



UNIVERSIDAD
DE GRANADA

ALGORITMICA

PRÁCTICA 2: ALGORITMOS DIVIDE Y VENCERÁS



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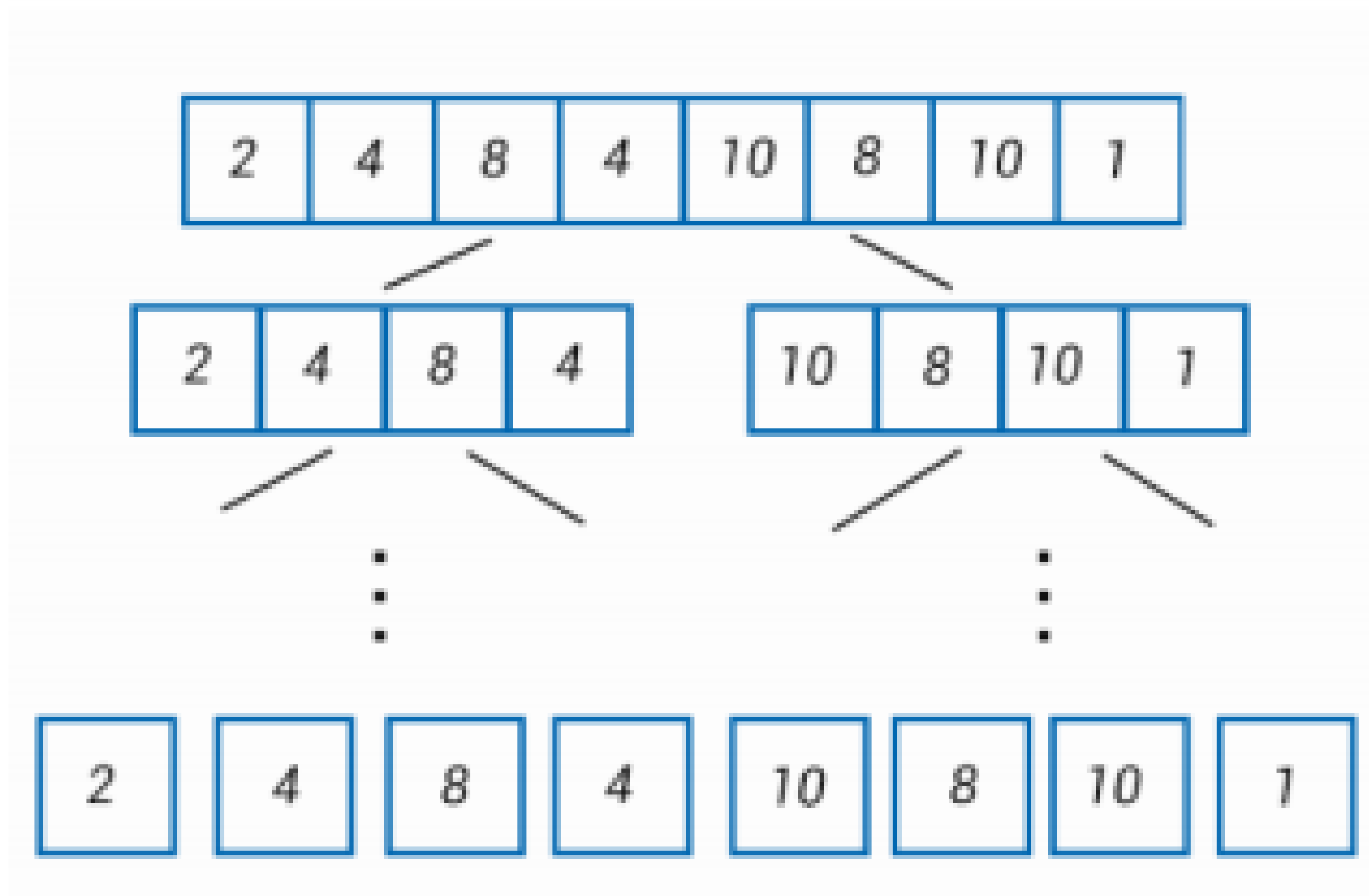
1. ALGORITMO CLASICO

```
bool yaExiste(vector<int> v, int x){  
    bool encontrado = false;  
    for(int i = 0; i < v.size() && !encontrado; i++)  
        if(v[i] == x)  
            encontrado = true;  
    return encontrado;  
}
```

```
vector<int> eliminarRepeticiones(vector<int> v){  
    vector<int> v_res;  
    for(int i = 0; i < v.size(); i++)  
        if(!yaExiste(v_res, v[i]))  
            v_res.push_back(v[i]);  
    return v_res;  
}
```

