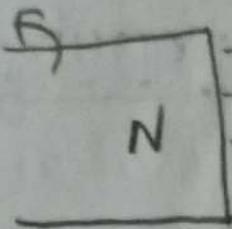


UNIT-II DC MACHINES

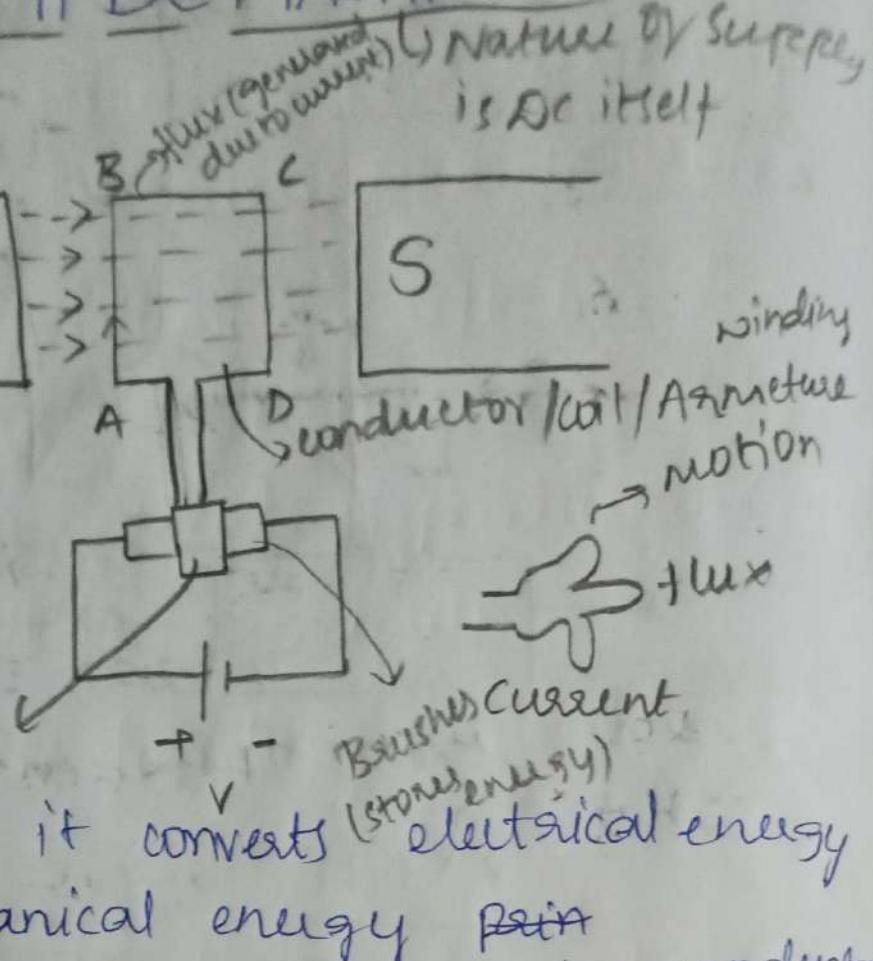
DC Motor:

Main field flux

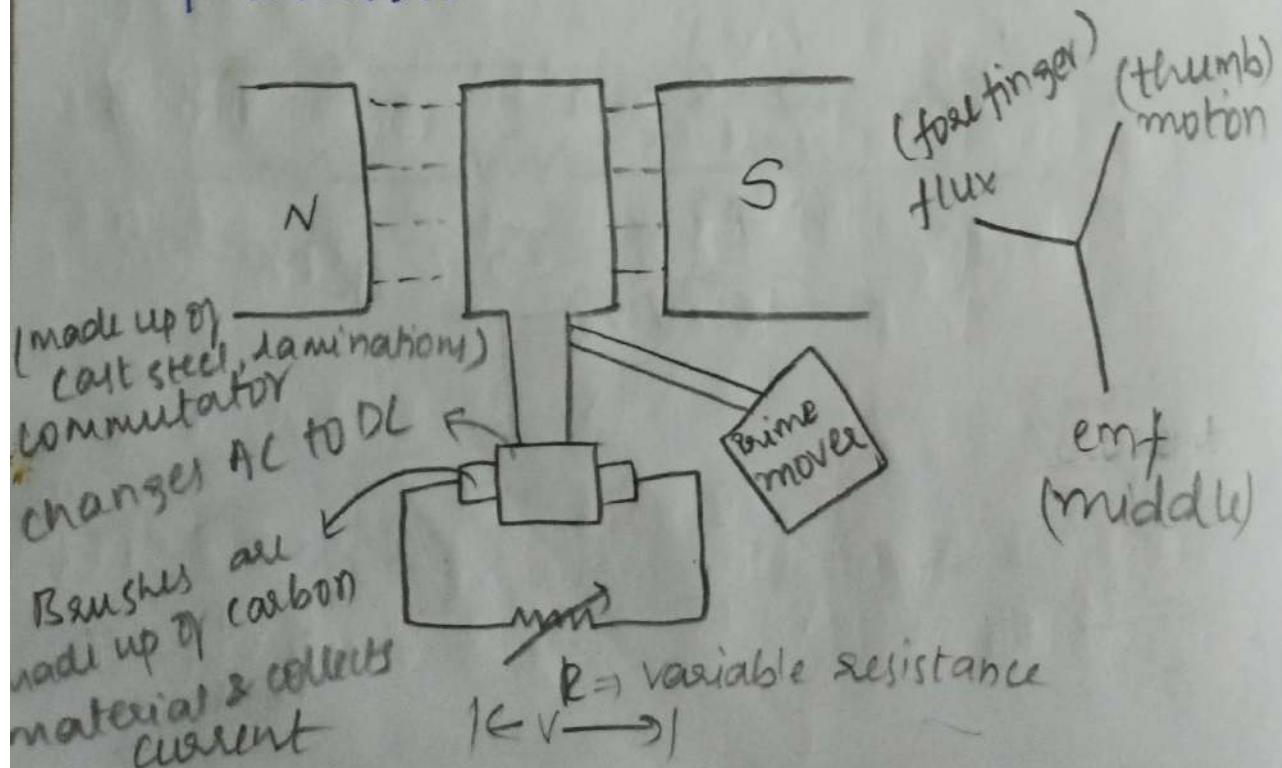


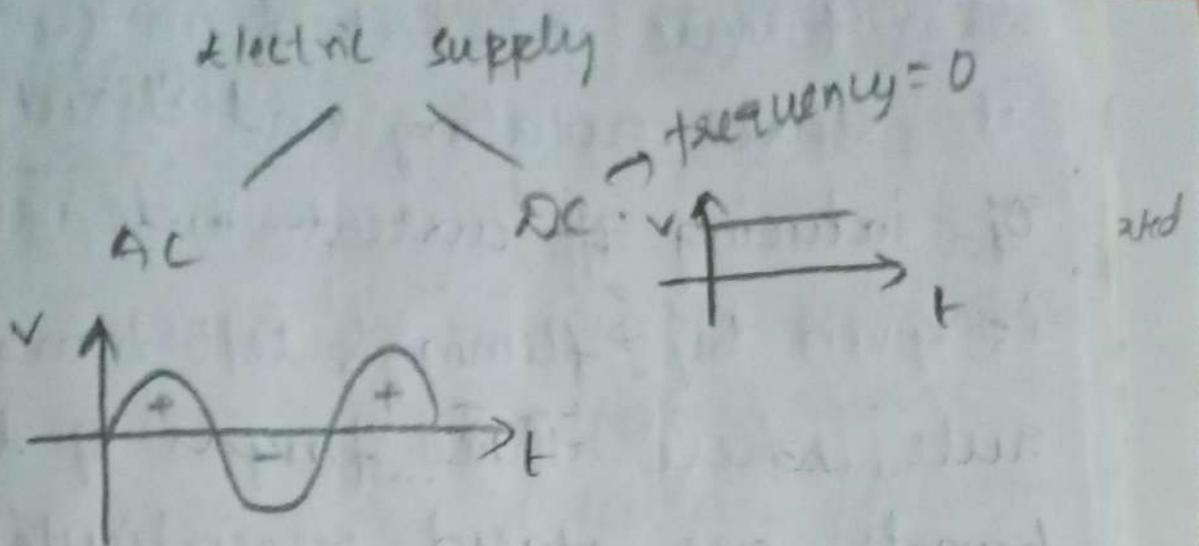
Motor converts electrical energy to mechanical energy.

commutator



DC Generator: hand rule





1 ϕ , 3 ϕ supplies will be there
 ↓ ↓ Indian standard
 240V, 415V, frequency 50Hz
 50Hz US standard
 frequency 60Hz

DC motor:

There are two fluxes produced in DC motor

- 1) Main field flux due to field winding
- 2) flux which is produced due to current flow in the conductor.

Due to interaction b/w these two fluxes there is a twisting or turning force produced which is nothing but torque.

