

# LINEAR DATA STRUCTURE

## LINKED LIST

**CO1:** Classify and Apply the concepts of stacks, queues and linked list in real life problem solving

**Reference:**

1. Reema Thareja; Data Structures using C; Oxford
2. Ellis Horowitz, Sartaj Sahni; Fundamentals of Data Structures; Galgotia Publications
3. Jean Paul Tremblay, Paul G. Sorenson; An introduction to data structures with applications; Tata McGrawHill



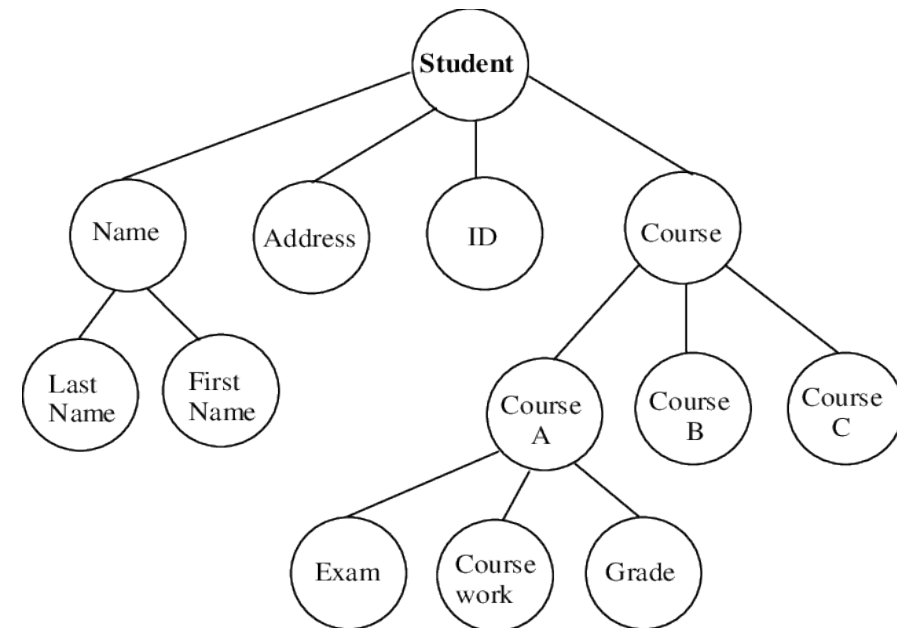
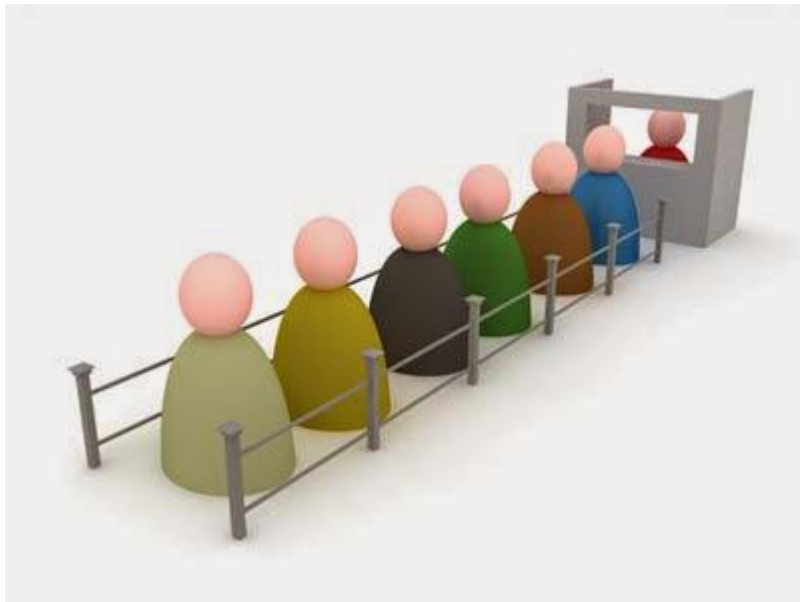
# LINKED LIST

- Introduction of data structures
- Types of data structures
- Operations of Data Structures
- Introduction of linked list
- Why linked list
- Linked List – Node Structure
- Types of linked list
- Dynamic Memory Management
- Dynamic memory allocation
- Singly linked list
- Doubly linked list
- Circular Linked List
- Applications of linked list
- Analysis of Algorithms
- Analysis of Array
- Analysis of Linked List

# INTRODUCTION OF DATA STRUCTURES

## Data Structure:

- Data structure is a way of storing and organizing data in a computer so that it can be used efficiently
- It shows the relationship of one data element with the other and organize it within the memory
- It helps you to analyse the data, store it and organize it in a logical or mathematical manner



# INTRODUCTION OF DATA STRUCTURES

## Data Structure:

- Data structure is a DFA.....set of Domains D, a set of functions F and a set of axioms A
- Domain (D) : Range of values the data may have
- Functions (F) : Set of operations that can be performed on data
- Axioms (A): Set of rules to perform set of operations (F)



Array X

- Domain (D): Range of integers
- Functions (F): Insert, Delete, Count, Traversal, Sorting, Empty, Full
- Axioms (A): Insert(X, n) -> X

Empty(X) - > True or False

Count(X) -> count\_no

# TYPES OF DATA STRUCTURES

- **Primitive and Non-primitive:**

- **Primitive Data Structure:** The fundamental data types which are supported by a programming language
  - int, char, float, pointers, bool
- **Non-primitive Data Structure:** Defines set of derived elements that can be formed using primitive data structure
  - Arrays, Structure, Linked list, Stack, Queue, Tree Graph

- **Static and Dynamic:**

- **Static Data Structure:** It has fixed memory size. Memory is allocated at the time of compilation
  - Array
- **Dynamic Data Structure:** It has no fixed size and memory can be allocated dynamically at run time
  - Linked List

# TYPES OF DATA STRUCTURES

- **Linear and Non-linear:**
- **Linear Data Structure:**
  - Elements are arranged to form a linear sequence
  - Every data element has a unique successor and predecessor
  - There is one to one relationship between the elements
  - Array, Linked Lists, Stack, Queue are examples of Linear Data Structures
- **Non-linear data structures:**
  - Every data element may have more than one predecessor as well as successor
  - They are used to represent the data containing hierarchical or network relationship among the elements
  - Trees and graphs are examples of non-linear data structures

# OPERATIONS ON DATA STRUCTURES

- ❖ **Traversing:** It means to access each data item exactly once so that it can be processed

To print the names of all the students in a class

- ❖ **Searching:** It is used to find the location of one or more data items that satisfy the given constraint

Such a data item may or may not be present in the given collection of data items

To find the names of all the students who has enrolled for course

Data structure

- ❖ **Inserting:** It is used to add new data items to the given list of data items

To add the details of a new student who has recently joined the course

Programming

Roll No.	Name of the student	Course
1	Smita Patil	Data Structure
2	Esha Surve	Programming
3	Monali Chaudhari	Data structure
4	Kunal Kamat	Data structure
5	Manthan Naik	Programming

6 Shahid Kapoor Programming

Smita Patil

Esha Surve

Monali Chaudhari

Kunal Kamat

Manthan Naik



# OPERATIONS ON DATA STRUCTURES

- ❖ **Deleting:** It means to delete a particular data item from the given collection of data items

To delete the name of a student who has left the course

- ❖ **Sorting:** Data items can be arranged in some order like ascending order or descending order depending on the type of application

Arranging the names of students in a class in an alphabetical order

- ❖ **Merging:** Lists of two sorted data items can be combined to form a single list of sorted data items

Combining students of two courses computer and IT

Roll No.	Name of the student	Course
1	Smita Patil	Data Structure
2	Esha Surve	Programming
3	Monali Chaudhari	Data structure
4	Kunal Kamat	Data structure
5	Manthan Naik	Programming
6	Shahid Kapoor	Programming
Roll No.	Name of the student	Course
2	Esha Surve	Programming
4	Kunal Kamat	Data structure
3	Monali Chaudhari	Data structure
6	Shahid Kapoor	Programming
1	Smita Patil	Data Structure



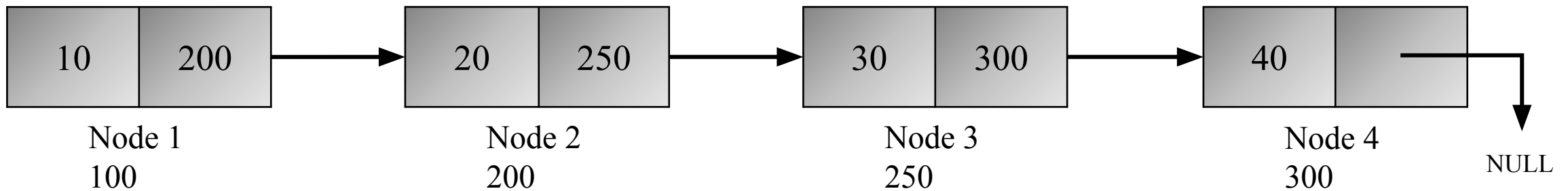
# INTRODUCTION OF LINKED LIST

- Linked list is an ordered collection of data elements called as nodes that are randomly stored in memory
- Linked list is a linear and dynamic data structure
- Node is a structure consisting of two fields: Data field and Next field



Node

- Linked list example:



# WHY LINKED LIST

## Limitations of Array:

Array declaration:

```
int a[10];
```

### Case 1: User has declared array of size 10 and stored 10 elements in an array

0	1	2	3	4	5	6	7	8	9
1	2	3	4	5	6	7	8	9	10

## Array

### Case 2: User has declared array of size 10 and stored only 5 elements

0	1	2	3	4	5	6	7	8	9
1	2	3	4	5					

## Array

### Case 3: User has declared array of size 10 and want to increase size of an array

[illegible]

# Array

## Memory

# WHY LINKED LIST

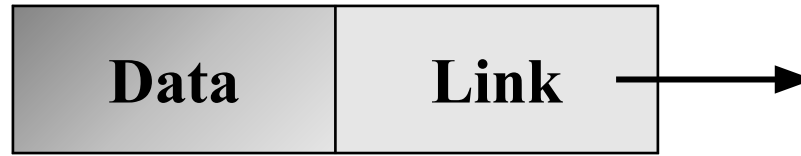
## Limitations of Array:

- In array, elements are stored in contiguous memory locations
- Static Data Structure: Size must be known at the time of declaration before compilation of the program
- Insertion and deletion of elements in between the array requires a lot of data movement

## Linked List:

- In linked list, elements are not stored contiguous memory locations
- Each node is connected to its successor through the link (implemented using pointers)
- Linked list is used to store similar type of data in memory

# LINKED LIST – NODE STRUCTURE



Node

Structure for Linked List:

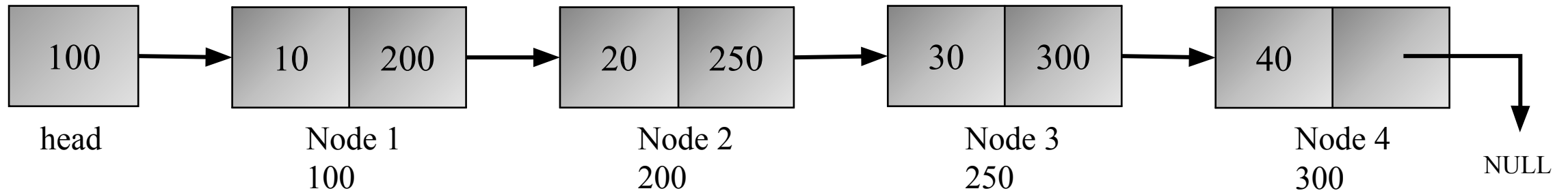
```
struct node
{
    int data;
    struct node *next;
};
```

# TYPES OF LINKED LIST

There are 4 Types of Linked List:

- Singly Linked List
- Doubly Linked List
- Circular Linked List
- Doubly Circular Linked List

Singly Linked List:



```
struct node
{
    int data;
    struct node *next;
};
```

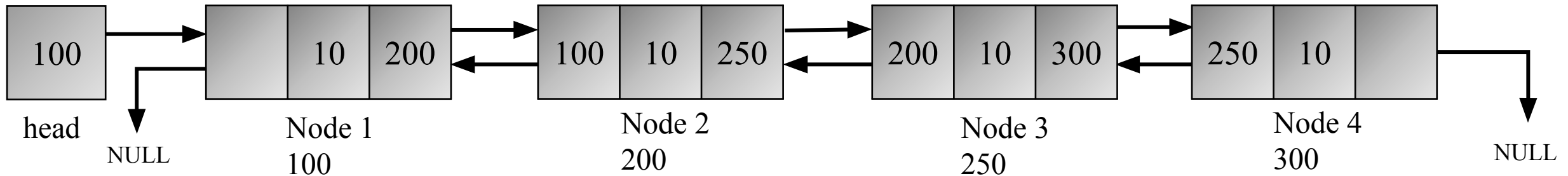
# TYPES OF LINKED LIST

## Doubly Linked List:

### Node Structure:



### Example:



```
struct node
```

```
{
```

```
    int data;
```

```
    struct node *next;
```

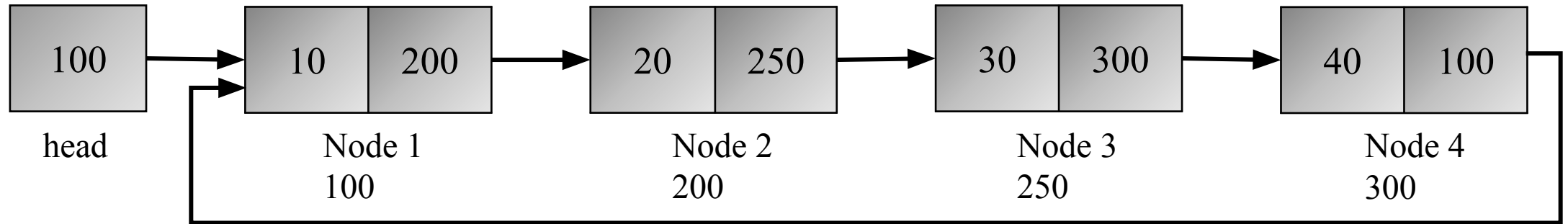
```
    struct node *prev;
```

```
};
```

# TYPES OF LINKED LIST

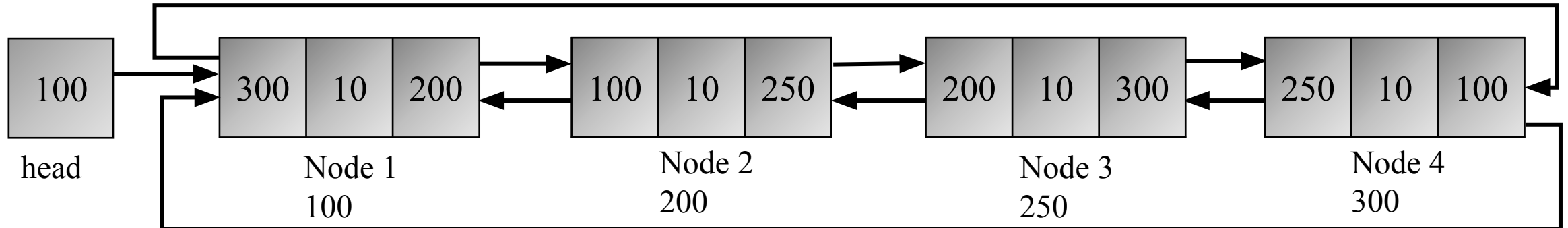
## Circular Linked List:

Example:



## Doubly Circular Linked List:

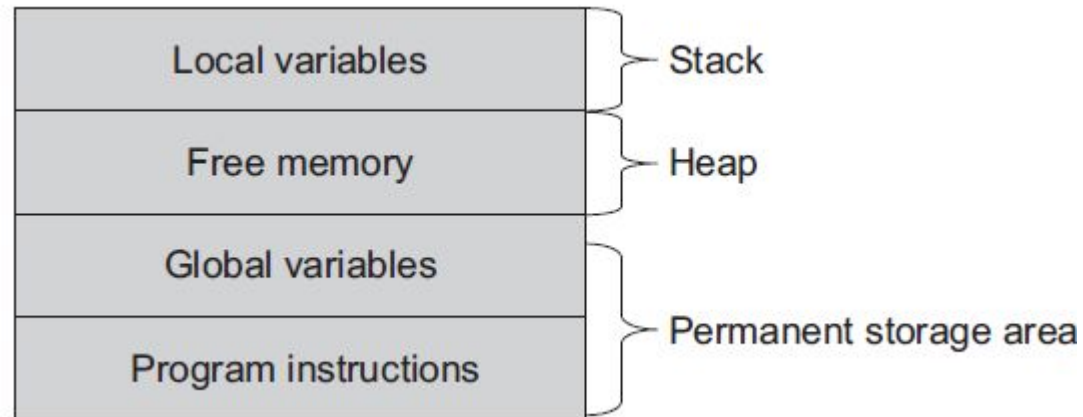
Example:





# DYNAMIC MEMORY MANAGEMENT

- Many languages permit a programmer to specify an array's size at run-time so they have the ability to calculate and assign, during execution, the memory space required by the variables in a program
- The process of allocating memory at run-time is known as *dynamic memory allocation*



- **Permanent Storage Area:** Program instructions, Global and Static variables are stored
- **Stack:** Local variables are stored on stack
- **Heap:** Memory space available between permanent storage area and stack can be used for dynamic allocation during program execution and Size of the heap keeps changing when a program is executed because of the creation and deletion of the variables that are local to the functions and blocks

# DYNAMIC MEMORY ALLOCATION

- Dynamic memory management technique allows us to allocate memory dynamically or release unwanted space at run time, optimizing the use of storage space
- There are 4 library functions available in C for dynamic memory allocation

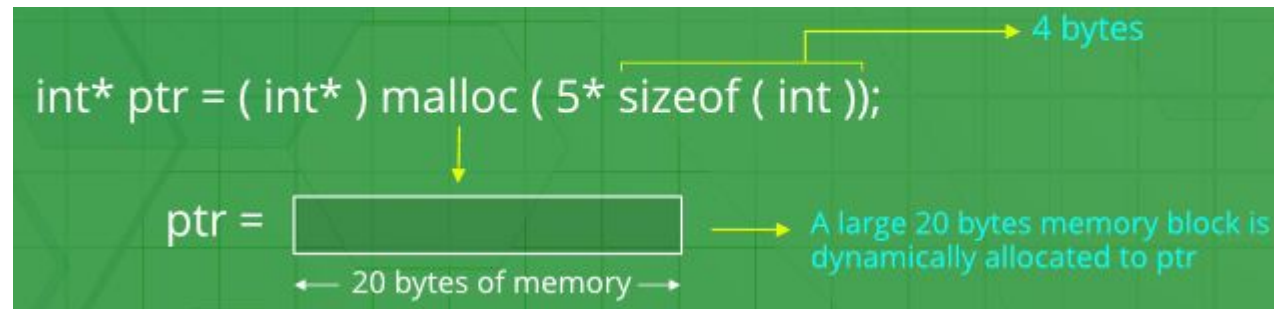
- malloc()
- calloc()
- free()
- realloc()

- **malloc(): - Memory Allocation**

- Reserves a block of memory of specified no. of bytes and returns a pointer of type void

**Syntax:** *ptr = (cast-type \*) malloc(byte size);*

**Example:** if we want to allocate space in memory for 5 integers



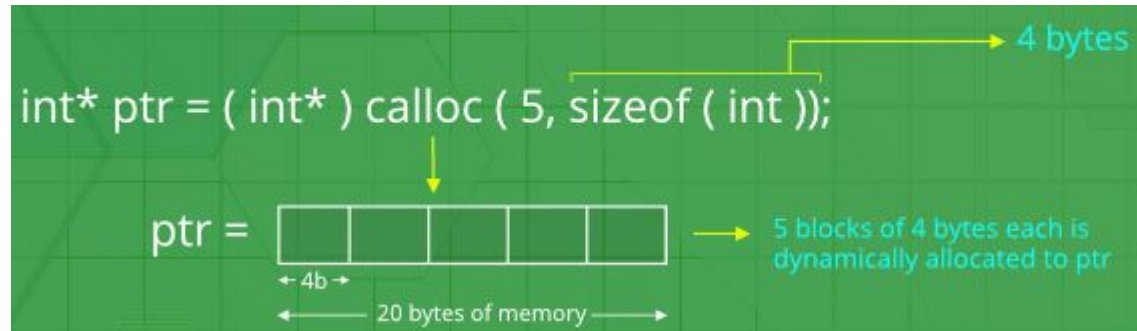
# DYNAMIC MEMORY ALLOCATION

- **calloc(): - Contiguous Allocation**

- Reserves a multiple block of memory each of same size and initializes all bits to zero

**Syntax:** *ptr = (cast-type \*) calloc(n, byte size);*

**Example:** if we want to allocate space in memory for 5 integers, 5 separate block of memory will be allocated



- **Free(): - Deallocate memory**

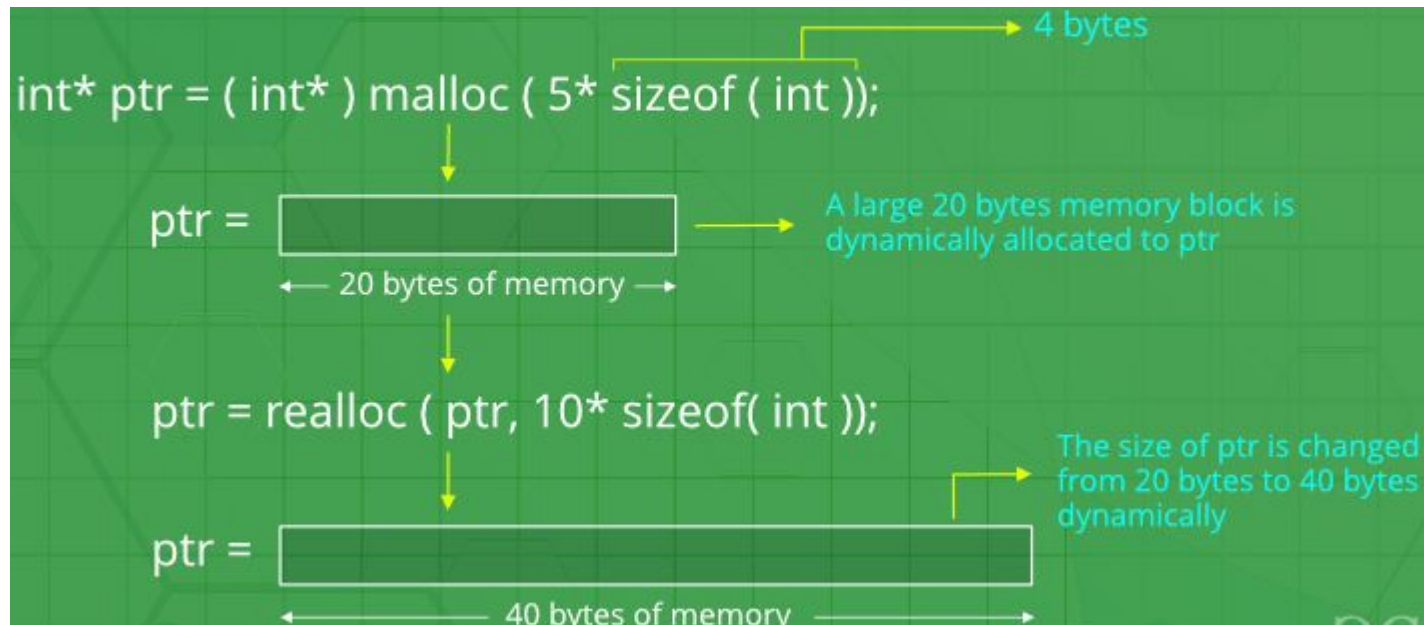
- Dynamically allocated memory created with either calloc() or malloc() doesn't get freed on their own. You must explicitly use free() to release the space.

**Syntax:** *free(ptr);*

# DYNAMIC MEMORY ALLOCATION

- **realloc(): - Re Allocation**
- If the dynamically allocated memory with the help of malloc() or calloc() is insufficient, realloc() can be used to dynamically re-allocate memory
- Re-allocation of memory maintains the already present value and new blocks will be initialized with default garbage value

**Syntax:** *ptr = realloc(ptr, new byte size);*



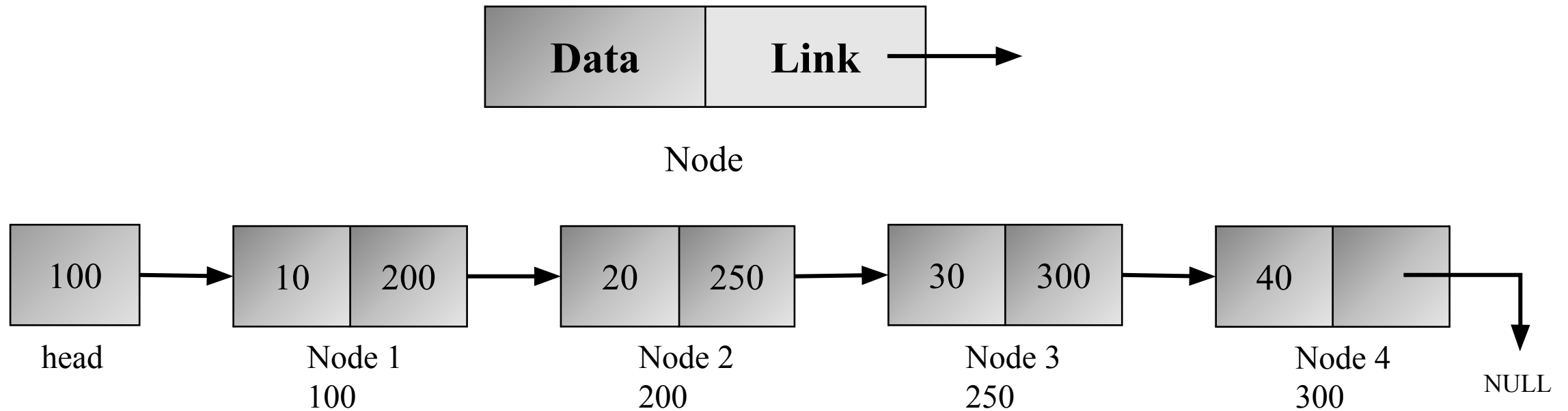


# SINGLY LINKED LIST

- Introduction
- Creation of linked list
- Display linked list
- Insertion of node in linked list
- Deletion of node from linked list
- Reverse linked list
- Updating linked list

# INTRODUCTION

## Singly Linked List:



*struct node*

{

*int data;*

*struct node \*next;*

};

# CREATION OF SINGLY LINKED LIST

```
node *createsll()
```

```
{
```

```
    node *head = NULL, *temp, *newnode;
```

```
    int x; char ans;
```

```
    do
```

```
    {
```

```
        printf("Enter data to node:");
```

```
        scanf("%d", &x);
```

```
        newnode = (node *)malloc(sizeof(node));
```

```
        newnode->data = x;
```

```
        newnode->next = NULL;
```

```
        if(head == NULL)
```

```
        else
```

```
        {
```

```
            head = temp = newnode;
```

```
            temp->next = newnode;
```

```
            temp = newnode;
```

```
        }
```

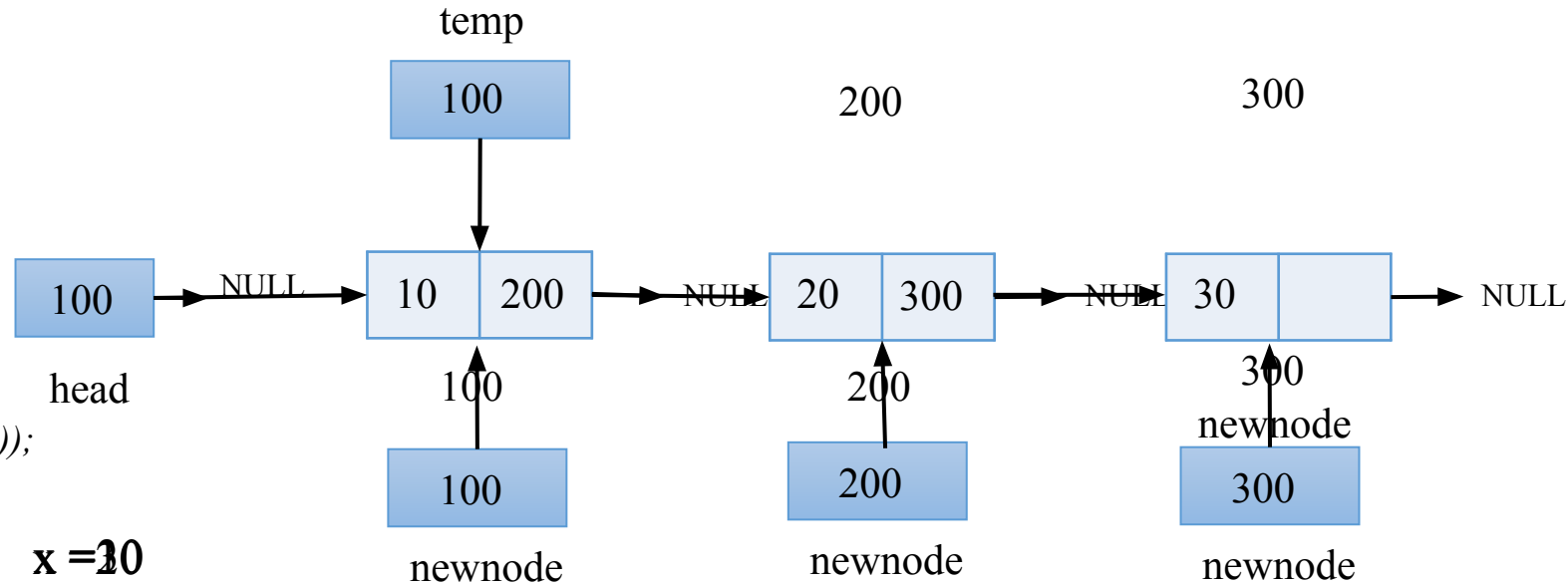
```
        printf("Do you want to add more nodes?");
```

```
        scanf("%c", &ans);
```

```
    }while(ans == 'Y');
```

```
    return head;
```

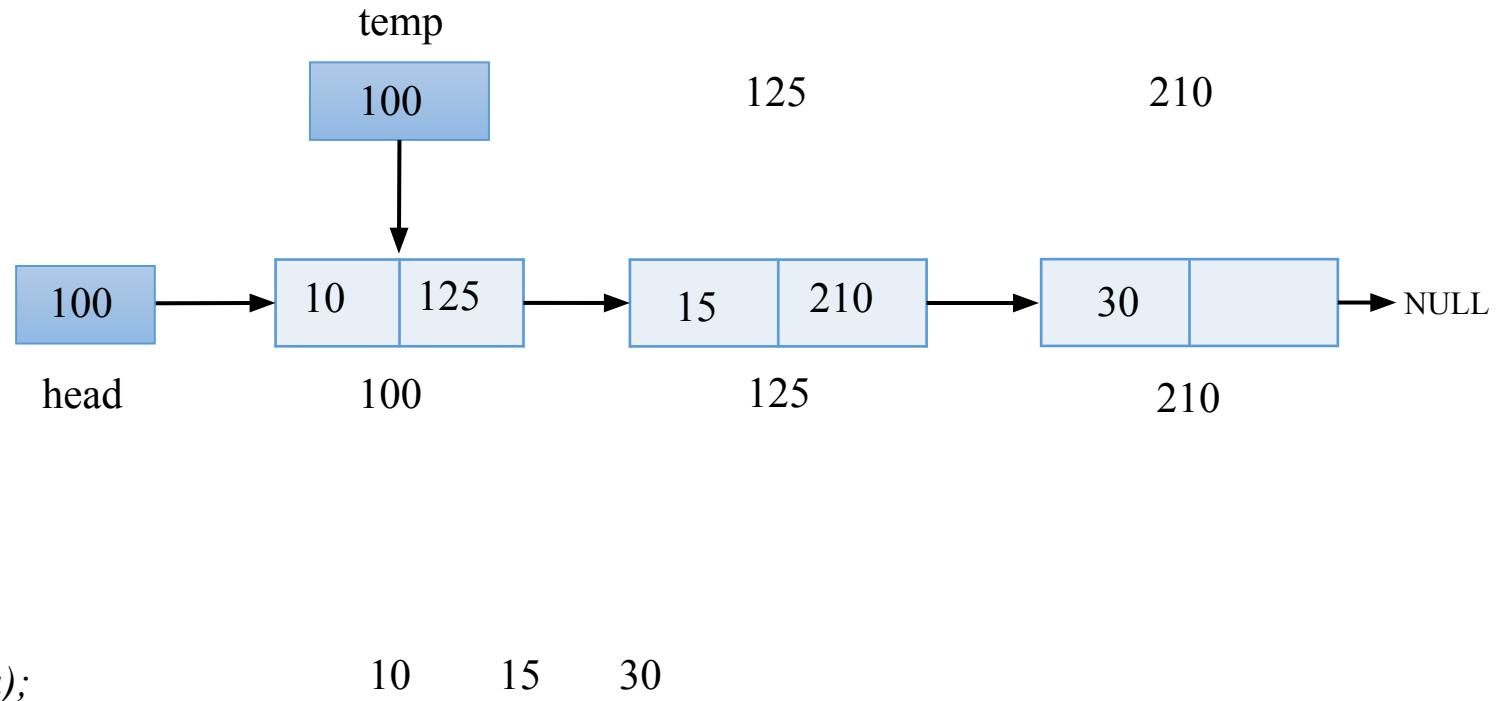
```
}
```





# DISPLAY SINGLY LINKED LIST

```
void display(node *head)
{
    node *temp = head;
    if(temp == NULL)
        printf("List is empty");
    else
    {
        while(temp!=NULL)
        {
            printf("%d ", temp->data);
            temp = temp->next;
        }
    }
}
```



