

CHAPTER - 1

★ Principle of Amplitudes:

⇒ Purpose of communication system:-

- is to transmit information bearing signal through communication channel from one point to another through succession of process

→ i) The generation of message signal; voice, music, picture or computer data

→ ii) The description of that message signal with certain measure of precision by a set of symbols: electrical, aural or visual

→ iii) The encoding of these symbols in a form that is suitable for transmission over a physical medium

iv) The transmission of the encoded symbols to the desired destinations

v) The decoding and reproduction of original symbols

vi) The recreation of the original signal ~~with~~ ^{exit by} and also eliminating the noise

Noise is added in during transmissions due to imperfections in the system.

Transmitted power:- It's the average power of the transmitted signal

Channel Bandwidth: It's defined as the band of frequencies allocated for the transmission of the message signal

Noise: refers to unwanted waves that tend to disturb the transmission and processing of message signal in a communication system.

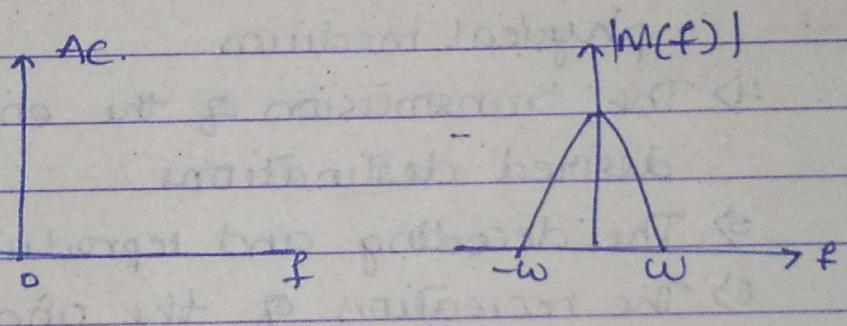
Sources may be internal or external to the system

Modulation:-

It is a process of frequency translation which imports the source information on to a Bandpass signal with carrier frequency f_c . By the introduction of amplitude or phase variations or both in accordance with modulating signal

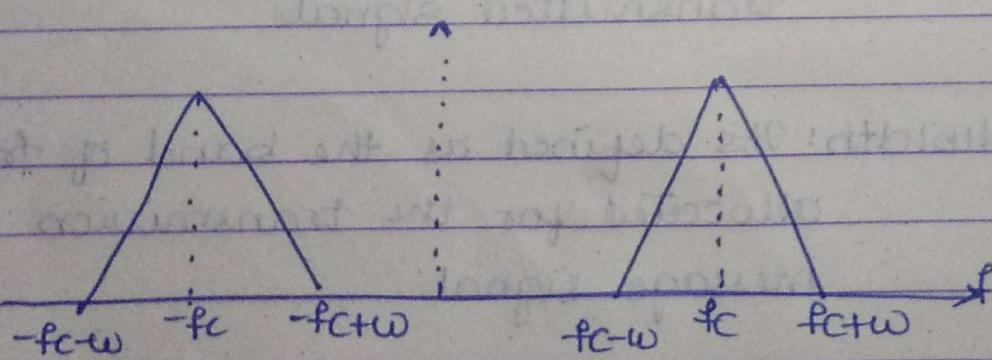
Base band:

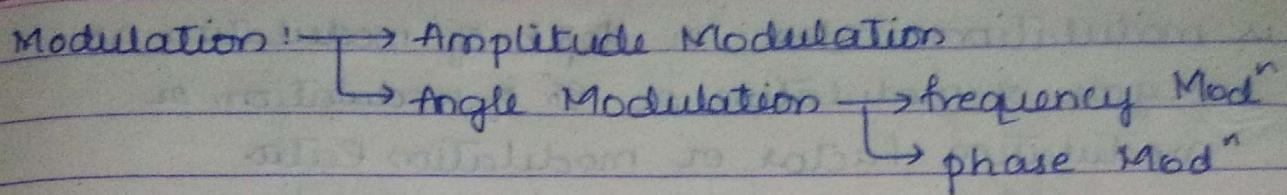
Base band waveform has a spectral magnitude is non zero for frequencies in the vicinity of origin and negligible elsewhere



Band pass:

Band pass signal has a spectrum magnitude is non zero for frequencies in same band concentrated above the frequencies $f = \pm f_c$ where $f_c > 0$. The spectral magnitude is 0 elsewhere





Amplitude Modulation:

It's a process of changing amplitude of carrier signal in accordance with instantaneous values of message signal keeping frequency and phase constant.

Derivation

$m(t)$ - message signal / Modulating signal

$c(t)$ - carrier signal

$s(t)$ - Modulated signal

$$c(t) = A_c \cos 2\pi f_c t$$

A_c - carrier amplitude

f_c - carrier frequency.

$$s(t) = [A_c + m(t)] \cos 2\pi f_c t$$

$$= A_c [1 + \gamma_{AC} m(t)] \cos 2\pi f_c t$$

$$s(t) = A_c [1 + k_a m(t)] \cos 2\pi f_c t$$

$$\left. \begin{array}{l} \gamma_{AC} = k_a \\ \text{general equation} \\ \text{for AM} \end{array} \right\}$$

k_a - amplitude sensitivity

$$\mu = |k_a m(t)|_{\max}$$

$$k_a = \frac{\mu}{m(t)_{\max}}$$

$$\mu = \frac{A_m}{A_c}$$

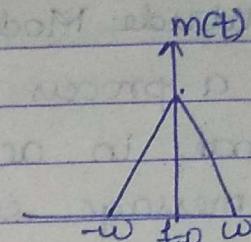
$$g) q(f) = \int_{-\infty}^{\infty} q(t) e^{-j2\pi f t} dt$$

μ is modulation index or depth of modulation or degree of modulation or % of modulation or modulation factor or modulation ratio.

$$\% \mu = \frac{A_m}{A_c} \times 100$$

$$s(t) = A_c \{ 1 + \mu m(t) \} \cos 2\pi f_c t$$

Applying FT



$$s(t) = A_c \cos 2\pi f_c t + A_c \mu m(t) \cos 2\pi f_c t$$

$$s(f) = \int_{-\infty}^{\infty} s(t) e^{-j2\pi f t} dt$$

$$s(f) = \int_{-\infty}^{\infty} (A_c \cos 2\pi f_c t + A_c \mu m(t) \cos 2\pi f_c t) e^{-j2\pi f t} dt$$

$$s(f) = \int_{-\infty}^{\infty} A_c \cos 2\pi f_c t e^{-j2\pi f t} + A_c \mu m(t) \cos 2\pi f_c t e^{-j2\pi f t} dt$$

$$s(f) = \int_{-\infty}^{\infty} A_c \left(\frac{e^{j2\pi f_c t} + e^{-j2\pi f_c t}}{2} \right) e^{-j2\pi f t} + A_c \mu m(t) \left[\frac{e^{j2\pi f_c t} + e^{-j2\pi f_c t}}{2} \right] e^{-j2\pi f t} dt$$

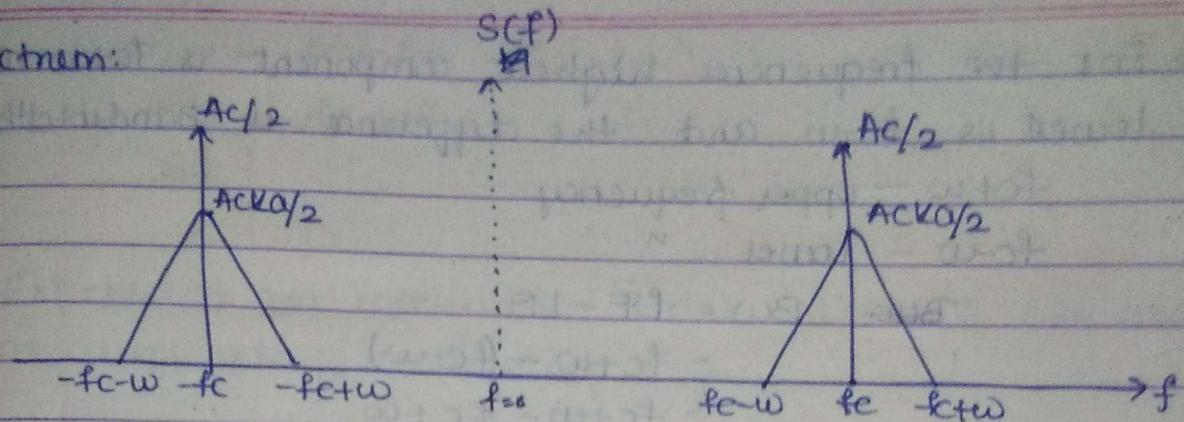
$$= \frac{A_c}{2} \int_{-\infty}^{\infty} e^{j2\pi f_c t} e^{-j2\pi f t} + e^{-j2\pi f_c t} e^{-j2\pi f t} dt + \frac{A_c \mu}{2} \int_{-\infty}^{\infty} m(t) e^{j2\pi f_c t} e^{-j2\pi f t} + m(t) e^{-j2\pi f_c t} e^{-j2\pi f t} dt$$

$$= \frac{A_c}{2} \int_{-\infty}^{\infty} e^{-j2\pi(f-f_c)t} + e^{-j2\pi(f+f_c)t} dt + \frac{A_c \mu}{2} \int_{-\infty}^{\infty} m(t) e^{-j2\pi(f-f_c)t} + m(t) e^{-j2\pi(f+f_c)t} dt$$

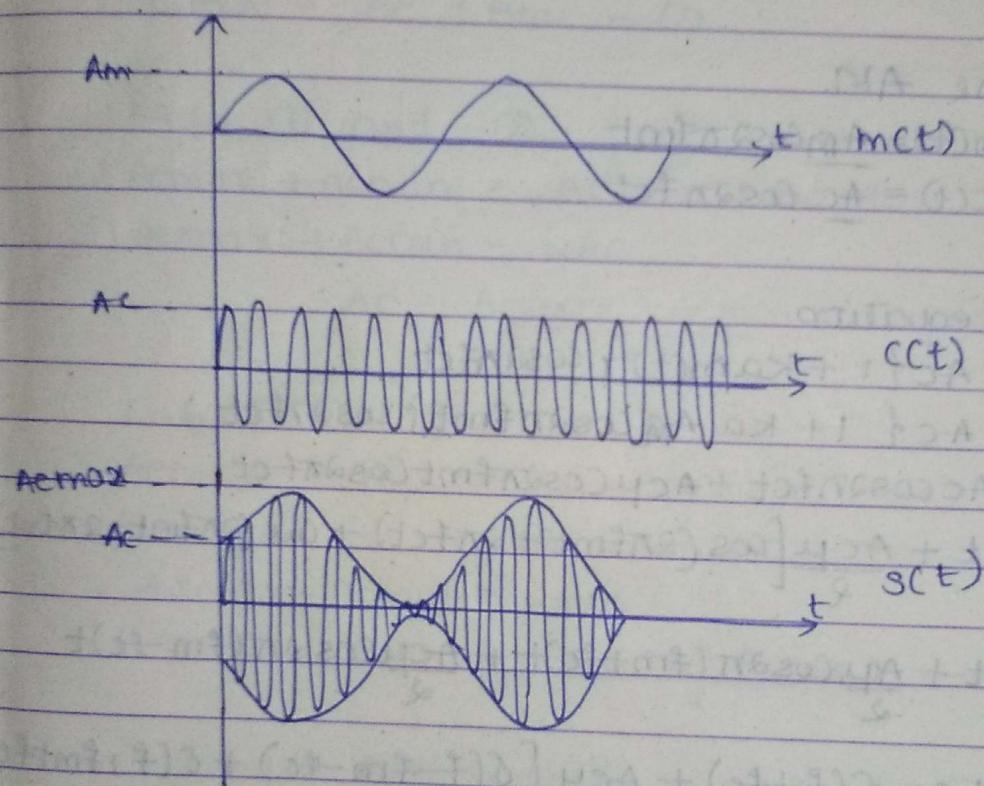
$$= \frac{A_c}{2} [\delta(f-f_c) + \delta(f+f_c)] + \frac{A_c \mu}{2} [m(f-f_c) + m(f+f_c)]$$

$$= \frac{A_c}{2} \delta(f-f_c) + \frac{A_c}{2} \delta(f+f_c) + \frac{A_c \mu}{2} M(f-f_c) + \frac{A_c \mu}{2} M(f+f_c)$$

spectrum:



waveform:



★

- Message signal centered @ $f=0$ extending from $-\omega$ to ω is translated to $f_c = \pm f_c$
- For $f_c >= \omega$ The spectrum is non overlapping and can be filtered out using Bandpass filter
if ~~$f_c < \omega$~~ $f_c < \omega$ The message spectrum is not same as the $m(t)$ and there is overlapping.
- Transmission Bandwidth is specified by the width of spectrum of the frequencies.

→ For the frequencies highest component is f_{ctw} and lowest is f_{cw} and the difference is Bandwidth

f_{ctw} - upper frequency

f_{cw} - lower "

$$B_{H.F.} = U.F. - L.F.$$

$$= f_{ctw} - f_{cw}$$

$$= f_{ctw} - f_{ctw}$$

$$B.W. = Q.W.$$

* single tone AM.

$$m(t) = A_m \cos 2\pi f_m t$$

$$c(t) = A_c \cos 2\pi f_c t$$

General AM equation

$$s(t) = A_c \{ 1 + k_a m(t) \} \cos 2\pi f_c t$$

$$= A_c \{ 1 + k_a A_m \cos 2\pi f_m t \} \cos 2\pi f_c t$$

$$= A_c \cos 2\pi f_c t + A_c k_a \cos 2\pi f_m t \cos 2\pi f_c t$$

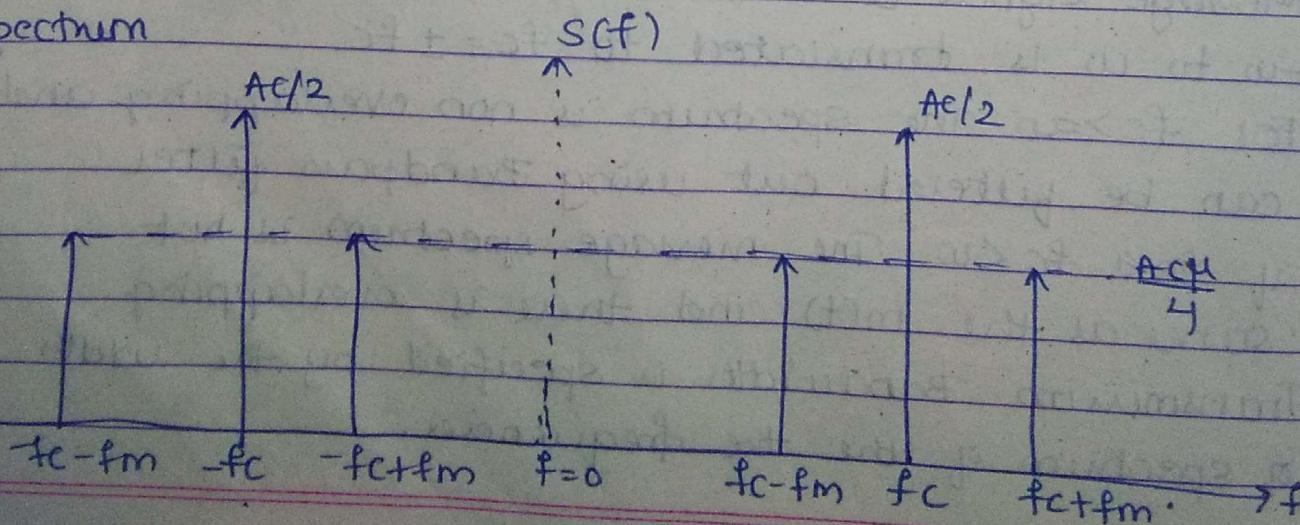
$$= A_c \cos 2\pi f_c t + \frac{A_c k_a}{2} [\cos(2\pi f_m t + 2\pi f_c t) + \cos(2\pi f_m t - 2\pi f_c t)]$$

$$= A_c \cos 2\pi f_c t + \frac{A_c k_a}{2} \cos 2\pi (f_m + f_c) t + \frac{A_c k_a}{2} \cos 2\pi (f_m - f_c) t$$

$$= \frac{A_c}{2} \delta(f - f_c) + \frac{A_c}{2} \delta(f + f_c) + \frac{A_c k_a}{4} [\delta(f - f_m - f_c) + \delta(f + f_m + f_c)$$

$$+ \delta(f - f_m + f_c) + \delta(f + f_m - f_c)]$$

Spectrum



$$\text{Bandwidth} = f_c + f_m - (f_c - f_m)$$

$$BW = f_c + f_m - f_c + f_m$$

$$BW = 2f_m$$

* Expression for modulation index in terms of min and max amplitude of modulating signal

$$A_{C\max} = A_c + A_m \quad \text{--- (1)}$$

$$A_{C\min} = A_c - A_m \quad \text{--- (2)}$$

Add (1) and (2)

$$A_{C\max} + A_{C\min} = A_c + A_m + A_c - A_m$$

$$A_{C\max} + A_{C\min} = 2A_c$$

$$A_c = \frac{A_{C\max} + A_{C\min}}{2} \quad \text{--- (3)}$$

Sub (1) and (2)

$$A_{C\max} - A_{C\min} = A_c + A_m - (A_c - A_m)$$

$$= A_c + A_m - A_c + A_m$$

$$A_{C\max} - A_{C\min} = 2A_m$$

$$A_m = \frac{A_{C\max} - A_{C\min}}{2} \quad \text{--- (4)}$$

$$\mu = \frac{A_m}{A_c} \quad \text{--- (5)}$$

Substitute (3) and (4) in (5)

