Deep R Programming

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Any bug reports/corrections/feature requests are welcome. To make this textbook even better, please file them at https://github.com/gagolews/deepr.

Typeset with Xe M_E X. Please be understanding: it was an algorithmic process. Hence, the results are \in [good enough, perfect).

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Deep R Programming by Marek Gagolewski¹ is a **comprehensive and in-depth introductory course** on one of the most popular languages for data science. It equips ambitious students, professionals, and researchers with the **knowledge and skills to become independent users** of this potent environment so that they can **tackle any problem** related to data wrangling and analytics, numerical computing, statistics, and machine learning.

For many students around the world, educational resources are hardly affordable. Therefore, I have decided that this book should **remain an independent, non-profit, open-access project** (available both in PDF² and HTML³ forms). Whilst, for some people, the presence of a "designer tag" from a major publisher might still be a proxy for quality, it is my hope that this publication will prove useful to those seeking knowledge for knowledge's sake.

Please spread the news about it by sharing the above URLs with your mates, peers, or students. Any bug/typo reports/fixes are appreciated. Please submit them via this project's GitHub repository⁴. Thank you.

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Make sure to check out my other open-access book, Minimalist Data Wrangling with Python⁶ [26].

¹ https://www.gagolewski.com/

² https://deepr.gagolewski.com/deepr.pdf

³ https://deepr.gagolewski.com/

⁴ https://github.com/gagolews/deepr/issues

⁵ https://dx.doi.org/10.5281/zenodo.7490464

⁶ https://datawranglingpy.gagolewski.com/

Preface

0.1 To R, or not to R

R has been named the eleventh most dreaded programming language in the 2022 StackOverflow Developer Survey⁷.

Also, it is a free app, so there must be something wrong with it, right?

But whatever, R is deprecated anyway; the modern way is to use tidyverse.

Or we should all just switch to Python⁸.

Yeah, nah.

0.2 R (GNU S) as a language and an environment

Let us get one⁹ thing straight: R is *not* just a *statistical package*. It is a general-purpose, high-level programming language that happens to be very powerful for numerical, data-intense computing activities of any kind. It offers extensive support for statistical, machine learning, data analysis, data wrangling, and data visualisation applications, but there is much more.

As we detail below, R has a long history. It is an open-source version of the S environment, which was written for statisticians, by statisticians. Therefore, it is a free, yet often more capable alternative to other software (but without any strings attached). Unlike in some of them, in R, a spreadsheet-like GUI is not the main gateway for performing computations on data. Here, we must *write code* to get things done. Despite the beginning of the learning curve's being a little steeper for non-programmers, in the long run, R empowers us more because we are not limited to tackling the most common scenarios. If some functionality is missing or does not suit our needs, we can easily (re)implement it ourselves.

⁷ https://survey.stackoverflow.co/2022

⁸ https://datawranglingpy.gagolewski.com/

⁹ Also, we must not confuse RStudio with R. The former is merely one of many development environments for our language. We program in R, not in RStudio.

R is thus very convenient for rapid prototyping. It helps turn our ideas into fully operational code that can be battle-tested, extended, polished, run in production, and otherwise enjoyed. As an interpreted language, it can not only be executed in an interactive read-eval-print loop (command-result, question-answer, ...), but also in batch mode (running standalone scripts).

Therefore, we would rather position R amongst the tools/languages for numerical or scientific computing such as Python with the **numpy** ecosystem, Julia, GNU Octave, Scilab, MATLAB, etc. However, it is more *specialised* in data science applications than all of them. Hence, it provides a much smoother experience. This is why, over the years, R has become the de facto standard in statistics and related fields.

Important R is a whole ecosystem (environment). Apart from the R language interpreter, it features advanced:

- graphics capabilities (see Chapter 13),
- a consistent, well-integrated help system (Section 1.4),
- ways for convenient interfacing with compiled code (Chapter 14),
- a package system and centralised package repositories (such as CRAN and Bioconductor; Section 7.3.1),
- a lively community of users and developers curious and passionate people, like you and yours cordially.

Note R [68] is a dialect of the very popular S system designed in the mid-1970s by Rick A. Becker, John M. Chambers, and Allan R. Wilks at Bell Labs; see [3, 4, 5, 6] and its later revisions [7, 9, 13, 56]. Quoting from [4]:

The design goal for S is, most broadly stated, to enable and encourage good data analysis, that is, to provide users with specific facilities and a general environment that helps them quickly and conveniently look at many displays, summaries, and models for their data, and to follow the kind of iterative, exploratory path that most often leads to a thorough analysis. The system is designed for interactive use with simple but general expressions for the user to type, and immediate, informative feedback from the system, including graphic output on any of a variety of graphical devices.

S became popular because it offered greater flexibility than the standalone statistical packages. It was praised for its high interactivity and array-centrism that was known

from APL, the familiar syntax of the C language that involves the use of {curly braces}, the ability to treat code as data known from Lisp (Chapter 15), the notion of lazy arguments (Chapter 17), and the ease of calling external C and Fortran routines (Chapter 14). Its newer versions were also somewhat object-orientated (Chapter 10).

However, S was a proprietary, and closed-source system. To address this, Robert Gentleman and Ross Ihaka of the Statistics Department, University of Auckland developed R in the 1990s¹⁰. They were later joined by many contributors¹¹. It has been decided that it will be distributed under the terms of the free GNU General Public License, version 2.

In essence, R was supposed to be backwards-compatible with S, but some design choices led to their evaluation models' being slightly different. In Chapter 16, we discuss that R's design was inspired by the Scheme language [1].

0.3 Aims, scope, and design philosophy

Many users were introduced to R by means of some very advanced operations involving data frames, formulae, and functions that rely on nonstandard evaluation (metaprogramming), like:

```
lm(
    Ozone~Solar.R+Temp,
    data=subset(airquality, Temp>60, select=-(Month:Day))
) |> summary()
```

This is horrible.

Another cohort was isolated from base R through a thick layer of popular third-party packages that introduce an overwhelming number of functions (every operation, regardless of its complexity, has a unique name). They often duplicate the core functionality, and might not be fully compatible with our traditional system.

Both user families ought to be fine, as long as they limit themselves to solving only the most common data processing problems.

But we yearn for more. We do not want hundreds of prefabricated *recipes* for popular dishes that we can mindlessly apply without much understanding.