2. ALGORITMO DyV

$O(\log n)$

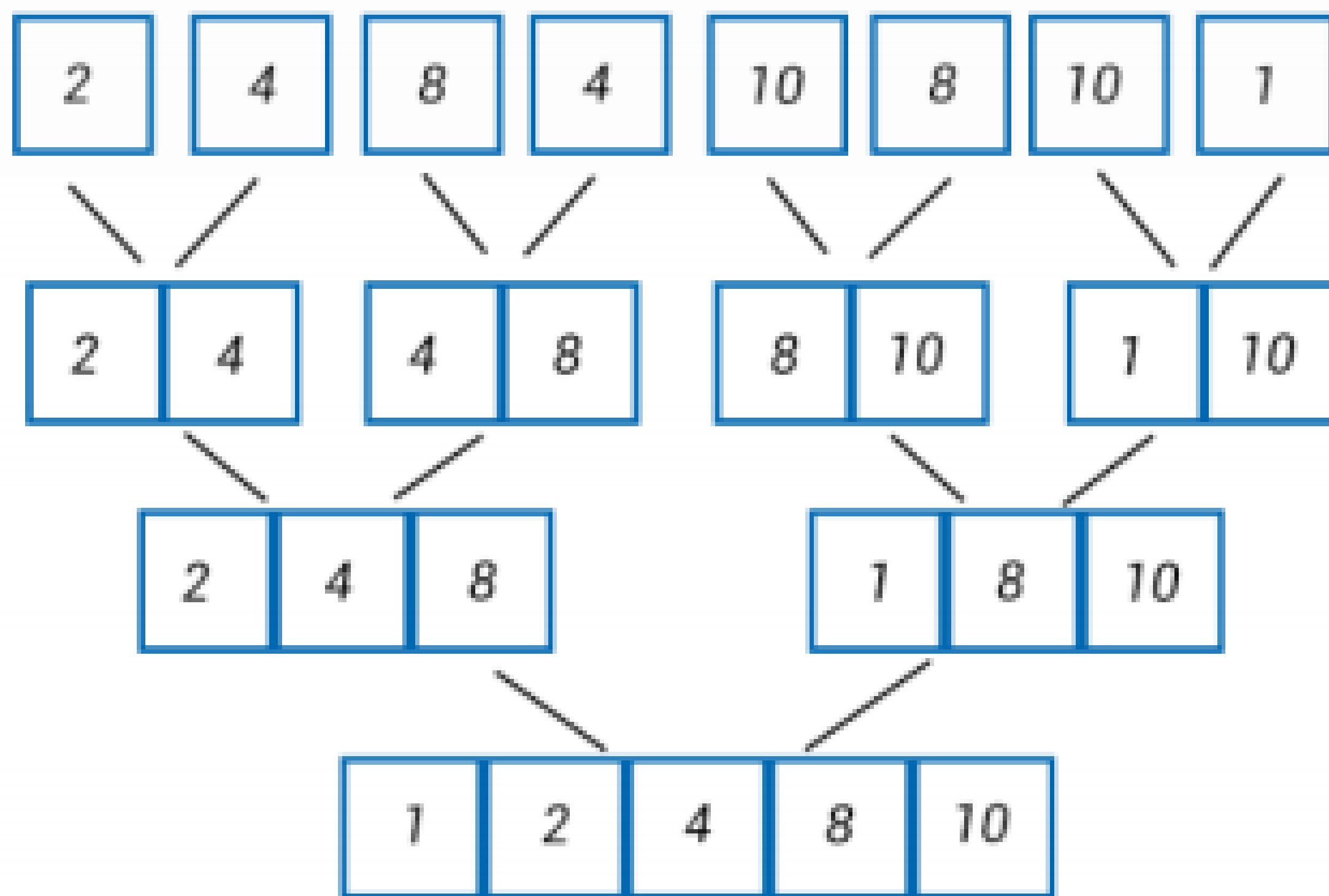


2. ALGORITMO DyV

```
vector<int> eliminarRepeticiones(vector<int> v){  
    if (v.size() != 1){  
        int m = (v.size())/2;  
        vector<int> v1;  
        vector<int> v2;  
  
        for(int i = 0; i < m; i++)  
            v1.push_back(v[i]);  
        for(int i = m; i < v.size(); i++)  
            v2.push_back(v[i]);  
  
        v1 = eliminarRepeticiones(v1);  
        v2 = eliminarRepeticiones(v2);  
  
        v = eliminar(v1, v2);  
    }  
    return v;  
}
```

2. ALGORITMO DyV

$O(n)$



2.ALGORITMO DyV

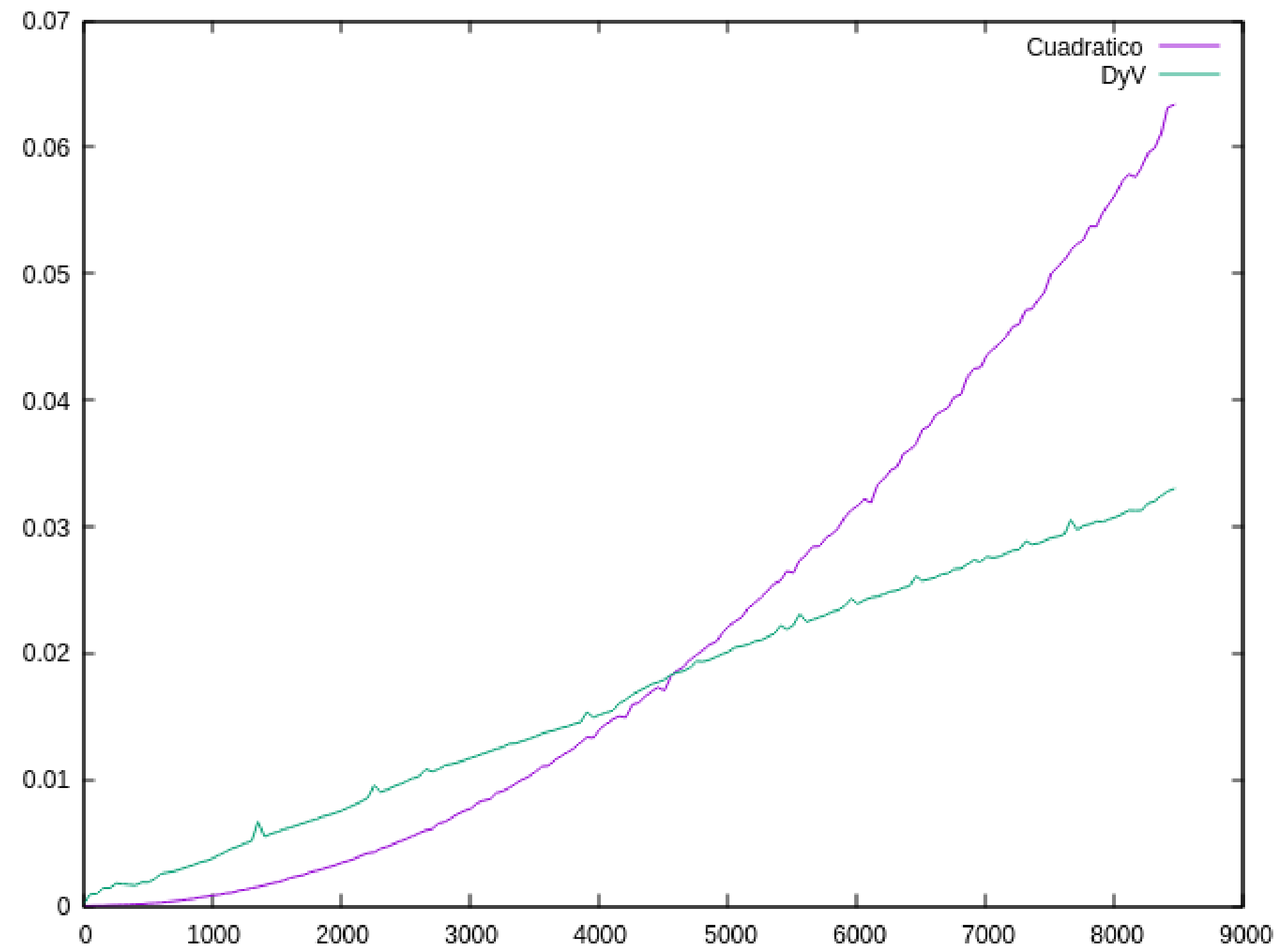
```
vector<int> eliminar(vector<int> v1, vector<int> v2){  
  
    int i = 0, j = 0;  
    int n1 = v1.size();  
    int n2 = v2.size();  
  
    vector<int> tmp;  
  
    while (i < n1 && j < n2) {  
        if (v1[i] < v2[j]){  
            tmp.push_back(v1[i]);  
            i++;  
        }  
        else if(v1[i] > v2[j]){  
            tmp.push_back(v2[j]);  
            j++;  
        }  
        else if(v1[i] == v2[j]){  
            tmp.push_back(v1[i]);  
            i++;  
            j++;  
        }  
    }  
  
    while (i < n1){  
        tmp.push_back(v1[i]);  
        i++;  
    }  
  
    while (j < n2){  
        tmp.push_back(v2[j]);  
        j++;  
    }  
  
    v1.clear();  
    v2.clear();  
    return tmp;  
}
```

