Benchmark Results for VeriNet

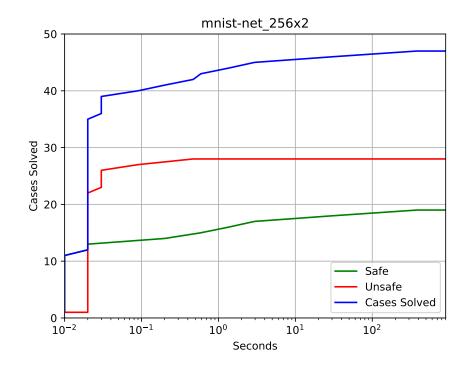
July 18, 2020

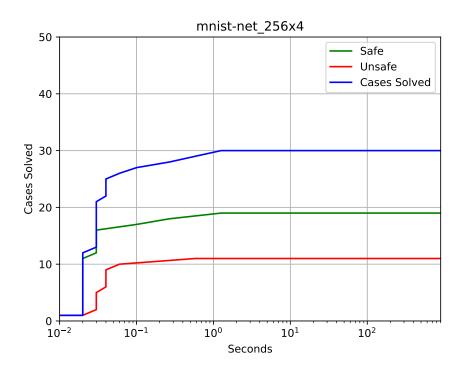
1 About

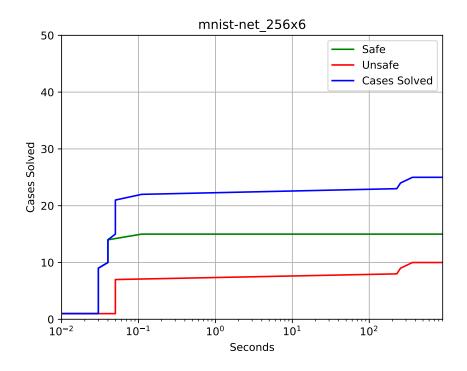
VeriNet [1] is a symbolic-interval propagation-based toolkit for local robustness properties supporting ReLU, Sigmoid and Tanh activation functions and Fully-Connected, Convolutional and Batch-normalisation layers. VeriNet uses several novels techniques to achieve a high level of performance, include a local gradient-based search around spurious counterexamples, an adaptive refinement strategy and optimal relaxations for the Sigmoid and Tanh activation functions.

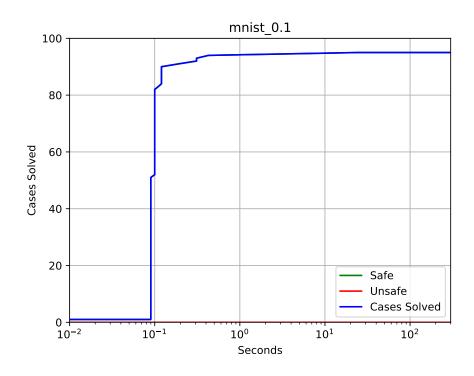
We ran our toolkit on benchmarks in all three categories; however, we did not evaluate the ACAS Xu Benchmarks as VeriNet does not support all of the properties at this point. We Also did not evaluate VeriNet on all of the Cifar10 convolutional networks due to time constraints. We ran all benchmarks on a workstation with a Ryzen 3700X 3.6 GHz 8-core CPU, 64 GB ram running Ubuntu 20.04 LTS with Linux kernel 5.4.0. The VeriNet code is available at https://vas.doc.ic.ac.uk/software/neural/