When torque is exerted on the coil it starts rotating and direction of inducing of current in dc motor is given by Fleming's left hand rule where three fingers of left hand are placed perpendicular (90°) to each other & namely

thumb, forefinger, middle finger

Where

thumb - Represents motion of the conductor

forefinger - Indicates the direction of flux lines

middle finger - Represents direction of inducing of current in it

DC Generator:

Working principle of DC generator:

It is a rotating electrical machine

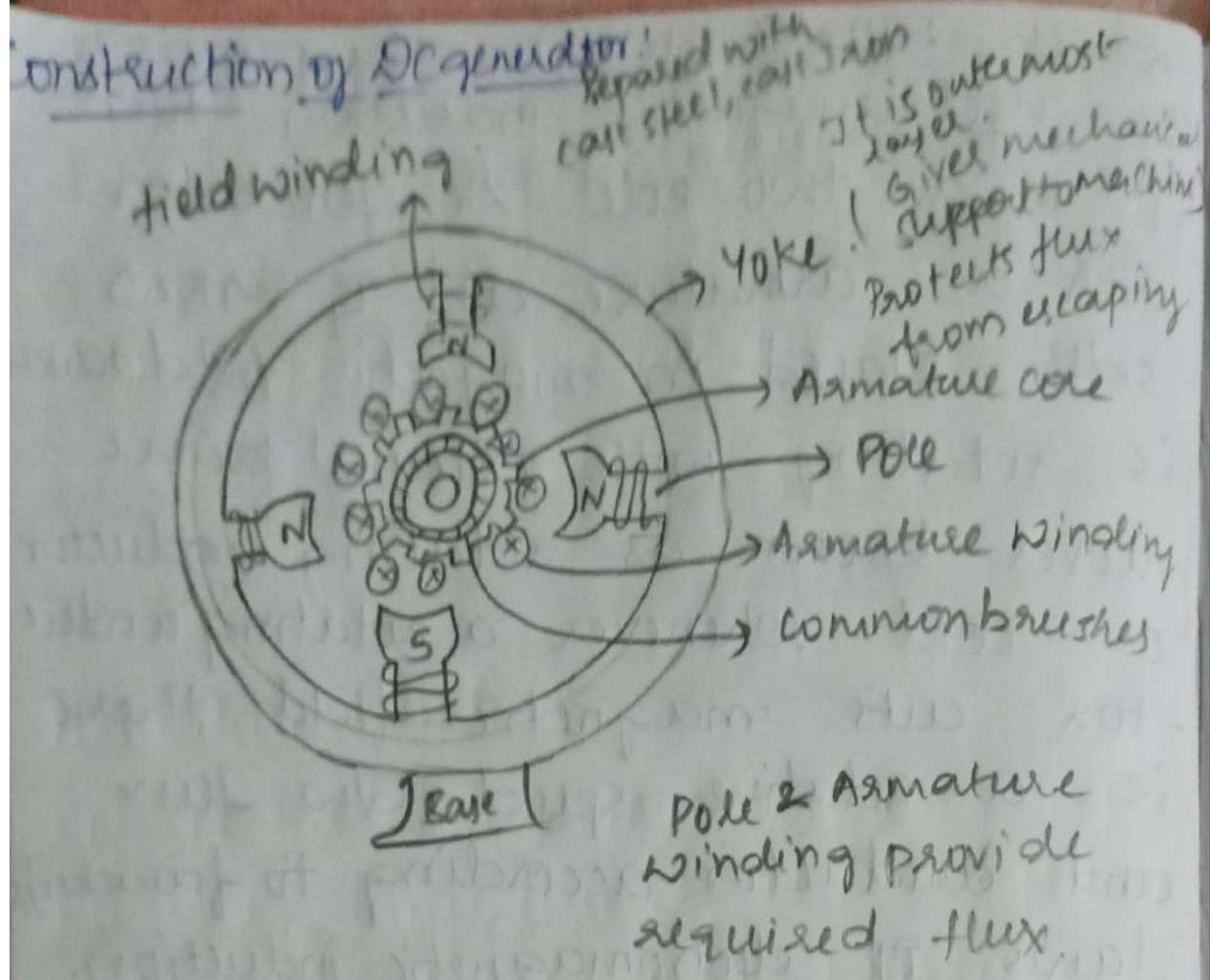
which works under the principle
of electromagnetic induction here
it is a two pole DC generator
with a armature coil of ABCD ^{and}
sides placed in magnetic field which
is rotating with external prime
mover known as rotating conductor
or coil. Whenever a rotating conductor
cuts magnetic field there
is a relative speed b/w flux
and conductor according to faraday's
laws of electromagnetic induction.
an emf gets induced in ABCD
coil.

According to Fleming's right hand
rule :

forefinger - Indicates flux
direction

Middle finger - Direction of induced
emf

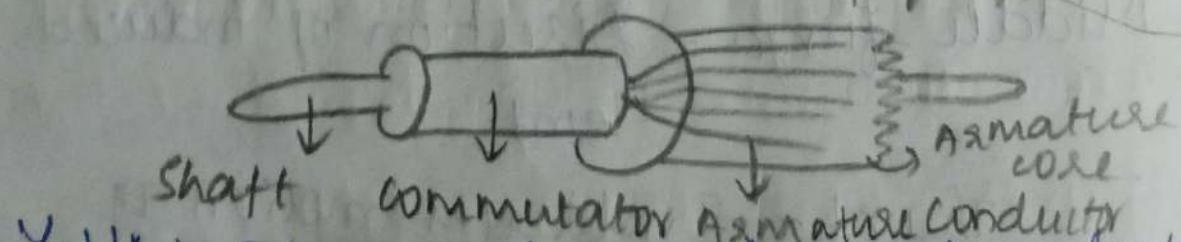
Thumb - Indicates motion of
conductor



Purpose of Pole is to hold the field winding.

(iii) conductor \Rightarrow Armature winding

Armature core \Rightarrow To hold
 Armature winding \Rightarrow made up of copper



Yoke: It provides mechanical protection to the entire machine made up

of cast iron or cast steel

Field Winding & Pole:

Pole is made up of high permeable material which holds field winding and also provides magnetic flux in the machine.

Field winding is made up of copper material which supports to develop magnetic flux.

Armature Core:

Armature core is a cylindrical drum shaped structure punched into slots on peripherals to hold armature winding made up of silicon laminated steel.

Commutator:

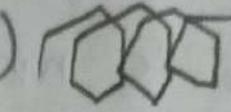
It is a mechanical rectifier used to convert pure AC to DC voltage. It is made up of ^{Hard drawn} COPPER.

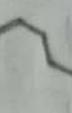
Brushes: It is soft material.

They are made up of carbon and used to collect current from rotating

commutator.

Axature winding: Made up of copper.

① Lap (it will be overlapped) 

② Wave (AVJI) 

At high current and low voltage

At high voltage & low current

Axature Winding:

It is a distributed winding as per the requirement it is classified into two types ① Lap winding

② Wave winding.

It is a main winding of the machine which supports to produce EMF and torque.

~~EMF~~ EMF ~~eqn~~ of a DC generator:

— According to Faraday law of EMF

$$E \propto \frac{d\phi}{dt}$$

induction

$$E = N \frac{d\phi}{dt}$$

$$N = 1$$

N = no of turns

E = Emt conductor per conductor

change in ϕ = $d\phi$ = $\phi \times p.$

ϕ = flux

p = Poles (no of poles)

change in time.

$$dt = \frac{60}{N}$$

$$E = \frac{d\phi}{dt} = \frac{\phi \times p}{\frac{60}{N}}$$

$$E = \frac{N \phi p}{60} \times \left(\frac{1}{A} \times z \right)$$

A = no of hel paths.

Z = no of conductors

ϕ = flux

N = speed.

p = poles.

$$Eq = \frac{\phi Z N P}{60 A}$$

$$E_g = \frac{\Phi Z N P}{60 A}$$

E_g = EMF or induced for 'z' no of
conductors.

A = no of parallel paths.

P = Poles.

Z = no of conductors.

N = Speed.

Φ = flux.

lap $A = P$ $\uparrow I \downarrow V$

lap $E_g = \frac{\Phi Z N P}{60 A} = \frac{\Phi Z N}{60}$

$$\boxed{\text{lap } E_g = \frac{\Phi Z N}{60}}$$

wave $A = 2$ $\uparrow V \downarrow I$

wave $E_g = \frac{\Phi Z N P}{60 \times 2} = \frac{\Phi Z N P}{120}$

$$\boxed{\text{wave } E_g = \frac{\Phi Z N P}{120}}$$

A four pole generator having wave wound armature winding has 51 slots each slot consisting of 20 conductors determine the generated EMF in the machine when driven at 1500 RPM if flux per pole is 7 milliwebers.

