Heuristic Analysis

The book "Artificial Intelligence: A Modern Approach" gives three tips to build an evaluation function. They are:

- 1. The evaluation function should order the terminal states in the same way as the true utility function.
- 2. The computation must not take too long.
- 3. The evaluation function should be strongly correlated with the actual chances of winning for the terminal states.

So, looking at the Isolation game context, we have to use something to measure the utility of the given state that should be simple and fast. The basic way to evaluate a state is using the quantity of the available moves. The available moves are somehow connected to the position on the board. The center of the board we have 8 available moves. As we get close to the wall we have less options. And finally, the corners are the worst position.

Evaluation Function 1

The function was given by:

f = 3 * sum(weights of own moves) - sum(weights of the opponent moves)

The weights is defined on the following table.

2	3	4	4	4	3	2
3	4	6	6	6	4	3
4	6	8	8	8	6	4
4	6	8	8	8	6	4
4	6	8	8	8	6	4
3	4	6	6	6	4	3
2	3	4	4	4	3	2

Table 1 - Board weights

This is a weighted linear function. This approach is similar to the "AB_Improved", however this one uses weights that gives some positional information about the board.

Evaluation Function 2

The function was given by:

$$f = 3 * own moves - opponent moves$$

This function works in a defensive way. It will be moving in order to maximize its own available moves.

Evaluation Function 3

The function was given by:

$$if move_count >= 12$$

$$f = -2 * opponent_moves$$

$$else$$

$$f = 2 * (own moves - common moves) + common moves - 3 * (opponent moves - common moves)$$

While working on the evaluation functions, I noticed that following a single strategy doesn't work. So, I tried to mix up the strategies.

This function works somehow offensive and defensive in the beginning of the game and after 12 moves, it will move more aggressively.

Results

I ran the tournament 6 times, so:

- the "AB_Custom" was able to achieve over 70% winning rate on 5 of 6 tournaments compared to the "AB_Improved" that achieved only on 2 tournaments;
- the "AB_Custom_2" seems to perform better than the "AB_Custom_3", since the perform was better in 4 of 6 tournaments.

Even though AB_Custom performed better than AB_Improved, I still would recommend the AB_Improved because:

- AB_Improved goes deeper because it performs simple operations allowing it to go deeper.
- AB_Custom might performs better than AB_Improved because it might go as deep as the AB_Improved, however defining a weight table isn't an easy task and changing the board size would require a redefinition of the weight table.

Match #	Opponent	AB_Improved	AB_Custom	AB_Custom_2	AB_Custom_3			
		Won Lost	Won Lost	Won Lost	Won Lost			
1	Random	6 4	9 1	9 1	10 0			
2	MM_Open	6 4	8 2	6 4	7 3			
3	MM_Center	8 2	9 1	7 3	8 2			
4	$\mathtt{MM}_\mathtt{Improved}$	5 5	9 1	8 2	9 1			
5	AB_Open	5 5	6 4	5 5	5 5			
6	AB_Center	5 5	6 4	6 4	5 5			
7	AB_Improved	7 3	6 4	5 5	6 4			
	Win Rate:	60.0%	75.7%	65.7%	71.4%			

Playing Matches

Match #	Opponent	AB_Improved	AB_Custom	AB_Custom_2	AB_Custom_3			
		Won Lost	Won Lost	Won Lost	Won Lost			
1	Random	10 0	10 0	9 1	10 0			
2	MM_Open	8 2	8 2	9 1	7 3			
3	MM_Center	6 4	10 0	10 0	8 2			
4	${\tt MM_Improved}$	5 5	5 5	7 3	9 1			
5	AB_Open	4 6	6 4	6 4	4 6			
6	AB_Center	6 4	4 6	5 5	5 5			
7	AB_Improved	5 5	6 4	3 7	7 3			
	Win Rate:	62.9%	 70.0%	70.0%	71.4%			

Playing Matches

Match #	Opponent	AB_I	mpr	oved	AB_	Cus	stom	AB_C	ust	om_2	AB_C	ust	om_3
		Won	:	Lost	Won		Lost	Won]	Lost	Won		Lost
1	Random	10		0	10		0	10		0	9		1
2	MM_Open	7		3	7		3	8		2	8		2
3	MM_Center	8		2	10		0	8		2	9		1
4	${\tt MM_Improved}$	7		3	9		1	5		5	3		7
5	AB_Open	5		5	5		5	6		4	5		5
6	AB_Center	7		3	8		2	6		4	7		3
7	AB_Improved	4		6	2		8	5		5	4	 	6

Playing Matches

Win Rate: 68.6% 72.9% 68.6% 64.3%

Match #	Opponent	AB_I: Won	-	oved Lost	AB_ Won		stom Lost	AB_C		om_2 Lost	AB_C Won		om_3 Lost
1	Random	9		1	10		0	10		0	8		2
2	MM_Open	10		0	8		2	7		3	7		3
3	MM_Center	9		1	10		0	8		2	9		1
4	${\tt MM_Improved}$	8		2	8		2	7		3	8		2
5	AB_Open	4		6	6		4	8		2	6		4
6	AB_Center	6		4	6		4	6		4	5		5
7	AB_Improved	5	 	5 	5 	 	5 	6	 	4	7	 	3

Win Rate: 72.9% 75.7% 74.3% 71.4%

Playing Matches

Match #	Opponent	AB_Improved	AB_Custom	AB_Custom_2	AB_Custom_3		
		Won Lost	Won Lost	Won Lost	Won Lost		
1	Random	9 1	8 2	10 0	8 2		
2	MM_Open	8 2	5 5	7 3	7 3		
3	MM_Center	10 0	9 1	9 1	8 2		
4	${\tt MM_Improved}$	5 5	9 1	6 4	7 3		
5	AB_Open	4 6	6 4	4 6	4 6		
6	AB_Center	5 5	5 5	6 4	5 5		
7	AB_Improved	7 3	4 6	5 5	3 7		
	Win Rate:	68.6%	65.7%	67.1%	60.0%		

Playing Matches

Match #	Opponent	AB_I	mpr	roved	AB_	Cu	stom	AB_C	ust	om_2	AB_C	ust	om_3
		Won		Lost	Won		Lost	Won		Lost	Won		Lost
1	Random	10		0	9		1	10		0	9		1
2	MM_Open	9		1	8		2	6		4	7		3
3	MM_Center	8		2	8		2	10		0	9		1
4	${\tt MM_Improved}$	7		3	10		0	8		2	8		2
5	AB_Open	7		3	3		7	7		3	5		5
6	AB_Center	6		4	5		5	6		4	6		4
7	AB_Improved	5		5	6	I	4	5		5	3		7

Win Rate: 74.3% 70.0% 74.3% 67.1%