

Non-Clairvoyant Dynamic Mechanism Design: Experimental Evidence

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Main Takeaways

What do we do?

- ▶ Bring Non-Clairvoyant Environment (Mirrokni et al., 2020) into Lab.
- ▶ Test optimal Non-Clairvoyant dynamic mechanism (NC).
- ▶ Compare the performance with Repeated Static optimal mechanism (RS).

What do we find?

- ▶ Dynamic NC works well as theory predicts - more revenue.
- ▶ Participants overbid less in NC.
- ▶ Risk aversion → No full participation → Revenue loss in NC.

Optimal Dynamic Mechanism Design

- ▶ How the principal (seller) establish the rules of allocation and price over **multi-period** as the agent (buyer) receives private information over time.
 - ▶ Long-term principal-agent relationship
 - ▶ **Repeated selling of perishable goods**
- ▶ Dynamic mechanism improves revenues and efficiency (Baron & Besanko, 1984).

Non-Clairvoyance

Clairvoyance: Future demand distribution is known at the beginning.

- ▶ Form of the optimal dynamic mechanism depends on environment.
- ▶ Buyers tend to have biased forecast on future demand (DellaVigna & Malmendier, 2006).

Non-Clairvoyance: Future demand is not accessible at the beginning.

- ▶ No needs to share unbiased belief.
- ▶ General Form.



F_2 is unknown in Day 1



$v_1 \sim F_1$



$v_2 \sim F_2 ?$

Mechanisms under Non-Clairvoyant Environment

Repeated Static optimal mechanism (Myerson, 1981)

- ▶ Rules in two days are independent of each other

Maximize intra-period revenue for each period separately.

$\Rightarrow \frac{Rev_S^*}{Rev^*}$ could be arbitrarily small (Papadimitriou et al., 2016)

Non-Clairvoyant optimal dynamic mechanism (Mirrokni et al., 2020)

- ▶ Rules in Day 2 depends on bid in day 1

Best Revenue Guarantee: $\Rightarrow \frac{Rev_D^*}{Rev^*} \geq \frac{1}{a}$

Achieve at least $\frac{1}{2}$ revenue produced by optimal clairvoyant mechanism under all scenarios in two-period single-buyer case.

When can Non-Clairvoyant dynamic mechanism do better?

Theoretically, Non-Clairvoyant mechanism can not always outperform.

	Intra-period Revenue	Inter-period Revenue
Repeated Static	optimal	zero
Non-Clairvoyant Dynamic	$\frac{1}{2}$ of optimal	$\frac{1}{2}$ of optimal

Inter-period is the key.

- ▶ Good Scenario: Expected value in 2nd period is high, Myerson's revenue is low.
- ▶ Bad Scenario: Expected value in 2nd period is low.

Experimental Design $2 * 2$

Two Mechanisms

- ▶ Non-Clairvoyant Dynamic * Repeated Static

Two Scenarios

$$F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_A = 3.$$

$$F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_B = 6.$$

- ▶ S1-Good Scenario: Non-Clairvoyant Dynamic has more revenue.

$$F_1 = F_A, F_2 = F_B \Rightarrow REV^{Static} = 4, REV^{Non} = 4.5 \uparrow 12.5\%$$

- ▶ S2-Bad Scenario: Non-Clairvoyant has less revenue than Repeated Static.

$$F_1 = F_B, F_2 = F_A \Rightarrow REV^{Static} = 4, REV^{Non} = 3.5 \downarrow 12.5\%$$

Non-Clairvoyant Environment

- ▶ **Buyer:** Participant
- ▶ **Robot Seller:** Experimenter, $c = 0$
- ▶ **Two periods :** Buyer can buy one item in each period from seller, $t = 1, 2$.
- ▶ **Non-clairvoyance :** The distribution of buyer's value (F_t) is common knowledge **only in that period**
- ▶ **Incomplete Information :**
 1. Only buyer knows his value for the item in each period, v_t .
 2. Buyer's value is drawn **independently**.

Variables for Environment

- ▶ **Endowment:** $E = 50$

Institution-Static Optimal Mechanism

Period 1

- ▶ Seller sets a secret reserve price r_1 based on the distributional knowledge F_1 .
- ▶ Buyer learns his value (v_1), makes a bid : b_1
- ▶ Buyer can get the item only when $b_1 \geq r_1$ and pay $p_1 = r_1$.

