

# VGP332 – Artificial Intelligence

Instructor: Peter Chan



# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Introductions & Administration

- Introduction
- Course syllabus
- Overview



# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Introduction to AI

- What is Artificial Intelligence?
- What is Artificial Intelligence in Games?
- Is there a difference?



# AI

- Computer vision
- Speech recognition
- Language recognition
- Expert systems
- Pathfinding / navigation
- Goal-driven
- ...

# AI in Games

- Give the **illusion** of intelligence
- Needs to be *fast*
- Often needs to be **suboptimal**



# AI in Games

- Give the **illusion** of intelligence
  - Behaviour that players would deem intelligent
  - Can use any means necessary:
    - Extra hit points
    - Scripted sequences
    - Can cheat unobtrusively
- Needs to be *fast*
- Often needs to be suboptimal

# AI in Games

- Give the illusion of intelligence
- Needs to be *fast*
  - Limited # of cycles
  - Can't afford expensive algorithms
- Often needs to be suboptimal

# AI in Games

- Give the illusion of intelligence
- Needs to be *fast*
- Often needs to be **suboptimal**
  - Perfect computer player is frustrating
  - Balancing act between too smart & too dumb

# AI in Games

The goal of AI in a game is to stop the computer from looking stupid

# AI Examples

- Can you think of examples of smart AI in games you've played?
- What about examples of bad AI?



# Agenda

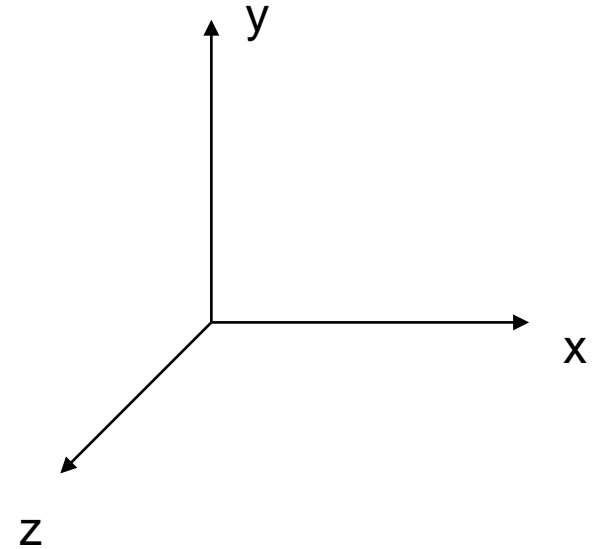
- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Math & Physics Review



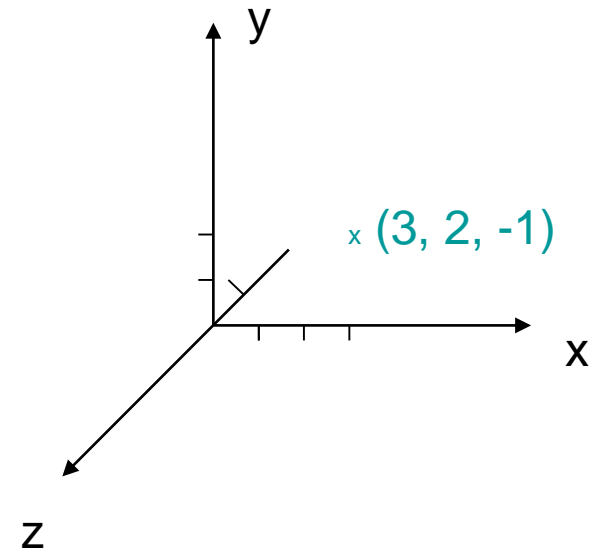
# Cartesian Coordinates

- 1 dimensional = 1 axis (x)
- 2 dimensional = 2 axes (x, y)
- 3 dimensional = 3 axes (x, y, z)





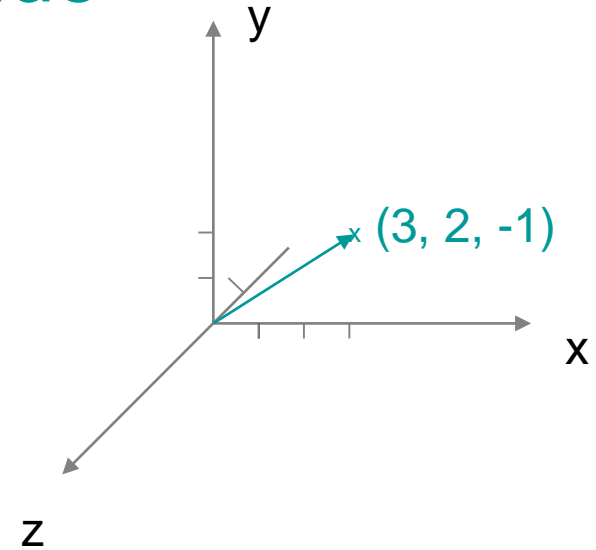
# Point



- A point in 3D space has 3 values for each of the 3 axes

# Vector

- Has **direction** and **magnitude**
- With  $(x, y, z)$  values, vector points from origin to  $(x, y, z)$



# Vector Math

- Addition piecewise by axis

$$\mathbf{v} + \mathbf{w} = (\mathbf{v}.x + \mathbf{w}.x, \quad \mathbf{v}.y + \mathbf{w}.y, \quad \mathbf{v}.z + \mathbf{w}.z)$$

- Subtraction is identical

$$\mathbf{v} - \mathbf{w} = (\mathbf{v}.x - \mathbf{w}.x, \quad \mathbf{v}.y - \mathbf{w}.y, \quad \mathbf{v}.z - \mathbf{w}.z)$$

- Commutative:

$$\mathbf{v} + \mathbf{w} = \mathbf{w} + \mathbf{v}$$

# Vector Math

- Multiplication by scalar

$$\mathbf{v} * s = (\mathbf{v}.x * s, \mathbf{v}.y * s, \mathbf{v}.z * s)$$

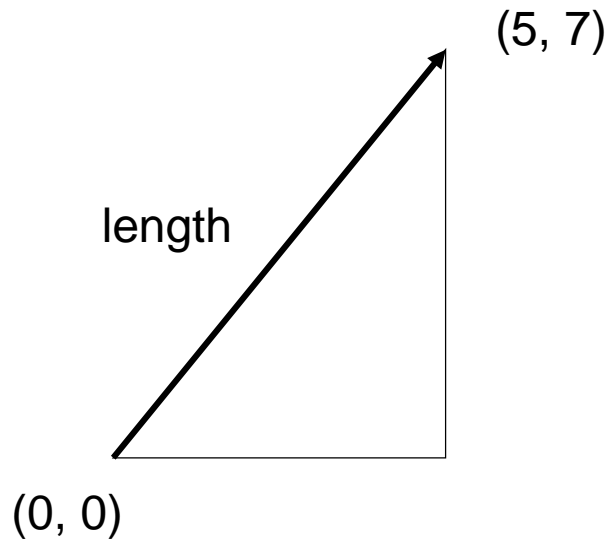
- Division is identical

$$\mathbf{v} / s = (\mathbf{v}.x / s, \mathbf{v}.y / s, \mathbf{v}.z / s)$$

(Note: watch for division by zero!)

