## Benchmark Results for VeriNet

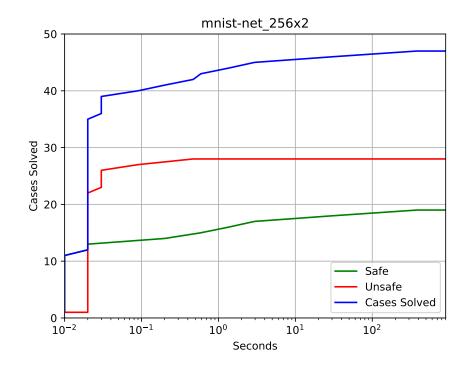
July 13, 2020

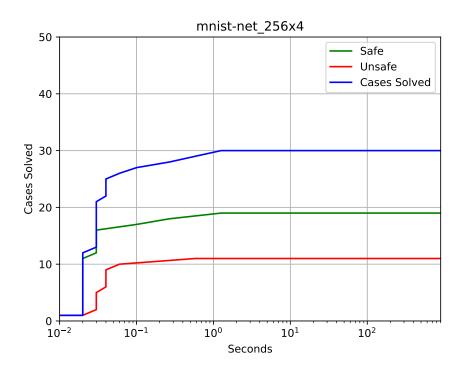
## 1 About

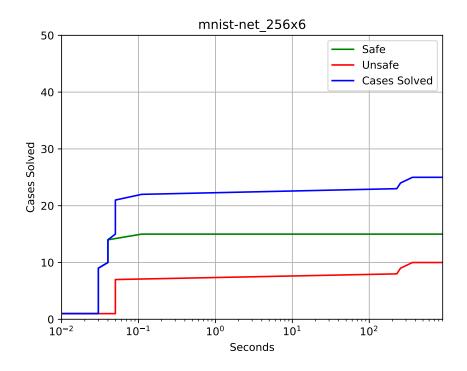
We here present our results for the 2020 vnn-comp with the VeriNet toolkit [1]. The VeriNet toolkit is a state-of-the-art symbolic-interval propagation-based toolkit for local robustness properties and supports ReLU, Sigmoid, Tanh activation functions and Fully-Connected, Convolutional and Batch-normalisation layers.

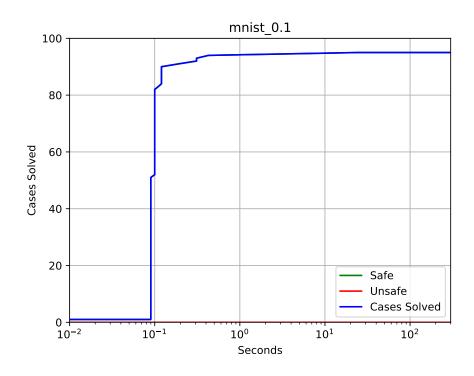
We ran our toolkit on benchmarks in all three categories; however, we did not evaluate the ACAS Xu Benchmarks as VeriNet does not support all of the properties at this point. We Also did not evaluate VeriNet on all of the Cifar10 convolutional networks due to time constraints. We ran all benchmarks on a workstation with a Ryzen 3700X 3.6 GHz 8-core CPU, 64 GB ram running Ubuntu 20.04 LTS with Linux kernel 5.4.0.