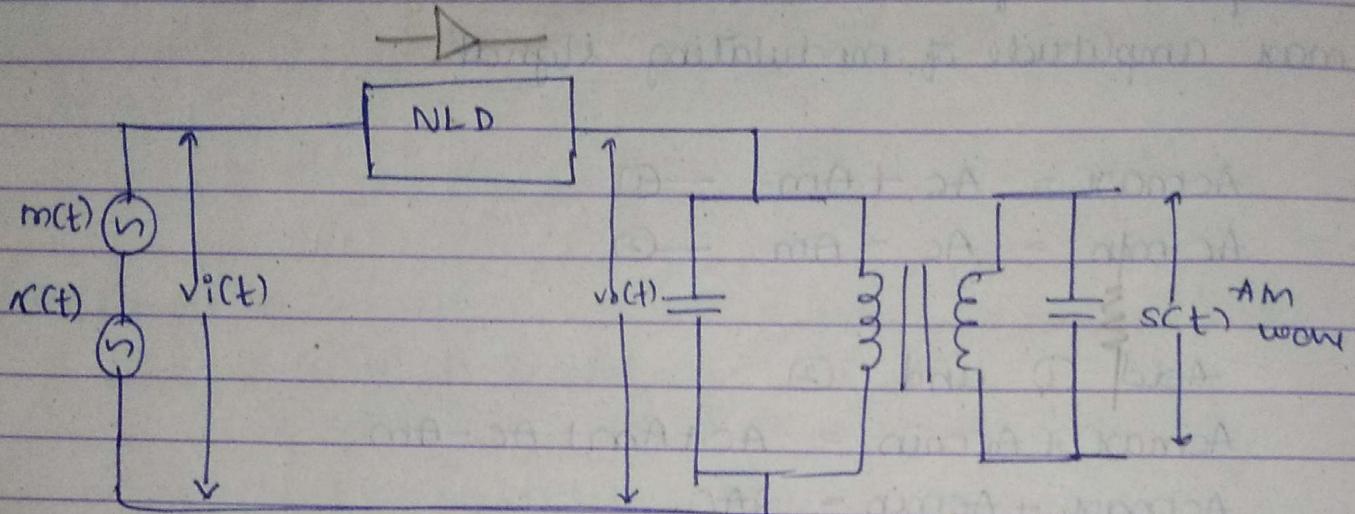
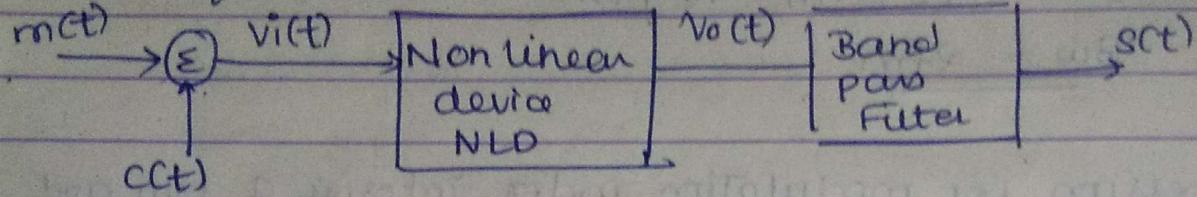
$$\mu = \frac{A_{C\max} - A_{C\min}}{2}$$

$$A_{C\max} + A_{C\min}$$

$$\mu = \frac{A_{C\max} - A_{C\min}}{A_{C\max} + A_{C\min}}$$

* Generation of AM Wave

Square Law Modulator



Require 3 feature

- ~~one~~ means of carrier and modulating signal
- a non linear element
- a band pass filter to extract desired modulated signal

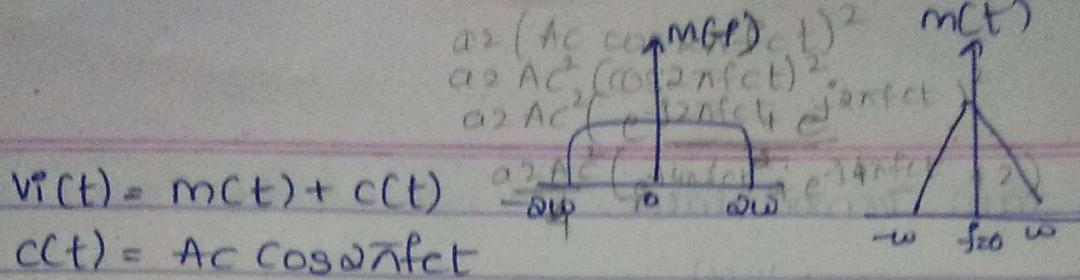
Semiconductor diodes and transistors are the most common non linear devices

filter required is usually satisfied using single or double tuned filter.

When a non linear element such as a diode is suitably biased and operated in its restricted ~~area~~ portion of its characteristics curve (ie relatively weak signal) it is observed that the characteristics of the diode load resistor combination is represented closely by square law.

$$V_o(t) = a_0 + a_1 V_i(t) + a_2 V_i(t)^2 + a_3 V_i(t)^3 + \dots$$

$$V_o(t) = a_0 + a_1 V_i(t) + a_2 V_i(t)^2$$



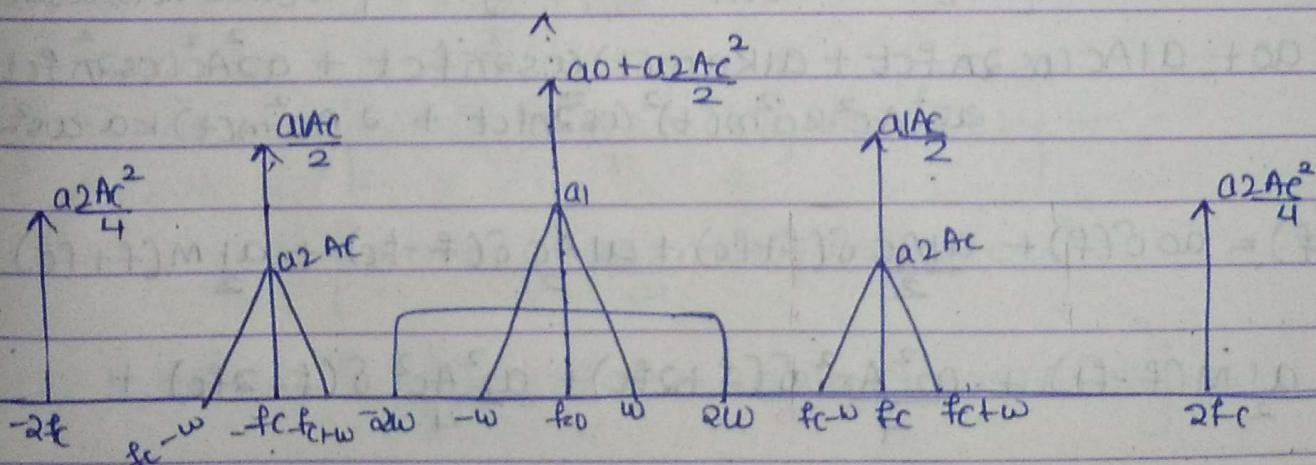
$$\begin{aligned}
 V_o(t) &= a_0 + a_1 [m(t) + c(t)] + a_2 [m(t)^2 + (Ac \cos \omega_f t)^2] \\
 &= a_0 + a_1 [m(t) + Ac \cos \omega_f t] + a_2 [m(t)^2 + (Ac \cos \omega_f t)^2] \\
 &\quad + 2a_2 m(t) Ac \cos \omega_f t \\
 &= a_0 + a_1 m(t) + a_1 Ac \cos \omega_f t + a_2 m(t)^2 + a_2 (Ac \cos \omega_f t)^2 \\
 &\quad + 2a_2 m(t) Ac \cos \omega_f t
 \end{aligned}$$

fourier transform.

$$= a_0 \delta(f) + a_1 M(f) + a_1 \frac{Ac}{2} \delta(f+f_c) + a_1 \frac{Ac}{2} \delta(f-f_c) +$$

$$a_2 M^2(f) + a_2 \frac{Ac^2}{4} \delta(f+f_c) + a_2 \frac{Ac^2}{4} \delta(f-f_c) + a_2 \frac{Ac^2}{2} \delta(f)$$

$$a_2 M(f) a_2 A C M(f+f_c) + a_2 A C M(f-f_c)$$

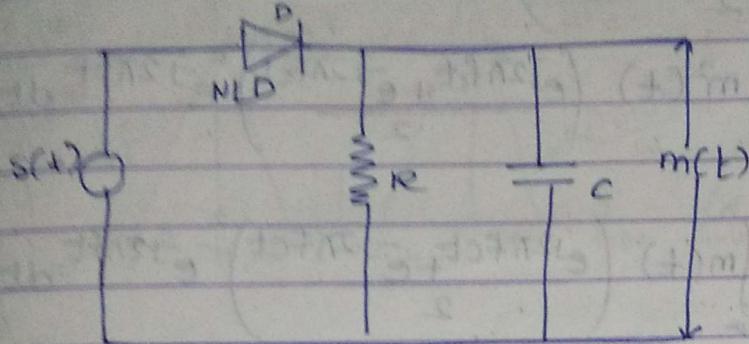
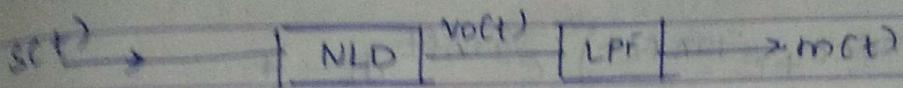


filter. $f_c - w > 2w$ $f_c + w < 2f_c$.

$f_c > 3w$ $f_c > w$.

↳ ~~filter~~ ~~filter~~

equation (ans demodulator)



$$V_i(t) = s(t)$$

$$v_o(t) = a_0 + a_1 v_i(t) + a_2 v_i(t)^2 + a_3 v_i(t)^3 + \dots$$

$$v_i(t) = a_0 + a_1 s(t) + a_2 s(t)^2 +$$

$$s(t) = a_1 A C \left(1 + \frac{2a_2}{a_1} m(t) \right) \cos 2\pi f_c t$$

$$\frac{2a_2}{a_1} = k_a$$

$$v_o(t) = a_0 + a_1 \left[a_1 A C \left(1 + \frac{2a_2}{a_1} m(t) \right) \cos 2\pi f_c t \right] +$$

$$a_2 \left[a_1 A C \left(1 + \frac{2a_2}{a_1} m(t) \right) \cos 2\pi f_c t \right]$$

$$v_o(t) = a_0 + a_1^2 A C \left[\cos 2\pi f_c t + \frac{2a_2}{a_1} m(t) \cos 2\pi f_c t \right] +$$

$$a_2 a_1^2 A C^2 \left[\cos 2\pi f_c t + \frac{2a_2}{a_1} m(t) \cos 2\pi f_c t \right]^2$$

$$v_o(t) = a_0 + a_1^2 A C \left[\cos 2\pi f_c t + \frac{2a_2}{a_1} m(t) \cos 2\pi f_c t \right] +$$

$$a_2 a_1^2 A C^2 \left[\cos^2 2\pi f_c t + \frac{4a_2^2 m^2(t)}{a_1^2} \cos^2 2\pi f_c t + \frac{4a_2 m(t) \cos^2 2\pi f_c t}{a_1^2} \right]$$

Applying FT

$$v_o(t) = \int a_0 e^{-j2\pi ft} + a_1^2 A C \int \cos \left(\frac{e^{j2\pi ft} + e^{-j2\pi ft}}{2} \right) e^{-j2\pi ft} dt +$$

$$\left[\frac{a_1^2 A C}{2} \frac{x_{02}}{a_1} \right] m(t) \left(e^{j2\pi f c t} + e^{-j2\pi f c t} \right) dt + c^{j2\pi f t} dt +$$

$$\left[\frac{a_2 a_1^2 A C^2}{a_1} \right] \left(\frac{e^{j2\pi f c t} + e^{-j2\pi f c t}}{2} \right)^2 e^{-j2\pi f t} dt +$$

$$\left[\frac{a_2 a_1^2 A C^2 4 a_2^2}{a_1^2} \right] \int_{-\infty}^t m^2(t) \left(\frac{e^{j2\pi f c t} + e^{-j2\pi f c t}}{2} \right)^2 e^{-j2\pi f t} dt$$

$$+ \left[\frac{a_2 a_1^2 A C^2 4 a_2}{a_1} \right] \int_{-\infty}^t m(t) \left(\frac{e^{j2\pi f c t} + e^{-j2\pi f c t}}{2} \right)^2 e^{-j2\pi f t} dt$$

$$= a_0 \delta(f) + \frac{a_1^2 A C}{2} \delta(f + f_c) + \frac{a_1^2 A C}{2} \delta(f - f_c) +$$

$$\frac{a_1^2 a_2 A C}{a_1} m(f + f_c) + \frac{a_1^2 a_2 A C}{a_1} m(f - f_c) +$$

$$\frac{a_2 a_1^2 A C^2}{4} \delta(f + 2f_c) + \frac{a_2 a_1^2 A C^2}{4} \delta(f - 2f_c) + \frac{a_2 a_1^2 A C^2}{2} \delta(f)$$

$$+ \frac{4 a_2 a_1^2 A C^2}{4 a_1^2} M^2(f + 2f_c) + \frac{4 a_2 a_1^2 A C^2}{4 a_1^2} M^2(f - 2f_c) + \frac{4 a_2 a_1^2 A C^2 M^2}{2 a_1}$$

$$+ \frac{4 a_1^2 a_2^2 A C^2}{4 a_1} M(f + 2f_c) + \frac{4 a_1^2 a_2^2 A C^2}{4 a_1} M(f - 2f_c) + \frac{4 a_1^2 a_2^2 A C}{2 a_1} M(f)$$

