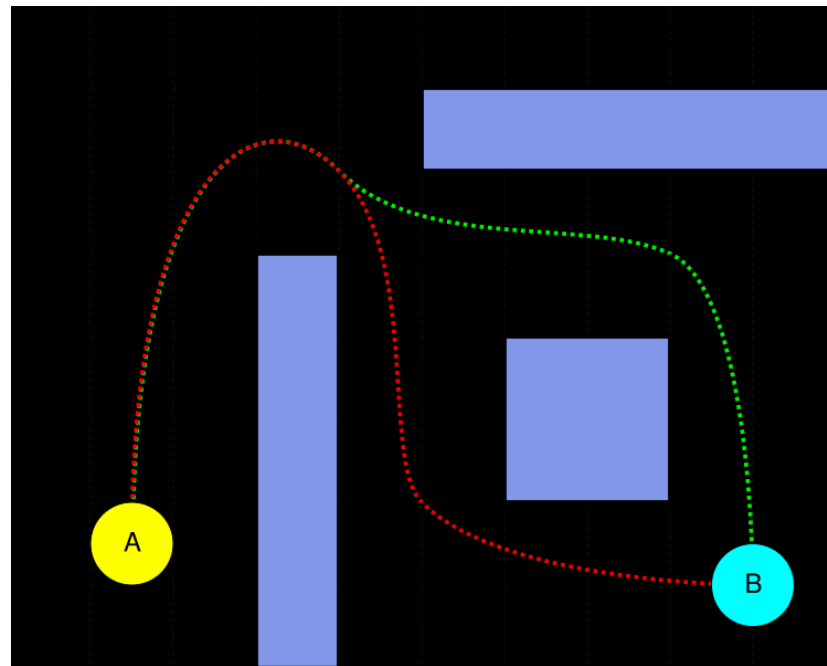


# VGP332 – Artificial Intelligence

Instructor: Peter Chan



# Agenda

- Assignment 1 Redux
- Review
- Dijkstra's Algorithm
- A\* Algorithm
- Graph Search Improvements
- Alternative Graph Searches
- Assignment 2 Overview

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# Assignment 1 Redux

- Questions?



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# Review

- What is pathfinding?
- What can graphs be used for?
- How can you implement graphs?



# Graph Searches

- Open list:
  - list of nodes you need to consider in the steps ahead
- Closed list:
  - list of nodes you've already visited and don't need to consider again

# Graph Searches

```
put start node in open list
while end node not reached && open list isn't empty:
    move node N from open list to closed list
    expand node N:
        if expanded node isn't in open or closed lists:
            add expanded node to open list
```



# DFS, BFS

- **DFS:**
  - Choose node from front of open list
  - Expanded nodes get added to front of open list
- **BFS:**
  - Choose node from front of open list
  - Expanded nodes get added to back of open list

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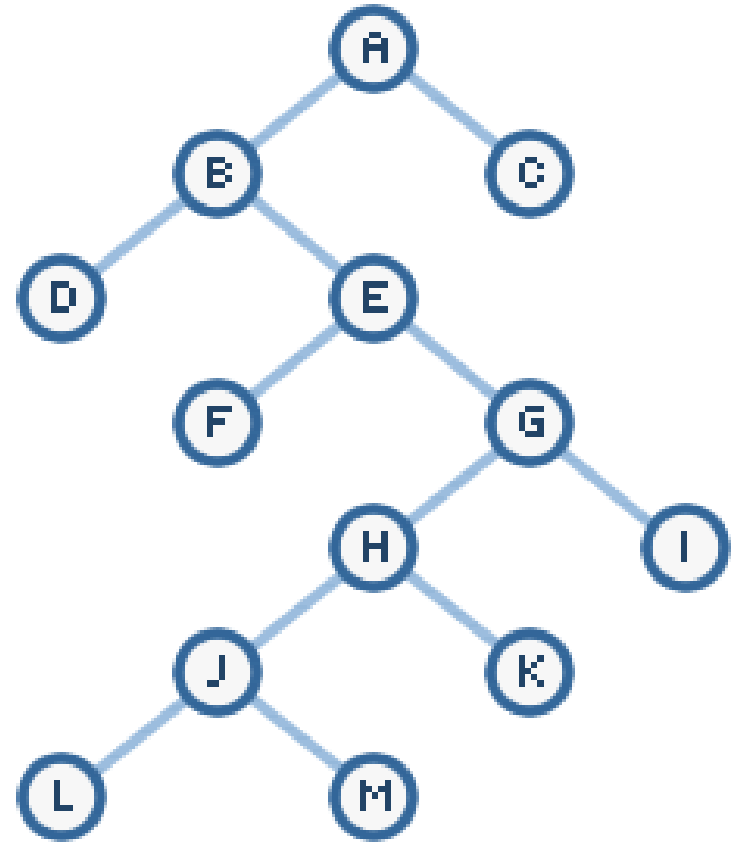
# Shortest Paths