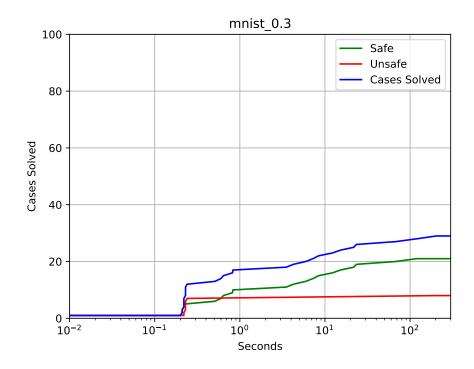
## 2 Results

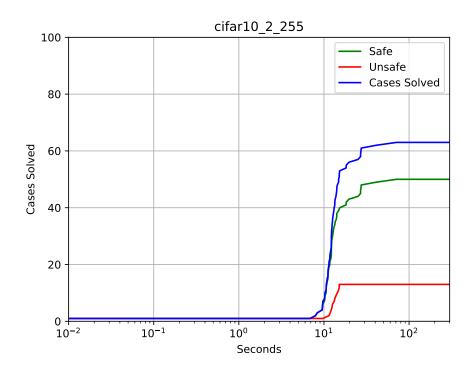


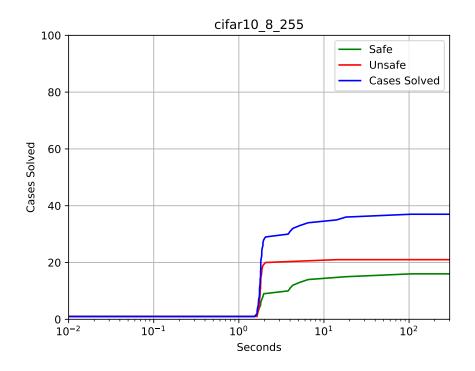


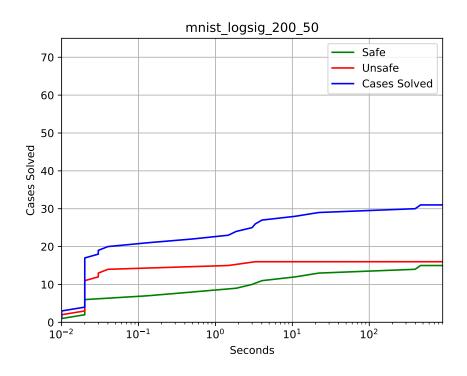


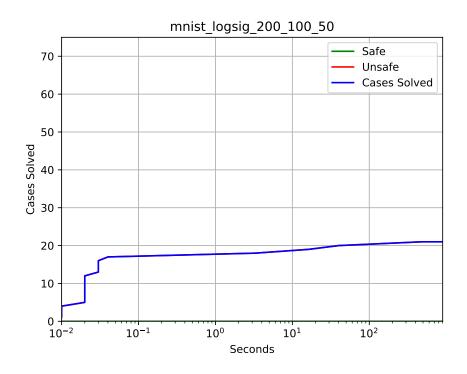


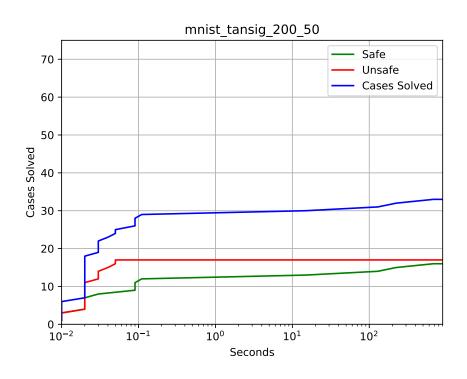












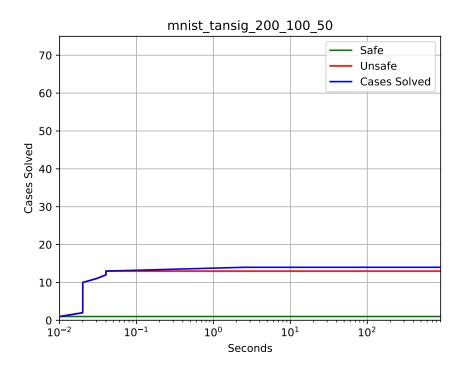


Table 1: mnist-net 256x2

E <sub>1</sub>	psilon: 0.0	020		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Image Status Ti	
0	Unsafe	0.09	0	Unsafe	0.02
1	Safe	0.01	1	Unsafe	0.02
2	Unsafe	0.02	2	Unsafe	0.02
3	Safe	0.01	3	Unsafe	0.02
4	Unsafe	0.02	4	Unsafe	0.02
5	Safe	0.2	5	Unsafe	0.02
6	Safe	378.33	6	Unsafe	0.02
7	Safe	2.94	7	Unsafe	0.02
8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	0.01	9	Unsafe	0.02
10 Safe		0.01	10	Undecided	900.0
11	Safe	0.01	11	Unsafe	0.03
12	Safe	0.01	12 Unsafe		0.02
13	Safe	0.01	13	13 Unsafe	
14	Safe	0.01	14	Unsafe	0.47
15	Safe	0.01	15	Undecided	900.0
16	Safe	0.01	16	Unsafe	0.03
17	Safe	30.92	17	Unsafe	0.02
18	Unsafe	0.03	18	Unsafe	0.02
19	Safe	0.59	19	Unsafe	0.02
20	Safe	0.02	20	Unsafe	0.02
21	Safe	1.36	21	Unsafe	0.02
22	Safe	0.02	22	Undecided	900.0
23	Safe	0.01	23	Unsafe	0.03
24	Unsafe	0.02	24	Unsafe	0.02

