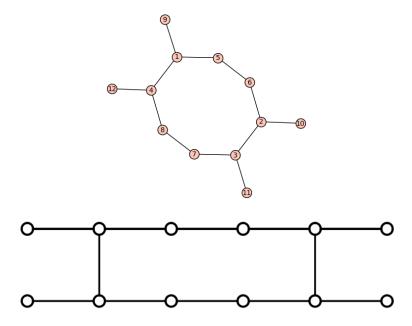
2. https://en.wikipedia.org/wiki/Wheel\_graph,

**Graphlopedia ID**: G000017 **Title**: Total Domishold Raft

**Degree Sequence**: [3, 3, 3, 3, 2, 2, 2, 2, 1, 1, 1, 1]

Vertices: 12

**Edges**: [[1, 4], [1, 5], [1, 9], [2, 3], [2, 6], [2, 10], [3, 7], [3, 11], [4, 8], [4, 12], [5, 6], [7, 8]]



#### **Comments:**

1. A total domishold graph that is not connected-domishold,

# Links:

arxiv.org/pdf/1610.06539v1.pdf,

#### **References**:

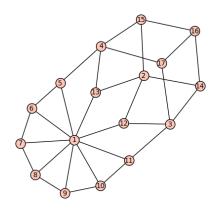
1. Chiarelli, Nina, and Martin Milanic. "A Threshold Approach to Connected Domination." 21 Oct. 2016, arxiv.org/pdf/1610.06539v1.pdf.,

Title:  $G_k K_{2,6}$  free

Vertices: 17

**Edges**: [[1, 5], [1, 6], [1, 7], [1, 8], [1, 9], [1, 10], [1, 11], [1, 12], [1, 13], [2, 12], [2, 13], [2, 14], [2, 15], [3, 11], [3, 12], [3, 14], [3, 17], [4, 5], [4, 13], [4, 15], [4, 17], [5, 6], [6, 7], [7, 8], [8, 9], [9, 10],

[10, 11], [14, 16], [15, 16], [16, 17]]



#### **Comments**:

- 1. 3-connected,
- 2.  $G_k$  where  $k \geq 1$ ,

#### **References**:

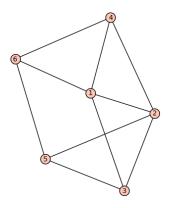
1. Ellingham, M. N. et al. "Hamiltonicity of Planar Graphs with a Forbidden Minor." ArXiv, ArXiv, 20 Oct. 2016, arxiv.org/pdf/1610.06558v1.pdf.,

**Graphlopedia ID**: G000019 **Title**: hexahedral graph 3

**Degree Sequence**: [4, 4, 3, 3, 3, 3]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 6], [2, 3], [2, 4], [2, 5], [3, 5], [4, 6], [5, 6]]



# **Comments:**

1. polyhedral graph,

# Links:

http://mathworld.wolfram.com/PolyhedralGraph.html,

#### **References**:

1. "Polyhedral Graph." Polyhedral Graph – from Wolfram MathWorld, mathworld.wolfram.com/PolyhedralGraph Author(s): Aaron Bode.

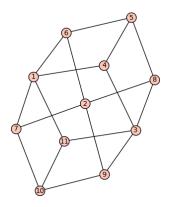
Title: Herschel Graph

**Degree Sequence**: [4, 4, 4, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 11

**Edges**: [[1, 4], [1, 6], [1, 7], [1, 11], [2, 6], [2, 7], [2, 8], [2, 9], [3, 4], [3, 8], [3, 9], [3, 11], [4, 5], [5, 6],

[5, 8], [7, 10], [9, 10], [10, 11]]



#### **Comments:**

- 1. smallest nonhamiltonion polyhedral graph,
- 2. planar,

#### Links:

http://mathworld.wolfram.com/HerschelGraph.html,

#### **References**:

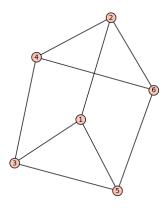
 $1. \ \ "Herschel Graph." \ Herschel Graph-from \ Wolfram \ Math World, \\ math world. \\ wolfram.com/Herschel Graph. \\ ht world. \\ math world. \\ wolfram.com/Herschel Graph. \\ ht world. \\ wolfram. \\ math world. \\ wolfram. \\$ 

**Title**: 3-regular graph 1

**Degree Sequence**: [3, 3, 3, 3, 3, 3]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 5], [2, 4], [2, 6], [3, 4], [3, 5], [4, 6], [5, 6]]