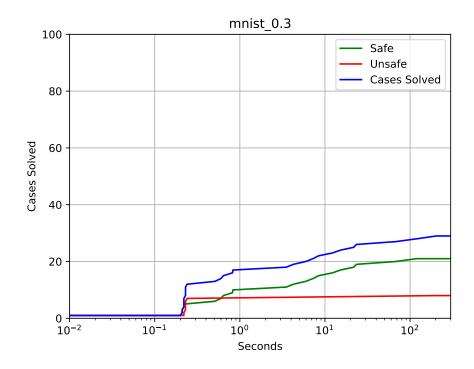
2 Results

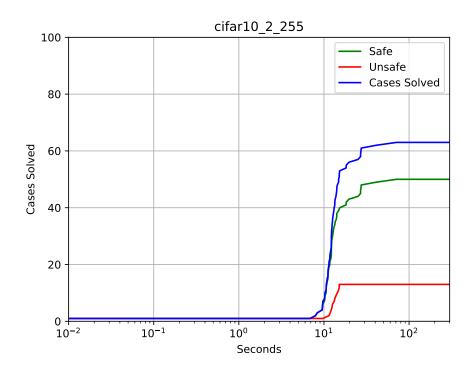


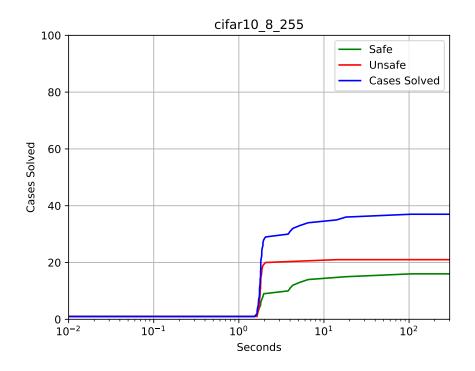


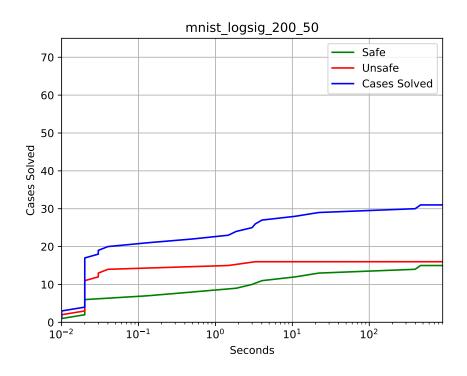


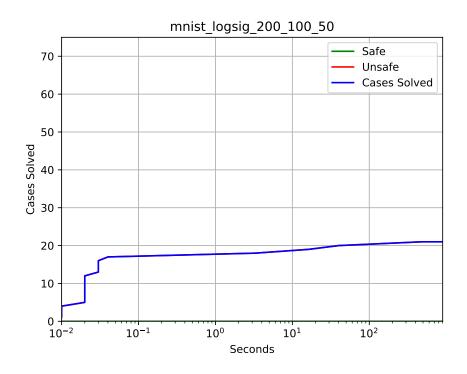


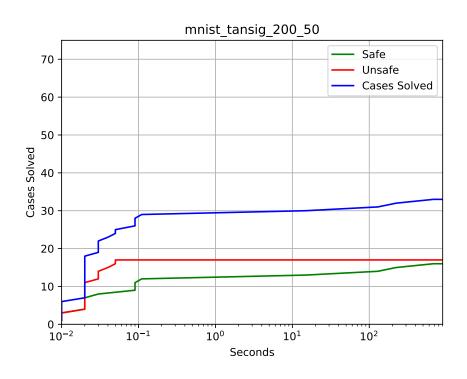












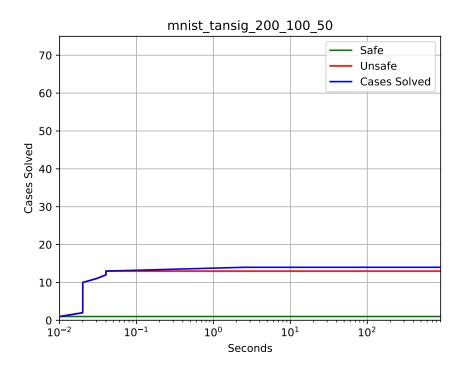


Table 1: mnist-net 256x2

E ₁	psilon: 0.0	020		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Image Status Ti	
0	Unsafe	0.09	0	Unsafe	0.02
1	Safe	0.01	1	Unsafe	0.02
2	Unsafe	0.02	2	Unsafe	0.02
3	Safe	0.01	3	Unsafe	0.02
4	Unsafe	0.02	4	Unsafe	0.02
5	Safe	0.2	5	Unsafe	0.02
6	Safe	378.33	6	Unsafe	0.02
7	Safe	2.94	7	Unsafe	0.02
8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	0.01	9	Unsafe	0.02
10 Safe		0.01	10	Undecided	900.0
11	Safe	0.01	11	Unsafe	0.03
12	Safe	0.01	12 Unsafe		0.02
13	Safe	0.01	13	13 Unsafe	
14	Safe	0.01	14	Unsafe	0.47
15	Safe	0.01	15	Undecided	900.0
16	Safe	0.01	16	Unsafe	0.03
17	Safe	30.92	17	Unsafe	0.02
18	Unsafe	0.03	18	Unsafe	0.02
19	Safe	0.59	19	Unsafe	0.02
20	Safe	0.02	20	Unsafe	0.02
21	Safe	1.36	21	Unsafe	0.02
22	Safe	0.02	22	Undecided	900.0
23	Safe	0.01	23	Unsafe	0.03
24	Unsafe	0.02	24	Unsafe	0.02