Ejemplo de ejecución:

```
pablorom@pablorom-MacBookPro:~/practicasAlgoritmica/p2$ ./eliminarDyv 20  
Vector antes de eliminar duplicados  
10 7 15 7 8 8 3 6 5 11 4 17 15 9 16 15 19 18 6 11  
Componentes 20 tiempo 0.000138  
  
Vector despues de eliminar duplicados  
3 4 5 6 7 8 9 10 11 15 16 17 18 19
```


3. ESTUDIO EMPIRICO

Componentes	Tiempos (seg.)	Componentes	Tiempos (seg.)
10	8.00E-06	10	1.92E-04
60	1.50E-05	60	9.28E-04
110	2.40E-05	110	9.72E-04
160	3.90E-05	160	1.43E-03
		210	1.43E-03
910	0.000668	1010	0.003766
960	0.000737	1060	0.004018
1010	0.000828	1110	0.004295
1060	0.000898	1160	0.004549
		1210	0.00474
2010	0.003419	2110	0.007998
2060	0.003575	2160	0.008272
2110	0.003747	2210	0.008526
2160	0.004002	2260	0.008536
		2310	0.009013
3010	0.007718		
3060	0.008124	3060	0.011876
3110	0.008337	3110	0.01208
3160	0.008451	3160	0.012256
		3210	0.012421
4010	0.014003	3260	0.012594
4060	0.01438		
4110	0.014768	4010	0.015116
4160	0.014997	4060	0.015291
4210	0.014892	4110	0.015474
		4160	0.016008
5010	0.02214	4210	0.016328
5060	0.022484		
5110	0.02283	5010	0.020114
5160	0.023568	5060	0.020469
		5110	0.020546
6060	0.032193	5160	0.020686
6110	0.031904	5210	0.020949
6160	0.033283		
6210	0.033774	6010	0.023697
		6060	0.024195
7060	0.044064	6110	0.024398
7110	0.044512	6160	0.02447
7160	0.045044	6210	0.024656
7210	0.045835		
		7010	0.027643
8310	0.05992	7060	0.027541
8360	0.061036	7110	0.027662
8410	0.063139	7160	0.027883
8460	0.063363	7210	0.028122
		8260	0.03187
		8310	0.032021
		8360	0.032422
		8410	0.032794



n^2 $n \log n$

4. ESTUDIO HIBRIDO

Algoritmo cuadrático

function used for fitting: $f(x) = a_0x^2 + a_1x + a_2$

After 11 iterations the fit converged.

final sum of squares of residuals : $9.82641e-06$

rel. change during last iteration : $-4.25933e-11$

Final set of parameters

Asymptotic Standard Error

=====

$a_0 = 8.86647e-10$

=====

$\pm 3.455e-12$ (0.3897%)