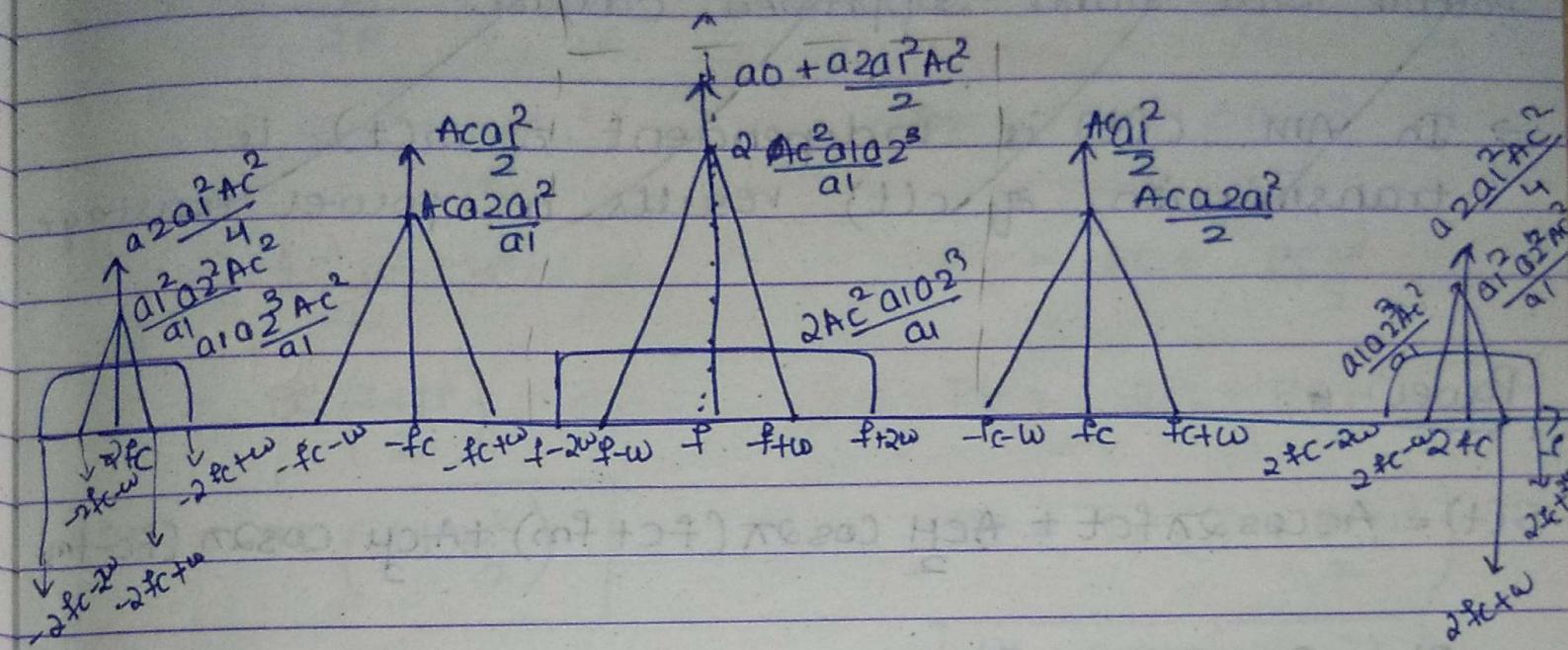
$$= a_0 \delta(f) + \frac{a_1^2 A C}{2} \delta(f + f_c) + \frac{a_1^2 A C}{2} \delta(f - f_c) +$$

$$\frac{a_1^2 a_2 A C}{a_1} M(f + f_c) + \frac{a_1^2 a_2 A C}{a_1} M(f - f_c) +$$

$$\frac{a_2 a_1^2 A C^2}{4} \delta(f + 2f_c) + \frac{a_2 a_1^2 A C^2}{4} \delta(f - 2f_c) + \frac{a_2 a_1^2 A C^2}{2} \delta(f)$$

$$+ \frac{a_1 a_2^2 A C^2}{a_1^2} M^2(f + 2f_c) + \frac{a_1 a_2^2 A C^2}{a_1^2} M^2(f - 2f_c) + \frac{2 a_1 a_2^2 A C^2 M^2}{a_1}$$

$$+ \frac{a_1^2 a_2^2 A C^2}{a_1} M(f + 2f_c) + \frac{a_1^2 a_2^2 A C^2}{a_1} M(f - 2f_c) + \frac{2 a_1^2 a_2^2 A C}{a_1} M(f)$$



$$w < f_c - w$$

$$f_c > 2w$$

$$-w < f_c + w$$

$$f_c > 2w$$

$$m'(t) = m(t) \cos 2\pi f_c t + \frac{2a_2}{a_1} a_1^2 A c \cos 2\pi f_c t$$

$$= a_1^2 A c \frac{2a_2}{a_1} m(t) \cos 2\pi f_c t + a_1^2 A c \cos 2\pi f_c t$$

$$= a_1 A C (1 + k_a m(t)) \cos 2\pi f_c t$$

$$\frac{2a_2}{a_1} = k_a$$

$$m'(t) = \underbrace{\frac{a_0 + a_2 A c^2}{2} A c^2 k_a a_2 m(t)}_{\text{component blocked by cap}} + a_2 A c a_1^2 m^2(t)$$

neglected
bcz low level
modulating signal.

$$m'(t) = A c^2 k_a a_2 m(t)$$

~~Double Side Band Suppressed carrier~~

→ In Am $c(t)$ is independent of $m(t)$ ie transmission of $c(t)$ results in power wastage

Power

$$S(t) = A_c \cos 2\pi f_c t + \frac{A_{CH}}{2} \cos 2\pi (f_c + f_m) t + \frac{A_{CH}}{2} \cos 2\pi (f_c - f_m) t$$

$$P_t = P_C + P_{USB} + P_{LSB}$$

$$= \frac{(A_c)^2}{R} + \frac{\left(\frac{A_{CH}}{2}\right)^2}{R} + \frac{\left(\frac{A_{CH}}{2}\right)^2}{R} \quad \left\{ P = \frac{V^2}{R} \text{ rms} \right.$$

$\sqrt{2}$

$$= \frac{A_c^2}{2R} + \frac{A_c^2 \mu^2}{8R} + \frac{A_c^2 \mu^2}{8R}$$

$$= \frac{A_c^2}{2R} + \frac{2A_c^2 \mu^2}{8R}$$

$P_t = \frac{A_c^2}{2R} + \frac{A_c^2 \mu^2}{4R}$	$P_C = \frac{A_c^2}{2R}$
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Side Band Power

$$P_S = \frac{A_c^2 \mu^2}{8R} + \frac{A_c^2 \mu^2}{8R}$$

$$= \frac{2A_c^2 \mu^2}{8R}$$

$$= \frac{A_c^2 \mu^2}{4R}$$

$$P_S = \frac{P_C \mu^2}{2}$$

$$P_T = \frac{AC^2}{2R} + \frac{AC^2\mu^2}{4R}$$

$$= \frac{2AC^2 + AC^2\mu^2}{4R}$$

$$= \frac{AC^2(2 + \mu^2)}{4R}$$

$$= PC \left(\frac{2 + \mu^2}{2} \right)$$

$$\boxed{P_T = PC \left(1 + \frac{\mu^2}{2} \right)}$$

$$P_T = PC + PC \frac{\mu^2}{4} + PC \frac{\mu^2}{4}$$

$$P_T = PC + 2PC \frac{\mu^2}{4}$$

$$P_T = PC + \frac{PC\mu^2}{2}$$

$$P_T = \frac{2PC + PC\mu^2}{2}$$

$$P_T = PC \left(\frac{2 + \mu^2}{2} \right)$$

$$\boxed{P_T = PC \left(1 + \frac{\mu^2}{2} \right)}$$

Average power in side band.

$$P_{SB} = P_{LSB} = P_{USB} = \frac{PC\mu^2}{2}$$

Efficiency

$$\eta = \frac{P_S}{P_T}$$

$$= \frac{PC\mu^2}{2}$$

$$\frac{PC(2 + \mu^2)}{2}$$

$$\boxed{\eta = \frac{\mu^2}{2 + \mu^2}}$$

Conclusion :-

If 100% modulation i.e. $\mu = 1$ $\gamma = \frac{1}{3}$ 33% mod.

$$\frac{P_s}{P_t} = \frac{1}{3}$$

$$\frac{P_s}{P_t} = \frac{1}{3}$$

$$3P_s = P_t$$

$$P_s = \frac{1}{3} P_t$$

$\frac{1}{3}^{\text{rd}}$ of total power is in modulated wave in AM

★ $s(t) = A_c(1 + k_m m(t)) \cos 2\pi f_c t$

$$P_t = P_c \left(1 + \frac{\mu^2}{2}\right)$$

$$P_s = P_c \frac{\mu^2}{2}$$

$$P_t = P_s 1 + P_s 2 + P_c$$

$$\mu_t = \sqrt{\mu_1^2 + \mu_2^2}$$

{ if two modulating signals are given

$$\mu = |k_m m(t)|_{\max}$$

$$V_t = V_c \sqrt{1 + \frac{\mu^2}{2}}$$

$$I_t = I_c \sqrt{1 + \frac{\mu^2}{2}}$$

$$BW = 2fm$$

side band frequency

$$f_{c\alpha} + f_m = \text{USB}$$

$$f_c - f_m = \text{LSB}$$

Avg amplitude of side band = $\frac{A_{CH}}{2}$

Amplitude of each side band = $\frac{A_{CH}}{4}$

$$\mu = \frac{A_{cm\alpha} - A_{cm\beta}}{A_{cm\alpha} + A_{cm\beta}}$$

(first diagram) Single sideband - (+)

Double sideband - (-)

Double tubeband - (1)

$$-127.5 \text{ mV} = (+)$$

$$110.5 \text{ mV} = (-)$$

$$110.5 - (-) = (+)$$

$$(+)(+)(+)(+) = (+)$$

$$110.5 - [110.5 + 127.5] = (-)$$

Double Side Band Suppressed Carrier

→ In AM $c(t)$ is independent of $m(t)$ this results in power wastage in transmission of $c(t)$

→ Suppressing the carrier component results in DSBSC
 → We obtain modulated wave ie proportional to product of carrier wave & message signal.

Derivation

so $m(t)$ - message signal (triangle w.)

$c(t)$ - carrier signal

$s(t)$ - modulated signal

$$\text{Set } c(t) = A \cos 2\pi f_c t$$

$$s(t) = A c m(t) \cos 2\pi f_c t$$

$$s(t) = \int_{-\infty}^{\infty} s(t) e^{-j 2\pi f t} dt$$

$$= \int_{-\infty}^{\infty} (A c m(t) \cos 2\pi f_c t) e^{-j 2\pi f t} dt$$

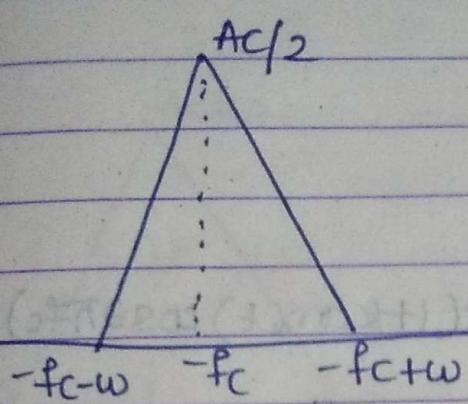
$$= \frac{Ac}{2} \int_{-\infty}^{\infty} m(t) \left[\frac{e^{j 2\pi f_c t} + e^{-j 2\pi f_c t}}{2} \right] e^{-j 2\pi f t} dt$$

$$= \frac{Ac}{2} \int_{-\infty}^{\infty} m(t) e^{j 2\pi f_c t} e^{-j 2\pi f t} + m(t) e^{-j 2\pi f_c t} e^{-j 2\pi f t} dt$$

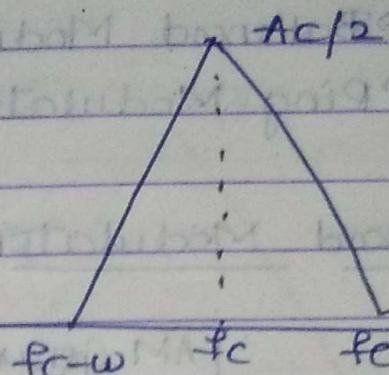
$$= \frac{Ac}{2} \int_{-\infty}^{\infty} m(t) e^{-j 2\pi (f - f_c)t} dt + \frac{Ac}{2} \int_{-\infty}^{\infty} m(t) e^{-j 2\pi (f + f_c)t} dt$$

$$= \frac{Ac}{2} M(f - f_c) + \frac{Ac}{2} M(f + f_c)$$

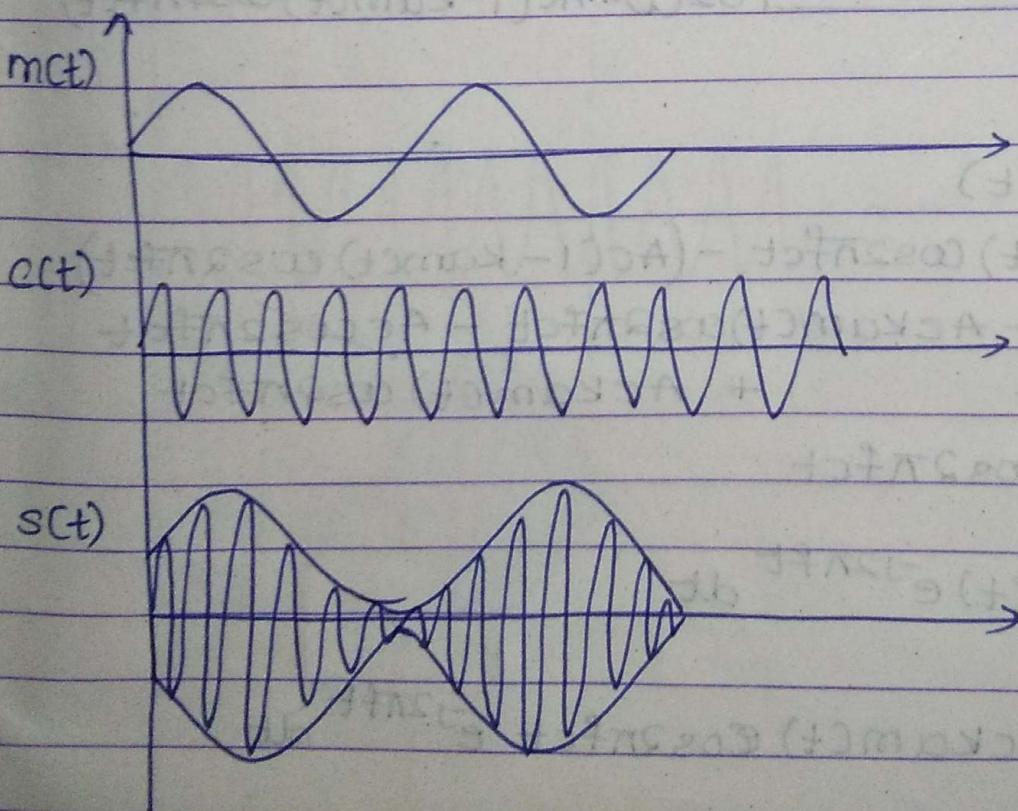
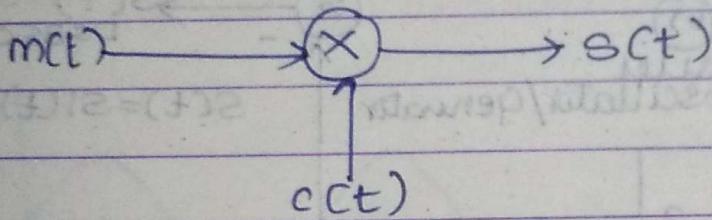
Spectrum



