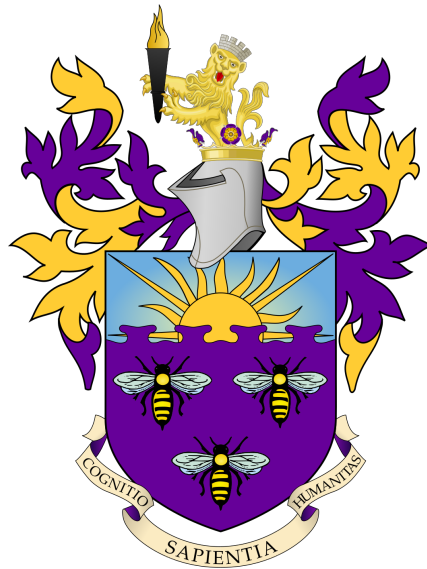


The University of Manchester

Building a Ray-Traced Rendering Engine on Sparse Voxel Grids



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Abstract

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Acknowledgements

What should I acknowledge?! I am citing [1], and [2] hell

1 Introduction

1.1 Motivation

1.2 Aims

1.3 Objectives

1.4 Report structure

2 Background and Literature Review

2.1 Rendering engines

Graphics engines serve as the core software components responsible for rendering visual content in applications ranging from video games to scientific simulations and visual effects in movies. Engines abstract the complexities of rendering by providing developers with high-level tools and interfaces to represent digital environments.

The evolution of rendering engines over time reflects the advancements in computational techniques and hardware capabilities enabling more realistic and immersive experiences

[add history]

2.1.1 Primitives

At the heart of any graphical engine is the concept of primitives, the simplest forms of graphical objects that the engine can process and render. Primitives are building blocks from which more complex shapes and scenes can be constructed.

Polygons, particularly triangles, are the most commonly used primitives in 3D graphics. This is owed to their simplicity and flexibility, allowing the construction of virtually any 3D shape through *tessellation*. Polygonal meshes define the surfaces of objects in a scene, with each vertex of a polygon typically associated with additional information such as color, texture coordinates, and normal vectors for lighting calculations.

Voxels represent a different approach to defining 3D shapes, they are essentially three-dimensional pixels. Where polygons define surfaces, voxels establish volume, with each voxel being able to contain color and density information. This characteristic makes voxels particularly well-suited for rendering scenes with materials that have intricate internal structures, such as fog, smoke, fire and fluids.

2.1.2 Ray-tracing vs. Rasterization

Rendering engines can utilise two main rendering techniques for rendering scenes: ray tracing and rasterization, both having their advantages and trade-offs.

Rasterization is the most widespread technique used in real-time applications. It converts the 3D scene into a 2D image by projecting vertices onto the screen, filling in pixels that make up polygons, and applying textures and lighting. Over the development of the industry of graphics programming, graphics hardware has become extremely efficient at performing rasterization, making it the standard for video games and interactive applications.

Ray-Tracing, in contrast, simulates the path of light as rays travelling through a scene to produce images with realistic lighting, shadows, reflections, and refractions. Ray tracing is computationally intensive but yields higher-quality images, making it favored for applications where visual fidelity is critical. However, recent advancements in hardware have begun to bring real-time ray tracing to interactive applications.

2.2 Representing voxels

To efficiently represent and manipulate voxels in program memory, various data structures can be employed. Each method entails trade-offs between memory usage, access speed and complexity of implementation. Access speed refers to the time complexity of querying the data structure at an arbitrary point in space to retrieve a potential voxel.

2.2.1 Voxel grids

A voxel grid is the most straightforward and intuitive approach to representing volumetric data. The 3D space is divided into a regular grid of voxels, each holding information such as color, material properties, or density. This method provides direct $O(1)$ access to voxel data.

However, this simplicity comes at a significant disadvantage: memory consumption. As the bounding volume or the level of detail of the scene increases, the memory required to store the voxel grows by $O(N^3)$. Additionally, empty space can occupy a majority of the memory space. For example, consider a scene with two voxels that are a million units apart in all axes. A voxel grid would have to store all the empty voxels inbetween; 10^{18} memory units reserved, 2 of which carry useful data. This limitation makes the naive voxel grids impractical for large or highly detailed scenes.

