## **Tutorial 5 sample answer**

Note that due to the nature of programming, there are multiple ways to write the functions. Any way of writing is fine as long as desired output is achieved.

```
Command/code:
        vector mean <- function(x) {</pre>
             n = length(x)
             output = sum(x)/n
             return(output)
        }
      Example output:
        > vector mean(c(1,2,3))
        [1] 2
        > mean(c(1,2,3))
        [1] 2
      Comment:
      The function length () gives the length of x (how many elements in x). Then to
      calculate the mean, just take the sum of x using sum(x) and divide by size of x.
2
      Command/code:
        multiple <- function(a,b) {</pre>
             remainder <- a %% b
             if(remainder == 0){
                  output=TRUE
             if(remainder != 0){
                  output=FALSE
             }
             return(output)
        }
      Example output:
        > multiple(3,2)
        [1] FALSE
        > multiple(3,3)
        [1] TRUE
        > multiple(27,5)
        [1] FALSE
        > multiple(27,9)
        [1] TRUE
      Comment:
      The important part here is to use the if statements. The code can also use if else
      statement.
```

```
3
     Command/code:
        square root <- function(x){</pre>
             if(!is.numeric(x) \mid x<0){
                  solution <- NA
                  error <- TRUE
             } else {
                  solution <- sqrt(x)</pre>
                  error <- FALSE
             return(list(solution=solution, error=error))
        }
     Example output:
        > square root("A")
        $solution
        [1] NA
        $error
        [1] TRUE
        > square root(9)
        $solution
        [1] 3
        $error
        [1] FALSE
        > square root(-9)
        $solution
        [1] NA
        $error
        [1] TRUE
     Comment:
     The function is.numeric() is used to check whether x is numerical or not.
     Since multiple outputs are required from the function, the list() is used.
4
     Command/code:
        i <- 0
        product <- 1</pre>
        while(product < 10000000) {</pre>
             i <- i+1
             product <- product*i</pre>
        print(i)
     Output:
        > print(i)
        [1] 11
```

### Comment:

In the code above, we initialize i as 0, and product as 1. Then at each loop, we add 1 to i, and multiply product by i, until the product is greater than or equal to 10 million.

# 5 Command/code:

```
Fibonacci <- function(n) {
  output <- rep(1,n)
  if(n > 2){
    for(i in 3:n) {
      output[i] <- output[i-1] + output[i-2]</pre>
    }
  return (output)
#OR
Fibonacci <- function(n) {
    if(n == 1) {
        output <- 1
    } else if(n==2){
        output < c(1,1)
    } else{
        output <- c(1,1)
         for(i in 3:n) {
             Fn <- output[i-1]+output[i-2]</pre>
             output <- c(output,Fn)</pre>
    return (output)
}
#OR
Fibonacci <- function(n) {
    output <- rep(0,n)
    for(i in 1:n) {
        if(i==1){
             output[i]=1
         } else if(i==2){
             output[i]=1
         } else{
             output[i]=output[i-1]+output[i-2]
    return (output)
}
```

# Example output:

```
> Fibonacci(1)
[1] 1
> Fibonacci(2)
[1] 1 1
> Fibonacci(3)
[1] 1 1 2
> Fibonacci(5)
[1] 1 1 2 3 5
```

#### Comment:

In the first example, we initialize output to be a vector of 1s with length n. Then for the 3rd term and above, we set the term according to the Fibonacci formula.

In the second example, we will set output to be 1 if n = 1, or c(1,1) if n = 2. For  $n \ge 3$ , we will have to calculate using the equation for Fibonacci number. The line c (output, Fn) will combine the vector of output, with the new Fibonacci number Fn.

In the third example, we initialize output by a vector of 0's with length n using rep (0, n). Another alternative is to use output <- vector ("numeric", n).

#### 6 Command/code:

```
summation <- 0
for(i in 1:10){
    die_value <- sample(1:6,1)
       summation <- summation + die_value
}
print(summation)</pre>
```

# Output:

```
> print(summation)
[1] 41
```

#### Comment:

In the code, we initialize summation to be 0, and at each loop, we add the die value to the summation. Due to randomness, the output may differ if you try it yourself.

```
Command/function:
  quadratic <- function(a, b, c){
      disc <- b^2 - 4*a*c
      if(disc==0){
           x < -b/(2*a)
          number solution <- 1</pre>
      } else if(disc>0){
          x1 <- (-b-sqrt(disc))/(2*a)
          x2 <- (-b+sqrt(disc))/(2*a)
           x < -c(x1, x2)
          number solution <- 2
       } else{
           x < - NA
           number solution <- 0
      return(list(solution = x, number of solution =
              number solution))
  }
Example output:
  > quadratic(1,0,-9)
  $solution
  [1] -3 3
  $number of solution
  [1] 2
  > quadratic(1,-6,9)
  $solution
  [1] 3
  $number of solution
  [1] 1
  > quadratic(1,0,9)
  $solution
  [1] NA
  $number of solution
  [1] 0
```

#### Comment:

Many students do not return a list from the function, but instead print out hte message of the solution and number of solutions. This is not fully correct.

The reason why we do not want to just print out the solution and number of solutions is because sometimes, the output from the function may be used in the next line of code. Only printing results will not allow us for this.

To return multiple output, use the list environment, as shown in the example.

## 8 Command/codes:

```
price <- 1
day <- 0
while(price < 1.5 & price > 0.75){
    price <- price + sample(c(-0.05,0,0.05),1)
    day <- day+1
}
print(day)</pre>
```

# Example output:

```
> print(day) [1] 42
```

## Comment:

Some students set a limit for the number of days it simulates. For example, some may use "for(i in 1:1000)". For large enough upper limit, the function may work fine. But it is better to use the while loop instead.

Some made the wrong condition in the while loop. E.g. "while(price  $\leq 1.5$  & price  $\geq 0.75$ )" is incorrect because it will run the code even when price is 1.5 or 0.75.

Using break when price is 1.5 or 0.75, as done by some students can mitigate these errors.