Our aim is to learn the fundamentals of base R, which constitutes the ligua franca for

¹⁰ See [12, 37] for historical notes. R version 0.49 released in April 1997 (the first whose source code is available on CRAN; see https://cloud.r-project.org/src/base/R-0), was already quite feature-rich. In particular, it implemented S3 methods, formulae, and data frames that were introduced in the 1991 version of S [13].

¹¹ The beauty of the employed open-source model is that all the contributors are real human beings, not anonymous contractors working for soulless corporations; see https://www.r-project.org/contributors.html.

all R users. We want to be able to indite code that everybody *should* understand; code that will work without modifications ten years from now (no slang!).

We want to be able to tackle *any* data-intense problem. Furthermore, we want to develop *transferable* skills so that learning new tools such as Python with **numpy** and **pandas** (e.g., [26, 47]) or Julia will be much easier later. After all, R is not the only notable environment out there.

Anyway, enough preaching. This graduate¹²-level textbook is for readers who:

- would like to experience the *joy* of solving problems by programming,
- want to become independent users of the R environment,
- can appreciate a more cohesively and comprehensively¹³ organised material,
- · do not mind a slightly steeper learning curve at the beginning,
- do not want to be made obsolete by artificial "intelligence" in the future.

Some readers will benefit from its being their first introduction to R (yet, without all the pampering). For others¹⁴, this will be a fine course from intermediate to advanced (do not skip the first chapters, though).

Either way, we should not forget to solve *all* the prescribed exercises.

Good luck!

0.4 Classification of R data types and book structure

The most commonly used R data types can be classified as follows; see also Figure 1.

- 1. *Basic types* are discussed in the first part of the book:
 - *atomic vectors* represent whole sequences of values, where every element is of the same type:
 - logical (Chapter 3) includes items that are TRUE ("yes", "present"), FALSE ("no", "absent"), or NA ("not available", "missing");

 $^{^{12}}$ The author taught similar courses for his wonderfully ambitious undergraduate data/computer science and mathematics students at the Warsaw University of Technology, where our approach has proven not difficult whatsoever.

¹³ Yours truly has chosen to be neither a historian, a stenographer, nor a grammarian. Thus, he made a few noninvasive idealisations for didactic purposes. Languages evolve over time, R is now different from what it used to be, and we can shape it (slowly; we value its stable API) to become something even better in the future.

¹⁴ It might also happen that for certain readers, this will not be an appropriate course at all, either at this stage of their career (come back later) or in general (no dramas). This is a non-profit, open-access project, but it does not mean it is ideal for everyone. We recommend giving other sources a try, e.g., [8, 10, 15, 45, 57, 59, 60, 67], etc. Some of them are freely available.



Figure 1. An overview of the most prevalent R data types; see Figure 17.2 for a more comprehensive list.

- numeric (Chapter 2) represents real numbers, such as 1, 3.14, -0.
 0000001, etc.;
- character (Chapter 6) contains strings of characters, e.g., "gгов", "123", or "Добрий день";
- function (Chapter 7) is used to group a series of expressions (code lines) so
 that they can be applied on miscellaneous input data to generate the (hopefully) desired outcomes, for instance, cat, print, plot, sample, and sum;
- list (generic vector; Chapter 4) can store elements of mixed types.

The above will be complemented with a discussion on vector indexing (Chapter 5) and ways to control the program flow (Chapter 8).

- 2. *Compound types* are mostly discussed in the second part. They are wrappers around objects of basic types that might behave unlike the underlying primitives thanks to the dedicated operations *overloaded* for them. For instance:
 - factor (Section 10.3.2) is a vector-like object that represents qualitative data (on a nominal or an ordered scale);
 - matrix (Chapter II) stores tabular data, i.e., arranged into rows and columns, where each cell is usually of the same type;
 - data.frame (Chapter 12) is also used for depositing tabular data, but this time such that each column can be of a different type;
 - formula (Section 17.6) is utilised by some functions to specify supervised learning models or define operations to be performed within data subgroups, amongst others;

• and many more, which we can arbitrarily define using the principles of S3-style object-orientated programming (Chapter 10).

In this part of the book, we also discuss the principles of sustainable coding (Chapter 9) as well as introduce the basic ways to prepare publication-quality graphics (Chapter 13).

- 3. More advanced material is discussed in the third part. For most readers, it should be of theoretical interest only. However, it can help gain a complete understanding of and control over our environment. This includes the following data types:
 - symbol (name), call, expression (Chapter 15) are objects representing unevaluated R expressions that can be freely manipulated and executed if needed;
 - environment (Chapter 16) store named objects in hash maps and provides the basis for the environment model of evaluation;
 - externalptr (Section 14.2.8) provides the ability to maintain any dynamically allocated C/C++ objects between function calls.

We should not be surprised that we did not list any data types defined by a few trendy¹⁵ third-party packages. We will later see that we can most often do without them. If that is not the case, we will become skilled enough to learn them quickly ourselves.

0.5 About the author

I, Marek Gagolewski¹⁶ (pronounced like Ma'rek Gong-olive-ski), am currently a Senior Lecturer in Data Science/Applied AI at Deakin University in Melbourne, VIC, Australia, and an Associate Professor at the Systems Research Institute of the Polish Academy of Sciences.

My research interests are related to data science, in particular: modelling complex phenomena, developing usable, general-purpose algorithms, studying their analytical properties, and finding out how people use, misuse, understand, and misunderstand methods of data analysis in research, commercial, and decision-making settings. I am an author of over 90 publications, including journal papers in outlets such as Proceedings of the National Academy of Sciences (PNAS), Journal of Statistical Software, The R Journal, Information Fusion, International Journal of Forecasting, Statistical Modelling, Physica A: Statistical Mechanics and its Applications, Information Sciences, Knowledge-Based Systems, IEEE Transactions on Fuzzy Systems, and Journal of Informetrics.

In my "spare" time, I write books for my students: check out my Minimalist Data

¹⁵ Which does not automatically mean *good*. For instance, sugar, salt, and some drugs are very popular, but it does not make them healthy.

¹⁶ https://www.gagolewski.com/

Wrangling with Python¹⁷ [26]. I also develop open-source data analysis software, such as **stringi**¹⁸ (one of the most often downloaded R packages), **genieclust**¹⁹ (a fast and robust clustering algorithm in both Python and R), and many others²⁰.