- What is the shortest path between two nodes on a graph?



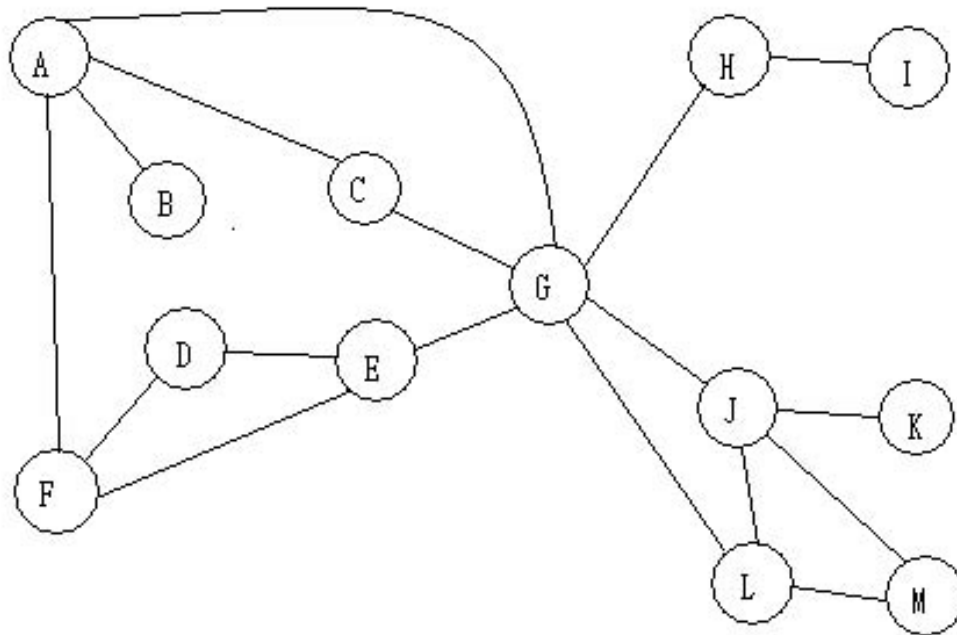
# Shortest Paths

- Consider this graph:



# Shortest Paths

- Consider this graph:



# Shortest Paths

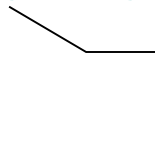
- Consider this map:



# Dijkstra's Algorithm

- Choose node from front of open list that is the shortest cumulative distance from the starting node
- Expanded nodes get added to ~~front of~~ open list

# Dijkstra's Algorithm

- Choose node from front of open list **that is the shortest cumulative distance from the starting node**  
 This is called a cost function
- Expanded nodes get added to ~~front of~~ open list



# Dijkstra's Algorithm

- Cost function

$$f(x) = g(x)$$

where  $g(x)$  is shortest distance traveled from initial node to current node

# Dijkstra's Algorithm

[http://en.wikipedia.org/wiki/Dijkstra\\_algorithm](http://en.wikipedia.org/wiki/Dijkstra_algorithm)

# Dijkstra's Search Applet

- Try this out:

<http://www-b2.is.tokushima-u.ac.jp/~ikeda/suuri/dijkstra/Dijkstra.shtml>



# Dijkstra's Search on Grid-Based

	A	B	C	D	E
1					
2					
3	S				E
4					
5					



# Observations on Dijkstra's Search

- Pros?
- Cons?
- Results?



