3. NUMERICAL DESCRIPTIVE MEASURES

Mean, median, mode, variance, IQR, etc

Objective



- In chapter 2, we have organized our data, and visually inspect them using various graphs and plots.
- In this chapter, we would like to describe or summarize the data numerically.
- We will only cover ungrouped data, as it is more common and relevant for this course.



Measures of center (ungrouped data)

Mean, median, mode

Measures of center



- Measure of center a value that represents a typical, or central, entry of a data set.
- Most common measures of central tendency:
 - Mean
 - Median
 - Mode

Mean



The sum of all the data entries divided by the number of entries.

Mean =
$$\frac{\text{Sum of all values}}{\text{Number of values}}$$

$$\frac{3 = 1, 2, 3}{2 = 1 + 2 + 3}$$

$$\frac{3 = 1, 2, 3}{2 + 2 + 3}$$

- \square Sigma notation: $\Sigma x = \mathsf{add}$ all of the data entries (x) in the data set.
- \square Suppose N is the population size, and n is the sample size.
- Population mean:

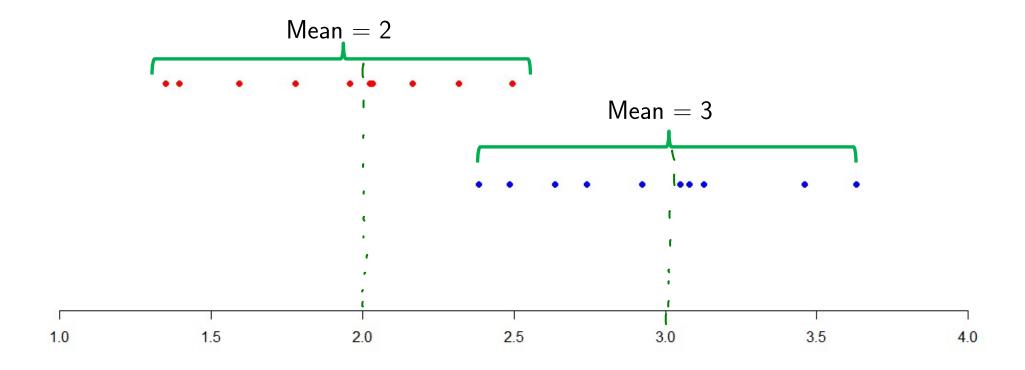
$$\mu = \frac{\sum x}{N}$$

Sample mean:

$$\bar{x} = \frac{\sum x}{n}$$

Mean









EXAMPLE 3-1 2014 Profits of 10 U.S. Companies

Table 3.1 lists the total profits (in million dollars) of 10 U.S. companies for the year 2014 (www. fortune.com).

Table 3.1 2014 Profits of 10 U.S. Companies		
Company	Profits (million of dollars)	
Apple	37,037	
AT&T	18,249	
Bank of America	11,431	
Exxon Mobil	32,580	
General Motors	5346	
General Electric	13,057	
Hewlett-Packard	5113	
Home Depot	5385	
IBM	16,483	
Wal-Mart	16,022	

Find the mean of the 2014 profits for these 10 companies.

Example – finding mean



- \square Sample size: n = 10
- \square Denote the variable Profits as x
- Sum of all profits:

$$\sum x = 37,037 + 18,249 + 11,431 + 32,580 + 5346$$

+13,057 + 5113 + 5385 + 16,483 + 16,022
= 160,703

Sample mean:

$$\bar{x} = \frac{\sum x}{n} = \frac{160,703}{10} = 16070.3$$

□ The mean profits is \$16070.3 million.





EXAMPLE 3–2 Ages of Employees of a Company

The following are the ages (in years) of all eight employees of a small company:

Find the mean age of these employees.

* population

Example – finding mean



- \square Population size, N=8
- Sum of all ages:

$$\sum x = 53 + 32 + 61 + 27 + 39 + 44 + 49 + 57 = 362$$

Population mean:

$$\mu = \frac{\sum x}{N} = \frac{362}{8} = 45.25$$

□ Mean age of all eight employees of the company is 45.25 years.

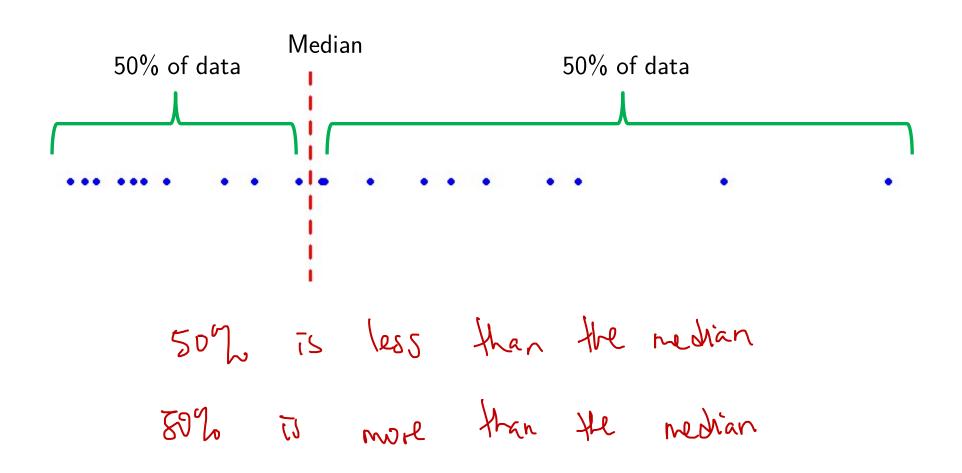
Median



- The value that lies in the middle of the data when the data set is ordered.
- Calculation:
 - 1. Rank the given data set in increasing order.
 - 2. Find the value that divides the ranked data in two equal size parts.
- If the data set has an
 - odd number of entries: median is the middle data entry.
 - even number of entries: median is the mean of the two middle data entries.

Median









EXAMPLE 3-4 Compensations of Female CEOs

Table 3.2 lists the 2014 compensations of female CEOs of 11 American companies (*USA TODAY*, May 1, 2015). (The compensation of Carol Meyrowitz of TJX is for the fiscal year ending in January 2015.)