Table 2: mnist-net 256x4

	Epsilon: 0.02	:0		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe 0.1		0	Undecided	900.0
1	Safe	0.02	1	Undecided	900.0
2	Undecided	900.0	2	Unsafe	0.58
3	Safe	0.03	3	Undecided	900.0
4	Safe	0.02	4	Undecided	900.0
5	Safe	0.27	5	Undecided	900.0
6	Safe	0.03	6	Unsafe	0.04
7	Undecided	900.0	7	Unsafe	0.03
8	Safe	1.26	8	Unsafe	0.03
9	Safe	0.03	9	Undecided	900.0
10	Safe 0.0		10	Undecided	900.0
11	Safe	0.02	11	Undecided	900.0
12	Safe	0.02	12	Undecided	900.0
13	Safe	0.02	13	Undecided	900.0
14	Safe	0.02	14	Unsafe	0.04
15	Safe	0.02	15	Undecided	900.0
16	Undecided	900.0	16	Unsafe	0.06
17	Safe	0.03	17	Undecided	900.0
18	Unsafe	0.02	18	Unsafe	0.04
19	Safe	0.02	19	Unsafe	0.03
20	Undecided	900.0	20	Unsafe	0.03
21	Safe	0.03	21	Undecided	900.0
22	Safe	0.02	22	Undecided	900.0
23	Safe	0.02	23	Undecided	900.0
24	Undecided	900.0	24	Unsafe	0.04

Table 3: mnist-net 256x6

	Epsilon: 0.02	:0		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.11	0	Unsafe	363.99
1	Safe	0.03	1	Undecided	900.0
2	Undecided	900.0	2	Unsafe	0.05
3	Safe	0.04	3	Undecided	900.0
4	Safe	0.03	4	Undecided	900.0
5	Undecided	900.0	5	Undecided	900.0
6	Undecided	900.0	6	Unsafe	0.05
7	Undecided	900.0	7	Unsafe	254.71
8	Unsafe	0.05	8	Unsafe	0.05
9	Safe	0.03	9	Undecided	900.0
10	Safe 0.03		10	Undecided	900.0
11	Safe 0.03		11	Unsafe	0.05
12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.04	13	Undecided	900.0
14	Safe	0.03	14	Undecided	900.0
15	Safe	0.03	15	Undecided	900.0
16	Undecided	900.0	16	Unsafe	227.87
17	Safe	0.04	17	Undecided	900.0
18	Undecided	900.0	18	Unsafe	0.05
19	Safe	0.04	19	Undecided	900.0
20	Undecided	900.0	20	Undecided	900.0
21	Safe	0.04	21	Undecided	900.0
22	Safe	0.03	22	Undecided	900.0
23	Safe	0.03	23	Undecided	900.0
24	Undecided	900.0	24	Unsafe	0.05

Table 4: mnist 0.1

	Epsilon: 0.10	00		Epsilon: 0.10	00
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.19	50	Safe	0.1
1	Safe	0.1	51	Safe	0.09
2	Safe	0.1	52	Safe	0.1
3	Safe	0.1	53	Safe	0.09
4	Safe	0.1	54	Safe	0.1
5	Safe	0.09	55	Safe	0.1
6	Undecided	300.0	56	Safe	0.09
7	Safe	0.12	57	Safe	0.1
8	Undecided	300.0	58	Safe	0.1
9	Safe	0.12	59	Safe	0.43
10	Safe	0.09	60	Safe	0.12
11	Safe	0.09	61	Safe	0.09
12	Safe	0.09	62	Undecided	300.0
13	Safe	0.09	63	Safe	0.12
14	Safe	0.09	64	Safe	0.1
15	Safe	0.09	65	Safe	24.58
16	Safe	0.09	66	Safe	0.12
17	Safe	0.09	67	Safe	0.09
18	Undecided	300.0	68	Safe	0.1
19	Safe	0.12	69	Safe	0.09
20	Safe	0.09	70	Safe	0.1
21	Safe	0.09	71	Safe	0.09
22	Safe	0.09	72	Safe	0.1
23	Safe	0.1	73	Safe	0.09
24	Safe	0.1	74	Safe	0.09
25	Safe	0.09	75	Safe	0.09
26	Safe	0.09	76	Safe	0.09
27	Safe	0.09	77	Safe	0.09
28	Safe	0.09	78	Safe	0.1
29	Safe	0.09	79	Safe	0.09
30	Safe	0.09	80	Safe	0.1
31	Safe	0.09	81	Safe	0.09
32	Safe	0.09	82	Safe	0.09
33	Safe	0.1	83	Safe	0.09
34	Safe	0.09	84	Safe	0.1
35	Safe	0.1	85	Safe	0.1
36	Safe	0.09	86	Safe	0.1
37	Safe	0.09	87	Safe	0.09
38	Safe	0.1	88	Safe	0.1
39	Safe	0.09	89	Safe	0.09
40	Safe	0.1	90	Safe	0.1
41	Safe	0.09	91	Safe	0.09
42	Safe	0.09	92	Undecided	300.0
43	Safe	0.09	93	Safe	0.31
44	Safe	0.09	94	Safe	0.11
45	Safe	0.09	95	Safe	0.31
46	Safe	0.09	96	Safe	0.12
47	Safe	0.1	97	Safe	0.09
48	Safe	0.1	98	Safe	0.1
49	Safe	0.1	99	Safe	0.09