$a_1 = -5.3324e-08$

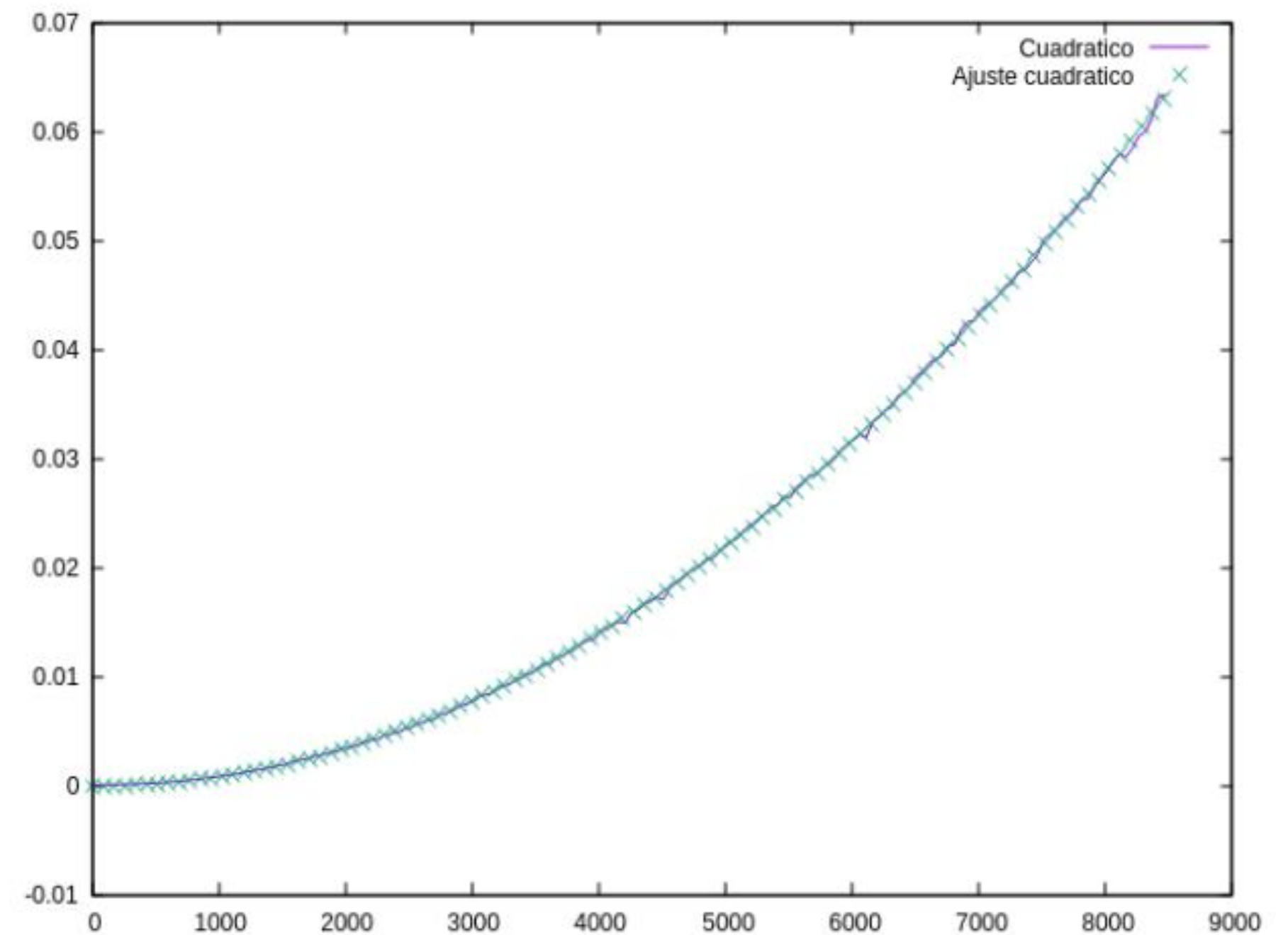
$\pm 3.023e-08$ (56.69%)