2.2.2 Hierarchical voxel grids (N-trees)

To mitigate this issues, hierarchical grids, such as octrees, are employed. An octree is a tree data structure where each node represents a cubic portion of 3D space and has up to eight children. This division continues recursively, allowing for varying levels of detail within the scene: larger volumes are represented by higher-level nodes, while finer details are captured in lower levels.

The primary advantage of using an octree is spatial efficiency. Regions of the space that are empty or contain uniform data can be represented by a single node, significantly reducing the memory footprint. Furthermore, octrees facilitate efficient querying operations, such as collision detection and ray tracing, by allowing the algorithm to quickly discard large empty or irrelevant regions of space.

Hierarchical grids introduce complexity in terms of implementation and management. Operations such as updating the structure or balancing the tree to ensure efficient access can be more challenging compared to uniform grids. Another sacrifice is access-time, as querying an arbitrary region of space can entail walking down the tree for several levels. Nonetheless, for applications requiring large, detailed scenes with a mix of dense and sparse regions, the benefits of hierarchical representations often outweigh these drawbacks. This is why N-trees are frequently used in voxel engines.

[add history]

2.2.3 VDB

VDB was introduced in 2013 by Ken Museth^[3] from the DreamWorks Animation team.

It is a Volumetric, Dynamic grid that shares several characteristics with B+trees. It exploits spatial coherency of time-varying data to separately and compactly encode data values and grid topology. VDB models a virtually infinite 3D index space that allows for cache-coherent and fast data access into sparse volumes of high resolution.

At its core, VDB functions as a shallow N-tree with a fixed depth, where nodes at different levels vary in size. The top level of this tree structure is managed through a hash map, enabling VDB models to cover extensive index spaces with minimal memory overhead. This design achieves $O(1)$ access performance and can effectively store tiled data across vast spatial regions.

The VDB data structure was introduced along with several algorithms that make full use of the data structures features, offering significant improvements in techniques for efficiently rendering volumetric data. These are some of the benefits VDB have, as detailed in the original paper.

1. *Dynamic*. Unlike most sparse volumetric data structures, VDB is developed for both dynamic topology and dynamic values typical of time-dependent numerical simulations and animated volumes.

2. *Memory efficient.* The dynamic and hierarchical allocation of compact nodes leads to a memory-efficient sparse data structure that allows for extreme grid resolution.
3. *Fast random and sequential data access.* VDB supports fast constant-time random data lookup, insertion, and deletion.
4. *Virtually infinite.* VDB in concept models an unbounded grid in the sense that the accessible coordinate space is only limited by the bit-precision of the signed coordinates.
5. *Efficient hierarchical algorithms.* The **B+tree** structure offers the benefits of cache coherency, inherent bounding-volume acceleration, and fast per-branch (versus per-voxel) operations.

These benefits make VDB a very compelling data structure to serve as the building block of voxel-based rendering engine.

2.3 Ray tracing

In order to render a scene using ray tracing, camera rays are shot through the view frustum and into the scene. At each object intersection, part of a ray will get absorbed, reflected and refracted. In order to achieve realistic results, a rendering engine needs to model as many of these light interactions as possible in each frame's time budget.

This section delves into the integration of ray tracing within the graphics pipeline and the methods used to implement it, focusing on casting a ray through a scene.

2.3.1 Graphics pipeline

The graphics pipeline of a rendering engine is the underlying system of a rendering engine that transforms a 3D scene into a 2D representation that is presented on a screen. While rasterization transforms 3D objects into 2D images through a series of stages (vertex processing, shape assembly, geometry shading, rasterization, and fragment processing), the ray tracing pipeline introduces a paradigm shift. It primarily involves calculating the path of rays from the eye (camera) through pixels in an image plane and into the scene, potentially bouncing off surfaces or passing through transparent materials before contributing to the color of a pixel.

This step of calculating a ray's path is central in ray tracing, and as such, the performance of the algorithm that does this calculation is critical.