0.6 Acknowledgements

R, and its predecessor S, is the result of a collaborative effort of many programmers²¹. Without their generous intellectual contributions, the landscape of data analysis would not be as beautiful as it is now. R is distributed under the terms of the GNU General Public License version 2. We occasionally display fragments of its source code for didactic purposes.

We describe and use R version 4.3.0 (2023-04-21). However, we expect 99.9% of the material covered here to be valid in future releases (consider filing a bug report if you discover this is not the case).

Deep R Programming is based on the author's experience as an R user (since ~2003), developer of open-source packages (mentioned above), tutor/lecturer (since ~2008), and an author of a quite successful Polish textbook Programowanie w języku R [25] which was published by PWN (1st ed. 2014, 2nd ed. 2016). Even though the current book is an entirely different work, its predecessor served as an excellent testbed for many ideas conveyed here.

In particular, the teaching style exercised in this book has proven successful in many similar courses that yours truly was responsible for, including at Warsaw University of Technology, Data Science Retreat (Berlin), and Deakin University (Melbourne). I thank all my students and colleagues for the feedback given over the last 15-odd years.

This work received no funding, administrative, technical, or editorial support from Deakin University, Warsaw University of Technology, Polish Academy of Sciences, or any other source.

This book was prepared in a Markdown superset called MyST²², Sphinx²³, and TeX (XeLaTeX). Code chunks were processed with the R package knitr [62]. All figures were plotted with the low-level graphics package using the author's own style template. A little help from Makefiles, custom shell scripts, and Sphinx plugins (sphinxcontrib-bibtex²⁴, sphinxcontrib-proof²⁵) dotted the j's and crossed the f's.

¹⁷ https://datawranglingpy.gagolewski.com/

¹⁸ https://stringi.gagolewski.com/

¹⁹ https://genieclust.gagolewski.com/

²⁰ https://github.com/gagolews

²¹ https://www.r-project.org/contributors.html

²² https://myst-parser.readthedocs.io/en/latest/index.html

²³ https://www.sphinx-doc.org/

²⁴ https://pypi.org/project/sphinxcontrib-bibtex

²⁵ https://pypi.org/project/sphinxcontrib-proof

The **Ubuntu** Mono²⁶ font is used for the display of code. Typesetting of the main text relies on the $Alegreya^{27}$ and $Lato^{28}$ typefaces.

0.7 You can make this book better

When it comes to quality assurance, open, non-profit projects have to resort to the generosity of the readers' community.

If you find a typo, a bug, or a passage that could be rewritten or extended for better readability/clarity, do not hesitate to report it via the *Issues* tracker available at https://github.com/gagolews/deepr/issues. New feature requests are welcome as well.

Please consider "starring" the book's *GitHub* repository²⁹. Some people (weirdly) use the number of "stars" as a proxy for quality.

Spread the news about this book by sharing the link https://deepr.gagolewski.com/with your mates, peers, or students. You may also want to cite it in your publications or reports. Thank you.

²⁶ https://design.ubuntu.com/font

²⁷ https://www.huertatipografica.com/en

²⁸ https://www.latofonts.com/

²⁹ https://github.com/gagolews/deepr

Part I

Deep

Introduction

1.1 Hello, world!

Traditionally, every programming journey starts by printing a "Hello, world"-like greeting. Let's then get it over with asap:

```
cat("My hovercraft is full of eels.\n") # `\n` == newline
## My hovercraft is full of eels.
```

By *calling (invoking)* the **cat** function, we printed out a given character string that we enclosed in double-quote characters.

Documenting code is a good development practice. It is thus worth knowing that any text followed by a hash sign (that is not part of a string) is a *comment*. It is ignored by the interpreter.

```
# This is a comment.
# This is another comment.
cat("I cannot wait", "till lunchtime.\n") # two arguments (another comment)
## I cannot wait till lunchtime.
cat("# I will not buy this record.\n# It is scratched.\n")
## # I will not buy this record.
## # It is scratched.
```

By convention, in this book, the textual outputs generated by R itself are always preceded by two hashes. This makes copy-pasting all code chunks easier in case we would like to experiment with them (which is always highly encouraged).

Whenever a call to a function is to be made, the round brackets are obligatory. All objects within the parentheses (they are separated by commas) constitute the input data to be consumed by the operation. Thus, the syntax is: a_function_to_be_called(argument1, argument2, etc.).

1.2 Setting up the development environment

1.2.1 Installing R

It is quite natural to pine for the ability to execute the above code ourselves – we cannot learn programming without getting our hands dirty.

The official precompiled binary distributions of R can be downloaded from https://cran.r-project.org/.

For serious programming work¹, we recommend, sooner rather than later, switching to² one of the UNIX-like operating systems. This includes the free, open-source (== good) variants of GNU/Linux, amongst others, or the proprietary (== not so good) m**OS. The users thereof might employ their favourite package manager (e.g., apt, dnf, pacman, or Homebrew) to install R.

Users of other operating systems (such as Wi***ws) might consider installing Anaconda or Miniconda if they would like to work with Jupyter (Section 1.2.5) or Python.

Below we review several ways in which we can write and execute R code. It is up to the benign readers to research, set up, and learn the development environment that suits their needs. As usual in real life, there is no single universal approach that always works best in all scenarios.

1.2.2 Interactive mode

R's read-eval-print loop (REPL) can give us instant gratification whenever we would like to compute something quickly, e.g., determine basic aggregates of a few numbers entered by hand or evaluate a mathematical expression like "2+2".

How to start the R console varies from system to system, e.g., users of UNIX-like boxes can simply execute **R** from the terminal (shell, command line). Wi***ws folks can fire up **RGui** from the *Start* menu.

Important When working interactively, the default³ command prompt, ">", means: *I* am awaiting orders. Moreover, "+" denotes: *Please continue*. In the latter case, we should either complete the unfinished expression or cancel the operation by pressing ESC or CTRL+C (depending on the operating system).

- > cat("And now
- + for something

(continues on next page)

¹ For instance, when interoperability with other programming languages/environments is required or when we think about scheduling jobs on Linux-based computing/container clusters.

² Or at least trying out – by installing a copy of GNU/Linux on a virtual machine (VM).

