

## 1. Conceptes bàsics

1.

$$\frac{3x^2y^3}{6xy^2}$$

2.

$$2x - 5 = 9$$

3.

$$0.000345$$

4.

$$120^\circ \text{ to radians}$$

## 2. Límits. Funcions contínues

1.

$$\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$$

2.

$$f(x) = \frac{x^2 - 1}{x - 1}$$

3.

$$f(x) = |x| \text{ at } x = 0$$

## 3. La derivada

1.

$$f'(x) \text{ for } f(x) = 3x^3 - 5x + 2$$

2.

$$y = e^{2x} \cdot \sin(x)$$

3.

Derivative as velocity interpretation

## 4. Optimització

1.

Two numbers sum to 20, product max

2.

Rectangle with perimeter 100m, max area

3.

$$y = \sqrt{x} \text{ closest to } (4, 0)$$

## 5. La integral per a funcions d'una variable

1.

$$\int (3x^2 - 4x + 1) dx$$

2.

$$\int e^{2x} dx$$

## 6. La integral definida

1.

$$\int_0^2 x^2 dx$$

2.

$$\int_1^3 v(t) dt \text{ as displacement}$$

## 7. Equacions diferencials ordinàries de primer ordre

1.

$$\frac{dy}{dx} = 3y, \quad y(0) = 2$$

2.

$$\frac{dy}{dx} + y = e^x$$

## 8. Algunes equacions diferencials de la biologia i el medi ambient

1.

$$\frac{dP}{dt} = 0.2P \left( 1 - \frac{P}{1000} \right)$$

2.

$$\frac{dN}{dt} = -\lambda N$$

**Note:** Attempt without reference, then check solutions.