NATIONAL UNIVERSITY OF SINGAPORE

CS2100 – COMPUTER ORGANISATION (Semester 2: AY2014/15)

Time Allowed: 2 Hours

INSTRUCTIONS TO CANDIDATES

- 1. This examination paper consists of ELEVEN (11) questions and comprises ELEVEN (11) printed pages.
- 2. This is a CLOSED BOOK examination. Two handwritten A4 reference sheets are allowed. Calculators are not allowed.
- 3. Answer all questions and write your answers in the $\ensuremath{\mathsf{ANSWER}}$ BOOKLET provided.
- 4. Fill in your Matriculation Number with a <u>pen</u>, <u>clearly</u> on odd-numbered pages of your ANSWER BOOKLET.
- 5. You may use pencil to write your answers.
- 6. The last three pages are for your rough work. They contain blank truth tables, K-maps, state table and timing charts for your use.
- 7. You are to submit only the ANSWER BOOKLET and no other document.

Questions 1 – 6: Each question has only one correct answer. Write your answers in the boxes provided in the Answer Booklet. One mark is awarded for a correct answer and no penalty for wrong answer.

 ${\bf 1.}\quad {\bf To~which~of~the~following~Boolean~expressions~is~the~Consensus~Theorem~applicable?}$

i.
$$(f+g)\cdot h + h\cdot k + (f+g)\cdot k$$

ii.
$$W' \cdot X' \cdot Y' + W' \cdot X' \cdot Y + W \cdot X \cdot Y$$

iii.
$$a \cdot b \cdot c \cdot d + a \cdot b \cdot c' \cdot e + b \cdot d \cdot e$$

iv.
$$P \cdot Q \cdot R \cdot S + P \cdot R \cdot S \cdot T + Q' \cdot R \cdot S \cdot T$$

- A. Only (i) and (iv)
- B. Only (iii) and (iv)
- C. Only (i), (ii) and (iii)
- D. Only (i), (iii) and (iv)
- E. Only (ii), (iii) and (iv)
- 2. Given a Boolean function $F(A,B,C) = \Sigma m(2, 4, 5, 7)$, how would you implement the function using a 4:1 multiplexer shown on the right, with the selector lines S_1 = A and S_0 = C?



- A. Input 0 = C; Input 1 = 0; Input 2 = C'; Input 3 = 1
- B. Input 0 = B; Input 1 = 0; Input 2 = B'; Input 3 = 1
- C. Input 0 = 0; Input 1 = B'; Input 2 = 1; Input 3 = B
- D. Input 0 = B; Input 1 = B; Input 2 = B'; Input 3 = B
- E. None of the above.
- 3. Which of the following Boolean expressions can be implemented using a single 2×4 decoder with 1-enable and active-high outputs, without any additional logic gates? Complemented literals are not available.
 - i. A·B'·C
 - ii. $X' \cdot Y \cdot Z'$
 - iii. P·Q'
 - A. Only (i)
 - B. Only (iii)
 - C. Only (i) and (ii)
 - D. Only (i) and (iii)
 - E. All of (i), (ii) and (iii)

- 4. If a program P executes on a machine M, which of the following sets of information allows us to calculate the execution time correctly?
 - i. From P: number of instructions; From M: Clock Frequency
 - ii. From P: number of instructions; From M: Clock Frequency and CPI
 - iii. From P: number of instructions and average CPI; From M: Clock Period
 - A. Only (i)
 - B. Only (iii)
 - C. Only (i) and (ii)
 - D. Only (i) and (iii)
 - E. All of (i), (ii) and (iii)
- 5. Given a program P, if we know there are 30% of the instructions are of type A and 30% of the instructions are of type B, which of the following statements is/are true?
 - Speeding up execution time for type-A instructions by 2x has the same impact on the overall execution time as speeding up type-B instructions by 2x.
 - ii. There are same number of instructions of type A and type B in program P.
 - iii. If we improve the execution time for both type-A and type-B instructions by 2x, the overall execution time will be (0.6/2+0.4) x original execution time.
 - A. Only (i)
 - B. Only (ii)
 - C. Only (ii) and (iii)
 - D. All of (i), (ii) and (iii)
 - E. None of the above.
- 6. Suppose register s0 contains a random 32-bit value. Which of the following MIPS statements can copy the content of s0 into s1?
 - i. xor \$s1, \$s0, \$0
 - ii. sll \$s1, \$s0, 1
 - srl \$s1, \$s1, 1
 - iii. andi \$s1, \$s0, 0xFFFF
 - A. Only (i)
 - B. Only (i) and (ii)
 - C. Only (ii) and (iii)
 - D All of (i) (ii) and (iii)
 - E. None of the above.

