# Cancer Classification

```
library(caret)
## Loading required package: lattice
## Loading required package: ggplot2
library(corrplot)
## corrplot 0.84 loaded
library(ggplot2)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
library(keep)
library(glmnet)
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16
library(NeuralNetTools)
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
       combine
##
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(tidyr)
## Warning: package 'tidyr' was built under R version 3.5.2
## Attaching package: 'tidyr'
## The following object is masked from 'package:Matrix':
##
```

```
## expand
```

```
set.seed(1101)
```

## read data

The breast cancer data consists of 30 features, they are computed from a digitized image of a fine needle aspirate (FNA) of a breast mass. They describe characteristics of the cell nuclei present in the image. n the 3-dimensional space is that described in: [K. P. Bennett and O. L. Mangasarian: "Robust Linear Programming Discrimination of Two Linearly Inseparable Sets", Optimization Methods and Software 1, 1992, 23-34].

This database is also available through the UW CS ftp server: ftp ftp.cs.wisc.edu cd math-prog/cpo-dataset/machine-learn/WDBC/

Also can be found on UCI Machine Learning Repository: https://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+%28Diagnostic%29

The target variable is diagnosis, tumor being malignant or benign. These 30 features are measures of the tumor such as radius, size, perimeter etc

```
bcancer <- read.csv("data.csv")
table(bcancer$diagnosis)
##
## B M</pre>
```

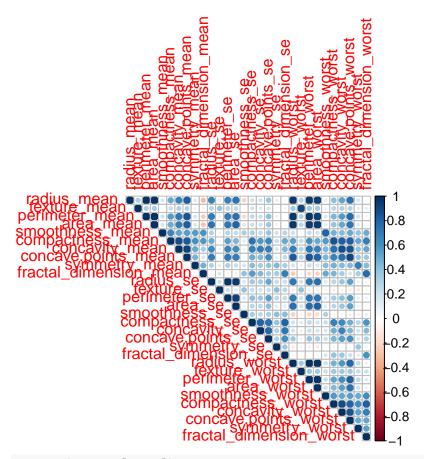
The objective of the analysis is to predict the the diagnosis of each patient id using these 30 features. I will use a classification model to identify the diagnosis.

### DATA EXPLORATION

## 357 212

There are no missing values in the data and the distribution of the target variable is 63% of benign cancer and 37% of malignant cancer cells.

```
corMatrix <- cor(bcancer[,3:32])
corrplot(corMatrix , tl.cex = 1, addrect = 8 , type = "upper")</pre>
```

