

A slit of width 0.16 mm is illuminated by a light of wavelength 5600 Å. Find the half angular width of the central maximum.

Data \rightarrow

$$a = 0.016 \text{ cm}, \quad \lambda = 5600 \times 10^{-8} \text{ cm}, \quad n = 1$$

Formula \rightarrow

$$a \sin \theta = n \lambda$$

$$a \sin \theta = \lambda$$

(As $n=1$)

$$\sin \theta = \frac{\lambda}{a}$$

$$\theta = \sin^{-1} \left(\frac{\lambda}{a} \right)$$

$$\theta = \sin^{-1} \left(\frac{5600 \times 10^{-8}}{0.016} \right)$$

$$\theta = 12'$$

A slit of variable width is illuminated by red light of $\lambda = 6500 \text{ Å}$. At what width of the slit, the first minimum will fall at $\theta = 30^\circ$?

Data \rightarrow

$$\lambda = 6500 \times 10^{-8} \text{ cm.}$$

$$\theta = 30^\circ$$

$$n = 1$$

Formula \rightarrow

$$a \sin \theta = n \lambda$$

$$a \sin \theta = \lambda$$

$$a = \frac{\lambda}{\sin \theta} = \frac{6500 \times 10^{-8}}{\sin 30}$$

$$a = 0.13 \times 10^{-3} \text{ cm.}$$

A light of wavelength 5×10^{-5} cm is incident normally on the plane transmission grating of width 3 cm and having 15000 lines. Find the angle of diffraction in the first order.

Data \Rightarrow

$$\lambda = 5 \times 10^{-5} \text{ cm}$$

$$(a+b) = \frac{3}{15000}$$

$$n = 1.$$

Formula \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

Solution \Rightarrow

$$\sin \theta = \frac{n\lambda}{(a+b)}$$

$$\theta = \sin^{-1} \left(\frac{\lambda}{a+b} \right) = \sin^{-1} \left(\frac{5 \times 10^{-5}}{3} \times 15000 \right)$$

$$\theta = 14^\circ 29'$$

A parallel beam of sodium light is allowed to be incident normally on a plane grating having 4250 lines per cm and a second order spectral line is observed to be deviated through 30° . Calculate the wavelength of the spectral line.

Data \Rightarrow

$$\theta = 30^\circ$$

$$a+b = \frac{1}{4250}$$

$$n=2$$

Formula \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

Solution \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

$$\text{but } n=2$$

$$(a+b) \sin \theta = 2\lambda$$

$$\lambda = \frac{(a+b) \sin \theta}{2}$$

Substituting

$$\lambda = \frac{1}{4250} \times \frac{1}{2} \times \frac{1}{2}$$

$$\lambda = 5.886 \times 10^{-5} \text{ cm}$$

$$\lambda = 5886 \text{ \AA}$$

A grating has 6000 lines/cm. Find the angular separation of two yellow lines of mercury of wavelengths 5770 \AA and 5791 \AA in the second order.

Data

$$\Rightarrow a+b = \frac{1}{6000} \text{ cm.}$$

$$\lambda_1 = 5770 \times 10^{-8} \text{ cm}$$

$$\lambda_2 = 5791 \times 10^{-8} \text{ cm.}$$

$$n=2$$

Formula \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

solution \Rightarrow

$$(a+b) \sin \theta_n = n\lambda$$

For λ_1

$$(a+b) \sin \theta_2 = n\lambda_1$$

$$\sin \theta_2 = \frac{n\lambda_1}{(a+b)} = \frac{2 \times 5770 \times 10^{-8} \times 6000}{(a+b)}$$

$$\sin \theta_2 = 0.6924$$

$$\theta_2 = 43.82^\circ$$

$$\& \sin \theta_2 = \frac{n\lambda_2}{(a+b)} = \frac{2 \times 5791 \times 10^{-8} \times 6000}{(a+b)} = 0.6949 = 44.02^\circ$$

$$\theta_1 - \theta_2 = 0.2^\circ \text{ or } 12'$$

What is the highest order spectrum that is visible with light of wavelength 6000 \AA by means of a grating having 5000 lines per cm?