Table 3.2 Compensations of 11 Female CEOs		
Company & CEO	2014 Compensation (millions of dollars)	
General Dynamics, Phebe Novakovic	19.3	
GM, Mary Barra	16.2	
Hewlett-Packard, Meg Whitman	19.6	
IBM, Virginia Rometty	19.3	
Lockheed Martin, Marillyn Hewson	33.7	
Mondelez, Irene Rosenfeld	21.0	
PepsiCo, Indra Nooyi	22.5	
Sempra, Debra Reed	16.9	
TJX, Carol Meyrowitz	28.7	
Yahoo, Marissa Mayer	42.1	
Xerox, Ursula Burns	22.2	

Find the median for these data.

Example – finding median



Ranked data in increasing order:

Find the middle value:

 \square Median = \$21.0 million





EXAMPLE 3-5 Cell Phone Minutes Used

The following data give the cell phone minutes used last month by 12 randomly selected persons.

230 2053 160 397 510 380 263 3864 184 201 326 721

Find the median for these data.

Example – finding median



Ranked data in increasing order:

□ Find the middle value:

Calculate median:

$$Median = \frac{326 + 380}{2} = 353$$

Median is 353 minutes.

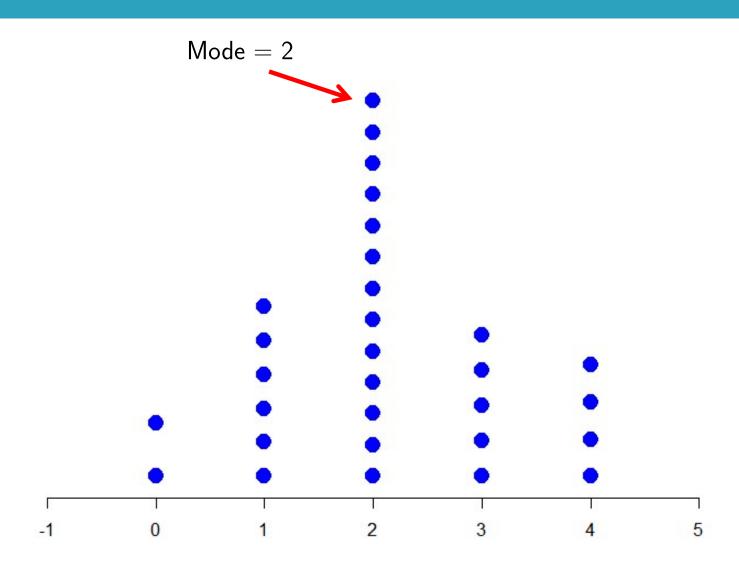
Mode



- □ The data entry that occurs with the highest frequency.
- □ If no entry is repeated the data set has no mode.
- □ If two entries occur with the same greatest frequency, each entry is a mode (bimodal).

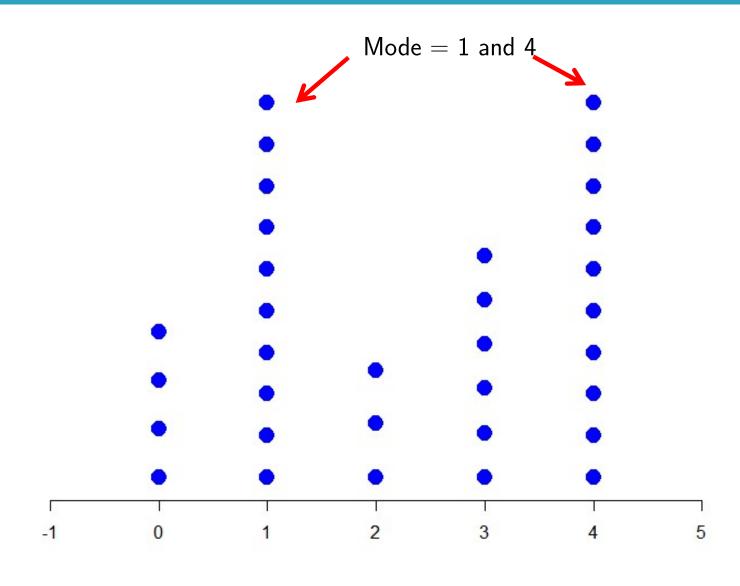
Mode





Mode









EXAMPLE 3–6 Speeds of Cars

The following data give the speeds (in miles per hour) of eight cars that were stopped on I-95 for speeding violations.

77 82 (74) 81 79 84 (74) 78

Find the mode.

- Only 74 occurs twice, while the other values occur only once.
- □ Therefore, Mode = 74.





EXAMPLE 3-7 Incomes of Families

Last year's incomes of five randomly selected families were \$76,150, \$95,750, \$124,985, \$87,490, and \$53,740. Find the mode.

- All values occur once.
- There is no mode in the data.

Example – finding mode



EXAMPLE 3–8 Commuting Times of Employees

A small company has 12 employees. Their commuting times (rounded to the nearest minute) from home to work are 23, 36, 14, 23, 47, 32, 8, 14, 26, 31, 18, and 28, respectively. Find the mode for these data.

- 14 and 23 occur twice in the data, while the other values occur once.
- □ This data has two modes: 14 and 23

Example – finding mode



EXAMPLE 3–10 Status of Students

The status of five students who are members of the student senate at a college are senior, sophomore, senior, junior, and senior, respectively. Find the mode.

- Senior occurs 3 times, whereas sophomore and junior occur once.
- Senior is the mode for this data set.
- Since this is a qualitative variable, we cannot calculate the mean and median.

Exercise



3.18 The following table gives the number of major penalties for each of the 15 teams in the Eastern Conference of the National Hockey League during the 2008–09 season (*NHL*, 2009). A major penalty is subject to 5 minutes in the penalty box for a player.

Team	Number of Major Penalties	+ population
Philadelphia	65 7	•
Columbus	59 \ ¬	- entires
Boston	53	entile)
Pittsburgh	51	
New York Rangers	50	
Tampa Bay	40	
Nashville	39 J	
Florida	38	
Ottawa	$\sqrt{35}$	
Washington	35	
Montreal	34	entries
Atlanta	31 \ +	en i les
New York Islanders	29	
Buffalo	26	
Toronto	25	

Compute the mean and median for the data on major penalties. Do these data have a mode? Why or why not?

median = 38

mode = 35, because it occurs twice whereas the other values occur once.

