

Energy Economics

Energy market module (focus on electricity markets)

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Textbook: Perez Arriaga, Regulation of the power sector, pp.341-379

Constrained market clearing



Constrained SMP mechanism

- **Definition:** A congestion occurs when a transmission line is used at its maximum capacity. Transactions on the power market may even exceed the above-mentioned capacity, and make it unfeasible to execute them “physically”
- **Market impact:** market results based on demand/supply matching is not fully dispatchable

Ex-post resolution

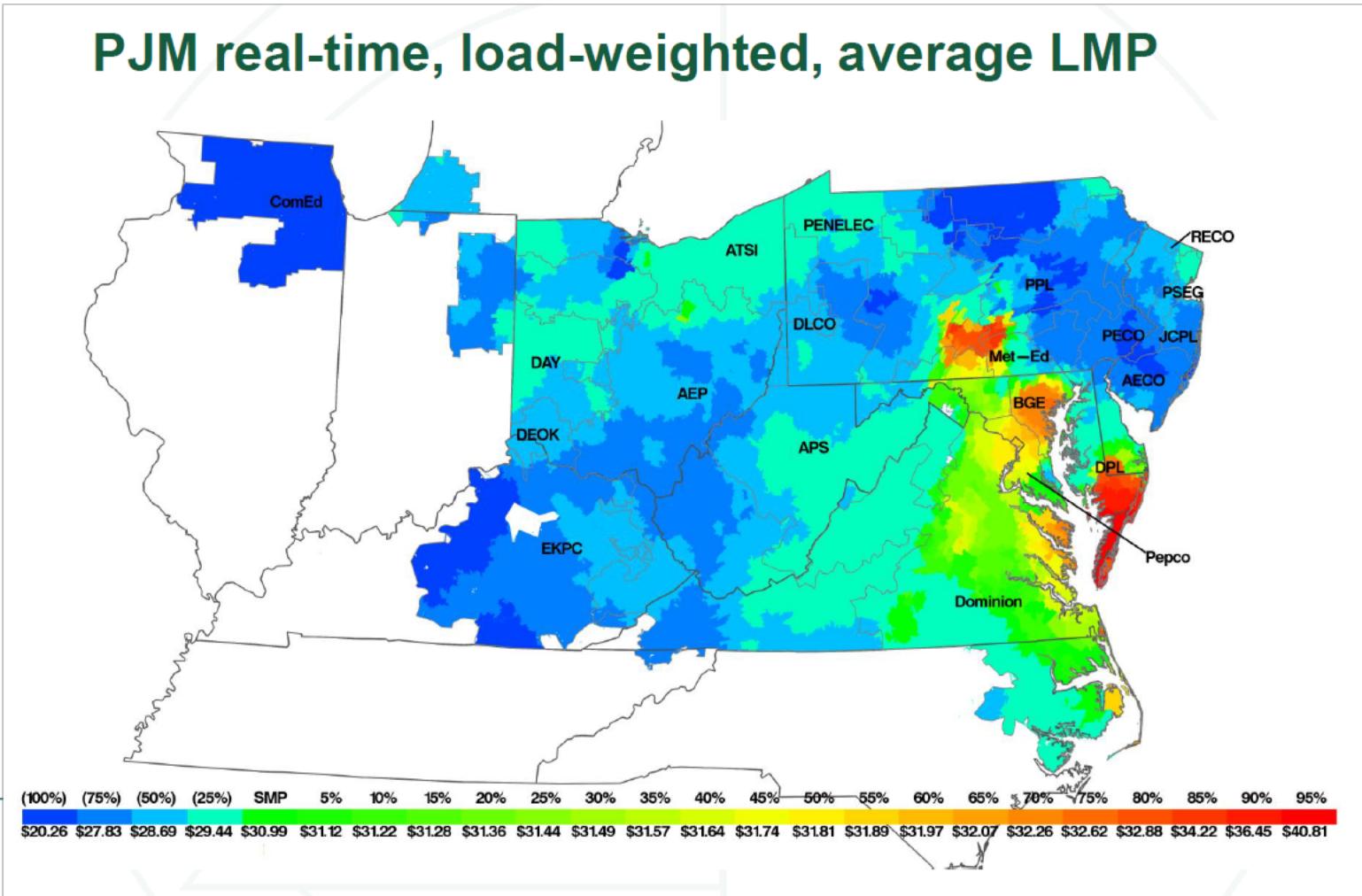
1. **Counter trading:** The transmission system operator (TSO) buys “services” for solving congestions on a dedicated market
2. **Redispatching:** The TSO curtails capacity to solve congestions (a problem of compensation arises)

