## Exp 4

Aim:Implementation of Statistical Hypothesis Test using Scipy and Sci-kit learn.

### **Theory and Output:**

#### 1. Loading dataset:

Data loading is the first step in data analysis. The dataset is stored in a CSV file and read  $using \ pandas.read\_csv()$ .

The first few rows are displayed to understand the dataset structure



#### 2. Pearson's Correlation Coefficient:

Pearson's Correlation Coefficient (denoted as **r**) measures the **linear** relationship between two continuous variables.

Values range from -1 to +1:

- +1: Perfect positive correlation
- 0: No correlation
- -1: Perfect negative correlation

The formula for Pearson's Correlation Coefficient is:

$$r = rac{\sum (X_i - ar{X})(Y_i - ar{Y})}{\sqrt{\sum (X_i - ar{X})^2 \sum (Y_i - ar{Y})^2}}$$

```
pearson_corr, pearson_p = stats.pearsonr(df['Age'], df['ExperienceInCurrentDomain'])
print(f"Pearson's Correlation Coefficient: {pearson_corr}")
print(f"P-value: {pearson_p}")

Pearson's Correlation Coefficient: -0.13464285083693067
P-value: 2.8637816441811323e-20
```

# 3. Spearman's Rank Correlation

- Spearman's Rank Correlation (denoted as  $\rho$ , rho) measures the monotonic relationship between two variables.
- It does not require normally distributed data.
- If ranks of two variables are related, it indicates correlation.
- The formula is:

$$ho=1-rac{6\sum d_i^2}{n(n^2-1)}$$

```
[13] spearman_corr, spearman_p = stats.spearmanr(df['Age'], df['ExperienceInCurrentDomain'])
    print(f"Spearman's Rank Correlation Coefficient: {spearman_corr}")
    print(f"P-value: {spearman_p}")
```

Spearman's Rank Correlation Coefficient: -0.14172932292026683 P-value: 2.6218815420869774e-22

## 4. Kendall's Rank Correlation

### Theory:

- Kendall's Tau  $(\tau)$  measures the **ordinal association** between two variables.
- It counts concordant and discordant pairs:
  - Concordant pairs: If one variable increases, the other also increases.
  - **Discordant pairs**: One increases while the other decreases.
- The formula is:

$$au = rac{(C-D)}{rac{1}{2}n(n-1)}$$

```
[14] kendall_corr, kendall_p = stats.kendalltau(df['Age'], df['ExperienceInCurrentDomain'])
    print(f"Kendall's Rank Correlation Coefficient: {kendall_corr}")
    print(f"P-value: {kendall_p}")
```

Kendall's Rank Correlation Coefficient: -0.05223701755751474 P-value: 2.2249017210277004e-06

# 5. Chi-Squared Test

- The **Chi-Squared Test** is used for **categorical data** to check if two variables are independent.
- It compares **observed** and **expected** frequencies.
- The formula is:

$$\chi^2 = \sum rac{(O_i - E_i)^2}{E_i}$$

```
df['Experience_Category'] = pd.cut(df['ExperienceInCurrentDomain'], bins=[0, 5, 10, 20, 30], labels=['0-5', '6-10', '11-20', '21-30'])
df['Performance_Category'] = pd.cut(df['Age'], bins=[20, 30, 40, 50, 60], labels=['20-30', '30-40', '40-50', '50-60'])

contingency_table = pd.crosstab(df['Experience_Category'], df['Performance_Category'])

chi2_stat, p_val, dof, expected = stats.chi2_contingency_contingency_table

print(f"Chi-Squared Statistic: {chi2_stat}")
print(f"P-value: {p_val}")
print(f"Pegrees of Freedom: {dof}")
print("Expected Frequencies Table:")
print(expected)

Chi-Squared Statistic: 43.97421499426579
P-value: 2.8256641457475885e-10
Degrees of Freedom: 2
Expected Frequencies Table:
[[3.08375430e+03 1.12254235e+03 7.47033504e+01]
[1.22456957e+01 4.45765472e+00 2.96649604e-01]]
```

## **Conclusion**

- 1. **Pearson's Correlation**: Measures **linear relationship** between numerical variables. If **p < 0.05**, the correlation is significant.
- 2. **Spearman's Correlation**: Checks for **monotonic relationship**. If **p < 0.05**, variables move together in a ranked order.
- 3. **Kendall's Correlation**: Identifies **ordinal association**. A small **p-value** means a strong relationship.
- 4. **Chi-Square Test**: Determines **independence of categorical variables**. If **p < 0.05**, variables are dependent; otherwise, they are independent.

#### **Final Summary:**

- If **p < 0.05**, the test indicates a significant relationship.
- If **p > 0.05**, no strong relationship exists.

These tests help understand **associations** in the dataset for data-driven decisions.