

```
1: import sympy as sp
2: import numpy as np
3: import functools
4:
5: x, y = sp.symbols('x y', real=True)
6: f = 3 * (x - 5)**4 + (10 * ((y - 9)**2))
7: g = sp.Max(x - 5, 0) + (10 * sp.Abs(y - 9))
8: relu = sp.Max(x, 0)
9:
10: def f_real(x, y):
11:     return 3 * (x - 5)**4 + 10 * (y - 9)**2
12:
13:
14: def g_real(x, y):
15:     return np.maximum(x - 5, 0) + 10 * np.abs(y - 9)
16:
17: def relu_real(x):
18:     return np.maximum(x, 0)
19:
20:
21: def apply_sym(x, f):
22:     for x_sym, x_val in zip(f.free_symbols, x):
23:         f = f.subs(x_sym, x_val)
24:     return f
25:
26: config = {
27:     "f": {
28:         "sym": f,
29:         "real": f_real,
30:         "name": "f",
31:     },
32:     "g": {
33:         "sym": g,
34:         "real": g_real,
35:         "name": "g",
36:     },
37:     "relu": {
38:         "sym": relu,
39:         "real": lambda x: max(x, 0),
40:         "name": "relu",
41:     }
42: }
43:
44: class GradientDescent():
45:     def __init__(self):
46:         self._max_iter = 1000
47:         self._debug = False
48:         self._converged = lambda x1, x2: False
49:         self._epsilon = 0.0001
50:         self._dimension = None
51:         self._beta = 0
52:         self._algorithm = None
53:         self._iteration = None
54:         self._function = None
55:         self._sum = None
56:         self._x_value = None
57:         self._step_coeff = None
58:         self._converged_value = None
59:         self._grad_value = None
60:         self._m = None
61:         self._v = None
62:         self._adam_grad = None
63:         self._beta = None
64:         self._beta2 = None
65:         self._step_size = None
66:         self._z = None
67:         self._f_star = None
68:
69:     def step_size(self, a):
70:         self._step_size = a
71:         return self
72:
73:     def beta(self, b):
74:         self._beta = b
75:         return self
76:
77:     def beta2(self, b):
78:         self._beta2 = b
79:         return self
80:
81:     def epsilon(self, e):
82:         self._epsilon = e
83:         return self
84:
85:     def function(self, f, function_name=None, dimension=None):
86:         self._function = f
87:         self.function_name = function_name
88:         self._dimension = dimension
89:         return self
90:
91:     def sym_function(self, function, function_name=None):
92:         self.function_name = function_name
93:         self._dimension = len(function.free_symbols)
94:         def fn(x):
95:             return apply_sym(x, function)
96:
97:         diffs = [function.diff(var) for var in function.free_symbols]
98:
99:         def grad(x):
100:             return np.array([
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101:         apply_sym(x, diff) for diff in diffs])
102:
103:     self._function = fn
104:     self._gradient = grad
105:     return self
106:
107: def gradient(self, g):
108:     self._gradient = g
109:     return self
110:
111: def max_iter(self, m):
112:     self._max_iter = m
113:     return self
114:
115: def start(self, s):
116:     self._start = s
117:     self._x_value = s
118:     return self
119:
120: def debug(self, d):
121:     self._debug = d
122:     return self
123:
124: def converged(self, c):
125:     self._converged = c
126:     return self
127:
128: def set_iterate(self, f):
129:     self.iterate = functools.partial(f, self)
130:     return self
131:
132: def algorithm(self, alg):
133:     self._algorithm = alg
134:     if self._algorithm == "rmsprop":
135:         import rmsprop
136:         self.set_iterate(rmsprop.iterate)
137:     elif self._algorithm == "adam":
138:         import adam
139:         self.set_iterate(adam.iterate)
140:     elif self._algorithm == "heavy_ball":
141:         import heavy_ball
142:         self.set_iterate(heavy_ball.iterate)
143:     else:
144:         raise Exception("Unknown algorithm:" + alg)
145:     return self
146:
147: def state_dict(self):
148:     print(self._function(self._x_value))
149:     return {
150:         "alg": self._algorithm,
151:         "function_name": self.function_name,
152:         "iteration": self._iteration,
153:         "step_coeff": self._step_coeff,
154:         "adam_grad": self._adam_grad,
155:         "f(x)": self._function(self._x_value),
156:         "epsilon": self._epsilon,
157:         "converged": self._converged_value,
158:         "gradient": self._grad_value,
159:         "m": self._m,
160:         "v": self._v,
161:         "beta1": self._beta,
162:         "beta2": self._beta2,
163:         "alpha": self._step_size,
164:         "sum": self._sum,
165:         "z": self._z,
166:         **{"x" + str(i): self._x_value[i] for i in range(len(self._x_value))},
167:     }
168:
169: def run2csv(self, fname, summarise=True):
170:     import pandas as pd
171:     iterations = list(self.iterate())
172:     df = pd.DataFrame(iterations)
173:     df.to_csv(fname)
174:     if summarise:
175:         with open(fname + ".summary", "w") as f:
176:             print(f"iterations: {len(df)}", file=f)
177:             print(f"start: {df['x0'][0]} {df['x1'][0]}", file=f)
178:             print(f"final: {df['x0'][len(df) - 1]} {df['x1'][len(df) - 1]}", file=f)
179:
180:
181: if __name__ == "__main__":
182:     print(f.diff(x), f.diff(y))
183:     print(g.diff(x), g.diff(y))
```