Ex-ante resolution

1. **Nodal price(es. PJM, Ercot)**
 - Market price arises in each injection/withdrawn point
 - Price differentials include congestion costs.
 - Algorithms for pricing are complex, price is not transparent, managing the system is rather difficult, but efficiency is the maximum possible.
2. **Zonal price (Nordpool, GME)**
 - Market is divided into market zones.
 - If power flows exceed the grid's maximum capacity the market splits into several sub-markets (depending on the number of the zones) and a price originates for each of them.



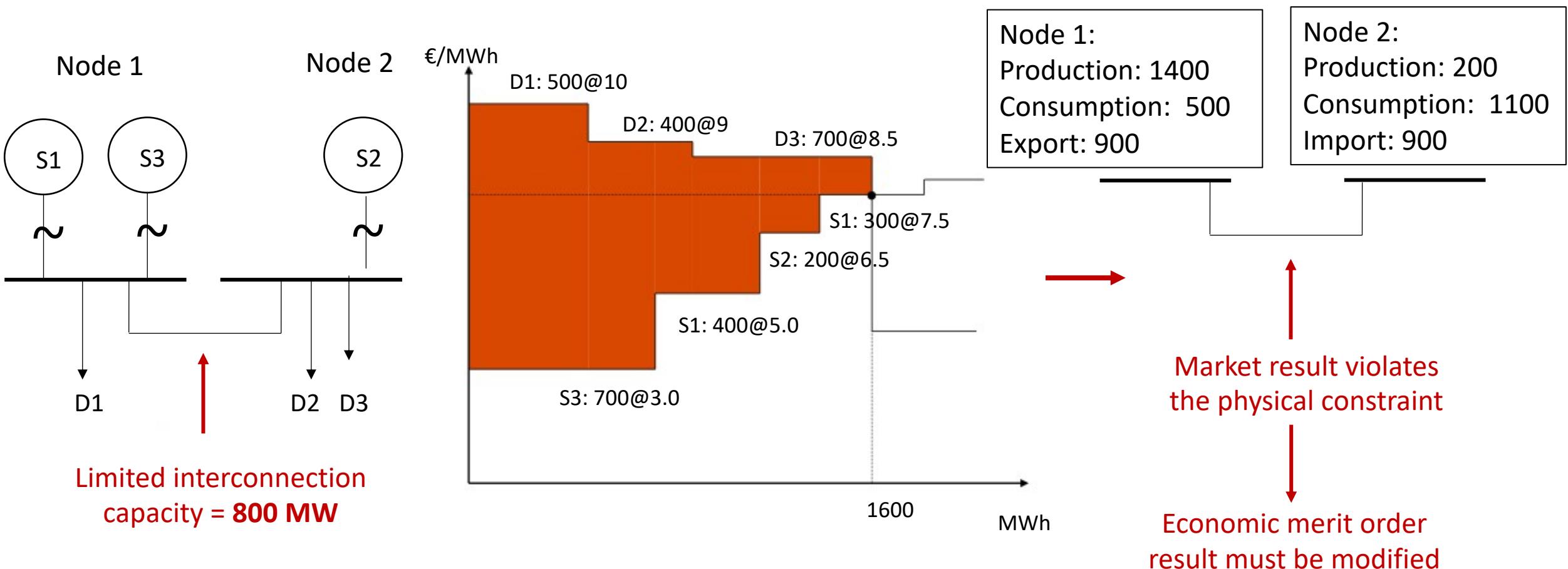
Constrained SMP mechanism: example PJM



Constrained SMP mechanism: example Nordpool



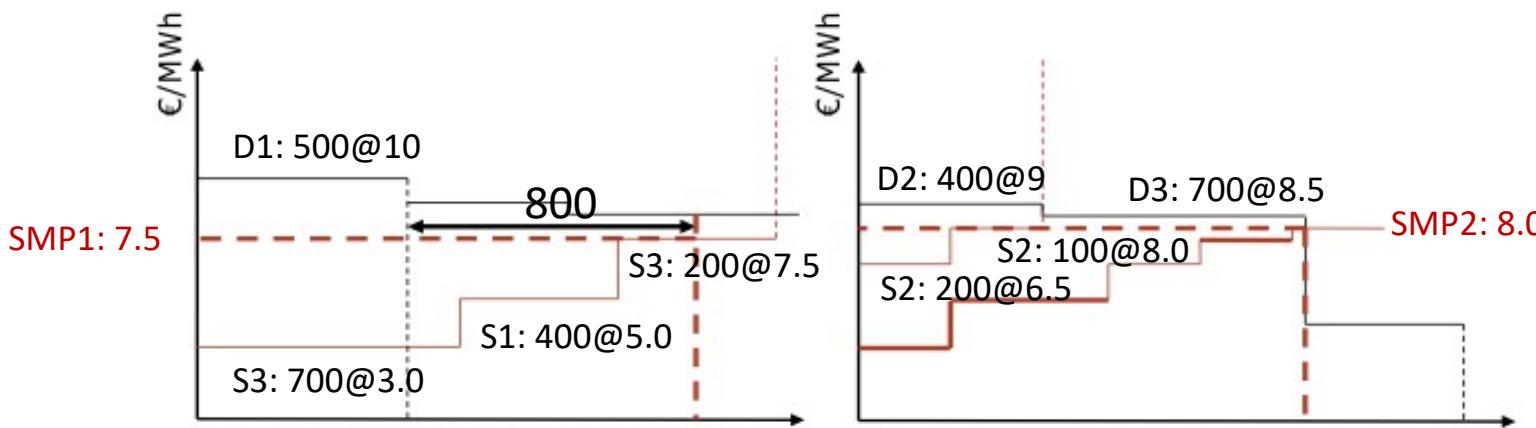
Constrained SMP mechanism



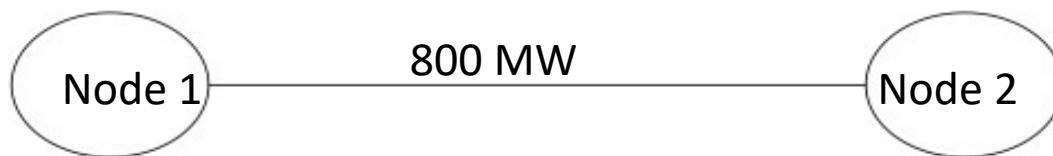
Constrained SMP mechanism

- The line flow limit splits the system into two markets, one at each node
- The economic generation at node 1 is used to the extent physically feasible to meet the load at node 2
- The demand in node 1 is modified to incorporate the demand from node 2
- The remaining demand at node 2 is supplied locally
- The two markets have different clearing prices (higher in the importing node than in the exporting one)

Constrained SMP mechanism



- If unconstrained solution is not feasible, the market is splitted
- In each market zone marginal supplier belong to the that zone



Constrained SMP mechanism

Player	Accepted quantity (MWh)	Price (€/MWh)	Revenues (€)	Costs (€)	Variation
S1	600	7.5	4500		-750
S2	300	8.0	2400		900
S3	700	7.5	5250		0
D1	500	7.5		3750	0
D2	400	8.0		3200	200
D3	700	8.0		5600	350
Total	1600		12150	12550	

Market splitting transfer to market participants price signals on overcapacity/shortage:

- Suppliers/Customers in net export zones reduces revenues (price/quantity effect)/costs
- Customers/Suppliers in net import zones increase costs/revenues



Price signal effect to address investments in electricity production capacity

Constrained SMP mechanism: congestion rent

Congestion rent:

- Difference between the amounts paid by buyers and the amounts received by sellers
- It is collected by the TSO
- It is part of the total surplus