7. [10 marks]

A sequential circuit cycles through the following states, whose state values are shown in decimal:

0 1 3 2 6 back to 0

- a. The states are represented by 3-bit values ABC. Implement the sequential circuit using a JK flip-flop for A, a T flip-flop for B, and a D flip-flop for C. Write out the simplified SOP expressions for all the flip-flop inputs. Note that the simplified expression for KA has been done for you (KA = 1). You do not need to draw the logic diagram. [6 marks]
- b. Complete the given state diagram on the answer booklet, by indicating the next state for each of the three unused states. [3 marks]
- c. Which states are sinks and why?

[1 mark]

8. [7 marks]

a. Given the following Boolean function:

$$F(A,B,C,D) = \Sigma m(0, 5, 10, 15)$$

You are to implement F using the smallest magnitude comparator and only one of it, without any other devices or additional logic gates. Note that complemented literals are not available. Label your diagram completely. [4 marks]

b.	You are given a 4-bit adder-cum-subtractor whose block diagram is shown on the right. $X = X_3 X_2 X_1 X_0 \ \text{and} \ Y = Y_3 Y_2 Y_1 Y_0 \ \text{are unsigned binary values.}$ The input S is a control signal. If S=0, it performs addition and the output is X + Y. If S=1,	S X ₈ X ₂ X ₁	4-bit //adder cum subtr	
	it performs subtraction and the output is X – Y. You are to design a circuit to convert a 4-bit 2's complement value ABCD into its equivalent 4-bit 1's complement value PQRS. For example, if ABCD=1011 (representing -5 in decimal), then PQRS must be 1010 (representing -5 in decimal).	X_0 X_0 Y_3 Y_2 Y_1 Y_0	S ₃ S ₂ S ₁ S ₀	

You may assume that the input ABCD=1000 will never happen since that represents -8 in decimal which is not possible to be represented in 4-bit 1's complement.

Implement the converter circuit by using the 4-bit adder-cum-subtractor and only one of it, without any other devices or additional logic gates. Note that complemented literals are not available. [3 marks]

9. [8 marks]
Study the following MIPS program:

```
#register $s0 contains a 32-bit value
   #register $s1 contains a non-zero 8-bit value
       at the right most (least significant) byte
      add $t0, $s0, $zero
                               #inst A
      add $s2, $zero, $zero #inst B
lp: bne $s2, $zero, done #inst C
      beq $t0, $zero, done #inst D
                           #inst E
      andi $t1, $t0, 0xFF
      bne $s1, $t1, nt
                          #inst F
      addi $s2, $s2, 1
                          #inst G
                      #inst H
nt: srl $t0, $t0, 8
j lp
                      #inst J
```

- a. Translate instructions C and D into a single C-like high-level program statement.
 Remember to indicate whether this is an IF-THEN-ELSE or a WHILE statement. Use the register names as variable names.
 [2 marks]
- b. If instruction J "j lp" is at memory address 0xBEBEC0C0, give the instruction encoding in hexadecimal. Opcode for jump is 0x02. [2 marks]
- c. Give the final result (i.e. when the code terminates at "done:") of register \$s2 if register \$s0 contains 0xAFAFFAFA and \$s1 contains 0xFF. [1 mark]
- d. Give the final result (i.e. when the code terminates at "done:") of register \$s0 if register \$s0 contains 0xBABABABA and \$s1 contains 0xBA. [1 mark]
- e. Explain the purpose of the code in a single sentence.