$P=4$

flux units = milli webers
= mwb.

$$\Phi = 7 \text{ mwb.} = 7 \times 10^{-3} = 0.007$$

$$P = 4.$$

$$Z = 51 \times 20.$$

$$N = 1500. \quad A = 2.$$

$$E_g = \frac{\Phi Z N P}{60 A} = \frac{10^3 \times 7 \times 51 \times 20 \times 1500 \times 4}{60 \times 2}$$

$$= \frac{7 \times 51 \times 18 \times 4}{60}$$

$$E = 357 V$$

Q) A 4 pole DC generator has a lap wound armature with 792 conductors if flux per pole is 0.012 Weber determine the speed at which it should run to generate $P=4$, $V=240V$

$$E_g = \frac{\phi Z N P}{60 A}$$

$$\phi = 0.012$$

$$N = ?$$

$$240 = 0.0121 \times 792 \quad E = V = 240$$

$$\frac{N}{60} = \frac{240 \times 60}{121 \times 792 \times 10^{-4}}$$

$$= \frac{24 \times 6 \times 10^6}{121 \times 792}$$

$$= \frac{144 \times 10^6}{95832} = 1502.6$$

$1500 \rightarrow$ Rated RPM. if load is there there would be around 1400.

Q) A 6 pole DC generator have wave wound armature with 574 conductors and armature is rotating with a 1492 RPM determine flux per pole at which it should run to generate

$$P=6 \quad z=574$$

$$220V$$

$$\boxed{A22}$$

$$N=1492$$

$$\phi=?$$

$$E=220V$$

$$220 = \frac{6 \times 574 \times 1492 \times \phi}{60 \times 2}$$

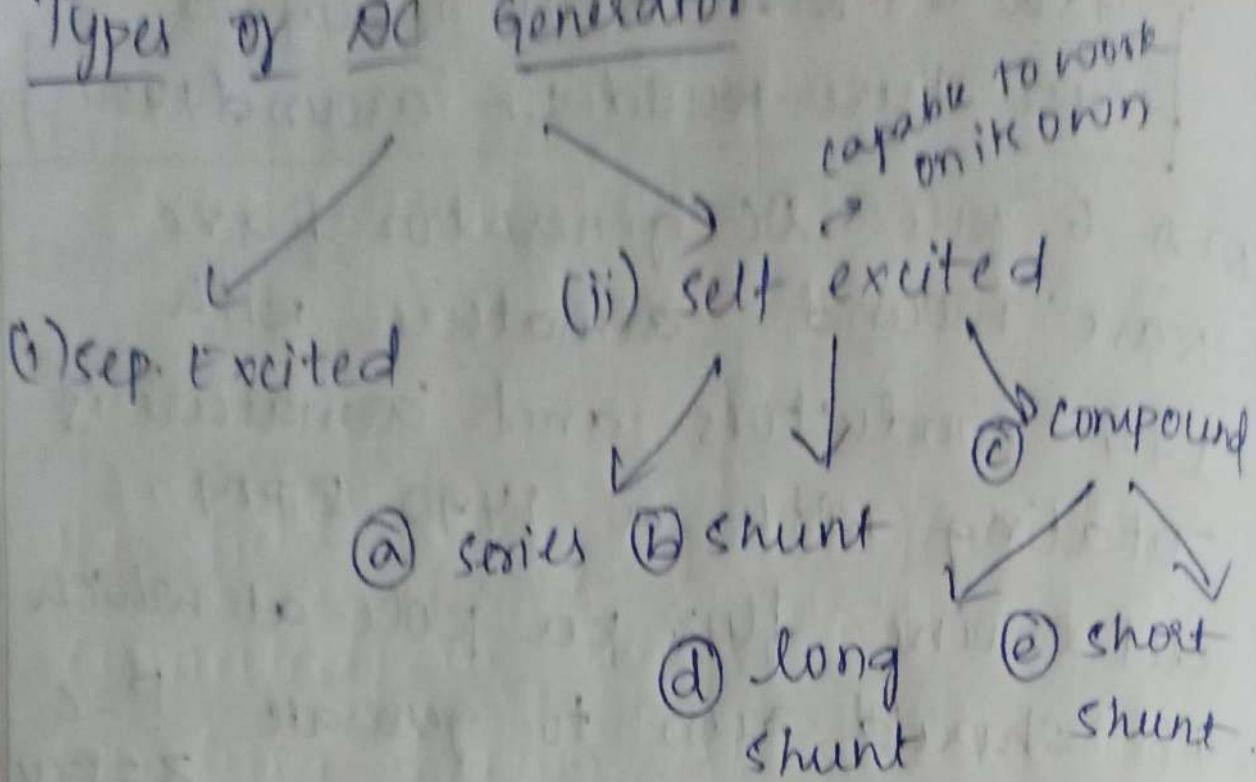
$$\phi = \frac{220 \times 60 \times 2}{6 \times 574 \times 1492}$$

$$= \frac{26400}{5138448}$$

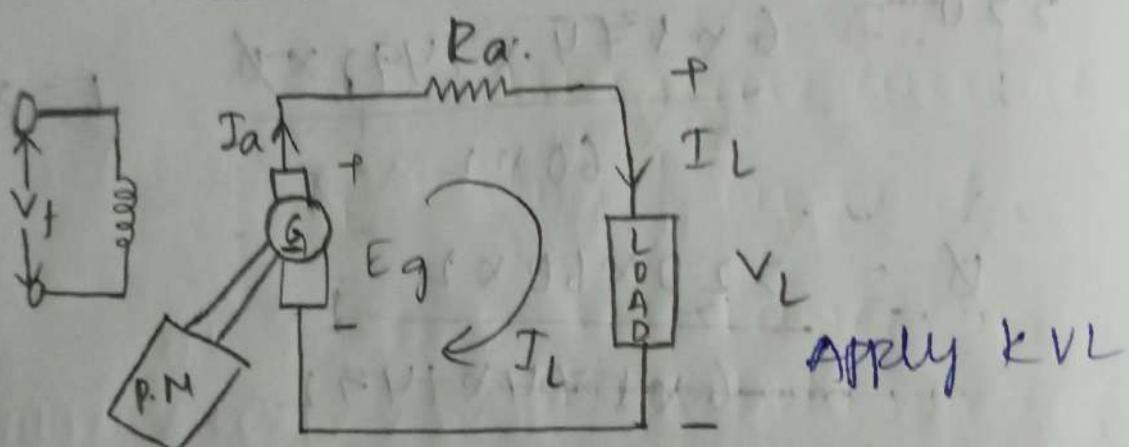
$$= 5.137 \times 10^{-3}$$

$$= 5.137 \text{ mWebers.}$$

Types of DC Generator?



(i) Separately generated DC generators:



$$-E_g + I_a R_a + V_L + B.C.D = 0.$$

$B.C.D$ = Brushes contact drop.

In problem-
If mentioned about BCD take
that BCD value if not take

$$BCD = 2V \text{ in problems.}$$

$$E_g = I_a R_a + v_L + BCD$$

armature generated power

$$P_g = E_g I_a$$

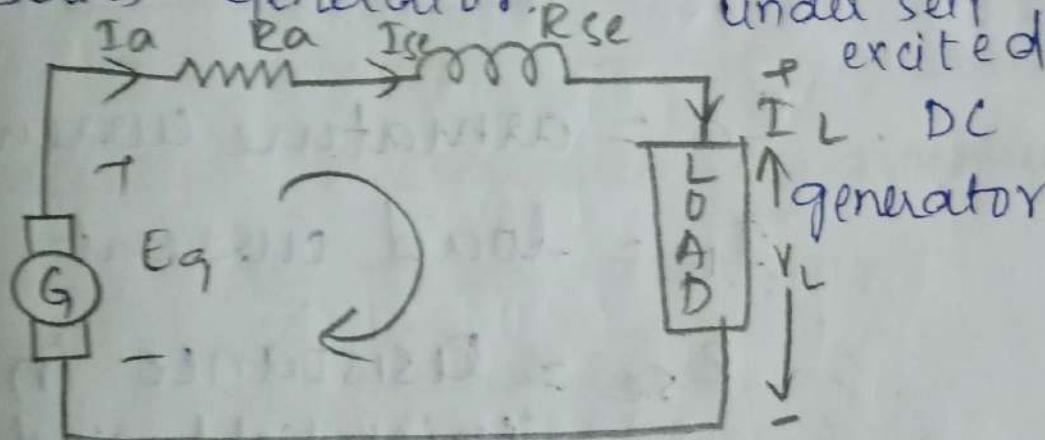
power consumed generated by load.

$$P_L = I_L V_L$$

$$I_a = I_L$$

(ii) Self Gen Excited:

② Series Generator: The field winding under self excited by



APPLY KVL

$$-E_g + I_a R_a + I_{se} R_{se} + V_L + BCD = 0$$

$$E_g = I_a R_a + I_{se} R_{se} + V_L + BCD$$

$$P_g = E_g I_a$$

Power generated in armature.

$$P_L = V_L I_L$$

Power consumed by load.

The field winding of DC generator connected in series with armature winding known as series generator current in.

I_{Se} = Series field winding

I_a = armature current.

I_L = load current.

R_{Se} = Resistance in series field winding.