$s(f)$



Block diagram

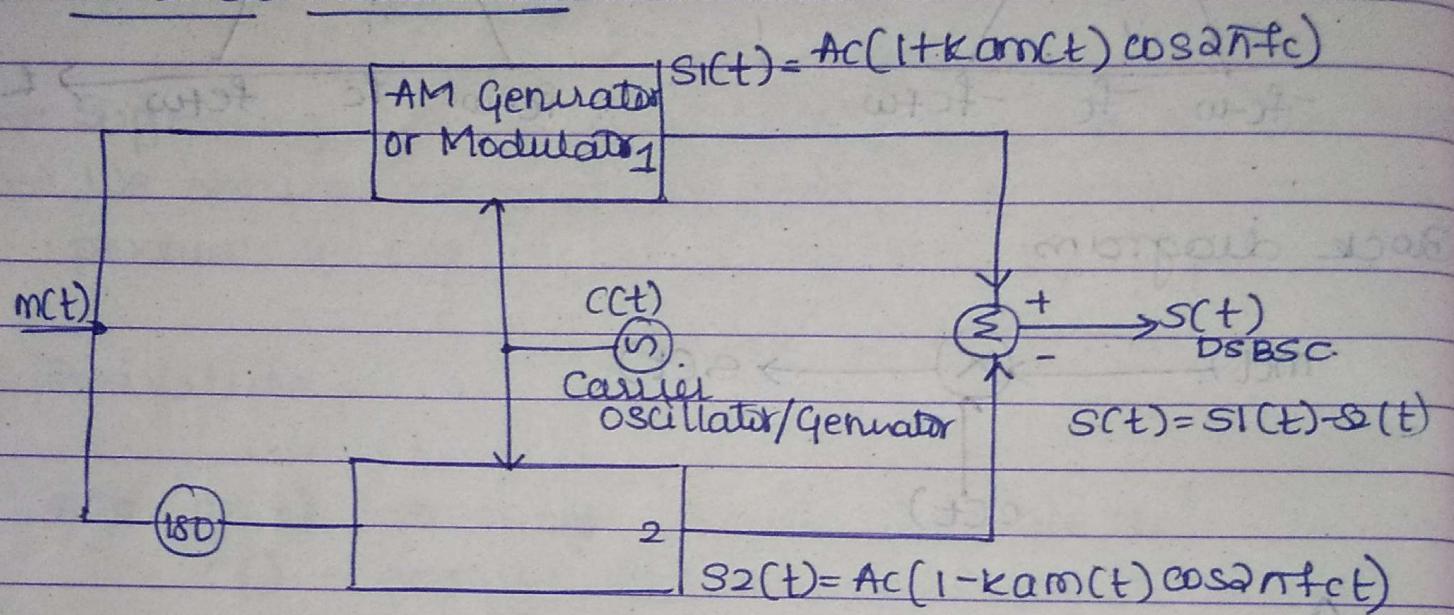


Generation of DSBSC Signal

→ Balanced Modulator

→ Ring Modulator

* Balanced Modulator



$$s(t) = s_1(t) - s_2(t)$$

$$\begin{aligned} &= A_c(1 + k_a m(t)) \cos 2\pi f_c t - (A_c(1 - k_a m(t)) \cos 2\pi f_c t) \\ &= A_c \cos 2\pi f_c t + A_c k_a m(t) \cos 2\pi f_c t - A_c \cos 2\pi f_c t \\ &\quad + A_c k_a m(t) \cos 2\pi f_c t \end{aligned}$$

$$s(t) = 2 A_c k_a m(t) \cos 2\pi f_c t$$

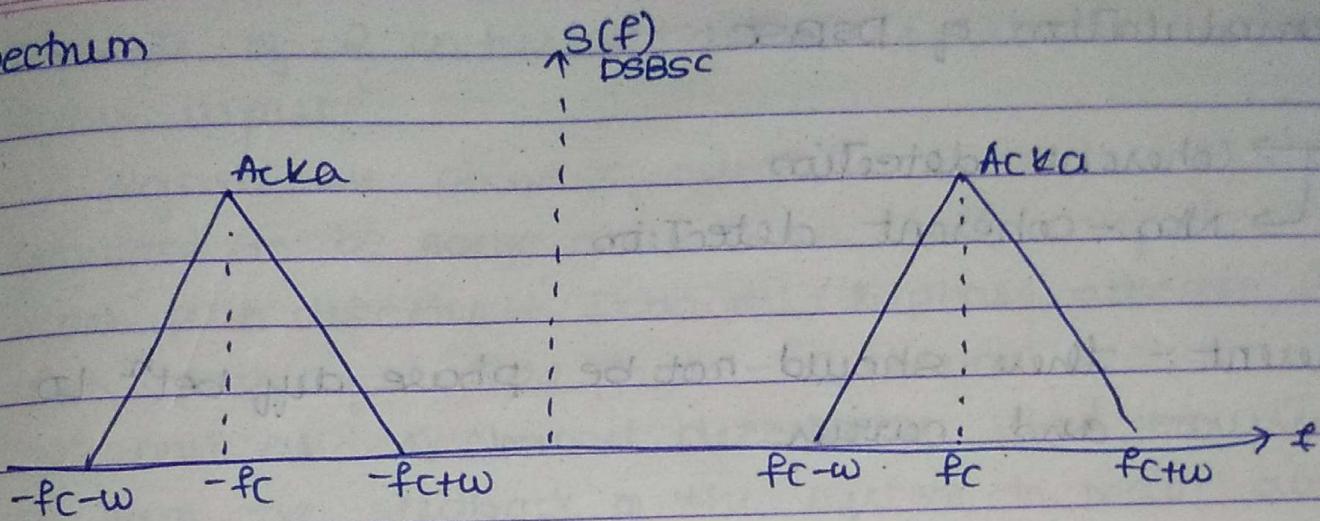
$$\begin{aligned} s(f) &= \int_{-\infty}^{\infty} s(t) e^{-j 2\pi f t} dt \\ &= \int_{-\infty}^{\infty} 2 A_c k_a m(t) \cos 2\pi f_c t e^{-j 2\pi f t} dt \end{aligned}$$

$$= 2 A_c k_a \int_{-\infty}^{\infty} \left(e^{j 2\pi f_c t} + e^{-j 2\pi f_c t} \right) e^{-j 2\pi f t} dt$$

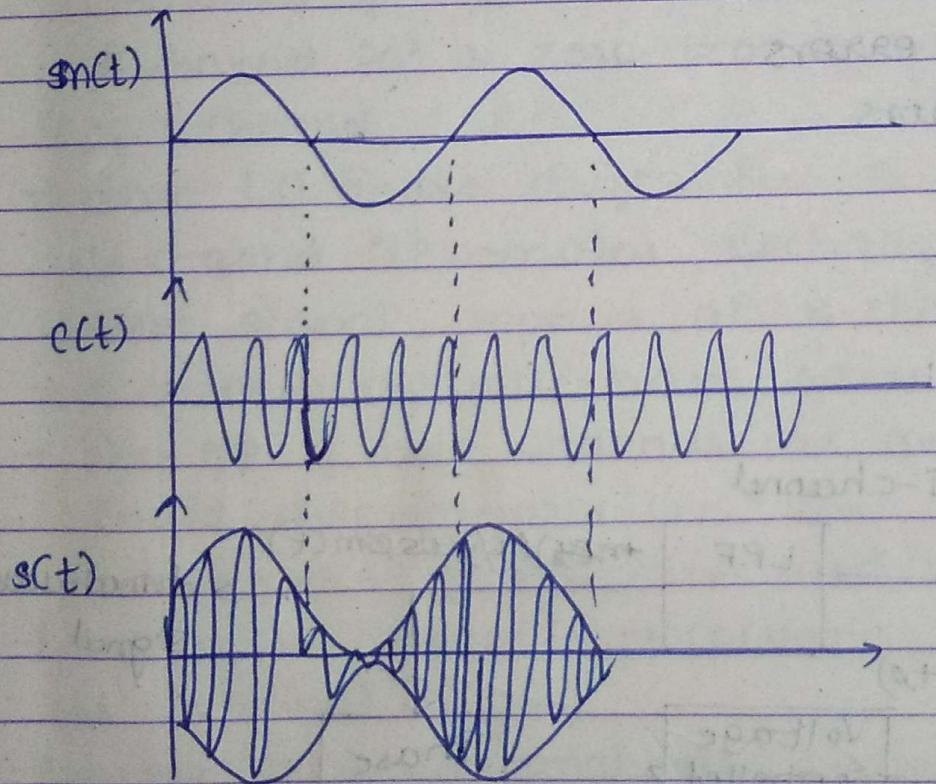
$$= A_c k_a \int_{-\infty}^{\infty} e^{j 2\pi (f - f_c) t} + e^{-j 2\pi (f + f_c) t} dt$$

$$= A_c k_a M(f - f_c) + A_c k_a M(f + f_c)$$

Spectrum



waveform



Demodulation of DSBSC

- Coherent detection
- Non-coherent detection

Coherent :- there should not be phase diff betn LO and carrier

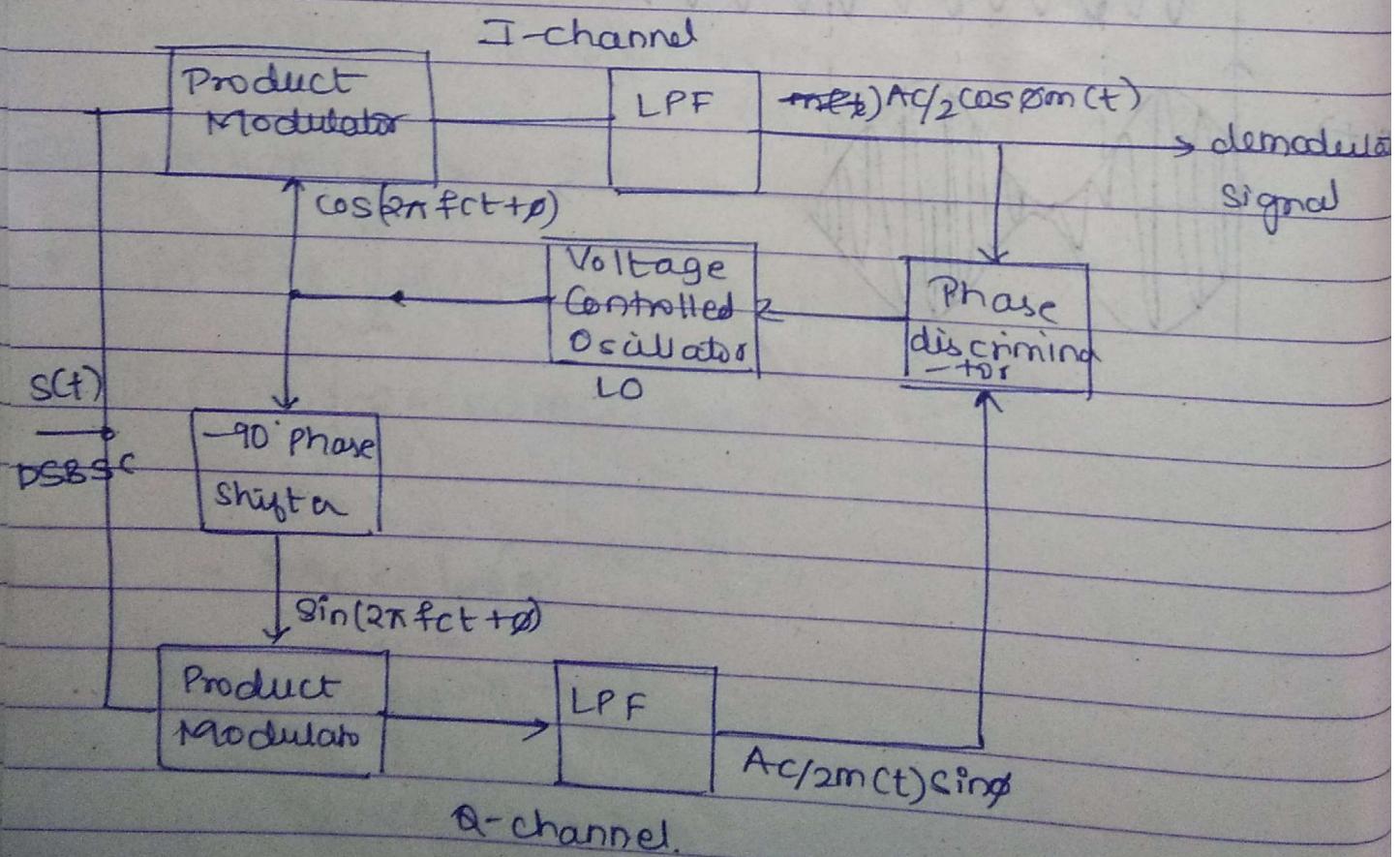
Non-coherent :- The π can be.

→ OR there can be no oscillator.

Errors → frequency errors
↳ phase errors

Coastas Receiver

Coherent receiver:



- consists of 2 coherent detectors supplied with same input.
- LO signals are phase quadrature to each other
- adjusted to be same as carrier frequency f_c .
- upper path detector - I channel / inphase detector
- lower path quadrature phase - Q channel detector
- I channel and Q channel detector are weakly coupled to form negative feedback of the system to maintain LO synchronous with carrier.
- when LO is in phase with f_c
 - I-channel O/P contains desired demodulated signal
 - Q channel O/P is zero bcoz of quadrature null effect of Q channel
- when LO phase drifts from its proper value by θ
 - I-channel O/P remains unchanged
 - some signal appears at Q-channel ~~$\sin \theta/2$~~ $\propto \sin \theta/2$
- Q channel O/P will have same polarity as I-channel
- The O/P of both channels are combined in Phase discriminator
 - ↳ consists of multiplier and LPF
- DC control signal - proportional to phase error θ is obtained as O/P.
- hence receiver automatically corrects for phase errors.
- Phase lock is ceased with modulation and has to be reestablished with the reappearance of modulation.

Quadrature Null effect:

- caused due to phase error in DSBSC.
- due to disturbance in the channel.
- phase error reduces O/P of demodulator
- phase error 90° output is 0
- phase error 0° output is maximum.

Single sideband Modulation

Single sideband suppressed carrier SSBSC

- Standard AM and DSBSC require bandwidth twice of message bandwidth hence wastage of bandwidth
- One half of transmission bandwidth is occupied by US and other half by LSB
- Both are uniquely related by virtue of symmetry property about f_c
- Given any one the other can be recovered
- In SSBSC only one side band is transmitted the other SB and carrier are suppressed thus the channel need to provide bandwidth same as that of the message bandwidth elimination of high power carrier wave.
- Disadvantage: cost and complexity

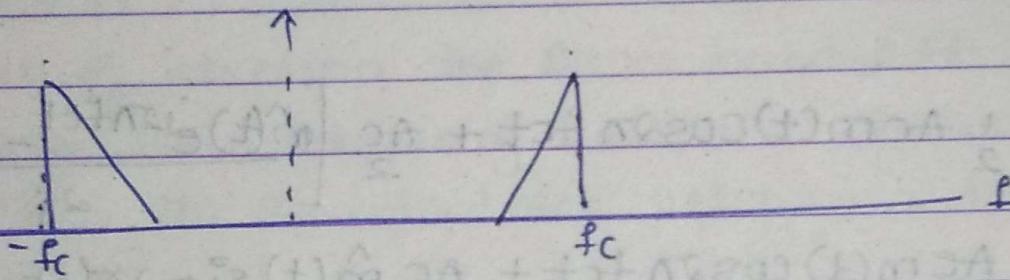
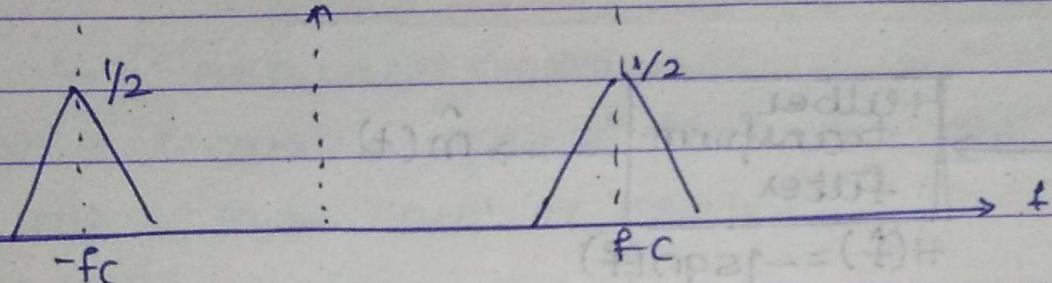
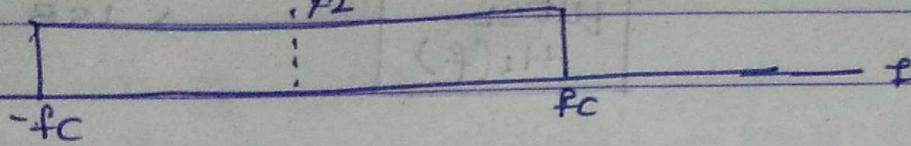
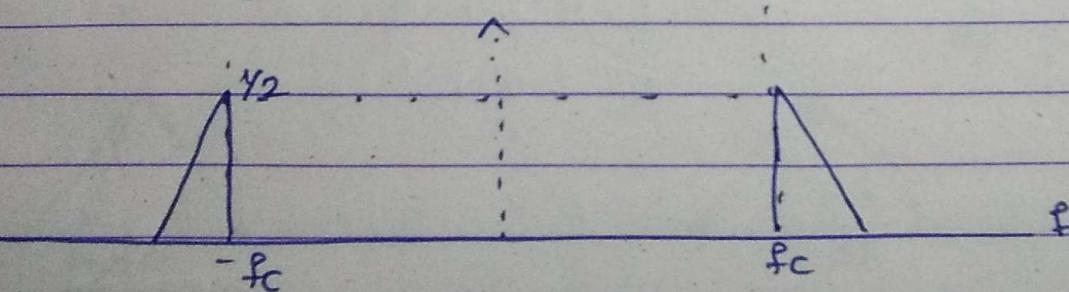
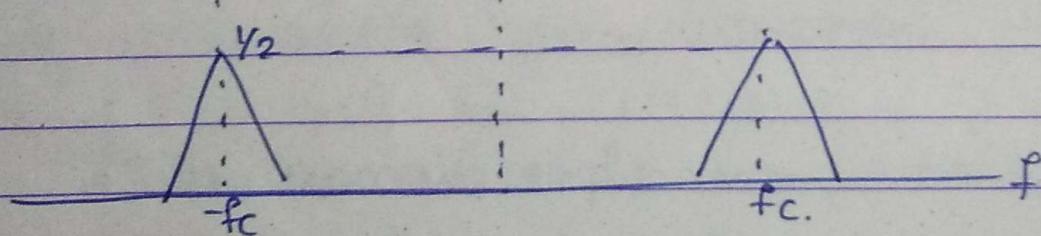
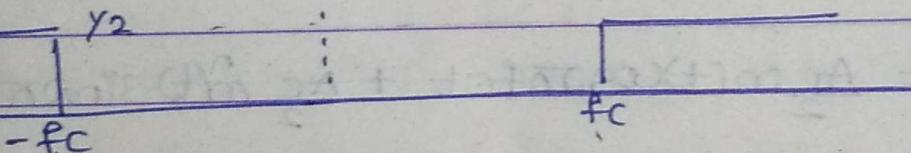
Generation of SSBSC.