Period 2

- ▶ $F_2 \Rightarrow r_2, v_2 \Rightarrow b_2$, pays $p_2 = r_2$ if $b_2 \geq r_2$

Myerson's Auction

monopoly price: $r_1 = r_2 = 2$

$$r_A = 2 \in \arg \max_r r \cdot P(v_A > r), \quad r_B = 2 \in \arg \max_r r \cdot P(v_B > r)$$

Optimal Non-Clairvoyant Dynamic Mechanism

How the dynamic mechanism work?



Half chance of free in period 1



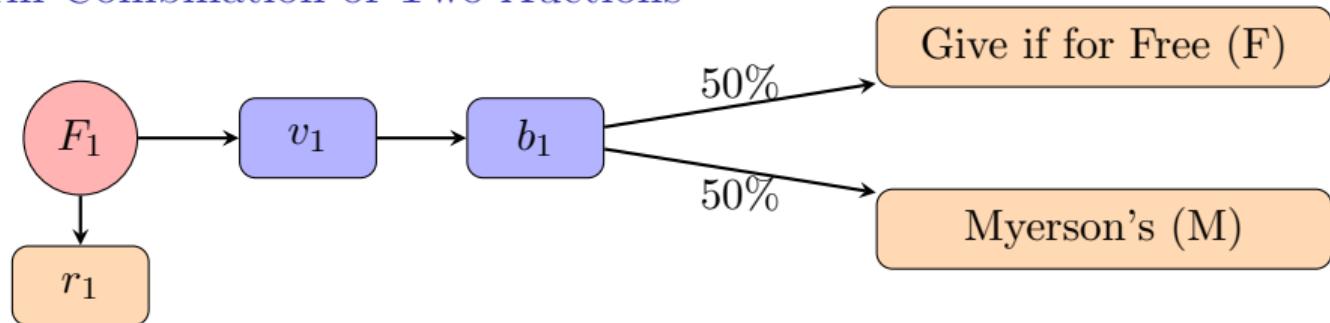
Half chance of membership fee in period 2

Non-Clairvoyant Mechanism

Period 1

- ▶ Seller sets a fixed secret reserve price r_1 based on the distribution F_1 .
- ▶ Buyer learns his value (v_1), makes a bid : b_1
- ▶ Buyer has 50% chance to get the item for free: $p_1 = 0$;
Otherwise, buyer can get the item only when $b_1 \geq r_1$ and pay $p_1 = r_1$.

Uniform Combination of Two Auctions

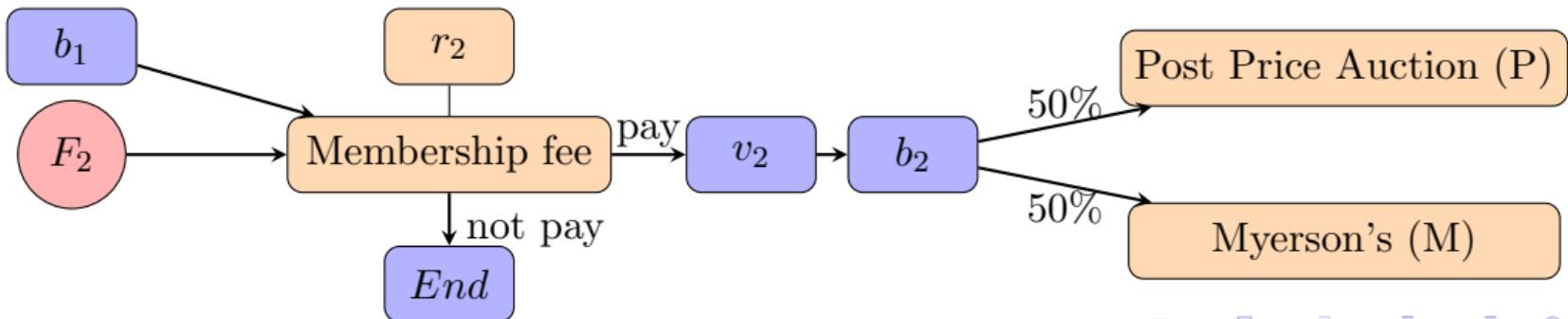


Institution-Non-Clairvoyant Mechanism

Period 2

- ▶ Seller set a membership fee $m_2 = \min(b_1, E(v_2))$.
- ▶ Buyer decides pay or leave. If buyer leave ($enter = 0$), game over.
- ▶ If buyer pays, ($enter = 1$),
 - ▶ Buyer learns his value, v_2 , and makes a bid: b_2
 - ▶ Buyer has 50% chance to redeem the membership fee ($luck = 1$).
 - ▶ Seller sets a secret reserve price r_2 based on the $F_2, m_2, luck$.
Buyer can get the item only when $b_2 \geq r_2$ and pay $p_2 = r_2$

Uniform Combination of Two Auctions



Hypotheses

Hypothesis 1 - Revenue Comparison

- ▶ In S1, Non-Clairvoyant mechanism has more revenue than repeated mechanism; has less revenue in S2.