Data \Rightarrow

$$\lambda = 6000 \text{ \AA.}$$

$$N = \frac{5000 \text{ lines}}{\text{cm}},$$

$$a+b = \frac{1}{5000} \text{ cm.}$$

Formula \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

Solution \Rightarrow

$$\text{Take, } \sin \theta = 1.$$

$$a+b = n\lambda$$

$$\frac{1}{5000} = n \times 6000 \times 10^{-8}$$

$$n = 3.3$$

The highest order is $n=3$.

Monochromatic light from He-Ne laser source ($\lambda = 6328 \text{ \AA}$) is incident normally on a diffraction grating having 6000 lines/cm. find the angle at which one would observe second order maximum.

Data \Rightarrow

$$\lambda = 623.8 \text{ nm} = 623.8 \times 10^{-7} \text{ cm}.$$

$$N = 6000 \frac{\text{lines}}{\text{cm}}$$

$$(a+b) = \frac{1}{6000} \text{ cm}.$$

Formula

$$\Rightarrow \textcircled{1} (a+b) = \frac{1}{N} \text{ cm}.$$

$$\textcircled{2} (a+b) \sin \theta = n\lambda.$$

Solution \Rightarrow

$$(a+b) \sin \theta = n\lambda$$

$$\text{for } n=1, \quad \theta_1 = \sin^{-1} \left(\frac{1 \times 623.8 \times 10^{-7}}{1.66 \times 10^{-4}} \right) = 22.31^\circ.$$

$$\text{for } n=2, \quad \theta_2 = \sin^{-1} \left(\frac{2 \times 623.8 \times 10^{-7}}{1.66 \times 10^{-4}} \right) = 49.39^\circ.$$

The angular separation of two stars is 1.5 seconds. Find the minimum aperture of a telescope objective, if the two stars are to be distinguished as separate, given $\lambda = 5700 \text{ \AA}$.

Data \Rightarrow

$$\lambda = 5700 \times 10^{-8} \text{ cm.}$$

$$d\theta = 1.5 \text{ second.}$$

$$1.5 \text{ second} = \frac{1.5^\circ}{3600} \times \frac{\pi}{180} \text{ radians.}$$

$$= 0.72 \times 10^{-5} \text{ radians.}$$

Formula \Rightarrow

$$d\theta = 1.22 \frac{\lambda}{d}$$

Solution \Rightarrow

$$d\theta = 1.22 \frac{\lambda}{d}$$

$$\text{aperture, } d = 1.22 \frac{\lambda}{d\theta}$$

$$d = \frac{1.22 \lambda}{d\theta}$$

$$\text{Substituting } d = 1.22 \frac{\lambda}{d\theta}$$

$$d = \frac{1.22 \times 5700 \times 10^{-8}}{0.72 \times 10^{-5}}$$

$$d = 9.65 \text{ cm.}$$

The objective of a telescope has a diameter of 40 inches. Calculate the smallest angular separation of two stars that may be resolved by it. Mean wavelength of light $\lambda = 5600 \text{ \AA}$.

Data \rightarrow

$$x = 40 \text{ inches.} = 40 \times 2.54 \text{ cm.} \\ = 1.016 \text{ m}$$

$$\lambda = 5600 \times 10^{-10} \text{ m.}$$

Formula \rightarrow

$$d\theta = 1.22 \frac{\lambda}{x}$$

Solution \rightarrow

$$d\theta = 1.22 \frac{\lambda}{x}$$

$$= \frac{1.22 \times 5600 \times 10^{-10}}{1.016}$$

$$d\theta = 6.724 \times 10^{-7} \text{ radians.}$$

$d\theta$ is the smallest Angular separation between the stars. Can be resolved by the telescope.