Exercise



*sample

3.23 The following data represent the numbers of tornadoes that touched down during 1950 to 1994 in the 12 states that had the most tornadoes during this period (*Storm Prediction Center*, 2009). The data for these states are given in the following order: CO, FL, IA, IL, KS, LA, MO, MS, NE, OK, SD, TX.

1113 2009 1374 1137 2110 1086 1166 1039 1673 2300 1139 5490

- a. Calculate the mean and median for these data.
- **b.** Identify the outlier in this data set. Drop the outlier and recalculate the mean and median. Which of these two summary measures changes by a larger amount when you drop the outlier?
- c. Which is the better summary measure for these data, the mean or the median? Explain.

a)
$$\leq n = 1113 + 2009 + \cdots + 5490 = 21636$$
, $n = 12$

Nearly $\pi = \frac{\leq n}{n} = \frac{21636}{12} = 1803$

Ranked data: 1080 1086 143 437 1439 1166 1

1374 1473 2020 240 2300 5490

Nedlan = $\frac{1166 + 1374}{166 + 1374} = 1270$ outlier

b) 5490 is an outlier because the value is much larger compared to the others

 $Nean = \frac{2x}{n} = \frac{16146}{11} = 1467.92$

me dian = 1166

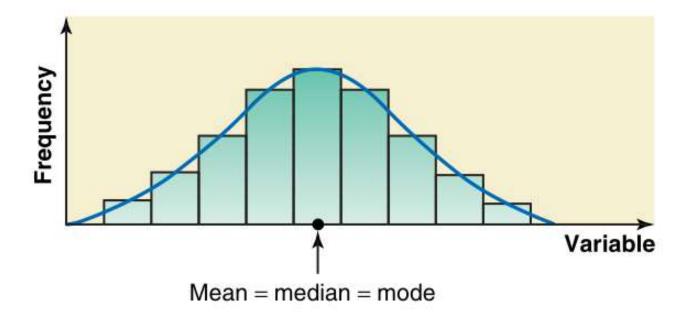
Mean changes by a larger amount when the outlier is dropped.

c) The dran is better compared to the mean because the data contains an outlier.

Relationships Between Mean, Median, and Mode



- Knowing the mean, median and, mode can give us some idea about the shape of a frequency distribution curve.
- \square Symmetric: Mean = median = mode

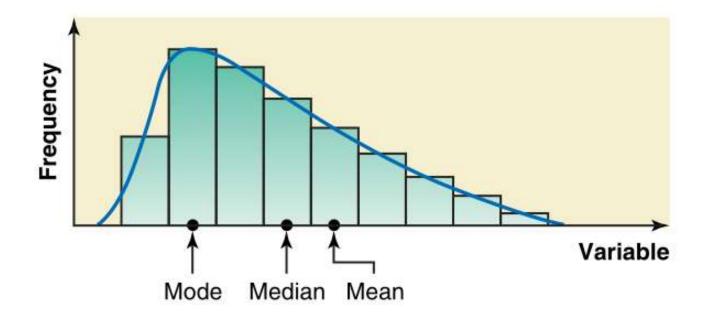


Relationships Between Mean, Median, and Mode



Skewed to the right (or positively skewed):

Mode < median < mean

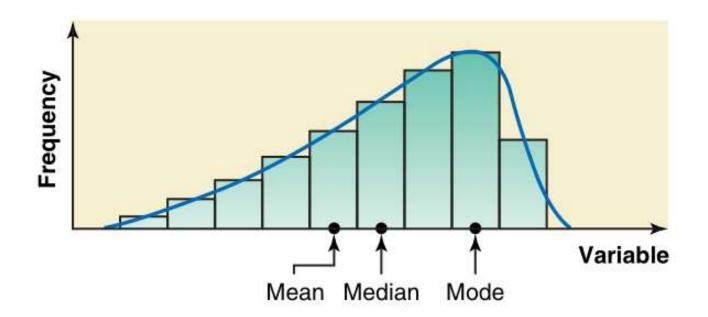


Relationships Between Mean, Median, and Mode



Skewed to the left (or negatively skewed):

Mean < median < mode





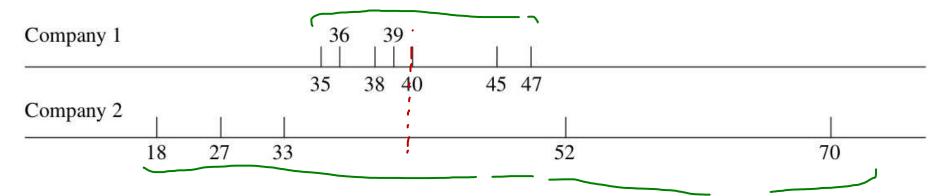
Measures of dispersion (ungrouped data)

Range, variance, standard deviation

Measures of dispersion



- The measures of center, such as the mean, median, and mode, do not reveal the whole picture of the distribution of a data set.
- □ Eg: Company 1: 47 38 35 40 36 45 39 Company 2: 70 33 18 52 27



- Same mean (40) for both companies.
- But company 2 has larger variation.

Range



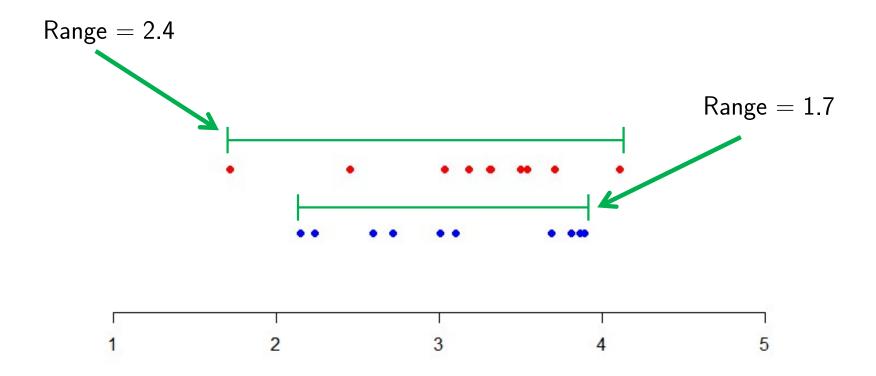
The difference between the largest and smallest data entries in the set.

Range = Largest value - Smallest value

- □ The larger the range, the more spread the data is.
- If data contains outlier, range is not suitable for measuring dispersion.