# **References**:

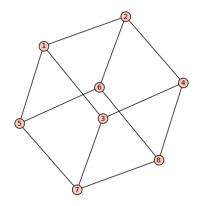
1. Kong, Qi, and Ligong Wang. "The Signless Laplacian Spectral Radius of Subgraphs of Regular Graphs." https://Arxiv.org/Pdf/1610.08855v1.Pdf, ArXiv, 28 Oct. 2016, arxiv.org/pdf/1610.08855v1.pdf.,

Title: 3-regular graph 2

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 8

**Edges**: [[1, 2], [1, 3], [1, 5], [2, 4], [2, 6], [3, 4], [3, 7], [4, 8], [5, 6], [5, 7], [6, 8], [7, 8]]



# **References**:

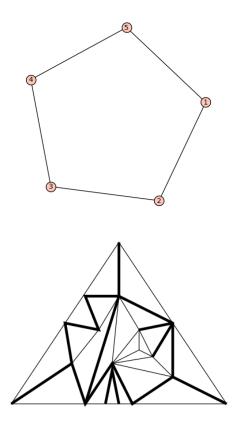
1. Q. Kong, L. Wang, The signless Laplacian spectral radius of subgraphs of regular graphs, Department of Applied Mathematics, School of Science, Northwestern Polytechnical University, 2016.,

Title: 5-Cycle,  $C_5$ 

**Degree Sequence**: [2, 2, 2, 2, 2]

Vertices: 5

**Edges**: [[1, 2], [1, 5], [2, 3], [3, 4], [4, 5]]



# Links:

https://en.wikipedia.org/wiki/Cycle\_graph,

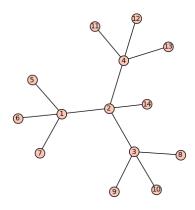
Author(s): Zachary Hamaker.

Title: Isobutane Molecule

**Degree Sequence**: [4, 4, 4, 4, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]

Vertices: 14

**Edges**: [[1, 2], [1, 5], [1, 6], [1, 7], [2, 3], [2, 4], [2, 14], [3, 8], [3, 9], [3, 10], [4, 11], [4, 12], [4, 13]]



#### **Comments:**

- 1. connected forest,
- 2. tree graph,
- 3. Error in pubchem link, I don't see the graph there, but it is about isobutane mol-SB,

#### Links:

- http://mathworld.wolfram.com/Tree.html,
- 2. https://pubchem.ncbi.nlm.nih.gov/compound/isobutane,

#### **References**:

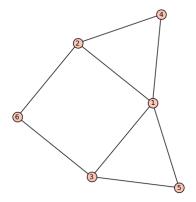
1. Tree – from Wolfram MathWorld, mathworld.wolfram.com/Tree.html.,

**Title**: Projective embedding of the positive roots of type  $A_3$ 

**Degree Sequence**: [4, 3, 3, 2, 2, 2]

Vertices: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 4], [2, 6], [3, 5], [3, 6]]



#### **Comments:**

1. Vertices are the intersections of the lines generated by the positive roots with a certain affine hyperplane. Lines represent two dimensional spans.,

# **References:**

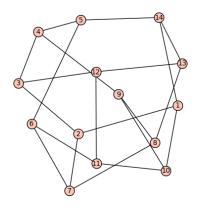
1. S. Billey and A. Postnikov. Smoothness of Schubert varieties via patterns in root subsystems. Advances in Applied Mathematics, vol 34 (2005). Page 453.,

Title: Heawood Graph

Vertices: 14

**Edges**: [[1, 2], [1, 10], [1, 14], [2, 3], [2, 7], [3, 4], [3, 12], [4, 5], [4, 9], [5, 6], [5, 14], [6, 7], [6, 11],

[7, 8], [8, 9], [8, 13], [9, 10], [10, 11], [11, 12], [12, 13], [13, 14]]



#### **Comments:**

- 1. cage graph,
- 2. non-planar,

#### Links:

http://mathworld.wolfram.com/HeawoodGraph.html,

#### **References**:

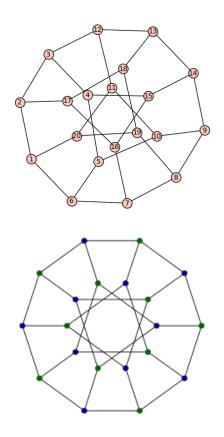
1. Y. Zhao, Extremal regular graphs: independent sets and graph homomorphisms, 2016.,

Title: Desargues' Graph

Vertices: 20

**Edges**: [[1, 2], [1, 6], [1, 20], [2, 3], [2, 17], [3, 4], [3, 12], [4, 5], [4, 15], [5, 6], [5, 10], [6, 7], [7, 8], [7, 16], [8, 9], [8, 19], [9, 10], [9, 14], [10, 11], [11, 12], [11, 20], [12, 13], [13, 14], [13, 18], [14, 15],