LSB

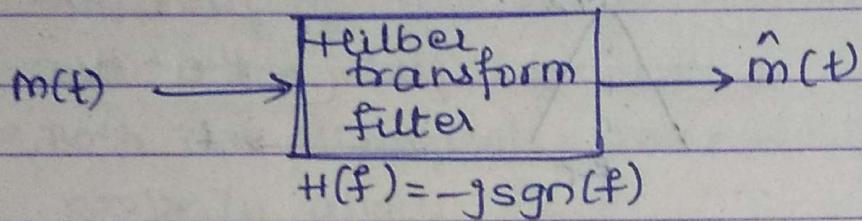
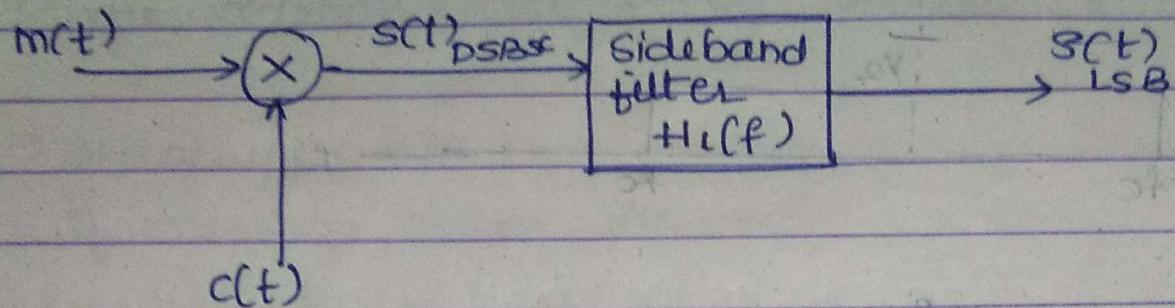
Side band filtering frequency:

Hilbert filter.

$$H_1(f) = \frac{1}{2} [\text{Sgn}(f+f_c) - \text{Sgn}(f-f_c)]$$

$H_L(f)$  $H_U(f)$ 

Block diagram



$$s(t)_{LSB} = \frac{1}{2} A_c m(t) \cos 2\pi f_c t + \frac{A_c}{2} \left[\hat{m}(t) e^{j 2\pi f_c t} - \hat{m}(t) e^{-j 2\pi f_c t} \right]$$

$$s(t)_{LSB} = \frac{A_c}{2} m(t) \cos 2\pi f_c t + \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

$$s(t)_{USB} = \frac{A_c}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

$$s(t)_{SSBSC} = \frac{A_c}{2} m(t) \cos 2\pi f_c t \pm \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

Vestigial side band Modulation

VSBSC: Vestigial side band suppressed carrier

→ overcome problem of filter.

→ extremely low frequencies signal is lost (TV, wideband)

compromise bet' SSB and DSBSC

one sideband is completely passed whereas the traces or vestige of other side band is retained.

$$B = \text{not } \delta f$$

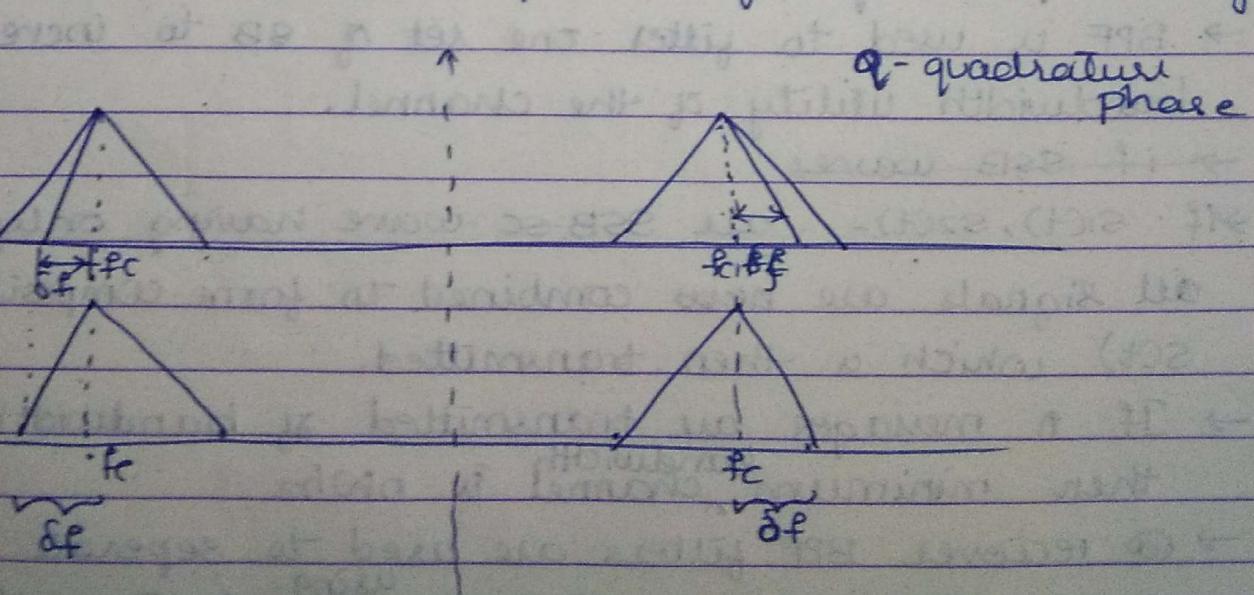
It has virtue of covering the same bandwidth as SSB while retaining low frequency baseband characteristic of DSBSC. Thus its standard for television transmission and similar ex

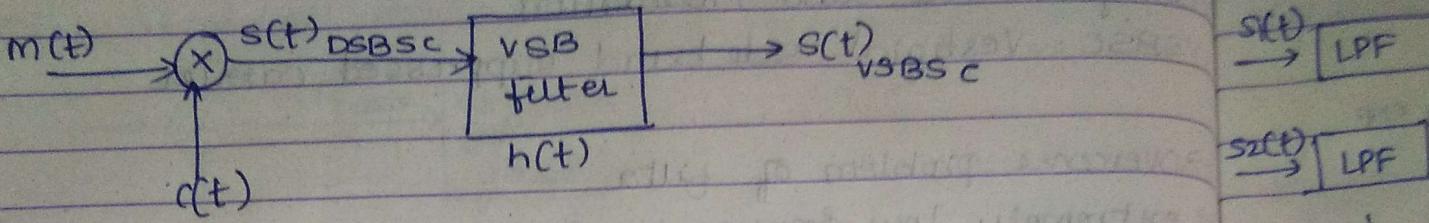
$$S(t)_{VSB} = \frac{A_c m(t) \cos 2\pi f_c t}{2} + \frac{A_c m_Q(t) \sin 2\pi f_c t}{} \quad (1)$$

↳ Time domain expⁿ having LSB and USB vestig

$$S(t)_{VSB} = \frac{A_c m(t) \cos 2\pi f_c t}{2} - \frac{A_c m_Q(t) \sin 2\pi f_c t}{} \quad (2)$$

↳ Time domain expⁿ having VSB and LSB vestig



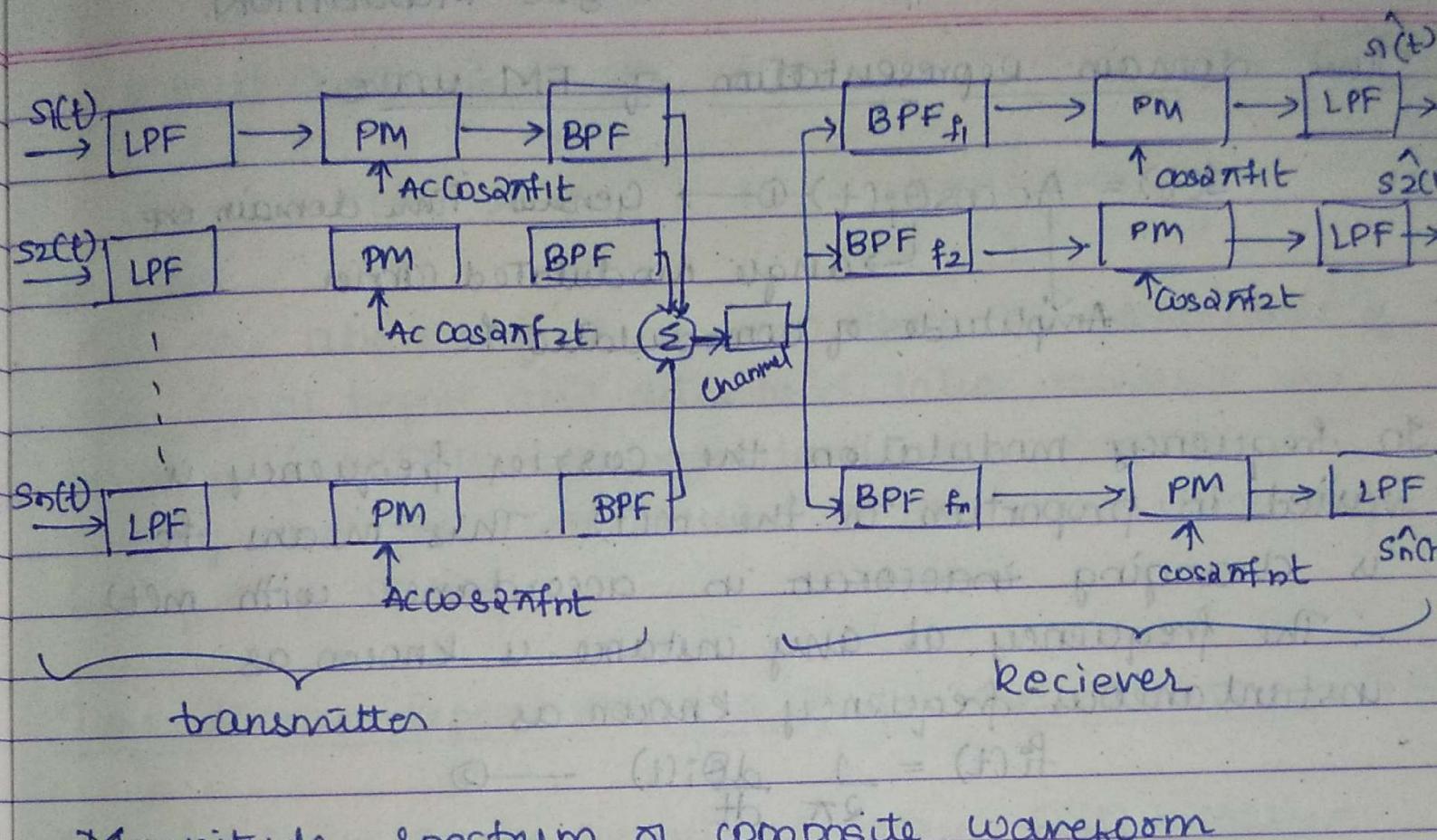


Frequency Division Multiplexing:

Multiplexing is a technique where a number of independent signals can be combined into a composite signal suitable for transmission over a single communication channel.

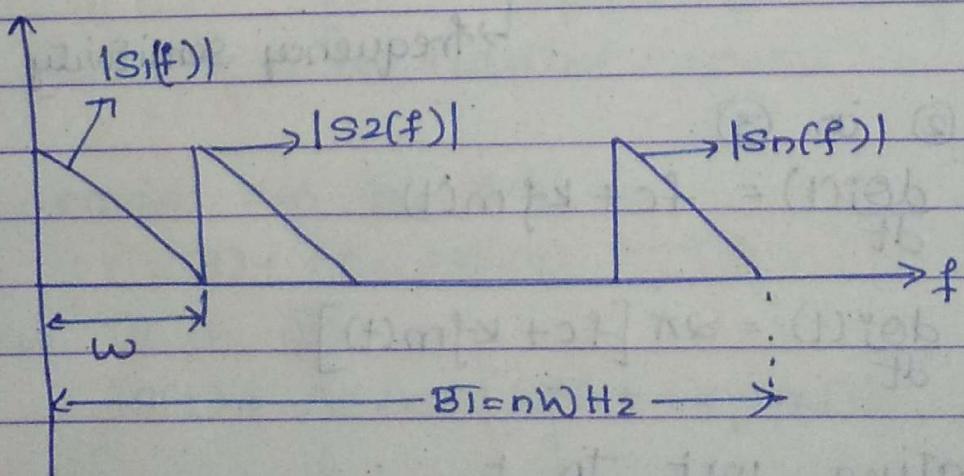
The technique of separating signal spectrum in frequency domain is called FDM.

- incoming message signal are assumed to be of LPF type
- LPF designed to remove high frequency component that donot contribute to message spectrum but is capable of disturbing other msg signal in the channel
- The filtered signals are modulated to carrier freq the resulting waves are DSBSC and donot overlap
- BPF is used to filter one set of SB to increase bandwidth utility of the channel.
- if SSB waves
- if $s_1(t), s_2(t), \dots$ are SSB-SC wave having only USB all signals are now combined to form composite signal $s(t)$ which is then transmitted.
- If n messages are transmitted of bandwidth w Hz then minimum ^{bandwidth} channel is nW Hz
- At receiver BPF filters are used to separate modulated signals & then by ^{using} detectors it is possible to recover original signal



+ Magnitude spectrum of composite waveform
 $s(t) = s_1(t) + s_2(t) + \dots + s_n(t)$

for the freq



Chapter-II

PRINCIPLES OF ANGLE MODULATION.

Time domain representation of FM wave:

$$s(t) = A \cos \theta_i(t) \quad \text{--- (1)}$$

Angle modulated carrier

Amplitude of unmodulated f_c

In frequency modulation the carrier frequency is varied in proportion to the $m(t)$. This means f_c is changing in accordance with $m(t)$. The frequency at any instance is known as instantaneous frequency known as

$$f_i(t) = \frac{1}{2\pi} \frac{d\theta_i(t)}{dt} \quad \text{--- (2)}$$

$f_i(t)$ is linearly varied with $m(t)$ \therefore

$$\therefore f_i(t) = f_c + k_f m(t) \quad \text{--- (3)}$$

frequency sensitivity h^2/V

Sub (2) in (3)

$$\frac{1}{2\pi} \frac{d\theta_i(t)}{dt} = f_c + k_f m(t)$$

$$\frac{d\theta_i(t)}{dt} = 2\pi [f_c + k_f m(t)]$$

Integrating wrt to t

$$\int \frac{d\theta_i(t)}{dt} dt = \int_0^t 2\pi [f_c + k_f m(t)] dt$$

$$\theta_i(t) = 2\pi \int_0^t [f_c + k_f m(t)] dt$$

$$\theta_i(t) = \int_0^t 2\pi f_c + 2\pi k_f m(t) dt$$

$$\theta_i(t) = 2\pi f_c t + 2\pi k_f \int_0^t m(t) dt \quad \text{--- (4)}$$

substituting ④ in ①

$$s(t) = A \cos [2\pi f_c t + 2\pi k_f \int m(t) dt]$$

Non linear function

Conclusion

from the above eq it is seen that the Amplitude of the signal before and after modulation remains the same. If $m(t)$ is varying instantaneous frequency is varying and the zero crossing of FM wave is no longer having same spacing.