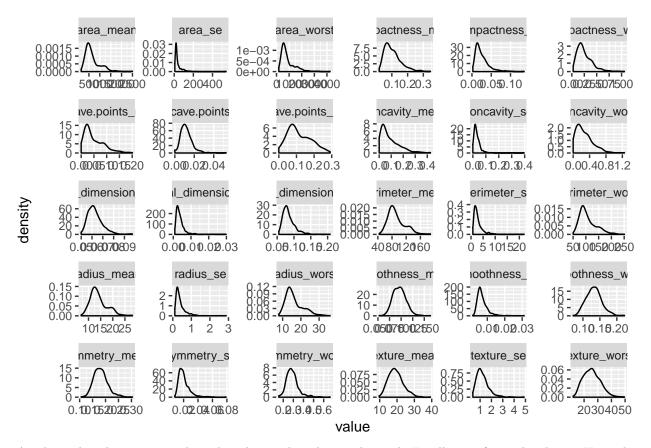


### summary(bcancer[,3:32])

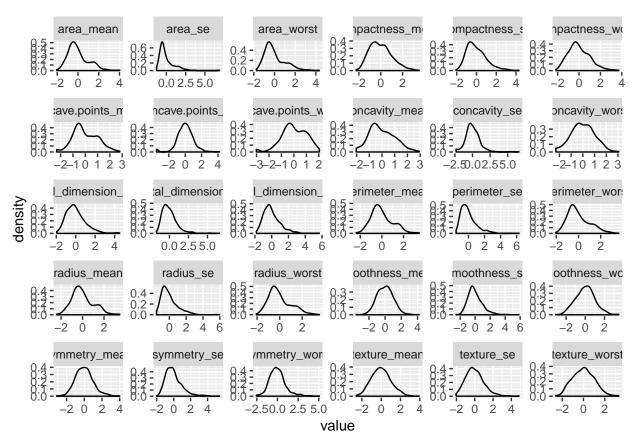
```
##
     radius_mean
                       texture_mean
                                       perimeter_mean
                                                           area_mean
          : 6.981
                             : 9.71
                                             : 43.79
                                                                : 143.5
##
    Min.
                      Min.
                                       Min.
                                                         Min.
##
    1st Qu.:11.700
                      1st Qu.:16.17
                                       1st Qu.: 75.17
                                                         1st Qu.: 420.3
    Median :13.370
##
                      Median :18.84
                                       Median: 86.24
                                                         Median: 551.1
##
    Mean
           :14.127
                             :19.29
                                              : 91.97
                                                                : 654.9
                      Mean
                                       Mean
                                                         Mean
##
    3rd Qu.:15.780
                      3rd Qu.:21.80
                                       3rd Qu.:104.10
                                                         3rd Qu.: 782.7
##
                                              :188.50
                                                         Max.
                                                                :2501.0
    Max.
           :28.110
                      Max.
                             :39.28
                                       Max.
##
    smoothness mean
                       compactness mean
                                          concavity mean
                                                             concave.points mean
##
    Min.
           :0.05263
                       Min.
                              :0.01938
                                          Min.
                                                  :0.00000
                                                             Min.
                                                                     :0.00000
##
    1st Qu.:0.08637
                       1st Qu.:0.06492
                                          1st Qu.:0.02956
                                                             1st Qu.:0.02031
                       Median :0.09263
                                                             Median :0.03350
##
    Median : 0.09587
                                          Median : 0.06154
    Mean
           :0.09636
                       Mean
                              :0.10434
                                          Mean
                                                  :0.08880
                                                             Mean
                                                                     :0.04892
##
    3rd Qu.:0.10530
                       3rd Qu.:0.13040
                                          3rd Qu.:0.13070
                                                             3rd Qu.:0.07400
           :0.16340
                              :0.34540
                                          Max.
                                                  :0.42680
                                                                     :0.20120
##
    Max.
                       Max.
##
    symmetry_mean
                      fractal_dimension_mean
                                                radius se
                                                                  texture_se
    Min.
           :0.1060
                                                      :0.1115
                                                                        :0.3602
                      Min.
                             :0.04996
                                              Min.
                                                                Min.
##
    1st Qu.:0.1619
                      1st Qu.:0.05770
                                              1st Qu.:0.2324
                                                                1st Qu.:0.8339
    Median :0.1792
                      Median :0.06154
                                              Median :0.3242
##
                                                                Median :1.1080
##
    Mean
           :0.1812
                             :0.06280
                                              Mean
                                                      :0.4052
                                                                        :1.2169
                      Mean
                                                                Mean
##
    3rd Qu.:0.1957
                      3rd Qu.:0.06612
                                              3rd Qu.:0.4789
                                                                3rd Qu.:1.4740
                                                      :2.8730
##
    Max.
           :0.3040
                      Max.
                             :0.09744
                                              Max.
                                                                Max.
                                                                        :4.8850
##
     perimeter_se
                         area_se
                                         smoothness_se
                                                             compactness_se
           : 0.757
                             : 6.802
                                                 :0.001713
                                                                     :0.002252
    1st Qu.: 1.606
                      1st Qu.: 17.850
                                         1st Qu.:0.005169
##
                                                             1st Qu.:0.013080
```

```
Median : 2.287
                      Median: 24.530
                                         Median :0.006380
                                                              Median: 0.020450
                                                 :0.007041
##
                             : 40.337
                                                                     :0.025478
    Mean
           : 2.866