# Vector Length

- Length (2D)



Use Pythagoras:

$$\text{Length}^2 = x^2 + y^2$$

$$\text{Length} = \text{sqrt}(x^2 + y^2)$$

For example:

$$\text{Length} = \text{sqrt}(5^2 + 7^2)$$

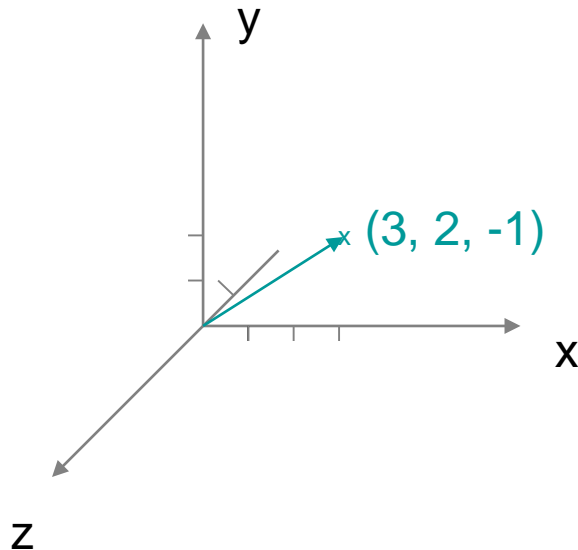
$$\text{Length} = \text{sqrt}(25 + 49)$$

$$\text{Length} = \text{sqrt}(74)$$

$$\text{Length} = 8.602\dots$$

# Vector Length

- Length (3D)



Use Pythagoras:

$$\text{Length}^2 = x^2 + y^2 + z^2$$

$$\text{Length} = \text{sqrt}(x^2 + y^2 + z^2)$$

For example:

$$\text{Length} = \text{sqrt}(3^2 + 2^2 + -1^2)$$

$$\text{Length} = \text{sqrt}(9 + 4 + 1)$$

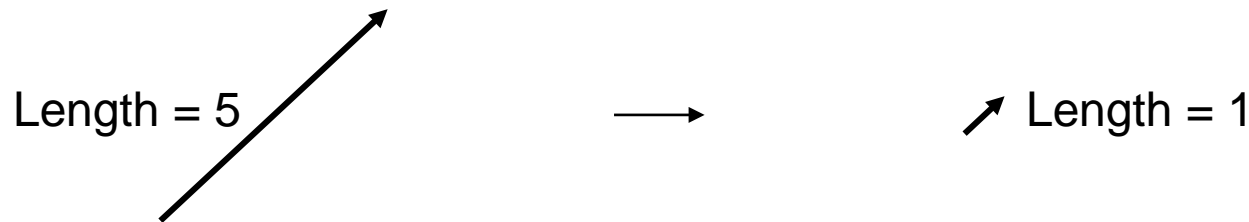
$$\text{Length} = \text{sqrt}(14)$$

$$\text{Length} = 3.742\dots$$

Notation: Given a vector  $\mathbf{v}$ , its length is denoted  $||\mathbf{v}||$

# Vector Normalization

- Normalization:
  - Keep vector direction the same
  - Scale vector magnitude to unit length



Divide vector by its length:  $\frac{\mathbf{v}}{\|\mathbf{v}\|}$

Notation: Given a vector  $\mathbf{v}$ , its unit vector is denoted  $\hat{\mathbf{v}}$

# Vector Dot Product

- Given two vectors,  $\mathbf{v}$  and  $\mathbf{w}$
- Defined as:

$$\mathbf{v} \cdot \mathbf{w} = \|\mathbf{v}\| \|\mathbf{w}\| \cos \Theta$$

(where  $\Theta$  is the angle between  $\mathbf{v}$  and  $\mathbf{w}$ )

returns **scalar** result

- Can be simplified to:

$$\mathbf{v} \cdot \mathbf{w} = \mathbf{v}.x * \mathbf{w}.x + \mathbf{v}.y * \mathbf{w}.y + \mathbf{v}.z * \mathbf{w}.z$$

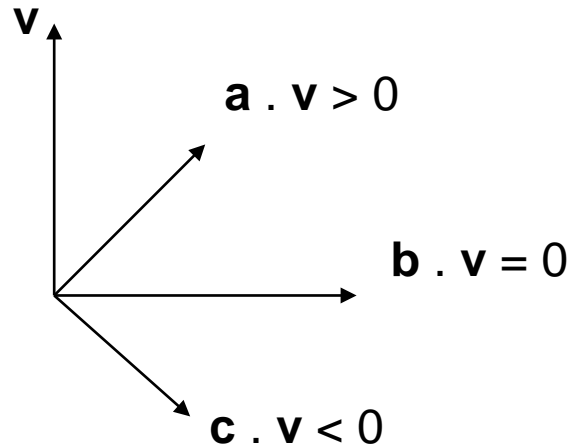
- Commutative:

$$\mathbf{v} \cdot \mathbf{w} = \mathbf{w} \cdot \mathbf{v}$$



# Vector Dot Product

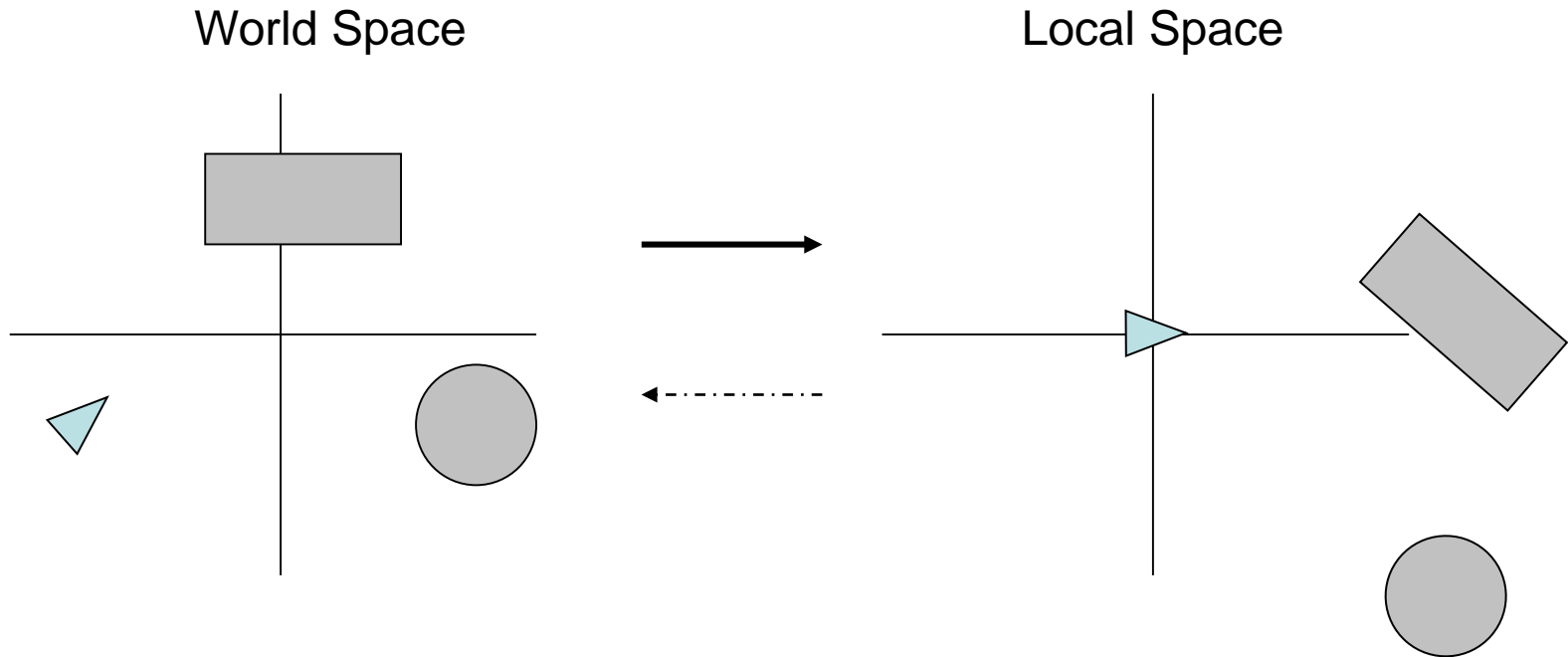
- Determine general angle between vectors



- Quick test to see if target is in front, beside or behind



# World Space vs. Local Space



# Physics Review



# Physics Review

- Velocity =  $\Delta$  Distance /  $\Delta$  Time

$$P_{t+1} = P_t + V\Delta t$$

- Acceleration =  $\Delta$  Velocity /  $\Delta$  Time

$$V_{t+1} = V_t + a \Delta t$$

- Force = mass x acceleration

Why physics in AI?

