

2. Statistical Learning

1

- a) Better. The model is unlikely to overfit for large dataset and small number of features.
- b) Worse. Too little data for the given number of features can cause overfitting.
- c) Better. We want more flexible function to capture the relationship between the predictors and response.
- d) Worse. More flexible model is more likely to pick up more noise.

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- a) $n=500$, $p=3$. Regression, inference.
- b) $n=20$, $p=13$, Classification, prediction.
- c) $n=52$, $p=3$, Regression, prediction.

3

Bias. Decreases with flexibility until it reaches 0.

Variance. Starts higher than 0, there is always some variance. Increases with flexibility.

Irreducible error. Constant, inherent to any ML problem.

Testing error = Bias + Variance + Irreducible error.

Training error = Bias + Irreducible error - noise we capture.

When training, we fit some of the noise in the data. This makes training error lower than the sum of Bias + Irreducible error. On the other hand, this introduces variability to the estimate which is reflected in the Variance factor of the testing error.

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- a)

Application: Cancer diagnosis.
Response: Patient has cancer: yes/no.
Predictors: Values in blood sample.
Goal: Prediction.

Application: Spam classifier.
Response: Mail is spam: yes/no.
Predictors: Bag of words, sender, number of similar emails.
Goal: Prediction.

Application: IVY school acceptance.
Response: Student was accepted in IVY school: yes/no.
Predictors: High school grades, place of birth.
Goal: Inference.

b)
Application: Stock price prediction.
Response: Next week's stock price.
Predictors: Historical stock prices, news feed.
Goal: Prediction.

Application: Housing prices.
Response: Price of the house.
Predictors: Area, size, number of rooms.
Goal: Inference.

Application: Salary estimation.
Response: Expected salary.
Predictors: Age, years of education.
Goal: Inference.

c)
Cluster analysis might be helpful for:
- Market segmentation for better customer targeting.
- Anomaly detection, such as broken engines.

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Very flexible methods are generally preferred to the less flexible ones because of the higher predictive power.

There are two scenarios where more flexibility might not be desirable: - We don't have enough training data for the chosen number of features. - We want our model to be more interpretable. E.g. we might prefer linear regression.

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Parametric approach has pros and cons.

Pros:

- Interpretable. We can investigate relationships between features and output.
- Clearly defined. We define the predictive function. This is simpler than estimating arbitrary function.
- Needs less data. If the predictive function is simple, we don't need much data to fit.

Cons:

- Less flexible. We need many parameters to capture highly non-linear relationship between features and output.

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a)

Obst	Dist	Y
1	3	R
2	2	R
3	$\sqrt{10}$	R
4	$\sqrt{5}$	G
5	$\sqrt{2}$	G
6	$\sqrt{3}$	R

b) Green. Observation 5 which is the closest point is green.

c) Red. Closes three observations are 2, 5, and 6. Two of which are green.

d) K will be small. If one wants to capture the decision boundary of highly non-linear function, the function should be able to quickly adjust to the local changes. This is only possible with small K.