Table 2: mnist-net 256x4

	Epsilon: 0.02	:0		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe 0.1		0	Undecided	900.0
1	Safe	0.02	1	Undecided	900.0
2	Undecided	900.0	2	Unsafe	0.58
3	Safe	0.03	3	Undecided	900.0
4	Safe	0.02	4	Undecided	900.0
5	Safe	0.27	5	Undecided	900.0
6	Safe	0.03	6	Unsafe	0.04
7	Undecided	900.0	7	Unsafe	0.03
8	Safe	1.26	8	Unsafe	0.03
9	Safe	0.03	9	Undecided	900.0
10	Safe 0.0		10	Undecided	900.0
11	Safe	0.02	11	Undecided	900.0
12	Safe	0.02	12	Undecided	900.0
13	Safe	0.02	13	Undecided	900.0
14	Safe	0.02	14	Unsafe	0.04
15	Safe	0.02	15	Undecided	900.0
16	Undecided	900.0	16	Unsafe	0.06
17	Safe	0.03	17	Undecided	900.0
18	Unsafe	0.02	18	Unsafe	0.04
19	Safe	0.02	19	Unsafe	0.03
20	Undecided	900.0	20	Unsafe	0.03
21	Safe	0.03	21	Undecided	900.0
22	Safe	0.02	22	Undecided	900.0
23	Safe	0.02	23	Undecided	900.0
24	Undecided	900.0	24	Unsafe	0.04

Table 3: mnist-net 256x6

	Epsilon: 0.02	:0		Epsilon: 0.05	0
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.11	0	Unsafe	363.99
1	Safe	0.03	1	Undecided	900.0
2	Undecided	900.0	2	Unsafe	0.05
3	Safe	0.04	3	Undecided	900.0
4	Safe	0.03	4	Undecided	900.0
5	Undecided	900.0	5	Undecided	900.0
6	Undecided	900.0	6	Unsafe	0.05
7	Undecided	900.0	7	Unsafe	254.71
8	Unsafe	0.05	8	Unsafe	0.05
9	Safe	0.03	9	Undecided	900.0
10	Safe 0.03		10	Undecided	900.0
11	Safe 0.03		11	Unsafe	0.05
12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.04	13	Undecided	900.0
14	Safe	0.03	14	Undecided	900.0
15	Safe	0.03	15	Undecided	900.0
16	Undecided	900.0	16	Unsafe	227.87
17	Safe	0.04	17	Undecided	900.0
18	Undecided	900.0	18	Unsafe	0.05
19	Safe	0.04	19	Undecided	900.0
20	Undecided	900.0	20	Undecided	900.0
21	Safe	0.04	21	Undecided	900.0
22	Safe	0.03	22	Undecided	900.0
23	Safe	0.03	23	Undecided	900.0
24	Undecided	900.0	24	Unsafe	0.05