R_a = armature resistance

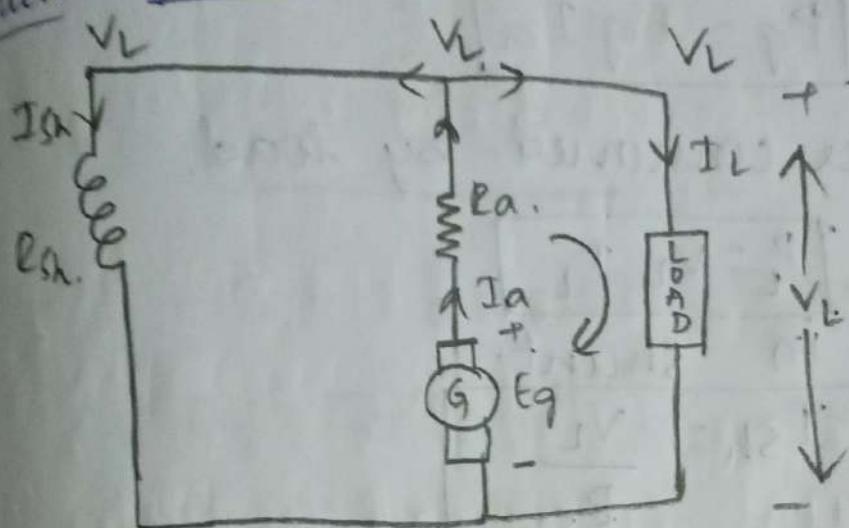
E_g = Generated voltage.

V_L = load voltage.

V_d ~~or~~ V_m BCD = Brush contact drop.

separately Generated!
 We need to separately provide electrical energy to the stator to get working flux on armature.

shunt Generator:



the field winding of the generator connected in parallel to armature known as shunt generator.

I_L = load current.

Applying $I_a = \text{armature current}$.

$E_g = \text{generated EMF}$.

$$E_g = I_a R_a + V_L + BCD$$

R_a = armature resistance.

R_{sh} = shunt field resistance.

V_L = load voltage or terminal voltage.

I_{sh} = shunt current.

$$\boxed{E_g = I_a R_a + V_L + BCD}$$

• Armature Current

$$I_a = I_L + I_{sh}$$

Power generated by armature

$$P_g = E_g I_a$$

Power consumed by load.

$$P_L = V_L I_L$$

current in shunt.

$$I_{sh} = \frac{V_L}{R_{sh}}$$

(e.g) weight lifting \rightarrow compound generator

train \rightarrow series generator \rightarrow to produce more torque

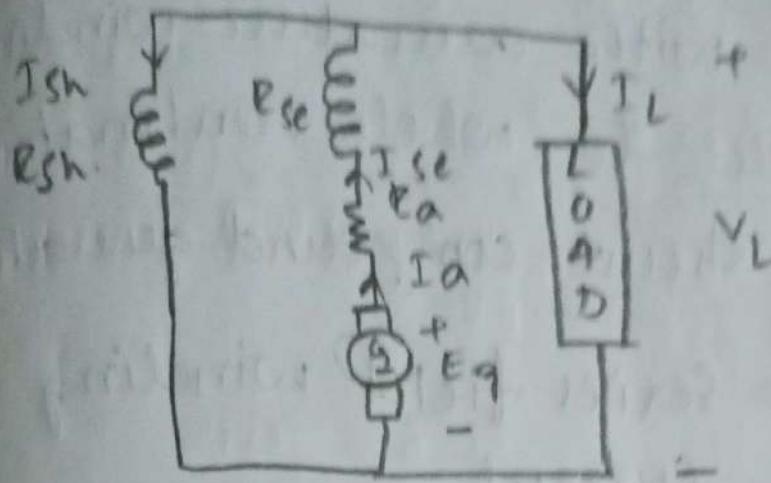
wills \rightarrow shunt generator \rightarrow for constant speed.

We use field winding in these series & shunt for flux.

② compound:

\hookrightarrow combination:

① long shunt compound generator:



$$-E_g + I_a R_a + I_{se} R_{se} + V_L + BCD = 0.$$

$$E_g = I_a R_a + I_{se} R_{se} + V_L + BCD$$

current through armature and shunt

are same

$$I_a = I_{se}$$

current is getting divided in $I_{sh}^2 I_L$

$$I_a = I_{se} = I_{sh} + I_L$$

Emf

$$E_g = I_a R_a + I_{se} R_{se} + V_L + BCD.$$

$$E_g = I_a (R_a + R_{se}) + V_L + BCD$$

Power generated by armature

$$P_g = E_g I_a = E_g I_{se}$$

$$P_L = V_L I_L$$

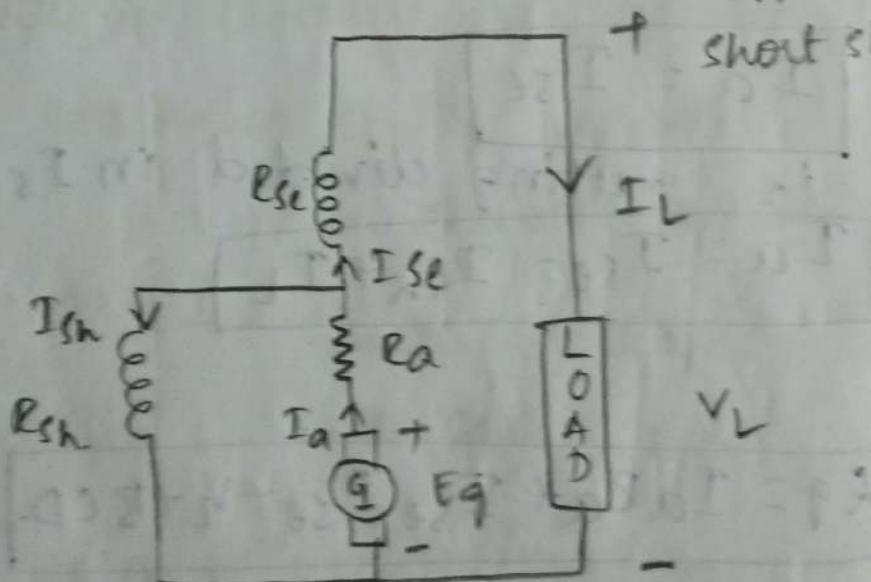
long shunt? The field winding in series with armature winding and parallel to whole combination is long shunt compound generator.

I_{se} = series field winding current

R_{se} = series field winding resistance

Short shunt compound generator:

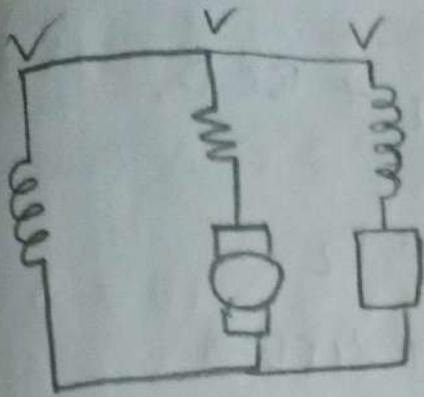
Application for short shunt



$$-E_q + I_a R_a + I_{se} R_{se} + V_L + BCD = 0$$

$$I_{sh} R_{sh} = I_{se} R_{se} + V_L$$

$$I_{sh} = \frac{I_{se} R_{se} + V_L}{R_{sh}}$$



$$I_a = I_{sh} + I_L$$

$$I_{se} = I_L$$

$$P_g = E_g I_g$$

$$P = V_L I_L$$

Q) A shunt generator delivers 450A at 230V the resistance of shunt field and armature resistance are 50Ω and 0.03Ω respectively calculate the generated emf.

~~$I_a = I_{sh} = 450 \text{ A}$~~

$I = 250 \text{ A}$

~~$V = 230 \text{ V}$~~

~~$R_a = 50 \Omega$~~

$R_{sh} = 50 \Omega$

~~$R_a = 0.03 \Omega$~~

~~V_{sh}~~

$I_a = 450 \text{ A}, V_L = 230 \text{ V}$

$R_{sh} = 50 \Omega, R_a = 0.03 \Omega$

$$E_g = I_a R_a + V_L + BCD.$$

$$I_a = I_{sh} + I_L$$

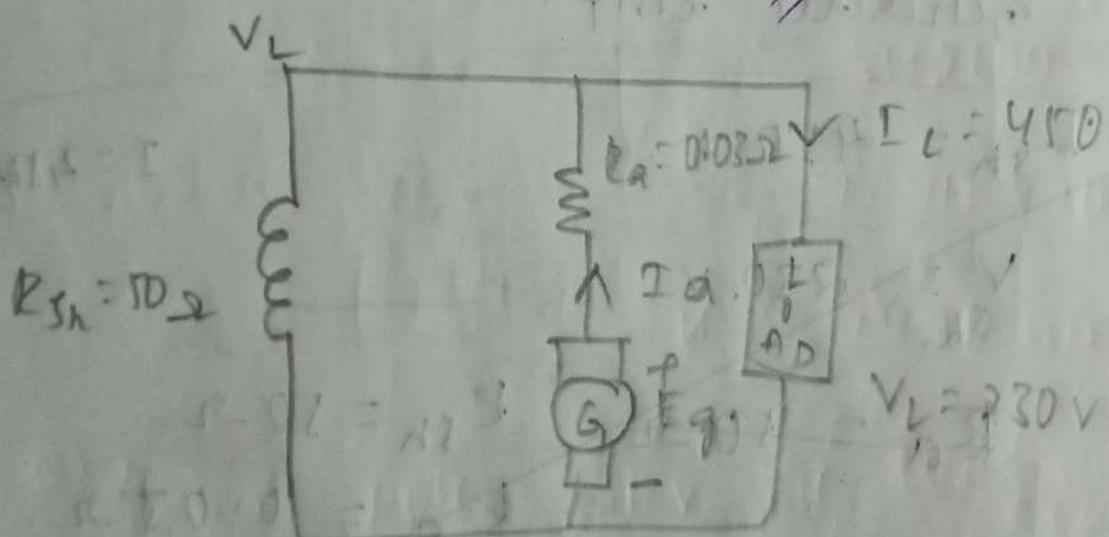
$$= \frac{230 + 450}{150}$$

$$= 4.6 + 450$$

$$= 454.6$$

$$E_g = (454.6)(0.03) + 230 + 2$$

$$= 245.638 V_{ff}$$



Q) A 8V 8 pole DC generator with 1778 wave connected armature running at 500 RPM supplies a load of 12.5Ω resistance. $N=1000$ $A=2$

$R_L = 12.5$ terminal voltage is 250V
 calculate 1) Armature current
 2) Generated EMF
 3) Flux per pole

assume armature resistance is
 0.24Ω and shunt field resistance
 is 250Ω.

