

Block Ciphers

Cryptography, Spring 2020

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Outline

Block encryption

Block cipher model and security definition

Data Encryption Standard (DES)

Rijndael and AES

Block encryption

The trouble with stream encryption

Stream encryption requires attention

- (1) Diversifier collisions are fatal and avoiding them is seen as difficult
 - taking a counter for D:
 - ▶ implies *keeping state* in between messages
 - ▶ in some architectures this is problematic
 - generating D randomly
 - generating high quality randomness is hard
 - ► there remains a risk of collisions
- (2) It does not protect integrity of the plaintext
 - · adversary can flip individual bits in ciphertext
 - ... flipping corresponding bits in plaintext
 - this is likely to go undetected by message recipient

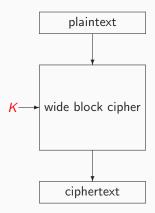
Some see the answer to these issues in different type of encryption

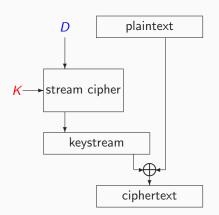
Block Encryption

Block encryption, ideally

- ► Encryption as a scrambling recipe
 - transforming the full plaintext by a sequence of operations
 - ullet (some of) these transformations depend on a secret key K
 - it must be invertible: there must be a recipe for decryption
 - ciphertext is as long as the plaintext (...or a little longer)
- ▶ Such a recipe is called a wide block cipher, considered secure if:
 - it maps similar plaintexts to seemingly unrelated ciphertexts
 - ...and vice versa
 - and this map is completely different for different keys K
- ▶ How does this address concerns of stream encryption?
 - similar plaintexts give unrelated ciphertexts, so no need for D
 - small changes in ciphertext give a completely different plaintext
- ▶ But . . .
 - some leakage remains: equal messages give equal ciphertexts
 - tamper detection isn't absolute: requires redundant plaintext
 - what about protection against replay attacks?

Block vs. stream encryption illustrated





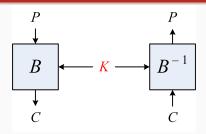
Block encryption in practice

- ▶ Problem: building a wide block cipher may be hard
 - until a few years ago in experimental stage
 - as *modes* of underlying primitives
- ▶ The established block ciphers have fixed length
 - best known: DES (8-byte plaintexts) and AES (16-byte)
 - longer plaintexts require splitting in blocks and padding
 - ...and the application of modes (see later)
- ▶ By fixing length, *advantages* of block encryption evaporate
 - unless we tolerate more leakage
 - redundancy in plaintext no longer provides integrity
- ▶ But we still will treat block ciphers in this course
 - most real world symmetric crypto still based on block ciphers
 - we'll look upon them as we do now on rotor machines

Block cipher model and security

definition

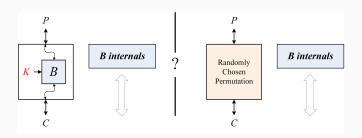
Block cipher definition



- ▶ Permutation B operating on $\{0,1\}^b$ with b the block length
 - parameterized by a secret key: B_K
 - with an inverse B_K^{-1} that should be efficient
- ▶ Computing $C = B_{\kappa}(P)$ or $P = B_{\kappa}^{-1}(C)$ should be
 - efficient knowing the secret key K
 - infeasible otherwise
- \blacktriangleright Dimensions: block length b and key length |K|

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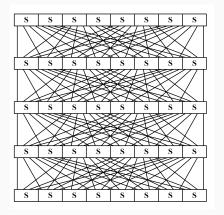
Pseudorandom Permutation (PRP) security



- ► Infeasibility to distinguish B_K from randomly chosen permutation
- ▶ Advantage as $\epsilon(M, N)$
 - Q_s to $B_K^{(-1)}$ or RCP⁽⁻¹⁾: online or data complexity M
 - ullet Q_c to B internals: offline or computational complexity N
- ▶ PRP if adversary can only make forward queries, SPRP if both forward and inverse ones
- ▶ Per default, block cipher considered secure if SPRP $Adv = N2^{-|K|}$

Data Encryption Standard (DES)

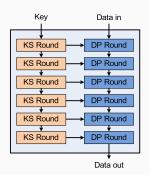
Product cipher [Claude Shannon, 1949] and SPN