                      Mean
                                         Mean
                                                              Mean
##
    3rd Qu.: 3.357
                      3rd Qu.: 45.190
                                         3rd Qu.:0.008146
                                                              3rd Qu.:0.032450
##
           :21.980
                              :542.200
                                         Max.
                                                 :0.031130
                                                             Max.
                                                                     :0.135400
    Max.
                      Max.
##
     concavity se
                       concave.points se
                                            symmetry se
##
           :0.00000
                               :0.000000
                                           Min.
                                                   :0.007882
    Min.
                       Min.
    1st Qu.:0.01509
                       1st Qu.:0.007638
                                           1st Qu.:0.015160
##
##
    Median : 0.02589
                       Median :0.010930
                                           Median :0.018730
##
    Mean
           :0.03189
                       Mean
                               :0.011796
                                           Mean
                                                   :0.020542
##
    3rd Qu.:0.04205
                       3rd Qu.:0.014710
                                           3rd Qu.:0.023480
    Max.
           :0.39600
                       Max.
                               :0.052790
                                           Max.
                                                   :0.078950
##
    fractal_dimension_se radius_worst
                                           texture_worst
                                                            perimeter_worst
##
    Min.
           :0.0008948
                          Min.
                                  : 7.93
                                                   :12.02
                                                            Min.
                                                                    : 50.41
                                           Min.
    1st Qu.:0.0022480
                                           1st Qu.:21.08
##
                          1st Qu.:13.01
                                                            1st Qu.: 84.11
##
    Median :0.0031870
                          Median :14.97
                                           Median :25.41
                                                            Median: 97.66
##
    Mean
           :0.0037949
                          Mean
                                  :16.27
                                           Mean
                                                   :25.68
                                                            Mean
                                                                    :107.26
##
                          3rd Qu.:18.79
                                           3rd Qu.:29.72
                                                            3rd Qu.:125.40
    3rd Qu.:0.0045580
##
           :0.0298400
                          Max.
                                  :36.04
                                           Max.
                                                   :49.54
                                                            Max.
                                                                    :251.20
##
                      smoothness_worst
      area_worst
                                         compactness_worst concavity_worst
                      Min.
##
           : 185.2
                              :0.07117
                                         Min.
                                                 :0.02729
                                                            Min.
                                                                    :0.0000
##
    1st Qu.: 515.3
                      1st Qu.:0.11660
                                         1st Qu.:0.14720
                                                            1st Qu.:0.1145
##
    Median : 686.5
                      Median :0.13130
                                         Median :0.21190
                                                            Median :0.2267
    Mean
           : 880.6
                              :0.13237
                                                 :0.25427
##
                      Mean
                                         Mean
                                                            Mean
                                                                    :0.2722
    3rd Qu.:1084.0
                      3rd Qu.:0.14600
                                         3rd Qu.:0.33910
##
                                                            3rd Qu.:0.3829
                              :0.22260
##
    Max.
           :4254.0
                      Max.
                                         Max.
                                                 :1.05800
                                                            Max.
                                                                    :1.2520
##
    concave.points_worst symmetry_worst
                                            fractal dimension worst
##
    Min.
           :0.00000
                          Min.
                                  :0.1565
                                            Min.
                                                    :0.05504
                          1st Qu.:0.2504
##
    1st Qu.:0.06493
                                            1st Qu.:0.07146
##
   Median :0.09993
                          Median :0.2822
                                            Median :0.08004
##
    Mean
           :0.11461
                          Mean
                                  :0.2901
                                            Mean
                                                    :0.08395
##
    3rd Qu.:0.16140
                          3rd Qu.:0.3179
                                             3rd Qu.:0.09208
##
    Max.
           :0.29100
                          Max.
                                  :0.6638
                                            Max.
                                                    :0.20750
```