Time domain representation of Phase Modulated Waves (PM)

here the phase of the modulated carrier $\phi_i(t)$ is varied in accordance with $m(t)$

$$\phi_i(t) = 2\pi f_c t + k_p m(t) \quad \text{--- ①}$$

\downarrow

phase sensitivity - radians/volt
phase of unmodulated carrier

time domain exp for PM

$$s(t) = A \cos \phi_i(t) \quad \text{--- ②}$$

sub ① in ②

$$s(t) = A \cos [2\pi f_c t + k_p m(t)]$$

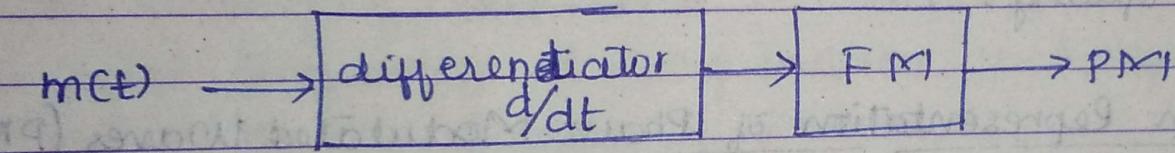
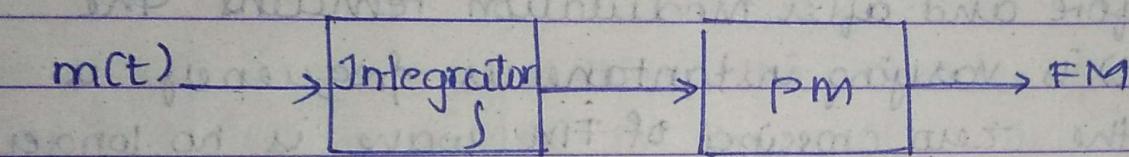
Conclusion:

→ The envelope of PM wave is a constant equal to the amp of unmodulated carrier

→ The zero crossing of PM is no longer in their regular spacing. bcoz the instantaneous freq of PM is proportional to the time derivative of $m(t)$

- * In FM and PM $\theta_i(t)$ changes but in diff man
- * In FM $\theta_i(t)$ is directly proportional to Integral of $m(t)$
- * " PM $\theta_i(t)$ " " " " " derivative " "

Block diagram



Frequency deviation and Modulation index (β)

Consider single tone modulating signal

$$m(t) = A_m \cos 2\pi f_m t \quad \text{--- (1)}$$

$$s(t) = A_c \left[\cos 2\pi f_c t + 2\pi k_f \int_0^t m(t) dt \right] \quad \text{--- (2)}$$

Sub (1) in (2)

$$s(t) = A_c \left[\cos 2\pi f_c t + 2\pi k_f \int_0^t A_m \cos 2\pi f_m t dt \right]$$

$$= A_c \left[\cos 2\pi f_c t + 2\pi k_f \cdot A_m \cdot \frac{\sin 2\pi f_m t}{2\pi f_m} \right]$$

$$= A_c \left[\cos 2\pi f_c t + k_f \frac{A_m}{f_m} \sin 2\pi f_m t \right]$$

$$= A_c \left[\cos 2\pi f_c t + k_f \frac{A_m}{f_m} \sin 2\pi f_m t - \sin 0 \right]$$

$$= A_c \left[\cos 2\pi f_c t + k_f \frac{A_m}{f_m} \sin 2\pi f_m t \right]$$

$k_f A_m = \Delta f$ — frequency deviation

$$= A_c \left[\cos 2\pi f_c t + \frac{\Delta f}{f_m} \sin 2\pi f_m t \right]$$

$\frac{\Delta f}{f_m} = \beta$ — modulation index

$$= A_c \left[\cos 2\pi f_c t + \beta \sin 2\pi f_m t \right]$$

$\Delta f \Rightarrow$ frequency deviation is the maximum departure of instantaneous freq of the resulting fm signal from f_c

$$\Delta f = |f_i(t) - f_c|_{\max}$$

$$= k_f A_m$$

Modulation Index $B = \frac{k_f A_m}{f_m}$

$$B = \frac{\Delta f}{f_m}$$

* $B < 1$ rad NBFM

$B > 1$ rad WBFM.

Narrow band frequency Modulation

has narrow bandwidth which is equal to twice msg signal.

Time domain exp of FM

$$s(t) = A_c \cos \theta_i(t) \quad \text{--- (1)}$$

for single tone sinusoidal modulation

$$\theta_i(t) = 2\pi f_c t + \beta \sin 2\pi f_m t \quad \text{--- (2)}$$

$$\therefore s(t) = A_c \cos [2\pi f_c t + \beta \sin 2\pi f_m t] \quad \text{FM}$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$s(t) = A_c \left[\cos [2\pi f_c t] \cos (\beta \sin 2\pi f_m t) - \sin 2\pi f_c t \sin (\beta \sin 2\pi f_m t) \right]$$

since $\sin \theta \approx \theta$

$\cos \theta \approx 1$

$\beta \ll 1$

$$f_c + f_m - f = 0$$

$$f_c + f_m = f$$

$$\cos(B \sin 2\pi f_m t) \approx 1$$

$$\sin(B \sin 2\pi f_m t) \approx B \sin 2\pi f_m t$$

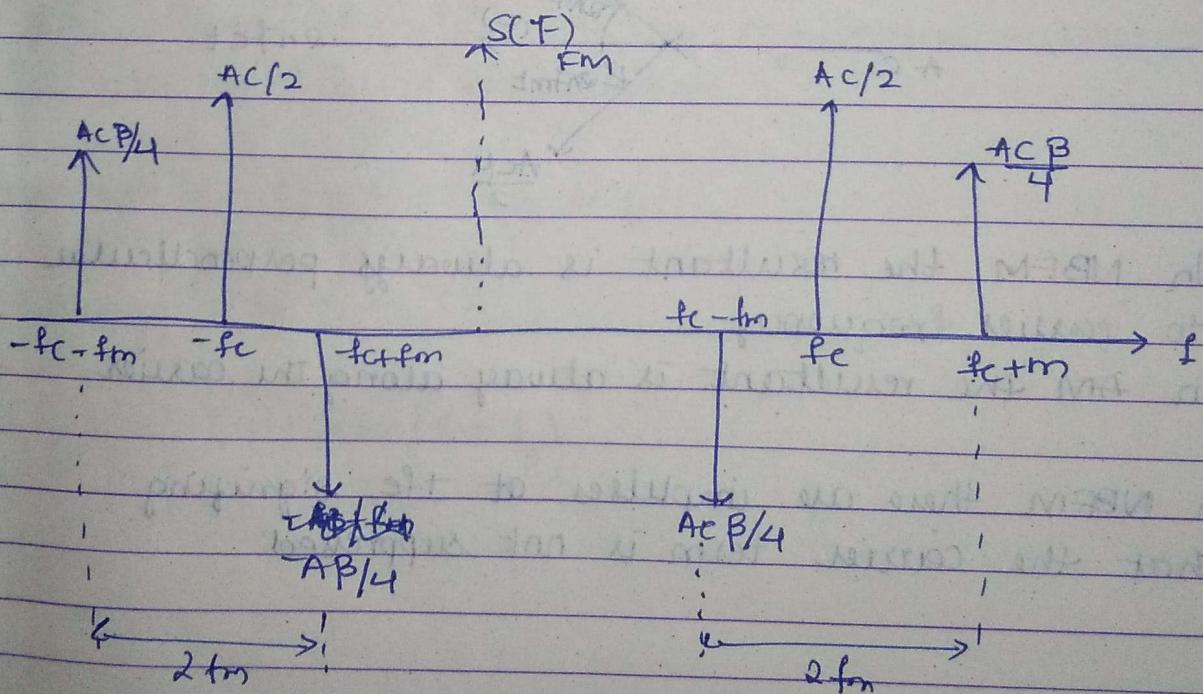
$$s(t) = \underset{f_m}{A c} [\cos 2\pi f_c t - \sin 2\pi f_c t B \sin 2\pi f_m t]$$

$$= A c \cos 2\pi f_c t - A c B \sin 2\pi f_c t \sin 2\pi f_m t$$

$$\sin A \sin B = -\frac{1}{2} (\cos(A+B) - \cos(A-B))$$

$$s(t)_{f_m} = A c \cos 2\pi f_c t + \frac{A c B}{2} \cos(2\pi f_c t + 2\pi f_m t) - \frac{A c B}{2} \cos(\frac{2\pi f_c t}{2\pi f_m t})$$

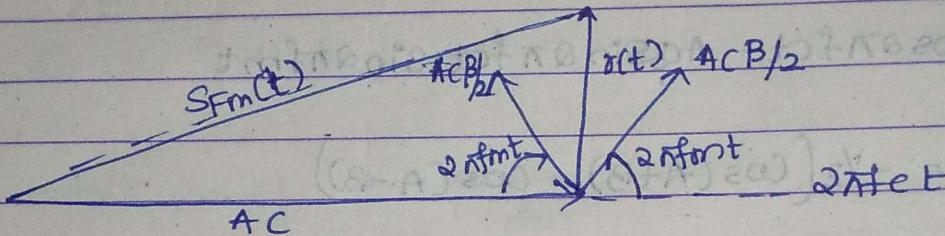
$$s(f)_{f_m} = \frac{A c}{2} [\delta(f + f_c) + \delta(f - f_c)] + \frac{A c B}{4} [\delta(f_c + f_m - f) + \delta(f_c + f_m + f)] - \frac{A c B}{4} [(f_c - f_m - f) + (f_c + f_m + f)]$$



$$o = f - \frac{f_m^2}{2} + \frac{f_m^2}{2}$$

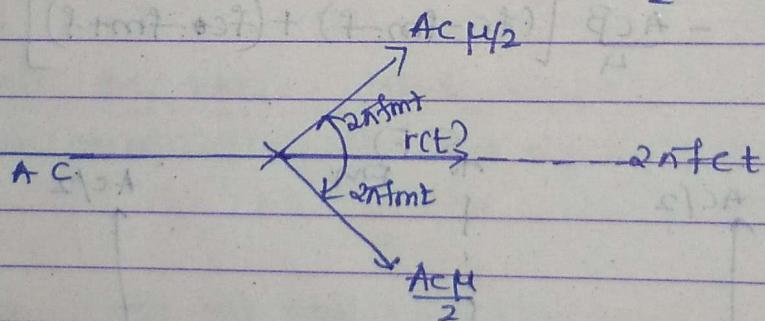
Phasor for NBFM

$$S_{FM}(t) = A_C \cos 2\pi f_c t + \frac{A_C}{2} \cos 2\pi (f_c + f_m) t - \frac{A_C}{2} \cos 2\pi (f_c - f_m) t$$



Phasor for conventional AM

$$s(t) = A_C \cos 2\pi f_c t + A_C \frac{\mu}{2} \cos 2\pi (f_c + f_m) t + A_C \frac{\mu}{2} \cos 2\pi (f_c - f_m) t$$



In NBFM the resultant is always perpendicular to carrier frequency

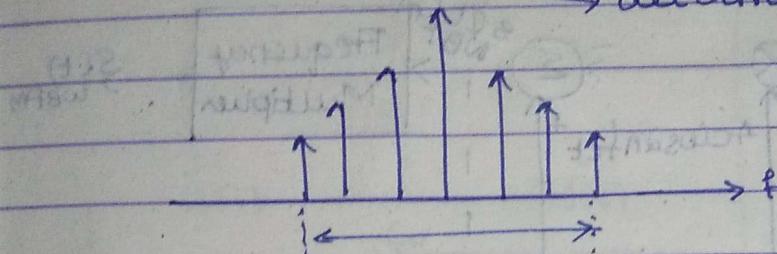
In AM the resultant is always along the carrier

In NBFM there are impulses at f_c signifying that the carrier term is not suppressed.

WBFM - Wide band FM

$$s(t) = A_c \sum_{n=-\infty}^{\infty} J_n(B) \cos [2\pi(f_c + n f_m)t]$$

determine the amplitude of
 n^{th} sideband



side band power is increasing @ the rate of carrier components hence the power is same

→ Amplitude Spectrum of FM signals contains a carrier component and an infinite set of side frequencies symmetrical on both sides

→ $B < 1$ $J_0(B)$ has significant value. and the FM signal comprises of f_c , $f_c + f_m$, $f_c - f_m$

→ $B > 1$, $J_0(B), J_1(B) \dots J_n(B)$ has significant values has ~~only~~ infinite Sidebands

Transmission Bandwidth of FM

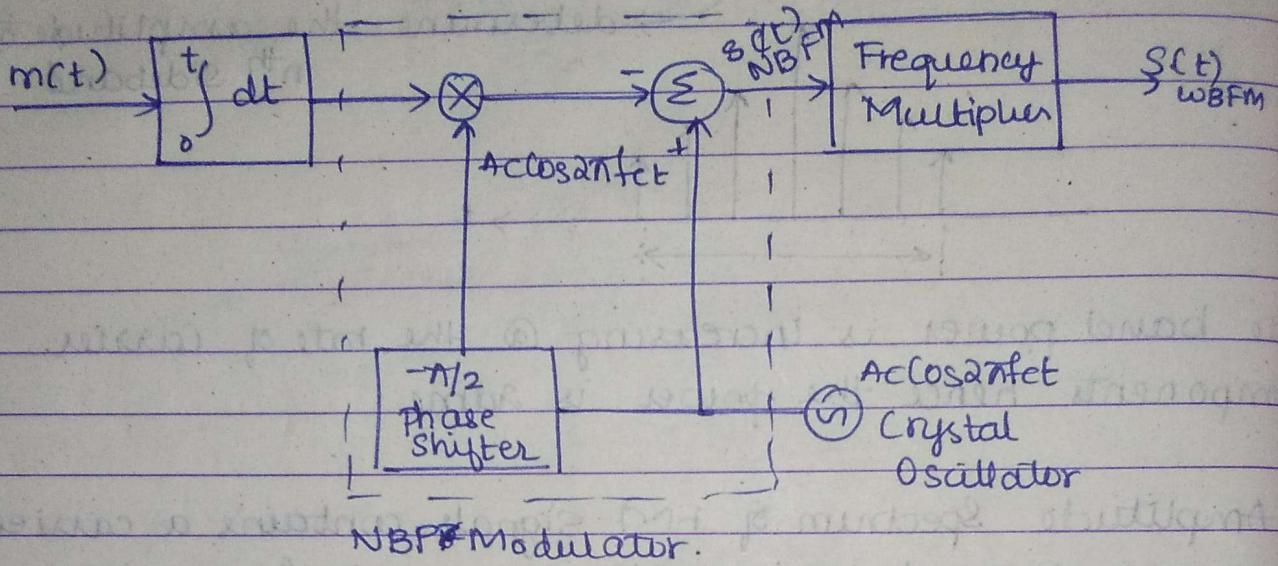
Carson's Rule:

$$BT = 2(\Delta f + f_m)$$

$$BT = 2\Delta f \left(1 + \frac{1}{B}\right)$$

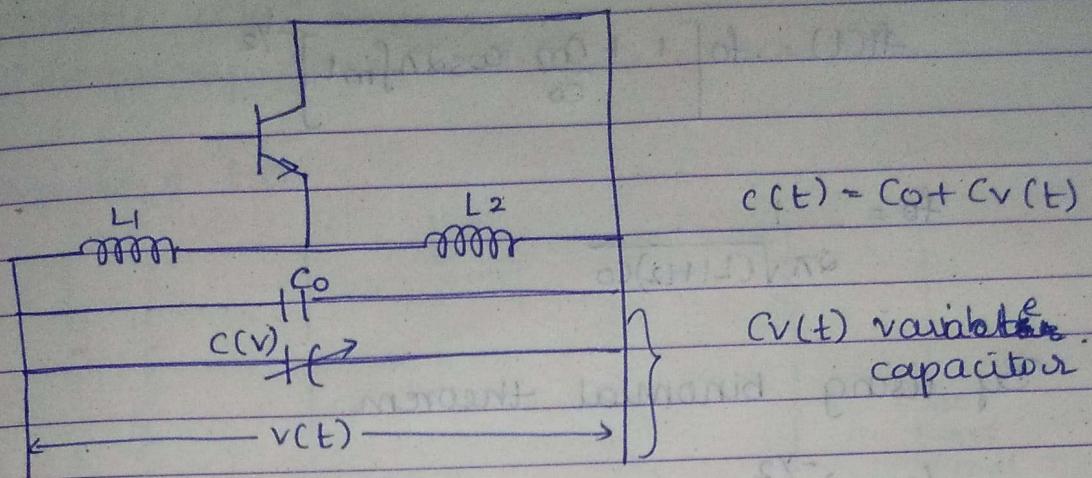
Generation of FM waves

Indirect Method of Generating FM waves



- A narrow band FM signal is generated using by integrating $m(t)$ and then using $\int m(t) dt$ to phase modulate the carrier generated by crystal oscillator.
- $k_p m(t) \ll 1$ in order to minimize distortion in PM.
- The NBFM thus generated is applied to frequency multiplier to increase the frequency deviation to desired level.
- Frequency Multiplier should ensure that it provides the desired frequency deviation and carrier simultaneously.