$a_2 = -5.00882e-05$

$\pm 5.542e-05$ (110.7%)

correlation matrix of the fit parameters:

	a_0	a_1	a_2
a_0	1.000		
a_1	-0.968	1.000	
a_2	0.743	-0.864	1.000



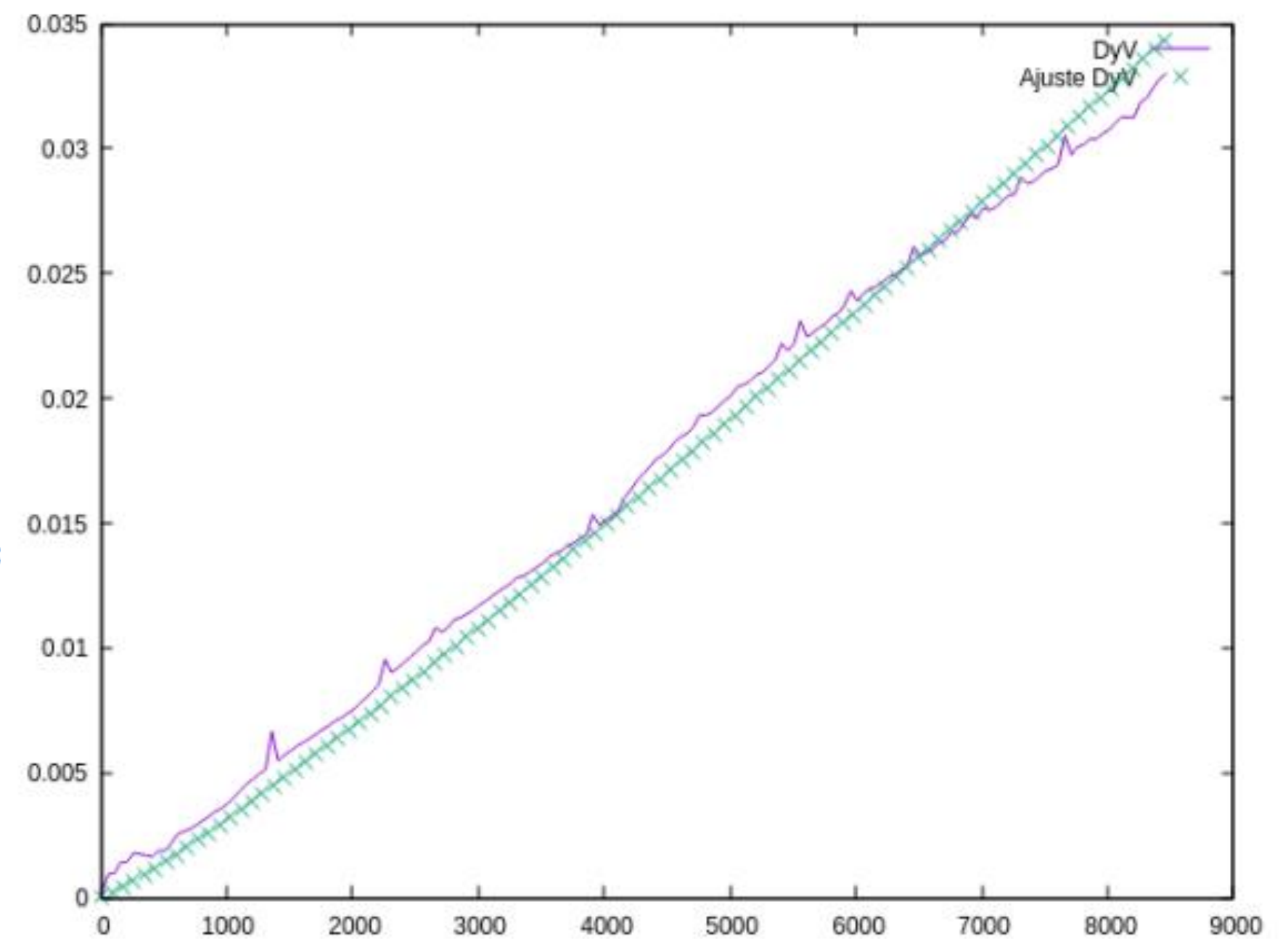
4. ESTUDIO HIBRIDO

Algoritmo DyV

function used for fitting: $f(x) = a_0 \cdot x \cdot \log(x)$
fitted parameters initialized with current variable values

After 3 iterations the fit converged.
final sum of squares of residuals : 0.000134044
rel. change during last iteration : -5.4938e-11