Many features in the data are highly correlated. For e.g. radius mean and radius worst. This could cause multicolinearity in our models. Looking at the univariate plot of the data, we can see that the variables are very skewed . Most variables are right skewed and have varying range and scales. The variance in some of the area\_se variable is quite high.



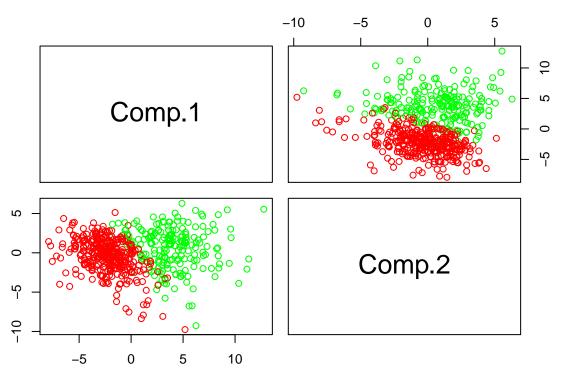
As these distributions are skewed and vary largely on the scale I will transform the data. Using log transformation will cause errors as some values are 0 leading to undefined cases. Hence, I use a square root transformation and then rescale the data.



Now that the data is centered we could try different models on our data set. As there are many features in the data , to reduce the dimentionality of the data I will run a PCA on the scaled and transformed data.

```
pca <- princomp(sdata[,3:32])
pca_scores <- pca$scores
#pca$loadings

pairs(pca_scores[,1:2] , col = c("red" , "green")[sdata$diagnosis])</pre>
```



From the factor loading we can see that none of the components contribute heavily into the classification and only 7% variance is explained by the first 2 components. There are some overlap regions between the two classes which would be difficult to classify. Its hard to say from the princomp to decide which component will classify the data correctly, I chose to not go ahead with pca.

```
s <- sdata[,2:32]
inTrain <- createDataPartition(y=s$diagnosis, p=0.7, list=FALSE)</pre>
training <- s[inTrain,]</pre>
testing <- s[-inTrain,]</pre>
SVM - Linear
train_control <- trainControl(method="repeatedcv", number=10, repeats=20)</pre>
s <- sdata[,2:32]
svmLinear <- train(diagnosis~., data= training, trControl=train_control, method="svmLinear")</pre>
fit_svmLinear <- predict(svmLinear , newdata = testing)</pre>
cm_svmL <- confusionMatrix(fit_svmLinear , testing$diagnosis)</pre>
{\tt cm} {\tt svmL}
## Confusion Matrix and Statistics
##
##
              Reference
## Prediction
                      7
             B 107
##
##
                 0
                    56
##
##
                   Accuracy : 0.9588
                      95% CI: (0.917, 0.9833)
##
##
       No Information Rate: 0.6294
       P-Value [Acc > NIR] : < 2e-16
##
```

##

```
##
                      Kappa: 0.9097
   Mcnemar's Test P-Value: 0.02334
##
##
##
               Sensitivity: 1.0000
##
               Specificity: 0.8889
            Pos Pred Value: 0.9386
##
##
            Neg Pred Value: 1.0000
##
                Prevalence: 0.6294
##
            Detection Rate: 0.6294
##
      Detection Prevalence: 0.6706
##
         Balanced Accuracy: 0.9444
##
          'Positive' Class : B
##
##
SVM - Radial
We will perform a 10 fold cross validation on the test data and do an out of sample testing for each model.
svmRadial <- train(diagnosis~., data= training, trControl=train_control, method="svmRadial")</pre>
fit_svmRadial <- predict(svmRadial , newdata = testing)</pre>
cm_svmR <- confusionMatrix(fit_svmRadial , testing$diagnosis)</pre>
cm svmR
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                В
            B 107
##
                     5
                  58
##
                0
##
##
                  Accuracy: 0.9706
##
                     95% CI: (0.9327, 0.9904)
##
       No Information Rate: 0.6294
##
       P-Value [Acc > NIR] : < 2e-16
##
##
                      Kappa: 0.9359
    Mcnemar's Test P-Value: 0.07364
##
##
##
               Sensitivity: 1.0000
##
               Specificity: 0.9206
##
            Pos Pred Value: 0.9554
##
            Neg Pred Value: 1.0000
##
                Prevalence: 0.6294
            Detection Rate: 0.6294
##
##
      Detection Prevalence: 0.6588
##
         Balanced Accuracy: 0.9603
##
          'Positive' Class : B
##
##
svmRadial$results$Accuracy
```

## [1] 0.9670545 0.9744583 0.9798365

```
svmRadial$results$AccuracySD
```

```
## [1] 0.02731376 0.02417758 0.02079046
```