Range









EXAMPLE 3-13 Total Areas of Four States

Table 3.4 gives the total areas in square miles of the four western South-Central states of the United States.

Table 3.4		
State	Total Area (square miles)	
Arkansas	53,182	
Louisiana	49,651	
Oklahoma	69,903	
Texas	267,277	

Find the range for this data set.

- □ Largest value = 267,277
- □ Smallest value = 49,651
- \square Range = 267,277 49,651 = 217,626

Variance and standard deviation



- Standard deviation is the most used measure of dispersion.
- □ The value tells how closely the observations are to the mean.
- Standard deviation is the square root of variance
- Population variance and population standard deviation:

$$\sigma^2 = \frac{\sum (x - \mu)^2}{N}, \qquad \sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}$$

Sample variance and sample standard deviation:

$$s^{2} = \frac{\sum (x - \bar{x})^{2}}{n - 1}, \qquad s = \sqrt{\frac{\sum (x - \bar{x})^{2}}{n - 1}}$$

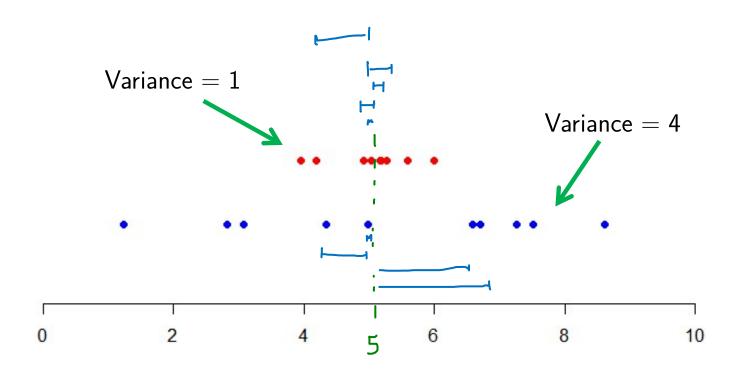
Variance and standard deviation



- □ If observations are close to the mean, then $x \mu$ or $x \bar{x}$ is small in magnitude.
- This leads to small variance and standard deviation.
- The higher the variance or standard deviation, the more spread the observations are.

Variance and standard deviation





 \square Mean = 5 for both data

Alternative formulas



Alternative formulas for population variance and population standard deviation:

$$\sigma^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{N}}{N}, \qquad \sigma = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{N}}{N}}$$

Alternative formulas for sample variance and sample standard deviation:

$$s^{2} = \frac{\sum x^{2} - \frac{(\sum x)^{2}}{n}}{n-1}, \qquad s = \sqrt{\frac{\sum x^{2} - \frac{(\sum x)^{2}}{n}}{n-1}}$$

Important note



- $\square \sum x^2$ is not the same as $(\sum x)^2$
- □ For example, let's say the observations are 1, 2, and 3.

$$\sum x^2 = 1^2 + 2^2 + 3^2 = 1 + 4 + 9 = 14$$

$$(\sum x)^2 = (1+2+3)^2 = 6^2 = 36$$

Example – finding variance and standard deviation



* sangle

EXAMPLE 3–14 Compensations of Female CEOs

Refer to the 2014 compensations of 11 female CEOs of American companies given in Example 3–4. The table from that example is reproduced below.

Company & CEO	2014 Compensation (millions of dollars)
General Dynamics, Phebe Novakovic	19.3
GM, Mary Barra	16.2
Hewlett-Packard, Meg Whitman	19.6
IBM, Virginia Rometty	19.3
Lockheed Martin, Marillyn Hewson	33.7
Mondelez, Irene Rosenfeld	21.0
PepsiCo, Indra Nooyi	22.5
Sempra, Debra Reed	16.9
TJX, Carol Meyrowitz	28.7
Yahoo, Marissa Mayer	42.1
Xerox, Ursula Burns	22.2

Find the variance and standard deviation for these data.

Example – finding variance and standard deviation



x	x^2
19.3	372.49
16.2	262.44
19.6	384.16
19.3	372.49
33.7	1135.69
21.0	441
22.5	506.25
16.9	285.61
28.7	823.69
42.1	1772.41
22.2	492.84
$\sum x = 261.5$	$\sum x^2 = 6849.07$

$$n = 11$$

$$s^{2} = \frac{\sum x^{2} - \frac{(\sum x)^{2}}{n}}{n - 1}$$

$$= \frac{6849.07 - \frac{(261.5)^{2}}{11}}{11 - 1}$$

$$= 63.250$$

$$s = \sqrt{63.25} = 7.953$$

- □ The table on the left is not necessary.
- You can simply calculate using calculator $\sum x = 19.3 + 16.2 + \dots + 22.2 = 261.5$ $\sum x^2 = 19.3^2 + 16.2^2 + \dots + 22.2^2 = 6849.07$
- Then apply the formula.

Exercise



3.32 The following data set belongs to a population:

-7 2 0 -9 16

Calculate the range, variance, and standard deviation.

largest = 16
smallest = -9
range = 1b - (-9)
= 25

$$N = 8$$

 $\leq a = 5 + (-7) + 2 + \cdots + 7$
= 24

10

Exercise



ksamore dita 3.47 The following data give the numbers of pieces of junk mail received by 10 families during the past month.

19

41

33

28

21

29

14

Find the range, variance, and standard deviation.

$$n = 10$$

$$S^{2} = \Xi n^{2} - \frac{(\Xi n)^{2}}{N}$$

$$= \frac{201^{2}}{10}$$



Use of standard deviation

Chebyshev's Theorem, empirical rule

Chebyshev's Theorem



By using the mean and standard deviation, we can approximate the total observations that fall within a given interval.

