CS2030 Lecture 10

Functional Programming Concepts

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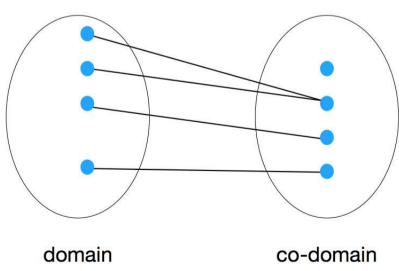
Lecture Outline and Learning Outcomes

- Understand the concepts of referential transparency and no-side-effects in pure functions
- Know how to perform function composition
- Appreciate how currying supports partial evaluation
- Understand how side effects can be handled within contexts represented as functors or monads
- Awareness of the laws of functors and monads
- Appreciate that object-oriented programming and functional programming are complementary techniques

Function

- \square A function is a mapping from a set of inputs X (domain) to a set of outputs Y (co-domain), $f:X\to Y$.
 - Every input in the domain maps to exactly one output
 - Multiple inputs can map to the same output
 - Not all values in the co-domain are mapped





Pure Function

- □ A *pure function* is a function that
 - takes in arguments and returns a deterministic value
 - has no other side effects
- □ Examples of side effects:
 - Modifying external state
 - Program input and output
 - Throwing exceptions
- The absence of side-effects is a necessary condition for referential transparency
 - any expression can be replaced by its resulting value, without changing the property of the program

Pure Function

□ Exercise:

– Are the following functions pure?

```
pure, as only making use of x and y,
int p(int x, int y) {
                                  it is not making use of some outside state
      return x + y;
int q(int x, int y) {
                                     not pure, when y = 0,
                                     there is an exception
      return x / y;
void r(List<Integer> queue, int i) {
     queue.add(i);
                                             not pure, as queue is an outside state that we take in,
                                             once we do a queue.add(), we change it
int s(int i) {
                                      depends on this.x is private final
      return this.x + i;
                                      when constant value: pure
```

Higher Order Functions

- Functions are first-class citizens
 - Higher-order functions can take in other functions

```
jshell> Function<Integer,Integer> f = x -> x + 1
f ==> $Lambda$16/0x000000008000b7840@5e3a8624
ishell> Function<Integer,Integer> q = x \rightarrow Math.abs(x) * 10
q = > $Lambda$17/0x000000008000b7c40@604ed9f0
jshell> f.apply(2)
$.. ==> 3
ishell> int sumList(List<Integer> list, Function<Integer,Integer> f) {
   \dots > int sum = 0:
   ...> for (Integer item : list) { sum += f.apply(item); }
   ...> return sum; }
   created method sumList(List<Integer>,Function<Integer,Integer>)
jshell> sumList(List.of(1, -2, 3), f)
$.. ==> 5
jshell> sumList(List.of(1, -2, 3), g)
$.. ==> 60
```

Function Composition

```
Function composition: (g \circ f)(x) = g(f(x))
 jshell> Function<String, Integer> f = str -> str.length()
 f ==> $Lambda$14/731395981@475530b9
 jshell> Function<Integer, Circle> g = x -> new Circle(x)
 g ==> $Lambda$15/650023597@4c70fda8
Function<T,R> has a default andThen method:
 default <V> Function<T,V> andThen(
          Function<? super R, ? extends V> after)
 jshell> f.andThen(g).apply("abc")
 $.. ==> Circle with radius: 3.0
 Function<T,R> has an alternative default compose method:
 default <V> Function<V,R> compose(
          Function<? super V, ? extends T> before)
 jshell> g.compose(f).apply("abc")
 $.. ==> Circle with radius: 3.0
```

Function With Multiple Arguments

Consider the following: jshell> BinaryOperator<Integer> f = (x,y) -> x + yf ==> \$Lambda\$14/1268650975@2b98378d jshell> f.apply(1, 2) \$.. ==> 3 We can achieve the same with just Function<T,R> jshell> Function<Integer, Function<Integer,Integer>> f = new Function<>() { @Override ...> public Function<Integer,Integer> apply(Integer x) { ...> return new Function<Integer, Integer>() { @Override ...> public Integer apply(Integer y) { ...> $return \times + y;$...> ...> **}**; ...> ...> ...> } f ==> 1@2b98378d jshell> f.apply(1).apply(2) \$.. ==> 3

Currying

- The lambda expression (x, y) -> x + y can be re-expressed
 as x -> (y -> x + y) or simply, x -> y -> x + y
 jshell> Function<Integer, Function<Integer,Integer>> f = x -> y -> x + y
 f ==> \$Lambda\$14/486898233@26be92ad
 jshell> f.apply(1).apply(2)
 \$.. ==> 3
- This is known as currying, and it gives us a way to handle lambdas of an arbitrary number of arguments
- Currying supports partial evaluation

\$.. ==> 11

E.g. partially evaluating f for increment: jshell> Function<Integer,Integer> inc = f.apply(1) inc ==> \$Lambda\$15/575593575@46d56d67 jshell> inc.apply(10)

Pure Functions.. or Pure Fantasy?

