

```
1: library(stats)
2:
3: # Define the functions for  $p(W \geq 8 \mid \theta)$  and  $p(\theta)$ 
4: p_W_given_theta <- function(theta) {
5:   1 - pbinom(7, 52, theta)
6: }
7:
8: p_theta <- function(theta) {
9:   dbeta(theta, 3, 29)
10: }
11:
12: # Compute the joint probability by integrating the product of the two functions
13: joint_probability <- function(theta) {
14:   p_W_given_theta(theta) * p_theta(theta)
15: }
16:
17: # Integrate the joint probability function numerically
18: result <- integrate(joint_probability, lower = 0, upper = 1)
19:
20: # The result$value contains the estimated probability
21: print(paste("Estimated probability:", result$value))
```