

Xin Yang  
xy213

#### Report of Homework 4

Q1:

This program using the depth first search to determine if a edge weighted digraph has a cycle in it. If there is no cycle, the program will output “No cycle!”, otherwise it will show “Cycle exists.”. In the given dataset, there is cycle.

```
/usr/local/lib/jdk1.8.0_161/bin/java ...  
Load done!  
Cycle exists.  
  
Process finished with exit code 0
```

Q2:

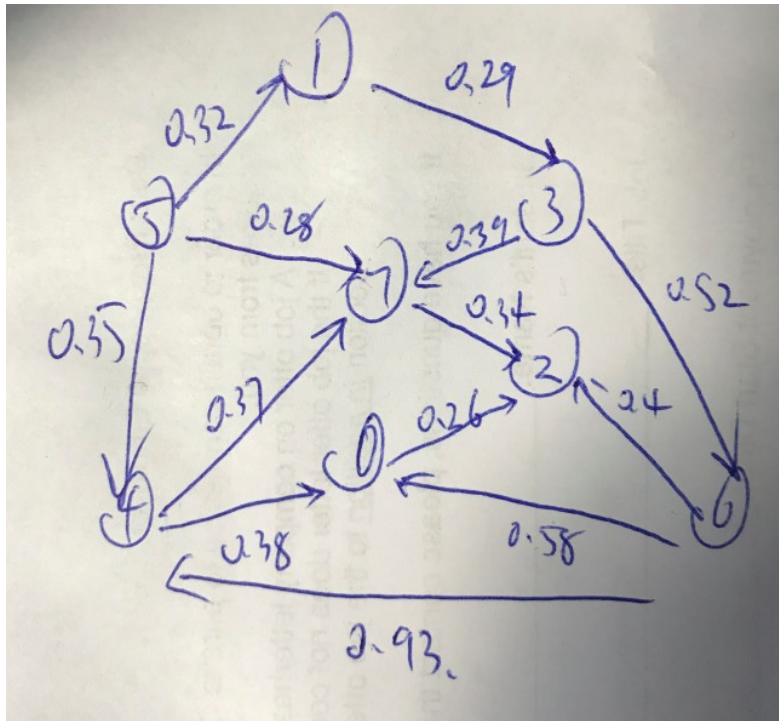
This program will by default print the total weight of both Prim’s algorithm and Kruskal’s algorithm. The implementation of Prim’s is based on the eager one.

The performance of Prim’s is better than Kruskal since Prim’s complexity is  $O(E \log V)$ , which means it will be better for dense graphs, in this dataset, the graph has 250 vertices and 1273 edges, which is a dense graph.

```
/usr/local/lib/jdk1.8.0_161/bin/java ...  
Load done!  
  
Kruskal total weight: 10.463510000000001 Duration: 5  
Prim total weight: 10.463509999999994 Duration: 2  
  
Process finished with exit code 0
```

Q3:

I will use topological sort to do the shortest and longest path since it’s a directed graph without directed cycle.



The topological sort is: 5 1 3 6 4 7 0 2.

Shortest				Longest			
0	<del>0→0</del> 1.71	4→0 0.73	4→0	0	<del>0→0</del> 1.78	4→0 2.51	4→0
1	5→1 0.32		5→1	1	5→1 0.32		5→1
2	<del>0→2</del> 1.58	7→2 0.62	7→2	2	<del>0→2</del> 1.0	7→2 2.84	7→2
3	1→3 0.61		1→3	3	1→3 0.68		1→3
4	5→4 0.35		5→4	4	5→4 0.35	6→4 2.13	6→4
5	—		—	5	—		—
6	3→6 1.13		3→6	6	3→6 1.2		3→6
7	5→7 0.28		5→7	7	5→7 0.28	3→7 1.07	4→7 2.5
5 1 3 6 4 7 0 2							

Q4:

(a):

0	-		
1		5-71 <del>1-05</del>	5-71 1-05 0.93
2	0-72 0.26		0-72 0.26
3		7-73 0.99 <del>6-74</del>	7-73 0.99
4	<del>2-74</del> 0.38	0.26 4-75 0.61 <del>3-76</del>	6-74 0.26
5	<del>4-75</del> 0.73		4-75 0.61
6		1.51	3-76 1.51
7	<del>2-77</del> 0.6	2-77 2-77 0.6	2-77 0.6

2 4 7 5 3 1 4

(b):

0		
1	5-71 1-05	
2	0-72 0.26	
3	7-73 0.99	
4	0-74 0.38	5-74 0.67
5	4-75 0.73	
6	3-76 1.51	
7	2-77 0.6	

2 4 7 5 3 1

Q5:

This program will print all the steps of both dfs and bfs, and the first number represents the counting number of visited vertices, the last number is the current visited vertex.

```
264344 DFS Visited: 236006
264345 DFS Visited: 236213
264346 DFS Visited: 236009
```

```
264344 BFS Visited: 84326  
264345 BFS Visited: 84337  
264346 BFS Visited: 84336
```

Q6:

Running the Dijkstra's algorithm on the datasets from Q4(a) and Q4(b) will both throw an `IllegalArgumentException`, as there are negative weights in both datasets. If I delete the negative weight detection code, then this program will fall into a dead loop because the negative weight will always decrease the total weights and to the nature of greedy algorithm, the program will keep following the negative weight edge.

```
/usr/local/lib/jdk1.8.0_161/bin/java ...  
Load done!  
Exception in thread "main" java.lang.IllegalArgumentException: Edge DirectedEdge@7f31245a has negative weight  
    at DijkstraSP.<init>(DijkstraSP.java:12)  
    at hw4_6.main(hw4_6.java:9)  
Process finished with exit code 1
```