2.3.2 Casting a ray

Ray casting techniques vary depending on the representation of the 3D world within the rendering engine. This section introduces basic ray casting techniques, while subsequent discussions will cover methods specific to voxel-based environments.

Ray marching

A straightforward way to represent a 3D environment would be a mathematical function of sorts. It would take as input the coordinates point and return the properties of a material at that point (provided there is an object at there).

The first algorithm one might develop when trying to cast a ray through an unknown scene is ray marching. It involves incrementally stepping along a ray, sampling the scene for collisions at each step. The chosen step size needs to be sufficiently small to ensure no detail is missed.

While simple, ray marching is not without its drawbacks, especially in terms of performance. Considering the need to process millions of pixels per frame within the time constraints of high frame

rates, it becomes apparent that iterating a ray tens of thousands of times for every pixel is impractical for modern engines.

This requires the exploration of more advanced techniques to meet the goal of visual realism and performance.

Ray casting

A 3D environment could also be represented as a collection of polygons that form meshes.

Ray casting finds the intersection of rays with geometric primitives like (e.g. triangles, circles). This method skips stepping along the ray entirely by making use of the underlying mathematics of intersecting lines with polygons.

The fundamental issue with this approach is that rays must be checked for an intersection with all the primitives in the scene. Thus computing a single ray intersection has linear complexity in the number of polygons in the scene.

SDF

Signed distance fields (**SDF**) are a different way of representing the environment. An SDF provides the minimum distance from a point in space to the closest surface, allowing the ray marching algorithm to efficiently skip empty space and accurately determine surface intersections. With the distance to the nearest surface known, ray marching can be performed by stepping along the ray with that distance, drastically reducing the number of steps needed to cast a ray.

Combining SDF with ray marching offers a powerful method for rendering complex scenes, including soft shadows, ambient occlusion, and volumetric effects. This combination is highly flexible and can create highly detailed and intricate visual effects, particularly in procedural rendering and visual effects.

SDF are not without drawbacks, they can be difficult to maintain, and computationally expensive to generate or update. In practice, distance data can't be of arbitrary size, as that distance information comes at the cost of program memory.

[add history]

2.3.3 Casting a ray on a voxel grid

The ray casting methods presented so far do not take advantage of the discrete grid of voxel that this rendering engine is based on. In this section, efficient algorithms that can use the underlying representation of hierarchical voxel grid are presented.

DDA

On a discrete voxel grid, basic ray marching can be improved by stepping from voxel to voxel. Because the voxels are the smallest unit of space, a ray can safely step from one to the next, knowing there is nothing else in between.

The Digital Differential Analyzer (**DDA**) line drawing algorithm does precisely that, it marches along a ray from voxel to voxel, skipping all space in between.

DDA works by breaking down the minimum distance a ray has to travel to intersect a grid line on each axis. At each iteration, it steps to the closest grid intersection along the ray.

[add history]

HDDA

On a hierarchical grid the DDA algorithm can take advantage of the topology of the data structure by stepping through empty larger chunks. A ray casted using **HDDA**, essentially performs DDA at the level in the tree it is currently at.

[add figure] [add history]

A version of the HDDA algorithm for the VDB data structure was introduced by Ken Museth in 2014^[4].

This algorithm can be highly efficient, large empty areas can be skipped in a single step, drastically reducing the required steps to march a ray.

2.4 Summary of similar systems

3 Methodology

This section outlines the implementation details of the voxel rendering engine, starting from the selection of programming languages and libraries, going over the architecture of the engine, and diving deep into the data structures and algorithms employed, particularly focusing on VDB for voxel representation and the optimization of ray casting algorithms. Finally, this section will discuss the extension of these algorithms to full-fledged ray tracing, allowing for dynamic lightning and glossy material support.

3.1 Rust & wgpu

The voxel rendering engine is built using **Rust**, a programming language known for its focus on safety, speed, and concurrency^[5]. Rust’s design emphasizes memory safety without sacrificing performance, making it an excellent choice for high-performance applications like a rendering engine. The language’s powerful type system and ownership model prevent a wide class of bugs, making it ideal for managing the complex data structures and concurrency challenges inherent in rendering engines. Thanks to this no memory leak or null pointer was ever encountered throughout the development of this project.

