# **Problem Set 1 Exercise #16: Triangle Incenter**

Reference: Lecture 2 notes

Learning objective: Writing methods; Math class method

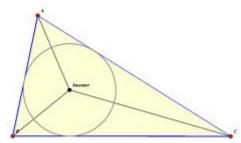
**Estimated completion time**: 30 minutes

#### **Problem statement:**

In geometry, the incircle (or inscribed circle) of a triangle is the largest circle contained in the triangle; it touches (is tangent to) the three sides. The center of the incircle is called the triangle's incenter.

Write a program **PS1\_Ex16\_TriangleIncenter.java** to read in the coordinates (of type **double**) of 3 vertices of a triangle and compute the coordinates of its incenter.

Your program should contain a method **computeLength()** that returns the length of a side of triangle given its two vertices.



### **Useful tips:**

The Cartesian coordinates of the incenter are a weighted average of the coordinates of the three vertices using the side lengths of the triangle as weights. If the three vertices are located at  $(\mathbf{x}_a, \mathbf{y}_a)$ ,  $(\mathbf{x}_b, \mathbf{y}_b)$ , and  $(\mathbf{x}_c, \mathbf{y}_c)$ , and the sides opposites these vertices have corresponding lengths  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , then the incenter is at

$$\left(\frac{ax_a+bx_b+cx_c}{p},\frac{ay_a+by_b+cy_c}{p}\right)$$

where p = a + b + c.

An incenter calculator is available on this website:

http://www.had2know.com/academics/centroid-circumcenter-orthocenter-incenter-triangle.html

Search online for more information if needed.

#### Sample run #1:

```
Coordinates of 1st vertex: -1 0
Coordinates of 2nd vertex: 3 0
Coordinates of 3rd vertex: 1 5
Coordinates of incenter = (1.00, 1.35)
```

## Sample run #2:

```
Coordinates of 1st vertex: 63.2 21.8
Coordinates of 2nd vertex: -15 -6
Coordinates of 3rd vertex: -19.2 5.7
Coordinates of incenter = (-11.52, 1.34)
```