# INSERTION OF NODE IN SINGLY LINKED LIST

There are three ways of inserting a node in a linked list –

- Insertion of a node at the beginning
- Insertion of a node in a middle
- Insertion of a node at the end

□ Insertion of a node at the beginning:

```
node *insertatbeginning(node *head)
```

```
{
```

```
    node *newnode;
```

```
    int x;
```

```
    printf("Enter data to node: ");
```

```
    scanf("%d", &x);
```

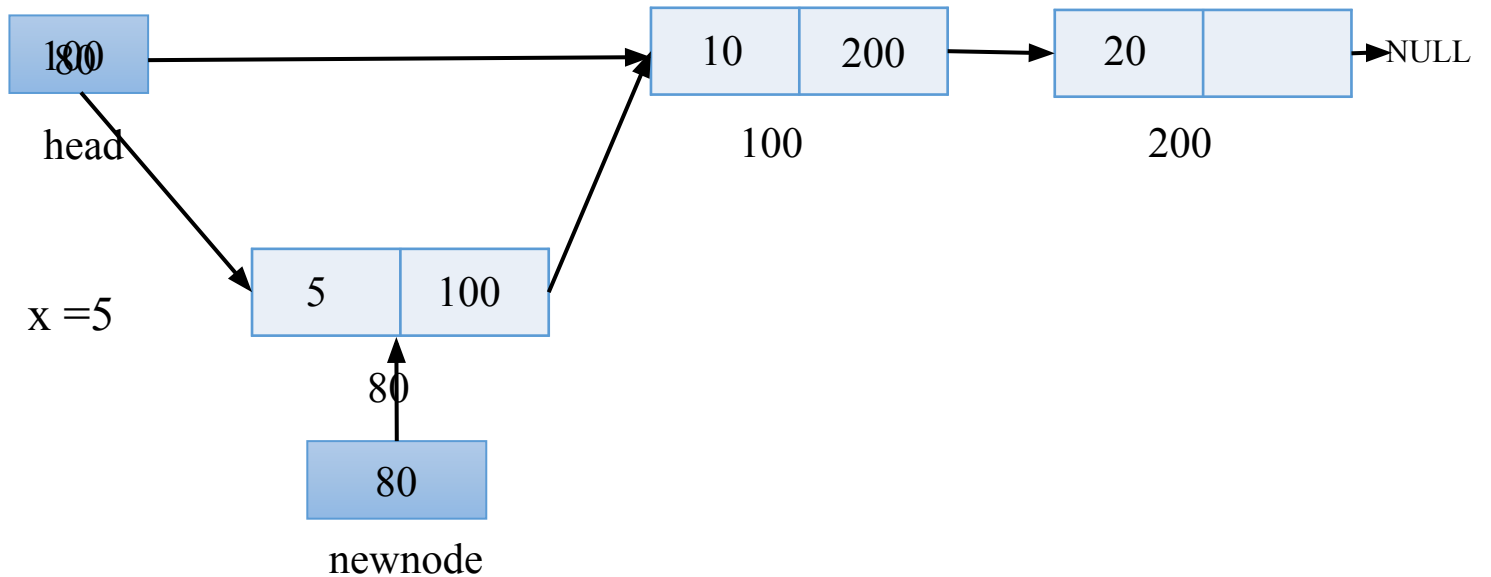
```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    newnode->next = head;
```

```
    head = newnode;
```

```
}
```



# INSERTION OF NODE IN SINGLY LINKED LIST

□ Insertion of a node in the middle:

```
node *insertinmiddle(node *head, int loc)
```

```
{
```

```
    node *newnode;
```

```
    int x, i=1;
```

```
    printf("Enter data to node:");
```

```
    scanf("%d", &x);
```

```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    temp = head;
```

```
    while(i < (loc-1))
```

```
{
```

```
        temp = temp->next;
```

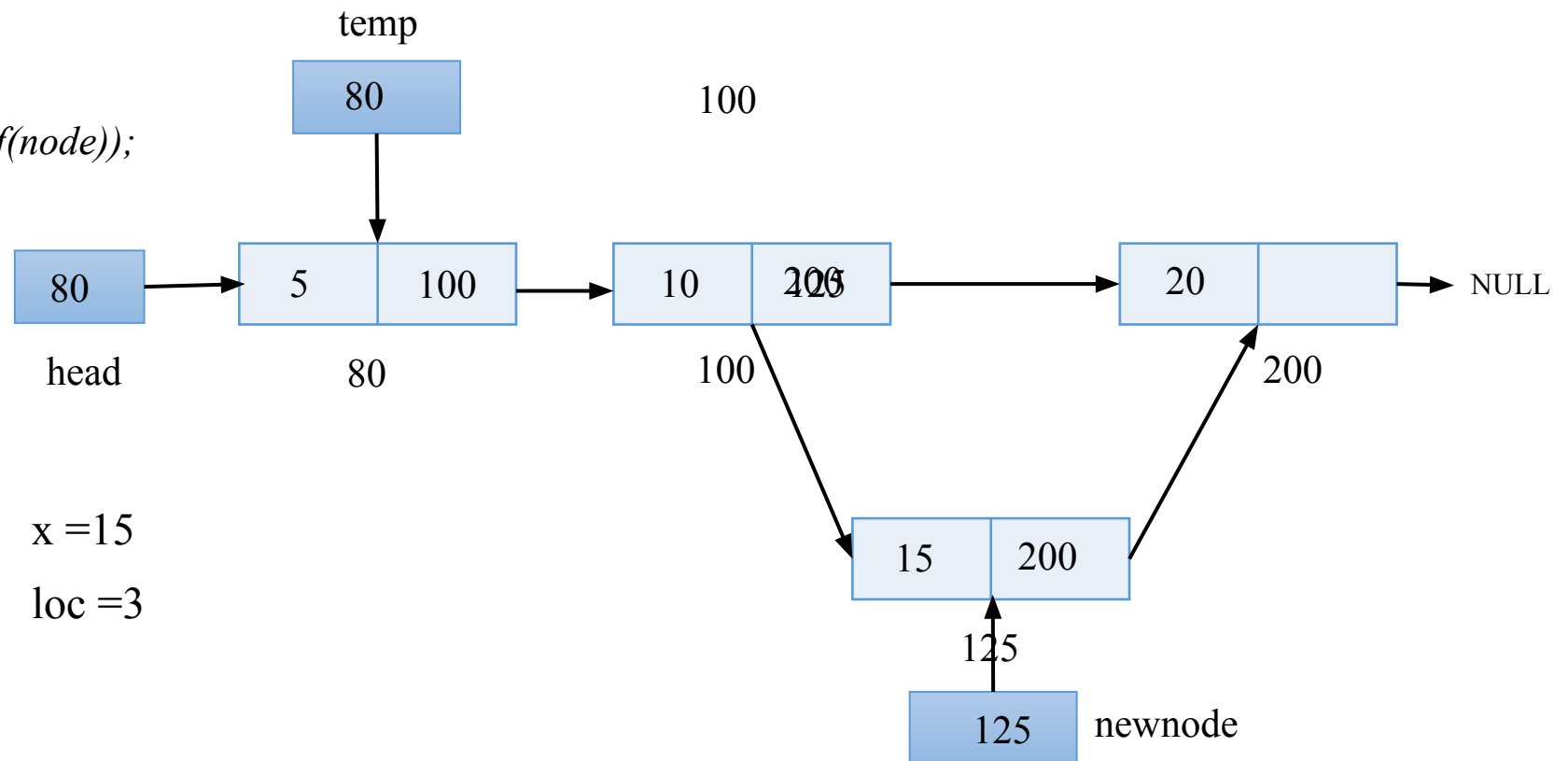
```
        i++;
```

```
}
```

```
    newnode->next = temp->next;
```

```
    temp->next = newnode;
```

```
}
```



# INSERTION OF NODE IN SINGLY LINKED LIST

□ Insertion of a node at the end:

```
node *insertatend(node *head)
```

```
{
```

```
    node *newnode;
```

```
    int x;
```

```
    printf("Enter data to node:");
```

```
    scanf("%d", &x);
```

```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    newnode->next = NULL;
```

```
    temp = head;
```

```
    while(temp->next != NULL)
```

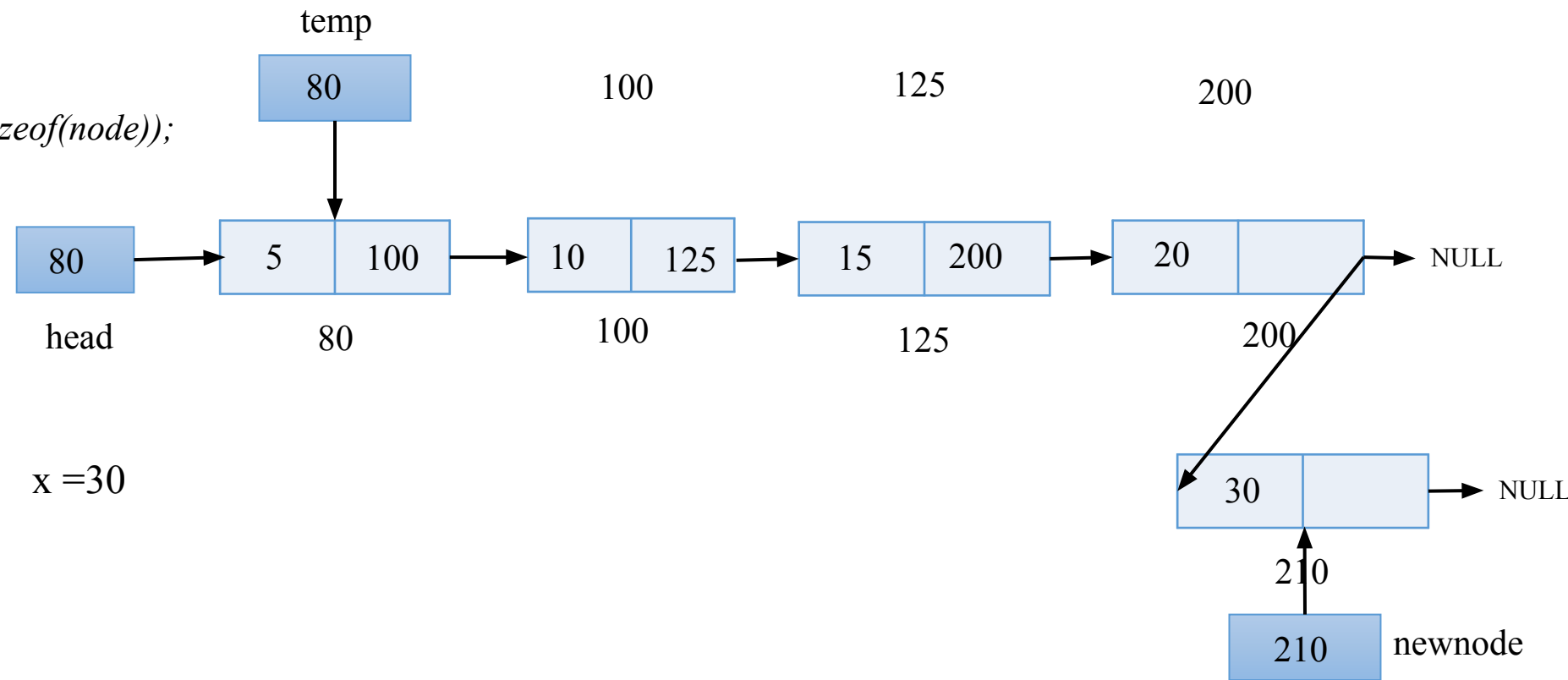
```
    {
```

```
        temp = temp->next;
```

```
    }
```

```
    temp->next = newnode;
```

```
}
```



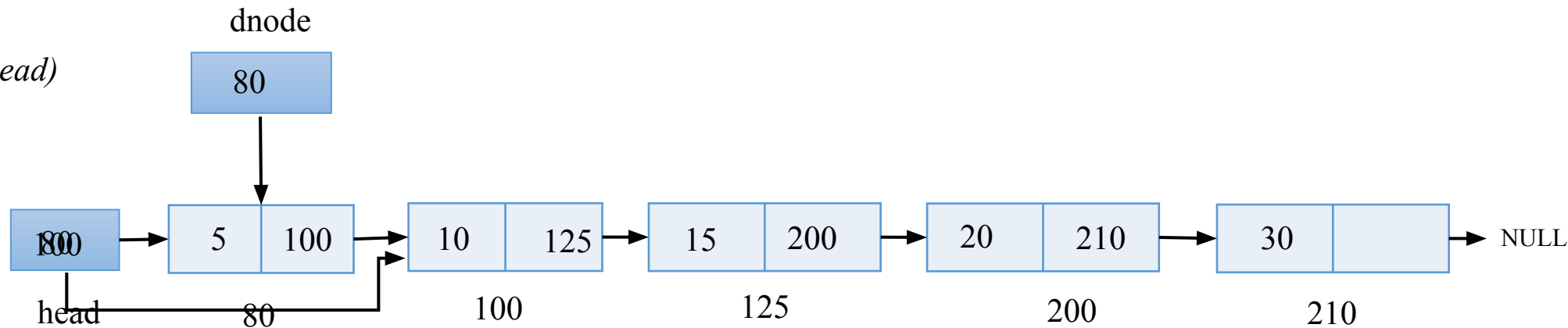
# DELETION OF NODE FROM SINGLY LINKED LIST

There are three ways of deleting a node from a linked list –

- ❑ Delete the first node
- ❑ Delete node from middle of linked list
- ❑ Delete the last node

## ❑ Deletion of the first node:

```
node *deletefirstnode(node *head)
{
    node *dnode;
    dnode = head;
    head = head->next;
    free(dnode);
    return head;
}
```



# DELETION OF NODE FROM SINGLY LINKED LIST

## □ Deletion of a middle node:

```
node *deletemiddlenode(node *head)
```

```
{
```

```
    node *temp, *dnode;
```

```
    int loc, i=1;
```

```
    printf("Enter the location of the node you want to delete: ");
```

```
    scanf("%d", &loc);
```

```
    temp = head;
```

```
    while(i < (loc-1))
```

```
{
```

```
        temp = temp->next;
```

```
        i++;
```

```
}
```

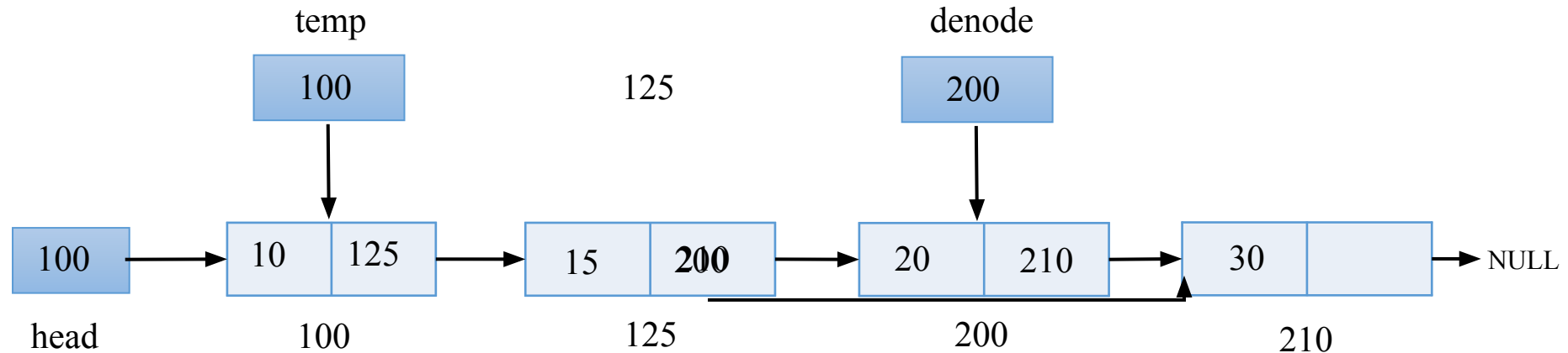
```
dnode = temp->next;
```

```
temp->next = dnode->next;
```

```
free(dnode);
```

```
return head;
```

```
}
```

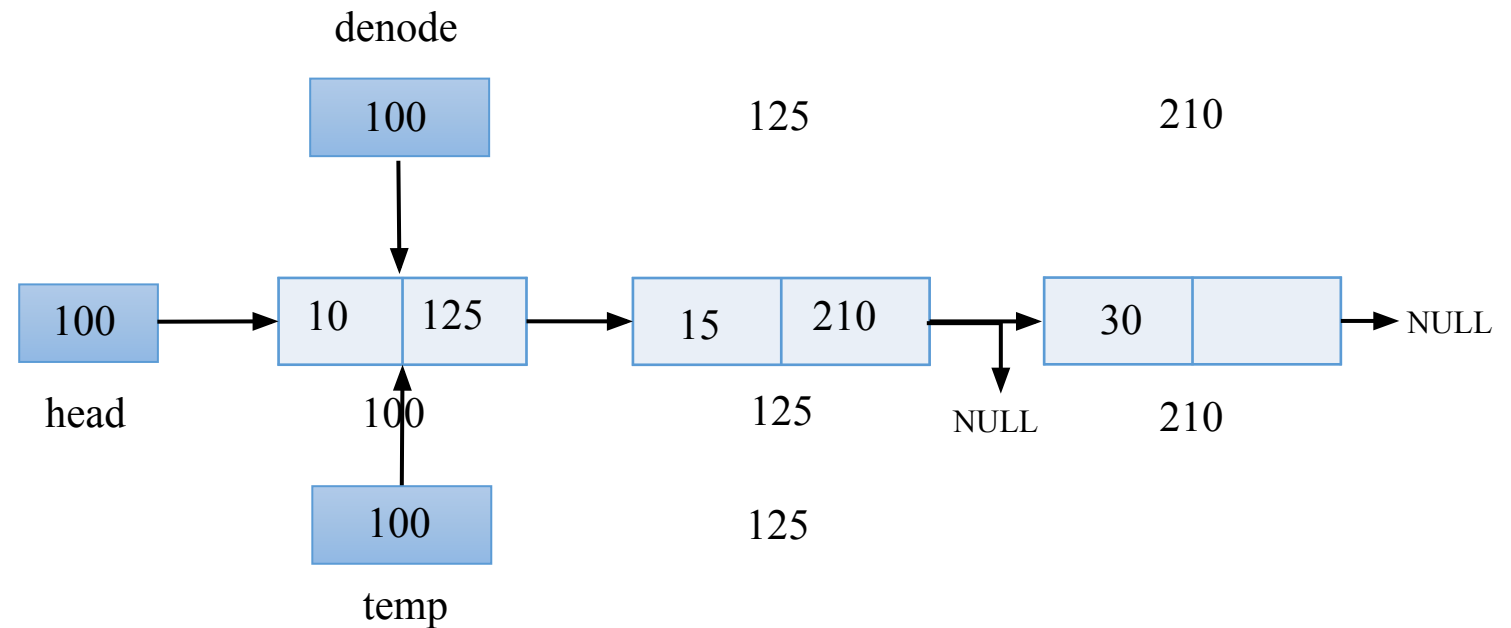


# DELETION OF NODE FROM SINGLY LINKED LIST

## □ Deletion of a last node:

```
node *deletelastnode(node *head)
{
    node *temp, *dnode;
    dnode = head;
    while(dnode->next != NULL)
    {
        dnode = temp;
        dnode = dnode->next;
    }
    if(dnode == head)
        head = NULL;
    else
    {
        temp->next = NULL;
    }

    free(dnode);
    return head;
}
```





# REVERSE SINGLY LINKED LIST

There are two methods to reverse a linked list:

□ Iterative Method

□ Recursive method

```
void *displayrevers(node *head)
```

```
{
```

```
    node *prevnode = NULL, *currentnode, *nextnode;
```

```
    currentnode = head;
```

```
    while(currentnode != NULL)
```

```
    {
```

```
        nextnode = currentnode->next;
```

```
        currentnode->next = prevnode;
```

```
        prevnode = currentnode;
```

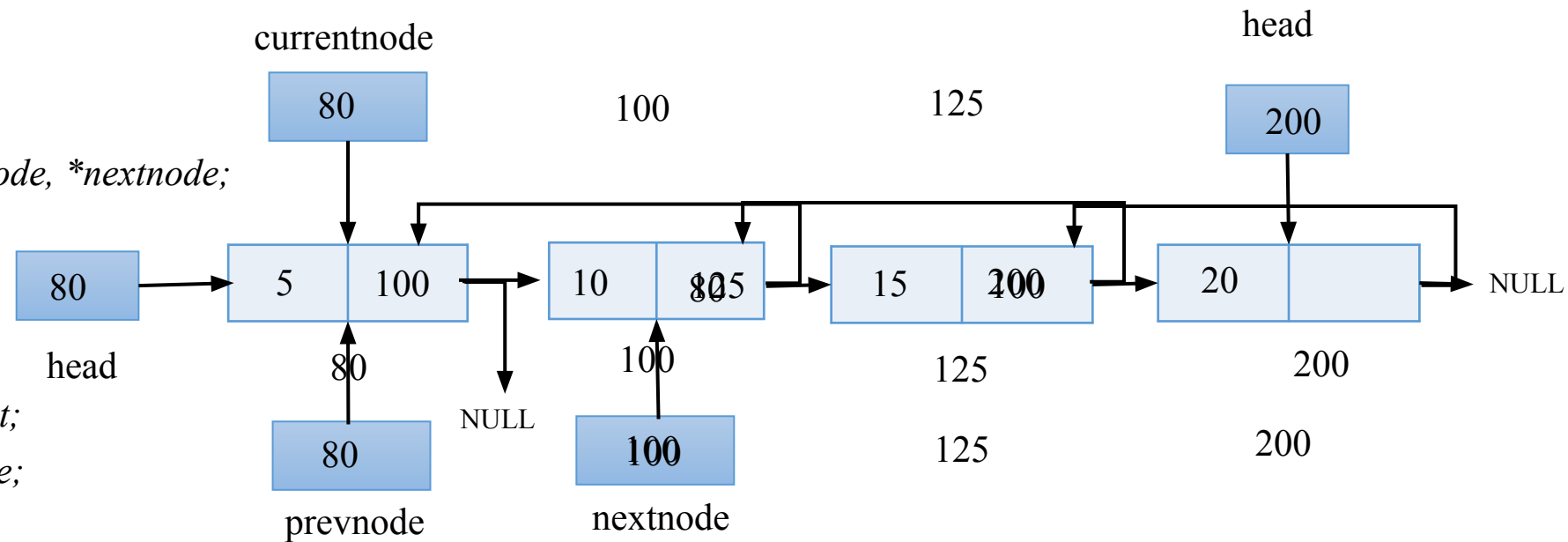
```
        currentnode = nextnode;
```

```
    }
```

```
    head = prevnode;
```

```
    display(head);
```

```
}
```

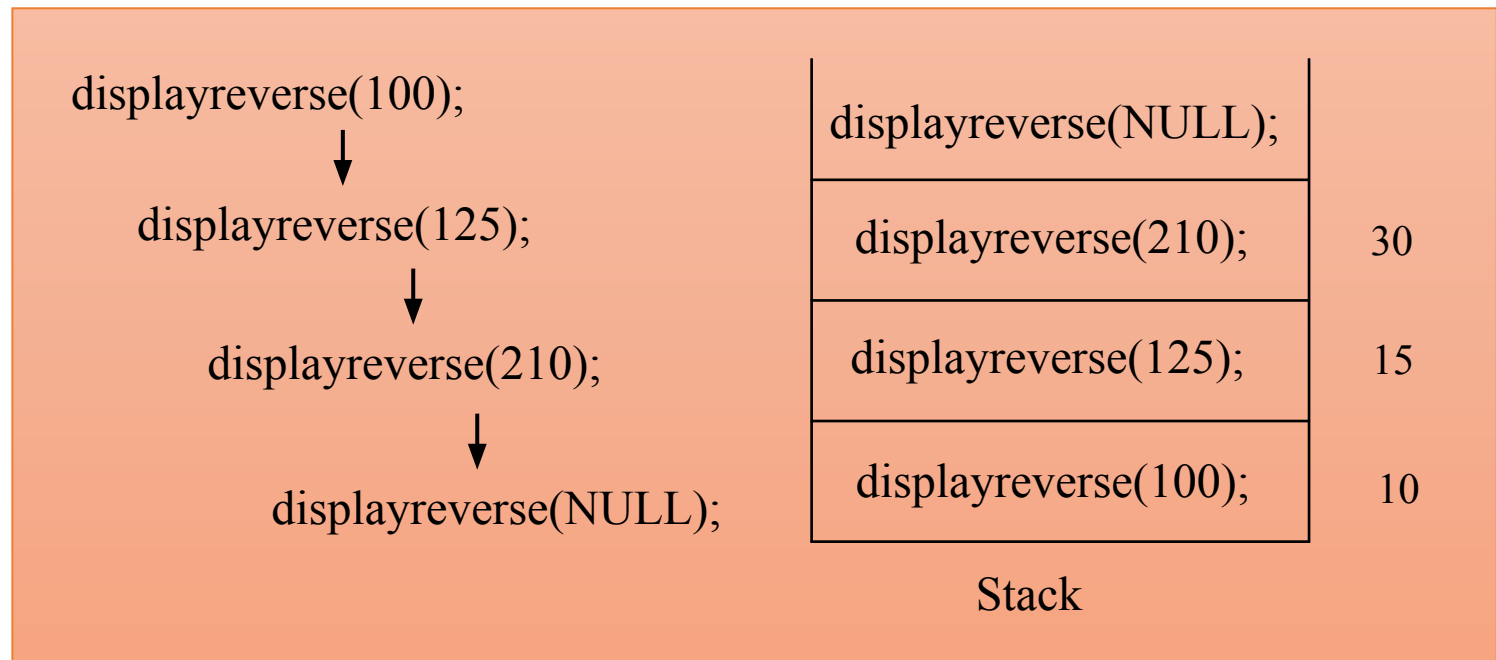
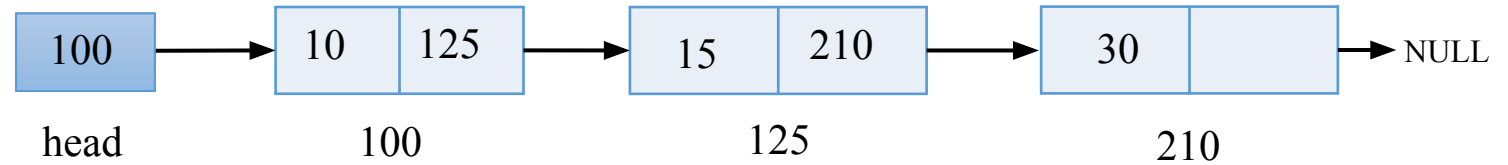


# REVERSE SINGLY LINKED LIST

There are two methods to reverse a linked list:

- Iterative Method
- Recursive method

```
void displayreverse(node *head)
{
    if(head != NULL)
    {
        displayreverse(head->next);
        printf("%d", head->data);
    }
}
```



# UPDATING SINGLY LINKED LIST

```
void updatesll(node *head, int old)
```

```
{
```

```
    node *temp;
```

```
    int dt;
```

```
    printf("Enter new data that you want to insert: ");
```

```
    scanf("%d", &dt);
```

```
    if(head == NULL)
```

```
        printf("\n Linked List is Empty !!");
```

```
    else
```

```
    {
```

```
        temp = head;
```

```
        while(temp != NULL)
```

```
        {
```

```
            if(temp->data == old);
```

```
            {
```

```
                temp->data = dt;
```

```
                break;
```

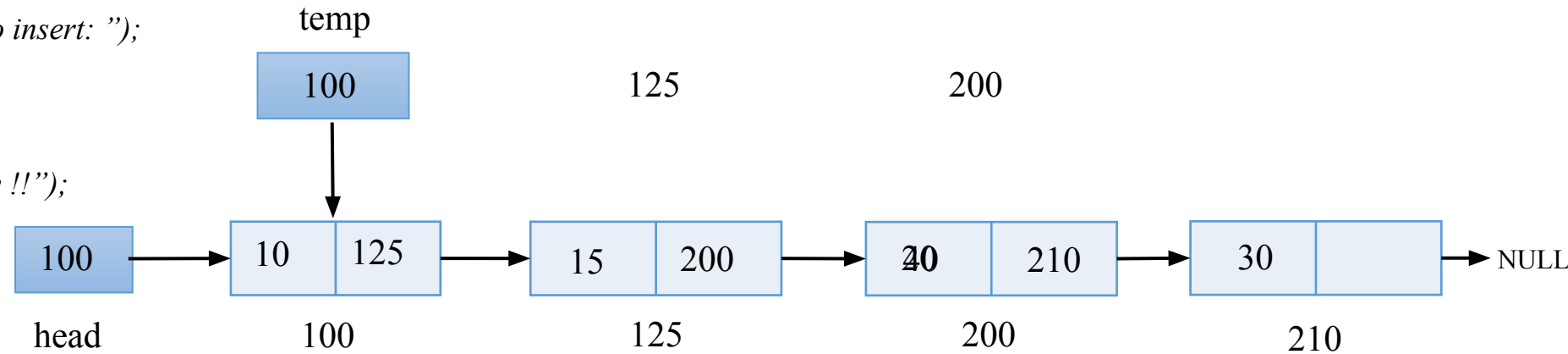
```
            }
```

```
            temp = temp->next;
```

```
        }
```

```
    }
```

```
}
```



old = 20

dt = 40



# DOUBLY LINKED LIST

- Introduction of doubly linked list
- Creation of doubly linked list
- Displaying doubly linked list
- Displaying reverse doubly linked list
- Insertion of node in doubly linked list
- Deletion of node from doubly linked list

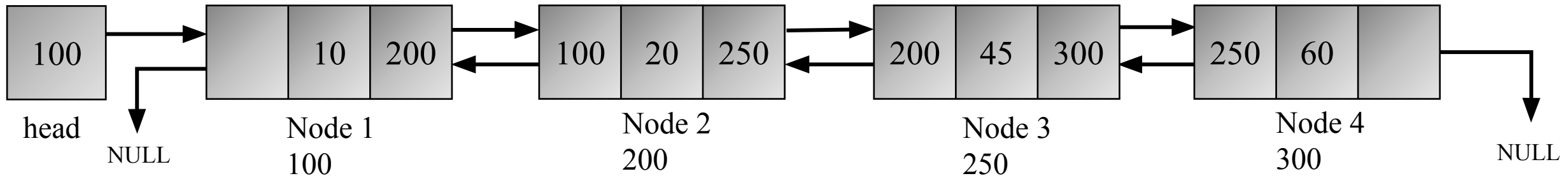
# INTRODUCTION OF DOUBLY LINKED LIST

Doubly Linked List:

Node Structure:



Example:



```
struct node
```

```
{
```

```
    int data;
```

```
    struct node *next;
```

```
    struct node *prev;
```

```
};
```

# CREATION OF DOUBLY LINKED LIST

```
node *createdll()
```

 $\{$ 

```
node *head = NULL, *temp, *newnode;
```

```
int x; char ans;
```

 $do$  $\{$ 

```
printf("Enter data to node:");
```

```
scanf("%d", &x);
```

```
newnode = (node *)malloc(sizeof(node));
```

```
newnode->data = x;
```

```
newnode->next = NULL;
```

```
newnode->prev = NULL;
```

```
if(head == NULL)
```

```
head = temp = newnode;
```

*else*

 $\{$ 

```
temp->next = newnode;
```

```
newnode->prev = temp;
```

```
temp = newnode;
```

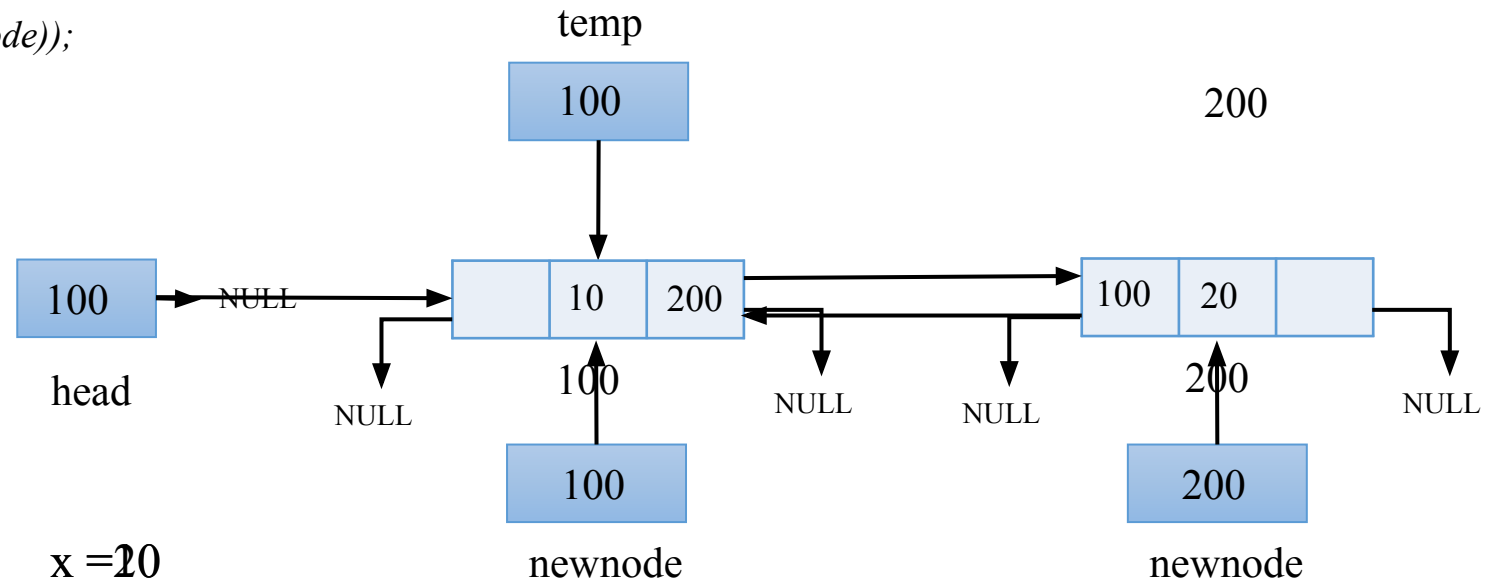
}

```
printf("Do you want to add more nodes?");
```

```
scanf("%c", &ans);
```

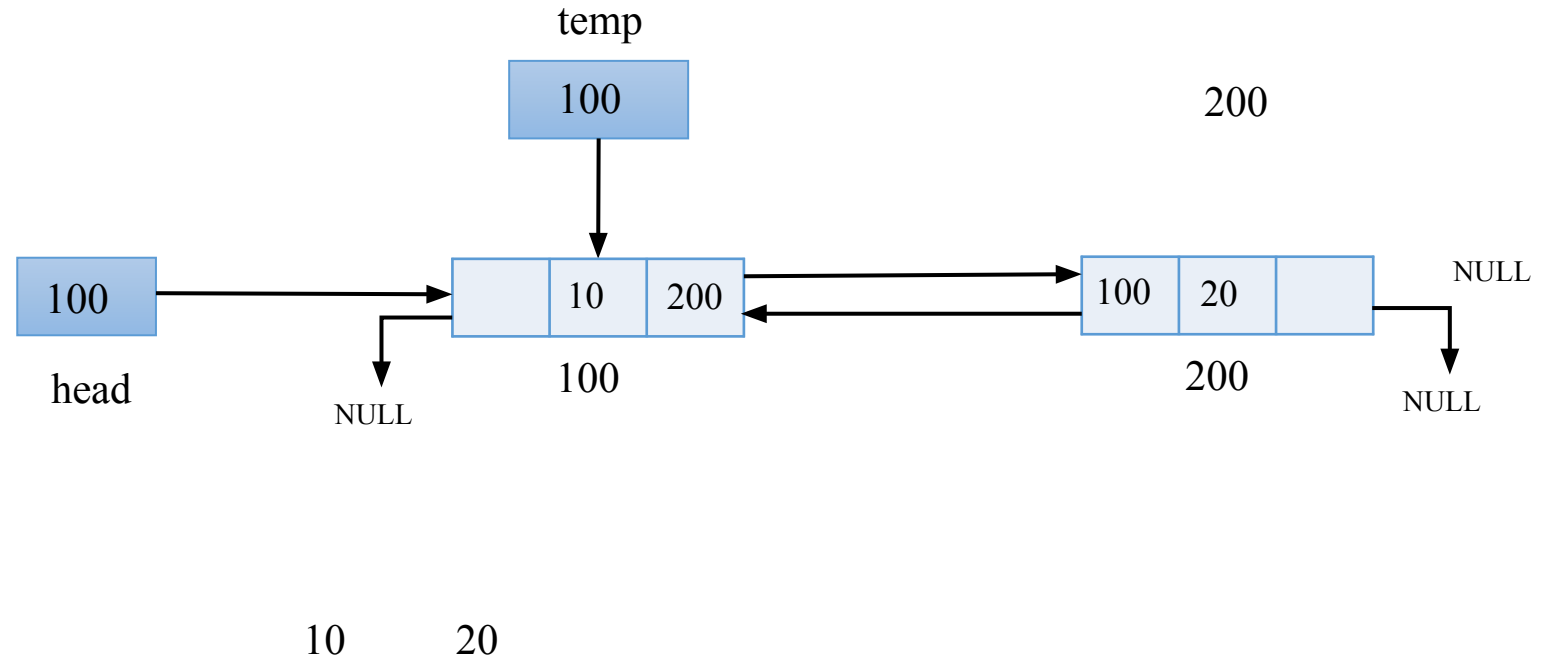
```
}while(ans == 'Y');
```

*return head;*



# DISPLAY DOUBLY LINKED LIST

```
void display(node *head)
{
    node *temp = head;
    if(temp == NULL)
        printf("List is empty");
    else
    {
        while(temp!=NULL)
        {
            printf("%d ", temp->data);
            temp = temp->next;
        }
    }
}
```





# REVERSE DISPLAY OF DOUBLY LINKED LIST

```
void displayreverse(node *head)
```

```
{
```

```
    node *temp = head;
```

```
    if(temp == NULL)
```

```
        printf("List is empty");
```

```
    else
```

```
    {
```

```
        while(temp->next != NULL)
```

```
        {
```

```
            temp = temp->next;
```

```
        }
```

```
        while(temp != NULL)
```

```
        {
```

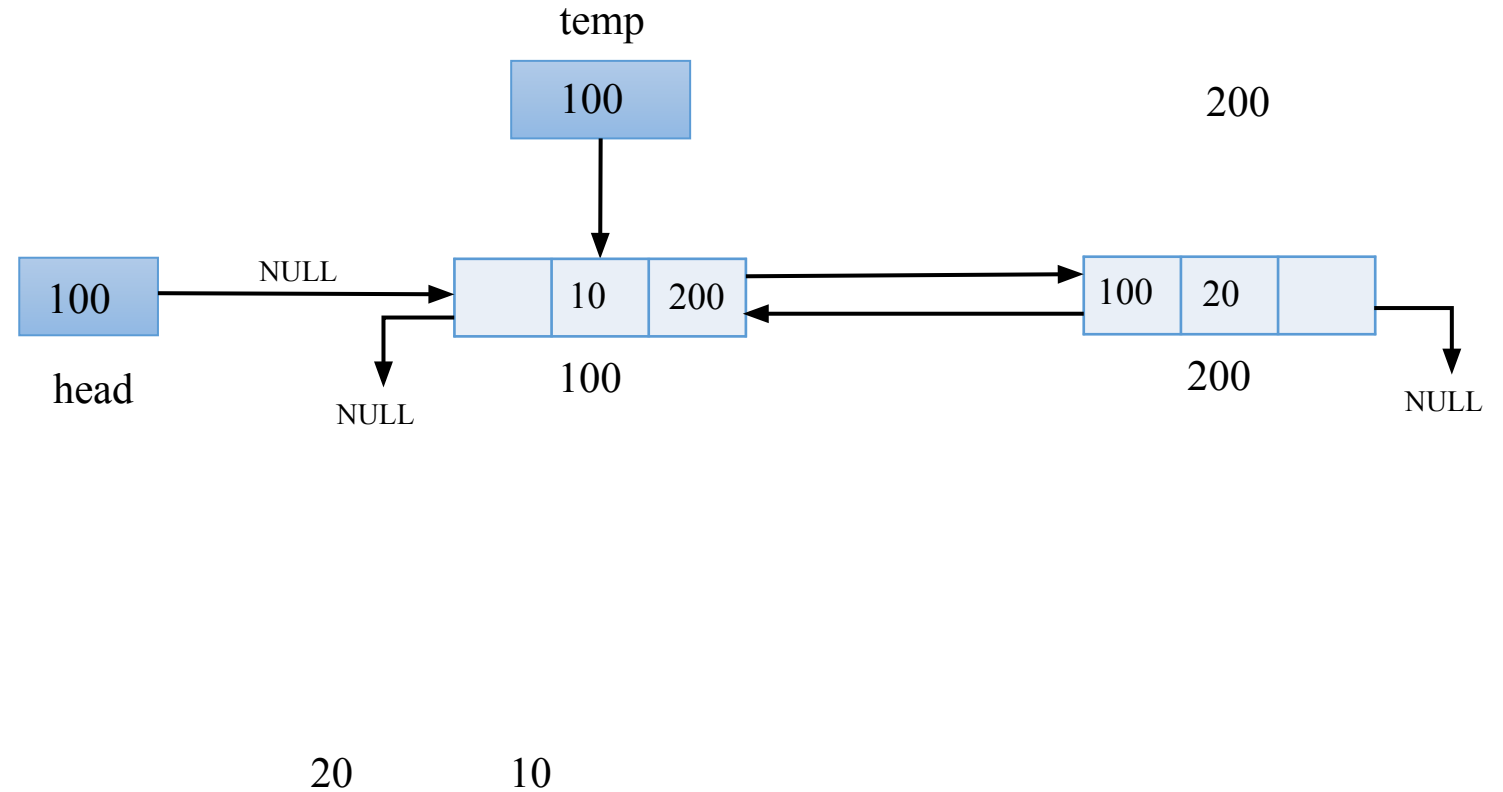
```
            printf("%d ", temp->data);
```

```
            temp = temp->prev;
```

```
        }
```

```
    }
```

```
}
```



# INSERTION OF NODE IN DOUBLY LINKED LIST

There are three ways of inserting a node in a doubly linked list –

- Insertion of a node at the beginning
- Insertion of a node in a middle
- Insertion of a node at the end

# INSERTION OF NODE IN DOUBLY LINKED LIST

## □ Insertion of a node at the beginning

```
node *insertatbeginning(node *head)
```

```
{
```

```
    node *newnode;
```

```
    int x;
```

```
    printf("Enter data to node:");
```

```
    scanf("%d", &x);
```

```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    newnode->next = NULL;
```

```
    newnode->prev = NULL;
```

```
    if(head == NULL)
```

```
    {
```

```
        head = newnode;
```

```
    }
```

```
    else
```

```
    {
```

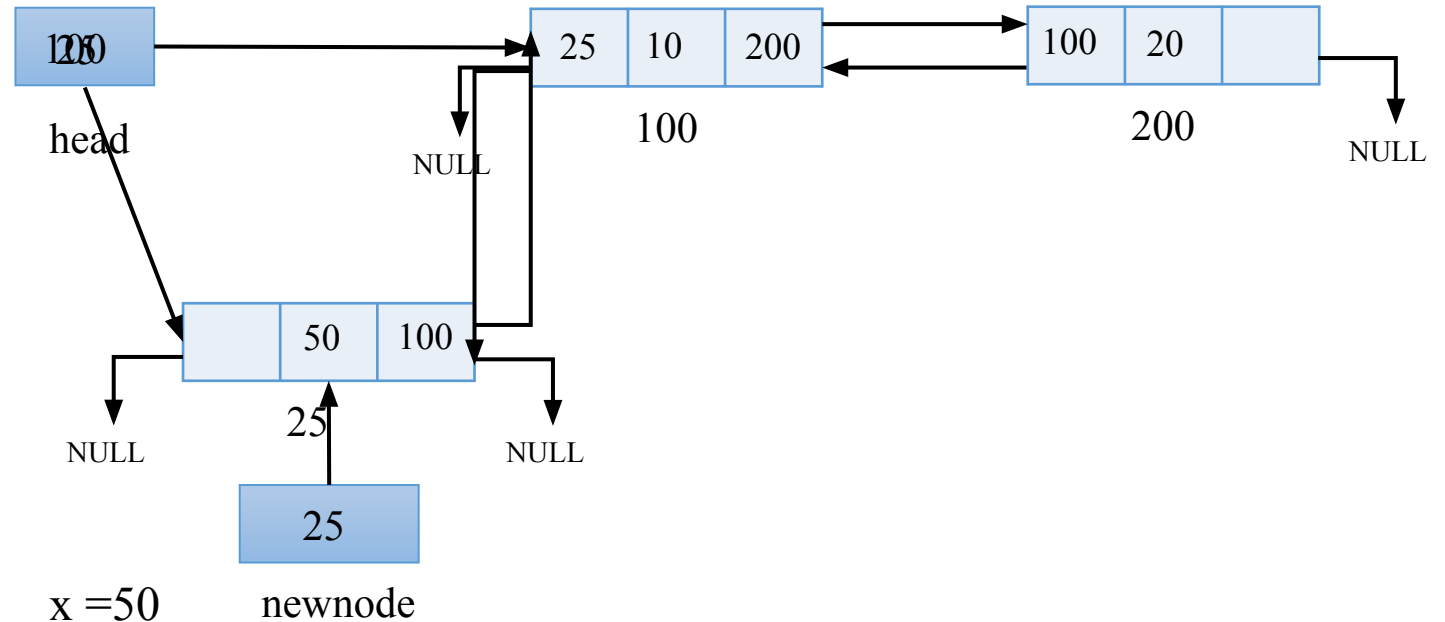
```
        newnode->next = head;
```

```
        head->prev = newnode;
```

```
        head = newnode;
```

```
    }
```

```
}
```



# INSERTION OF NODE IN DOUBLY LINKED LIST

## □ Insertion of a node in the middle

```
node *insertmiddenode(node *head, int loc)
```

```
{
```

```
    node *newnode;
```

```
    int x, i=1;
```

```
    printf("Enter data to node:");
```

```
    scanf("%d", &x);
```

```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    newnode->next = NULL;
```

```
    newnode->prev = NULL;
```

```
    temp = head;
```

```
    while(i < (loc-1))
```

```
{
```

```
        temp = temp->next;
```

```
        i++;
```

```
}
```

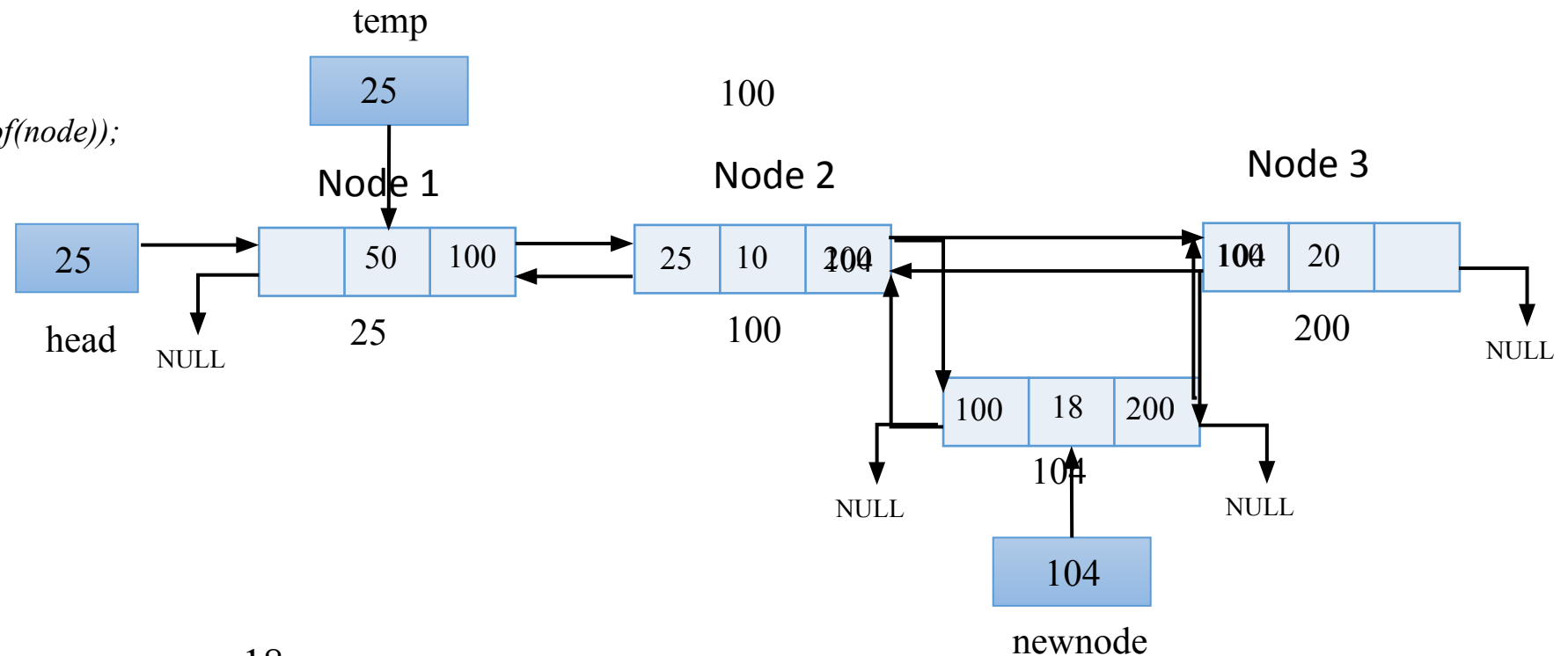
```
    newnode->next = temp->next;
```

```
    newnode->prev = temp;
```

```
    newnode->next->prev = newnode;
```

```
    temp->next = newnode;
```

```
}
```



x = 18

Loc = 3

# INSERTION OF NODE IN DOUBLY LINKED LIST

## □ Insertion of a node at the end

```
node *insertnodeatend(node *head)
```

```
{
```

```
    node *newnode;
```

```
    int x;
```

```
    printf("Enter data to node:");
```

```
    scanf("%d", &x);
```

```
    newnode = (node *)malloc(sizeof(node));
```

```
    newnode->data = x;
```

```
    newnode->next = NULL;
```

```
    newnode->prev = NULL;
```

```
    temp = head;
```

```
    if(head == NULL)
```

```
{
```

```
        head = newnode;
```

```
}
```

```
else
```

```
{
```

```
    while(temp->next != NULL);
```

```
        temp = temp->next;
```

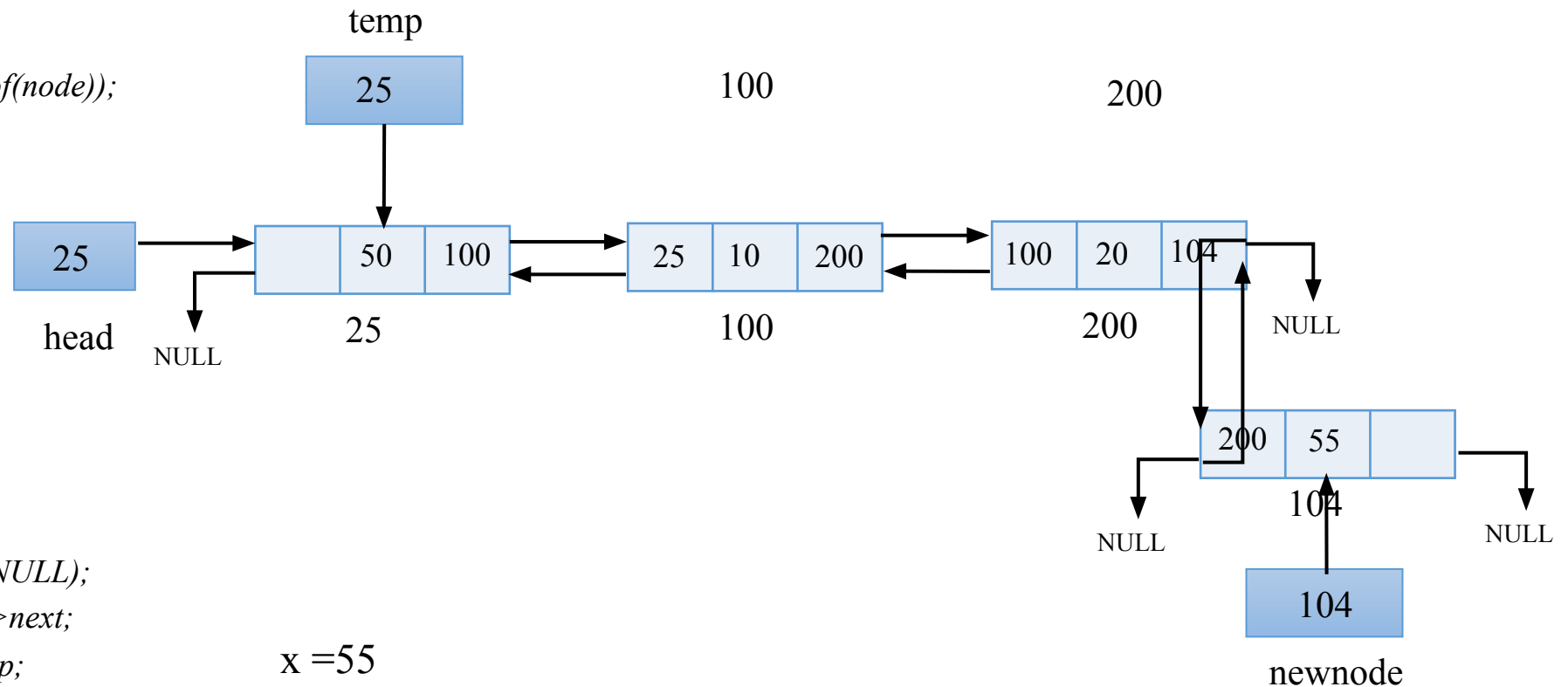
```
    newnode->prev = temp;
```

```
    newnode->next = temp->next;
```

```
    temp->next = newnode;
```

```
}
```

```
}
```



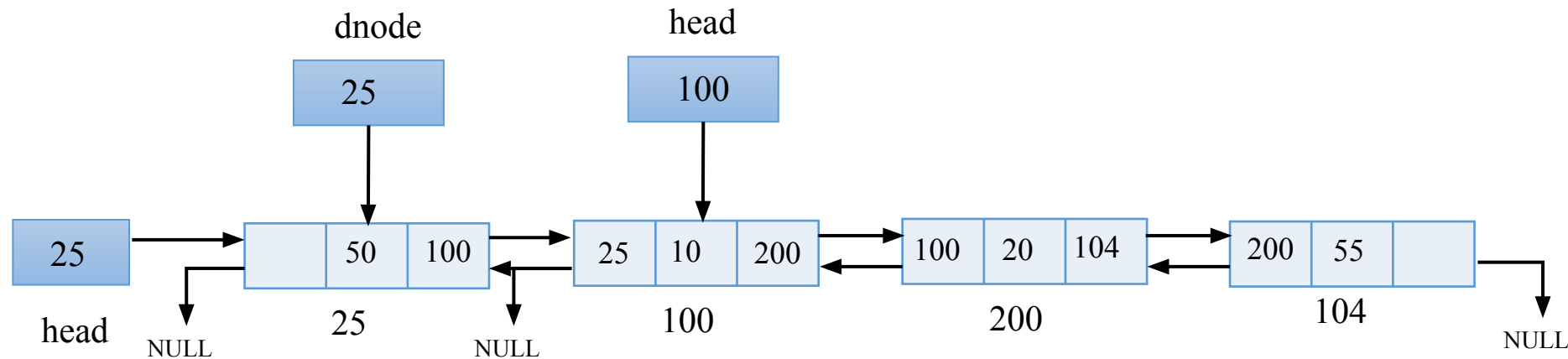
# DELETION OF NODE FROM DOUBLY LINKED LIST

There are three ways of deleting a node from a linked list –

- ❑ Delete the first node
- ❑ Delete node from middle of linked list
- ❑ Delete the last node

## ❑ Deletion of first node

```
node *deletefirstnode(node *head)
{
    node *dnode;
    dnode = head;
    head = head ->next;
    head ->prev = NULL;
    free(dnode);
    return(head);
}
```



# DELETION OF NODE FROM DOUBLY LINKED LIST

## □ Deletion of middle node

```
node *deletemiddlenode(node *head)
```

```
{
```

```
    node *temp;
```

```
    int loc, i=1;
```

```
    printf("Enter the location of the node you want to delete: ");
```

```
    scanf("%d", &loc);
```

```
    temp = head;
```

```
    while(i < (loc))
```

```
{
```

```
        temp = temp->next;
```

```
        i++;
```

```
}
```

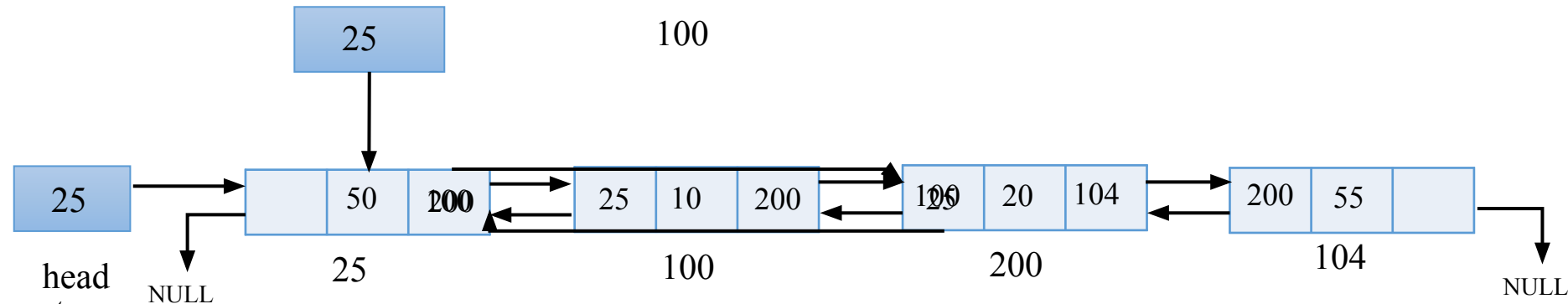
```
temp->prev->next = temp->next;
```

```
temp->next->prev = temp->prev;
```

```
free(temp);
```

```
return(head);
```

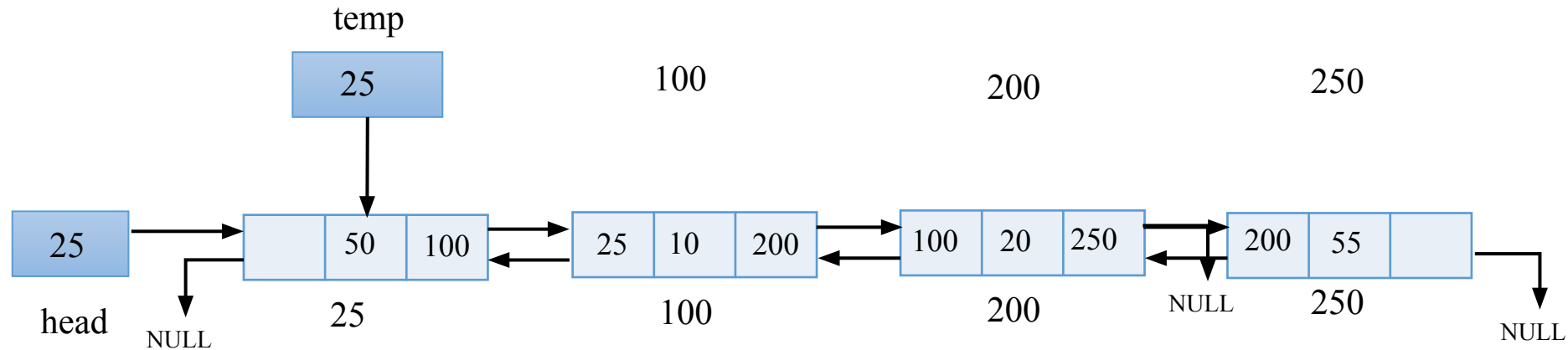
```
}
```



# DELETION OF NODE FROM DOUBLY LINKED LIST

## □ Deletion of last node

```
node *deletelastnode(node *head)
{
    node *temp;
    temp = head;
    while(temp->next != NULL)
    {
        temp = temp->next;
    }
    temp->prev->next = NULL;
    free(temp);
    return(head);
}
```







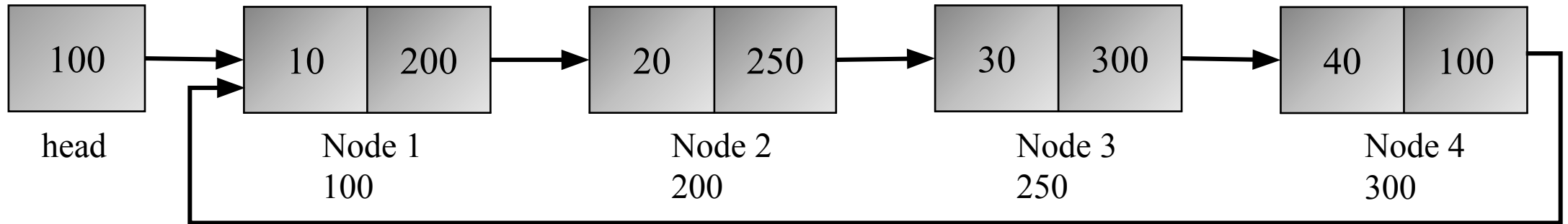
# CIRCULAR LINKED LIST

- Introduction
- Creation of circular linked list
- Insertion of node in circular linked list
- Deletion of node from circular linked list

# INTRODUCTION

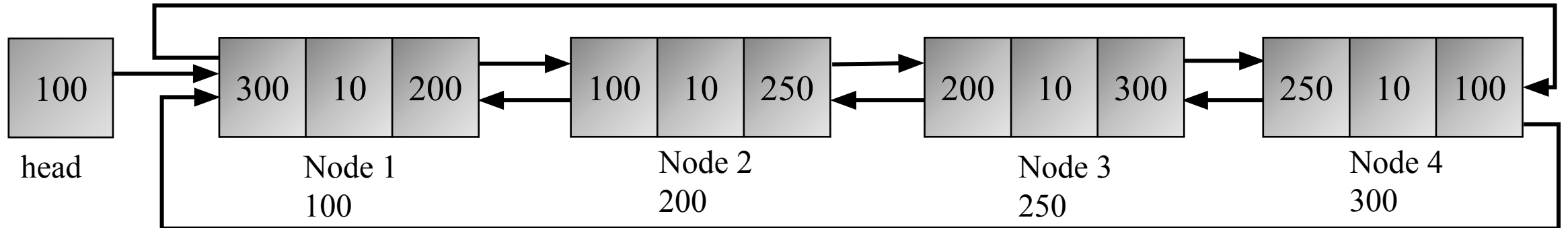
## Circular Linked List:

Example:



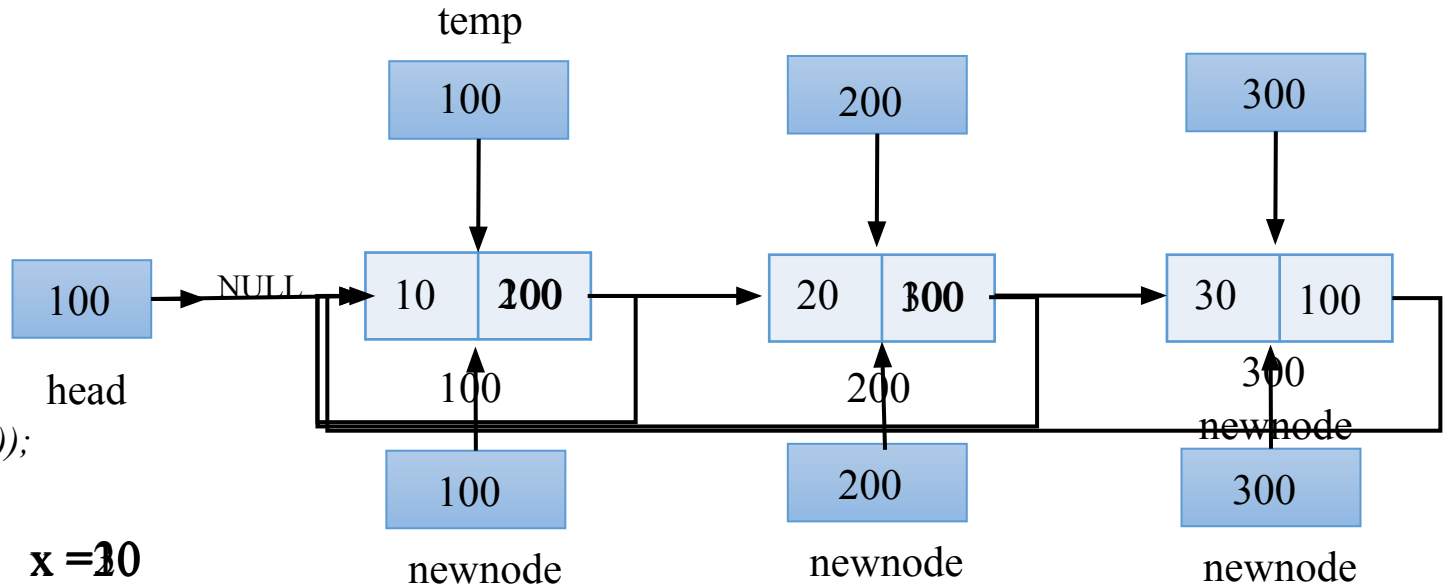
## Doubly Circular Linked List:

Example:



# CREATION OF CIRCULAR LINKED LIST

```
node *createcll()  
{  
    node *head = NULL, *temp, *newnode;  
    int x; char ans;  
    do  
    {  
        printf("Enter data to node:");  
        scanf("%d", &x);  
        newnode = (node *)malloc(sizeof(node));  
        newnode->data = x;  
        if(head == NULL)  
            head = temp = newnode;  
        else  
        {  
            temp->next = newnode;  
            temp = newnode;  
        }  
        temp->next = head;  
        printf("Do you want to add more nodes?");  
        scanf("%c", &ans);  
    }while(ans == 'Y');  
    return head;  
}
```



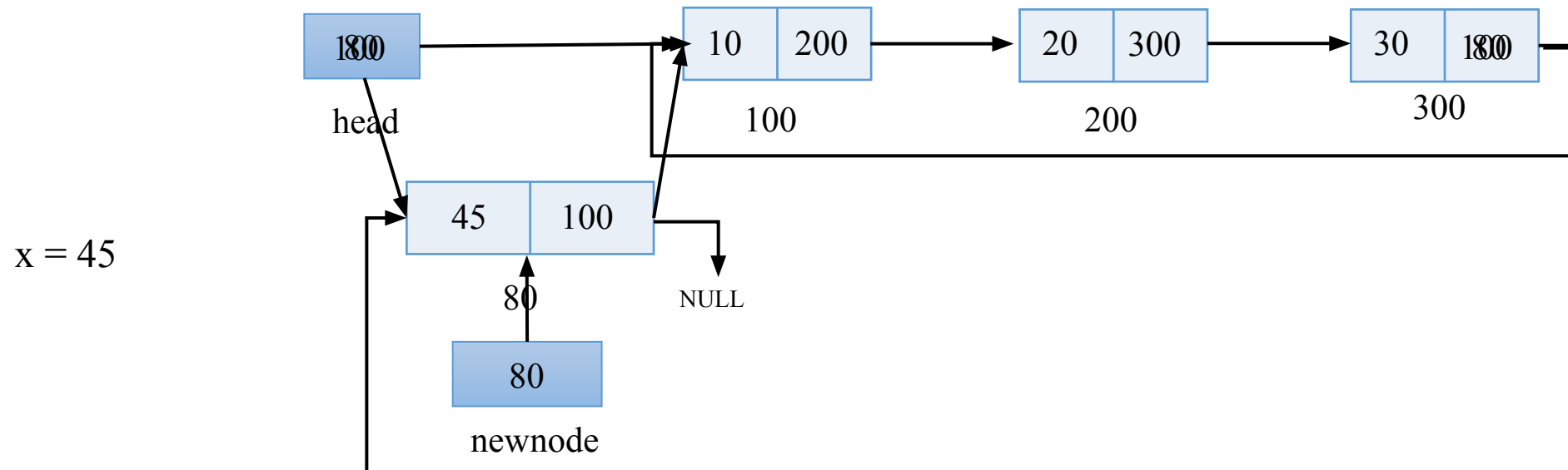
# INSERTION OF CIRCULAR LINKED LIST

There are three ways of inserting a node in a linked list –

□ Insertion of a node at the beginning

□ Insertion of a node in a middle

□ Insertion of a node at the end



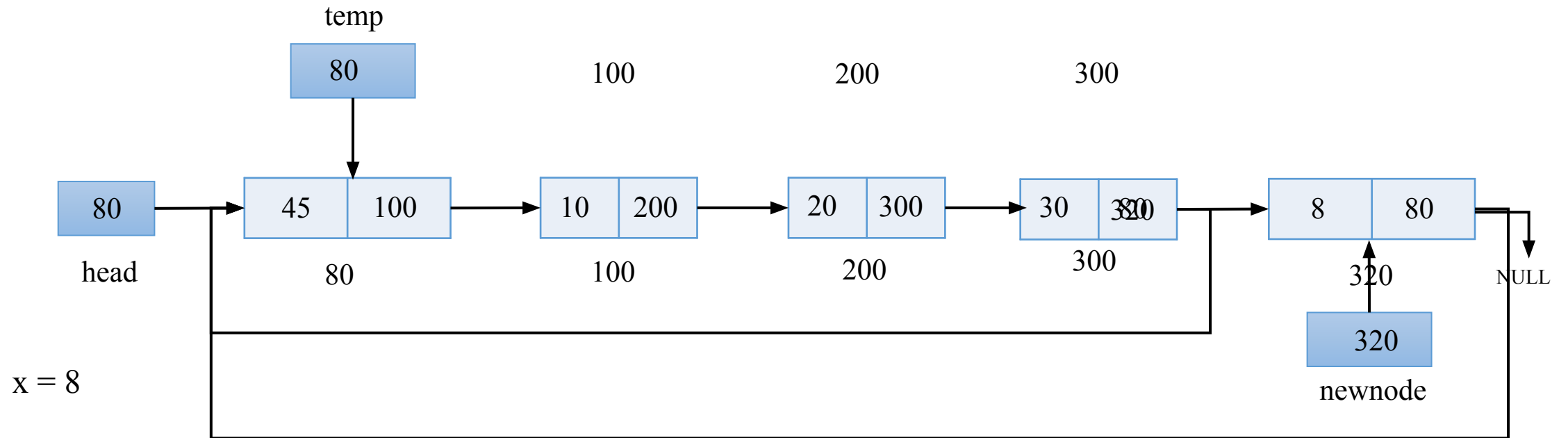
# INSERTION OF CIRCULAR LINKED LIST

There are three ways of inserting a node in a linked list –

□ Insertion of a node at the beginning

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□ Insertion of a node at the end



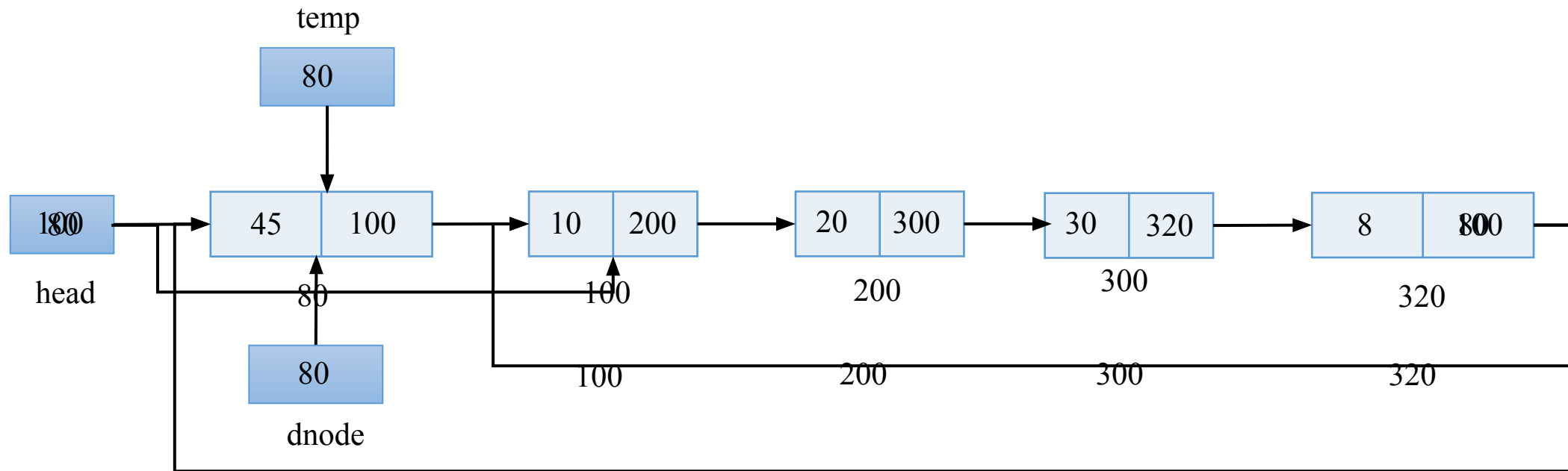
# DELETION OF CIRCULAR LINKED LIST

There are three ways of deleting a node from a linked list –

❑ Delete the first node

❑ Delete node from middle of linked list

❑ Delete the last node



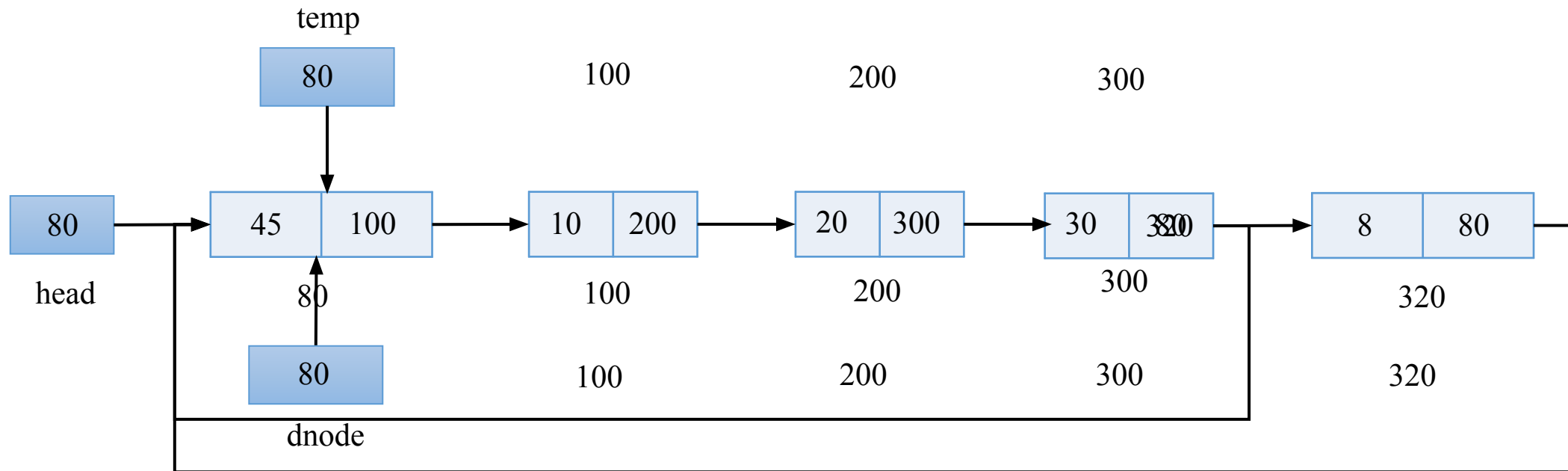
# DELETION OF CIRCULAR LINKED LIST

There are three ways of deleting a node from a linked list –

□ Delete the first node

□ Delete node from middle of linked list

□ Delete the last node



# APPLICATIONS OF LINKED LISTS

## Applications in Computer Science:

- ❖ Implementation of stacks and queues
- ❖ Implementation of graphs : Adjacency list representation of graphs is most popular which uses linked list to store adjacent vertices
- ❖ Maintaining directory of names
- ❖ Manipulation of polynomials by storing constants in the node of linked list

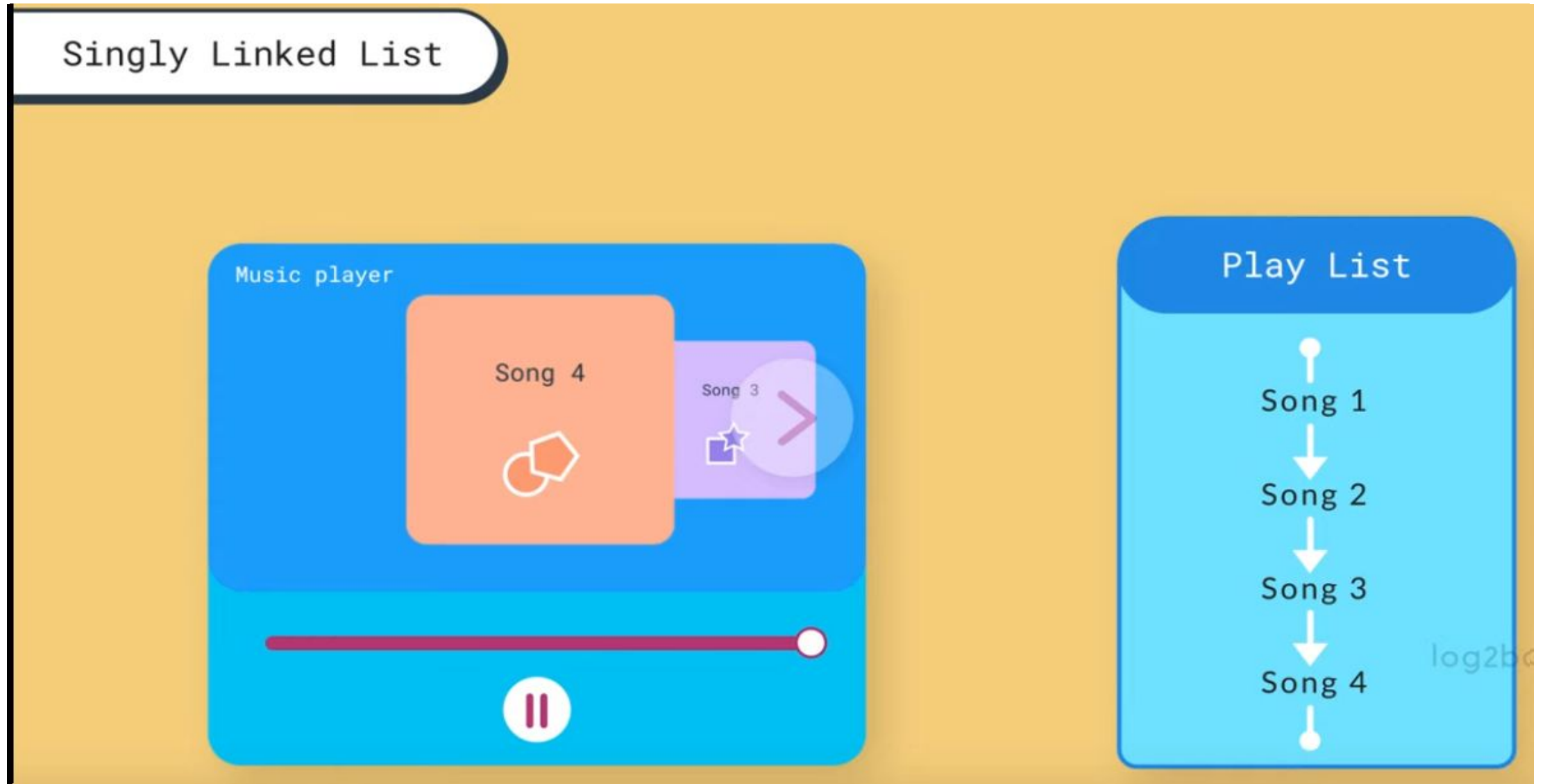
## Applications in real world:

- ❖ Image viewer – Previous and next images are linked, hence can be accessed by next and previous button
- ❖ Previous and next page in web browser – We can access previous and next url searched in web browser by pressing back and next button since, they are linked as linked list
- ❖ Music Player – Songs in music player are linked to previous and next song, you can play songs either from starting or ending of the list