□ Chebyshev's Theorem:

- For any number k greater than 1, at least $100 \left(1 \frac{1}{k^2}\right) \%$ of the data values lie within k standard deviations of the mean.
- $lue{}$ It gives a lower bound of how much data is between the k standard deviations of the mean

Chebyshev's Theorem



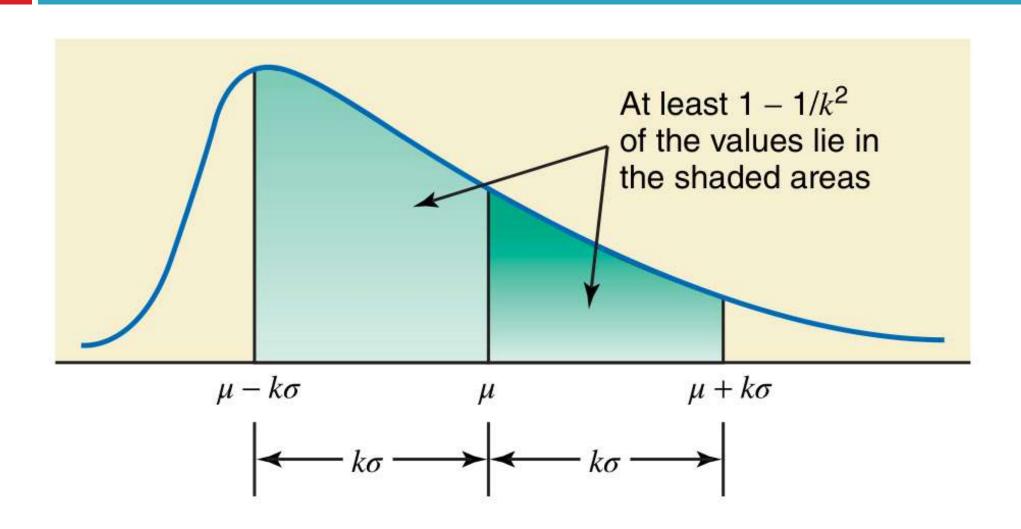




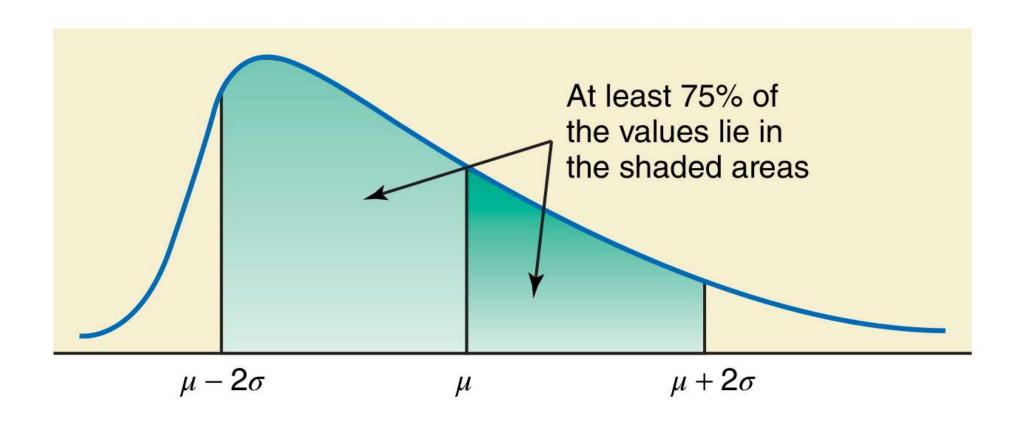


Table 3.14 Areas Under the Distribution Curve Using Chebyshev's Theorem

k	Interval	$1-\frac{1}{k^2}$	Minimum Area Within k Standard Deviations
1.5	$\mu \pm 1.5\sigma$	$1 - \frac{1}{1.5^2} = 144 = .56$	56%
2.0	$\mu \pm 2\sigma$	$1 - \frac{1}{2^2} = 125 = .75$	75%
2.5	$\mu \pm 2.5\sigma$	$1 - \frac{1}{2.5^2} = 116 = .84$	84%
3.0	$\mu \pm 3\sigma$	$1 - \frac{1}{3.0^2} = 111 = .89$	89%

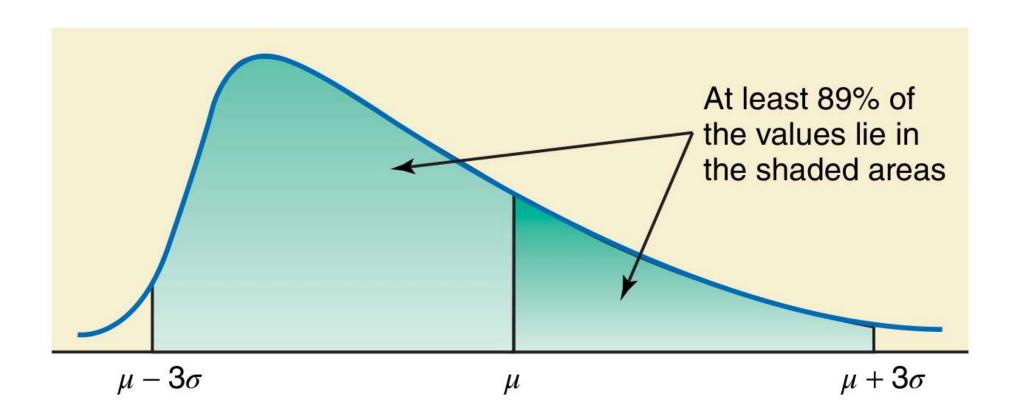












Example – Chebyshev's Theorem



EXAMPLE 3–21 Blood Pressure of Women

The average systolic blood pressure for 4000 women who were screened for high blood pressure was found to be 187 mm Hg with a standard deviation of 22. Using Chebyshev's theorem, find the minimum percentage of women in this group who have a systolic blood pressure between 143 and 231 mm Hg.

Example – Chebyshev's Theorem



$$\mu = 187, \, \sigma = 22$$

$$143 \qquad \mu = 187 \qquad 233$$

 \square Determine k:

$$\mu - k\sigma = 143$$
 $187 - k\sigma = 143$
 $k\sigma = 187 - 143 = 44$
 $k = \frac{44}{22} = 2$

Chebyshev's Theorem:

■ At least
$$100 \left(1 - \frac{1}{k^2}\right) = 100 \left(1 - \frac{1}{4}\right) = 75\%$$
 of data is between 143 mm Hg and 231 mm Hg.

Empirical rule



- The Chebyshev's Theorem applies to all distribution.
- But if the distribution has a bell shape, we can approximate the proportion of data better.
- □ Empirical rule for a bell-shaped distribution:
 - 68% of observations lie within 1 standard deviation of the mean.
 - 95% of observations lie within 2 standard deviation of the mean.
 - 99.7% of observations lie within 3 standard deviation of the mean.