$$k = \sum_{i=1}^n SMP_i(Q_{Di}) - \sum_{j=1}^m SMP_j(Q_{Sj})$$

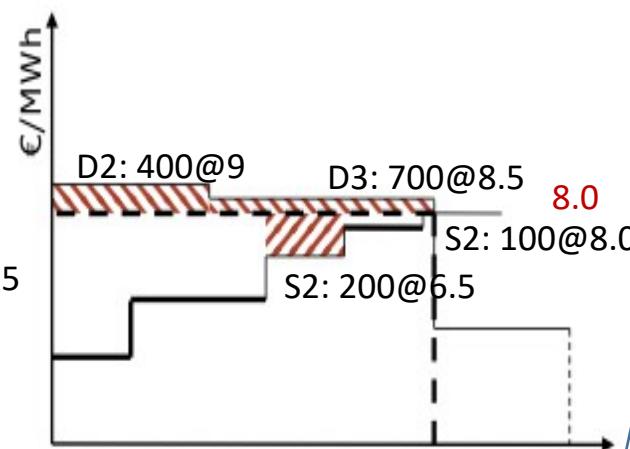
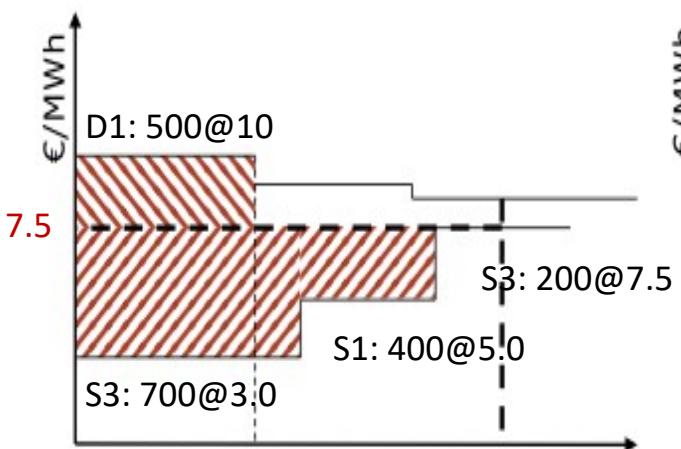
$$\bar{S} = \overline{S^D} - \overline{S^S} + k$$

Constrained total
surplus



Constrained SMP mechanism: congestion rent

Constrained Surplus calculation



Sellers	Surplus	Buyers	Surplus
S1	1000	D1	1250
S2	300	D2	400
S3	3150	D3	350
Total	4450		2000
Congestion rent			12550-12150=400
Total surplus			4450+2000+400=6850



Maximum interconnection flows times zonal difference in price: $800 \text{ MW} \times (0.5 \text{ €}/\text{MWh}) = 400 \text{ €}$

Constrained SMP mechanism: congestion costs

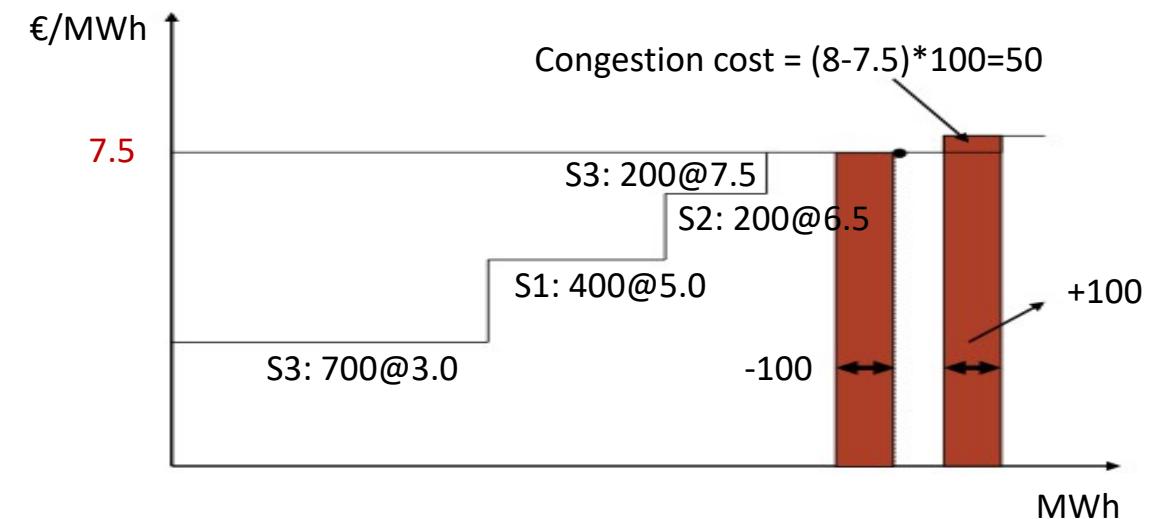
Congestion cost:

- Congestions produce a reduction in total surplus
- This reduction is called **deadweight loss**

$$\varepsilon = -(\bar{S} - S)$$
$$\varepsilon = -(6850 - 6900) = 50$$

Congestion cost:

- The efficiency loss represent the redispatch costs: the costs incurred because of the use of out-of-merit units to avoid violation of the network constraints



Constrained SMP mechanism: congestion costs

Short term effects

- Change in merit order wrt unconstrained equilibrium
- Multiple prices
- Change in producer and consumer surplus
- Congestion rents
- Redispatch costs

Long term effects:

- Price difference: siting of power plants in nodes with higher prices
- Congestion rent: transmission expansion necessary



Constrained SMP mechanism: exercise

- The electricity market in Country A consist of 2 zones: North and South
- Myplants owns 2 power plants and competes with other power plants
- Myplants must define the optimal bidding knowing the competitors' bid strategies and level of market demand (and constraint) in each hour

	Hour 1	Hour 2
North zone - demand (MW)	60	80
South zone - demand (MW)	70	90
Total demand MW	130	170
Transmisison capacity MW	80	80
bid granularity €/MWh	0.1	0.1

Competitors	Capacity (MW)	bid €/MWh	Zone
plant 1 hydro	40	4	North
plant 2 CCGT	60	8	North
plant 3 peakloader	20	9	South
plant 4 peakloader	30	12	South
Total Competitors' Capacity	150		

Myplants	Capacity (MW)	variable costs €/MWh	zone
myCCGT	80	7.5	North
mypeakloader	40	9	South
Total Myplants' Capacity	120		

Constrained SMP mechanism: exercise



10:00

Aim: calculate the optimal bids for

Myplants in hours 1 assuming that:

- **Myplants maximize its profit**
- **Myplants doesn't bid below its variable costs**
- **Competitors plants have priority of dispatch wrt Myplants**

Hint:

- Build the supply curve based on bid and variable costs level
- Verify grid constraint condition
- Set the bid for Myplants to maximize its' profit

	Hour 1	Hour 2	
North zone - demand (MW)	60	80	
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Myplants	Capacity (MW)	variable costs €/MWh	zone
myCCGT	80	7.5	North
mypeakloader	40	9	South
Total Myplants' Capacity	120		



Constrained SMP mechanism: solution – hour 1

Zone	Hour 1	Zone	MW - capacity	Cumulative max production	Cumulative production	Variable costs	Bid	Dispatched (Yes/no)
North	plant 1 hydro	North	40	40	40		4	Yes
North	plant 2 CCGT	North	80	120	120		8	Yes
North	myCCGT	North	60	180	130	7.5	8.4	Yes
South	plant 3 peakloader	South	20	200	0		8.5	No
South	mypeakloader	South	30	230	0	9	0	No
South	plant 4 peakloader	South	30	260	0		12	No

- myCCGT plant can bid at competitors' bid- ε price: $9-0.1=8.9$ €/MWh. This bid is higher than the variable costs of CCGT plant
- Mypeakloader has higher variable cost wrt equilibrium SMP: rationale strategy is not bidding
- Profit for Myplants company: $8.4\text{€}/\text{MWh} \times (130-120) = 84$ €

Constrained SMP mechanism: exercise



10:00

Aim: calculate the optimal bids for Myplants in hours 2 assuming that:

- Myplants maximize its profit
- Myplants doesn't bid below its variable costs
- Competitors' plants have priority of dispatch wrt Myplants

Hint:

- Build the supply curve based on bid and variable costs level
- Verify grid constraint condition
- Set the bid for Myplants to maximize its' profit

	Hour 1	Hour 2	
North zone - demand (MW)	60	80	
South zone - demand (MW)	70	120	
Total demand MW	130	200	
Transmision capacity MW	80	80	
bid granularity €/MWh	0.1	0.1	

Competitors	Capacity (MW)	bid €/MWh	Zone
plant 1 hydro	40	4	North
plant 2 CCGT	60	8	North
plant 3 peakloader	20	8.5	South
plant 4 peakloader	30	12	South
Total Competitors' Capacity	150		

Myplants	Capacity (MW)	variable costs €/MWh	zone
myCCGT	80	7.5	North
mypeakloader	40	9	South
Total Myplants' Capacity	120		