³ It can be changed; see **help**("options").

(continued from previous page)

For readability, we never print out the command prompt characters in this book.

1.2.3 Batch mode: Working with R scripts (**)

The interactive mode of operation is unsuitable for more complicated tasks, though.

The users of UNIX-like operating systems will be interested in another extreme, which involves writing standalone R scripts that can be executed line by line without any user intervention.

To do so, in the terminal, we can invoke:

```
Rscript file.R
```

where file. R is the path to a source file.

Exercise 1.1 (**) In your favourite text editor (e.g., **Notepad++**, **Kate**, **vi**, **Emacs**, **RStudio**, or **VSCodium**), create a file named test.R. Write a few calls to the **cat** function. Then, execute this script from the terminal through **Rscript**.

1.2.4 Weaving: Automatic report generation (**)

Reproducible data analysis⁴ requires us to keep the results (text, tables, plots, auxiliary files) synchronised with the code and data that generate them.

utils::Sweave (the Sweave function from the utils package) and knitr [62] are two example template processors that evaluate R code chunks within documents written in LaTeX, HTML, or other markup languages. The chunks are replaced by the outputs they yield.

This book is a showcase of such an approach: all the results, including Figure 2.3 and the message about busy hovercrafts, were generated programmatically. Thanks to its being written in the highly universal Markdown⁵ language, it could be easily converted

⁴ The idea dates back to Knuth's literate programming concept; see [40].

⁵ https://daringfireball.net/projects/markdown

to a single PDF document⁶ as well as the whole website⁷. Tools like **pandoc** and **docutils** facilitate such operations.

Exercise 1.2 (**) Install the **knitr** package by calling **install.packages**("knitr") from within an R session. Then, create a text file named test. Rmd with the following content:

```
# Hello, Markdown!
This is my first automatically generated report,
where I print messages and stuff.

```{r}
print("G'day!")
print(2+2)
plot((1:10)^2)
...
Thank you for your attention.
```

Assuming that the file is located in the current working directory (compare Section 7.3.2), call <code>knitr::knit("test.Rmd")</code> from the R console or run the following in the terminal:

```
Rscript -e 'knitr::knit("test.Rmd")'
```

Then, inspect the generated Markdown file, test.md.

Furthermore, if you have the **pandoc** tool installed, to generate a standalone HTML file, execute in the terminal:

```
pandoc test.md --standalone -o test.html
```

Alternatively, for ways to call external programs from R, see Section 7.3.2.

# 1.2.5 Semi-interactive modes (Jupyter Notebooks, sending code to the associated R console, etc.)

The nature of the most frequent use cases of R encourages a semi-interactive workflow, where we quickly progress with prototyping by trial and error. In this mode, we compose a series of short code fragments inside a standalone R script. Each fragment implements a simple, well-defined task, such as loading data files, data cleansing, feature visualisation, computations of information aggregates, etc. Importantly, any code chunk can be *sent* to the associated R console and executed there. This way, we can inspect the result it generates. If we are not happy with the outcome, we can apply the necessary corrections.

There are quite a few integrated development environments that enable such a work-

<sup>6</sup> https://deepr.gagolewski.com/deepr.pdf

<sup>7</sup> https://deepr.gagolewski.com/

flow, including JupyterLab, Emacs, RStudio, and VSCodium. Some of them require additional plugins for R.

Executing an individual code line or a whole text selection is usually done by pressing (configurable) keyboard shortcuts such as Ctrl+Enter or Shift+Enter.

**Exercise 1.3** (\*) **Jupy terLab**<sup>8</sup> is a development environment that runs in a web browser. It was programmed in Python, but supports many programming languages. Thanks to **IRkernel**<sup>9</sup>, we can use it with R.

- 1. Install JupyterLab and IRkernel (for instance, if you use Anaconda, run conda install -c r r-essentials).
- 2. From the File menu, select Create a new R source file and save it as, e.g., test.R.
- 3. Click File and select Create a new console for the editor running the R kernel.
- 4. Input a few print "Hello, world"-like calls.
- 5. Press Shift+Enter (whilst working in the editor) to send different code fragments to the console and execute them. Inspect the results.

See Figure 1.1 for an illustration. Note that issuing **options**(jupyter.rich\_display=FALSE) may be necessary to disable rich HTML outputs and make them look more like ones in this book.

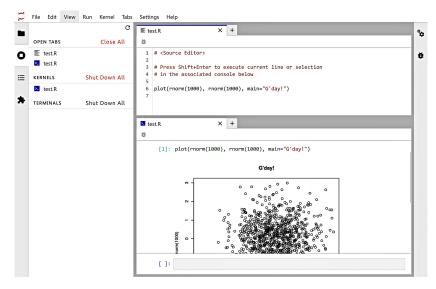


Figure 1.1. JupyterLab: A source file editor and the associated R console, where we can run arbitrary code fragments.

**Example 1.4** (\*) **JupyterLab** also handles dedicated Notebooks, where editable and executable code chunks and results they generate can be kept together in a single .ipynb (JSON) file; see

<sup>8</sup> https://jupyterlab.readthedocs.io/en/stable

<sup>9</sup> https://irkernel.github.io/

Figure 1.2 for an illustration and Chapter 1 of [26] for a quick introduction (from the Python language kernel perspective).

This environment is quite convenient for live coding (e.g., for teachers) or performing exploratory data analyses. However, for more serious programming work, the code can get messy. Luckily, there is always an option to export a notebook to an executable, plain text R script.

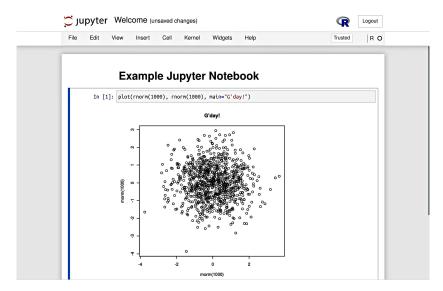


Figure 1.2. An example Jupyter Notebook, where we can keep code and results together.

# 1.3 Atomic vectors at a glance

After printing "Hello, world", a typical programming course would normally proceed with the discussion on basic data types for storing individual numeric or logical values. Next, we would be introduced to arithmetic and relational operations on such scalars, followed by the definition of whole arrays or other collections of values, complemented by the methods to iterate over them, one element after another.

In R, no separate types representing individual values have been defined. Instead, what seems to be a single datum, is already a *vector* (sequence, array) of length one.