SVM does a good job in predicting the classes with only 3 data points misclassified in the Radial SVM model. The insample accuracy of the model is also quite high with the standard deviation of 0.02. We can say the accuracy estimate of SVM is strong. In this problem, the false negatives are of high importance. It is crucial to detect the tumor so that the patients get treatments. Hence, we will try to reduce the false negatives, i.e those cases that are originally malignant but classified as benign.

```
knn <- train(diagnosis~., data= training, trControl=train_control, method="knn")
fit_knn <- predict(knn , newdata = testing)
CM_KNN <- confusionMatrix(fit_knn , testing$diagnosis)
CM_KNN</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                В
                    М
            B 105
                    5
##
                2
                   58
##
            M
##
##
                  Accuracy: 0.9588
                    95% CI : (0.917, 0.9833)
##
##
       No Information Rate: 0.6294
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.9109
    Mcnemar's Test P-Value: 0.4497
##
##
               Sensitivity: 0.9813
##
##
               Specificity: 0.9206
##
            Pos Pred Value: 0.9545
##
            Neg Pred Value: 0.9667
##
                Prevalence: 0.6294
##
            Detection Rate: 0.6176
##
      Detection Prevalence: 0.6471
##
         Balanced Accuracy: 0.9510
##
##
          'Positive' Class : B
##
```

KNN also has high accuracy but again there are more false negatives, which is not desirable.

We will try thr random forest model with grid search approach.

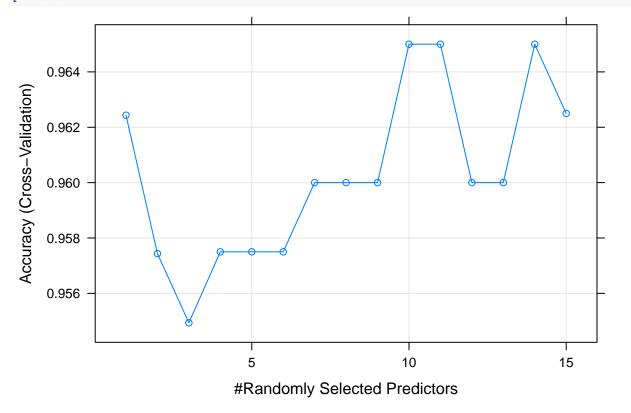
## Prediction

В

```
tuneGrid <- expand.grid(.mtry = c(1:15) )
trControl <- trainControl(method = "cv", number = 10, search = "grid")
rf <- train(diagnosis~., data= training ,method = "rf", metric = "Accuracy", trControl =trControl,tune
pred_rf <-predict(rf, testing)
CM_RF <- confusionMatrix(pred_rf , testing$diagnosis)
CM_RF</pre>
## Confusion Matrix and Statistics
##
Reference
```

```
##
            B 104
                    4
                   59
##
            М
                3
##
##
                  Accuracy : 0.9588
##
                    95% CI: (0.917, 0.9833)
       No Information Rate: 0.6294
##
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.9114
    Mcnemar's Test P-Value : 1
##
##
##
               Sensitivity: 0.9720
##
               Specificity: 0.9365
            Pos Pred Value: 0.9630
##
##
            Neg Pred Value: 0.9516
##
                Prevalence: 0.6294
##
            Detection Rate: 0.6118
##
      Detection Prevalence: 0.6353
##
         Balanced Accuracy: 0.9542
##
##
          'Positive' Class : B
##
```

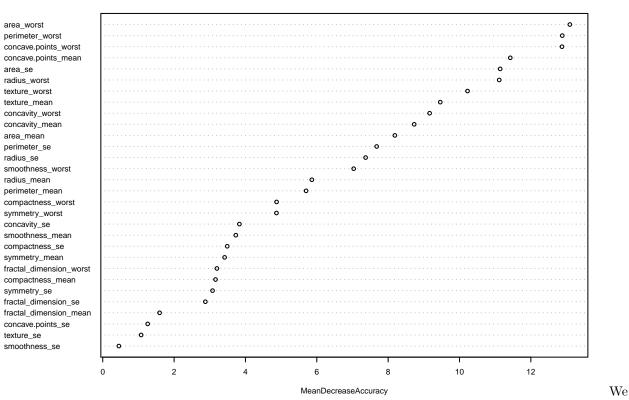
### plot(rf)



The results of random forest are more promising with just 2 false negatives. There are still 2 malignant cases that are classified as benign. We also have increased number of false positive in this model. I tried out different mtry for grid search and we can see that the maximum accuracy is obtained when 7 features are randomly sampled for each evaluation which also close to sqrt(30)