For the graphical backend, the engine utilizes **wgpu**^[6], a Rust library that serves as a safe and portable graphics API. wgpu is designed to run on top of various backends, including Vulkan, Metal, DirectX 12, and WebGL, ensuring cross-platform compatibility. This API provides a modern, low-level interface for GPU programming, allowing for fine-grained control over graphics and compute operations. wgpu is aligned with the WebGPU specification^[7], aiming for broad support across both native and web platforms. This choice ensures that the engine can leverage the latest advancements in graphics technology while maintaining portability and performance.

The combination of Rust and wgpu offers several advantages for the development of a rendering engine:

1. *Safety and Performance:* Rust’s focus on safety, coupled with wgpu’s design, minimizes the risk of memory leaks and undefined behaviors, common issues in high-performance graphics programming. This is thanks to Rust’s idea of zero-cost abstractions.
2. *Cross-Platform Compatibility:* With wgpu, the engine is not tied to a specific platform or graphics API, enhancing its usability across different operating systems and devices.
3. *Future-Proofing:* wgpu’s adherence to the WebGPU specification ensures that the engine is built on a forward-looking graphics API, designed to be efficient, powerful, and broadly supported. It also allows the future option of supporting web platforms, once browsers adopt WebGPU more thoroughly.
4. *Concurrency:* Rust’s advanced concurrency features enable the engine to efficiently utilize multi-core processors, crucial for the heavy computational demands of rendering pipelines.

These technical choices form the foundation upon which the voxel rendering engine is constructed. Following this, the engine’s architecture is designed to take full advantage of Rust’s performance and safety features and wgpu’s flexible, low-level graphics capabilities, setting the stage for the implementation of advanced voxel representation techniques and optimized ray tracing algorithms.

3.2 Engine architecture

The engine’s operation is centered around an event-driven main loop that blocks the main thread. This loop processes various events, ranging from keyboard inputs to redraw requests, and updates the window, context, and scene accordingly, routing each event to its corresponding handler.

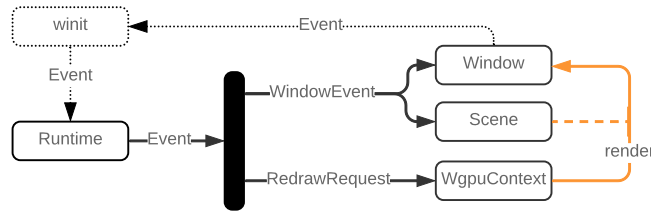


Fig. 1. Engine event-loop diagram. Dotted arrows are implemented in **winit** crate. Black lines represent the flow of events. The arrow line represents the main render function called on the GPU context on the scene for the window.

3.2.1 Runtime

At the engine's core, sits **Runtime** structure, which manages the interaction between the it's main components:

- The **Window** is a handler to the engine's graphical window. It is used in filtering **OS** events that relevant to engine, grabbing the cursor and other boilerplate.
- The **Wgpu Context** holds the creation and application of the rendering pipeline.
- The **Scene** contains information about the camera and enviornment as well as a container voxel data structure.

```

pub struct Runtime {
    context: WgpuContext,
    window: Window,
    scene: Scene,
}

impl Runtime {
    ...
    pub fn main_loop(&mut self, event: Event, ...) {
        match event {
            ...
        }
    }
};

```

Listing 1. Runtime definition

For example, window events (e.g. keyboard & mouse input) generally modify the scene, like the camera position, and therefore are routed to the **Scene** struct.

Another key event is the **RedrawRequested** event, which signals that a new frame should be rendered. This is routed to the wgpu context to start the rendering pipeline.

The **RedrawRequested** event is actually emmited in **Runtime**, when it receives the **MainEventsCleared** event, it scheduels the window for a redraw.

3.2.2 Window

The **Window** data structure, included in the **winit**^[8] crate, handles window creation and management, and provides an interface to the GUI window through an event loop. This event loop is what **Runtime**'s main loop is mounted on.