```
2.71828 # input a number; here: the same as print(2.71828)
[1] 2.7183
length(2.71828) # it is a vector with one element
[1] 1
```

To create a vector of any length, we can call the **c** function, which combines given arguments into a single sequence:

```
c(1, 2, 3) # three values combined
[1] 1 2 3
length(c(1, 2, 3)) # indeed, it is a vector of length three
[1] 3
```

In Chapter 2, Chapter 3, and Chapter 6, we will discuss the most prevalent types of atomic vectors: numeric, logical, and character ones, respectively.

```
c(0, 1, -3.14159, 12345.6) # four numbers
[1] 0.0000 1.0000 -3.1416 12345.6000
c(TRUE, FALSE) # two logical values
[1] TRUE FALSE
c("spam", "bacon", "spam") # three character strings
[1] "spam" "bacon" "spam"
```

We call them *atomic* for they can only group together values of the same type. Lists, which we will discuss in Chapter 4, are, on the other hand, referred to as *generic* vectors. They can be used for storing items of mixed types: other lists as well.

**Note** Not having separate scalar types greatly simplifies the programming of numerical computing tasks. Vectors are prevalent in our main areas of interest: statistics, simulations, data science, machine learning, and all other data-orientated computing. For example, columns and rows in tables (characteristics of clients, ratings of items given by users) or time series (stock market prices, readings from temperature sensors) are all best represented by means of such sequences.

The fact that vectors are the core part of the R language makes their use very natural, as opposed to the languages that require special add-ons for vector processing, e.g., numpy for Python [34]. By learning different ways to process them as a whole (instead of one element at a time), we will ensure that our ideas can quickly be turned into operational code. For instance, computing summary statistics such as, say, the mean absolute deviation of a sequence x, will be as effortless as writing mean(abs(x-mean(x))). Such code is not only easy to read and maintain, but it is also fast to run.

# 1.4 Getting help

Our aim is to become independent, advanced R programmers.

Independent, however, does not mean omniscient. The *R help system* is the authoritative source of knowledge about specific functions or more general topics. To open a help page, we call:

```
help("topic") # equivalently: ?"topic"
```

**Exercise 1.5** Sight (without going into detail) the manual on the **length** function by calling **help**("length"). Note that most help pages are structured as follows:

- 1. Header: package:base means that the function is a base one (see Section 7.3.1 for more details on the R package system);
- 2. Title;
- 3. Description: a short description of what the function does;
- 4. Usage: the list of formal arguments (parameters) to the function;
- 5. Arguments: the meaning of each formal argument explained;
- 6. Details: technical information;
- 7. Value: return value explained;
- 8. References: further reading;
- 9. See Also: links to other help pages;
- 10. Examples: R code that is worth inspecting.

We can also search within all the installed help pages by calling:

```
help.search("vague topic") # equivalently: ??"vague topic"
```

This way, we will be able to find answers to our questions more reliably than when asking DuckDuckGo or G\*\*gle, which commonly return many low-quality, irrelevant, or distracting results from splogs. We do not want to lose the sacred code writer's flow! It is a matter of personal hygiene and good self discipline.

**Important** All code chunks, including code comments and textual outputs, form an integral part of this book's text. They should not be skipped by the reader. On the contrary, they must become objects of our intense reflection and thorough investigation.

For instance, whenever we introduce a function, it may be a clever idea to look it up in the help system. Moreover, playing with the presented code (running, modifying, experimenting, etc.) is also very beneficial. We should develop the habit of asking ourselves questions like "What would happen if...", and then finding the answers on our own.

We are now ready to discuss the most significant operations on numeric vectors, which constitute the main theme of the next chapter. See you there.

# 1.5 Exercises

**Exercise 1.6** What are the three most important types of atomic vectors?

**Exercise 1.7** According to the classification of the R data types we introduced in the previous chapter, are atomic vectors basic or compound types?

# Numeric vectors

In this chapter, we discuss the uttermost common operations on numeric vectors. They are so fundamental that we will also find them in other scientific computing environments, including Python with numpy or tensorflow, Julia, MATLAB, GNU Octave, or Scilab.

At first blush, the number of functions we are going to explore may seem quite large. Still, the reader is kindly asked to place some trust (a rare thing these days) in yours truly. It is because our selection is comprised only of the most representative and educational amongst the plethora of possible choices. More complex building blocks can often be reduced to a creative combination of the former or be easily found in a number of additional packages or libraries (e.g., GNU GSL [28]).

A solid understanding of base R programming is crucial for dealing with popular packages (such as **data.table**, **dplyr**, or **caret**). Most importantly, base R's API is *stable*. Hence, the code we compose today will most likely work the same way in ten years. It is often not the case when we rely on external add-ons.

In the sequel, we will be advocating a minimalist, keep-it-simple approach to the art of programming data processing pipelines, one that is a healthy balance between "doing it all by ourselves", "minimising the information overload", "being lazy", and "standing on the shoulders of giants".

**Note** The exercises that we suggest below are all self-contained unless explicitly stated otherwise. The use of language constructs that are yet to be formally introduced (in particular, **if**, **for**, and **while** explained in Chapter 8) is not just unnecessary: it is discouraged. Moreover, we recommend against taking shortcuts by looking up partial solutions on the internet. Rather, to get the most out of this course, we should be seeking relevant information within the current and preceding chapters as well as the R help system.

# 2.1 Creating numeric vectors

#### 2.1.1 Numeric constants

The simplest numeric vectors are those of length one:

```
-3.14
[1] -3.14
1.23e-4
[1] 0.000123
```

The latter is in what we call *scientific notation*, which is a convenient means of entering numbers of very large or small orders of magnitude. Here, "e" stands for "... times 10 to the power of...". Therefore, 1.23e-4 is equal to  $1.23 \times 10^{-4} = 0.000123$ . In other words, given 1.23, we move the decimal separator by four digits towards the left, adding zeroes if necessary.

In real life, some information items may be inherently or temporarily missing, unknown, or Not Available. As R is orientated towards data processing, it was equipped with a special indicator:

```
NA_real_ # numeric NA (missing value)
[1] NA
```

It is similar to the *Null* marker in database query languages such as SQL. Note that NA\_real\_ is displayed simply as "NA", chiefly for readability.

Moreover, Inf denotes infinity,  $\infty$ , i.e., an element that is larger than the largest representable double-precision (64 bit) floating point value. Also, NaN stands for *not-anumber*, which is returned as the result of some illegal operations, e.g., 0/0 or  $\infty - \infty$ .

Below we provide a few ways to create numeric vectors with possibly more than one element.

# 2.1.2 Concatenating vectors with c

First, the **c** function can be used to combine (concatenate) many numeric vectors, each of any length. It results in a single object:

```
c(1, 2, 3) # three vectors of length one -> one vector of length three
[1] 1 2 3
c(1, c(2, NA_real_, 4), 5, c(6, c(7, Inf)))
[1] 1 2 NA 4 5 6 7 Inf
```

**Note** Running help("c"), we will see that its usage is like c(...). In the current context, this means that the c function takes an arbitrary number of arguments. In Section 9.4.6, we will study the dot-dot-dot (ellipsis) parameter in more detail.

# 2.1.3 Repeating entries with rep

Second, rep replicates the elements in a vector a given number of times.

```
rep(1, 5)

[1] 1 1 1 1 1

rep(c(1, 2, 3), 4)

[1] 1 2 3 1 2 3 1 2 3 1 2 3
```

In the second case, the whole vector (1, 2, 3) has been *recycled* (tiled) four times. Interestingly, if the second argument is a vector of the same length as the first one, the behaviour will be different:

```
rep(c(1, 2, 3), c(2, 1, 4))
[1] 1 1 2 3 3 3 3
rep(c(1, 2, 3), c(4, 4, 4))
[1] 1 1 1 1 2 2 2 2 3 3 3 3
```

Here, each element is repeated the corresponding number of times.

Calling help("rep"), we find that the function's usage is like rep(x, ...). It is rather peculiar. However, reading further, we discover that the ellipsis (dot-dot-dot) may be fed with one of the following parameters:

- times,
- length.out<sup>1</sup>,
- · each.

So far, we have been playing with times, which is listed second in the parameter list (after x, the vector whose elements are to be repeated).

**Important** It turns out that the following function calls are all equivalent:

```
rep(c(1, 2, 3), 4) # positional matching of arguments: `x`, then `times` rep(c(1, 2, 3), times=4) # `times` is the second argument rep(x=c(1, 2, 3), times=4) # keyword arguments of the form name=value rep(times=4, x=c(1, 2, 3)) # keyword arguments can be given in any order rep(times=4, c(1, 2, 3)) # mixed positional and keyword arguments
```

We can also pass each or length.out, but their names must be mentioned explicitly:

```
rep(c(1, 2, 3), length.out=7)
[1] 1 2 3 1 2 3 1
rep(c(1, 2, 3), each=3)
[1] 1 1 1 2 2 2 3 3 3
rep(c(1, 2, 3), length.out=7, each=3)
[1] 1 1 1 2 2 2 3
```

<sup>&</sup>lt;sup>1</sup> A dot has no special meaning in R; see Section 2.2.

**Note** Whether it was a good programming practice to actually implement a range of varied behaviours inside a single function is a matter of taste. On the one hand, in all of the examples above, we do repeat the input elements somehow, so remembering just one function name is really convenient. Nevertheless, a drastic change in the repetition pattern depending, e.g., on the length of the times argument can be bug-prone. Anyway, we have been warned<sup>2</sup>.

Zero-length vectors are possible too:

```
rep(c(1, 2, 3), 0)
numeric(0)
```

Even though their handling might be a little tricky, we will later see that they are indispensable in contexts like "create an empty data frame with a specific column structure".

Also, note that R often allows for partial matching of named arguments, but its use is a bad programming practice; see Section 15.4.4 for more details.

```
rep(c(1, 2, 3), len=7) # not recommended (see later)
Warning in rep(c(1, 2, 3), len = 7): partial argument match of 'len' to
'length.out'
[1] 1 2 3 1 2 3 1
```

We see the warning only because we have set **options**(warnPartialMatchArgs=TRUE) in our environment. It is not used by default.

# 2.1.4 Generating arithmetic progressions with seq and `:`

Third, we can call the **seq** function to create a sequence of equally-spaced numbers on a linear scale, i.e., an arithmetic progression.

```
seq(1, 15, 2)
[1] 1 3 5 7 9 11 13 15
```

From the function's help page, we discover that **seq** accepts the from, to, by, and length.out arguments, amongst others. Thus, the above call is equivalent to:

```
seq(from=1, to=15, by=2)
[1] 1 3 5 7 9 11 13 15
```

<sup>&</sup>lt;sup>2</sup> Some "caring" R users might be tempted to introduce two new functions now, one for generating (1, 2, 3, 1, 2, 3, ...) only and the other outputting patterns like (1, 1, 1, 2, 2, 2, ...). They would most likely wrap them in a new package and announce that on social media. But this is nothing else than a multiplication of entities without actual necessity. This way, we would end up with three functions. First is the original one, rep, which everyone ought to know anyway because it is part of the standard library. Second and third are the two redundant procedures whose user-friendliness is only illusory. See also Chapter 9 for a discussion on the design of functions.

Note that to actually means "up to":

```
seq(from=1, to=16, by=2)
[1] 1 3 5 7 9 11 13 15
```

We can also pass length.out instead of by. In such a case, the increments or decrements will be computed via the formula ((to - from)/(length.out - 1)). This default value is reported in the Usage section of help("seq").

```
seq(1, 0, length.out=5)
[1] 1.00 0.75 0.50 0.25 0.00
seq(length.out=5) # default `from` is 1
[1] 1 2 3 4 5
```

Arithmetic progressions with steps equal to 1 or -1 can also be generated via the `:` operator.

```
1:10 # seq(1, 10) or seq(1, 10, 1)

[1] 1 2 3 4 5 6 7 8 9 10

-1:10 # seq(-1, 10) or seq(-1, 10, 1)

[1] -1 0 1 2 3 4 5 6 7 8 9 10

-1:-10 # seq(-1, -10) or seq(-1, -10, -1)

[1] -1 -2 -3 -4 -5 -6 -7 -8 -9 -10
```

Let us highlight the order of precedence of this operator: -1:10 means (-1):10, and not -(1:10); compare Section 2.4.3.

**Exercise 2.1** Take a look at the manual page of **seq\_along** and **seq\_len**. Determine Having **seq**<sup>3</sup> at hand, determine whether they can easily be done without.

## 2.1.5 Generating pseudorandom numbers

We can also generate sequences drawn independently from a range of univariate probability distributions.