### varImpPlot(rf\$finalModel,type=1 ,cex=.5)

#### rf\$finalModel



also look at the variable importance to understand the contribution of each variable in the classification process. To try an improve our model I will next try a neural network.

```
set.seed(1101)
tuneGrid <- expand.grid(.size = c(1:6), .decay=c(0,2.5e-2,5e-2,7.5e-2,1e-1,1e-2) )
nnet <- capture.output(nn <- caret::train(diagnosis~., data= training, method = "nnet", metric = "Accur
fit_nn <- predict(nn , testing)
t <- confusionMatrix(fit_nn , testing$diagnosis)
t</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                В
            B 106
##
                    4
##
                1
                   59
##
                  Accuracy: 0.9706
##
                    95% CI: (0.9327, 0.9904)
##
##
       No Information Rate: 0.6294
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.9363
##
   Mcnemar's Test P-Value: 0.3711
##
```

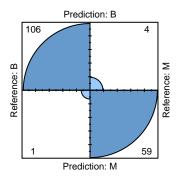
```
##
                       Sensitivity: 0.9907
                       Specificity: 0.9365
##
                  Pos Pred Value: 0.9636
##
##
                  Neg Pred Value: 0.9833
##
                         Prevalence: 0.6294
##
                  Detection Rate: 0.6235
         Detection Prevalence: 0.6471
##
##
              Balanced Accuracy: 0.9636
##
##
                'Positive' Class : B
##
nnet_vatimpt <- varImp(nn)</pre>
plot(nnet_vatimpt)
       texture_worst
smoothness_worst
   smootnness_worst
compactness_se
concave.points_mean
area_worst
concavity_mean
fractal_dimension_se
radius_worst
concave.points_worst
          perimeter_worst
area_mean
symmetry_worst
texture_mean
          radius_mean
perimeter_mean
            smoothness_se
                      area se
fractal dimension mean
      compactness_mean
          symmetry_mean
concavity_se
radius_se
                   texture_se
compactness_worst
perimeter_se
fractal_dimension_worst
symmetry_se
smoothness_mean
        concave.points_se
                                       0
                                                       20
                                                                        40
                                                                                        60
                                                                                                         80
                                                                                                                         100
                                                                        Importance
```

The neural network model also gives high accuracy and the missclassified rate is also low. Both the models random forest and Neural Network work well for this data. But I would like to go ahead with NNet model as it is less computational expensive compared to random forest.

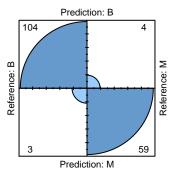
```
par(mfrow=c(2,2))

fourfoldplot(t$table ,conf.level = 0, margin = 1 , main = "Neural Net")
fourfoldplot(CM_RF$table ,conf.level = 0, margin = 1 , main = "Random Forest")
fourfoldplot(CM_KNN$table,conf.level = 0, margin = 1 , main = "KNN")
fourfoldplot(cm_svmR$table ,conf.level = 0, margin = 1 , main = "Linear SVM")
```

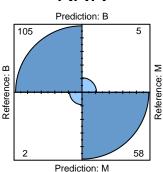
## **Neural Net**



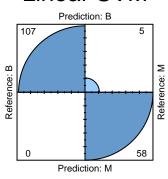
## Random Forest



## **KNN**



## Linear SVM



Analysing the missclassified data to understand the error in our model. Through bivariate plots it is difficult to understand the error. Some expertise on the data and knowledge of the subject would probably help us understand the problem and build a finer model to detect the cancer.