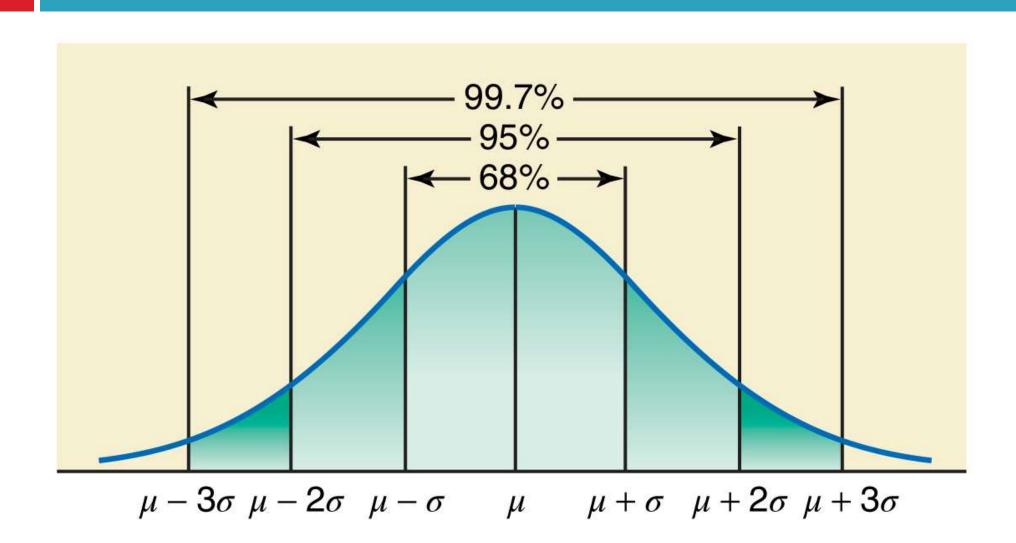


Table 3.15 Approximate Areas under a Bell-Shaped Distribution Using the Empirical Rule

Interval	Approximate Area	
$\mu \pm 1 \sigma$	68%	
$\mu \pm 2 \sigma$	95%	
$\mu \pm 3 \sigma$	99.7%	

Empirical rule









EXAMPLE 3–22 Age Distribution of Persons

The age distribution of a sample of 5000 persons is bell-shaped with a mean of 40 years and a standard deviation of 12 years. Determine the approximate percentage of people who are 16 to 64 years old.

$$\bar{x} = 40, s = 12$$

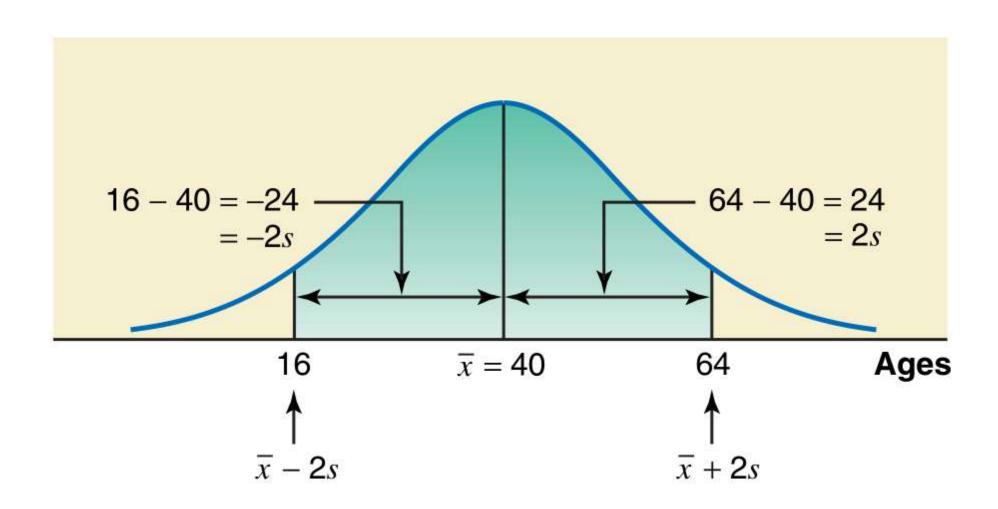
 \square Determine k:

$$\bar{x} - ks = 16$$
 $40 - 12k = 16$
 $k = \frac{24}{12} = 2$

- Empirical rule:
 - Approximately 95% of the people in the sample is between 16 to 64 years old.







Exercise



- **3.81** The mean monthly mortgage paid by all home owners in a town is \$2365 with a standard deviation of \$340.
 - a. Using Chebyshev's theorem, find at least what percentage of all home owners in this town pay a monthly mortgage of
 - i. \$1685 to \$3045

- ii. \$1345 to \$3385
- *b. Using Chebyshev's theorem, find the interval that contains the monthly mortgage payments of at least 84% of all home owners.

(A) i)
$$M = 2365$$
 $T = 340$
 $M - k = 1685$
 $2365 - k(340) = 1685$
 $2365 - 645 = 340k$
 $340k = 680$
 $k = 2$

$$100 \left(1 - \frac{1}{2^2} \right) = 100 \left(1 - \frac{1}{2^2} \right)$$

$$= 757$$

At least 75% of home owners pay a monthly mortgral between \$1685 to \$3045

ii)
$$M+k\sigma = 3385$$

$$2365 + k(340) = 3385$$

$$340k = 1020$$

$$k = 3$$

$$100(1-\frac{1}{k^2}) = 100(1-\frac{1}{3^2})$$

$$= 88.8976$$
At least 88.8976 of home owner page a

home owners per a monthly mortgage between \$ 1845 to \$ 3335

b)
$$100(1-\frac{1}{12}) = 84$$
 $1-\frac{1}{12} = 0.84$
 $\frac{1}{12} = (-0.84 = 0.16)$
 $1-\frac{1}{12} = (-0.84$

= 3215

The interval v betreen 23215

Exercise



- 3.84 The prices of all college textbooks follow a bell-shaped distribution with a mean of \$105 and a standard deviation of \$20.
 - a. Using the empirical rule, find the percentage of all college textbooks with their prices between
 - i. \$85 and \$125

- ii. \$65 and \$145
- *b. Using the empirical rule, find the interval that contains the prices of 99.7% of college textbooks.

$$4 = 105$$

 $4 = 20$
 $4 + 4 = 125$
 $105 + 200 = 125$
 $2 = 1$
Approximately 6920 13
between \$185 + \$125

b) to get 99-72 in the interval, k=3

M-kt = (05 - 3(20) = 45

M+kd = 105 + 3(20) = 165

The interval is between \$45 to \$165



Measures of position

Quartiles, interquartile range, percentiles

Measures of position

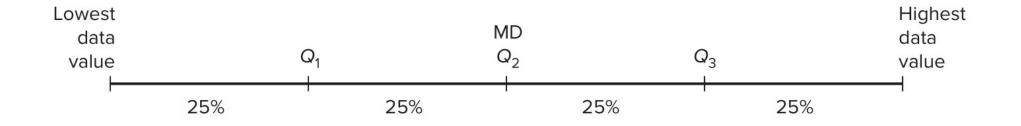


- Determines the position of a single value in relation to other values in a sample or a population data set.
- We will cover quartiles, percentiles, and deciles here. These are known as quantiles.