Table 4: mnist 0.1

	Epsilon: 0.10	00		Epsilon: 0.10	00
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.19	50	Safe	0.1
1	Safe	0.1	51	Safe	0.09
2	Safe	0.1	52	Safe	0.1
3	Safe	0.1	53	Safe	0.09
4	Safe	0.1	54	Safe	0.1
5	Safe	0.09	55	Safe	0.1
6	Undecided	300.0	56	Safe	0.09
7	Safe	0.12	57	Safe	0.1
8	Undecided	300.0	58	Safe	0.1
9	Safe	0.12	59	Safe	0.43
10	Safe	0.09	60	Safe	0.12
11	Safe	0.09	61	Safe	0.09
12	Safe	0.09	62	Undecided	300.0
13	Safe	0.09	63	Safe	0.12
14	Safe	0.09	64	Safe	0.1
15	Safe	0.09	65	Safe	24.58
16	Safe	0.09	66	Safe	0.12
17	Safe	0.09	67	Safe	0.09
18	Undecided	300.0	68	Safe	0.1
19	Safe	0.12	69	Safe	0.09
20	Safe	0.09	70	Safe	0.1
21	Safe	0.09	71	Safe	0.09
22	Safe	0.09	72	Safe	0.1
23	Safe	0.1	73	Safe	0.09
24	Safe	0.1	74	Safe	0.09
25	Safe	0.09	75	Safe	0.09
26	Safe	0.09	76	Safe	0.09
27	Safe	0.09	77	Safe	0.09
28	Safe	0.09	78	Safe	0.1
29	Safe	0.09	79	Safe	0.09
30	Safe	0.09	80	Safe	0.1
31	Safe	0.09	81	Safe	0.09
32	Safe	0.09	82	Safe	0.09
33	Safe	0.1	83	Safe	0.09
34	Safe	0.09	84	Safe	0.1
35	Safe	0.1	85	Safe	0.1
36	Safe	0.09	86	Safe	0.1
37	Safe	0.09	87	Safe	0.09
38	Safe	0.1	88	Safe	0.1
39	Safe	0.09	89	Safe	0.09
40	Safe	0.1	90	Safe	0.1
41	Safe	0.09	91	Safe	0.09
42	Safe	0.09	92	Undecided	300.0
43	Safe	0.09	93	Safe	0.31
44	Safe	0.09	94	Safe	0.11
45	Safe	0.09	95	Safe	0.31
46	Safe	0.09	96	Safe	0.12
47	Safe	0.1	97	Safe	0.09
48	Safe	0.1	98	Safe	0.1
49	Safe	0.1	99	Safe	0.09

Table 5: mnist 0.3

	Epsilon: 0.30	00		Epsilon: 0.300)
Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	12.23	50	Undecided	300.0
1	Undecided	300.0	51	Undecided	300.0
2	Undecided	300.0	52	Undecided	300.0
3	Undecided	300.0	53	Undecided	300.0
4	Undecided	300.0	54	Undecided	300.0
5	Safe	21.79	55	Safe	15.22
6	Undecided	300.0	56	Undecided	300.0
7	Undecided	300.0	57	Undecided	300.0
8	Unsafe	0.22	58	Undecided	300.0
9	Undecided	300.0	59	Undecided	300.0
10	Safe	23.35	60	Safe	0.22
11	Undecided	300.0	61	Undecided	300.0
12	Undecided	300.0	62	Unsafe	204.86
13	Undecided	300.0	63	Unsafe	0.23
14	Safe	0.2	64	Undecided	300.0
15	Undecided	300.0	65	Misclassified	0.0
16	Undecided	300.0	66	Undecided	300.0
17	Safe	5.95	67	Undecided	300.0
18	Unsafe	0.24	68	Undecided	300.0
19	Undecided	300.0	69	Undecided	300.0
20	Undecided	300.0	70	Safe	0.22
21	Undecided	300.0	71	Safe	7.25
22	Undecided	300.0	72	Undecided	300.0
23	Undecided	300.0	73	Unsafe	0.22
24	Undecided	300.0	74	Safe	0.6
25	Safe	8.41	75	Undecided	300.0
26	Undecided	300.0	76	Undecided	300.0
27	Undecided	300.0	77	Undecided	300.0
28	Undecided	300.0	78	Undecided	300.0
29	Undecided	300.0	79	Safe	0.83
30	Undecided	300.0	80	Undecided	300.0
31	Undecided	300.0	81	Undecided	300.0
32	Safe	4.25	82	Safe	0.82
33	Unsafe	0.23	83	Safe	120.14
34	Undecided	300.0	84	Undecided	300.0
35	Undecided	300.0	85	Safe	3.52
36	Undecided	300.0	86	Undecided	300.0
37	Safe	0.21	87	Undecided	300.0
38	Undecided	300.0	88	Undecided	300.0
39	Safe	0.21	89	Undecided	300.0
40	Safe	0.51	90	Undecided	300.0
41	Undecided	300.0	91	Undecided	300.0
42	Undecided	300.0	92	Unsafe	0.23
43	Unsafe	0.23	93	Undecided	300.0
44	Undecided	300.0	94	Safe	67.79
45	Undecided	300.0	95	Undecided	300.0
46	Safe	0.64	96	Undecided	300.0
47	Undecided	300.0	97	Undecided	300.0
48	Undecided	300.0	98	Undecided	300.0
49	Undecided	300.0	99	Undecided	300.0