Round function in data path with two (or three) layers

- ▶ non-linear substitution layer: S-boxes applied in parallel
- ▶ permutation layer: moves bits to different S-box positions
- ▶ K?: either key-dependent S-boxes or third layer of key addition

Iterative block ciphers

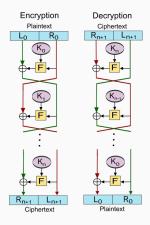


- ▶ Data path (right): transforms input data to output data
 - iteration of a non-linear round function
 - ...that depends on a round key
- Key schedule (left)
 - generates round keys from cipher key K

Data encryption standard (DES)

- ► Standard by and for US government
- ▶ By National Institute for Standardization and Technology (NIST)
- ▶ Designed by IBM in collaboration with NSA
- ▶ 1977: Federal Information Processing Standard (FIPS) 46
 - complete block cipher specification
 - block length: 64 bits, key length: 56 bits
 - no design rationale
 - freely usable
- Massively adopted by banks and industry worldwide
- Dominated symmetric crypto for more than 20 years

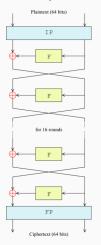
The Feistel structure



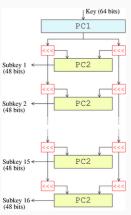
- ► State: left half *L* and right half *R*
- Alternation of involutions
 - apply F to R_i and add to L_i
 - swap left and right
- Omit swap in last round
- $ightharpoonup B^{-1}$ similar to B
 - same operation sequence
 - round keys in reversed order
- ▶ No need for F^{-1}
- ▶ Used in DES

Data encryption standard: overview

data path



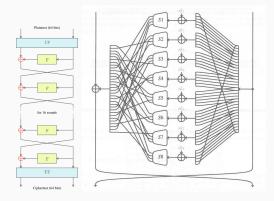
key schedule



DES algorithmic structure

- ▶ Data path
 - 16-round Feistel
 - Initial (IP) and final permutations (FP):
 - ► no cryptographic significance
 - ▶ historical, due to addressing in hardware implementation
- Key schedule
 - 8 bits thrown away in permuted choice 1 (PC1)
 - remaining 56-bit string
 - ► split in two 28-bit strings
 - rotated for each round over 1 or 2 bits
 - 48-bit round key obtained with PC2 of these 56 bits
 - each round key bit is just a cipher key bit

Data encryption standard: F-function



- ▶ Variant of SPN with 4 layers:
 - expansion E: from 32 to 48 bits
 - bitwise round key addition
 - substitution: 8 different 6-to-4 bit non-linear S-boxes
 - permutation P: moving nearby bits to remote positions
- ▶ Clearly hardware-oriented

Non-ideal DES property: Weak Keys

- ▶ What happens in the case of $K = 0^*$: the all-zero cipher key?
 - all round keys are all-zero
 - all rounds are the same
 - cipher and its inverse are the same
- ▶ Same is true for $K = 1^*$: the all-one cipher key
- And two more keys due to symmetry in key schedule
- ▶ These keys, including 0^* and 1^* are called weak keys K_w :

$$\mathsf{DES}_{K_w} \circ \mathsf{DES}_{K_w} = \mathrm{I}$$

▶ Also 6 semi-weak key pairs (K_1, K_2)

$$\mathsf{DES}_{\mathcal{K}_1} \circ \mathsf{DES}_{\mathcal{K}_2} = \mathrm{I}$$

Mostly of academic interest

Non-ideality in DES: Complementation Property

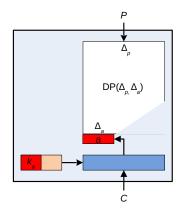
- ▶ What happens if we complement the cipher input?
 - flip all bits in key
 - flip all bits in plaintext
- ▶ In first round
 - input to F complemented so output of E complemented
 - round key also complemented so input to S-boxes unaffected
 - output of F unaffected
- Output of first round is simply complemented
- Repeat this until you reach the ciphertext
- Complementation property:

$$\mathsf{DES}_{\mathcal{K}}(P) = C \Leftrightarrow \mathsf{DES}_{\overline{\mathcal{K}}}(\overline{P}) = \overline{C}$$

▶ Reduces security strength from 56 to 55 due to speed up of exhaustive key search

Differential cryptanalysis [basic idea, more about it later]