Quartile



- Quartiles divide the distribution into four equal groups.
- The boundaries for the groups are denoted by Q_1 (first quartile), Q_2 (second quartile), Q_3 (third quartile).



- □ Eg: Approximately 75% of values in a ranked data set are more than Q_1 .
- \square Note that the median is equal to \mathbb{Q}_2 .

Quartile



- \square Finding Q_1 , Q_2 , and Q_3 :
 - Rank the data in increasing order.
 - \blacksquare Find the median (Q_2) .
 - \square For values that are less than the median, find the point that divides the values equally (Q_1) .
 - \blacksquare For values that are greater than the median, find the point that divides the values equally (Q_3) .
- □ Interquartile range (IQR):
 - Is the difference between the third quartile and the first quartile.
 - $\square IQR = Q_3 Q_1$

Example – quartile



EXAMPLE 3–23 Commuting Times for College Students

A sample of 12 commuter students was selected from a college. The following data give the typical one-way commuting times (in minutes) from home to college for these 12 students.

- 29 14 39 17 7 47 63 37 42 18 24 55
- (a) Find the values of the three quartiles.
- **(b)** Where does the commuting time of 47 fall in relation to the three quartiles?
- (c) Find the interquartile range.

Example – quartile



□ Find median:

■ Ranked data: 17, 14, 17, 18, 24, 29, 37, 39, 42, 47, 55, 63

$$Q_2 = \frac{29 + 37}{2} = 33$$

 \Box Find Q_1 :

■ Data less than Q_2 : 7, 1, 1, 17, 18, 2, 2

$$Q_1 = \frac{17+18}{2} = 17.5$$

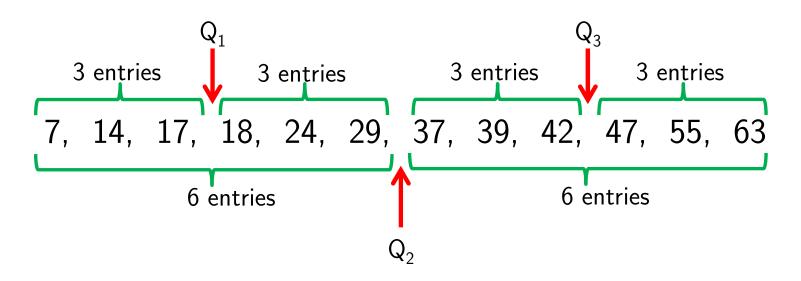
 \Box Find Q_3 :

■ Data more than Q_2 : 3/7, 3/9, 42, 4/7, 5/5, 6/3

$$Q_3 = \frac{42+47}{2} = 44.5$$

Example – quartile





- 47 minutes is in the top 25%.
- \square IQR = Q₃ Q₁ = 44.5 17.5 = 27 minutes.
- Interpretation:
 - \mathbb{Q}_1 : 25% of the students takes less than 17.5 minutes commuting time.

Exercise



The following data give the speeds of 13 cars (in mph) measured by radar, traveling on I-84.

a. Find the values of the three quartiles and the interquartile range.

$$Q_{1} = 73$$

$$Q_{1} = 61+69$$

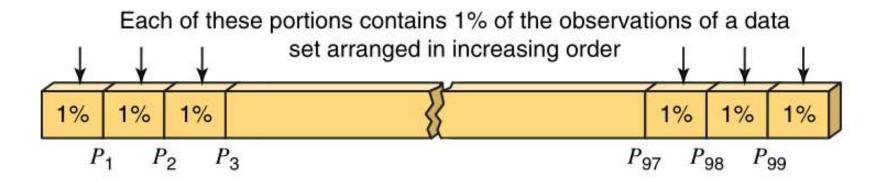
$$Q_{1} = 61+23 = 76-5$$

$$Q_{2} = 76+23 = 76-5$$

Percentiles



Percentiles divide a ranked data set into 100 equal parts.

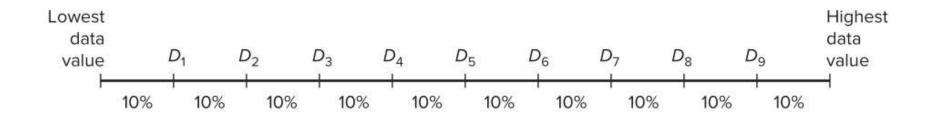


- □ The kth percentile is denoted by P_k , where k is an integer in the range 1 to 99.
- □ About k% of the measurements are smaller than P_k , and about (100 k)% of the measurements are greater than P_k .

Deciles



Deciles divide a ranked data set into 10 equal parts.



- □ The kth decile is denoted by D_k , where k is an integer in the range 1 to 9.
- \square Note that $D_1 = P_{10}$, $D_5 = Q_2 = P_{50}$, etc.



Box-and-whisker plot

Box-and-whisker plot



- Box-and-whisker plot (also called box plot or boxplot) gives a graphic presentation of data using five measures:
 - Median
 - \blacksquare First quartile, Q_1
 - \blacksquare Third quartile, Q_3
 - The smallest values in the data set between the lower and the upper inner fences.
 - The largest values in the data set between the lower and the upper inner fences.