# Observations on Dijkstra's Search

- Optimal
- Informed

# Agenda

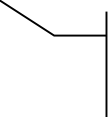
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# A\* Algorithm

- Choose node from front of open list that is on the shortest path from the starting node to the ending node
- Expanded nodes get added to ~~front of~~ open list



# A\* Algorithm

- Choose node from front of open list **that is on the shortest path from the starting node to the ending node**  Anything odd about this cost function?
- Expanded nodes get added to ~~front of~~ open list



# A\* Algorithm

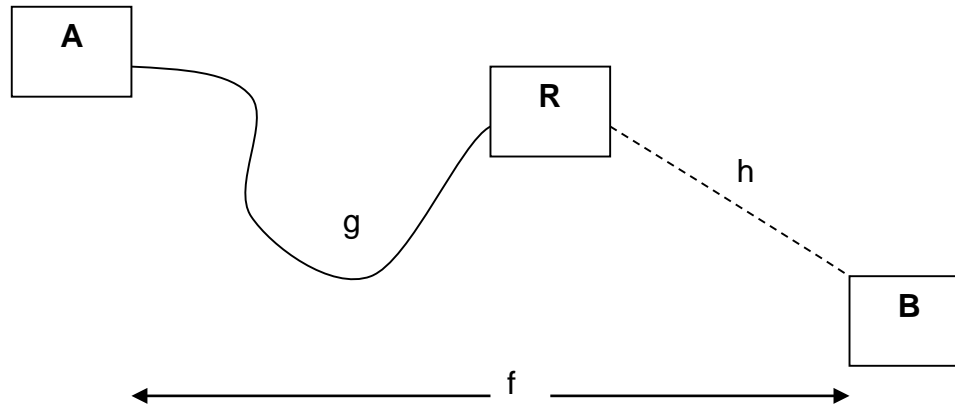
- Q: If you're searching for a path but haven't found one yet, how can you know how long the full path is?



# A\* Algorithm

- Q: If you're searching for a path but haven't found one yet, how can you know how long the full path is?
- A: Make an informed guess

# A\* Algorithm



- For any path you're considering from A to B
  - Suppose you're as far along as node R
  - You know how far you've come: distance =  $g$
  - Best case from R to B: distance =  $h$

# A\* Algorithm

- Cost function

$$f(x) = g(x) + h(x)$$

where  $g(x)$  is shortest distance traveled from initial node to current node  
and  $h(x)$  is the guessed distance from the current node to the end node

# A\* Algorithm

[http://en.wikipedia.org/wiki/A-star\\_algorithm](http://en.wikipedia.org/wiki/A-star_algorithm)

# A\* Search on Grid-Based

	A	B	C	D	E
1					
2					
3	S				E
4					
5					

# A\* Search Applet

- Try this out:

<http://www.vision.ee.ethz.ch/~cvcourse/astar/AStar.html>



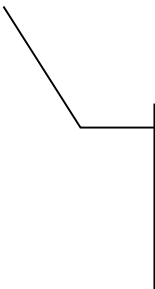
# Observations on A\* Search

- Pros?
- Cons?
- Results?



# Observations on A\* Search

- Optimal
- Informed
- $h(x)$  needs to be admissible



This means that the estimate must be less than or equal to the actual lowest cost

# A\* Search Heuristics

- Can you think of other heuristics to use?



# Search Algorithm Comparison

- Try this out:

<http://www.stefan-baur.de/cs.web.mashup.pathfinding.html>



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# Graph Search Improvements

- What improvements can you think of for:
  - BFS
  - DFS
  - Dijkstra's
  - A\*



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# “Best-first” search

- Favour paths that would lead towards the goal
- E.g.

Start

Which search directions are preferable in this case?

End

- Can combine with  $A^*$  search's cost function





# Minimax Search

- Usually used in turn-based two-player games
- Scoring function evaluates board/moves
- Create branching tree of move possibilities
- Maximize AI's move and minimize opponent's move

<http://wolfey.110mb.com/GameVisual/launch.php>



# Alpha-beta pruning

- Optimization for minimax searches
- Prune (don't generate/evaluate) unnecessary branches



# Minimax & Alpha-Beta Example

- Petri
- Blob Wars



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