- Realistic-looking behaviours & motion
- Useful for prediction

# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- **Intro to Pathfinding**
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Pathfinding

- How would you define pathfinding?



# Pathfinding

- Go from point A to point B
- Avoid obstacles
- Avoid getting stuck
- Simpler in 2D, but can extend to 3D
- Find shortest path (optional?)
- Should be dynamic

# Pathfinding

- How would you do pathfinding?





# Pathfinding is Hard!

<http://www.youtube.com/watch?v=lw9G-8gL5o0>



# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- **Graphs & Nodes**
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Graphs

- A graph is formally defined as:

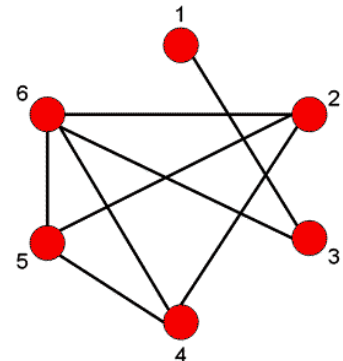
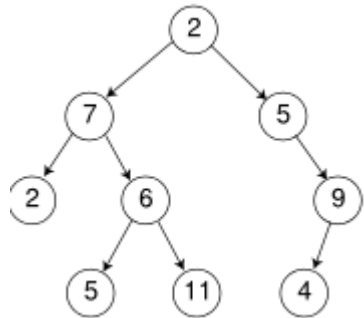
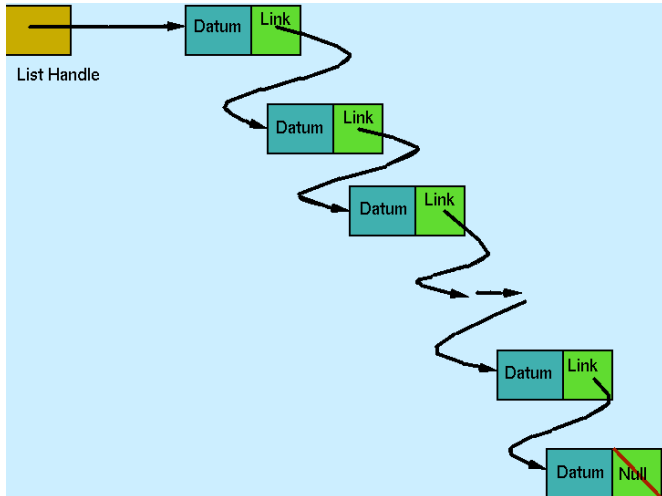
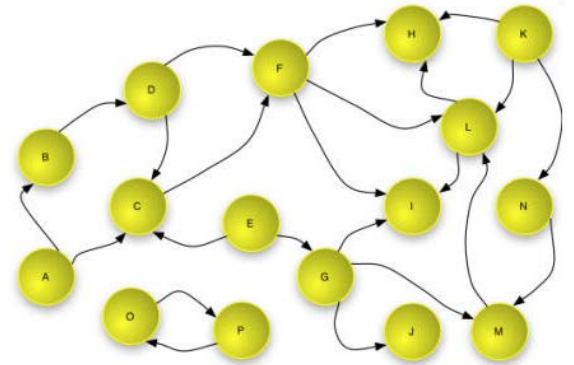
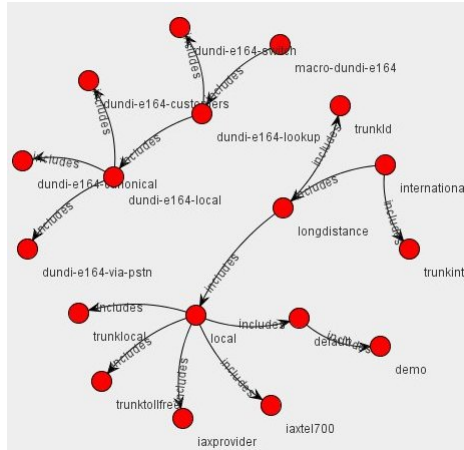
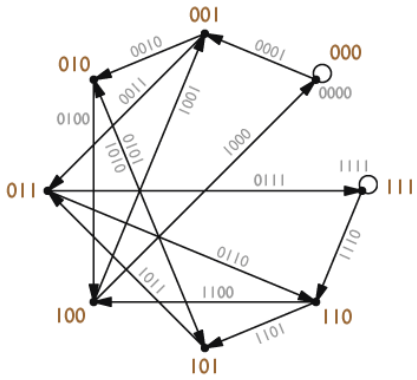
$$G = \{N, E\}$$

where  $N$  is the set of nodes

and  $E$  is the set of edges connecting those nodes

# Graphs

- What does that really mean?