10. [7 marks]

This question uses the same MIPS code in Question 9, duplicated below for your reference:

```
#register $s0 contains a 32-bit value
   #register $s1 contains a non-zero 8-bit value
        at the right most (least significant) byte
      add $t0, $s0, $zero
                                #inst A
      add $s2, $zero, $zero #inst B
lp: bne $s2, $zero, done #inst C
      beq $t0, $zero, done #inst D
      andi $t1, $t0, 0xFF
                           #inst E
                           #inst F
      bne $s1, $t1, nt
      addi $s2, $s2, 1
                           #inst G
                      #inst H
nt: srl $t0, $t0, 8
      j lp
                      #inst J
done:
```

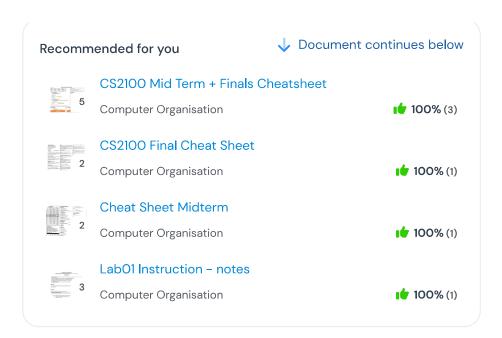
We assume that the register \$s0 contains 0xAFAFFAFA and \$s1 contains 0xFF. (i.e. as in Q9, part (c)).

Given a 5-stage MIPS pipeline processor, for each of the parts below, give the total number of cycles needed for the 1st iteration of the execution from instructions A to H (i.e. excluding the "j lp"). Remember to include the cycles needed for instruction H to finish the WB stage. Note that the questions are independent from each other.

a. With only data forwarding mechanisms and no control hazard mechanism.

[2 marks]

- b. With data forwarding and "assume not taken" branch prediction. Note that there is no early branching. [3 marks]
- By swapping two instructions (from Instructions A to H), we can improve the
 performance of early branching (with all additional forwarding paths). Give the
 two instructions that can be swapped. You only need to indicate the instruction
 letters in your answer.



11. [12 marks]

There are two major categories of memory accesses initiated by a processor:

- a. Instruction memory access: Fetch an instruction by instruction address.
- b. Data memory access: Read/Write a data value from/to memory.

We can analyze the cache performance by looking at the sequence of memory addresses generated during program execution. Below is the sequence of memory addresses generated by four iterations of the same loop.

1st Iteration		2 nd Iteration		3 rd Ite	ration	4 th Iteration		
Inst.	Data	Inst.	Data	Inst.	Data	Inst.	Data	
0xEBD8		0xEBD8		0xEBD8		0xEBD8		
0xEBDC		0xEBDC		0xEBDC		0xEBDC		
0xEBE0	0xAA18	0xEBE0	0xAA58	0xEBE0	0xAA28	0xEBE0	0xAA68	
0xEBE4		0xEBE4		0xEBE4		0xEBE4		
0xFA10	0xBB94	0xFA10	0xBBA4	0xFA10	0xBBA4	0xFA10	0xBBB4	
0xFA14		0xFA14		0xFA14		0xFA14		
0xEBE0	0xAA1C	0xEBE0	0xAA5C	0xEBE0	0xAA2C	0xEBE0	0xAA6C	
0xEBE4		0xEBE4		0xEBE4		0xEBE4		

Note: The upper 16-bit for instruction addresses is 0xABCD. The upper 16-bit for data addresses is 0x0000. This table is also available on the last page if you need more space to work out the answers.

You can see that the instruction addresses are mostly sequential (first instruction of the loop at 0xABCD EBD8, then second instruction at 0xABCD EBDC, etc.) with a "jump" in the middle. Data addresses are generated only by memory instructions, e.g. the instruction 0xABCD EBE0 is likely to be memory load/store instruction which accesses memory location at 0x0000 AA18.