Armature current

$$R_{sh} = 250\Omega$$

$$I_a = I_{sh} + I_L$$

$$V_L, R_{sh} = 250\Omega$$

$$I_a = \frac{V_L}{R_a}$$

$$R_a = 0.24\Omega$$

B

$$Z = 778$$

$$= \cancel{\frac{250}{0.24}} + \frac{250}{12.5}$$

$$\approx 10.41$$

$$I = 21.3$$

$$\frac{V_L}{R_{sh}}$$

$$I_L = \frac{V_L}{R_L} = \frac{250}{12.5} = 20A$$

$$= \frac{V}{R_{sh}} = \frac{250}{250} = 1A$$

$$I_a = 21A$$

$$E_g = I_a R_a + V_1 + BCD$$

$$= (21)(0.24) + 250 + 2.$$

$$E_g = 257.04 V$$

$$\cancel{\Phi} \Rightarrow E = \frac{\Phi Z N S}{60 A}$$

$$257.04 = \frac{\Phi \times 7.78 \times 8 \times 500}{120}$$

$$\Phi = \frac{30844.8}{3112000}$$

$$= 9.911 \times 10^{-3}$$

$$\Phi = 9.911 \text{ mwb.}$$

Q) A 4 pole 250V DC long shunt compound generator supplies a load of 10kW at the rated voltage. the armature, series ~~A~~ N_{sh} field and shunt field

distances are 0.1, 0.15, 250.52 respectively the armature is lap connected.

$$P=4$$

$$N = ?$$

$$P_L = 10 \text{ kW}$$

$$\Phi = 50 \text{ mwb}$$

$$A = P$$

$$Z = 50 \times 6$$

with 10 slots each slot containing 6 conductors if the flux per pole is 50 mwb. calculate N.

$$R_a = 0.1 \Omega \quad V_L = 250 \text{ V}$$

$$R_{Se} = 0.15 \Omega$$

$$R_{Sh} = 250 \Omega$$

$$E = \frac{\Phi Z N P}{60 A}$$

$$E = I_a R_a + I_{Se} R_{Se} + V_L + BCD.$$

$$I_a = 250 = 2500 \text{ A}$$

$$I_{Se} = \frac{V_L}{R_{Se}} = \frac{250}{0.15} = 1666.66$$

$$R_g = \frac{V_{NA}}{I_A}$$

$$= 60 \Omega$$

$$E_s = I_A R_{Ae} + I_{Se} R_{Se} + V_L + BCD$$

$$I_A = I_{Se}$$

$$= I_A (R_{Ae} + R_{Se}) + V_L + BCD$$

$$\text{Given } P_L = 10 \text{ kW} = V_L I_L$$

$$I_L = \frac{P_L}{V_L} = \frac{10 \times 10^3}{250}$$

$$= 40 \text{ A}$$

$$I_{Sh} = \frac{V}{R_{Sh}} = \frac{250}{250} = 1 \text{ A}$$

$$I_a = I_{se} = I_{sh} + I_L$$

$$I_a = 1440 = 41A.$$

$$E_b = 41(0.1 + 0.15) \times 250 \times 2$$

$$= 262.25V.$$

$$262 = \frac{50 \times 10^{-3} \times 300 \times N \times \phi}{60 \times \pi}$$

$$N = 10498 \text{ rpm}/\text{V}$$

Torque eq'n of a DC motor:

Torque is defined as twisting
turning force or movement
of pulley.

Product of force and it is given by
force and radius.

Let us consider a pulley of
radius r acted upon circumferen-
tial force newton's which causes
it to rotate at ' N ' rpm

$$T = F \times r \quad (\because P = \frac{W}{T})$$

$$W = F \times D$$

where $D =$ Distance travelled in
1 revolution.

Work done to complete 1 revolution

$$W = F \times D$$

$$= F \times 2\pi r$$

time taken complete 1 revolution

$$N - \text{rpm}$$

$$N \text{ rev} - 60 \text{ sec}$$

$$\text{rev} - ? \Rightarrow \frac{60}{N}$$

$$t = \frac{60}{N}$$

$$P = \frac{W}{t} = \frac{F \times D}{\frac{60}{N}}$$

$$P = \frac{F \times 2\pi r}{60/N}$$

$$= F \times r \times \frac{2\pi N}{60}$$

$$\boxed{T = T \times w}$$

$$\omega = \frac{2\pi N}{60} \Rightarrow \text{Angular velocity}$$

$$P = E_b \times I_a$$

$$E_b I_a = T \times w$$

$$E_b = \frac{T \times w}{I_a}$$

$$\frac{\phi \times r \times P}{60 A} = T_a \times \frac{2\pi N}{60 + a}$$

$$\boxed{T_a = \frac{\phi \times P \times I_a}{2\pi \times A}} \quad N \cdot m$$

Units of torque are $N \cdot m$!

where Φ = flux

Z = speed

P = pole

I_a = armature current

A = No of slot paths.

Q) calculate the value of Torque established by the armature of a 4 pole motor having 774 conductors. 2 paths in slot 24 mwb flux per pole when I_a is

50 A.

$P = 4$ $Z = 774$

$A = 2$ $\Phi = 24 \text{ mwb}$

$I_a = 50 \text{ A.}$

$$T_a = \frac{4 \times 24 \times 774 \times 50 \times 10^{-3}}{2 \times 3.14 \times 2} \quad \text{Ans.}$$

$$= \frac{4 \times 9288 \times 10^{-3}}{12.56} = 295.718 \text{ N.m.} \quad (\text{or})$$

Q) Determine the value of T in N-m developed by armature of 6 pole wave wound motor having 492 conductors and has an armature current of 10A, find out E_a ? $P=6$ $A=2$ $Z=492$

$$\theta = 30 \times 10^{-3} \quad I_a = 10.$$

$$E_a = \frac{8 \times 30 \times 10^{-3} \times 10 \times 492}{60 \times 2}$$

$$= \frac{3542.4}{60 \times 2} = 29.52.$$

$$= \frac{30 \times 40 \times 492 \times 10^{-2}}{29}$$

$$= 15 \times 492 \times 10^{-2}$$

$$= 282.032.$$

Q) A 250V dc motor runs at 1500 rpm and takes I_a of 50A back emf of DC motor is 240V obtain Torque developed in motor.

$$\frac{V_L}{K_B} = 250$$

$$N = 1500 \text{ rpm}$$

$$I_a = 50 \text{ A}$$

$$K_B = 240 \text{ V}$$

$$K_g = \frac{\Phi \times N}{60 \text{ A}}$$

$$K_B = \frac{T \times \omega}{I_a} \quad \omega = \frac{2\pi N}{60}$$

$$240 = \frac{157 \times T}{50} \quad \omega = 157$$

$$\frac{12000}{157} = T$$

$$T = 76.433 \text{ N-m}$$

Q) A 250V 4 pole wave wound dc series generator delivers a current of 180A. take $R_{ad} = 0.75\Omega$ and $r_s = 0.15\Omega$ calculate Emf generated & I_a of generator
 $P=4$ $A=2$