Hypothesis 2 - Individual Rationality

- ▶ Risk-aversed buyers not paying membership fee hurts the revenue of Non-Clairvoyant mechanism.

Hypothesis 3 - Incentive Compatibility

- ▶ Randomization in NC lead participants overbid less.

Experiments

- ▶ 256 George Mason Students. September to November 2021.

Treatment	Scenario 1		Scenario 2	
	Non-Clairvoyant	Static	Non-Clairvoyant	Static
Age	21.6	22.3	21.9	22.7
Gender (Male=1)	0.48	0.44	0.52	0.47
Risk aversion	4.46	4.90	4.55	4.63
Observation	64	64	64	64

Table 1: Summary Statistic

Results

Result 1.

Experimental observations match with theoretical prediction.

- ▶ In S1, Non-Clairvoyant mechanism has more revenue than Repeated Static mechanism.
- ▶ In S2, Non-Clairvoyant mechanism has less revenue than Repeated Static mechanism.

Experimental Revenue Comparison - Period 1

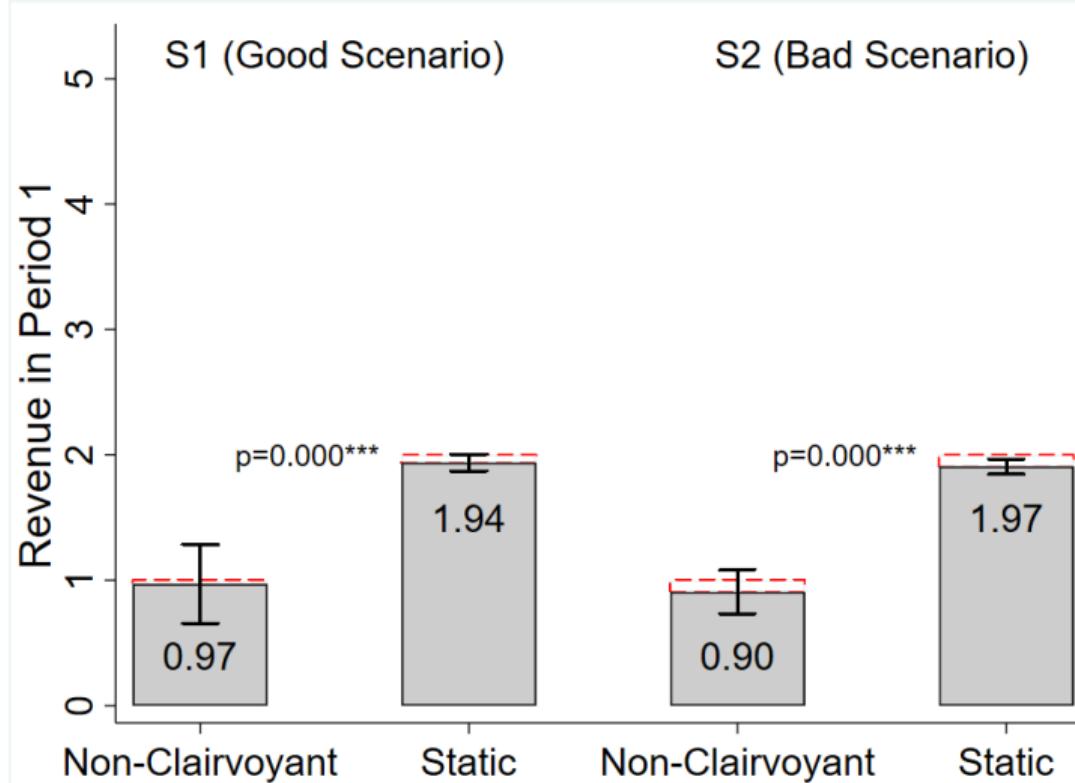


Figure 3: Revenues of Period 1 in each Treatment

Experimental Revenue Comparison - Period 2

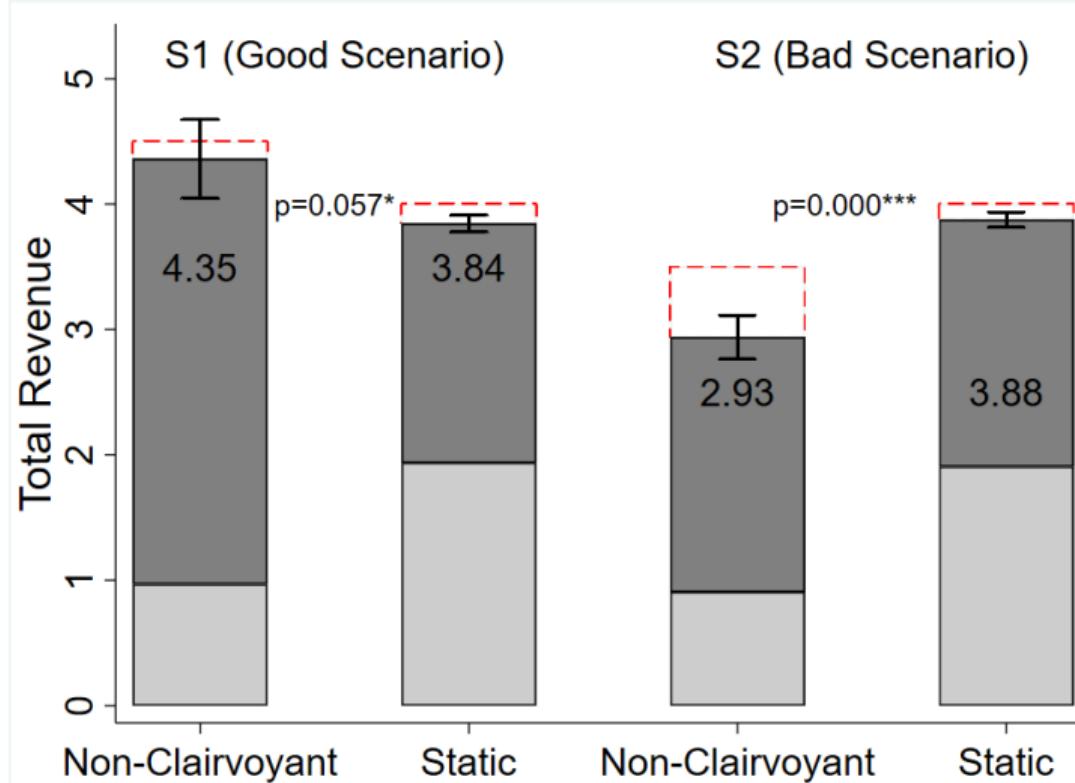


Figure 4: Revenues in each Treatment

Results

Result 2.

Risk aversion hurt the revenue of Non-Clairvoyant mechanism.

- ▶ In good scenario (S1) 4 buyers quit the second period, and the number goes to 8 in bad scenario.
- ▶ The more risk-aversed the buyer is, the more likely they will refused to pay the membership fee and quit the second period.

Revenue Loss Decomposition

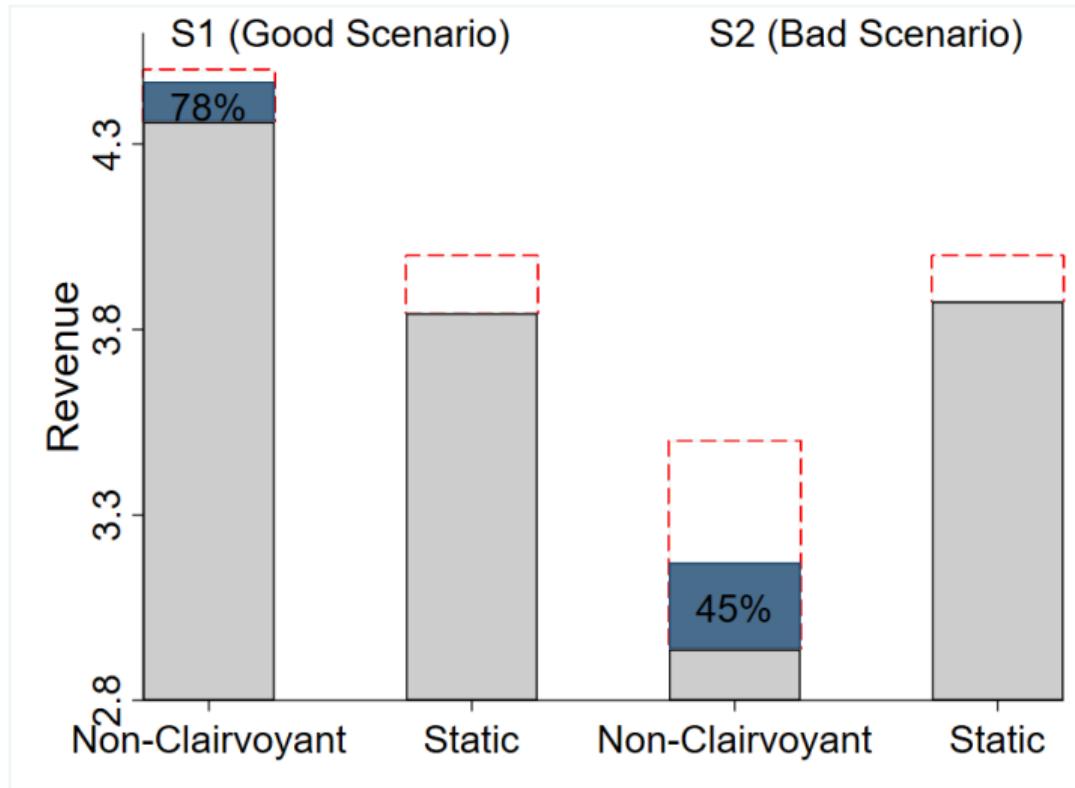


Figure 5: Revenues Increase if all Buyers enter in Period 2.

Why not pay the membership fee

- ▶ “Since I got a profit the first time I didn’t want to go again with my luck”
- ▶ “Risk vs Reward..... I got lucky and did not have to pay.”
- ▶ “Based on the membership fee. ”
- ▶ “didn’t want to take any big risks so I just lowballed my offers and refused to take the membership”
- ▶ “i read the instructions carefully. i think the second period isn’t worth losing the points - i had to pay membership fee and could only get the item by bidding higher than the price set by the seller..... honestly, i haven’t been feeling lucky so i’d rather not take my chances. so i tried not to lose money in the first period and just left it as is.”

Risk Aversion Affects Second-period Participation

	Enter in period 2 (=1)					
	S1 - Good Scenario			S2 - Bad Scenario		
	(1)	(2)	(3)	(1)	(2)	(3)
risk aversion	-0.0279* (0.0161)	-0.0281* (0.0164)	-0.0465** (0.0199)	-0.0909** (0.0437)	-0.0825* (0.0462)	-0.0938* (0.0503)
$Free_1 (= 0)$	0.044 (0.0620)	0.044 (0.0629)	0.140* (0.0707)	-0.026 (0.124)	-0.013 (0.134)	0.004 (0.146)
Membership fee	-0.028 (0.0215)	-0.003 (0.0304)	-0.020 (0.0227)	-0.243** (0.107)	-0.203* (0.109)	-0.232** (0.111)
$Value_1$	0.046 (0.0313)		0.029 (0.0342)	0.0142* (0.00799)		0.008 (0.00955)
Male (=1)	0.014 (0.0607)	0.007 (0.0613)	-0.036 (0.0681)	0.196 (0.123)	0.141 (0.124)	0.177 (0.140)
Age	-0.002 (0.0104)	-0.004 (0.0105)	0.006 (0.0122)	-0.0637*** (0.0201)	-0.0550** (0.0204)	-0.0590** (0.0220)
Graduate (=1)	-0.145 (0.0902)	-0.115 (0.0915)	-0.110 (0.103)	0.016 (0.124)	-0.010 (0.131)	-0.042 (0.155)
$Bid/Value_1$		-0.025 (0.0300)			-0.007 (0.0185)	
Constant	1.068*** (0.272)	1.139*** (0.271)	0.968*** (0.304)	2.971*** (0.651)	2.756*** (0.678)	2.907*** (0.728)

Standard errors in parentheses. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$.

Results

Result 3.

- ▶ Generally overbid.
- ▶ Buyers overbid less under Non-Clairvoyant mechanism when the distribution of their valuation has low variance.

Bid-Value Ratio Comparison

Bid/value	Non-Clairvoyant Dynamic	Repeated Static	(p-value) ¹
F1 (Low variance)	1.264 (0.04)	1.379 (0.04)	0.060*
F2 (High variance)	1.194 (0.05)	1.251 (0.04)	0.392
(p-value)	0.116	0.008***	

Table 3: Bid-Value Ratio Comparison

¹We report two-sided p-value under t-test.