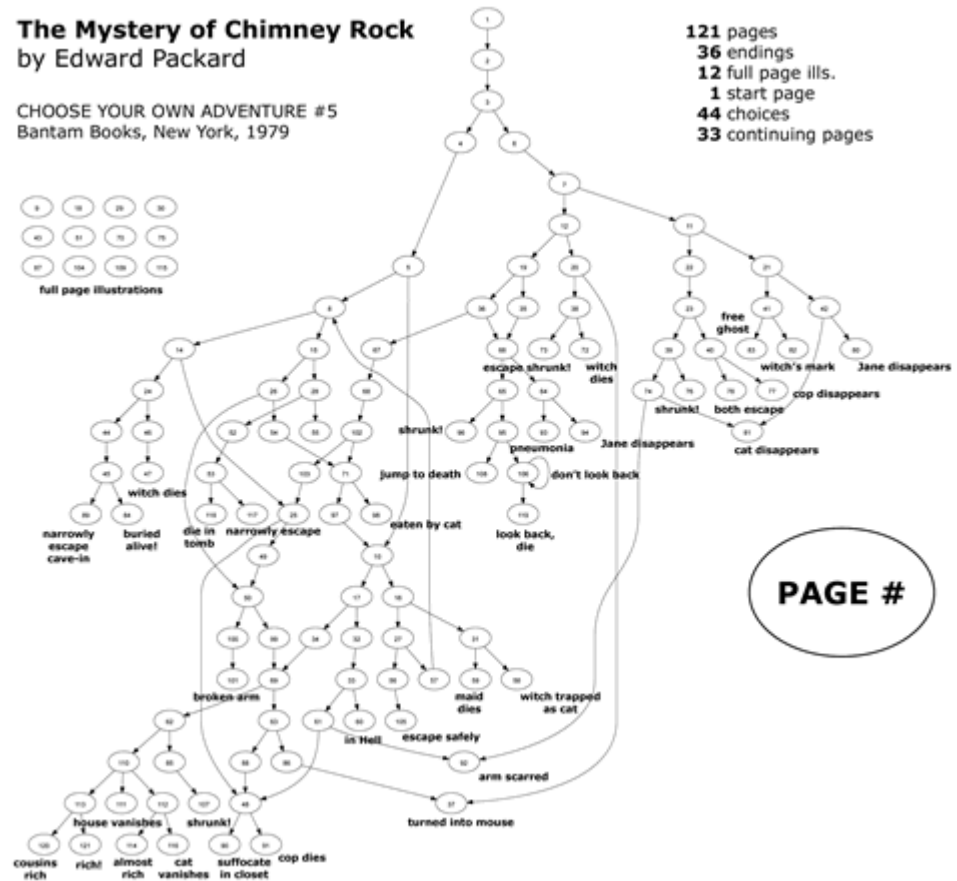
# Graph Versatility

- Decisions

## The Mystery of Chimney Rock by Edward Packard

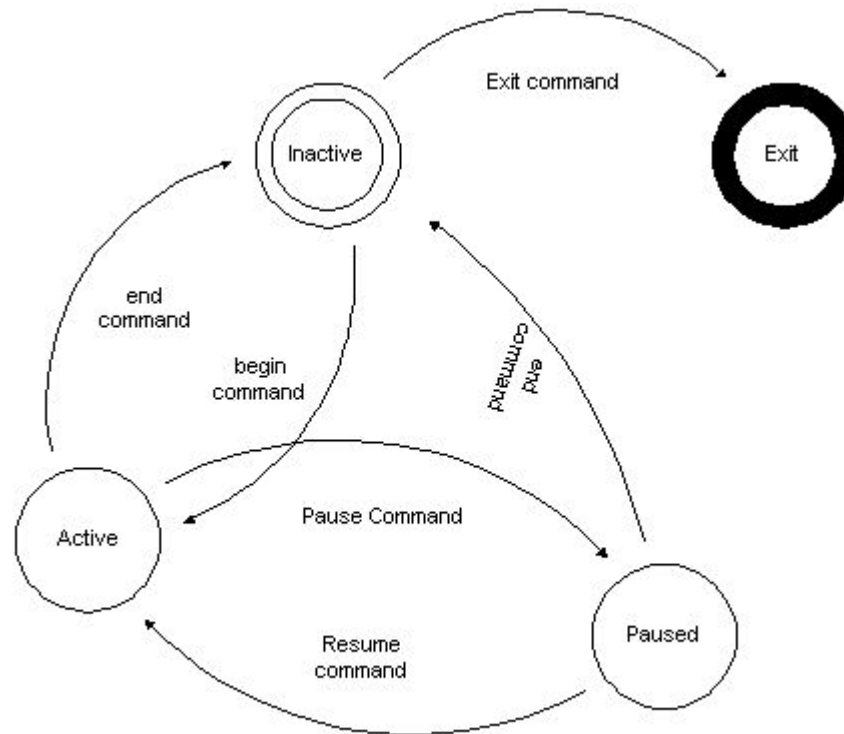
CHOOSE YOUR OWN ADVENTURE #5  
Bantam Books, New York, 1979

121 pages  
36 endings  
12 full page ill.  
1 start page  
44 choices  
33 continuing pages



# Graph Versatility

- States



# Graph Versatility

- Geometry

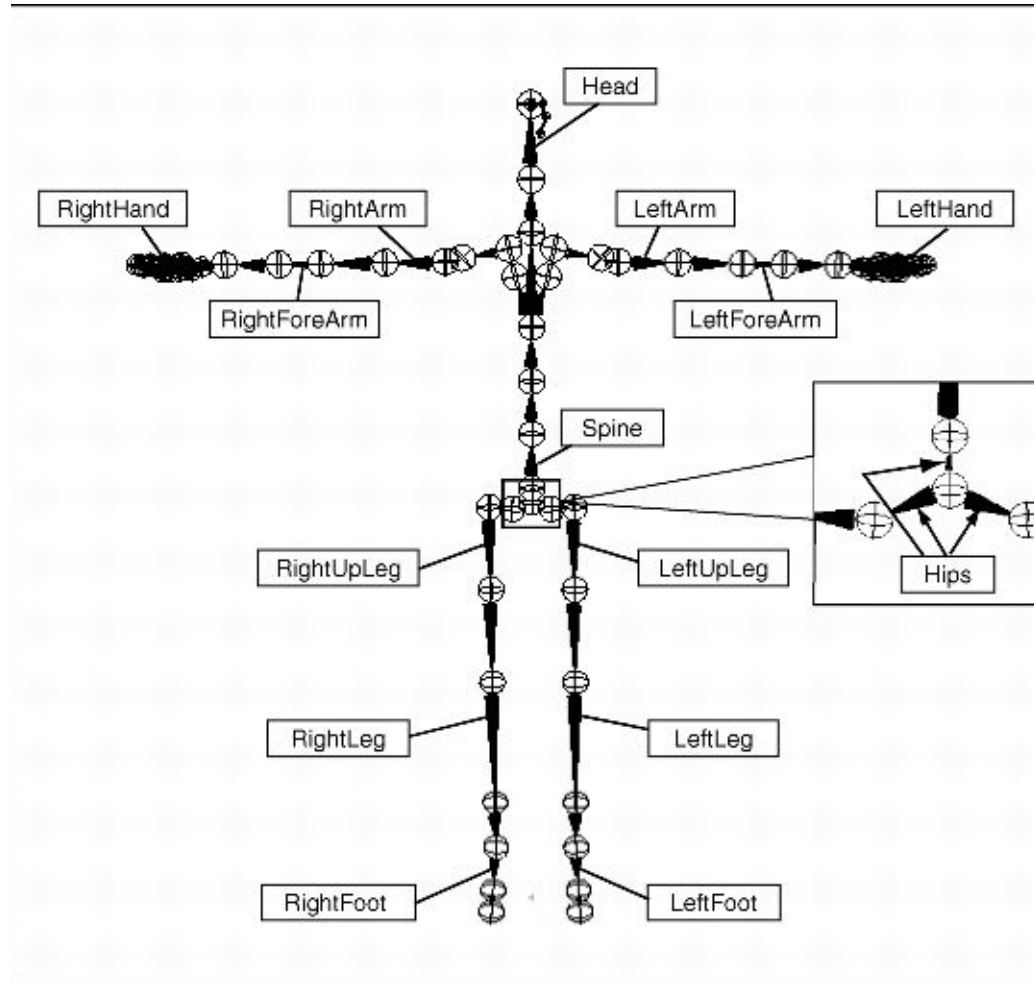
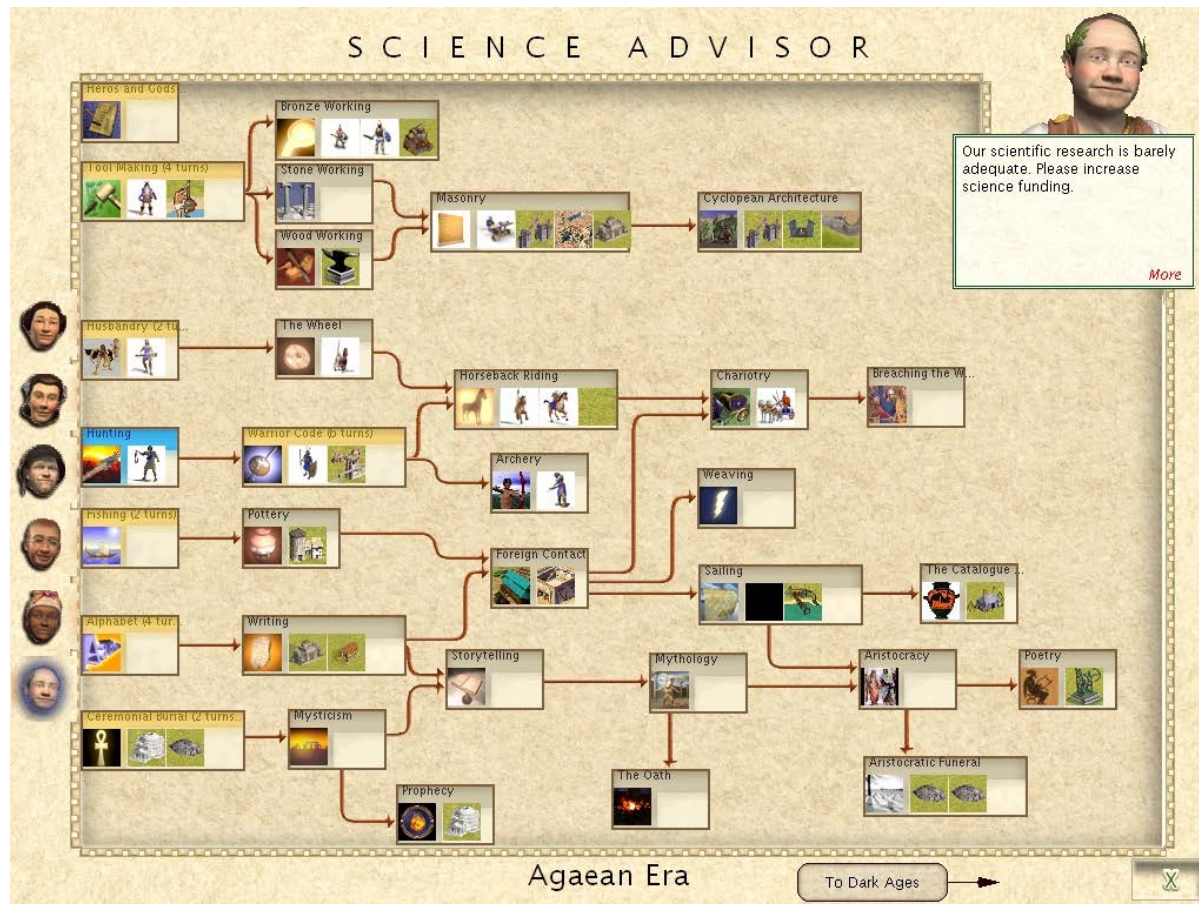