[15, 16], [16, 17], [17, 18], [18, 19], [19, 20]]



#### **Comments:**

- 1. cubic-symmetric graph,
- 2. Desargues graph is the first of four graphs depicted on the cover of Harary (1994).,

#### Links:

- http://mathworld.wolfram.com/DesarguesGraph.html,
- 2. https://en.wikipedia.org/wiki/Desargues\_graph,

#### **References**:

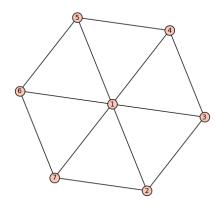
1. Kagno, I. N. Desargues' and Pappus' Graphs and Their Groups. Amer. J. Math. 69, 859-863, 1947.,

**Title**: Figure 2(a)

**Degree Sequence**: [6, 3, 3, 3, 3, 3, 3]

Vertices: 7

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [1, 7], [2, 3], [2, 7], [3, 4], [4, 5], [5, 6], [6, 7]]



# Links:

https://arxiv.org/pdf/math/0608624.pdf,

# **References**:

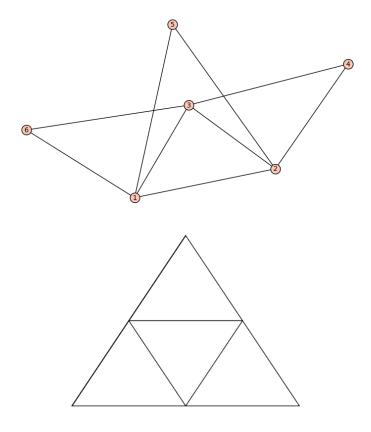
1. W. Wood. Combinatorial Modulus and Types of Graphs, 2006.,

**Title**: Figure 2(b)

**Degree Sequence**: [4, 4, 4, 2, 2, 2]

**Vertices**: 6

**Edges**: [[1, 2], [1, 3], [1, 5], [1, 6], [2, 3], [2, 4], [2, 5], [3, 4], [3, 6]]



# Links:

1. https://arxiv.org/pdf/math/0608624.pdf],,

# **References**:

1. W. Wood. Combinatorial Modulus and Types of Graphs, 2006.,

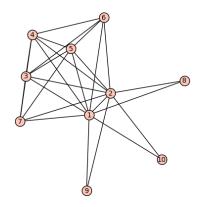
Title: threshold graph 2

**Degree Sequence**: [9, 9, 6, 6, 6, 5, 5, 2, 2, 2]

Vertices: 10

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [1, 7], [1, 8], [1, 9], [1, 10], [2, 3], [2, 4], [2, 5], [2, 6], [2, 7],

[2, 8], [2, 9], [2, 10], [3, 4], [3, 5], [3, 6], [3, 7], [4, 5], [4, 6], [4, 7], [5, 6], [5, 7]]



#### **Comments:**

1. threshold graph with binary string 0011100011,

# **References**:

1. A. Banerjee1, R. Mehatari. On the normalized spectrum of threshold graphs, Indian Institute of Science Education and Research Kolkata, 2016.,

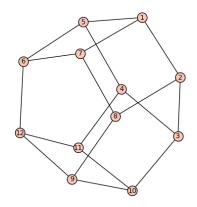
Title: Plabic Graph

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 12

**Edges**: [[1, 2], [1, 5], [1, 7], [2, 3], [2, 8], [3, 4], [3, 10], [4, 5], [4, 11], [5, 6], [6, 7], [6, 12], [7, 8], [8,

9], [9, 10], [9, 12], [10, 11], [11, 12]]



#### **Comments:**

- 1. plabic,
- 2. nonplanar,
- 3. undirected,

#### Links:

1. https://arxiv.org/pdf/1106.0023.pdf,

# **References**:

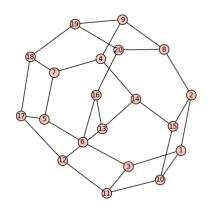
1. Y. Kodoma, L. Williams. KP Solutions and Total Positivity for the Grassmannian, 2014.,

Title: Figure 8

Vertices: 20

**Edges**: [[1, 2], [1, 3], [1, 10], [2, 8], [2, 15], [3, 6], [3, 11], [4, 7], [4, 9], [4, 14], [5, 6], [5, 7], [5, 17], [6, 16], [7, 18], [8, 9], [8, 20], [9, 19], [10, 11], [10, 15], [11, 12], [12, 13], [12, 17], [13, 14], [13, 16],

[14, 15], [16, 20], [17, 18], [18, 19], [19, 20]]