$$I_{Ld} = 180 \quad R_{ad} = 0.75\Omega$$

~~$E_g = 250V$~~

$$R_{se} = 0.15\Omega \quad V_L = 250V$$

$$I_a = I_{se} = I_d \quad I_a = \frac{E_g}{R_a}$$

$$E_g = I_a R_a + I_{se} R_{se} + V_L + BCD \quad - \frac{250}{0.75} =$$

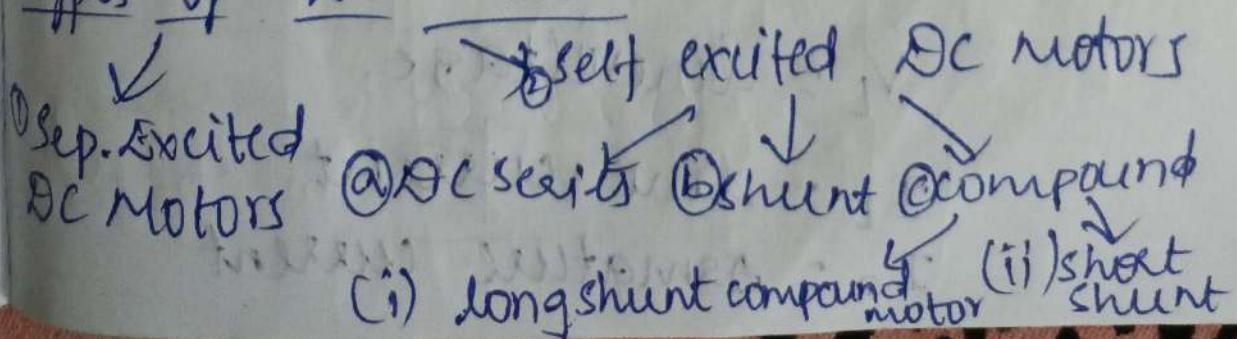
$$= (180)(0.75) + I_a = 333.3$$

$$(180)(0.15) + 250 + 2$$

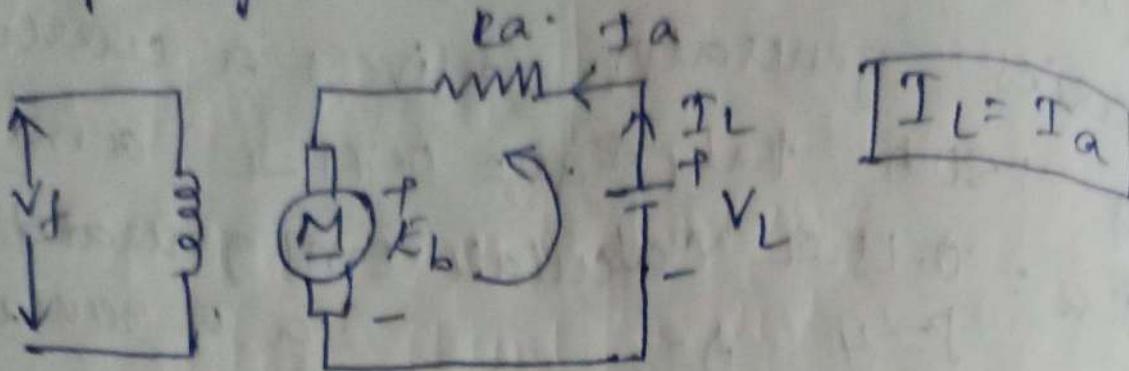
$$= 135 + 27 + 252$$

$$= 414V$$

Types of DC Motors:



① Separately excited DC motor:



Applying KVL

$$-V + I_a R_a + E_b = 0.$$

$$E_b = V - I_a R_a \quad \text{BCD}$$

Power generated across source.

$$P_S = V_L I_L$$

Mechanical

Power generated by motor armature

$$P_m = E_b I_a$$

→ whenever excitation to the field winding is provided by some external source is called separately excited DC motor.

V_L = line voltage.

I_L = line current

I_a = armature current

R_a = armature resistance.

V_f = field excitation.

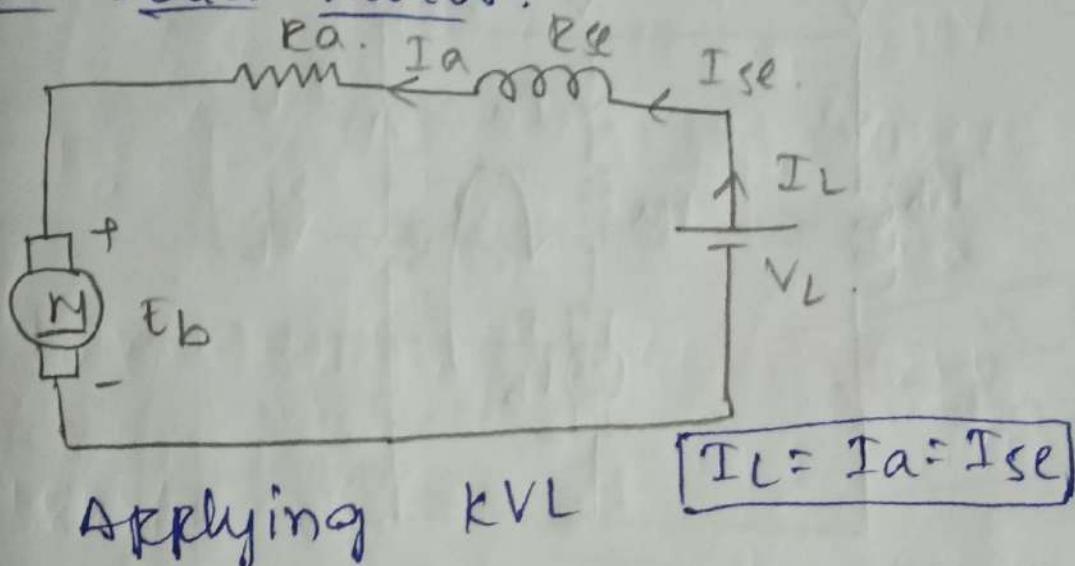
P_S = source power.

E_b = back emf.

P_m = mechanical power generated by armature.

2) Self-Excited DC motors:

a) DC series motor:



$$-V_L + I_{se} R_{se} + I_a R_a + E_b = 0$$

~~$$V_L = I_{se} R_{se} + I_a R_a + E_b + BCD$$~~

$$-V_L + I_a (R_a + R_{se}) + E_b = 0$$

~~$$E_b = V - I_a (R_a + R_{se}) - BCD$$~~

source power

$$P_S = V_L I_L$$

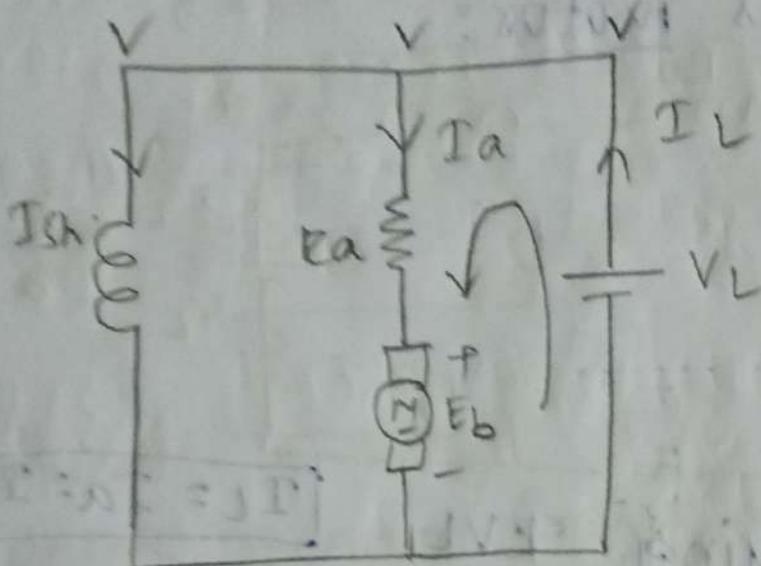
Mechanical power generated

$$P_m = E_b I_a$$

R_{sh} = shunt resistance

I_{sh} = shunt current

b) DC shunt motor:



Applying KVL:

$$-V + I_a R_a + E_b = 0$$

$$E_b = V - I_a R_a \rightarrow BCD$$

$$I_{sh} = \frac{V}{R_{sh}}$$

$$I_L = I_a + I_{sh}$$

$$\Phi_s = V_L I_L$$

$$P_m = E_b I_a$$

DC series motor:

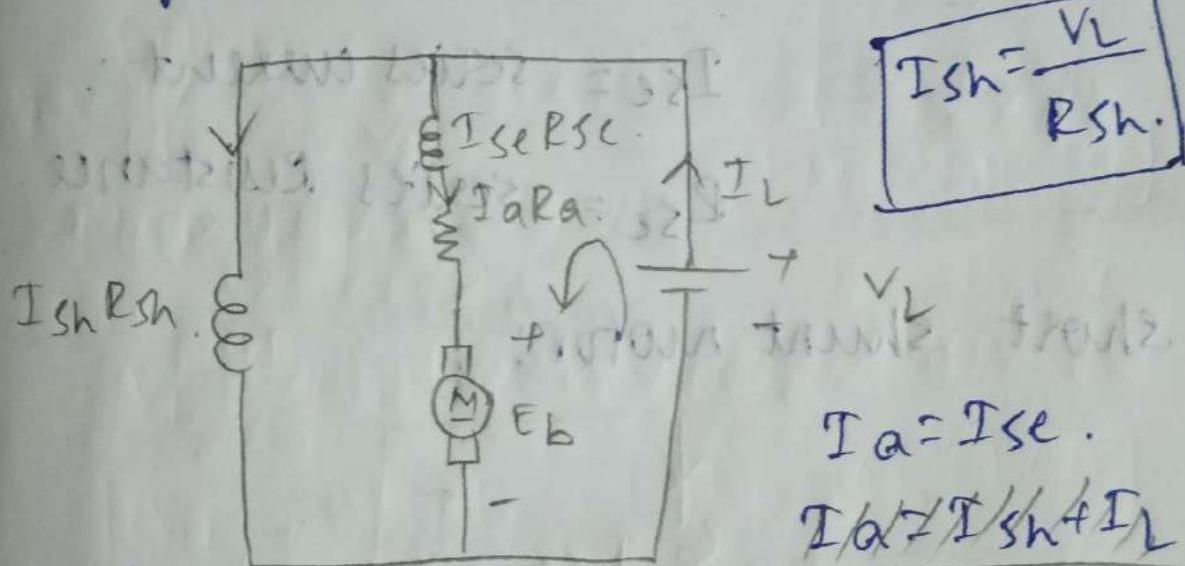
Whenever the field winding is connected in series with armature it is called DC series motor.