- ► Statistical attack with following distinguisher:
 - inputs P_i and P_i^* with $P_i \oplus P_i^* = \Delta_p$
 - lead to difference Δ_a at input of last round
 - with relatively high probability $\mathsf{DP}(\Delta_p, \Delta_a)$
- ▶ Requires about $1/DP(\Delta_p, \Delta_a)$ input/output pairs
- ► Many variants exist



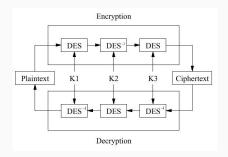
Breaking DES: differential and linear cryptanalysis (DC & LC)

- ▶ Differential cryptanalysis attack by Eli Biham and Adi Shamir, 1990
 - Requires $M \approx 2^{47}$ (1000 TeraByte) chosen plaintexts
 - Breaks DES because total complexity for the break is below 2⁵⁵
 - No real-world relevance: unrealistic amount of data required
- ▶ Linear cryptanalysis attack by Mitsuru Matsui, 1992
 - Also statistical attack, the dual of DC
 - Requires about $M \approx 2^{43}$ (64 TeraByte) known plaintexts
 - Less data than DC but still unrealistic amount for real-world attack
- Academic relevance:
 - provided first systematic design criterion for block ciphers
 - \bullet LC/DC resistance is basis of modern symmetric crypto design

The real problem of DES: the short key

- ▶ Exhaustive key search: about 3.6×10^{14} trials
- ▶ More than 21 years ago: "software" cracking
 - about 10.000 workstations, each 500.000 trials/second
 - expected time: 7.200.000 seconds: 2,5 months
 - applied in cracking RSA labs DES challenge, June '97
- Cracking using dedicated hardware
 - COPACOBANA RIVYERA (2008)
 - board with 128 Spartan-3 5000 FPGAs, costs about 10.000\$
 - finds a DES key in less than a day
- ▶ Following Moore's law, same budget would now give < 10 minutes
- Short DES key is real-world concern!

Triple DES (FIPS 46-2 and 46-3)



- ▶ Double DES allows meet-in-the-middle attacks
- ► Three variants of Triple-DES
 - 3-key: 168-bit key, only option allowed by NIST
 - 2-key: 112-bit key by taking $K_3 = K_1$
 - still massively deployed by banks worldwide
 - 1-key: 56-bit key by taking $K_3 = K_2 = K_1$

Rijndael and AES

The AES competition

- ▶ NIST launches the AES open contest to replace DES in 1997
 - 128-bit block length, 128-, 192- and 256-bit keys
 - specs, code, design rationale and preliminary analysis
 - Vincent Rijmen and I submitted RIJNDAEL
- ► First round: August 1998 to August 1999
 - 15 candidates at 1st AES conference in Ventura, California
 - analysis presented at 2nd AES conf. in Rome, March 1999
 - NIST narrowed down to 5 finalists using this analysis
- ▶ Second round: August 1999 to summer 2000
 - analysis presented at 3rd AES conf. in New York, April 2000
 - NIST selected winner using this analysis: RIJNDAEL
- NIST motivated their choice in two reports

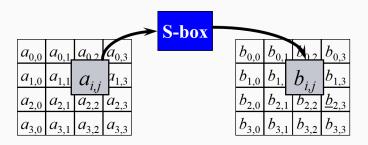
Rijndael

- ▶ Block cipher with block and key lengths \in {128, 160, 192, 224, 256}
 - set of 25 block ciphers
 - AES limits block length to 128 and key length to multiples of 64

we only treat AES in this course

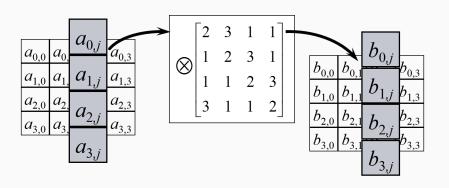
- ▶ Iteration of a round function with following properties:
 - 4 layers: nonlinear, shuffling, mixing and round key addition
 - all rounds are identical
 - ... except for the round keys
 - ...and omission of mixing layer in last round
 - parallel and symmetric
- Key schedule
 - Expansion of cipher key to round key sequence
 - Recursive procedure that can be done in-place
- ▶ Manipulates bytes rather than bits

The non-linear layer: SubBytes



- ▶ The same invertible S-box applied to all bytes of the state
- Assembled from building blocks that were proposed and analyzed in cryptographic literature
- ► Criteria:
 - to offer resistance against DC, LC and algebraic attacks
 - ... when combined with the other layers

