

$$initialState := \emptyset \quad (1)$$

$$occupies(p, c) \text{ iff } (p, c) \in currentState \quad (2)$$

$$occupied(c) \text{ iff } occupies('x, c) \vee occupies('o, c) \quad (3)$$

$$rows := hRows \cup vRows \cup diagonals \text{ where } hRows = \{\{1, 2, 3\}, \{4, 5, 6\}, \{7, 8, 9\}\} \wedge vRows = \{\{1, 4, 7\}, \{2, 5, 8\}, \{3, 6, 9\}\} \quad (4)$$

$$threeInRow(p) \text{ iff } \exists R \in rows. \forall c \in R. occupies(p, c) \quad (5)$$

$$boardFull := |currentState| = 9 \quad (6)$$

$$gameOver := boardFull \vee threeInRow('x) \vee threeInRow('o) \quad (7)$$

$$playerToMove := \begin{cases} 'x & \text{if even}(|currentState|) \\ 'o & \text{otherwise} \end{cases} \quad (8)$$

$$even(n) \text{ iff } n \bmod 2 = 0 \quad (9)$$

$$legalToMoveIn(c) \text{ iff } \neg occupied(c) \wedge \neg gameOver \quad (10)$$

$$BLACK := color(0, 0, 0) \quad (11)$$

$$WHITE := color(255, 255, 255) \quad (12)$$

$$BLUE := color(0, 0, 255) \quad (13)$$

$$GREEN := color(0, 255, 0) \quad (14)$$

$$RED := color(255, 0, 0) \quad (15)$$

$$gridDisplay := \{L1, L2, L3, L4\} \text{ where } L1 = segment(point(200, 700), point(200, 400), BLACK) \wedge L2 = segment(point(200, 400), point(200, 100), BLACK) \wedge L3 = segment(point(200, 100), point(200, 400), BLUE) \wedge L4 = segment(point(200, 400), point(200, 700), BLUE) \quad (16)$$

$$fontSize := 36 \quad (17)$$

$$centerX(c) := 150 + 100 \times c - 1 \bmod 3 \quad (18)$$

$$centerY(c) := 650 - 100 \times \lfloor c - 1 / 3 \rfloor \quad (19)$$

$$xImage(c) := text("x", point(centerX(c), centerY(c)), fontSize, BLUE) \quad (20)$$

$$oImage(c) := text("o", point(centerX(c), centerY(c)), fontSize, GREEN) \quad (21)$$

$$cellDisplay(c) := \begin{cases} \{xImage(c)\} & \text{if } (x, c) \in currentState \\ \{oImage(c)\} & \text{if } (o, c) \in currentState \\ \emptyset & \text{otherwise} \end{cases} \quad (22)$$

$$gameBoard := \{1..9\} \quad (23)$$

$$cellDisplays := \bigcup_{c \in gameBoard} cellDisplay(c) \quad (24)$$

$$currentPlayerDisplay := \begin{cases} \{text("x's turn", point(100, 750), fontSize, BLACK)\} & \text{if } playerToMove = 'x \\ \{text("o's turn", point(100, 750), fontSize, BLACK)\} & \text{otherwise} \end{cases} \quad (25)$$

$$restartLeft := 350 \quad (26)$$

$$restartRight := 550 \quad (27)$$

$$restartBottom := 725 \quad (28)$$

$$restartTop := 775 \quad (29)$$

$$restartBottomLeftPoint := point(restartLeft, restartBottom) \quad (30)$$

$$restartBottomRightPoint := point(restartRight, restartBottom) \quad (31)$$

$$restartTopLeftPoint := point(restartLeft, restartTop) \quad (32)$$

$$restartTopRightPoint := point(restartRight, restartTop) \quad (33)$$

$$mid(a, b) := a + b / 2 \quad (34)$$

$$restartMidX := mid(restartLeft, restartRight) \quad (35)$$

$$restartMidY := mid(restartBottom, restartTop) \quad (36)$$

$$restartButton := \{A1, A2, A3, A4, txt\} \text{ where } A1 = segment(restartBottomLeftPoint, restartBottomRightPoint) \quad (37)$$

$$gameResultDisplay := \begin{cases} \{text("xwon", point(200, 750), fontSize, BLUE)\} & \text{if } threeInRow('x) \\ \{text("owon", point(200, 750), fontSize, GREEN)\} & \text{if } threeInRow('o) \\ \{text("catgotit", point(200, 750), fontSize, RED)\} & \text{otherwise} \end{cases} \quad (38)$$

$$images := \begin{cases} gameOverDisplay & \text{if } gameOver \\ inPlayDisplay & \text{otherwise} \end{cases} \text{ where } alwaysDisplay = gridDisplay \cup cellDisplays \cup restartButton \quad (39)$$

$$xMin(c) := 100 + 100 \times c - 1 \mod 3 \quad (40)$$

$$xMax(c) := 200 + 100 \times c - 1 \mod 3 \quad (41)$$

$$yMin(c) := 600 - 100 \times \lfloor c - 1 / 3 \rfloor \quad (42)$$

$$yMax(c) := 700 - 100 \times \lfloor c - 1 / 3 \rfloor \quad (43)$$

$$cellClicked(c) \text{ iff } mouseClicked \wedge mouseX > xMin(c) \wedge mouseX < xMax(c) \wedge mouseY > yMin(c) \wedge mouseY < yMax(c) \quad (44)$$

$$restartClicked := mouseClicked \wedge mouseX > restartLeft \wedge mouseX < restartRight \wedge mouseY > restartBottom \wedge mouseY < restartTop \quad (45)$$

$$moveMadeIn(c) \text{ iff } cellClicked(c) \wedge legalToMoveIn(c) \quad (46)$$

$$movesMade := \{(playerToMove, c) \mid c \in gameBoard \wedge moveMadeIn(c)\} \quad (47)$$

$$newState := \begin{cases} initialState & \text{if } restartClicked \\ currentState \cup movesMade & \text{otherwise} \end{cases} \quad (48)$$