Direct Method of generating FM waves.



- The instantaneous freq of the carrier is varied in accordance with $m(t)$ this is achieved by VCO
- VCO may be constructed using sinusoidal oscillator with a highly resonant n/w
- A fixed capacitor in parallel with variable voltage known as varactor can be used in frequency selective n/w.
- Capacitance of RB varactor diode depends on the voltage applied at the pn junction
Larger vtg \rightarrow less small is its transition capacitance

→ ~~Max~~ total capacitance

$$C(t) = C_0 + C_m \cos 2\pi f_m t$$

$$C(t) = C_0 + C_m \cos 2\pi f_m t \quad \text{--- (1)}$$

↓

Max change in total capacitance
total capacitance
in absence of Modulation

$$f_p(t) = \frac{1}{2\pi \sqrt{L_1 + L_2} C(t)} \quad \text{--- (2)}$$

Sub ① in ②

$$f(t) = f_0 \left[1 + \frac{cm}{co} \cos 2\pi f_m t \right]^{-\gamma_2}$$

$$f_0 = \frac{(f_1)}{2\pi\sqrt{(L_1+L_2)co}}$$

By using binomial theorem.

$$(1+x)^{-\gamma_2} = 1 - \frac{1}{2}x \quad \text{if } |x| \ll 1$$

$$\text{if } \left| \frac{cm}{co} \right| \ll 1$$

$$f(t) = f_0 \left[1 - \frac{cm}{2co} \cos 2\pi f_m t \right]$$

$$\text{let } \frac{\Delta f}{f_0} = -\frac{cm}{2co}$$

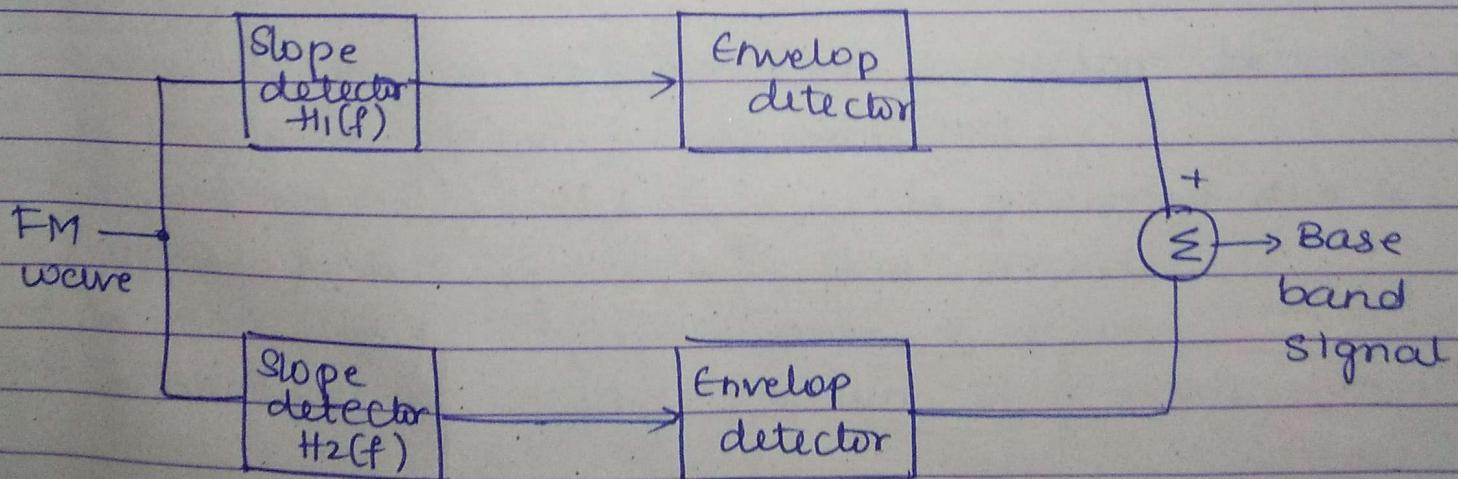
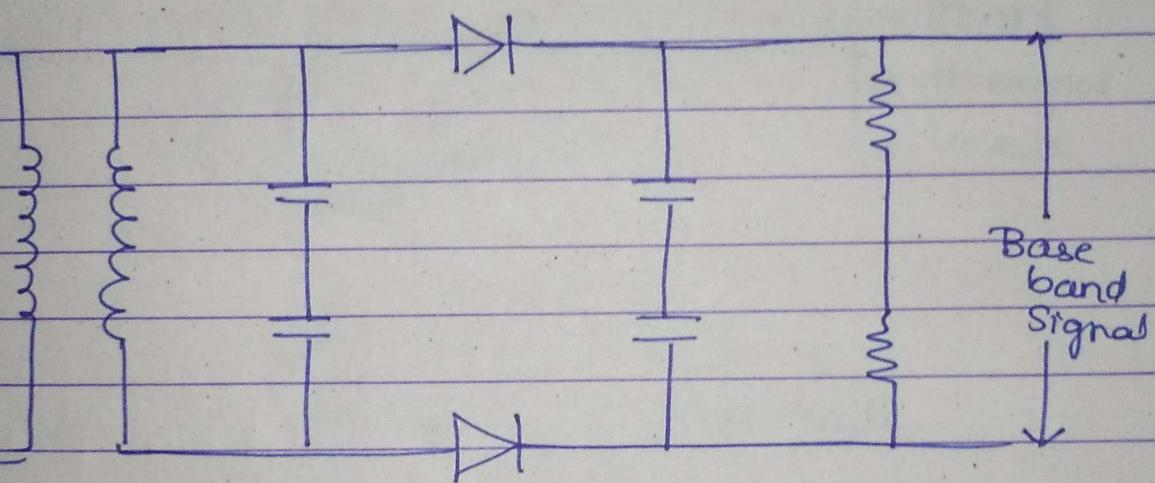
$$\therefore f(t) = f_0 - \Delta f \cos 2\pi f_m t$$

Demodulation of FM

→ Phase locked loop

→ frequency discriminator → Balance FD

Balanced FD



Demodulation of FM waves

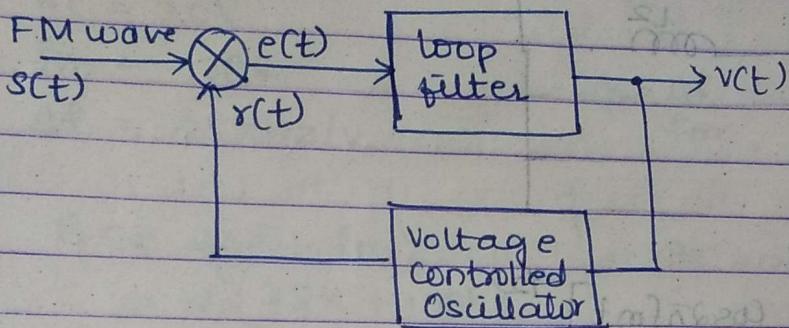
→ Phase locked loop (PLL)

→ Frequency discriminator

→ Balanced frequency discrimination

* Phase locked loop (PLL)

Block diagram:



It's a -ve feedback system

consists of 3 major components → Multiplier

→ loop filter

→ Voltage controlled oscillator

All the 3 components are connected together to form a feedback network

VCO is a sine wave generator → whose frequency is determined by the voltage applied external to it

Initially it's assumed that VCO is adjusted and control voltage is zero : two conditions are

satisfied i) VCO frequency and f_c (unmodulated) are precisely set 2) VCO o/p has 90° phase shift with respect to unmodulated carrier f_c

$$s(t) = A \cos(\omega f_c t + \phi_1(t)) \quad \text{--- (1)}$$

be the input signal

VCO o/p is defined as

$$r(t) = A_v \cos(\omega f_c t + \phi_2(t)) \quad \text{--- (2)}$$

both these signals are applied to multiplier producing the following two components

1) high frequency component

$$k_m A_c A_v \cos [4\pi f_c t + \phi_1(t) + \phi_2(t)]$$

2) low frequency component

$$k_m A_c A_v \cos [\phi_1(t) - \phi_2(t)]$$

k_m - multiplier gain

high frequency component is eliminated by low pass action of the filter and VCO...: Input to the loop filter is

$$e(t) = k_m A_c A_v \cos [\phi_e(t)] \quad \text{--- (3)}$$

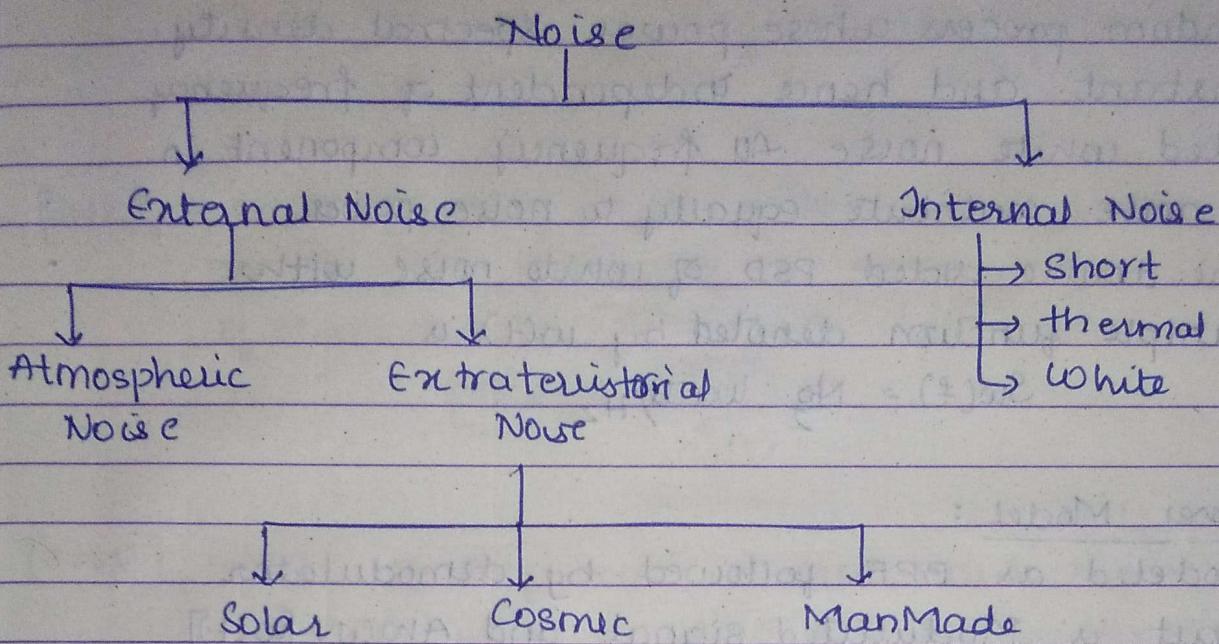
$\phi_e(t)$ \rightarrow phase error

The loop filter operates on its input to produce the output

$$v(t) = A_m \cos 2\pi f_m t$$

Chapter 3

NOISE & EFFECT OF NOISE ON RECEIVER



Short Noise:

- appears in active device due to random behaviour of change in charge carriers and holes
- In vacuum tubes short noise is generated due to random emission of electrons from cathode
- In SCD due to random diffusion of electrons.
- In photodiode random emission of photons

Thermal Noise:

- generated due to random movement of electrons inside the volume of conductors or resistor even in the absence of electric field or potential diff.
- The motion of free electron is due to thermal energy path of individual electron is random or zigzag
Bcoz of random movement of electrons there will be random fluctuations of currents & voltages

white noise:

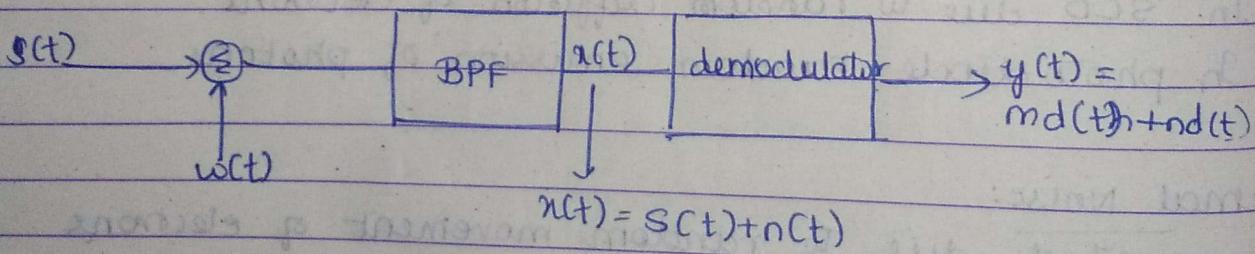
A random process whose power spectral density is constant and hence independent of frequency is called white noise. All frequency component in white noise contribute equally to noise power.

The double sided PSD of white noise with a sample function denoted by $w(t)$ is

$$S_w(f) = \frac{N_0}{2} \text{ watt/Hz}$$

Receiver Model:

- Modeled as BPF followed by demodulator
- input is Modulated signal and AWGN [$w(t)$]
- $w(t)$ accounts for channel noise & receiver noise called front-end noise.
- Bandwidth of BPF is equal to transmission bandwidth of modulated signal $s(t)$
- Hence modulated signal is passed without distortion while AWGN is within the Bandwidth of BPF



$$x(t) = s(t) + n(t)$$

$$n(t) = n_c \cos \omega_f t - n_s \sin \omega_f t$$

$n_c(t)$ & $n_s(t)$ are in phase quadrature component wrt $\cos \omega_f t$

$\text{SNR} = \frac{\text{ratio of average power of the modulated signal } s(t)}{\text{to the average power of the filtered noise } n(t)}$

$[\text{SNR}]_o = \frac{\text{ratio of avg power of the demodulated signal}}{\text{to the avg power of the noise at the output of demodulator}}$

$$[\text{SNR}]_o = \frac{m^2 d(t)}{n_d^2(t)}$$

$[\text{SNR}]_c = \frac{\text{ratio of avg power of modulated signal}}{\text{average power of noise in a Bandwidth of } 10\text{Hz}}$

$$\begin{aligned} [\text{SNR}]_c &= \frac{s^2(t)}{n^2(t)} \\ &= \frac{s^2(t)}{N_0 W} \end{aligned}$$

Figure of Merit $\gamma = \frac{[\text{SNR}]_o}{[\text{SNR}]_c}$

$\gamma > 1 \quad [\text{SNR}]_o > [\text{SNR}]_c \quad \gamma \text{ is desirable}$

$\gamma = 1 \quad [\text{SNR}]_o = [\text{SNR}]_c \quad " " \quad \text{permissible}$

$\gamma < 1 \quad [\text{SNR}]_o < [\text{SNR}]_c \quad " " \quad \text{not "}$

* Avg power of $m(t)$

$$P_m = \overline{m^2(t)}$$

* Avg power of $km(t)$

$$\begin{aligned} \overline{[km(t)]^2} &= \overline{k^2 m^2(t)} \\ &= k^2 P_m \end{aligned}$$

* Avg power of $A \cos 2\pi f_m t$

$$= (A \cos 2\pi f_m t)^2$$

$$= \left(\frac{Am}{r_2}\right)^2$$

$$= \frac{Am^2}{2}$$

* Avg power of $km(t) \cos 2\pi f_m t$

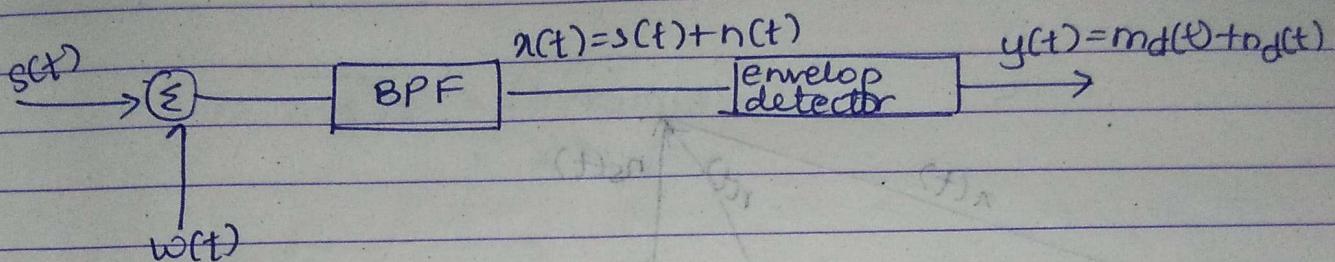
$$= \overline{(km(t) \cos 2\pi f_m t)^2}$$

$$= k^2 \overline{P_m} \frac{Am^2}{2}$$

$$= k^2 P_m \left(\frac{Am}{r_2}\right)^2$$

$$= \frac{k^2 P_m}{2} A^2$$

Noise in AM Receivers



$$s(t) = A \{ 1 + k_a m(t) \} \cos 2\pi f_c t$$

$$[\text{SNR}]_c = \frac{\overline{s(t)^2}}{N_{\text{ow}}}$$

$$\begin{aligned}\overline{s(t)^2} &= \overline{(A_c \cos 2\pi f_c t)^2} + \overline{(A_c k_a m(t) \cos 2\pi f_c t)^2} \\ &= \frac{A_c^2}{2} + \frac{A_c^2 k_a^2 P_m}{2} \\ &= \frac{A_c^2}{2} [1 + k_a^2 P_m]\end{aligned}$$

$$[\text{SNR}]_c = \frac{A_c^2}{2 N_{\text{ow}}} [1 + k_a^2 P_m]$$

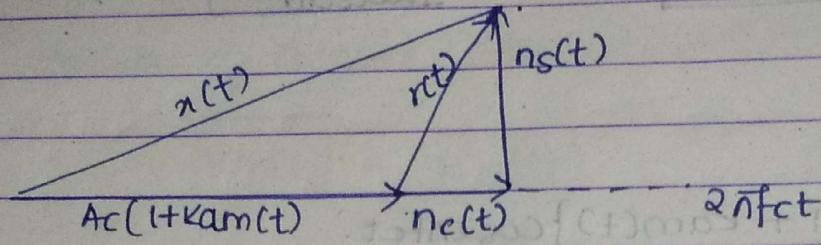
$n(t)$ appearing @ BPF

$$n(t) = n_c(t) \cos 2\pi f_c t - n_s(t) \sin 2\pi f_c t$$

Input to demodulator of AM receiver.