Constrained SMP mechanism: solution – hour 2

Zone	Hour 2	MW - capacity	Cumulative max production	Cumulative production	Variable costs	Bid	Dispatched (Yes/no)
North	plant 1 hydro	40	40	40		4	Yes
North	plant 2 CCGT	60	100	100		8	Yes
North	myCCGT	80	180	180	7.5	8.4	Yes
South	plant 3 peakloader	20	200	200		8.5	Yes
South	mypeakloader	40	240	0	9	0	No
South	plant 4 peakloader	30	270	0		12	No

- North-South flows: demand – south plant dispatched = $120-20=100$ -> **violation grid constraints**
- The unconstrained dispatch is not feasible
- We must find the optimal dispatch wrt 2 single market zones

Constrained SMP mechanism: solution – hour 2

Zone	Hour 2	MW - capacity	Cumulative max production	Cumulative production	Variable costs	Bid	Dispatched (Yes/no)
North	plant 1 hydro	40	40	40		4	Yes
North	myCCGT	80	120	120	7.5	7.9	Yes
North	plant 2 CCGT	60	180	160		8	Yes

Profit

- $(7.9-7.5)*80$
- $(11.9-9)*20$
- Profit: 90 €

Zone	Hour 2	MW - capacity	Cumulative max production	Cumulative production	Variable costs	Bid	Dispatched (Yes/no)
South	plant 3 peakloader	20	20	20		9	Yes
South	mypeakloader	40	60	40	9	11.9	Yes
South	plant 4 peakloader	30	90	0		12	No

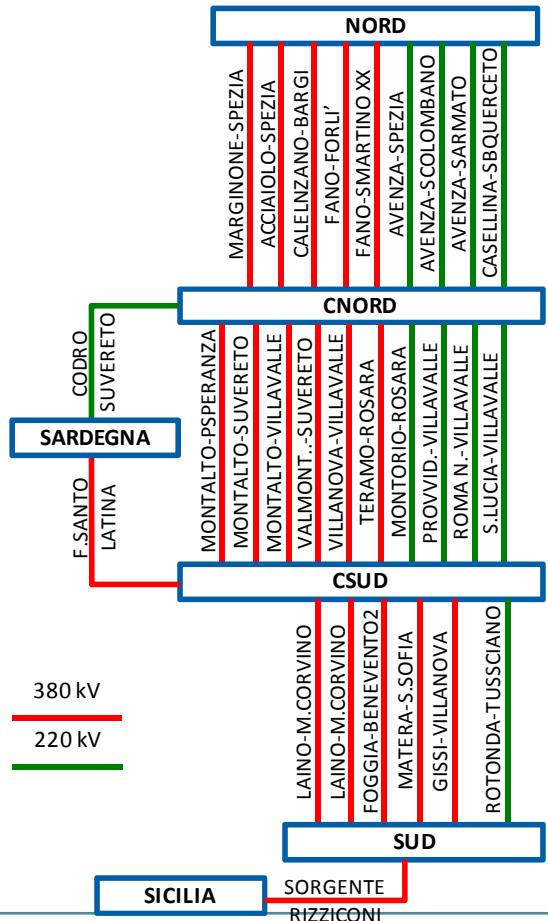
- myCCGT plant can bid at competitors' bid- ε price: $8-0.1=7.9$ €/MWh. This bid is higher than the variable costs of CCGT plant
- Mypeakloader plant can bid at competitors' bid- ε price: $12-0.1=11.9$ €/MWh. This bid is higher than the variable costs of CCGT plant



Italian DAM



Italian asymmetric zonal mechanism



Criteria for the definition of market zones:

- Constrained inter-zone transmission capacity
- No intra-zonal congestion
- The location of injection and withdrawal points within a zone does not affect transport capacity between zones

