

SYMBIOSIS INTERNATIONAL (DEEMED UNIVERSITY)

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Tutorial-8 (CO_I)
Subject Name: Discrete Mathematics
B.Tech. AIML SEM-IV 2023-27 (AY-2024-25)

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Q.1 Find the solution of the following recurrence relations.

(i)
$$a_n = 5a_{n-1}$$
; $a_0 = 1$

(ii).
$$y_{n+2} - 4y_{n+1} + 3y_n = 2^n$$
; $n \ge 0$

(iii)
$$a_{n+1} - 3a_n = (n^2 + 1); n \ge 1; a_0 = 1.$$

(iv).
$$a_{n+2} - 6a_{n+1} + 9a_n = 3(2^n) + 7(3^n), n \ge 0$$

(vi).
$$a_n - 5a_{n-1} + 6a_n = 3^n + 2n$$
; $n \ge 0$

(vii).
$$y_{n+2} - 4y_{n+1} + 4y_n = 2n (4)^n$$
; $n \ge 0$, $y_0 = 0$, $y_1 = 1$.

Some Application based Problems

- **Q.2** Model the rabbit growth model (a type of population growth model) by using recurrence relation. Also find the solution of the same to calculate the populations of the rabbits after n-unit of time. Consider the following rules for it.
 - young pair of rabbits (one of each sex) is placed on an island. A pair of rabbits does not breed until they are 2 months old. After they are 2 months old, each pair of rabbits produces another pair each month.
 - \square Find a recurrence relation for the number of pairs of rabbits on the island after n months, assuming that no rabbits ever die.
- **Q.3** Do the modelling of the <u>Tower of Hanoi game</u> in terms of recurrence relation. Also find the solution of it.