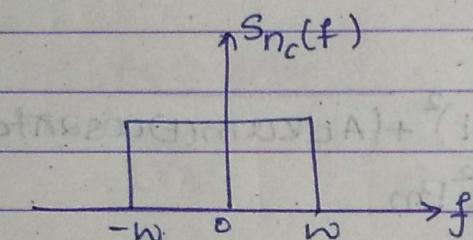
$$\begin{aligned}x(t) &= s(t) + n(t) \\ &= A_c [1 + k_a m(t)] \cos 2\pi f_c t + n_c(t) \cos 2\pi f_c t - \\ &\quad n_s(t) \sin 2\pi f_c t\end{aligned}$$

Phasor diagram
for $x(t)$



$$Ac \gg n_s(t) \text{ & } n_c(t)$$

PSD of Noise / Noise spectrum



Output of envelope detector

$$y(t) = |x(t)|$$

$$= \sqrt{[Ac(1+Kam(t)) + n_c(t)]^2 + n_s^2(t)}$$

$$Ac \gg n_c(t) \text{ and } n_s(t)$$

$$= \sqrt{[Ac(1+Kam(t)) + n_c(t)]^2}$$

$$= Ac(1+Kam(t)) + n_c(t)$$

$$= Ac + Ackam(t) + n_c(t)$$

Passing through filter dc component is removed

$$y(t) = Ackam(t) + n_c(t) = m_d(t) + n_g(t)$$

$$[\text{SNR}]_o = \frac{\overline{m^2(t)}}{\overline{n_d^2(t)}}$$

$$\Rightarrow \overline{m^2(t)} = (\overline{A c k a m(t)})^2 \\ = A c^2 k a^2 P_m$$

$$\overline{n_d^2(t)} = \overline{n_c(t)^2} = N_0 2W$$

$$[\text{SNR}]_o = \frac{A c^2 k a^2 P_m}{N_0 2W}$$

$$\text{FOM} = \gamma = [\text{SNR}]_o$$

$$[\text{SNR}]_c$$

$$= \frac{A c^2 k a^2 P_m}{2 N_0 W}$$

$$\frac{A c^2}{2 N_0 W} [1 + k a^2 P_m]$$

$$= \frac{k a^2 P_m}{1 + k a^2 P_m}$$

Let $m(t)$ be single tone modulated signal

$$m(t) = A_m \cos \omega_n f_m t$$

$$\overline{m^2(t)} = \frac{A_m^2}{2} = P_m$$

$$\text{FOM} = \gamma = \frac{k a^2}{2} \frac{A_m^2}{P_m}$$

$$1 + k a^2 \frac{A_m^2}{P_m}$$

$$\Rightarrow \mu = k a A_m$$

$$= \frac{\mu^2 / 2}{1 + \mu^2 / 2} - \frac{\mu^2 / 2}{2 + \mu^2 / 2} \\ = \frac{\mu^2}{2 + \mu^2}$$

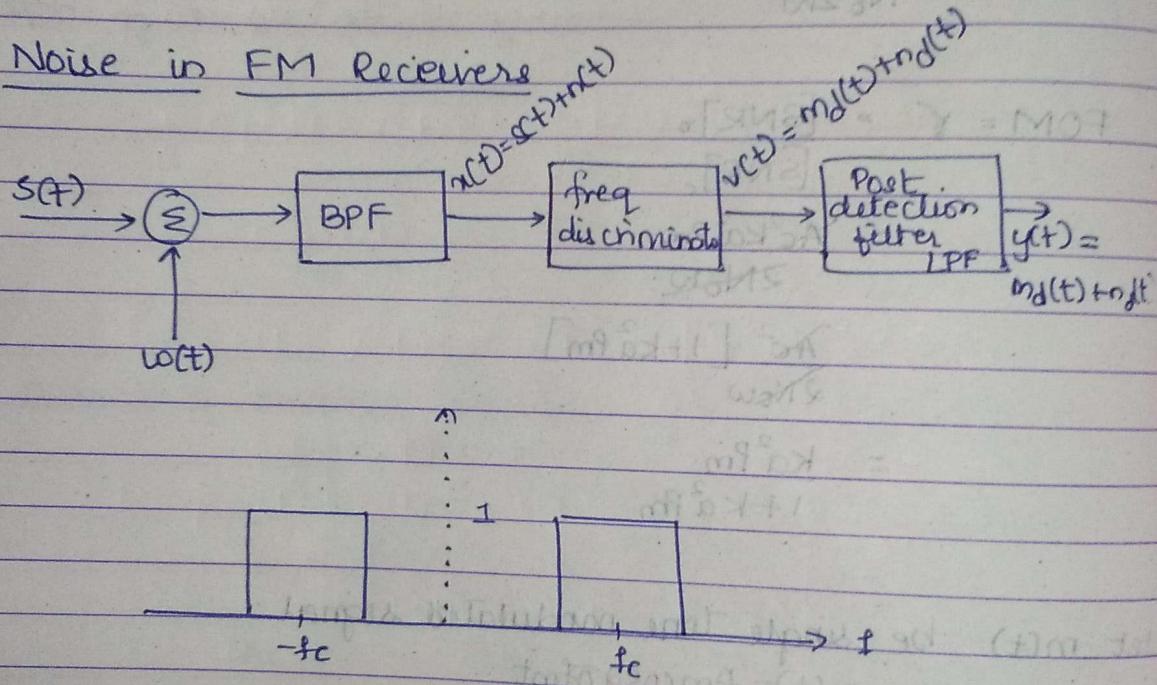
considering 100% modulation

$$\mu = 1$$

$$r = \frac{1}{2+1} = \frac{1}{3}$$

AM system must transmit 3 times as much avg power as suppressed carrier system to achieve same quality of performance.

Noise in FM Receiver



$$s(t) = A \cos[2\pi f_c t + \phi(t)]$$

$$\phi(t) = 2\pi k_f \int_0^t m(t) dt$$

$$[\text{SNR}]_c = \frac{\text{Avg power of } s(t)}{\text{Avg power of } n(t) \text{ in bandwidth}}$$

$$\text{Avg power of } s(t) = \overline{s^2(t)}$$

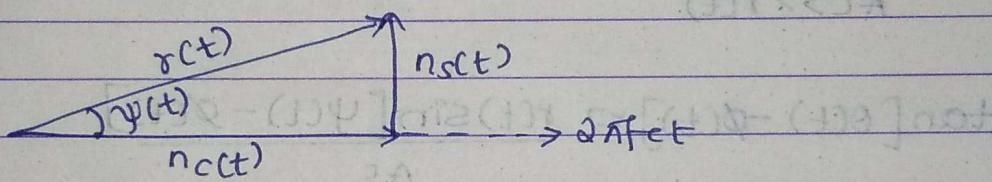
$$= \frac{A^2}{2}$$

$$\therefore \text{ " } n(t) = \overline{n^2(t)} \\ = N_0 W$$

$$[\text{SNR}]_c = \frac{A^2}{2 N_0}$$

$$n(t) = n_c(t) \cos 2\pi f_c t - n_s(t) \sin 2\pi f_c t$$

Phasor diagram for $n(t)$



$n(t)$ rewritten

$$n(t) = r(t) \cos[2\pi f_c t + \psi(t)]$$

↳ envelope of $n(t)$

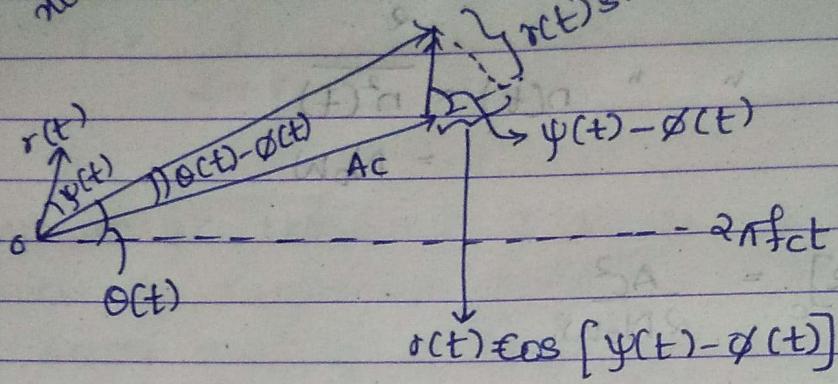
$$r(t) = \sqrt{n_c^2(t) + n_s^2(t)}$$

$$\psi(t) = \tan^{-1} \left[\frac{n_s(t)}{n_c(t)} \right]$$

Input of discriminator.

$$n(t) = s(t) + n(t) \\ = A \cos[2\pi f_c t + \phi(t)] + r(t) \cos[2\pi f_c t + \psi(t)]$$

Phasor diagram
for $x(t) = n(t) + s(t)$



from phasor diagram

$$\tan[\theta(t) - \phi(t)] = \frac{r(t) \sin[\psi(t) - \phi(t)]}{Ac + r(t) \cos[\psi(t) - \phi(t)]}$$

$Ac \gg r(t)$

$$\tan[\theta(t) - \phi(t)] \approx \frac{r(t) \sin[\psi(t) - \phi(t)]}{Ac}$$

$$\tan[\theta(t) - \phi(t)] \approx \frac{r(t) \sin \psi(t)}{Ac}$$

~~$r(t) \sin \psi(t) = n_s(t)$~~

$$\tan[\theta(t) - \phi(t)] \approx \frac{n_s(t)}{Ac}$$

$Ac \gg n_s(t)$

$$\theta(t) - \phi(t) \approx \frac{n_s(t)}{Ac}$$

$$\theta(t) = \frac{n_s(t)}{Ac} + \phi(t)$$

Avg

Taking

frequency of $\omega(t)$.

$$f(t) = \frac{1}{2\pi} \frac{d\omega(t)}{dt}$$

$$f(t) = \frac{1}{2\pi} \frac{d}{dt} \left[\phi(t) + \frac{n_s(t)}{A_c} \right]$$

$$f(t) = \frac{1}{2\pi} \frac{d\phi(t)}{dt} + \frac{1}{2\pi A_c} \frac{dn_s(t)}{dt}$$

$$= \frac{1}{2\pi} \frac{d}{dt} \left[2\pi k_f \int_0^t m(\tau) d\tau \right] + \frac{1}{2\pi A_c} \frac{dn_s(t)}{dt}$$

output of frequency discriminator is proportional to $f(t)$

$$v(t) = K' f(t)$$

$$K' \approx 1$$

$$v(t) = f(t)$$

$$v(t) = K_f m(t) + \frac{1}{2\pi A_c} \frac{dn_s(t)}{dt}$$

$$= m_d(t) + n_d(t)$$

$$\begin{aligned} \text{Avg power of } m_d(t) &= \overline{m_d(t)^2} \\ &= [K_f m(t)]^2 \\ &= K_f^2 P_m \end{aligned}$$

$$n_d(t) = \frac{1}{2\pi A_c} \frac{dn_s(t)}{dt}$$

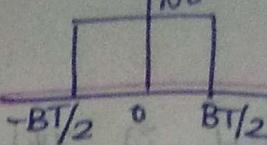
Taking transform

$$N_D(f) = \frac{1}{2\pi A_c} j 2\pi f N_s(f)$$

$$|N_D(f)|^2 = \frac{f^2}{AC^2} |N_s(f)|^2$$

$$S_{nd}(f) = \frac{f^2}{Ac^2} S_{ns}^2(f)$$

$$= \begin{cases} f^2/Ac^2 No & |f| \leq BT \\ 0 & \text{otherwise} \end{cases}$$



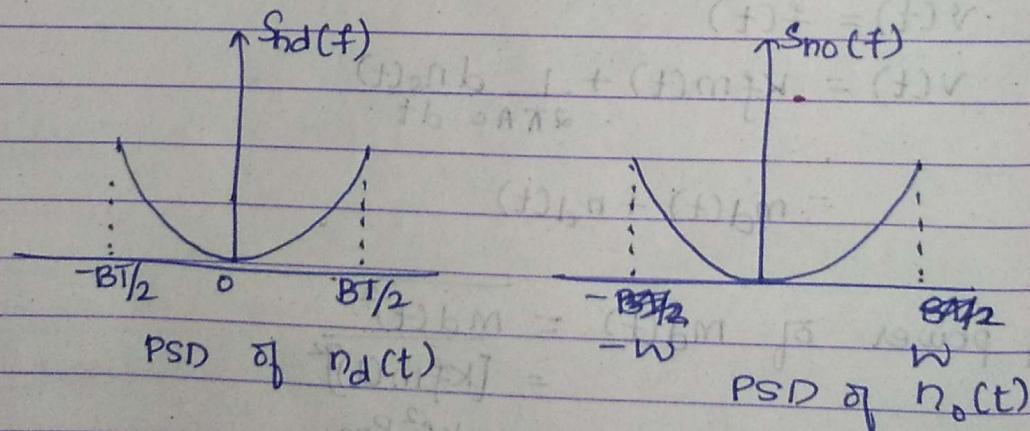
PSD of $n_s(t)$

$$\text{Avg power of } \overline{n_o(t)^2} = \frac{No}{Ac^2} \int_{-w}^w f^2 df$$

$$(f)_{avg} + (f)_{avg} = 2 \frac{No w^3}{3 Ac^2}$$

$$[\text{SNR}]_o = \frac{\overline{m_d^2(t)}}{\overline{n_o^2(t)}} = \frac{k_f^2 P_m}{2 No w^3 / 3 Ac^2}$$

$$= \frac{3 Ac^2 k_f^2 P_m}{2 No w^3}$$



$$FOM = r = [\text{SNR}]_o$$

$$[\text{SNR}]_c$$

$$= \frac{3 Ac^2 k_f^2 P_m}{2 No w^3}$$

$$\frac{Ac^2}{2 No w^3}$$

$$= \frac{3 k_f^2 P_m}{w^2}$$

Let $m(t)$ be single tone modulating signal

$$m(t) = A_m \cos 2\pi f_m t$$

$$P_m = m^2(t) = \left(\frac{A_m}{\sqrt{2}}\right)^2$$

$$\Rightarrow \frac{A_m^2}{2} = P_m$$

$$FOM = \frac{3k_f^2 A_m^2}{2 f_m^2}$$

$$= \frac{3}{2} \left[\frac{k_f^2 A_m}{f_m} \right]^2$$

$$= \frac{3}{2} \beta^2$$

$$\left\{ \begin{array}{l} k_f A_m \\ \hline f_m \end{array} \right\} = \beta$$

$\mu = 1$ ie 100% modulation

$$\frac{\mu^2}{2 + \mu^2} = \frac{3}{2} \beta^2$$

$$\frac{1}{1+2} = \frac{3}{2} \beta^2$$

$$\frac{1}{3} = \frac{3}{2} \beta^2$$

$$\underline{\underline{\beta = 0.5}}$$

Capture Effect: