

Problem 1 (40 points) Choose the answers in the following question.

**(a) What is the class of the object defined by `vec <- c(5, TRUE)` ?**

• **Numeric**

- Integer
- Matrix
- Logical

**Answer: The Class of the object is Numeric.**

**(b) Suppose I have vectors `x <- 1:4` and `y <- 1:2`. What is the result of the expression `x + y`?**

- A numeric vector with the values 1, 2, 5, 7
- A numeric vector with the values 2, 4, 2, 4
- **An integer vector with the values 2, 4, 4, 6**
- An error

**Answer: • An integer vector with the values 2, 4, 4, 6**

**(c) Suppose I define the following function in R:**

**`fsin <- function(x) sin(pi*x)`**

**What will be returned by `fsin(1)` ?**

- **The number 0 is returned**
- The number 1 is returned
- A warning is given with no value returned
- An error is returned because 'pi' is not specified in the call to 'fsin'.

**Answer: the value returned is 1.224606e-16. This value `sin(pi)` is 0.**

**(d) What is returned by the R command `c(1,2) %*% t(c(1,2))` ?**

- The number 5
- A one by two matrix
- **A two by two matrix**
- An error is returned because the dimensions mismatch

**Answer: • A two by two matrix**

**(e) Suppose I define the following function in R:**

```
f <- function(x) {  
  g <- function(y) {  
    y + z  
  }  
  z <- 4  
  x + g(x)  
}
```

**If I then run in R the following statements**

```
z <- 15
```

```
f(3)
```

**What value is returned?**

- 16
- 7
- **10**
- 4

**Answer: the value returned is 10**

**Problem 2 (20 points)**

Use R to calculate  $\sum_{x=1}^{1000} x^2 = 1^2 + 2^2 + \dots + 1000^2$ .

Please hand in your R commands and the results you produce by running those commands.

**Answer:**

```
> x=1:1000
> y<-sum(x^2)
[1] 333833500
```

**Question 3 (40 points)**

Write an R script that does all of the following:

**a) Create a vector X of length 20, with the kth element in  $X = 2k$ , for  $k=1\dots 20$ . Print out the values of X.**

Answer:

```
v=(1:20)
```

```
k<-v
```

```
X<-(2*k)
```

```
print(X)
```

**b) Create a vector Y of length 20, with all elements in Y equal to 0. Print out the values of Y**

Answer:

```
Y<-rep(0,20)
```

```
print (Y)
```

c) Using a for loop, reassigns the value of the k-th element in Y, for k = 1...20. When  $k < 12$ , the kth element of Y is reassigned as the cosine of k. When the  $k \geq 12$ , the kth element of Y is reassigned as the value

of integral  $\int_0^k \sqrt{t} dt$

Answer:

```
integrand<-function(t)sqrt(t)
for(K in 1:20){
  if (k < 12) {
    Y[k] = cos(k)}
  else {
    Y[k]<-integrate(integrand, lower=0, upper=k)
  }
}
print (Y)
```