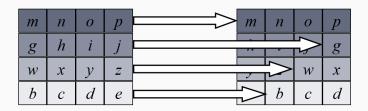
The mixing layer: MixColumns



- ▶ Same invertible mapping applied to all 4 columns
- ▶ Multiplication by a 4×4 circulant matrix [for info: in \mathbb{F}_{2^8}]
 - difference in single input byte propagates to 4 output bytes
 - difference in 2 input bytes propagates to 3 output bytes
 - difference in 3 input bytes propagates to 2 output bytes

 \Rightarrow we say: it has branch number 5

The shuffling layer: ShiftRows



- ▶ Each row is shifted by a different amount
- ▶ Different shift offsets for higher block lengths
- ▶ Moves bytes in a given column to 4 different columns
- ► Combined with MixColumns and SubBytes this gives fast diffusion

Round key addition: AddRoundKey

$a_{0,0}$	$a_{0,1}$	$a_{0,2}$	$a_{0,3}$	+	$k_{0,0}$	$k_{0,1}$	$k_{0,2}$	$k_{0,3}$	=	$b_{0,0}$	$b_{0,1}$	$b_{0,2}$	$b_{0,3}$
$a_{1,0}$	$a_{1,1}$	$a_{1,2}$	$a_{1,3}$		$k_{1,0}$	$k_{1,1}$	$k_{1,2}$	$k_{1,3}$		$b_{1,0}$	$b_{1,1}$	$b_{1,2}$	$b_{1,3}$
$a_{2,0}$	$a_{2,1}$	$a_{2,2}$	$a_{2,3}$		$k_{2,0}$	$k_{2,1}$	$k_{2,2}$	$k_{2,3}$		$b_{2,0}$	$b_{2,1}$	$b_{2,2}$	$b_{2,3}$
$a_{3,0}$	$a_{3,1}$	$a_{3,2}$	$a_{3,3}$		$k_{3,0}$	$k_{3,1}$	$k_{3,2}$	$k_{3,3}$		$b_{3,0}$	$b_{3,1}$	$b_{3,2}$	$b_{3,3}$

Round key is computed from the cipher key K

Key schedule: example with 192-bit key K

<i>k</i> ₀	<i>k</i> ₁	<i>k</i> ₂	<i>k</i> ₃	k ₄	<i>k</i> ₅	<i>k</i> ₆	k ₇	k ₈	<i>k</i> ₉	k ₁₀	k ₁₁	k ₁₂	k ₁₃	k ₁₄	k ₁₅		
Round key 0				Ro	Round key 1				Round key 2								

Expansion: put K in 1st columns and compute others recursively:

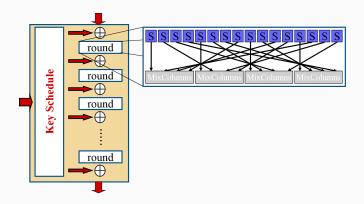
$$k_{6n} = k_{6n-6} \oplus f(k_{6n-1})$$

 $k_i = k_{i-6} \oplus k_{i-1}, i \neq 6n$

with f: 4 parallel AES S-boxes followed by 1-byte cyclic shift

▶ Selection: round key *i* is columns 4i to 4i + 3

AES: summary



- ightharpoonup 10 rounds for 128-bit key, 12 for 192-bit key and 14 for 256-bit key
- ▶ Last round has no MixColumns so that inverse is similar to cipher

AES security status anno 2020

- Cryptanalysis with respect to SPRP (in public domain)
 - no attacks of full-round version after 2 decades of intense public scrutiny
 - attacks on reduced-round versions with more than 5 rounds have huge data complexity
 - this leads to high assurance about SPRP security of AES
- ▶ Implementation attacks: exploiting physical features
 - timing attacks: cache misses in table-lookups
 - power analysis: exploiting dependence of current on data
 - electromagnetic analysis: same for EM emanations
 - fault attacks: exploiting forced faults
- ▶ Implementation attacks are the ones that matter in practice!

Summary

Summary

- ▶ Block ciphers are keyed *b*-bit permutations
 - a different permutation B_K per key K
 - with an efficient inverse B_K^{-1}
 - (S)PRP-secure if B_K is hard to distinguish from random permutation
 - exhaustive keysearch should be best method and has success probability $N2^{-|K|}$
- ▶ DES and AES are the most widespread block ciphers
 - constructed by iterating a simple round function
 - round has layers for non-linearity, mixing, shuffling and key addition