figure 6: Basic skeleton with Base nodes labelled

# Graph Versatility

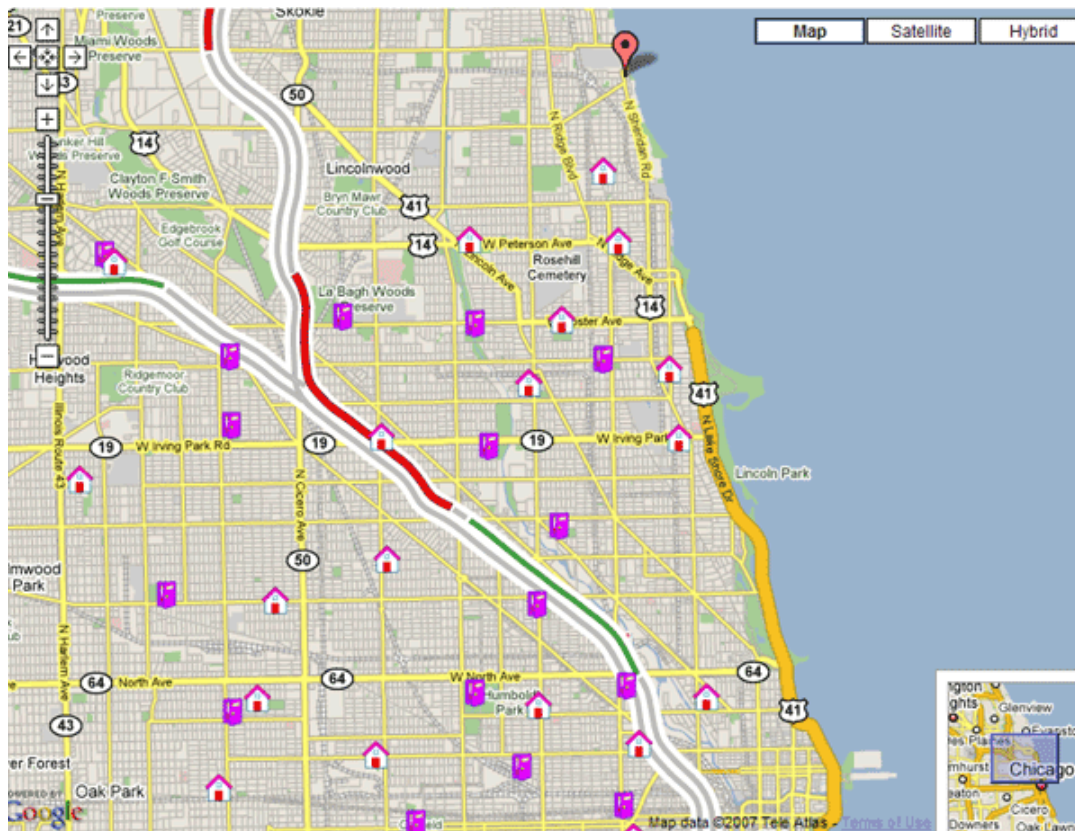
- Dependencies (e.g. tech trees)





# Graph Versatility

- Navigation



# Pathfinding using Graphs

- Warcraft II



Can you think of a way to represent this map using a graph?



# Pathfinding using Graphs

- Warcraft III

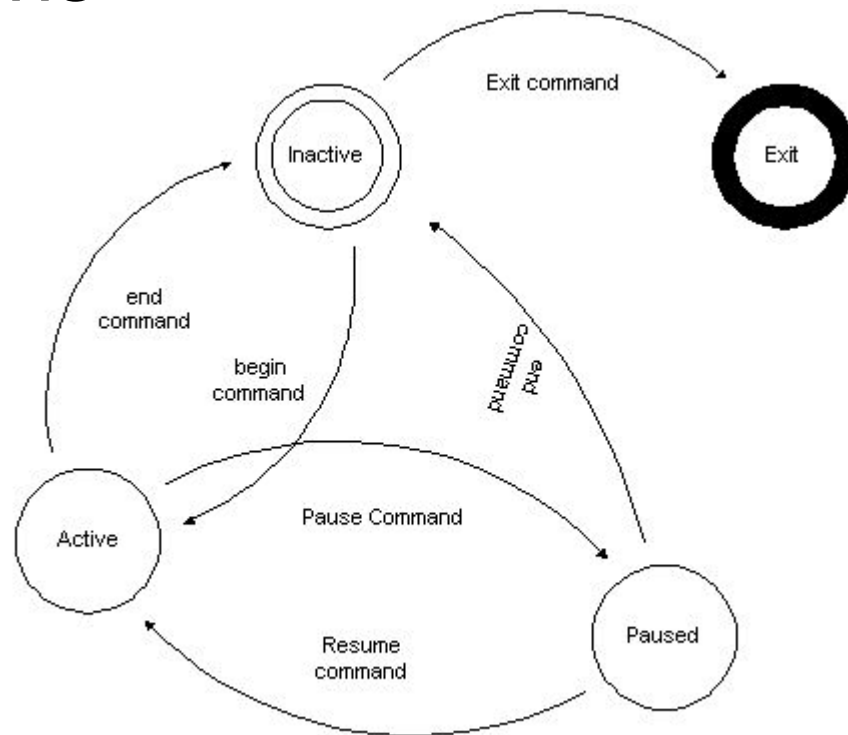


What about this one?