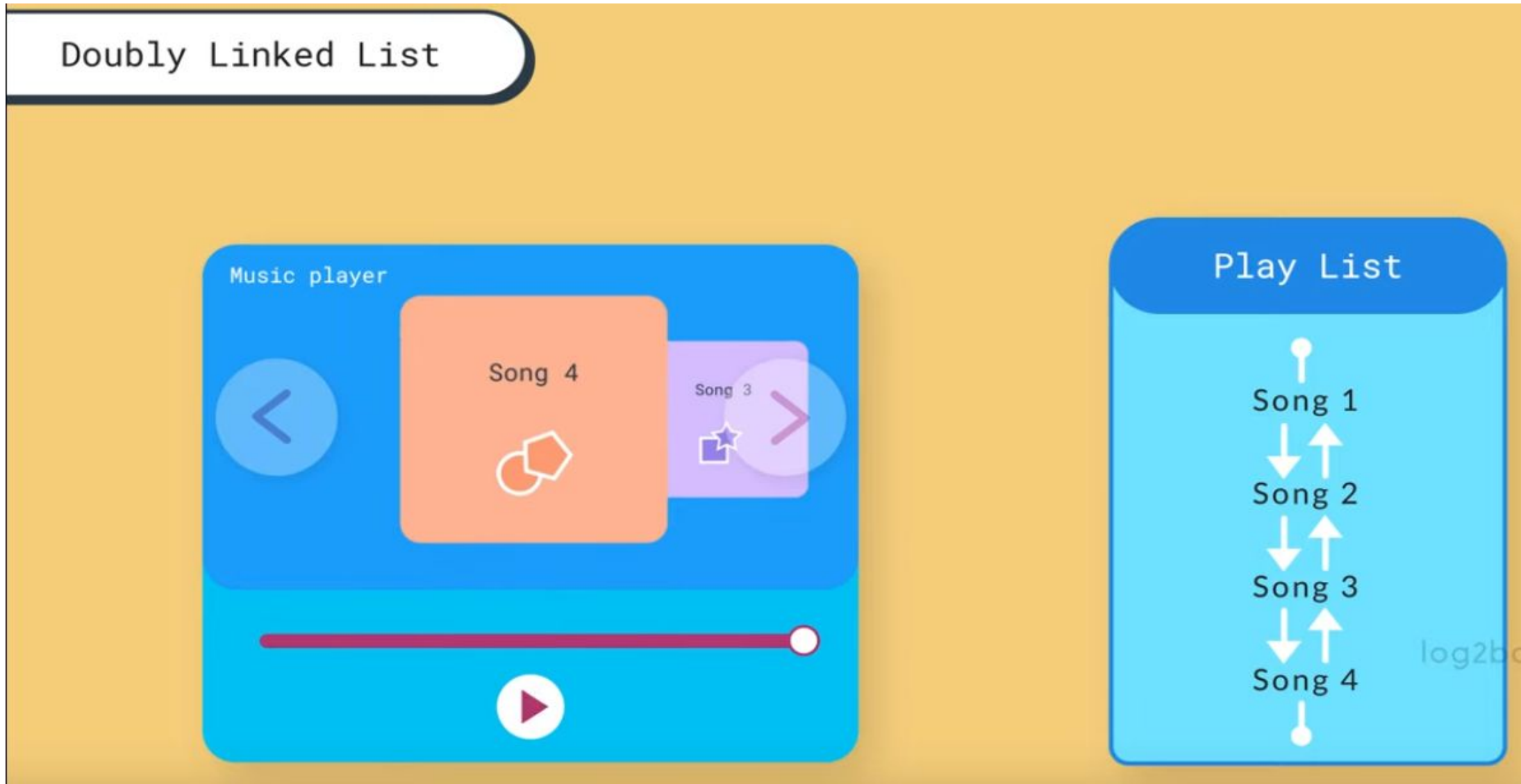
# APPLICATION OF SINGLY LINKED LISTS

## Music Player



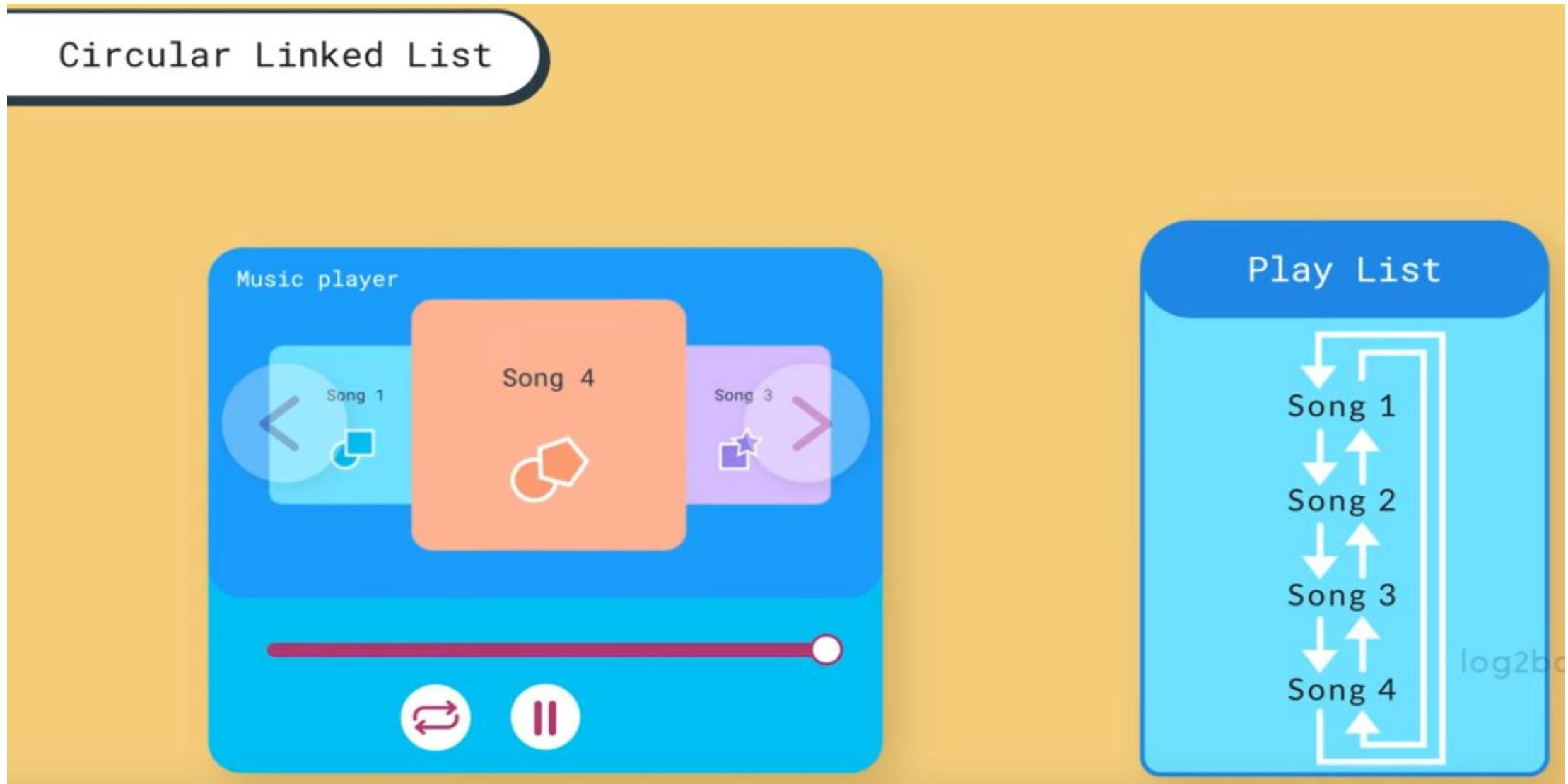
# APPLICATION OF DOUBLY LINKED LISTS

## Music Player



# APPLICATION OF CIRCULAR LINKED LISTS

## Music Player

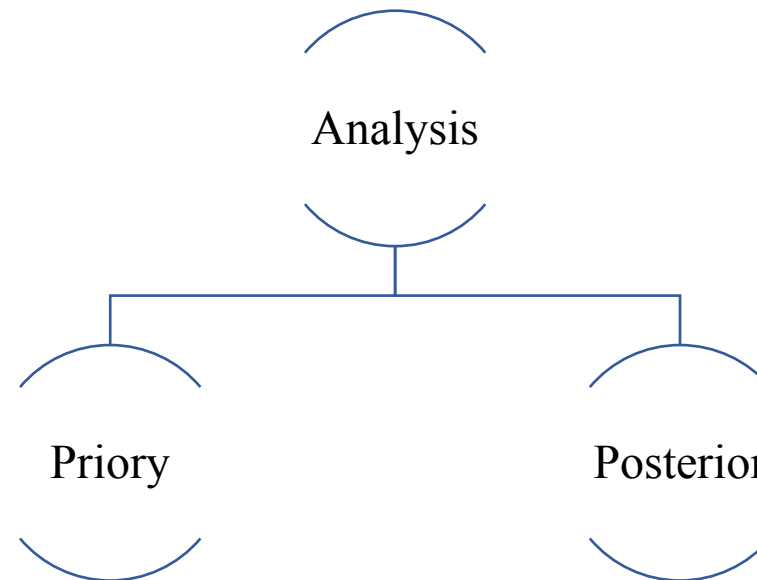


# ANALYSIS OF ALGORITHMS

The analysis of algorithm is the process of finding the computational complexity of algorithm – the amount of time, storage, or other resources needed to execute them

**Time complexity:** Running time of the program. Calculating the time required for each step

**Space Complexity:** how much space an algorithm needs to complete its task



# ANALYSIS OF ALGORITHMS

## Time Complexity:

### Asymptotic Notation:

- ❖ Mathematical way of representing the time complexity
- ❖ It is a technique of representing limiting behavior
- ❖ Asymptotic notations are used to write fastest and slowest possible running time for an algorithm

### Types of analysis -

- ❖ Worst-case:  $f(n)$  defined by the maximum number of steps taken on any instance of size  $n$

#### Big – Oh Notation ( $O$ )

- ❖ Best-case:  $f(n)$  defined by the minimum number of steps taken on any instance of size  $n$

#### Omega Notation ( $\Omega$ )

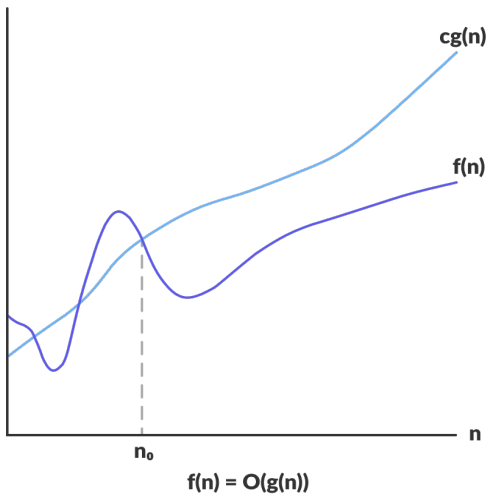
- ❖ Average case:  $f(n)$  defined by the average number of steps taken on any instance of size  $n$

#### Theta Notation ( $\theta$ )

# ANALYSIS OF ALGORITHMS

## Asymptotic Notations:

### Big – Oh Notation ( $O$ )



$$f(n) = O(g(n))$$

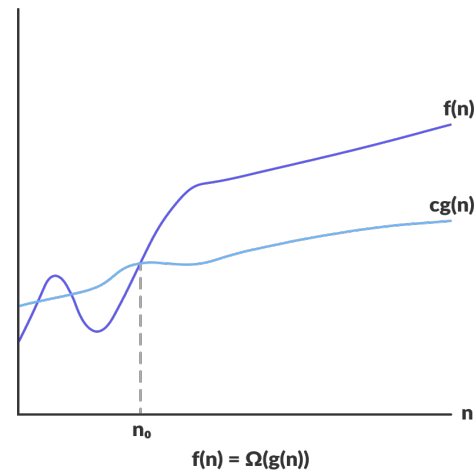
$$f(n) \leq c \cdot g(n)$$

$$\text{Example: } 2n^2 + n \leq 3n^2$$

$$n \leq n^2$$

$$\text{for all } n \geq 1$$

### Omega Notation ( $\Omega$ )



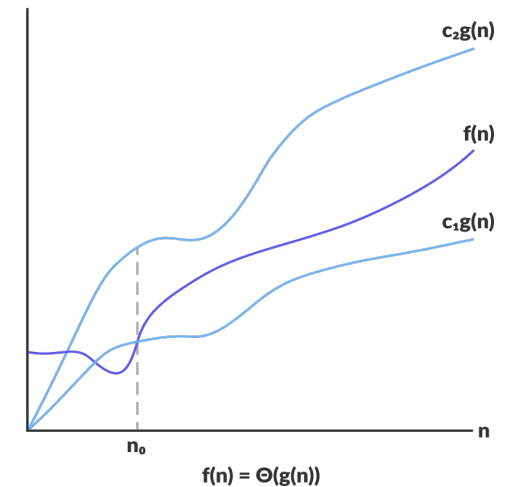
$$f(n) = \Omega(g(n))$$

$$f(n) \geq c \cdot g(n)$$

$$\text{Example: } 2n^2 + n \geq 2n^2$$

$$\text{for all } n \geq 0$$

### Theta Notation ( $\theta$ )



$$f(n) = \Theta(g(n))$$

$$c_1 \cdot g(n) \leq f(n) \leq c_2 \cdot g(n)$$

$$\text{Example: } 2n^2 \leq 2n^2 + n \leq 3n^2$$

$$\text{for all } n \geq 1$$

# ANALYSIS OF ALGORITHMS

Each instruction affects the overall performance of an algorithm

## ❖ $O(1)$ : Constant

Time complexity of a function is considered as  $O(1)$  if it doesn't contain loop, recursion and call to any other non-constant time function

## ❖ $O(n)$ : Linear

Time Complexity of a loop is considered as  $O(n)$  if the loop variables is incremented / decremented by a constant amount

## ❖ $O(n^x)$ : Quadratic / Cubic

Time complexity of nested loops is equal to the number of times the innermost statement is executed

## ❖ $O(\log n)$ : Logarithmic

Time Complexity of a loop is considered as  $O(\log n)$  if the loop variables is divided by a constant amount

## ❖ $O(n \log n)$ : Logarithmic

Time complexity of a loop is considered as  $O(n \log n)$  when a set of data is repeatedly divided into half and each half is processed again independently

# ANALYSIS OF ARRAY

Array elements are stored continuously in memory, so the time required to compute the memory address of an array element `arr[i]` is independent of the array's size: It's the *start address* of `arr` plus  $i * (\text{size of an individual element})$

Assume  $n$  elements are there in array

## Insert:

At the end (Best Case):  $O(1)$  - Just insert element at an index

At the beginning (Worst Case):  $O(n)$  - adding an element to the first location: all  $n$  elements in the array have to be shifted one place to the right before the new element can be added

In the Middle (Average Case):  $O(n)$  - Adding an element in the middle so rest of the elements need to be shifted one place to the right before the new element can be added

0	1	2	3	4
10	2	34		

Array



# ANALYSIS OF ARRAY

## Delete:

At the end (Best Case):  $O(1)$  - Just delete last element from the index

At the beginning (Worst Case):  $O(n)$  - deleting first element: all  $n$  elements in the array have to be shifted one place to the left after the first element is deleted

In the Middle (Average Case):  $O(n)$  - deleting middle element: so rest of the elements need to be shifted one place to the left after the middle element is deleted

0	1	2	3	4
10	2	34		

Array

## Access / Update:

Any element can be accessed with index so access time:  $O(1)$

Any element can be updated with index given:  $O(1)$

## Search:

For searching we need to start from first index till you find element:  $O(n)$

# ANALYSIS OF SINGLY LINKED LISTS

## Insert:

- ❖ Insertion of a node at the beginning (Best Case) :  $O(1)$
- ❖ Insertion of a node at the end (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Insertion of a node at the end :  $O(1)$
- ❖ Insertion of a node in the middle (Average Case) - Need to traverse the linked list till the position of the node :  $O(n)$

## Delete:

- ❖ Deletion of a node at the beginning (Best Case) :  $O(1)$
- ❖ Deletion of a node at the end (Worst Case) - Need to traverse the linked list till the end to find the node to be deleted:  $O(n)$
- ❖ Deletion of a node in the middle (Average Case) - Need to traverse the linked list to find the node till the position of the node :  $O(n)$

# ANALYSIS OF SINGLY LINKED LISTS

## Access:

- ❖ Accessing the First node (Best Case) :  $O(1)$
- ❖ Accessing the Last node (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Accessing the First node :  $O(1)$
- ❖ Accessing the Middle node (Average Case) - Need to traverse the linked list till the position of the node :  $O(n)$

## Search / Find:

- ❖ Find the First node (Best Case) :  $O(1)$
- ❖ Find the Last node (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Accessing the First node :  $O(1)$
- ❖ Find the Middle node (Average Case) - Need to traverse the linked list till the node :  $O(n)$

# ANALYSIS OF DOUBLY LINKED LISTS

## Insert:

- ❖ Insertion of a node at the beginning (Best Case) :  $O(1)$
- ❖ Insertion of a node at the end (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Insertion of a node at the end :  $O(1)$
- ❖ Insertion of a node in the middle (Average Case) - Need to traverse the linked list till the position of the node :  $O(n)$

## Delete:

- ❖ Deletion of a First node: (Best Case) :  $O(1)$
- ❖ Deletion of a Last node: (Worst Case) - Need to traverse the linked list till the end to find the node to be deleted:  $O(n)$   
If the tail pointer is pointing to last node then deletion of last node :  $O(1)$
- ❖ Deletion of a Middle node: (Average Case) - Need to traverse the linked list to find the node till the position of the node :  $O(n)$

# ANALYSIS OF DOUBLY LINKED LISTS

## Access:

- ❖ Accessing the First node (Best Case) :  $O(1)$
- ❖ Accessing the Last node (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Accessing the First node :  $O(1)$
- ❖ Accessing the Middle node (Average Case) - Need to traverse the linked list till the position of the node :  $O(n)$

## Search / Find:

- ❖ Find the First node (Best Case) :  $O(1)$
- ❖ Find the Last node (Worst Case) - Need to traverse the linked list till the end :  $O(n)$   
If the tail pointer is pointing to last node then Accessing the First node :  $O(1)$
- ❖ Find the Middle node (Average Case) - Need to traverse the linked list till the node :  $O(n)$