Conclusions

- ▶ We find the experimental observations match with theoretical predictions on revenue comparison between mechanisms.
- ▶ Buyer's risk aversion matters in the success of Non-Clairvoyant mechanism.
- ▶ Randomization in non-clairvoyant mechanism leads buyer to overbid less.

Discussion

- ▶ Experiment on multi-buyer with more than 2 periods.
- ▶ Can participants (human sellers) set up correct rules ?

Thank you!

Reserve price (r_1, r_2) for Scenario 1

$$F_1 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_1 = 3.$$

$$F_2 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_2 = 6.$$

Period 1

- ▶ Myserson's Auction: $r_1 = 2$

Period 2

- ▶ If $luck = 1$, Myserson's Auction: $r_2 = 2$
- ▶ If $luck = 0$, Posted Price Auction: r_2 satisfies

$$E_{v_2}[(v_2 - r_2)^+] = \min(b_1, E(v_2)) = \text{membership fee}.$$

Piece-wise function: $r_2^P = 0$ if $b_1 \geq 6$, $r_2^P = 2$ if $b_1 = 4$, $r_2^P = 8$ if $b_1 = 2$, and $r_2^P = 32$ if $b_1 = 0$.

Reserve price (r_1, r_2) for Scenario 2

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_1 = 6.$$
$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_2 = 3.$$

Period 1

- Myserson's Auction: $r_1 = 2$

Period 2

- If $luck = 1$, Myserson's Auction: $r_2 = 2$
- If $luck = 0$, Posted Price Auction: r_2 satisfies

$$E_{v_2}[(v_2 - r_2)^+] = \min(b_1, E(v_2)) = \text{membership fee}.$$

Piece-wise function: $r_2^P = 0$ if $b_1 \geq 3$, $r_2^P = 1$ if $b_1 = 2$ and $r_2^P = 4$ if $b_1 = 0$.

Mechanism Comparison for Scenario 1

$$F_1 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\} \quad \mathbb{E}_1 = 3.$$

$$F_2 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \quad \mathbb{E} = 6.$$

- ▶ Non-Clairvoyant Mechanism increases revenue, $\uparrow 12.5\%$

E1-Revenue	Non-clairvoyant Dynamic	Repeated Static		
Period 1	Give for Free (F)	0	Myerson's Auction (M)	2
	Myerson's Auction (M)	2		
Period 2	Post Price Auction (P)	5	Myerson's Auction (M)	2
	Myerson's Auction (M)	2		
Total		4.5		4

Table 4: Theoretical Revenues in Scenario 1.

Mechanism Comparison for Scenario 2

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_1 = 6.$$
$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_2 = 3.$$

- ▶ Non-Clairvoyant Mechanism decreases revenue, $\downarrow 12.5\%$

E1-Revenue	Non-clairvoyant Dynamic	Repeated Static		
Period 1	Give for Free (F)	0	Myerson's Auction (M)	2
	Myerson's Auction (M)	2		
Period 2	Post Price Auction (P)	3	Myerson's Auction (M)	2
	Myerson's Auction (M)	2		
Total		3.5		4

Table 5: Theoretical Revenues in Scenario 2.

Experimental Revenue Decomposition in S1

E1 Revenue	Non-clairvoyant Theory	Dynamic Experiment	Repeated Theory	Static Experiment
Period 1	Give it for free	0	0	
	Myerson's auction	2	1.94(0.06)	Myerson's 2 1.94(0.04)
Period 2	Post Price Auction	5	4.84(0.47)	Myerson's 2 1.91(0.05)
	Myerson's auction	2	1.94(0.06)	
Total		5	4.35(0.32)	4 3.84(0.07)

Table 6: Revenue decomposition under E1 (Good Environment)

Experimental Revenue Decomposition in S2

E2 Revenue	Non-clairvoyant Theory	Dynamic Experiment	Repeated Theory	Static Experiment
Period 1	Give it for free	0	0	
	Myerson's auction	2	1.93(0.06)	Myerson's 2 1.91(0.05)
Period 2	Post Price Auction	3	2.25(0.21)	Myerson's 2 1.97(0.03)
	Myerson's auction	2	1.75(0.12)	
Total		3.5	2.91 (0.18)	4 3.88 (0.06)

Table 7: Revenue decomposition in S2 (Bad Scenario)