Box-and-whisker plot



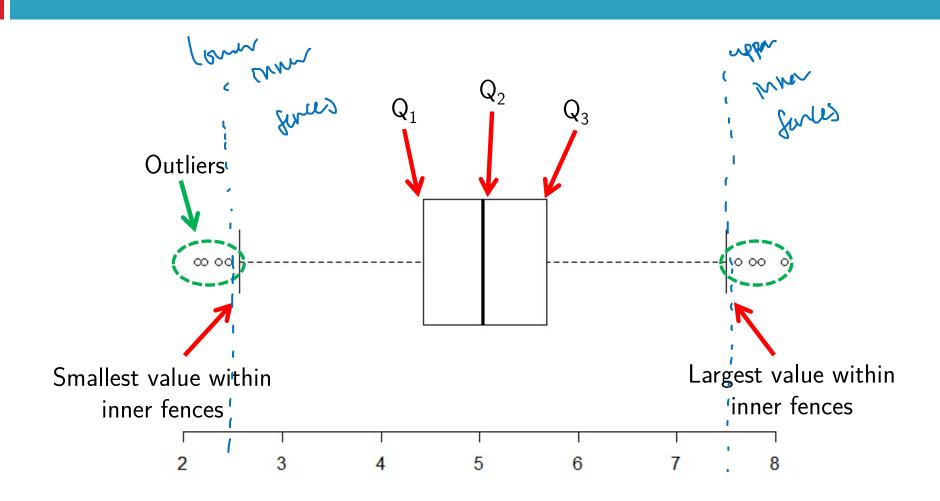
- Inner fences:
 - Lower inner fence = $Q_1 1.5 \times IQR$
 - Upper inner fence = $Q_3 + 1.5 \times IQR$

□ Outlier:

- Extreme observations, either too high or too low.
- Using box plot, any observations outside the inner fences are considered outlier.







Box-and-whisker plot



Steps:

- \blacksquare Find the values of median, Q_1 , and Q_3 .
- Calculate the lower and upper inner fences.
- Determine the smallest and largest value within the lower and upper inner fences.
- Draw a horizontal axis and place the scale on the axis.
- \square Draw a box whose vertical sides go through Q_1 to Q_3 .
- Draw a vertical line through the median.
- Draw a line from the smallest value within the fences to the left side of the box.
- Draw a line from the largest value within the fences to the right side of the box.

Box-and-whisker plot and skewness



- Symmetric:
 - The median is at the center of the box
 - The left and right whiskers have the same length
- Skewed to the right:
 - The median is at the left of the center the box
 - The right whiskers is longer compared to the left whisker
- Skewed to the left:
 - The median is at the right of the center the box
 - The left whiskers is longer compared to the right whisker







Example – box plot



EXAMPLE 3-27 Incomes of Households

The following data are the incomes (in thousands of dollars) for a sample of 12 households.

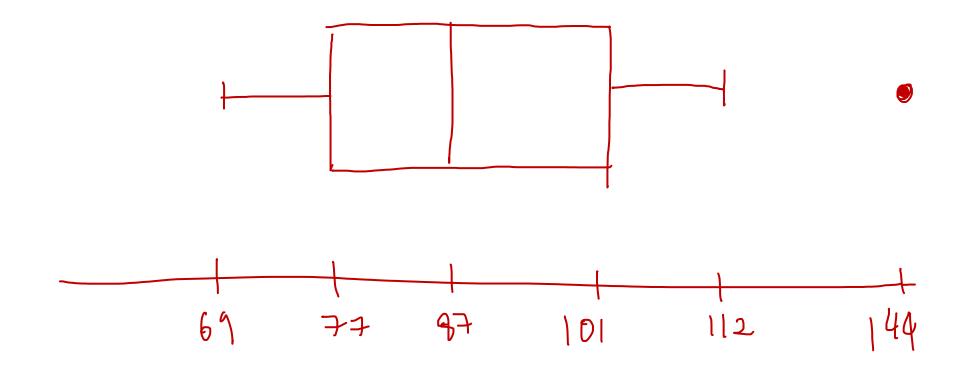
75 69 84 112 74 104 81 90 94 144 79 98

Construct a box-and-whisker plot for these data.

Ranked data:
$$Q_1$$
 Q_2 Q_3 Q_4 , Q_5 , Q_5 , Q_5 , Q_6 , Q_7 , Q_8

lover inver fence = $Q_1 - 1.5 \times 10R = 74 - 1.5(24) = 41$ upper inner fence = $Q_3 + 1.5 \times 10R = 101 + 1.5(24) = 137$

smallest within inner fences = 69 largest u = 112





Exploratory data analysis (EDA)

Exploratory data analysis (EDA)



- Exploratory data analysis (EDA) is a process to analyze and summarize data using their main characteristics and data visualization methods.
- It is often done early during the analysis, before further analysis is performed.
- □ It can help detecting
 - Outliers and errors
 - Relationship between variables
 - Patterns and trend
- □ The methods on graphing data which we covered in previous topic and the numerical measures covered in this topic can be used for EDA.

Example – EDA



EXAMPLE 3–38 Speeds of Roller Coasters

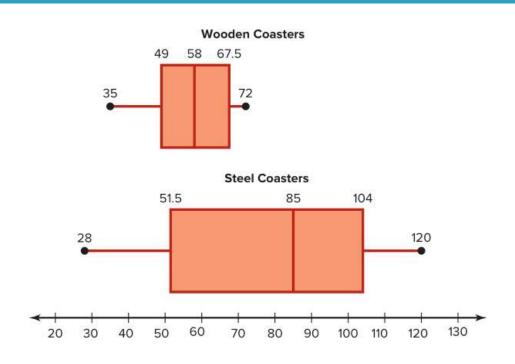
The data shown are the speeds in miles per hour of a sample of wooden roller coasters and a sample of steel roller coasters. Compare the distributions by using boxplots.

Wood				Steel			
50	56	60	48	55	70	48	28
35	67	72	68	100	106	102	120

Source: UltimateRollerCoaster.com

Example – EDA





- Median of the speeds of the steel coasters is much higher than that of the wooden coasters.
- □ Interquartile range of the steel coasters is much larger than that of the wooden coasters.
- □ The range of the speeds of the steel coasters is larger than that of the wooden coasters.
- Both the speeds of the wooden and steel coasters are slightly skewed to the left.

Summary



- □ Measure of center mean, median, mode
- □ Measure of dispersion − range, variance, standard deviation
- Using standard deviation Chebyshev's Theorem, empirical rule.
- Quartiles, percentiles, deciles.
- Box-and-whisker plot.