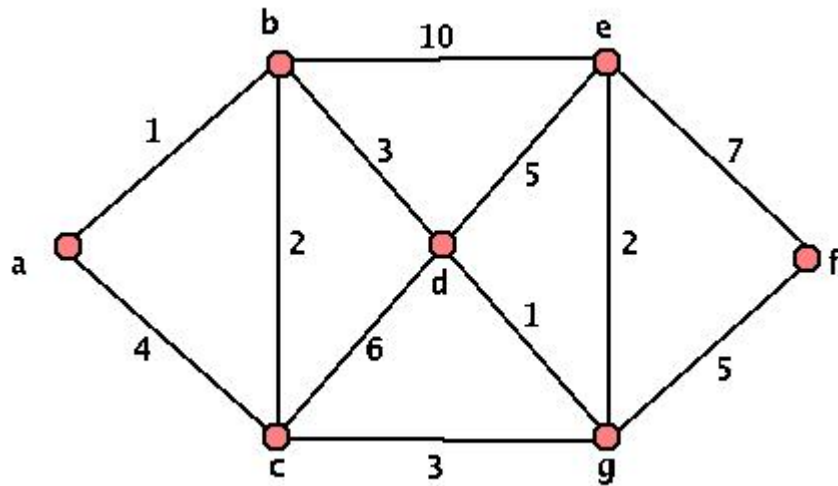
# Additional Graph Features

- Directed graphs



# Additional Graph Features

- Weighted edges



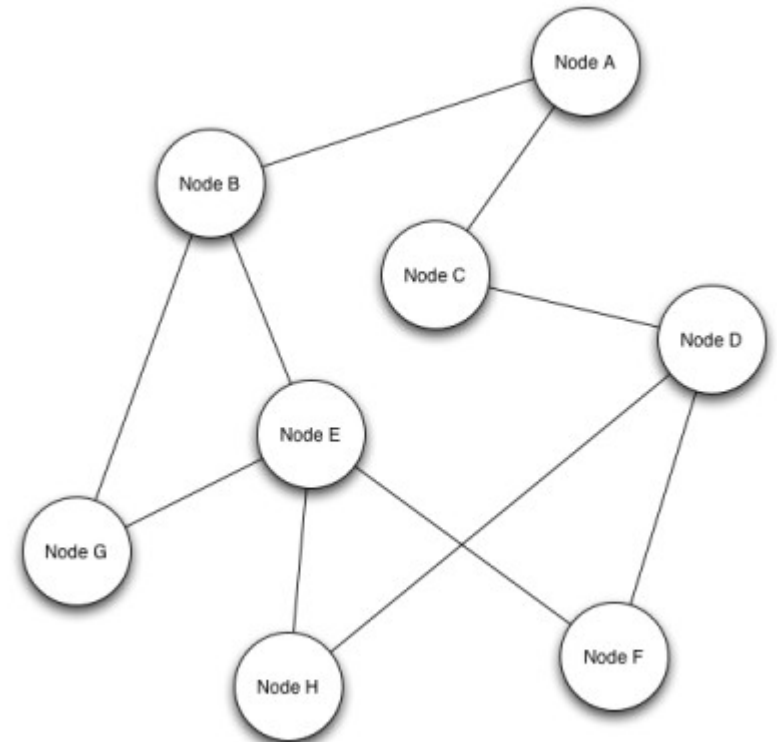


# Graph Implementation

- Adjacency matrix
- Adjacency list
- Grid-based

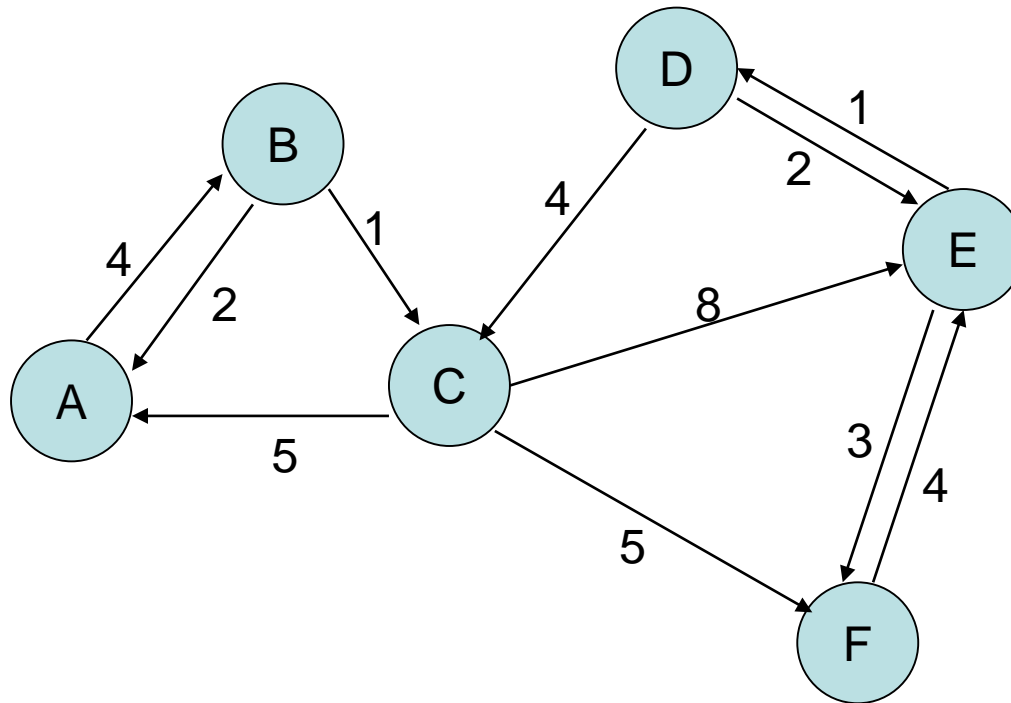
# Adjacency Matrix

	A	B	C	D	E	F	G	H
A	0	1	1	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
B	1	0	$\infty$	$\infty$	1	$\infty$	3	$\infty$
C	1	$\infty$	0	1	$\infty$	$\infty$	$\infty$	$\infty$
D	$\infty$	$\infty$	1	0	$\infty$	2	$\infty$	5
E	$\infty$	1	$\infty$	$\infty$	0	2	1	1
F	$\infty$	$\infty$	$\infty$	2	2	0	$\infty$	$\infty$
G	$\infty$	3	$\infty$	$\infty$	1	$\infty$	0	$\infty$
H	$\infty$	$\infty$	$\infty$	10	1	$\infty$	$\infty$	0



# Adjacency Matrix

- Create the adjacency matrix for this graph:



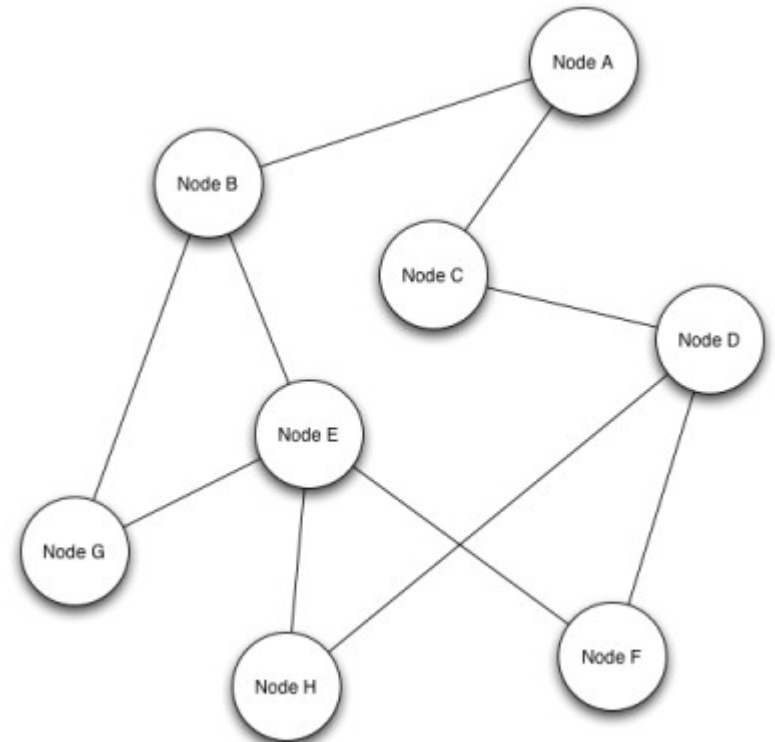


# Adjacency Matrix

- Pro: can represent directed graphs easily
- Pro: can represent weighted graphs easily
- Con: lots and lots of wasted space

