# TUTORIAL FOR WEEK 12 (Prof. Navathe) RELATIONAL DESIGN ALGORITHMS

# Q1. Binary Decomposition with Non-additive decomposition

Consider the relation

SUPPLY (Supplier#, Part#, Date, Project, Quantity, Suppliname,

Part name)

The FDs are:

Fd1: Supplier#, Part#, Date → SUPPLY

Fd2: Supplier# → Supp name

Fd3: Part# → Part name.

If we decompose SUPPLY into:

A. SUPPLY1 (Supplier#, Part#, Date, Project, Quantity, Part\_name)

SUPPLIER (Supplier#, Supp\_name)

- Have we preserved the Fds?Is this decomposition non-additive (lossless) why?
- What NF is SUPPLY1 in?
- B. Show a further decomposition of SUPPLY 1 and show that the decomposition is non-additive and achieves BCNF.

## **SOLUTION:**

# A.

- (i) Yes, all of Fd1, Fd2 and Fd3 are preserved in the design.
- (ii) To test for non-additive decomposition, we apply the NJB test.

R1 = SUPPLY1; R2 = SUPPLIER.

R1 n R2 = Supplier#

R2 - R1 = Supp name

Because R1 n R2  $\rightarrow$  (R2 - R1), we conclude that the decomposition is non-additive.

(iii)SUPPLY1 is still only in 1NF because of the Fd3 present in it.

## B.

Further 2<sup>nd</sup> normalization of SUPPLY1 produces:

SUPPLY11 (Supplier#, Part#, Date, Project, Quantity) which preserves

Fd1

PART (Part#, Part name).

Now, R1 = SUPPLY11 and R2 = PART

 $R1 \cap R2 = Part#$ 

R2 - R1 = Part name

Because R1 n R2  $\rightarrow$  (R2 - R1), we conclude that the decomposition is non-additive.

Hence the final design contains SUPPLIER, PART and

**SUPPLY11** where successive decompositions were non-additive. Hence the final set of relations also posseses the non-additive join

property. Since all of them contain only FDs with LHS as the key, the design is in BCNF.

## Q2. Relational Synthesis into 3NF relations.

Assume that we are given a universal relation corresponding to the data we have on students and courses which looks like:

STUDENT\_COURSE (Stud#, Course#, St\_name, Course\_name, Course\_credit\_hr, Grade, Major dept, Dept phone no)

The given set of F.d.s for the universal relation are:

F: {Stud#, Course# → St\_name, Course\_name, Course\_credit\_hr, Grade, Major\_dept, Dept phone no;

Stud# → St name, Major dept, Dept phone no;

Course# → Course\_name, Course\_credit\_hr

Major\_dept → Dept\_phone\_no.}.

- A. Apply the <u>synthesis algorithm</u> 15.4 that constructs 3NF relations from a given set of F.d.'s, on the universal relation. What 3NF design will be produced by this algorithm? Show how you get the answer
- B. Evaluate your 3NF design and evaluate if it meets BCNF design.

#### **SOLUTION:**

#### PART A:

#### Given F:

 $\{FD1: Stud\#, Course\# \rightarrow St\_name, Course\_name, Course\_credit\_hr, Grade, Major\_dept, Dept\_phone\_no;$ 

FD2: Stud# → St name, Major dept, Dept phone no;

FD3: Course# → Course name, Course credit hr

FD4: Major dept → Dept phone no.},

#### **Computing Min. Cover of F:**

Note: We are skipping the second step of algo. 15.2 where each FD is decomposed to have only one attribute on RHS.

The minimal cover is:

 $F_{min} = \{Stud\# \rightarrow St name, Major dept, \}$ 

```
Course# → Course_name, Course_credit_hr,

Major_dept → Dept_phone_no,

Stud#, Course# → Grade }

Why? Because,
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- (i) The part of FD1 based on the key (Stud#, Course#) on LHS has extraneous attribute Course# in order to functionally determine Stud#, Course#. Hence it is identical to FD2 and can be eliminated.
- (ii) The part of FD1 based on the key (Stud#, Course#) on LHS **has extraneous attribute Stud#** in order to functionally determine Course\_name, Course\_credit\_hr. Hence it is identical to FD3 and can be eliminated.
- (iii) After removing these attributes on the RHS of FD1, it reduces to Stud#, Course# → Grade.
   That results in the above min. cover.

**NOTE Also** that the min cover in standard form contains FDs as follows:

```
Stud# → St_name,

Stud# → Major_dept,

Course# → Course_name,

Course# → Course_credit_hr.

We REGROUP them into

Stud# → St_name, Major_dept

And

Course# → Course_name, Course_credit_hr

Before going to form the 3NF design in step 3 of the .
```

Once, the above min.cover is obtained, the second step in algorithm 15.4 constructs one relation per FD in the min. cover, giving:

```
R1( Stud#, St_name, Major_dept )
R2 (Course#, Course_name, Course_credit_hr)
R3 (Major_dept , Dept_phone_no)
R4( Stud#, Course# , Grade)
```

**PART B:** Each of R1, R2, R3 and R4 contains an FD where the LHS is the key for that relation. There are no other known FDs. Hence, it meets the requirement of BCNF and hence the design is in BCNF.

## Q3. BCNF Decomposition and n-ary non-additive decomposition test:

#### Consider a relation:

PATIENT\_PROC (Patient#, Doctor#, Date, Doctor\_name, Doctor\_specialty, Procedure, Charge)

The Fds are:

FD1:Patient#, Doctor#, Date → PATIENT PROC

FD2:Doctor# → Doctor name, Doctor specialty

FD3:Procedure → Doctor

#### A. Successive Normalization

- (i) Evaluate and explain the normal form status of the given relation.
- (ii) Follow the practice of successive normalization upto BCNF. For converting 3Nf to BCNF, apply the decomposition as per the decomposition in algorithm 15.5.

## B. Direct testing and application of Algo 15.5

- (i) Argue using the BCNF general definition that PATIENT\_PROC does not meet BCNF '
- (iii) . By applying decomposition in algorithm 15.5 successively produce the BCNF design.

## C. Applying n-ary non-additive decomposition test in Algo 15.3

Show that the resulting relations you produced as BCNF design in A meet the non-additive join property using this algorithm.

#### **SOLUTION:**

- (i) The FD2 shows non-full functional dependencies of the attributes Doctor\_name and Doctor\_specialty on Doctor# and hence is only in 1 NF.
- (ii) Successive decomposition:

#### Second normalization:

PP1 (Patient#, Doctor#, Date, Procedure, Charge)

DOCTOR (Doctor#, Doctor name, Doctor specialty)

## **Third Normalization:**

PP1 and DOCTOR are in 3NF.

PP1 is in 3 NF because it has 2 Fds:

FD11: Patient#, Doctor#, Date → Procedure, Charge

FD12: Procedure → Doctor#

FD11 meets the condition that LHS is superkey

FD12 meets the condition that RHS is prime attribute.

## **BCNF Normalization**

However, FD12 violates BCNF.

Hence apply Algo 15.5 to PP1 and decompose it into:

PP11(Patient#, Date, Procedure, Charge) and

PP12 (Procedure, Doctor#).

Hence the final design is: DOCTOR, PP11 and PP12 tables.

NOTE: The dependency FD1 which is primary-key based FD has been lost.

B.

FIRST ATTEMPT (CASE X):

By Applying the BCNF definition directly, we see that PATIENT\_PROC is not in BCNF because of

FD2 and FD3 which do not meet the requirement of LHS being a superkey. Suppose we fix the FD2 first. Then the first decomposition will produce:

PX1 (Patient#, Doctor#, Date, Procedure, Charge)

DOCTOR (Doctor#, Doctor name, Doctor specialty)

Now PX1 has the FDX1: Procedure  $\rightarrow$  Doctor where LHS is not a superkey.

Hence we apply 15.5 and decompose into:

PX11 (Patient#, Date, Procedure, Charge) and

PX12 (Procedure, Doctor#)

Thus the final design is DOCTOR, PX11, PX12 which is identical with A.

#### SECOND ATTEMPT (CASE Y):

Suppose we fix FD3 first. Then the first decomposition produces:

PY1 (Patient#, Date, Doctor\_name, Doctor\_specialty, Procedure, Charge) and PY2 ((Procedure, Doctor#)

PY1 now has the FD:

FY11: Patient#, Date, Procedure → Doctor\_name, Doctor\_specialty, Charge And

FY12: Procedure → Doctor\_name, Doctor\_specialty.

Now, FY11 has an LHS that is a superkey;

However, FY12 does not meet BCNF. Hence we apply 15.5 to decompose PY1 as:

PY11( Patient#, Date, Procedure, Charge) and

PY12 (Procedure, Doctor name, Doctor specialty).

Thus the final BCNF design contains:

PY2, PY11,PY12. Notice that it is almost identical to the first case X except the Doctor# from first design X is replaced by Procedure in PY12 in the second design Y.



TESTING FOR non-additive decomposition.

Set up the initial tableau for the 3 decomposed relations as 3 rows and one column for each attribute. A's represent columns that are present in the relation. B's represent columns that are absent in the relation.

The goal is to see if we can get any row of the tableau to have all a's after the algorithm is applied. That proves that the n-ary decomposition is non-additive.

(iv)P#	Doc#	Date	Dname	Doctor_	Procedu	Charge	

					Specialty	re	
R1	b	a2	b	a4	a5	b	b
R2	a1	b	a 3	a4	b	a 6	a 7
R3	b	a2	b	b	b	a 6	b

R1: DOCTOR (Doctor#, Doctor\_name, Doctor\_specialty)

R2: PP11(Patient#, Date, Procedure, Charge)

R3: PP12 (Procedure, Doctor).

FIRST STEP: Because Procedure  $\rightarrow$  Doctor and a6  $\rightarrow$  a2 is present in row3,

We can set Doc# column from b to a in R2

(\	<b>√)</b> P#	Doc#	Date	Dname	Doctor_ Specialty	Procedu re	Charge
R1	b	a2	b	a4	a5	b	b
R2	a1	<del>b</del> a2	a 3	b	b	a 6	a 7
R3	b	a2	b	b	b	a 6	b

**SECOND STEP**: Because Doctor#  $\rightarrow$  Doctor\_name, Doctor\_specialty and a2  $\rightarrow$  a4,a5 is present in row1, and now we have a2 present in row2, we can set Doc# column from b to a in R2

(\	vi)P#	Doc#	Date	Dname	Doctor_ Specialty	Procedu re	Charge
R1	b	a2	b	a4	a5	b	b
R2	a1	<del>b</del> a2	a 3	<del>b</del> <mark>a4</mark>	<del>b</del> a5	a 6	a 7
R3	b	a2	b	b	b	a 6	b

Now, entire row 2 for R2 has been set to a's. That concludes the procedure and determines that the R1, R2, R3 decomposition has the non-additive join property.