Tutorial - 1

Ans i Osymptotic notation is used to describe the running time of an algorithm and how much time of an algorithm takes with a given input and when input is very Large.

Types of notations:-

1.7 Big O notation (O): - The notation O(n) is the formal way to running time. It measure the worst case time complexity on the longest amount of time an algorithm can possibly take to complet.

Eg:- for function f(n) o(fa)) = 0 (q(n))

V-C>O, n>h.

f(n) < c.g (n) g(n) is tight upper bond of f(n)

2.7 Big Omega Notation (-2):- The notation 2 (n) is the formal way to express the lower bound of an algorithm's running time. It measure the best amount of time an Case time complexity of the best amount of time an algorithm can possibly take to complete.

Eg: O(f(n)) = 2(g(n)) + c>o, n/no g(n) < c.f(n)

3.7 Thata Notation (0): - This notation is formal way to express both lower bound and the upper bound of an algorithm's running time. f(n) = 0(gn) $4 C_{1}.g(n) < f(n) < C_{2}.g(n)$ $+ n > max (n_{1}, n_{2})$ $C_{1} > 0 A C_{2} > 0$ Ansz for (i=1 ton) 110 (lag(n)) (= i + 2; 110(1) for i= 1, 2, 4, 8, 16 - 2 K. this means (K) times as per this code, it will run till 2K=n which means K=logn Complexity is O (log n) = 1+2+4+8 ----+ h T(n)=ank-1 => 1x2x-1 , h-2 K-1 2h = 2Klog (2n) = K log 2 $\log (n+1) = K$ $O(K) = O(1 + \log n)$ $= O(\log(n))$

ans T(n)= (3T(n-2) if n70 otherwise 13 T(n)= 3T(n-1)-(Put n=n-1 T(n-1)=3T(n-2)-(2) from 1 And 2 T(n)= 3(37(n-2)) => 97 (n-2) -(3 Put n= n-2 in (1) T(n)=3(T(n-3))-(9) T(n)= 27 (T(n-3) T(n) = 3 K(T(n-K)) 1 K=35 Put n-K=0 n=K T(n)=3 "[T(n-n)] T(n)= 3h [T (0)] (T(n)=13 $T(n) = 3^n \times 1$ T(n)=0(3") ans4 T(n) = (2T(n-1), n >0 } using backward substitution (T(n)= 2T(n-1) T(n-1) = 2T(n-2) T(n-2)=2T(n-3)T(1)=2T(0) T (0)=1

N+1 H >0(i*;*K)=0(n+1)*lgn*lgn] => 0[(n+1)* (lag2h)2] $T(n) = O(h(\log_2 n)^2)$ T(n)=T(n-3)+n2-0 Ons8 T (1)=1-(2) Put n=n-3 in 190 $T(n-3) + T(n-6) + (n-3)^2 - (3)$ Put (3) in 1 T(n)=T(n-6)+(n-3)2+ n2-69 Put n= n-6 in O T(n-6)=T(n-9)+(n-6)2-(5) Put 5 in 4 T(n)= T(n-9)+(n-6)2+(n-3)2+ 4 $T(n) = T(n-3K) + (n-3(K-1))^2 + (n-3(K-2))^2 + ... + h^2$ n=3K=1 > h-1=K $T(n) = T(1) + \left[n-3 \left(\frac{n-1}{3} - 2 \right) \right]^{2} + \left[n-3 \left(\frac{n-1}{3} - 2 \right) \right]^{2}$

for l=3, j=1+4+1+2 n=1+(K-1)d n=1+(K-1)3 $\frac{h-1}{3}+1=K$ K=n+2 11No of terms Generalizing for(j=h) j=n+K-1 times

 $T(n) = h + \frac{h+1}{2} + \frac{h+3}{3} + - - - \frac{h+K-1}{k} - n + c ms$

·: \= n+k-1 => \= n + \= k - \\ = \\ $= \frac{h(n+1)+hK-h}{2}$ $\Rightarrow \frac{n^2+h}{2} + nK-h$ h²+h+2nK-2h 2K After riemaining constant terms and lower T(n)=0(n2) Ans 10 nk y o (ch) as nk < a. Ch + n>, no for some constant a>0 for no=1 => 1× 50(2) no=1 & C=2,