Table 5: mnist 0.3

	Epsilon: 0.30	00		Epsilon: 0.300	)
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	12.23	50	Undecided	300.0
1	Undecided	300.0	51	Undecided	300.0
2	Undecided	300.0	52	Undecided	300.0
3	Undecided	300.0	53	Undecided	300.0
4	Undecided	300.0	54	Undecided	300.0
5	Safe	21.79	55	Safe	15.22
6	Undecided	300.0	56	Undecided	300.0
7	Undecided	300.0	57	Undecided	300.0
8	Unsafe	0.22	58	Undecided	300.0
9	Undecided	300.0	59	Undecided	300.0
10	Safe	23.35	60	Safe	0.22
11	Undecided	300.0	61	Undecided	300.0
12	Undecided	300.0	62	Unsafe	204.86
13	Undecided	300.0	63	Unsafe	0.23
14	Safe	0.2	64	Undecided	300.0
15	Undecided	300.0	65	Misclassified	0.0
16	Undecided	300.0	66	Undecided	300.0
17	Safe	5.95	67	Undecided	300.0
18	Unsafe	0.24	68	Undecided	300.0
19	Undecided	300.0	69	Undecided	300.0
20	Undecided	300.0	70	Safe	0.22
21	Undecided	300.0	71	Safe	7.25
22	Undecided	300.0	72	Undecided	300.0
23	Undecided	300.0	73	Unsafe	0.22
24	Undecided	300.0	74	Safe	0.6
25	Safe	8.41	75	Undecided	300.0
26	Undecided	300.0	76	Undecided	300.0
27	Undecided	300.0	77	Undecided	300.0
28	Undecided	300.0	78	Undecided	300.0
29	Undecided	300.0	79	Safe	0.83
30	Undecided	300.0	80	Undecided	300.0
31	Undecided	300.0	81	Undecided	300.0
32	Safe	4.25	82	Safe	0.82
33	Unsafe	0.23	83	Safe	120.14
34	Undecided	300.0	84	Undecided	300.0
35	Undecided	300.0	85	Safe	3.52
36	Undecided	300.0	86	Undecided	300.0
37	Safe	0.21	87	Undecided	300.0
38	Undecided	300.0	88	Undecided	300.0
39	Safe	0.21	89	Undecided	300.0
40	Safe	0.51	90	Undecided	300.0
41	Undecided	300.0	91	Undecided	300.0
42	Undecided	300.0	92	Unsafe	0.23
43	Unsafe	0.23	93	Undecided	300.0
44	Undecided	300.0	94	Safe	67.79
45	Undecided	300.0	95	Undecided	300.0
46	Safe	0.64	96	Undecided	300.0
47	Undecided	300.0	97	Undecided	300.0
48	Undecided	300.0	98	Undecided	300.0
49	Undecided	300.0	99	Undecided	300.0