The interaction between the **Window** and the **Runtime** forms an event-driven workflow. The window emmits events and the runtime manages and distributes these events accordingly, forming a sort of feedback loop.

3.2.3 Scene

The **Scene** data structe holds information about the enviornment that is being rendered, this includes the model, camera, and engine state.

```
pub struct Scene {  
    pub state: State,  
    pub camera: Camera,  
    pub model: VDB,  
}
```

Listing 2. Scene definition

In this section, the camera and satte implementation is covered, the model will be covered in later [add link] when discussing the **VDB** implementation.

State handles information about the engine state such as cursor state and time synchronising to decouple engine events from the **FPS** (e.g. camera movement shouldn't be slower at lower FPS).

Camera describes all the elements needed to control and represent a camera:

1. *Eye*: The camera's position in the 3D space, acting as the point from which the scene is observed.
2. *Target*: The point in space the camera is looking at, determining the direction the camera is pointed in.
3. *Field of View (FOV)*: An angle representing the range that is in view. In the implementation, this refers to the FOV on the *Y* (vertical) axis.
4. *Aspect ratio*: The ratio between the width and height of the viewport. It esnures that the rendered scene maintains the correct proportions.

The eye and target are updated when moving the camera through a **CameraController** struct that handles keyboard and mouse input. Th FOV and aspect ratio are set based on the window proportions, to avoid distortion. The way in which this camera information is used will be detailed in the primitives section [add link] where we dive into what information is actually sent to the GPU in compute shaders.

3.2.4 WgpuContext

The **WgpuContext** structure is the backbone of the rendering pipeline in the voxel rendering engine. It contains the necessary components for interfacing with the GPU using the wgpu API, managing resources such as textures, shaders, and buffers, and executing rendering commands.

Broadly, **WgpuContext** has the follwing responsablities:

1. *Initialization*: The constructor sets up the wgpu instance, device, queue, and surface. It also configures the surface with the desired format and dimensions, preparing the context for rendering.
2. *Resource Setup*: The constructor prepares various resources such as textures for the atlas representation of VDB data, uniform buffers for rendering state, and bind groups for shader inputs. It also dynamically reads VDB files, processes the data, and updates GPU resources accordingly.

3. *Rendering*: The render method handles updating the window surface. It triggers compute shaders for voxel data processing, manages texture and buffer updates, and executes the render pipeline. Additionally, it manages shader hot-reloading, renders the developer GUI and handles screen capture for recording.

3.2.5 Graphics Pipeline

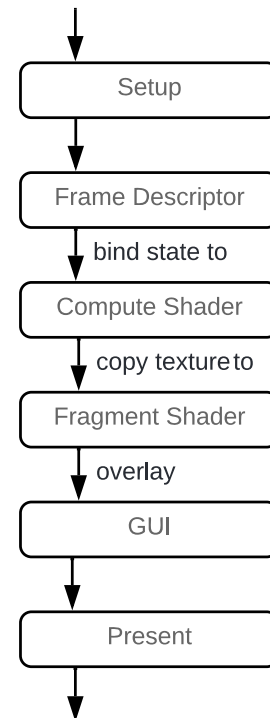
This section provides an overview of the graphics pipeline that is initiated at a `RedrawRequest` event.

When the `WgpuContext`'s render method is invoked, it starts by obtaining a reference to the output texture and creates a corresponding view. Following this, a command encoder is initialized to record GPU commands.

Next, it uses the `FrameDescriptor`, a structure designed to transform scene information (including the model, camera, and engine state), stored on the CPU, into GPU-compatible bindings. This step prepares all necessary bindings for the compute shaders, which then execute the ray-tracing algorithm across distributed workgroups, with the results written to a texture.

Once computation is complete, the texture containing the rendered image is prepared for display. This involves creating a vertex shader to generate a full-screen rectangle, onto which the texture is rasterized using fragment shaders, effectively transferring the rendered image to the output texture.

The final phase involves adding the GUI layer over the rendered scene before presenting the completed output texture on the screen.