Table 6: cifar10 2 255

	Epsilon: 0.008	3		Epsilon: 0.008	B
Image	Status	Time(s)	Image	Status	Time(s)
0	Unsafe	9.7	50	Undecided	300.0
1	Safe	7.96	51	Undecided	300.0
2	Undecided	300.0	52	Misclassified	0.0
3	Safe	18.21	53	Undecided	300.0
4	Undecided	300.0	54	Safe	10.8
5	Safe	71.23	55	Safe	10.65
6	Safe	19.63	56	Misclassified	0.0
7	Misclassified	0.0	57	Misclassified	0.0
8	Undecided	300.0	58	Misclassified	0.0
9	Undecided	300.0	59	Misclassified	0.0
10	Safe	15.32	60	Safe	13.06
11	Safe	9.65	61	Misclassified	0.0
12	Unsafe	13.84	62	Safe	11.31
13	Safe	12.19	63	Misclassified	0.0
14	Safe	13.4	64	Undecided	300.0
15	Safe	12.28	65	Unsafe	13.41
16	Undecided	300.0	66	Undecided	300.0
17	Safe	13.54	67	Safe	10.12
18	Safe	11.43	68	Undecided	300.0
19	Safe	14.13	69	Misclassified	0.0
20	Safe	25.12	70	Misclassified	0.0
21	Safe	6.88	71	Undecided	300.0
22	Misclassified	0.0	72	Safe	9.58
23	Safe	12.76	73	Safe	12.03
24	Misclassified	0.0	74	Unsafe	12.18
25	Undecided	300.0	75	Safe	11.16
26	Unsafe	15.14	76	Unsafe	12.46
27	Undecided	300.0	77	Undecided	300.0
28	Unsafe	12.58	78	Safe	27.22
29	Safe	14.16	79	Safe	9.53
30	Undecided	300.0	80	Safe	11.73
31	Unsafe	14.35	81	Safe	10.26
32	Unsafe	14.85	82	Safe	12.22
33	Undecided	300.0	83	Safe	10.25
34	Safe	12.41	84	Safe	10.59
35	Misclassified	0.0	85	Misclassified	0.0
36	Unsafe	15.12	86	Unsafe	11.85
37	Unsafe	11.47	87	Misclassified	0.0
38	Safe	12.91	88	Safe	11.72
39	Safe	41.37	89	Safe	12.22
40	Safe	12.64	90	Safe	11.15
41	Safe	12.04	91	Misclassified	0.0
42	Undecided	300.0	91	Safe	10.91
43	Safe	14.87	92	Safe	26.9
4 3 44	Safe	14.67	93	Safe	26.94
44 45	Safe	10.62	95	Saie Unsafe	13.2
45 46			1		
l	Safe Misclessified	27.41	96	Safe	13.98
47	Misclassified	0.0	97	Safe	18.3
48	Undecided	300.0	98	Safe	8.34
49	Misclassified	0.0	99	Safe	12.21

Table 7: cifar10 8 255

1 Safe 6.53 51 Undecided 300.0 2 Undecided 300.0 52 Misclassified 0.0 3 Misclassified 0.0 53 Misclassified 0.0 4 Unsafe 1.85 54 Safe 4. 5 Undecided 300.0 55 Safe 105. 6 Misclassified 0.0 56 Misclassified 0.0 7 Misclassified 0.0 57 Misclassified 0.0 8 Misclassified 0.0 58 Misclassified 0.0 9 Unsafe 1.77 59 Misclassified 0.0 10 Undecided 300.0 60 Unsafe 1. 11 Undecided 300.0 61 Misclassified 0.0 12 Misclassified 0.0 62 Misclassified 0.0 14 Undecided 300.0 65 Misclassified 0.0	(s)
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19 Unsafe 1.88 69 Misclassified 0 20 Misclassified 0.0 70 Misclassified 0 21 Safe 1.53 71 Undecided 300 22 Misclassified 0.0 72 Undecided 300 23 Unsafe 1.81 73 Undecided 300 24 Misclassified 0.0 74 Unsafe 1. 25 Misclassified 0.0 75 Misclassified 0 26 Misclassified 0.0 76 Undecided 300 27 Misclassified 0.0 77 Misclassified 0 28 Undecided 300.0 78 Misclassified 0 29 Safe 3.8 79 Unsafe 1 30 Unsafe 2.06 80 Undecided 300 31 Misclassified 0.0 81 Safe 1	0.0
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26 Misclassified 0.0 76 Undecided 300 27 Misclassified 0.0 77 Misclassified 0 28 Undecided 300.0 78 Misclassified 0 29 Safe 3.8 79 Unsafe 1. 30 Unsafe 2.06 80 Undecided 300 31 Misclassified 0.0 81 Safe 1.	0.0
27 Misclassified 0.0 77 Misclassified 0.0 28 Undecided 300.0 78 Misclassified 0.0 29 Safe 3.8 79 Unsafe 1. 30 Unsafe 2.06 80 Undecided 300 31 Misclassified 0.0 81 Safe 1.	
28 Undecided 300.0 78 Misclassified 0 29 Safe 3.8 79 Unsafe 1. 30 Unsafe 2.06 80 Undecided 300 31 Misclassified 0.0 81 Safe 1.	0.0
29 Safe 3.8 79 Unsafe 1. 30 Unsafe 2.06 80 Undecided 300 31 Misclassified 0.0 81 Safe 1.	0.0
30	64
31 Misclassified 0.0 81 Safe 1.	
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	66
34 Safe 4.3 84 Undecided 300	
	0.0
	86
	0.0
38 Unsafe 1.82 88 Undecided 300	
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	75
	0.0
	.7
	0.0
	0.0
	75
46 Misclassified 0.0 96 Unsafe 14.	
47 Misclassified 0.0 97 Undecided 300	
	64
49 Safe 18.1 99 Unsafe 1.	- 1