DC shunt motor:

Whenever the field winding is connected in parallel with armature it is called DC shunt motor.

② Compound motors:

long shunt compound motor:



$$I_{sh} = \frac{V_L}{R_{sh}}$$

$$I_a = I_{se}$$

$$I_a = I_{sh} + I_L$$

$$I_L = I_{se} + I_{sh}$$

Applying KVL

$$-V_L + I_{se} R_{se} + I_a R_a + E_b = 0.$$

+BCD.

$$V_L = I_{se} R_{se}$$

$$E_b = V_L - I_{se} R_{se} - I_a R_a$$

+BCD

$$E_b = V_L - I_a (R_{se} + R_a) - BCD$$

+BCD

Power in motor

$$P_M = F_b I_L$$

Power across source

$$P_S = V_L I_L$$

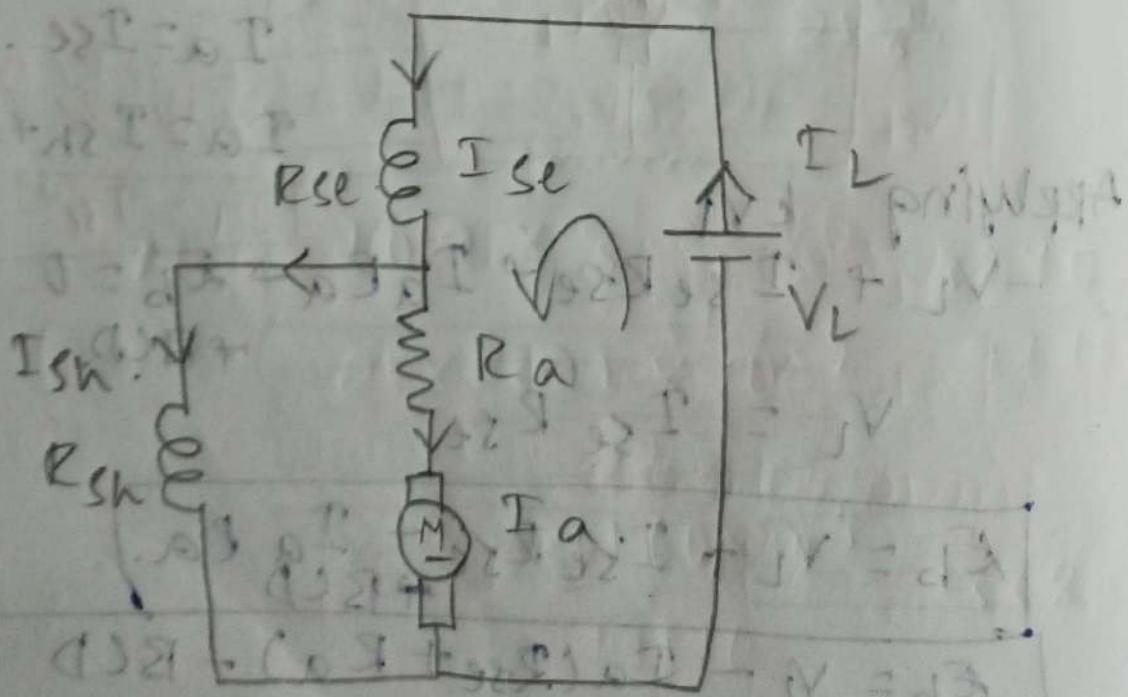
$$I_{Sh} = \frac{V}{R_{Sh}}$$

$$I_L = I_{Se} + I_{Sh}$$

I_{Se} = series current.

R_{Se} = series resistance.

short shunt motor:



$$-V_L + I_{se} R_{se} + I_a R_a + BCD = 0.$$

+ E_b

$$E_b = V_L - I_{se} R_{se} - I_a R_a - E_b - BCD.$$

$$I_L = I_{se}$$

$$I_L = I_{se} = I_{sh} + I_a$$

$$V_L I_L + I_{se} R_{se} = I_{sh} R_{sh}$$

$$I_{sh} = \frac{I_{se} R_{se} + V_L}{R_{sh}}$$

Q) A $\frac{SC}{6}$ pole shunt motor has wave connected armature with 87 slots, each slot containing 6 conductors. The $\Phi = 30 \text{ mwb}$. The armature has resistance $= 0.10 \Omega$. Calculate N , when motor is connected to 250V.

$$P = 6, A = 2 \quad \text{Supply} \propto$$

$$Z = 87 \times 6 \quad \text{taking } I_a = 80A$$

$$\Phi = 30 \text{ mwb} = 30 \times 10^{-3}$$

$$R_a = 0.10 \Omega$$

$$V_L = 250V$$

$$I_a = 80A$$

$$I_{sh} = \frac{V}{R_{sh}}$$

$$E_b = V - I_a R_a + BCD$$

$$= 250 - 80 \times 0.10 + 2$$

$$= 250 - 8 + 2$$

$$= 250 - 10 = 240$$

$$I_L = I_a + I_{sh}$$

$$P_s = V I_L$$

$$P_m =$$

$$\mathcal{E}_b = \frac{\phi Z N P}{60 A}$$

$$240 = \frac{30 \times 10^{-3} \times 87 \times 6 \times N \times 6}{60 \times 2}$$

$$\frac{240 \times 120}{3 \times 87 \times 6 \times 6 \times 10^{-2}} = N$$

$$\frac{240 \times 12}{3 \times 36 \times 87} = \frac{288}{9396} = N = 0.03065 \\ = 306.5$$

(Q) A 4 pole DC shunt motor has $\phi = 0.04 \text{ WB}$ & Armature is lap wound with 720 conductors

$$P = 4, \phi = 0.04 \text{ WB}, A = P \\ Z = 720$$

Shunt field resistance is 240Ω & $R_a = 0.2\Omega$
 $R_{sh} = 240\Omega$ BCD is $12V$ per

brush. Determine drop across the N of
machine running as motor at
60 A.

$$BCD = 24V$$

$$\text{P} = 4 \quad \therefore \quad = 2V$$

$$I_L = 60A$$

$$E_b = V - I_a R_a - BCD \quad V = 240V$$

$$E_b = 240 - (I_a)(0.2) - 2$$

$$I_L = I_a + I_{sh} \quad I_{sh} = \frac{V}{R_{sh}}$$

$$60 = I_a + I_{sh} \quad = \frac{240}{240}$$

$$60 = I_a + 1 \quad = 1$$

$$I_a = 59$$

$$E_b = 240 - (59)(0.2) - 2$$

$$E_b = 226.2$$

$$\frac{226.2 \pi}{0.04 \times 720} = L_b. \quad \frac{0.2 \pi N_p}{60 \pi}$$

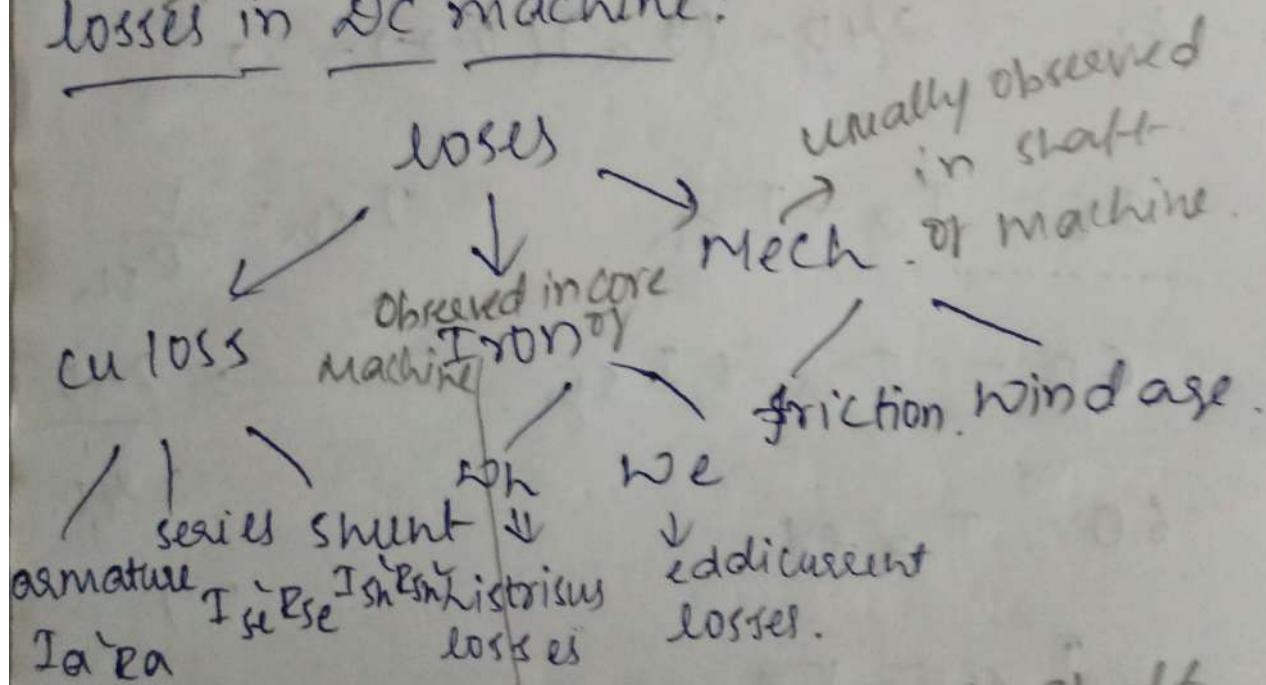
$$\frac{226.2 \times 60}{0.04 \times 720} = N.$$

$$\frac{13572}{28.8} = N.$$

$$N = 471.25 \text{ rpm.}$$

Power lost in the form of heat.