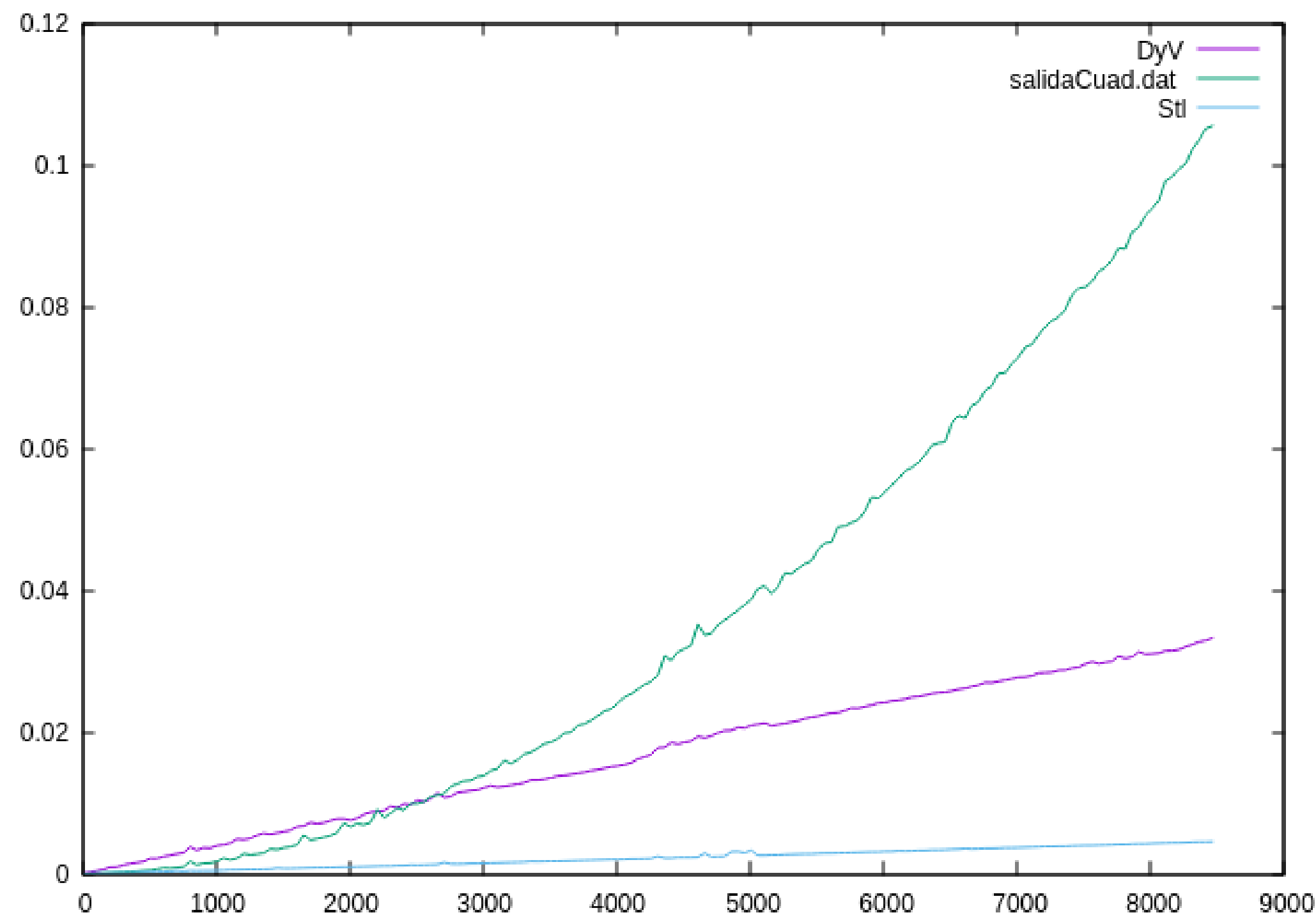
Final set of parameters	Asymptotic Standard Error
=====	=====
a0 = 4.49249e-07	+/- 1.601e-09 (0.3563%)



5. ANEXO: Uso de la stl

Algoritmo stl

```
for(vector<int>::iterator it = v.begin(); it != v.end(); it++)  
    tmp.insert(*it);  
for(set<int>::iterator it = tmp.begin(); it != tmp.end(); it++)  
    v2.push_back(*it);
```



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