misclassified <- testing[which(fit\_nn != testing[,1]), ]
misclassified</pre>

```
##
       diagnosis radius_mean texture_mean perimeter_mean
                                                            area mean
## 74
               M -0.03606509
                               -0.81124238
                                              -0.002097492 -0.1028500
  136
                                0.77621175
##
               M -0.34756777
                                              -0.386399045 -0.3688263
##
  216
                  -0.01828376
                               -0.51937386
                                               0.020676442 -0.1200526
##
  264
               М
                   0.48438093
                                0.07632073
                                               0.399369535
                                                             0.4355538
##
   364
                  0.72920285
                               -0.18375347
                                               0.665137478
                                                             0.6600813
##
       smoothness_mean compactness_mean concavity_mean concave.points_mean
                                              0.08907512
##
   74
            0.34321220
                               0.5685772
                                                                    0.2517173
   136
                                                                   -0.4400026
##
           -0.38574209
                              -0.9443617
                                             -0.38190215
##
  216
            0.47551577
                               0.9760872
                                              0.35911332
                                                                    0.3832229
## 264
           -1.31440991
                              -0.9834196
                                             -0.47216534
                                                                   -0.3910957
   364
##
            0.07195321
                              -0.2893660
                                             -0.19160176
                                                                    0.1918038
##
       symmetry_mean fractal_dimension_mean radius_se
                                                           texture_se
##
  74
          -0.5288348
                                   0.4396747 -0.4519290 -1.24250505
##
   136
          -0.8301097
                                   -0.2883112 -0.6796914
                                                           0.41341433
##
  216
           1.0865208
                                   0.9318799 -0.5710834
                                                           0.06242961
## 264
          -0.9814880
                                   -1.2353503 -0.7189902 -0.33678578
                                   -1.0022117 -0.1535941 0.51973648
  364
          -1.1916831
##
##
       perimeter_se
                         area_se smoothness_se compactness_se concavity_se
                                     -0.8500412
                                                    -0.1549129
                                                                  -0.4492374
## 74
         -0.4568406 -0.39407448
##
  136
         -0.8507038 -0.54233489
                                      0.2635577
                                                     -0.8319450
                                                                  -0.1635229
                                     -0.3204383
                                                     0.6742002
## 216
         -0.4745039 -0.42129666
                                                                   0.4767663
```

```
## 264
         -0.7860712 -0.44260427
                                     -1.8147117
                                                     -1.1144742
                                                                  -0.7071624
## 364
         -0.1856965 -0.01308313
                                      0.1759969
                                                     -0.3407554
                                                                  -0.4104797
##
       concave.points_se symmetry_se fractal_dimension_se radius_worst
               -0.2837356 -1.18118889
## 74
                                                 -0.1858153
                                                               0.13602251
##
   136
               -0.3340067 -0.48928137
                                                 -0.4569881
                                                              -0.32625021
## 216
               0.5142158 -0.06704247
                                                  0.4863016
                                                              -0.04254602
## 264
               -1.0875033 -1.56060319
                                                  -1.3042620
                                                               0.41857230
                                                               0.46393764
               -0.0933569 -0.41892717
## 364
                                                  -0.8366042
##
       texture_worst perimeter_worst
                                         area_worst
                                                    smoothness worst
                                        0.007198285
## 74
         -0.77038345
                           0.16919269
                                                            0.4207874
   136
          1.23708790
                          -0.41966855 -0.339458820
                                                            0.4548136
## 216
          0.26229439
                          -0.01534565 -0.124366960
                                                            0.6277119
##
  264
          0.98965394
                           0.33983417
                                        0.354132653
                                                           -1.0636702
## 364
          0.02225315
                           0.37885383 0.392226809
                                                            0.1057293
##
       compactness_worst concavity_worst concave.points_worst symmetry_worst
## 74
                0.7683540
                               0.23384268
                                                       0.4739518
                                                                     -0.4901866
## 136
               -0.6292397
                              -0.05728276
                                                      -0.1483584
                                                                     -0.0708075
  216
                1.2179557
                               0.97257653
                                                       0.8000677
                                                                      1.2132903
## 264
               -0.3916455
                              -0.01493833
                                                      -0.2678673
                                                                     -0.3237052
##
  364
               -0.4962290
                              -0.33978416
                                                      -0.1804370
                                                                     -0.8454749
##
       fractal_dimension_worst
## 74
                      1.1103462
## 136
                     -0.1430000
## 216
                      1.2626932
## 264
                     -0.9138259
## 364
                     -1.1508780
plot(testing$texture_worst, col=ifelse(rownames(testing) %in% rownames(misclassified[1,])
, 'red', c("green", "blue")[testing$diagnosis]), lower.panel = NULL)
legend(120, 3, legend = c("Malignant" , "Benign" , "Misscfd as B") , col = c( "green" , "blue" , "red")
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      \sim
:esting$texture_worst
                                                                    Misscfd as B
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