

## Homework 4

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### Describe:

Using the algorithm given by professor in the lecture, my code can construct the illumination cone of my object.

1. I took 5 photos of an up-side-down bowl in a dark room. The only light source is the smart phone's flashlight.
2. Load the images, change them to grayscale and create the sample images matrix  $T$ .
3. Get the SVD of the matrix  $T \cdot T'$ . Thus, in my opinion,  $B = T' \cdot V$  is the approximation. Because, the  $s$  is composed of the magnitude matrix  $Sc$  and the direction vector of the light source  $s$ . So,  $T' = B \cdot (Sc \cdot s)$ , where  $T'$  is  $N \times 5$ ,  $B$  is  $N \times 3$ ,  $Sc$  is  $3 \times 3$  and  $s$  is  $3 \times 5$ .  $B$  is the product of the albedo and normal.  $T \cdot T' = s' \cdot (Sc' \cdot B' \cdot B \cdot Sc) \cdot s$ . If we do SVD of  $T \cdot T' = V D V'$  in this equation  $V$  is  $5 \times 5$  and the norm of each row equals 1. We need to choose the first 3 largest singular value and their corresponding matrix  $V$ . We can approximate  $s' = V$  which is  $5 \times 3$ . This time the norm of each row of  $V$  does not equal 1 but we need  $V' \cdot V = s \cdot s' = 1$ ,  $B \cdot Sc = T' \cdot V$ . I think the  $D^{(-0.5)}$  in the algorithm given by professor may be another kind of approximation, but I don't fully understand.
4. Another approximation, we can use any other  $s$  whose norm equals 1, to get synthetic images.
5. I think it is better to display all the images in a video. So, I make a video of all the images.

Note: In my code, the  $\theta$  is the angle between Z axis and the direction of illumination vector  $S$  in the illumination sphere. And the angle  $\phi$  is between the X axis and the projection of  $S$  in XY plane. Because it is a sphere in 3D,  $\theta$  is from 0 to  $\pi$  and  $\phi$  is from 0 to  $2\pi$ . These notations are a little different from the professor's in the lecture. But it makes sense and is easy for me to understand.

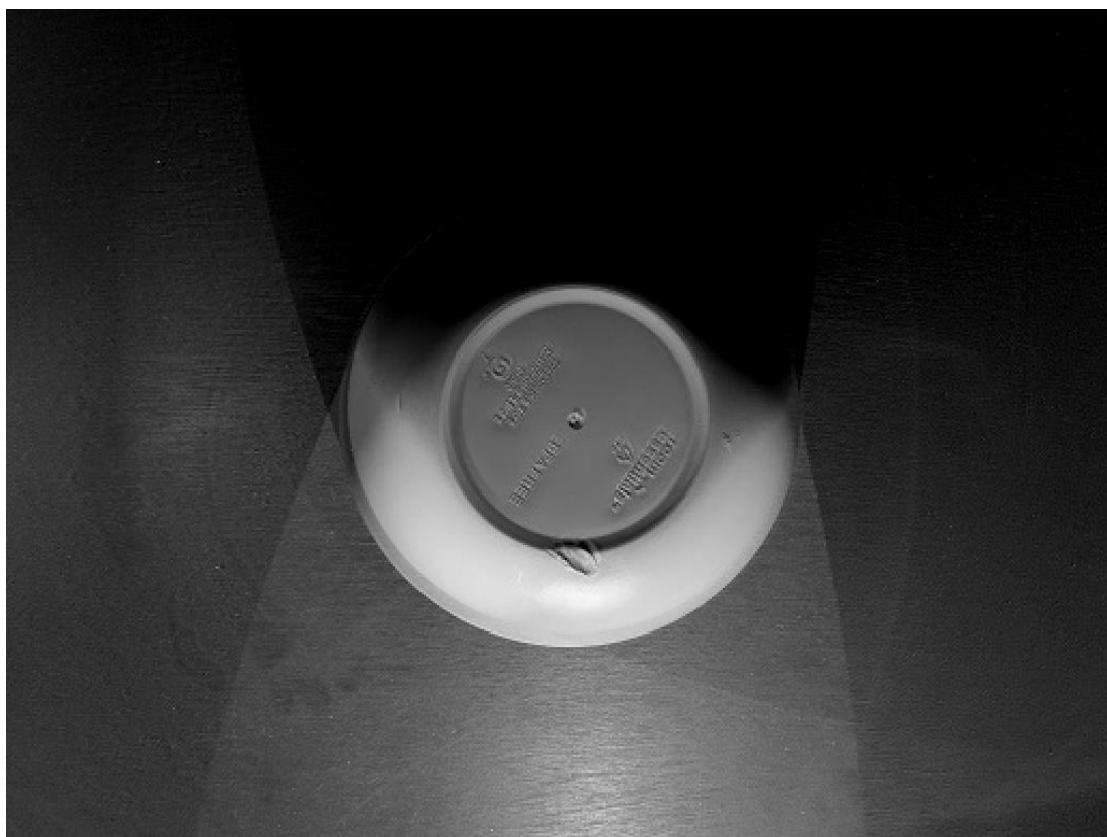
Here are the 5 samples:



Here are two synthetic images picked up from the video.



Theta=0.4 phi=1.4



Theta=0.9 phi=1.1