3.2.6 GPU Types

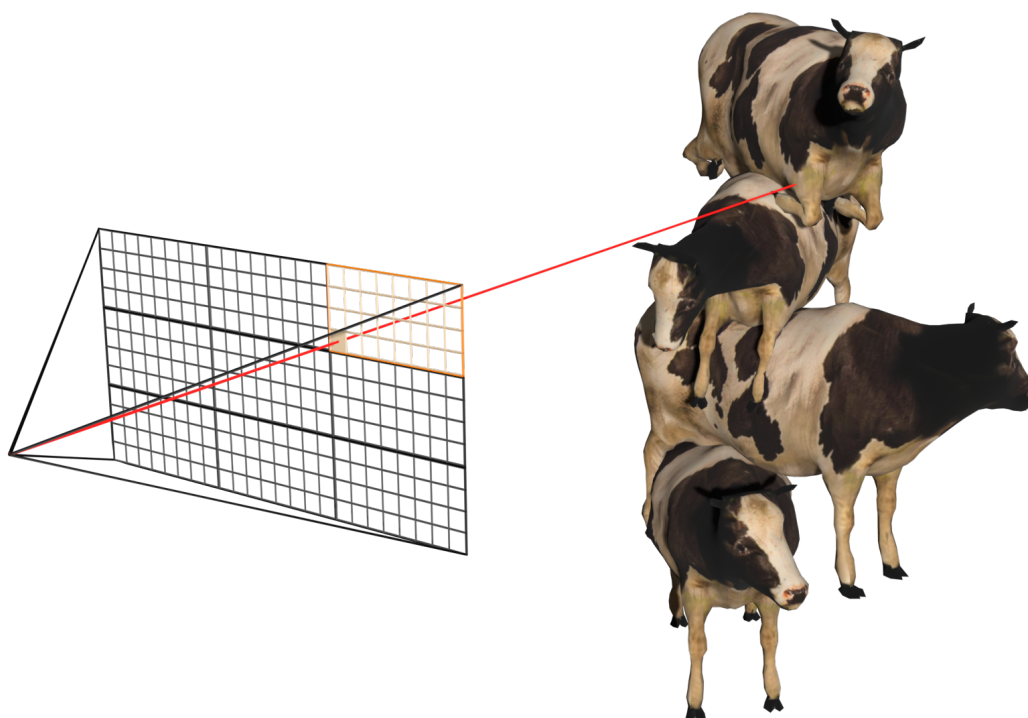
This section covers the `FrameDescriptor` data structure and how it generates GPU bindings from the data in `Scene` which is stored on the CPU.

Virtually the entire ray-tracing algorithm is run in compute shaders. This means all the information about the model, camera, lights, and metadata has to be passed through.

The statically sized data i.e. the camera, sunlight and metadata is passed in an uniform buffer. This buffer is assembled inside the `FrameDescriptor` which wraps `ComputeState`. This is a data structure that converts bla bla. Matrix Conversion: The camera's view projection matrix and the transformation from camera to world coordinates are flattened into 4x4 f32 arrays. Camera Position and Orientation: The camera's position (eye) and orientation vectors (u, -v, and w') are represented as arrays, facilitating the calculation of ray directions within the compute shader. Rendering Parameters: Additional fields such as `render_mode`, `show_345` (a flag array for toggling voxel boundary highlighting), `sun_dir`, and `sun_color` (with the alpha channel representing intensity) are included to control various aspects of the rendering process, from the mode of rendering to the simulation of lighting conditions.

3.2.7 Camera

3.2.8 Shaders



3.2.9 Utilities

3.3 VDB Implementation

References

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Acronyms

B+tree A m-ary tree with a variable but often large number of children per node.. 10

DDA Digital Differential Analyzer, line drawing algorithm described in section 2.3.3. 11, 18

FPS Frames per second. 15

HDDA Hierarchical **DDA**, line drawing algorithm described in section 2.3.3. 12

OS Operating System. 14

SDF Signed distance fields, described in section 2.3.2. 11

VDB Volumetric Dynamic B+tree grid data structure introduced by Ken Museth^[3]. 9, 15

Appendices

A Project outline

Project outline as submitted at the start of the project is a required appendix.

B Risk assessment

Risk assessment is a required appendix. Put here. And there as well