losses in DC machine:



for mechanical energy we use shaft.

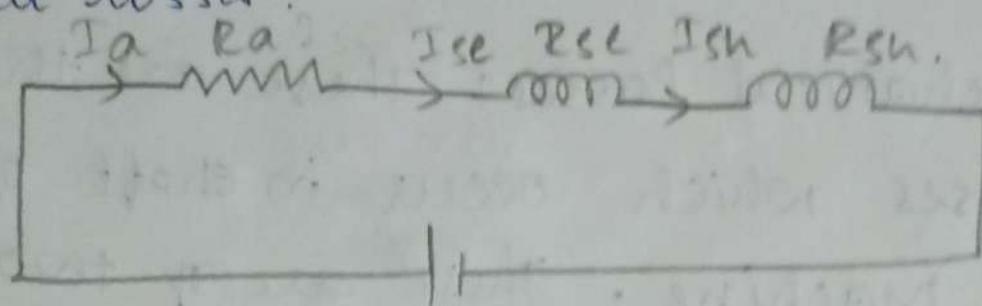
depends on material used

$B_h \Rightarrow$ max. flux density $\eta_h \Rightarrow$ histone coefficient

To reduce we use laminate core

t = thickness of each lamination

(i) cu losses:



$$\text{cu losses} = I_a^2 R_a + I_{se}^2 R_{se} + I_{sn}^2 R_{sn}$$

load will be connected to shaft.
It will be coupled directly.

(ii) iron loss: γ_h = eddy current co-efficient.

$$\text{hysteresis}(\text{wh}) = \gamma_h B_m^{1.6} f v.$$

$$\text{eddy losses}(\text{we}) = \gamma_e B_{\max}^2 f^2 + L$$

γ_h = hysteresis co-efficient.

$B_m^{1.6}$ = maximum flux density.

f = frequency.

V = volume of core.

t = thickness of lamination losses.
 \hookrightarrow to minimize the eddy current

- \sim

γ_e = eddy current co-efficients.

B_{max} = Maximum flux density.

f = frequency.

t = thickness.

Mechanical losses: These are the losses which occur in shaft or DC machine. These are of two types. 1) friction loss. 2) windage loss.

Copper losses: Power wasted in the form of $I^2 R$ and these type of losses occur in dc winding of the machine are called copper losses. These are of three types.

Efficiency (η) 1) armature

2) series

3) shunt.

Efficiency (η): The ratio of output power and input power is known as

efficiency. It is denoted by η

$$\eta = \frac{\text{output power}}{\text{input power}}$$

$$\begin{aligned}\eta &= \frac{P_o}{P_i} \\ &= \frac{P_o}{P_o + \text{losses}}\end{aligned}$$

$$\boxed{\therefore \eta = \frac{P_o}{P_o + \text{losses}} \times 100.}$$

Q) A 230V shunt motor delivers 30 HP at the shaft at 1120 RPM if the motor has efficiency of 87%. at this load determine

i) Total input power

ii) line current. (I_L)

$$V_L = 230V \quad N = 1120 \text{ RPM.}$$

$$\eta = 87\%$$

$$\begin{aligned}P_{\text{out}} &= 30 \text{ HP.} \\ &= 30 \times 10^3 \text{ W.} \\ &= 746\end{aligned}$$

$$\eta = \frac{P_o}{P_i} \times 100$$

$$\eta = \frac{30 \times 746}{P_i} \times 100$$

$$P_i = \frac{30 \times 746}{87} \times 100$$

$$P_i = 25724.137 \\ = 25724$$

$$I_L = \frac{V_L}{R_i}$$

$$= \frac{230}{25724}$$

$$P_i = I_L V_L$$

$$I_L = \frac{P_i}{V_L}$$

$$= \frac{25724}{230} = 111.843 A$$

Q) A shunt generator delivers 195A at a terminal voltage of 250V the armature & sh. R are 0.02Ω , 50Ω respectively. The iron & friction losses = 950W. find 1) Emf generated.
 2) Cu losses.
 3) Output of generator.
 4) n .

$$I_a = 195A.$$

$$V_L = 250V.$$

$$R_a = 0.02\Omega$$

$$R_{sh} = 50\Omega. \quad n_i \& n_f.$$

$$P_{AM} = 950W.$$

$$n_h B_m^{1.6} f_v$$

$$I_a = I_L + E_{sh}.$$

$$n_{cu} = ?$$

$$I_{sh} = \frac{V_L}{R_{sh}}$$

$$E_{mt} =$$

$$= \frac{250}{50} \\ = 5.$$

$$I_a = 195 + 5$$

$$= 200.$$

$$K_m = I_a R_a + V_L + R_{CD}$$

$$= (200)(0.02) + 250 + 2$$

$$= 4 + 252$$

$$= 256$$

$$N_C u = I_a' R_a + I_{sh}' R_{sh}$$

$$= (200)(200)(0.02) + (5)(5)(50)$$

$$= (200)(4) + (25)(50)$$

$$= 800 + 1250$$

$$= 2050 \text{ W}$$

$$P_0 = V_L I_L$$

$$= (250)(200)$$

$$= 500$$

$$\eta = \frac{P_0}{P_i} = (250)(195)$$

$$P_0 + \text{loss.}$$

$$= 48750$$

$$51710.$$

$$= \frac{48750}{48750 + 300}$$

$$\times 100 = 94.2\%$$

$$\eta = \frac{P_o}{P_o + \text{losses.}}$$

$$\begin{aligned}\text{losses} &= W_{Cu} + W_i + W_m \\ &= 950 + 2050 \\ &= 3000.\end{aligned}$$

~~W_{sh}~~

Q) A long shunt compound generator gives 240V at full load output of 100Amp resistance of ~~100~~ Ω . The resistance of various windings of the machine are $R_a = 0.1 \Omega$, $R_{se} = 0.02 \Omega$, $R_{sh} = 100 \Omega$. The iron loss on full load is 1000W. Windage & friction losses 500W. calculate full load efficiency of the machine.

$$\left. \begin{array}{l} V_L = 240V \\ I_L = 100A \\ W_i = 1000W \\ W_{sh} = 500W \end{array} \right\} \quad \begin{array}{l} R_a = 0.1 \Omega \\ R_{se} = 0.02 \Omega \\ R_{sh} = 100 \Omega \end{array}$$

$$\eta = \frac{P_0}{P_0 + \text{losses}}$$

$$I_a = I_{\text{reverse}} = I_{\text{shunt}} + I_L$$

$$E_g = I_a R_a + I_{\text{reverse}} R_{\text{reverse}} + V_L + E_L \text{ BCD}$$

$$P_0 = V_L \times I_L$$

$$P_0 = (100) (240)$$

$$= 24000.$$

$$I_a = I_{\text{shunt}} + I_L$$

$$I_{\text{shunt}} = \frac{V}{R_{\text{shunt}}} = \frac{240}{100} = 2.4$$

$$= 12.4 + 100 = 102.4$$

$$= 102.4 \times 2.4 = 240$$

$$E_g = 102.4 (0.1 + 0.02) + 240$$

$$= (102.4) (0.12) + 240$$

$$= 12.288 + 240$$

$$= 254.288$$

$$P_{cu} = (I_a R_a) + I_{se} R_{se} + I_{sh} R_{sh}$$

$$= (102.4)(102.4)(0.1) + (102.4) \text{ (labeled)} \\ (102.4)(0.02) + \\ (2.4)(2.4)(100)$$

$$= 1048.57 + 213.4576.$$

$$= 1837.57 -$$

$$\text{losses} = 1837.57 + 1000 + 500.$$

$$= 3337.57.$$

$$\eta = \frac{24000}{240000 + 3337.57} \times 100.$$

$$= \frac{24000}{27337.57} \times 100. \\ = 87.79.$$

$$= 87.8.$$