

8i70fawma

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[1]: def pagerank(G, alpha=0.85, personalization=None, max_iter=100, tol=1.0e-6,
      ↪nstart=None, weight='weight', dangling=None):
    if len(G) == 0:
        return {}

    if not G.is_directed():
        D = G.to_directed()
    else:
        D = G

    # Create a copy in (right) stochastic form
    W = nx.stochastic_graph(D, weight=weight)
    N = W.number_of_nodes()

    # Choose fixed starting vector if not given
    if nstart is None:
        x = dict.fromkeys(W, 1.0 / N)
    else:
        # Normalized nstart vector
        s = float(sum(nstart.values()))
        x = dict((k, v / s) for k, v in nstart.items())

    if personalization is None:
        # Assign uniform personalization vector if not given
        p = dict.fromkeys(W, 1.0 / N)
    else:
        missing = set(G) - set(personalization)
        if missing:
            raise NetworkXError('Personalization dictionary must have a value_
            ↪for every node. Missing nodes %s' % missing)
        s = float(sum(personalization.values()))
        p = dict((k, v / s) for k, v in personalization.items())

    if dangling is None:
        # Use personalization vector if dangling vector not specified
        dangling_weights = p
    else:
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missing = set(G) - set(dangling)
if missing:
    raise NetworkXError('Dangling node dictionary must have a value for_
every node. Missing nodes %s' % missing)
s = float(sum(dangling.values()))
dangling_weights = dict((k, v/s) for k, v in dangling.items())

dangling_nodes = [n for n in W if W.out_degree(n, weight=weight) == 0.0]

# power iteration: make up to max_iter iterations
for _ in range(max_iter):
    xlast = x
    x = dict.fromkeys(xlast.keys(), 0)
    danglesum = alpha * sum(xlast[n] for n in dangling_nodes)
    for n in x:
        # this matrix multiply looks odd because it is
        # doing a left multiply  $x^T = xlast^T W$ 
        for nbr in W[n]:
            x[nbr] += alpha * xlast[n] * W[n][nbr][weight]
        x[n] += danglesum * dangling_weights[n] + (1.0 - alpha) * p[n]

    # check convergence, l1 norm
    err = sum([abs(x[n] - xlast[n]) for n in x])
    if err < N*tol:
        return x
    raise NetworkXError('Pagerank: power iteration failed to converge in %d_
iterations.' % max_iter)

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[2]: import networkx as nx
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[3]: G = nx.barabasi_albert_graph(60, 41)
pr = nx.pagerank(G, 0.4)
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[4]: print(pr)
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{0: 0.028121839712461336, 1: 0.013572060204606995, 2: 0.012377192811464105, 3:
0.01276660315849177, 4: 0.012959694372101743, 5: 0.013566505760540899, 6:
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0.012757344165725625, 37: 0.013573406710585708, 38: 0.013362677844185263, 39:
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0.02210779500473849, 58: 0.021848949694802174, 59: 0.021341625642380603}

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