Table 6: cifar10 2 255

	Epsilon: 0.008	3		Epsilon: 0.008	B
Image	Status	Time(s)	Image	Status	Time(s)
0	Unsafe	9.7	50	Undecided	300.0
1	Safe	7.96	51	Undecided	300.0
2	Undecided	300.0	52	Misclassified	0.0
3	Safe	18.21	53	Undecided	300.0
4	Undecided	300.0	54	Safe	10.8
5	Safe	71.23	55	Safe	10.65
6	Safe	19.63	56	Misclassified	0.0
7	Misclassified	0.0	57	Misclassified	0.0
8	Undecided	300.0	58	Misclassified	0.0
9	Undecided	300.0	59	Misclassified	0.0
10	Safe	15.32	60	Safe	13.06
11	Safe	9.65	61	Misclassified	0.0
12	Unsafe	13.84	62	Safe	11.31
13	Safe	12.19	63	Misclassified	0.0
14	Safe	13.4	64	Undecided	300.0
15	Safe	12.28	65	Unsafe	13.41
16	Undecided	300.0	66	Undecided	300.0
17	Safe	13.54	67	Safe	10.12
18	Safe	11.43	68	Undecided	300.0
19	Safe	14.13	69	Misclassified	0.0
20	Safe	25.12	70	Misclassified	0.0
21	Safe	6.88	71	Undecided	300.0
22	Misclassified	0.0	72	Safe	9.58
23	Safe	12.76	73	Safe	12.03
24	Misclassified	0.0	74	Unsafe	12.18
25	Undecided	300.0	75	Safe	11.16
26	Unsafe	15.14	76	Unsafe	12.46
27	Undecided	300.0	77	Undecided	300.0
28	Unsafe	12.58	78	Safe	27.22
29	Safe	14.16	79	Safe	9.53
30	Undecided	300.0	80	Safe	11.73
31	Unsafe	14.35	81	Safe	10.26
32	Unsafe	14.85	82	Safe	12.22
33	Undecided	300.0	83	Safe	10.25
34	Safe	12.41	84	Safe	10.59
35	Misclassified	0.0	85	Misclassified	0.0
36	Unsafe	15.12	86	Unsafe	11.85
37	Unsafe	11.47	87	Misclassified	0.0
38	Safe	12.91	88	Safe	11.72
39	Safe	41.37	89	Safe	12.22
40	Safe	12.64	90	Safe	11.15
41	Safe	12.04	91	Misclassified	0.0
42	Undecided	300.0	91	Safe	10.91
43	Safe	14.87	92	Safe	26.9
<del>4</del> 3   44	Safe	14.67	93	Safe	26.94
<del>44</del>   45	Safe	10.62	95	Saie Unsafe	13.2
45 46			1		
l	Safe Misclessified	27.41	96	Safe	13.98
47	Misclassified	0.0	97	Safe	18.3
48	Undecided	300.0	98	Safe	8.34
49	Misclassified	0.0	99	Safe	12.21

Table 7: cifar10 8 255

1   Safe   6.53   51   Undecided   300.0     2   Undecided   300.0   52   Misclassified   0.0     3   Misclassified   0.0   53   Misclassified   0.0     4   Unsafe   1.85   54   Safe   4.     5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0.0     7   Misclassified   0.0   57   Misclassified   0.0     8   Misclassified   0.0   58   Misclassified   0.0     9   Unsafe   1.77   59   Misclassified   0.0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.0     12   Misclassified   0.0   62   Misclassified   0.0     14   Undecided   300.0   65   Misclassified   0.0	(s)
1   Safe   6.53   51   Undecided   300.0     2   Undecided   300.0   52   Misclassified   0.0     3   Misclassified   0.0   53   Misclassified   0.0     4   Unsafe   1.85   54   Safe   4.     5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0.0     7   Misclassified   0.0   57   Misclassified   0.0     8   Misclassified   0.0   58   Misclassified   0.0     9   Unsafe   1.77   59   Misclassified   0.0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.0     12   Misclassified   0.0   62   Misclassified   0.0     14   Undecided   300.0   65   Misclassified   0.0	
2   Undecided   300.0   52   Misclassified   0     3   Misclassified   0.0   53   Misclassified   0     4   Unsafe   1.85   54   Safe   4.     5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0     7   Misclassified   0.0   57   Misclassified   0     8   Misclassified   0.0   58   Misclassified   0     9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300	96
3   Misclassified   0.0   53   Misclassified   0.0     4   Unsafe   1.85   54   Safe   4.     5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0.0     7   Misclassified   0.0   58   Misclassified   0.0     8   Misclassified   0.0   58   Misclassified   0.0     9   Unsafe   1.77   59   Misclassified   0.0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.0     12   Misclassified   0.0   62   Misclassified   0.0     13   Safe   5.19   63   Misclassified   0.0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0.0	0.0
4   Unsafe   1.85   54   Safe   4.     5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0.0     7   Misclassified   0.0   57   Misclassified   0.0     8   Misclassified   0.0   58   Misclassified   0.0     9   Unsafe   1.77   59   Misclassified   0.0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.0     12   Misclassified   0.0   62   Misclassified   0.0     13   Safe   5.19   63   Misclassified   0.0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0.0     16   Safe   1.8   66   Undecided   300	0.0
5   Undecided   300.0   55   Safe   105.     6   Misclassified   0.0   56   Misclassified   0.0     7   Misclassified   0.0   57   Misclassified   0.0     8   Misclassified   0.0   58   Misclassified   0.0     9   Unsafe   1.77   59   Misclassified   0.0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.0     12   Misclassified   0.0   62   Misclassified   0.0     13   Safe   5.19   63   Misclassified   0.0     14   Undecided   300.0   64   Undecided   300.0     15   Undecided   300.0   65   Misclassified   0.0     16   Safe   1.8   66   Undecided   300.0     18   Safe   1.74   68   Misclassified   0.0	0.0
6   Misclassified   0.0   56   Misclassified   0     7   Misclassified   0.0   57   Misclassified   0     8   Misclassified   0.0   58   Misclassified   0     9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1     18   Safe   1.74   68   Misclassified   0	01
7   Misclassified   0.0   57   Misclassified   0     8   Misclassified   0.0   58   Misclassified   0     9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1     18   Safe   1.74   68   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0	64
7   Misclassified   0.0   57   Misclassified   0     8   Misclassified   0.0   58   Misclassified   0     9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0	0.0
9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.8   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300 <td< td=""><td>0.0</td></td<>	0.0
9   Unsafe   1.77   59   Misclassified   0     10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300 <t< td=""><td>0.0</td></t<>	0.0
10   Undecided   300.0   60   Unsafe   1.     11   Undecided   300.0   61   Misclassified   0.     12   Misclassified   0.0   62   Misclassified   0.     13   Safe   5.19   63   Misclassified   0.     14   Undecided   300.0   64   Undecided   300.0     15   Undecided   300.0   65   Misclassified   0.     16   Safe   1.8   66   Undecided   300.0     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0.     19   Unsafe   1.88   69   Misclassified   0.     20   Misclassified   0.0   70   Misclassified   0.     21   Safe   1.53   71   Undecided   300.0     23   Unsafe   1.81   73   Undecided   300.0	0.0
11   Undecided   300.0   61   Misclassified   0     12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     <	81
12   Misclassified   0.0   62   Misclassified   0     13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1     25	0.0
13   Safe   5.19   63   Misclassified   0     14   Undecided   300.0   64   Undecided   300.0     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300.0     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300.0     22   Misclassified   0.0   72   Undecided   300.0     23   Unsafe   1.81   73   Undecided   300.0     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0.0	0.0
14   Undecided   300.0   64   Undecided   300.0     15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300.0     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300.0     22   Misclassified   0.0   72   Undecided   300.0     23   Unsafe   1.81   73   Undecided   300.0     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0.0     26   Misclassified   0.0   76   Undecided   300.0	0.0
15   Undecided   300.0   65   Misclassified   0     16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0	
16   Safe   1.8   66   Undecided   300     17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0	0.0
17   Misclassified   0.0   67   Unsafe   1.     18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0     29   Safe   3.8   79   Unsafe   1	
18   Safe   1.74   68   Misclassified   0     19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0     29   Safe   3.8   79   Unsafe   1     30   Unsafe   2.06   80   Undecided   300 <t< td=""><td>78</td></t<>	78
19   Unsafe   1.88   69   Misclassified   0     20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0     29   Safe   3.8   79   Unsafe   1     30   Unsafe   2.06   80   Undecided   300     31   Misclassified   0.0   81   Safe   1	0.0
20   Misclassified   0.0   70   Misclassified   0     21   Safe   1.53   71   Undecided   300     22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0     29   Safe   3.8   79   Unsafe   1     30   Unsafe   2.06   80   Undecided   300     31   Misclassified   0.0   81   Safe   1	0.0
21 Safe 1.53 71 Undecided 300   22 Misclassified 0.0 72 Undecided 300   23 Unsafe 1.81 73 Undecided 300   24 Misclassified 0.0 74 Unsafe 1.   25 Misclassified 0.0 75 Misclassified 0   26 Misclassified 0.0 76 Undecided 300   27 Misclassified 0.0 77 Misclassified 0   28 Undecided 300.0 78 Misclassified 0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	0.0
22   Misclassified   0.0   72   Undecided   300     23   Unsafe   1.81   73   Undecided   300     24   Misclassified   0.0   74   Unsafe   1.     25   Misclassified   0.0   75   Misclassified   0     26   Misclassified   0.0   76   Undecided   300     27   Misclassified   0.0   77   Misclassified   0     28   Undecided   300.0   78   Misclassified   0     29   Safe   3.8   79   Unsafe   1.     30   Unsafe   2.06   80   Undecided   300     31   Misclassified   0.0   81   Safe   1.	
23 Unsafe 1.81 73 Undecided 300   24 Misclassified 0.0 74 Unsafe 1.   25 Misclassified 0.0 75 Misclassified 0   26 Misclassified 0.0 76 Undecided 300   27 Misclassified 0.0 77 Misclassified 0   28 Undecided 300.0 78 Misclassified 0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	
24 Misclassified 0.0 74 Unsafe 1.   25 Misclassified 0.0 75 Misclassified 0.0   26 Misclassified 0.0 76 Undecided 300   27 Misclassified 0.0 77 Misclassified 0.0   28 Undecided 300.0 78 Misclassified 0.0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	
25 Misclassified 0.0 75 Misclassified 0   26 Misclassified 0.0 76 Undecided 30   27 Misclassified 0.0 77 Misclassified 0   28 Undecided 300.0 78 Misclassified 0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 30   31 Misclassified 0.0 81 Safe 1.	92
26 Misclassified 0.0 76 Undecided 300   27 Misclassified 0.0 77 Misclassified 0   28 Undecided 300.0 78 Misclassified 0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	0.0
27 Misclassified 0.0 77 Misclassified 0.0   28 Undecided 300.0 78 Misclassified 0.0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	
28 Undecided 300.0 78 Misclassified 0   29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	0.0
29 Safe 3.8 79 Unsafe 1.   30 Unsafe 2.06 80 Undecided 300   31 Misclassified 0.0 81 Safe 1.	0.0
30	64
31 Misclassified 0.0 81 Safe 1.	
	86
, or onsure 1./0   02 bate 1.	81
	66
34 Safe 4.3 84 Undecided 300	
	0.0
	86
	0.0
38 Unsafe 1.82 88 Undecided 300	
	.8
	75
	0.0
	.7
	0.0
	0.0
	75
46 Misclassified 0.0 96 Unsafe 14.	
47 Misclassified 0.0 97 Undecided 300	
	64
49 Safe 18.1 99 Unsafe 1.	- 1

Table 8: mnist logsig 200 50

Epsilon: 3.000			Epsilon: 5.00	0	Epsilon: 12.000			
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.13	0	Undecided	900.0	0	Undecided	900.0
1	Safe	4.03	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.03
3	Safe	0.02	3	Safe	464.32	3	Undecided	900.0
4	Safe	22.06	4	Undecided	900.0	4	Unsafe	0.03
5	Safe	0.02	5	Undecided	900.0	5	Undecided	900.0
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.02
7	Undecided	900.0	7	Undecided	900.0	7	Undecided	900.0
8	Unsafe	0.02	8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	2.99	9	Undecided	900.0	9	Unsafe	0.01
10	Safe	0.02	10	Undecided	900.0	10	Undecided	900.0
11	Undecided	900.0	11	Undecided	900.0	11	Unsafe	0.04
12	Safe	10.91	12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.02	13	Undecided	900.0	13	Undecided	900.0
14	Safe	0.01	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.02
16	Undecided	900.0	16	Undecided	900.0	16	Unsafe	3.3
17	Safe	0.02	17	Undecided	900.0	17	Undecided	900.0
18	Unsafe	0.01	18	Unsafe	0.02	18	Unsafe	0.02
19	Safe	0.5	19	Undecided	900.0	19	Undecided	900.0
20	Safe	1.86	20	Undecided	900.0	20	Unsafe	0.02
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	1.47
22	Safe	394.82	22	Undecided	900.0	22	Undecided	900.0
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02

Table 9: mnist logsig 200 100 50

Epsilon: 3.000			Epsilon: 5.00	0	Epsilon: 12.000			
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Undecided	900.0	0	Undecided	900.0	0	Undecided	900.0
1	Undecided	900.0	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.03
3	Undecided	900.0	3	Undecided	900.0	3	Undecided	900.0
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.02
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.02
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.01
7	Undecided	900.0	7	Undecided	900.0	7	Unsafe	0.02
8	Unsafe	3.29	8	Unsafe	0.03	8	Unsafe	0.01
9	Undecided	900.0	9	Undecided	900.0	9	Unsafe	484.32
10	Undecided	900.0	10	Undecided	900.0	10	Unsafe	16.27
11	Undecided	900.0	11	Undecided	900.0	11	Unsafe	0.03
12	Undecided	900.0	12	Undecided	900.0	12	Unsafe	0.01
13	Undecided	900.0	13	Undecided	900.0	13	Undecided	900.0
14	Undecided	900.0	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.03
16	Undecided	900.0	16	Undecided	900.0	16	Unsafe	40.09
17	Undecided	900.0	17	Undecided	900.0	17	Undecided	900.0
18	Unsafe	0.02	18	Unsafe	0.02	18	Unsafe	0.02
19	Undecided	900.0	19	Undecided	900.0	19	Unsafe	0.02
20	Undecided	900.0	20	Unsafe	0.04	20	Unsafe	0.01
21	Undecided	900.0	21	Undecided	900.0	21	Undecided	900.0
22	Undecided	900.0	22	Undecided	900.0	22	Undecided	900.0
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02

Table 10: mnist tansig 200 50

Epsilon: 3.000				Epsilon: 5.00	0	Epsilon: 12.000		
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.09	0	Undecided	900.0	0	Undecided	900.0
1	Safe	0.01	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.02
3	Safe	0.11	3	Undecided	900.0	3	Undecided	900.0
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.03
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.04
6	Safe	224.27	6	Undecided	900.0	6	Unsafe	0.02
7	Safe	0.02	7	Undecided	900.0	7	Undecided	900.0
8	Unsafe	0.01	8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	683.25	9	Undecided	900.0	9	Unsafe	0.05
10	Safe	14.84	10	Undecided	900.0	10	Unsafe	0.01
11	Safe	0.09	11	Undecided	900.0	11	Unsafe	0.03
12	Safe	0.02	12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.01	13	Undecided	900.0	13	Undecided	900.0
14	Safe	0.09	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Unsafe	0.02	15	Unsafe	0.02
16	Safe	129.39	16	Undecided	900.0	16	Undecided	900.0
17	Safe	0.02	17	Undecided	900.0	17	Undecided	900.0
18	Undecided	900.0	18	Unsafe	0.02	18	Unsafe	0.02
19	Safe	0.02	19	Undecided	900.0	19	Undecided	900.0
20	Undecided	900.0	20	Undecided	900.0	20	Unsafe	0.05
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	0.01
22	Safe	0.03	22	Undecided	900.0	22	Undecided	900.0
23	Safe	0.01	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.03

Table 11: mnist tansig 200 100 50

Epsilon: 3.000				Epsilon: 5.000			Epsilon: 12.000		
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)	
0	Undecided	900.0	0	Undecided	900.0	0	Undecided	900.0	
1	Undecided	900.0	1	Undecided	900.0	1	Undecided	900.0	
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.02	
3	Undecided	900.0	3	Undecided	900.0	3	Undecided	900.0	
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.04	
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.02	
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.02	
7	Undecided	900.0	7	Undecided	900.0	7	Unsafe	0.02	
8	Unsafe	0.02	8	Unsafe	0.02	8	Unsafe	0.01	
9	Undecided	900.0	9	Undecided	900.0	9	Unsafe	0.04	
10	Undecided	900.0	10	Undecided	900.0	10	Undecided	900.0	
11	Undecided	900.0	11	Undecided	900.0	11	Undecided	900.0	
12	Undecided	900.0	12	Undecided	900.0	12	Undecided	900.0	
13	Safe	2.55	13	Undecided	900.0	13	Undecided	900.0	
14	Undecided	900.0	14	Undecided	900.0	14	Undecided	900.0	
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.02	
16	Undecided	900.0	16	Undecided	900.0	16	Undecided	900.0	
17	Undecided	900.0	17	Undecided	900.0	17	Undecided	900.0	
18	Undecided	900.0	18	Undecided	900.0	18	Unsafe	0.02	
19	Undecided	900.0	19	Undecided	900.0	19	Undecided	900.0	
20	Undecided	900.0	20	Undecided	900.0	20	Undecided	900.0	
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	0.03	
22	Undecided	900.0	22	Undecided	900.0	22	Undecided	900.0	
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0	
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02	

REFERENCES REFERENCES

## References

[1] P. Henriksen and A. Lomuscio. Efficient neural network verification via adaptive refinement and adversarial search. In *Proceedings of the 24th European Conference on Artificial Intelligence (ECAI20)*, 2020.