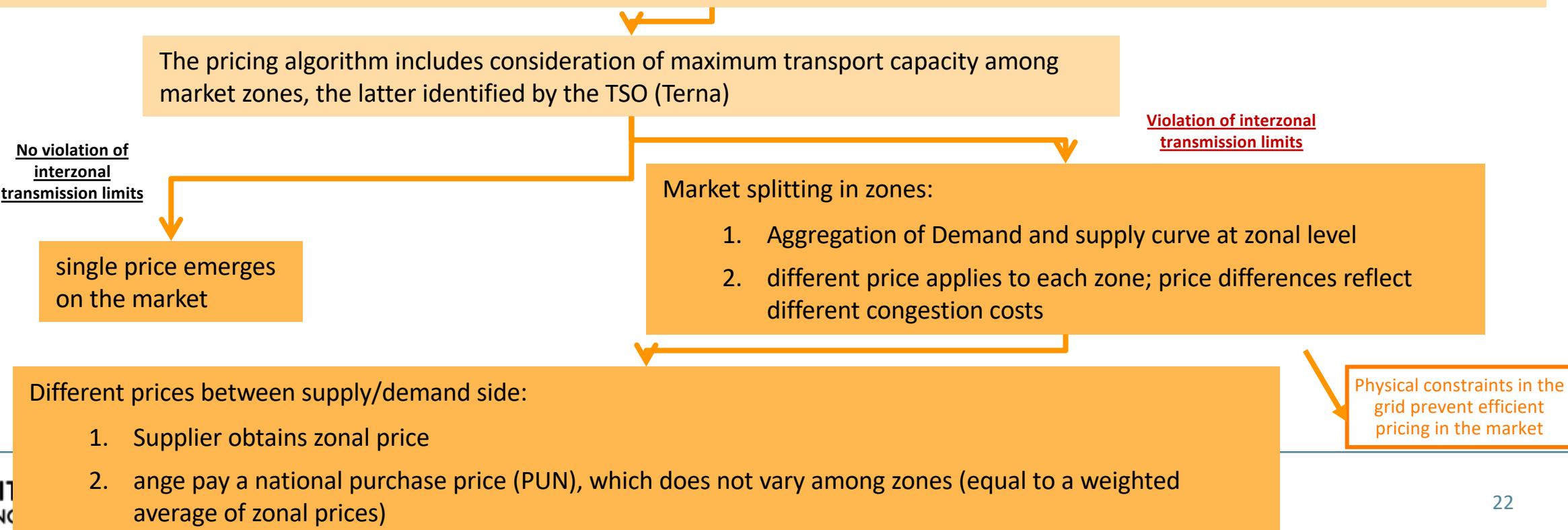
The market is currently divided in 6 zones. This configuration may change according to changes in congestions

There are also limited production sites



Italian asymmetric zonal mechanism

Day-ahead market (MGP) works as a non discriminatory auction, where all operators bidding to sell electricity are paid the **system marginal price**
GME ranks bids for selling and buying electricity based on a **economic merit order** criterium
bilateral agreements are considered as zero-price bids – for quantities sold – and undetermined-price bids – for quantities purchased.



Italian asymmetric zonal mechanism

Price differences among market zones represent an indication of the efficiency gain resulting from an upgrade of inter-zone transmission capacity. In other words, price differences represent the **value of transmission capacity**

- Producers injecting electricity in “exporting” zones **contribute to increase network congestions**
- Then they implicitly **pay the cost of transmission capacity**
- They receive a **lower electricity price** (and thus a lower revenue)

- Producers injecting electricity in “importing” zones **contribute to lower network congestions**
- Then they implicitly **receive the cost of transmission capacity**
- They receive a payment for transmission capacity through a **higher electricity price** (and thus a higher revenue)

Zonal pricing provides an incentive to localize investments in new capacity where prices are higher due to scarce or inefficient production capacity

Italian asymmetric zonal mechanism: additional costs for bilateral agreements

In the day-head market (MGP), operators “implicitly” pay or receive a price for using available inter-zone transport capacity

For bilateral agreements, operators pay or receive a similar price – namely the CCT – which is equal to the value of the available transport capacity plus a component for preventing arbitrage between exchange and OTC transactions

$$CCT = PUN - P_{\text{injection zone}}$$

if $PUN > P_{\text{injection zone}}$ (exporting zone), the operator that signs the bilateral agreement owes the CCT to GME

if $PUN < P_{\text{injection zone}}$ (importing zone), the operator that signs the bilateral agreement receives the CCT from GME

CCT components:

- Congestion cost (price of withdrawal zone minus price of injection zone)
- Non-arbitrage component (PUN minus price of withdrawal zone)

As a result of the PUN mechanism, CCT
is also due by those operators who
inject and withdraw electricity in the
same market zone

