

relative frequency of category $i = \frac{\text{frequency of category } i}{n}$

relative frequency = $\frac{\text{frequency of each group}}{\text{total number of observations}}$

Mean: population of size $N: \mu = \frac{\sum_{i=1}^N x_i}{N}$ sample of size $n: \bar{x} = \frac{\sum_{i=1}^n x_i}{n}$

Variance: population: $\sigma^2 = \frac{\sum_{i=1}^N (x_i - \mu)^2}{N}$ sample: $s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$

Standard deviation: $SD = \sqrt{\text{variance}}$

Process capability index: $C_p = \frac{\text{upper specification} - \text{lower specification}}{\text{total variation}}$

Standard value: Z-Score for i^{th} observation: $Z_i = \frac{x_i - \bar{x}}{s}$

Coefficient of variation: $CV = \frac{\text{standard deviation}}{\text{mean}}$

Coefficient of skewness: $CS = \frac{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^3}{\sigma^3}$

Coefficient of kurtosis: $CK = \frac{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^4}{\sigma^4}$

Covariance: population: $\text{cov}(x, y) = \frac{\sum_{i=1}^N (x_i - \mu_x)(y_i - \mu_y)}{N}$, sample: $\text{cov}(x, y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n}$

Correlation: population: $P_{xy} = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$ sample: $r_{xy} = \frac{\text{cov}(x, y)}{s_x s_y}$

Standard Error of the mean = $\frac{\sigma}{\sqrt{n}}$

Confidence interval for mean with known population SD: $\bar{x} \pm Z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}} \right)$

Confidence interval for mean with unknown population SD: $\bar{x} \pm t_{\alpha/2, n-1} \left(\frac{s}{\sqrt{n}} \right)$

Confidence interval for proportion: $\hat{p} \pm Z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

Prediction interval: $\bar{x} \pm t_{\alpha/2, n-1} \left(s \sqrt{1 + \frac{1}{n}} \right)$

Sample size for mean: $n \geq \left(Z_{\alpha/2} \right)^2 \frac{\sigma^2}{E^2}$ ($E = \text{margin of error}$)

Sample size of proportion: $n \geq \left(Z_{\alpha/2} \right)^2 \frac{\pi(1-\pi)}{E^2}$ ($E = \text{sampling error}$, $\pi = \text{proportion}$)

One sample t-test for mean, σ known: $Z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$

One sample t-test for mean, σ unknown: $Z = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$

One sample t-test on a proportion: $Z = \frac{\hat{p} - \pi_0}{\sqrt{\pi_0(1-\pi_0)/n}}$

Smoothing window $_t = \frac{1}{k} (Y_t + Y_{t-1} + \dots + Y_{t-(k-1)})$

Exponential smoothing model: $\hat{Y}_{t+1} = \alpha Y_t + (1-\alpha) \hat{Y}_t$

$$= \alpha Y_t + (1-\alpha) (\alpha Y_{t-1} + (1-\alpha) \hat{Y}_{t-1})$$

$$= \alpha (Y_t + (1-\alpha) Y_{t-1} + (1-\alpha)^2 Y_{t-2} + \dots)$$

Root mean square error: $RMSE = \sqrt{\frac{1}{n} \sum_i (y_i - \hat{y}_i)^2}$

$$= \text{sqrt}(\text{mean}(\text{residuals}(\text{fit})^2))$$

Classification accuracy = $\frac{\text{True Positive} + \text{True Negative}}{\text{TP} + \text{TN} + \text{FP} + \text{FN}}$

Recall = $\frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}}$

Precision = $\frac{\text{True Positive}}{\text{True Positive} + \text{False Positive}}$

F1 score = $\frac{2 \times \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$