#### **Comments:**

- 1. soliton,
- 2. plabic,

#### Links:

1. https://arxiv.org/pdf/1106.0023.pdf,

#### **References**:

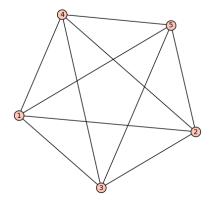
1. Y. Kodoma, L. Williams. KP Solutions and Total Positivity for the Grassmannian, 2014.,

**Title**: Figure 5

**Degree Sequence**: [4, 4, 4, 4, 4]

Vertices: 5

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 5], [3, 4], [3, 5], [4, 5]]



# Links:

1. https://arxiv.org/pdf/1106.0023.pdf,

# **References**:

1. M. Han. Cosmological Constant in LQG Vertex Amplitude, 2011.,

Title: 6-cycle

**Degree Sequence**: [2, 2, 2, 2, 2, 2]

**Vertices**: 6

**Edges**: [[1, 2], [1, 6], [2, 3], [3, 4], [4, 5], [5, 6]]

Links:

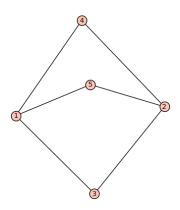
https://en.wikipedia.org/wiki/Cycle\_graph,

**Title**: Complete Bipartite Graph  $K_{2,3}$ 

**Degree Sequence**: [3, 3, 2, 2, 2]

Vertices: 5

**Edges**: [[1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 5]]



#### **Comments:**

1. The class of outerplanar graphs is closed under minor taking: its obstruction set consists of the graphs  $K_{2,3}$  and  $K_4$ .

# **References:**

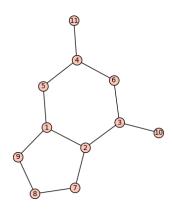
- 1. H.L. Bodlaender. A partial k-arboretum of graphs with bounded treewidth, Theoretical Computer Science 209. (1998). Page. 34,
- 2. M.M. Syslo, Characterisations of outerplanar graphs, Discrete Math. 26 (1979) 47-53.,

**Graphlopedia ID**: G000036 **Title**: Guanine Structure

**Degree Sequence**: [3, 3, 3, 3, 2, 2, 2, 2, 2, 1, 1]

Vertices: 11

**Edges**: [[1, 2], [1, 5], [1, 9], [2, 3], [2, 7], [3, 6], [3, 10], [4, 5], [4, 6], [4, 11], [7, 8], [8, 9]]



# Links:

https://arxiv.org/pdf/cs/0703132.pdf,

# **References**:

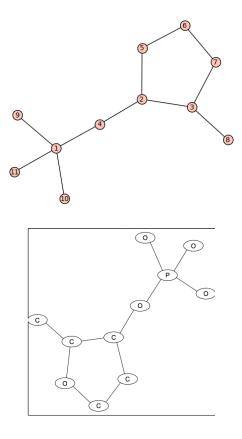
1. L. Peshkin. Center for Biomedical Informatics, Harvard Medical School."Structure Induction by Lossless Graph Compression" (2007).,

Title: Sugar

**Degree Sequence**: [4, 3, 3, 2, 2, 2, 2, 1, 1, 1, 1]

Vertices: 11

**Edges**: [[1, 4], [1, 9], [1, 10], [1, 11], [2, 3], [2, 4], [2, 5], [3, 7], [3, 8], [5, 6], [6, 7]]



#### **Comments:**

- 1. The compound object induced by the Graphitour algorithm, which corresponds to the backbone of the molecule: phosphate and sugar.,
- 2. Error in GRAPH: G000037 degree seq [4, 3, 3, 2, 2, 2, 2, 1, 1, 1, 1] should be [4, 3, 3, 2, 1, 0, 1, 1, 1, 1, 1] [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11] [[1, 4], [1, 9], [1, 10], [1, 11], [2, 3], [2, 4], [2, 5], [3, 7], [3, 8]],

# Links:

1. https://arxiv.org/pdf/cs/0703132.pdf,

#### **References:**

1. L. Peshkin. Structure Induction by Lossless Graph Compression, (2007).,

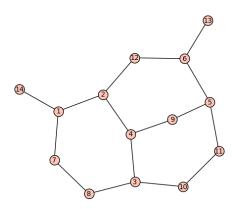
# **Graphlopedia ID**: G000038 **Title**: Original Factor Graph

 $\textbf{Degree Sequence} \colon [3, 3, 3, 3, 3, 3, 2, 2, 2, 2, 2, 2, 1, 1]$ 

Vertices: 14

**Edges**: [[1, 2], [1, 7], [1, 14], [2, 4], [2, 12], [3, 4], [3, 8], [3, 10], [4, 9], [5, 6], [5, 9], [5, 11], [6, 12],

[6, 13], [7, 8], [10, 11]]



# Links:

1. https://arxiv.org/pdf/cs/0612030.pdf,

# **References**:

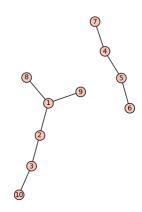
1. J. Mooji, B. Kappen. "Loop Corrections for Approximate Inference" (2006),

Title: Cavity Graph of i

**Degree Sequence**: [3, 2, 2, 2, 2, 1, 1, 1, 1, 1]

**Vertices**: 10

**Edges**: [[1, 2], [1, 8], [1, 9], [2, 3], [3, 10], [4, 5], [4, 7], [5, 6]]



# Links:

1. https://arxiv.org/pdf/cs/0612030.pdf,

# **References**:

1. J. Mooji, B. Kappen. "Loop Corrections for Approximate Inference" (2006),

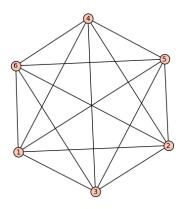
Title: Fig.1

**Degree Sequence**: [5, 5, 5, 5, 5, 5]

**Vertices**: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [2, 3], [2, 4], [2, 5], [2, 6], [3, 4], [3, 5], [3, 6], [4, 5], [4, 6],

[5, 6]]



# Links:

1. https://arxiv.org/pdf/hep-th/0611042.pdf,

# **References**:

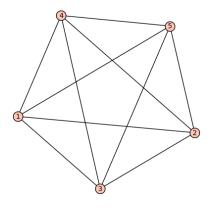
1. A. Baratin, L. Friedel. Perimeter Institute for Theoretical Physics. "Hidden Quantum Gravity in 4d Feynman Diagrams" (2007),

Title: K5 Graph

**Degree Sequence**: [4, 4, 4, 4, 4]

Vertices: 5

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 5], [3, 4], [3, 5], [4, 5]]



# Links:

https://arxiv.org/pdf/hep-th/0611042.pdf,

# **References**:

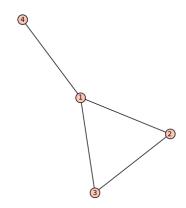
1. A. Baratin, L. Friedel. Perimeter Institute for Theoretical Physics. "Hidden Quantum Gravity in 4d Feynman Diagrams" (2007),

**Title**: Figure 1

**Degree Sequence**: [3, 2, 2, 1]

Vertices: 4

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 3]]



# Links:

1. https://arxiv.org/pdf/1304.0478.pdf,

# **References**:

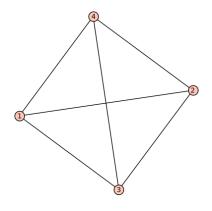
1. Z. Cinkir. "Explicit Computation of Certain Arakelov-Green Functions" (2013).,

**Graphlopedia ID**: G000043 **Title**: Tetrahedral Graph

**Degree Sequence**: [3, 3, 3, 3]

Vertices: 4

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 3], [2, 4], [3, 4]]



# Links:

1. https://arxiv.org/pdf/1304.0478.pdf,

# **References**:

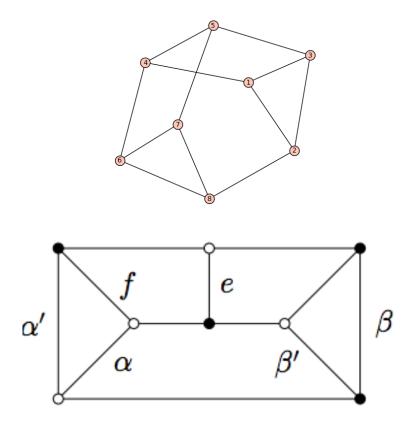
1. Z. Cinkir. "Explicit Computation of Certain Arakelov-Green Functions" (2013).,

Title: The staircase of order eight, St8

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 8

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 3], [2, 8], [3, 5], [4, 5], [4, 6], [5, 7], [6, 7], [6, 8], [7, 8]]



# Links:

1. https://arxiv.org/pdf/1611.07899.pdf,

#### **References**:

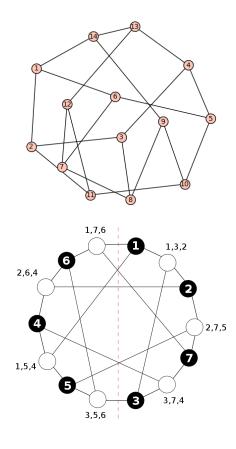
1. N. Kothari. "Generating Near-Bipartite Bricks" arXiv (2016). Page 4.,

Title: Fano Graph

Vertices: 14

**Edges**: [[1, 2], [1, 6], [1, 14], [2, 3], [2, 11], [3, 4], [3, 8], [4, 5], [4, 13], [5, 6], [5, 10], [6, 7], [7, 8], [7,

12], [8, 9], [9, 10], [9, 14], [10, 11], [11, 12], [12, 13], [13, 14]]



#### **Comments:**

1. The Fano graph is formed as the Levi graph of the Fano plane.,

#### Links:

- 1. https://commons.wikimedia.org/wiki/File:Fano\_plane-Levi\_graph.svg,
- 2. https://en.wikipedia.org/wiki/Levi\_graph,
- 3. https://en.wikipedia.org/wiki/Fano\_plane,

#### **References**:

1. Coxeter, H. S. M. Self-Dual Configurations and Regular Graphs. Bull. Amer. Math. Soc. 56, 413-455, 1950. Page 424.,

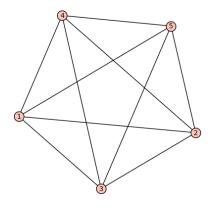
**Author(s)**: Sara Billey.

**Graphlopedia ID**: G000046 **Title**: Complete Bipartite  $K_5$ 

**Degree Sequence**: [4, 4, 4, 4, 4]

Vertices: 5

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 5], [3, 4], [3, 5], [4, 5]]



# **Comments:**

1. Nonplanar,

# Links:

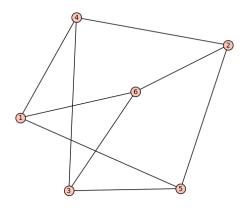
https://en.wikipedia.org/wiki/Planar\_graph,

**Graphlopedia ID**: G000047 **Title**: Complete Bipartite  $K_{3,3}$ 

**Degree Sequence**: [3, 3, 3, 3, 3, 3]

**Vertices**: 6

**Edges**: [[1, 4], [1, 5], [1, 6], [2, 4], [2, 5], [2, 6], [3, 4], [3, 5], [3, 6]]



# **Comments:**

1. Nonplanar,

# Links:

https://en.wikipedia.org/wiki/Planar\_graph,

2. http://mathworld.wolfram.com/NonplanarGraph.html,

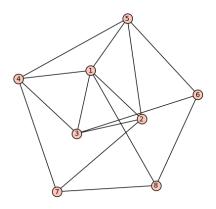
**Title**: Petersen Graph 1

**Degree Sequence**: [5, 4, 4, 4, 4, 3, 3, 3]

Vertices: 8

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 8], [2, 3], [2, 5], [2, 7], [3, 4], [3, 6], [4, 5], [4, 7], [5, 6], [6, 8],

[7, 8]]



# **Comments:**

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

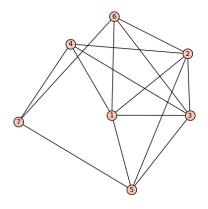
**Title**: Petersen Graph 2

**Degree Sequence**: [5, 5, 5, 4, 4, 4, 3]

Vertices: 7

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [2, 3], [2, 4], [2, 5], [2, 6], [3, 4], [3, 5], [3, 6], [4, 7], [5, 7],

[6, 7]]



# **Comments:**

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

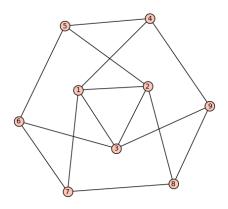
**Title**: Petersen Graph 3

**Degree Sequence**: [4, 4, 4, 3, 3, 3, 3, 3, 3]

**Vertices**: 9

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 7], [2, 3], [2, 5], [2, 8], [3, 6], [3, 9], [4, 5], [4, 9], [5, 6], [6, 7], [7, 8],

[8, 9]]



# **Comments:**

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

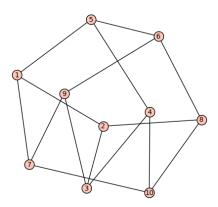
Title: Petersen Graph 4

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 10

**Edges**: [[1, 2], [1, 5], [1, 7], [2, 3], [2, 8], [3, 4], [3, 9], [4, 5], [4, 10], [5, 6], [6, 8], [6, 9], [7, 9], [7, 10],

[8, 10]]



#### **Comments**:

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

# **References**:

1. Y. Zhao, Extremal regular graphs: independent sets and graph homomorphisms, 2016.,

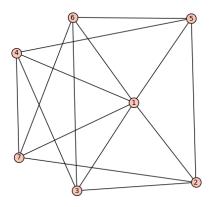
Title: Petersen Graph 5

**Degree Sequence**: [6, 4, 4, 4, 4, 4, 4]

Vertices: 7

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [1, 7], [2, 3], [2, 5], [2, 7], [3, 4], [3, 6], [4, 5], [4, 7], [5, 6],

[6, 7]]