Table 8: mnist logsig 200 50

Epsilon: 3.000			Epsilon: 5.00	0	Epsilon: 12.000			
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.13	0	Undecided	900.0	0	Undecided	900.0
1	Safe	4.03	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.03
3	Safe	0.02	3	Safe	464.32	3	Undecided	900.0
4	Safe	22.06	4	Undecided	900.0	4	Unsafe	0.03
5	Safe	0.02	5	Undecided	900.0	5	Undecided	900.0
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.02
7	Undecided	900.0	7	Undecided	900.0	7	Undecided	900.0
8	Unsafe	0.02	8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	2.99	9	Undecided	900.0	9	Unsafe	0.01
10	Safe	0.02	10	Undecided	900.0	10	Undecided	900.0
11	Undecided	900.0	11	Undecided	900.0	11	Unsafe	0.04
12	Safe	10.91	12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.02	13	Undecided	900.0	13	Undecided	900.0
14	Safe	0.01	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.02
16	Undecided	900.0	16	Undecided	900.0	16	Unsafe	3.3
17	Safe	0.02	17	Undecided	900.0	17	Undecided	900.0
18	Unsafe	0.01	18	Unsafe	0.02	18	Unsafe	0.02
19	Safe	0.5	19	Undecided	900.0	19	Undecided	900.0
20	Safe	1.86	20	Undecided	900.0	20	Unsafe	0.02
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	1.47
22	Safe	394.82	22	Undecided	900.0	22	Undecided	900.0
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02

Table 9: mnist logsig 200 100 50

Epsilon: 3.000			Epsilon: 5.00	0	Epsilon: 12.000			
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Undecided	900.0	0	Undecided	900.0	0	Undecided	900.0
1	Undecided	900.0	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.03
3	Undecided	900.0	3	Undecided	900.0	3	Undecided	900.0
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.02
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.02
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.01
7	Undecided	900.0	7	Undecided	900.0	7	Unsafe	0.02
8	Unsafe	3.29	8	Unsafe	0.03	8	Unsafe	0.01
9	Undecided	900.0	9	Undecided	900.0	9	Unsafe	484.32
10	Undecided	900.0	10	Undecided	900.0	10	Unsafe	16.27
11	Undecided	900.0	11	Undecided	900.0	11	Unsafe	0.03
12	Undecided	900.0	12	Undecided	900.0	12	Unsafe	0.01
13	Undecided	900.0	13	Undecided	900.0	13	Undecided	900.0
14	Undecided	900.0	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.03
16	Undecided	900.0	16	Undecided	900.0	16	Unsafe	40.09
17	Undecided	900.0	17	Undecided	900.0	17	Undecided	900.0
18	Unsafe	0.02	18	Unsafe	0.02	18	Unsafe	0.02
19	Undecided	900.0	19	Undecided	900.0	19	Unsafe	0.02
20	Undecided	900.0	20	Unsafe	0.04	20	Unsafe	0.01
21	Undecided	900.0	21	Undecided	900.0	21	Undecided	900.0
22	Undecided	900.0	22	Undecided	900.0	22	Undecided	900.0
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02