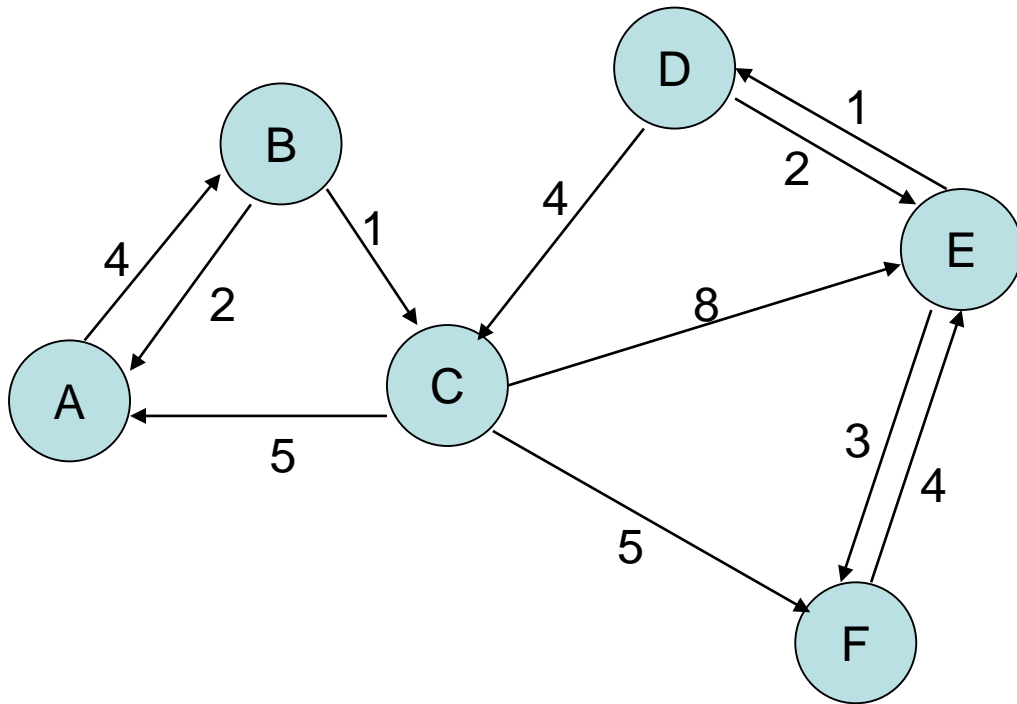
# Adjacency List

A	B	C		
B	A	E	G	
C	A	D		
D	C	F	H	
E	B	F	G	H
F	D	E		
G	B	E		
H	D	E		



# Adjacency List

- Create the adjacency list for this graph:

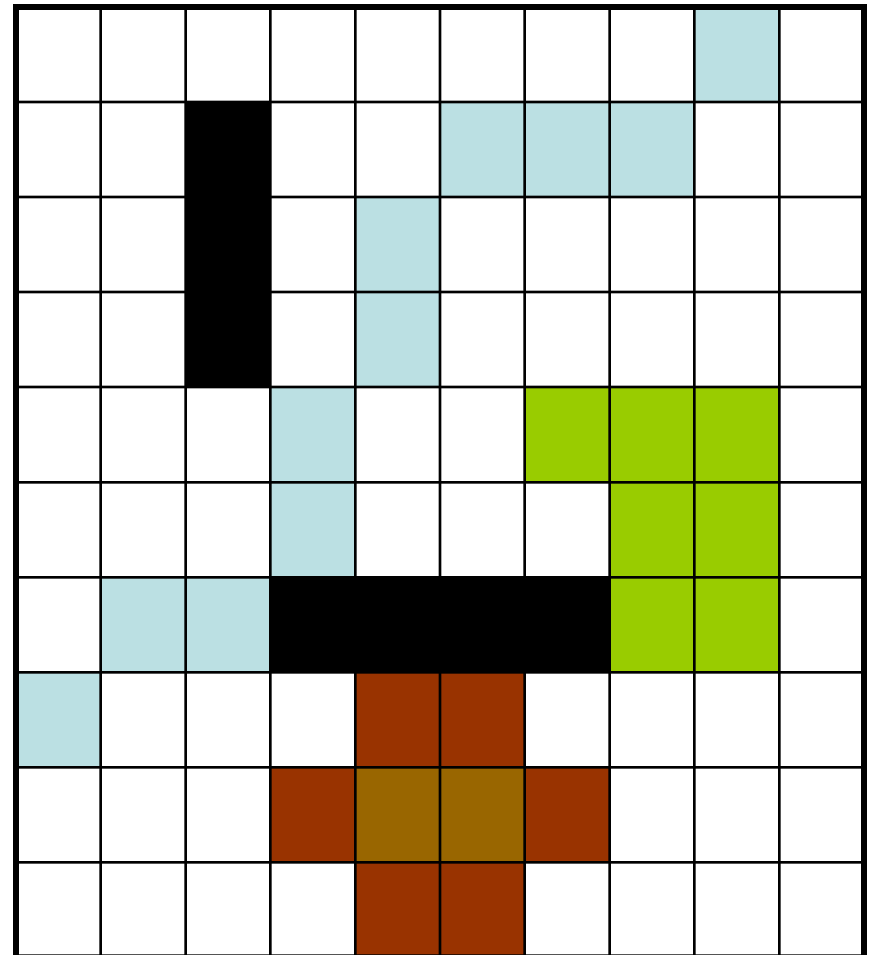


# Adjacency List

- Pro: only takes up a little space
- Pro: can represent directed graphs easily
- Con: additional attribute needed for weight

# Grid-Based

- Graph is represented implicitly
- Edge weights & directions represented by terrain types
- Pros and cons?



# Compare grid-based map



# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Graph Searches

- Used to find desired node
  - Existence
  - Connection
  - State
  - Destination (navigation)



# Graph Searches

- Open list:
  - list of nodes you need to consider in the steps ahead
- Closed list:
  - list of nodes you've already visited and don't need to consider again
- Parent:
  - for each node, keep track of which node it was expanded from

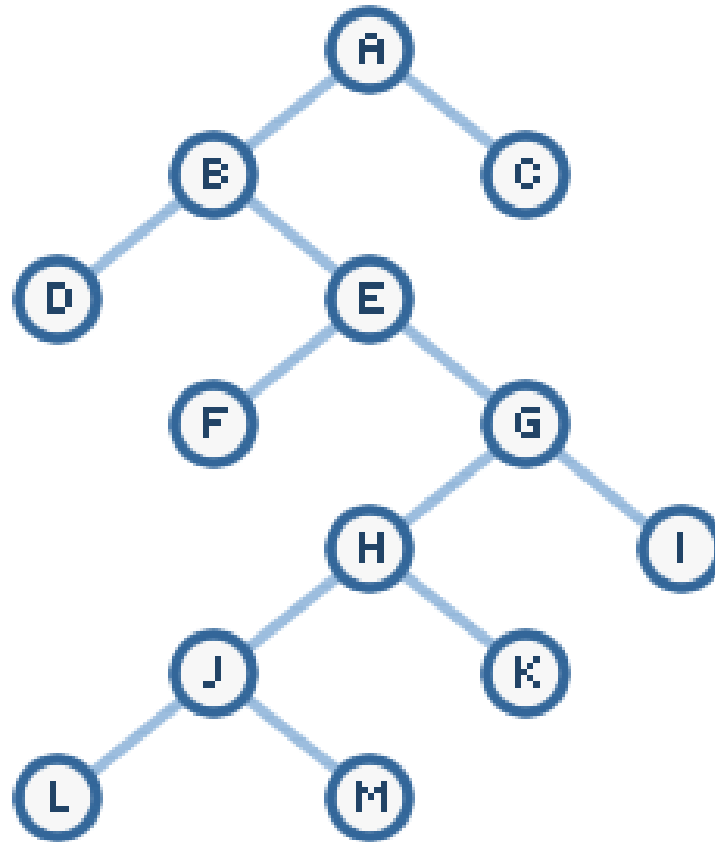
# Graph Searches

```
put start node in open list
while end node not reached && open list isn't empty:
    move node N from open list to closed list
    expand node N:
        if expanded node isn't in open or closed lists:
            add expanded node to open list
```

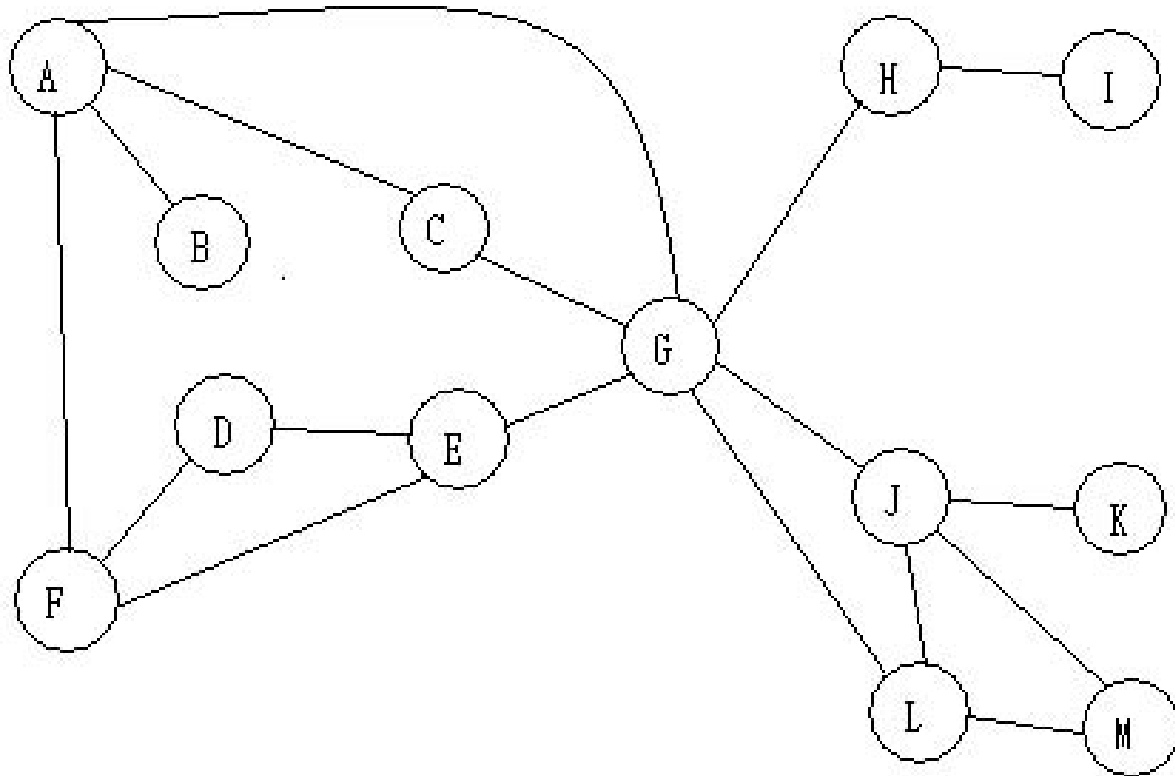
# Breadth-first Search

- Uninformed search
- Choose node from **front** of open list
- Expanded nodes get added to **back** of open list

# BFS Example 1



# BFS Example 2



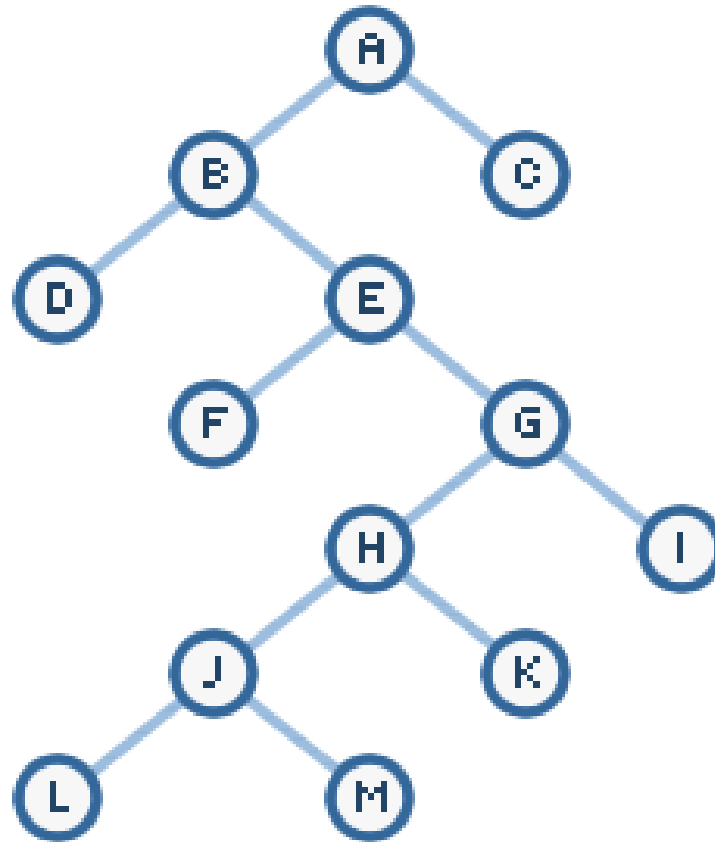
# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Depth-first Search

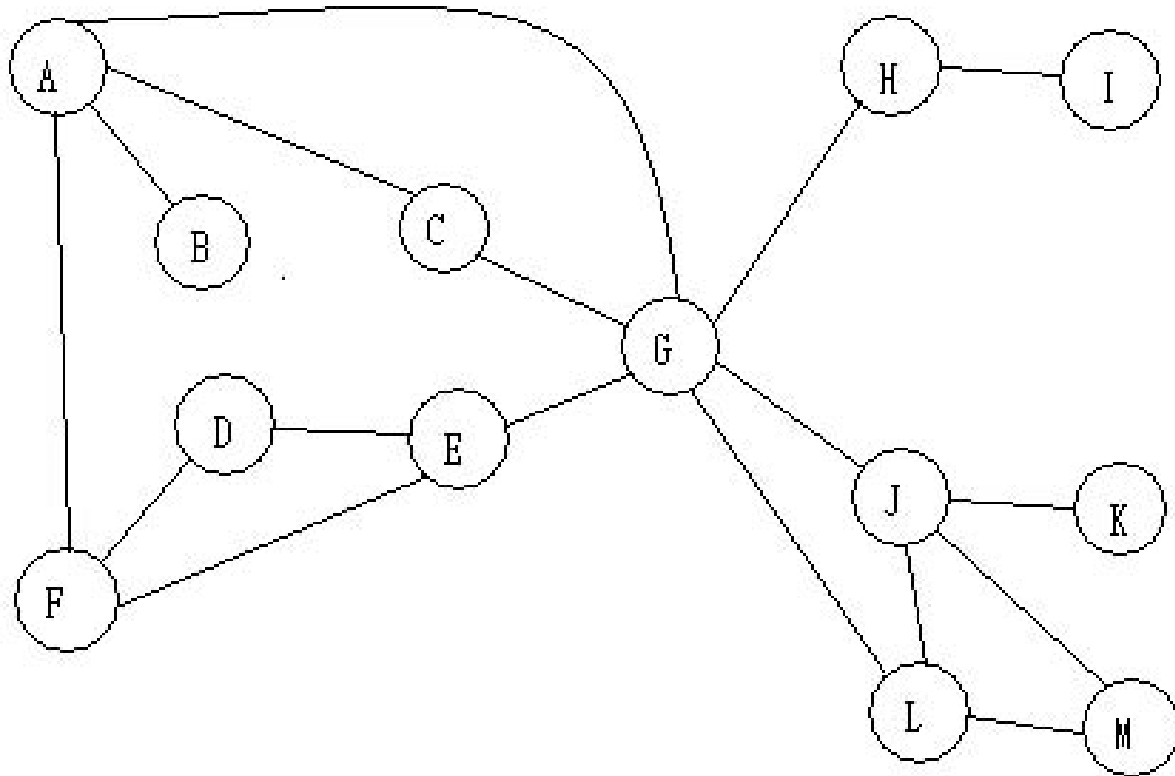
- Uninformed
- Choose node from **front** of open list
- Expanded nodes get added to **front** of open list

# DFS Example 1





# DFS Example 2



# Grid-Based DFS, BFS

	A	B	C	D	E
1					
2					
3	S				E
4					
5					

# Agenda

- Intro & Admin
- Intro to AI
- Math & Physics Review
- Intro to Pathfinding
- Graphs & Nodes
- Breadth-First Search
- Depth-First Search
- Assignment Overview

# Assignment

- Grid-based map, 10 x 10
- Specify map in text file
- Implicit representation of graph by grid
- Different map tiles types
- Bonus: user-specified dimensions