# **Comments:**

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

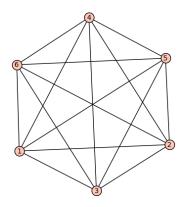
**Graphlopedia ID**: G000053 **Title**: Petersen Graph 6

**Degree Sequence**: [5, 5, 5, 5, 5, 5]

**Vertices**: 6

**Edges**: [[1, 2], [1, 3], [1, 4], [1, 5], [1, 6], [2, 3], [2, 4], [2, 5], [2, 6], [3, 4], [3, 5], [3, 6], [4, 5], [4, 6],

[5, 6]]



# **Comments:**

1. Petersen graph,

# Links:

https://en.wikipedia.org/wiki/Petersen\_family,

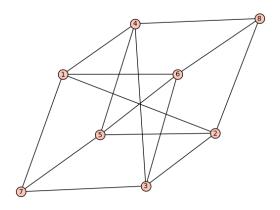
**Title**: Petersen Graph 7

**Degree Sequence**: [4, 4, 4, 4, 4, 4, 3, 3]

Vertices: 8

**Edges**: [[1, 2], [1, 4], [1, 6], [1, 7], [2, 3], [2, 5], [2, 8], [3, 4], [3, 6], [3, 7], [4, 5], [4, 8], [5, 6], [5, 7],

[6, 8]]



# **Comments:**

1. Petersen graph,

# Links:

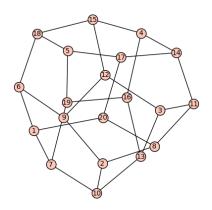
https://en.wikipedia.org/wiki/Petersen\_family,

Title: Starfish

Vertices: 20

**Edges**: [[1, 6], [1, 7], [1, 20], [2, 8], [2, 9], [2, 10], [3, 11], [3, 12], [3, 13], [4, 14], [4, 15], [4, 16], [5, 17], [5, 18], [5, 19], [6, 9], [6, 18], [7, 10], [7, 19], [8, 11], [8, 20], [9, 12], [10, 13], [11, 14], [12, 15], [12, 15], [13, 15], [14, 15], [15, 16], [15

[13, 16], [14, 17], [15, 18], [16, 19], [17, 20]]



#### **Comments:**

1. Let G be theta-connected, and not contain Petersen. If G contains Starfish then G is isomorphisc to Starfish.,

#### **References:**

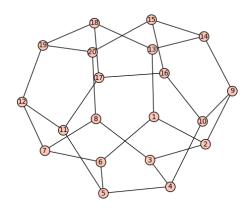
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995.,

Title: Jaws

Vertices: 20

**Edges**: [[1, 2], [1, 6], [1, 13], [2, 3], [2, 9], [3, 4], [3, 8], [4, 5], [4, 10], [5, 6], [5, 11], [6, 7], [7, 8], [7, 12], [8, 20], [9, 10], [9, 14], [10, 16], [11, 12], [11, 17], [12, 19], [13, 14], [13, 18], [14, 15], [15, 16],

[15, 20], [16, 17], [17, 18], [18, 19], [19, 20]]



#### **Comments:**

1. Let G be theta-connected, and not contain Petersen. If G contains Jaws then G is doublecross.,

#### **References**:

1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995.,

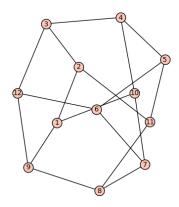
Title: Triplex

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 12

**Edges**: [[1, 2], [1, 9], [1, 10], [2, 3], [2, 11], [3, 4], [3, 12], [4, 5], [4, 10], [5, 6], [5, 11], [6, 7], [6, 12],

[7, 8], [7, 10], [8, 9], [8, 11], [9, 12]]



#### **Comments:**

1. Petersen, Triplex and Box are the only graphs minimal with the property of being dodecahedrally-connected and having crossing number > 1.,

#### Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

#### **References**:

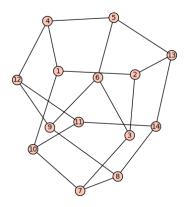
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995.,

Title: Box

Vertices: 14

**Edges**: [[1, 2], [1, 4], [1, 10], [2, 3], [2, 13], [3, 6], [3, 7], [4, 5], [4, 12], [5, 6], [5, 13], [6, 9], [7, 8], [7,

10], [8, 9], [8, 14], [9, 12], [10, 11], [11, 12], [11, 14], [13, 14]]



#### **Comments:**

1. Petersen, Triplex and Box are the only graphs minimal with the property of being dodecahedrally-connected and having crossing number > 1.,

#### Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

#### **References:**

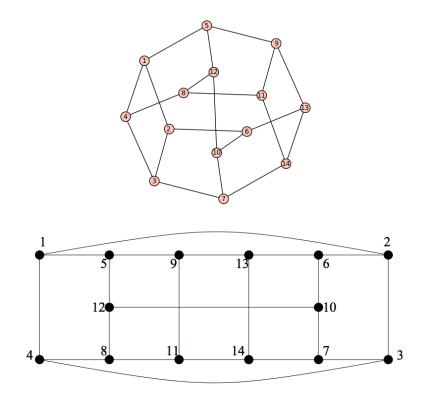
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995.,

Title: Antibox

Vertices: 14

**Edges**: [[1, 2], [1, 4], [1, 5], [2, 3], [2, 6], [3, 4], [3, 7], [4, 8], [5, 9], [5, 12], [6, 10], [6, 13], [7, 10], [7,

14], [8, 11], [8, 12], [9, 11], [9, 13], [10, 12], [11, 14], [13, 14]]



#### Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

# **References**:

1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995. Page 36.,

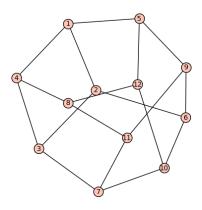
Title: Window

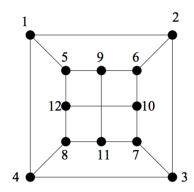
**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 12

**Edges**: [[1, 2], [1, 4], [1, 5], [2, 3], [2, 6], [3, 4], [3, 7], [4, 8], [5, 9], [5, 12], [6, 9], [6, 10], [7, 10], [7,

11], [8, 11], [8, 12], [9, 11], [10, 12]]





# Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

# **References**:

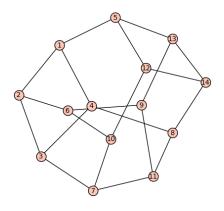
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995. Page 36.,

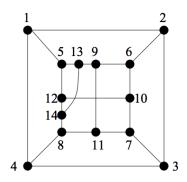
Title: Drape

Vertices: 14

**Edges**: [[1, 2], [1, 4], [1, 5], [2, 3], [2, 6], [3, 4], [3, 7], [4, 8], [5, 12], [5, 13], [6, 9], [6, 10], [7, 10], [7,

11], [8, 11], [8, 14], [9, 11], [9, 13], [10, 12], [12, 14], [13, 14]]





# Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

#### **References**:

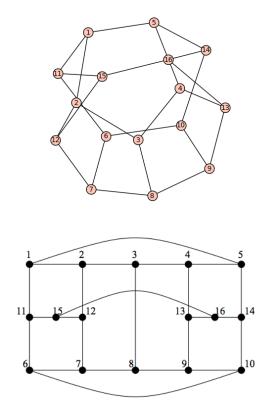
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995. Page 36.,

Title: Superbox

Vertices: 16

**Edges**: [[1, 2], [1, 5], [1, 11], [2, 3], [2, 12], [3, 4], [3, 8], [4, 5], [4, 13], [5, 14], [6, 7], [6, 10], [6, 11],

[7, 8], [7, 12], [8, 9], [9, 10], [9, 13], [10, 14], [11, 15], [12, 15], [13, 16], [14, 16], [15, 16]



#### **Comments:**

1. Related to Box, G000058,

#### Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

#### **References**:

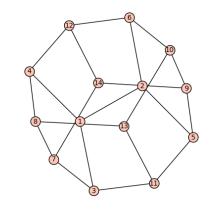
1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995. Page 39.,

Title: Drum

Vertices: 14

**Edges**: [[1, 2], [1, 3], [1, 4], [2, 5], [2, 6], [3, 7], [3, 11], [4, 8], [4, 12], [5, 9], [5, 11], [6, 10], [6, 12],

[7, 8], [7, 14], [8, 13], [9, 10], [9, 14], [10, 13], [11, 13], [12, 14]]



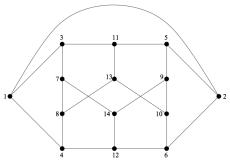


Figure 10: Drum.

# Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

#### **References**:

1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995. Page 41.,

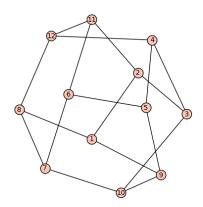
Title: Twinplex

**Degree Sequence**: [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3]

Vertices: 12

**Edges**: [[1, 2], [1, 8], [1, 9], [2, 3], [2, 11], [3, 4], [3, 10], [4, 5], [4, 12], [5, 6], [5, 9], [6, 7], [6, 11], [7,

8], [7, 10], [8, 12], [9, 10], [11, 12]]



# Links:

1. https://arxiv.org/pdf/1403.2118.pdf,

# **References**:

1. N. Robertson, P. Seymour, R. Thomas, Excluded Minors in Cubic Graphs, 1995.,