Table 10: mnist tansig 200 50

Epsilon: 3.000				Epsilon: 5.00	0	Epsilon: 12.000		
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)
0	Safe	0.09	0	Undecided	900.0	0	Undecided	900.0
1	Safe	0.01	1	Undecided	900.0	1	Undecided	900.0
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.02
3	Safe	0.11	3	Undecided	900.0	3	Undecided	900.0
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.03
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.04
6	Safe	224.27	6	Undecided	900.0	6	Unsafe	0.02
7	Safe	0.02	7	Undecided	900.0	7	Undecided	900.0
8	Unsafe	0.01	8	Unsafe	0.02	8	Unsafe	0.02
9	Safe	683.25	9	Undecided	900.0	9	Unsafe	0.05
10	Safe	14.84	10	Undecided	900.0	10	Unsafe	0.01
11	Safe	0.09	11	Undecided	900.0	11	Unsafe	0.03
12	Safe	0.02	12	Undecided	900.0	12	Undecided	900.0
13	Safe	0.01	13	Undecided	900.0	13	Undecided	900.0
14	Safe	0.09	14	Undecided	900.0	14	Undecided	900.0
15	Undecided	900.0	15	Unsafe	0.02	15	Unsafe	0.02
16	Safe	129.39	16	Undecided	900.0	16	Undecided	900.0
17	Safe	0.02	17	Undecided	900.0	17	Undecided	900.0
18	Undecided	900.0	18	Unsafe	0.02	18	Unsafe	0.02
19	Safe	0.02	19	Undecided	900.0	19	Undecided	900.0
20	Undecided	900.0	20	Undecided	900.0	20	Unsafe	0.05
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	0.01
22	Safe	0.03	22	Undecided	900.0	22	Undecided	900.0
23	Safe	0.01	23	Undecided	900.0	23	Undecided	900.0
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.03

Table 11: mnist tansig 200 100 50

Epsilon: 3.000				Epsilon: 5.000			Epsilon: 12.000		
Image	Status	Time(s)	Image	Status	Time(s)	Image	Status	Time(s)	
0	Undecided	900.0	0	Undecided	900.0	0	Undecided	900.0	
1	Undecided	900.0	1	Undecided	900.0	1	Undecided	900.0	
2	Undecided	900.0	2	Undecided	900.0	2	Unsafe	0.02	
3	Undecided	900.0	3	Undecided	900.0	3	Undecided	900.0	
4	Undecided	900.0	4	Undecided	900.0	4	Unsafe	0.04	
5	Undecided	900.0	5	Undecided	900.0	5	Unsafe	0.02	
6	Undecided	900.0	6	Undecided	900.0	6	Unsafe	0.02	
7	Undecided	900.0	7	Undecided	900.0	7	Unsafe	0.02	
8	Unsafe	0.02	8	Unsafe	0.02	8	Unsafe	0.01	
9	Undecided	900.0	9	Undecided	900.0	9	Unsafe	0.04	
10	Undecided	900.0	10	Undecided	900.0	10	Undecided	900.0	
11	Undecided	900.0	11	Undecided	900.0	11	Undecided	900.0	
12	Undecided	900.0	12	Undecided	900.0	12	Undecided	900.0	
13	Safe	2.55	13	Undecided	900.0	13	Undecided	900.0	
14	Undecided	900.0	14	Undecided	900.0	14	Undecided	900.0	
15	Undecided	900.0	15	Undecided	900.0	15	Unsafe	0.02	
16	Undecided	900.0	16	Undecided	900.0	16	Undecided	900.0	
17	Undecided	900.0	17	Undecided	900.0	17	Undecided	900.0	
18	Undecided	900.0	18	Undecided	900.0	18	Unsafe	0.02	
19	Undecided	900.0	19	Undecided	900.0	19	Undecided	900.0	
20	Undecided	900.0	20	Undecided	900.0	20	Undecided	900.0	
21	Undecided	900.0	21	Undecided	900.0	21	Unsafe	0.03	
22	Undecided	900.0	22	Undecided	900.0	22	Undecided	900.0	
23	Undecided	900.0	23	Undecided	900.0	23	Undecided	900.0	
24	Undecided	900.0	24	Undecided	900.0	24	Unsafe	0.02	

REFERENCES REFERENCES

References

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