LIMITS, CONTINUITY

EE24BTECH11046 - NENAVATH VASU *

C: MCQs with One Correct Answer

2) For a real number y, let [y] denote the greatest integer less then or equal to y. Then the function $f(x) = \frac{\tan \pi [x-\pi]}{1+[x]^2}$ is

(1981 - 2 Marks)

- (a) discontinuous at some x
- (b) continuous at all x, but the derivative f'(x)does not exist for some x
- (c) f'(x) exists for all x, but the second derivative f''(x) does not exist for some x
- (d) f'(x) exists for all x
- 3) There exists a function f(x), satisfying f(0) =1, f'(0) = -1, f(x) > 0 for all x, and

(1982 - 2 Marks)

- (a) f'(x) > 0 for all x
- (b) -1 < f''(x) < 0 for all x
- (c) $-2 \le f''(x) \le -1$ for all
- (d) f''(x) < -2 for all x
- 4) If $G(x) = -\sqrt{25 x^2}$ then $\lim_{x \to 1} \frac{G(x) G(1)}{x 1}$ has the value (1983 1 Mark)
 - a) $\frac{1}{24}$ b) $\frac{1}{5}$

 - c) $\sqrt{24}$
 - d) none of these
- 5) If f(a) = 2, f'(a) = 1, g(a) = -1, g'(a)2, then the value of $\lim_{x\to a} \frac{g(x)f(a) g(a)f(x)}{x-a}$ is

(1983 - 1 Mark)

- a) -5
- b) $\frac{1}{5}$ c) 5
- d) none of these
- 6) The function $f(x) = \frac{\ln(1+ax)-\ln(1-bx)}{x}$ is not defined at x=0. The value which should be assigned to f at x=0 so that it is continuous at x=0, is

(1983 - 1 Mark)

- a) a-b
- b) a+b
- c) $\ln a \ln b$

d) none of these

7) $\lim_{n\to\infty} \left(\frac{1}{1-n^2} + \frac{2}{1-n^2} + \dots + \frac{n}{1-n^2} \right)$ is equal to (1984 - 2 Marks)

1

- b) $-\frac{1}{2}$ c) $\frac{1}{2}$ d) none of these

8) If $f(x) = \begin{cases} \frac{\sin[x]}{[x]}, [x] \neq 0 \\ = 0, [x] = 0 \end{cases}$ where [x] denotes the greatest integer less than or equal to x, then

(1985 - 2 Marks) $\lim_{x\to 0}$ equals

- a) 1
- b) 0
- c) -1
- d) none of these
- 9) Let $f: R \rightarrow R$ be a differentiable function and f(1) = 4. Then the value of $\lim_{x\to 1}$

$$\int_{4}^{f(x)} \frac{2t}{x-1} \, dt$$

(1990 - 2 Marks)

a) 8f'(1)

is

- b) 4f'(1)
- c) 2f'(1)
- d) f''(1)
- 10) Let [.] denote the greatest integer function and $f(x) = [\tan^2 x]$, then (1993 - 1 Mark)
 - a) $\lim_{x\to 0}$ does not exist
 - b) f(x) is continuous at x=0
 - c) f(x) is not differentiable at x=0
 - d) f'(0) = 1
- 11) The function $f(x) = [x] \cos(\frac{2x-1}{2})\pi$, denotes[.] denotes the greatest integer function, is discontinuous at (1995S)
 - a) All x
 - b) All integer points
 - c) No x
 - d) x which is not an integer
- 12) $\lim_{n\to\infty} \frac{1}{n} \sum_{r=1}^{2n} \frac{r}{\sqrt{n^2+r^2}}$ equals (1997 2 Marks)
 - a) $1 + \sqrt{5}$
 - b) $-1+\sqrt{5}$

- c) $-1 + \sqrt{2}$ d) $1 + \sqrt{2}$
- 13) The function $f(x) = [x]^2 [x^2]$ (where [y] is the greatest integer less than or equal to y), is discontinuous at (1992 - 2 Marks)
 - a) all integers
 - b) all integers except 0 and 1
 - c) all integers except 0
 - d) all integers except 1
- 14) The function $f(x) = (x^2 1)|x^2 3x + 2| + \cos(|x|)$ is NOT differentiable at

(1999 - 2 Marks)

- a) -1
- b) 0
- c) 1
- d) 2
- 15) $\lim_{x\to 0} \frac{x \tan(2x) 2x \tan(x)}{(1-\cos(2x))^2}$ is (1999 - 2 Marks)
 - a) 2

 - b) -2 c) $\frac{1}{2}$ d) $\frac{-1}{2}$
- 16) For $x \in \mathbb{R}$, $\lim_{x \to \infty} (\frac{x-3}{x+2})^x =$ (2000S)
 - a) *e*
 - b) e^{-1}
 - c) e^{-5}
 - d) e^5