- □ Side-effects are a necessary evil
- Handle side-effects within a context, e.g.
 - Maybe/Optional handles the context of missing values
 - ImList handles the context of list processing
 - Stream handles the context of loops (and parallel) processing
 - etc.
- Values wrapped within contexts can be represented by Functors (with map) or Monads (with flatMap)
- In the following slides, assume Functor<T> and Monad<T> are generic interfaces with specific methods to be implemented

Everything you can do outside the context, you can do inside inside the context

- Functor has a method:
 - <R> Functor<R> map(Function<T,R> f)

$$\boxed{c} \xrightarrow{x \to f(x)} \boxed{f(c)}$$

- A functor must obey the two functor laws:
 - **Identity**: if mapping over an identity function $x \to x$, then resulting functor should be unchanged:

functor mapped with an identity = functor functor.map(x -> x) \equiv functor $\boxed{c} \xrightarrow{x \to x} \boxed{c}$

$$\boxed{\mathsf{c}} \xrightarrow{x \to x} \boxed{\mathsf{c}}$$

Associative: if mapping over $g \circ h$, then the resulting functor should be the same as mapping over h then q $functor.map(h.andThen(g)) \equiv functor.map(h).map(g)$

 $functor.map(g.compose(h)) \equiv functor.map(h).map(g)$

$$\boxed{\mathtt{c}} \stackrel{g \circ h}{\Longrightarrow} \boxed{\mathtt{g}(\mathtt{h}(\mathtt{c}))} \equiv \boxed{\mathtt{c}} \stackrel{h}{\Longrightarrow} \boxed{\mathtt{h}(\mathtt{c})} \stackrel{g}{\Longrightarrow} \boxed{\mathtt{g}(\mathtt{h}(\mathtt{c}))}$$

Functor

Doptional is a functor with map

```
jshell> Optional<String> opt1 = Optional.of("abc")
opt1 ==> Optional[abc]
ishell> Optional<String> opt0 = Optional.empty()
opt0 ==> Optional.empty
ishell > opt1.map(x -> x).equals(opt1) // identity
$3 ==> true
ishell > opt0.map(x -> x).equals(opt0) // identity
$4 ==> true
ishell> Function<String, Integer> h = x -> x.length()
h ==> $Lambda$16/1282473384@224edc67
ishell> Function<Integer,Integer> q = x -> x * 10
g ==> $Lambda$17/1188392295@d8355a8
jshell> opt1.map(g.compose(h)).equals(opt1.map(h).map(g)) // associative
$.. ==> true
jshell> opt0.map(g.compose(h)).equals(opt0.map(h).map(g)) // associative
$.. ==> true
```

- Monad with the following methods:
 - Monad<T> of (T value), that creates the Monad
 - <R> Monad<R> flatMap(Function<T, Monad<R>> f)

$$\begin{array}{c}
x \to f(x) \\
\hline
f(c)
\end{array}$$

- ☐ Just like functor laws, there are monad laws.
- In the following slide, suppose
 - Monad.of(x) gives |x|, i.e. wraps x within a context
 - monad is a constant represented by c, i.e. some fixed value wrapped within a context

Monad

 \Box **Right identity**: monad.flatMap(x -> Monad.of(x)) \equiv monad

 \Box **Left identity**: Monad.of(x).flatMap(f) \equiv f.apply(x)

$$\boxed{\mathbf{x}} \xrightarrow{x \to \boxed{\mathbf{f}(\mathbf{x})}} \boxed{\mathbf{f}(\mathbf{x})} \equiv x \to \boxed{\mathbf{f}(\mathbf{x})}$$

Associative

 $monad.flatMap(h).flatMap(g) \equiv monad.flatMap(x -> h.apply(x).flatMap(g))$

Note the composition $g \circ h$ is expressed as x -> h.apply(x).flatMap(g)

Monad

Optional is also a Monad

```
jshell> Function<String,Optional<Integer>> f = x -> Optional.of(x.length())
f ==> $Lambda$19/1529306539@61832929
jshell> Optional.of("abc").flatMap(f).equals(f.apply("abc")) // left identity
$.. ==> true
jshell> Function<String,Optional<Integer>> e = x -> Optional.empty()
e ==> $Lambda$20/1582797472@26653222
jshell> Optional.of("abc").flatMap(e).equals(e.apply("abc")) // left identity
$.. ==> true
jshell> Optional<String> opt = Optional.of("monad")
opt ==> Optional[monad]
ishell > opt.flatMap(x -> Optional.of(x)).equals(opt) // right identity
$.. ==> true
ishell> opt = Optional.empty()
opt ==> Optional.empty
ishell > opt.flatMap(x -> Optional.of(x)).equals(opt) // right identity
$.. ==> true
```

OOP and FP Are Complementary

□ continued...

OO makes code understandable by encapsulating moving parts. FP makes code understandable by minimizing moving parts.

— Michael Feathers