Given a 64 bytes direct mapping instruction cache with 16 bytes block, answer the following:

- a) Give the index and offset for the first instruction access $0xABCD\ EBD8$ in binary. [1 mark]
- b) For the first iteration of loop only, what is the total number of cache misses for the instruction address sequence? [2 marks]

1 st Iteration		ation	2 nd Iteration		3 rd Ite	ration	4 th Iteration		
	Inst.	Data	Inst.	Data	Inst.	Data	Inst.	Data	
	0xEBD8		0xEBD8		0xEBD8		0xEBD8		
	0xEBDC		0xEBDC		0xEBDC		0xEBDC		
	0xEBE0	0xAA18	0xEBE0	0xAA58	0xEBE0	0xAA28	0xEBE0	0xAA68	
	0xEBE4		0xEBE4		0xEBE4		0xEBE4		
	0xFA10	0xBB94	0xFA10	0xBBA4	0xFA10	0xBBA4	0xFA10	0xBBB4	
	0xFA14		0xFA14		0xFA14		0xFA14		
	0xEBE0	0xAA1C	0xEBE0	0xAA5C	0xEBE0	0xAA2C	0xEBE0	0xAA6C	
	0xEBE4		0xEBE4		0xEBE4		0xEBE4		

Same table: duplicated for your convenience. Note: The upper 16-bit for instruction addresses is 0xABCD. The upper 16-bit for data addresses is 0x0000.

Given a 128 bytes 2-way set associative data cache with 16 bytes block, answer the following assuming Least Recently Used block replacement policy:

- c) For the first iteration of loop only, what is the total number of cache misses for the given data address sequence? [2 marks]
- d) For all four iterations, what is the total number of cache misses for the given data access sequence? You can assume that the data memory accesses are all generated by load word instructions. [3 marks]

Suppose we employ a combined direct mapping cache for instruction and data with 64 bytes total size and 16 bytes block size.

Note that if both instruction and data memory are accessed at the same "time step", the instruction memory access will be processed first.

- e) For the first iteration of loop only, what is the total number of cache misses with the given instruction and data access sequences? [2 marks]
- f) For all four iterations, what is the total number of cache misses with the given instruction and data access sequences? [2 marks]

$\sim\sim$ END OF PAPER $\sim\sim\sim$

(Blank truth tables, K-maps, state table and timing charts are provided in the next three pages.)

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This page is for your rough work.

A	В	C	Α	В	С	D	Α	В	C	D
0	0	0	0	0	0	0	0	0	0	0
0	0	1	0	0	0	1	0	0	0	1
0	1	0	0	0	1	0	0	0	1	0
0	1	1	0	0	1	1	0	0	1	1
1	0	0	0	1	0	0	0	1	0	0
1	0	1	0	1	0	1	0	1	0	1
1	1	0	0	1	1	0	0	1	1	0
1	1	1	0	1	1	1	0	1	1	1
			1	0	0	0	1	0	0	0
			1	0	0	1	1	0	0	1
			1	0	1	0	1	0	1	0
			1	0	1	1	1	0	1	1
			1	1	0	0	1	1	0	0
			1	1	0	1	1	1	0	1
			1	1	1	0	1	1	1	0
			1	1	1	1	1	1	1	1

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This page is for your rough work.

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1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23

1 st Iteration		2 nd Iteration		3 rd It	eration	4 th Iteration		
Inst.	Data	Inst.	Data	Inst.	Data	Inst.	Data	
0xEBD8		0xEBD8		0xEBD8		0xEBD8		
0xEBDC		0xEBDC		0xEBDC		0xEBDC		
0xEBE0	0xAA18	0xEBE0	0xAA58	0xEBE0	0xAA28	0xEBE0	0xAA68	
0xEBE4		0xEBE4		0xEBE4		0xEBE4		
0xFA10	0xBB94	0xFA10	0xBBA4	0xFA10	0xBBA4	0xFA10	0xBBB4	
0xFA14		0xFA14		0xFA14		0xFA14		
0xEBE0	0xAA1C	0xEBE0	0xAA5C	0xEBE0	0xAA2C	0xEBE0	0xAA6C	
0xEBE4		0xEBE4		0xEBE4		0xEBE4		

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