

## Assignment - 2

Find global minimum point and value for function  $f(x, y)$

$$f(x, y) = x^2 + y^2 + 10$$

Do manual calculation for 2 iterations

step 1 :-  $x = 2, y = 3, \eta = 0.01, \text{epochs} = 2$

step 2 :- iter = 1

$$\text{step 3 :- } \frac{\partial f}{\partial x} = 2x \Rightarrow 2(2) = 4$$

$$\frac{\partial f}{\partial y} = 2y = 2(3) = 6$$

$$\text{step 4 :- } \Delta x = -\eta \frac{\partial f}{\partial x} = -0.01 \times 4 \\ = -0.04$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -0.01 \times 6 \\ = -0.06$$

$$\text{step 5 :- } x = x + \Delta x \\ = 2 + 0.04$$

$$x = 1.96$$

$$y = y + \Delta y \\ = 3 - 0.06$$

$$y = 2.94$$

step 6 :- iter = iter + 1 = 2

step 7 :- if (iter > epochs)

$$2 > 2$$

goto next step

else

goto step 2

step 3 :-  $\frac{\partial f}{\partial x} = 2(1.96) = 3.92$

$\frac{\partial f}{\partial y} = 2(2.94) = 5.88$

step 4 :-  $\Delta x = -\eta \frac{\partial f}{\partial x}$

$\Delta y = -\eta \frac{\partial f}{\partial y}$

$\Delta x = -0.01 \times 3.92$   
 $= -0.0392$

$= -0.01 \times 5.88$   
 $= -0.0588$

step 5 :-  $x = x + \Delta x$

$y = y + \Delta y$

$= 1.96 - 0.0392$

$= 2.94 - 0.0588$

$= 1.92$

$y = 2.881$

step 6 :-  $\text{iter} = 2 + 1 = 3$

step 7 :- if (iter > epochs)

$3 > 2$

goto step 8

else

goto step 3

step 8 :- print m, c values

$m = 1.92$

$c = 2.881$