```
runif(7) # uniform U(0, 1)
[1] 0.287578 0.788305 0.408977 0.883017 0.940467 0.045556 0.528105
rnorm(7) # normal N(0, 1)
[1] 1.23950 -0.10897 -0.11724 0.18308 1.28055 -1.72727 1.69018
```

These correspond to seven pseudorandom deviates following the uniform distribution on the unit interval (i.e., (0,1)) and the standard normal distribution (i.e., with expectation 0 and standard deviation 1), respectively; compare Figure 2.3.

For more *named* distribution classes frequently occur in various real-world statistical modelling exercises, see Section 2.3.4.

<sup>&</sup>lt;sup>3</sup> Certain configurations of **seq** and its variants might return vectors of the type integer instead of double, some of them in a compact (ALTREP) form; see Section 6.4.1.

Another worthwhile function picks items from a given vector, either with or without replacement:

```
sample(1:10, 20, replace=TRUE) # 20 with replacement (allow repetitions)
[1] 3 3 10 2 6 5 4 6 9 10 5 3 9 9 9 3 8 10 7 10
sample(1:10, 5, replace=FALSE) # 5 without replacement (do not repeat)
[1] 9 3 4 6 1
```

The distribution of the sampled values does not need to be uniform; the prob argument may be fed with a vector of the corresponding probabilities. For example, here are 20 independent realisations of the random variable X such that  $\Pr(X=0)=0.9$  (the probability that we obtain 0 is equal to 90%) and  $\Pr(X=1)=0.1$ :

```
sample(0:1, 20, replace=TRUE, prob=c(0.9, 0.1))
[1] 0 0 0 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1
```

**Note** If n is a single number (a numeric vector of length 1), then sample(n, ...) is equivalent to sample(1:n, ...). Similarly, seq(n) is a synonym for seq(1, n) or seq(1, length(n)), depending on the length of n. This is a dangerous behaviour that can occasionally backfire and lead to bugs (check what happens when n is, e.g., o). Nonetheless, we have been warned. From now on, we are going to be extra careful (but are we really?). Read more at help("sample") and help("seq").

Let us stress that the numbers we obtain are merely *pseudo*random because they are generated algorithmically. R uses the Mersenne-Twister MT19937 method [46] by default; see **help**("RNG") and [21, 29, 42]. By setting the *seed* of the random number generator, i.e., resetting its state to a given one, we can obtain results that are *reproducible*.

```
set.seed(12345) # seeds are specified with integers
sample(1:10, 5, replace=TRUE) # a,b,c,d,e
[1] 3 10 8 10 8
sample(1:10, 5, replace=TRUE) # f,g,h,i,j
[1] 2 6 6 7 10
```

Setting the seed to the one used previously gives:

```
set.seed(12345)
sample(1:10, 5, replace=TRUE) # a,b,c,d,e
[1] 3 10 8 10 8
```

We did not(?) expect that! And now for something completely different:

```
set.seed(12345)
sample(1:10, 10, replace=TRUE) # a,b,c,d,e,f,g,h,i,j
[1] 3 10 8 10 8 2 6 6 7 10
```

Reproducibility is a crucial feature of each truly scientific experiment. The same initial condition (here: the same seed) leads to exactly the same outcomes.

**Note** Some claim that the only unsuspicious seed is 42 but in matters of taste, there can be no disputes. Everyone can use their favourite picks: yours truly savours 123, 1234, and 12345 as well.

When performing many runs of Monte Carlo experiments, it may also be a clever idea to call **set.seed(i)** in the i-th iteration of a simulation we are trying to program.

We should ensure that our seed settings are applied consistently across all our scripts. Otherwise, we might be accused of tampering with evidence. For instance, here is the ultimate proof that we are very lucky today:

This is exactly why reproducible scripts and auxiliary data should be published alongside all research reports or papers. Only open, transparent science can be fully trustworthy.

If **set.seed** is not called explicitly, and the random state is not restored from the previously saved R session (see Chapter 16), then the random generator is initialised based on the current wall time and the identifier of the running R instance (PID). This may justify the impression that the numbers we generate appear surprising.

To understand the "pseudo" part of the said randomness better, in Section 8.3, we will build a very simple random generator ourselves.

## 2.1.6 Reading data with scan

An example text file named euraud-20200101-20200630.csv<sup>4</sup> gives the EUR to AUD exchange rates (how many Australian Dollars can we buy for 1 Euro) from 1 January to 30 June 2020 (remember COVID-19?). Let us preview the first couple of lines:

```
EUR/AUD Exchange Rates
Source: Statistical Data Warehouse of the European Central Bank System
https://www.ecb.europa.eu/stats/policy_and_exchange_rates/
(provided free of charge)
NA
1.6006
1.6031
NA
```

The four header lines that begin with "#" merely serve as comments for us humans.

<sup>4</sup> https://github.com/gagolews/teaching-data/raw/master/marek/euraud-20200101-20200630.csv

They should be ignored by the interpreter. The first "real" value, NA, corresponds to 1 January (Wednesday, New Year's Day; Forex markets were closed, hence a missing observation).

We can invoke the **scan** function to read all the inputs and convert them to a single numeric vector:

```
scan(paste0("https://github.com/gagolews/teaching-data/raw/",
 "master/marek/euraud-20200101-20200630.csv"), comment.char="#")
[1]
 NA 1.6006 1.6031
 NA
 NA 1.6119 1.6251 1.6195 1.6193 1.6132
 NA 1.6117 1.6110 1.6188 1.6115 1.6122
[11]
 NA
[21] 1.6177 1.6184 1.6149 1.6127 NA
 NA 1.6291 1.6290 1.6299 1.6412
[31] 1.6494
 NA 1.6521 1.6439 1.6299 1.6282 1.6417
 NA
[41] 1.6373 1.6260 1.6175 1.6138 1.6151 NA
 NA 1.6129 1.6195 1.6142
[51] 1.6294 1.6363
 NA
 NA 1.6384 1.6442 1.6565 1.6672 1.6875
[61]
 NA 1.6998 1.6911 1.6794 1.6917 1.7103 NA
 NA 1.7330 1.7377
[71] 1.7389 1.7674 1.7684
 NA
 NA 1.8198 1.8287 1.8568 1.8635 1.8226
 NA 1.8586 1.8315 1.7993 1.8162 1.8209
 NA 1.8021
[91] 1.7967 1.8053 1.7970 1.8004
 NA
 NA 1.7790 1.7578 1.7596
[reached getOption("max.print") -- omitted 83 entries]
```

We used the **paste0** function (Section 6.1.3) to concatenate two long strings (too long to fit a single line of code) and form a single URL.

We can also read the files located on our computer. For example:

```
scan("~/Projects/teaching-data/marek/euraud-20200101-20200630.csv",
 comment.char="#")
```

It used an absolute file path that starts at the user's *home directory*, denoted "~". Yours truly's case is /home/gagolews.

**Note** For portability reasons, we suggest slashes, "/", as path separators; see also **help**("file.path") and **help**(".Platform"). They are recognised by all UNIX-like boxes as well as by other popular operating systems, including W\*\*\*\*\*ws. Note that URLs, such as https://deepr.gagolewski.com/, consist of slashes too.

Paths can also be relative to the *current working directory*, denoted ".", which can be read via a call to **getwd**. Usually, it is the directory from where the R session has been started.

For instance, if the working directory was /home/gagolews/Projects/teaching-data/marek, we could write the file path equivalently as ./euraud-20200101-20200630.csv or even euraud-20200101-20200630.csv.

On as side note, ".." marks the *parent directory* of the current working directory. In the above example, ../r/iris.csv is equivalent to /home/gagolews/Projects/teaching-data/r/iris.csv.

**Exercise 2.2** Read the help page about **scan**. Take note of the following formal arguments and their meaning: dec, sep, what, comment.char, and na. strings.

Later we will discuss the **read.table** and **read.csv** functions. They are wrappers around **scan** that reads *structured* data. Also, **write** exports an atomic vector's contents to a text file.

**Example 2.3** Figure 2.1 shows the graph of the aforementioned exchange rates, which was generated by calling:

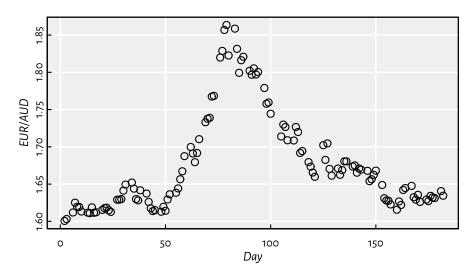


Figure 2.1. EUR/AUD exchange rates from 2020-01-01 (day 1) to 2020-06-30 (day 182).

Somewhat misleadingly (and for reasons that will become apparent later), the documentation of **plot** can be accessed by calling **help**("plot.default"). Read about, and experiment with, different values of the main, xlab, ylab, type, col, pch, cex, lty, and lwdarguments. More plotting routines will be discussed in Chapter 13.

## 2.2 Creating named objects

The objects we bring forth will often need to be memorised so that they can be referred to in further computations. The assignment operator, `<-`, can be used for this purpose:

```
x <- 1:3 # creates a numeric vector and binds the name `x` to it
```

The now-named object can be recalled<sup>5</sup> and dealt with as we please:

```
print(x) # or just `x` in the R console
[1] 1 2 3
sum(x) # example operation: compute the sum of all elements in `x`
[1] 6
```

**Important** In R, all names are *case-sensitive*. Hence, x and X can coexist peacefully: when set, they refer to two different objects. If we tried calling Print(x), print(X), or PRINT(x) above, we would get an error.

Typically, we will be using syntactic names. In help("make.names"), we read: A syntactically valid name consists of letters, numbers and the dot or underline characters and starts with a letter or the dot not followed by a number. Names such as . 2way are not valid, and neither are the reserved words such as if, for, function, next, and TRUE, but see Section 9.3.1 for an exception.

A fine name is self-explanatory and thus reader-friendly: patients, mean, and average\_scores are way better (if they are what they claim they are) than xyz123, crap, or spam. Also, it might not be such a bad idea to get used to denoting:

- vectors with x, y, z,
- matrices (and matrix-like objects) with A, B, ..., X, Y, Z,
- integer indexes with letters i, j, k, l,
- object sizes with n, m, d, p or nx, ny, etc.,

especially when they are only of temporary nature (for storing auxiliary results, iterating over collections of objects, etc.).

There are numerous naming conventions that we can adopt, but most often they are a matter of taste; snake\_case, lowerCamelCase, UpperCamelCase, flatcase, or dot. case are equally sound as long as they are used coherently (for instance, some use snake\_case for vectors and UpperCamelCase for functions). Occasionally, we have little choice but to adhere to the naming conventions of the project we are about to contribute to.

**Note** Generally, a dot, ".", has no special meaning<sup>6</sup>; na.omit is as appropriate a name as na\_omit, naOmit, NAOMIT, naomit, and NaOmit. Readers who know other programming languages will need to habituate themselves to this convention.

<sup>&</sup>lt;sup>5</sup> Name bindings are part of environment frames; see Chapter 16.

<sup>&</sup>lt;sup>6</sup> See Section 10.2 and Section 16.2.1 for a few asterisks.

R, as a dynamic language, allows for introducing new variables at any time. Moreover, existing names can be bound to new values. For instance:

```
(y <- "spam") # bracketed expression - printing not suppressed
[1] "spam"
x <- y # overwrites the previous `x`
print(x)
[1] "spam"</pre>
```

Now x refers to a verbatim copy of y.

**Note** Objects are automatically destroyed when we cannot access them anymore. By now, the *garbage collector* is likely to have got rid of the 1:3 vector begotten above (to which the name x was bound previously).

#### 2.3 Vectorised mathematical functions

Mathematically, we will be denoting a given vector  $\mathbf{x}$  of length n with  $(x_1, x_2, \dots, x_n)$ . In other words,  $x_i$  is its i-th element.

Let us review a few operations that are ubiquitous in numerical computing.

#### 2.3.1 abs and sqrt

R implements *vectorised* versions of the most popular mathematical functions, e.g., **abs** (absolute value, |x|) and **sqrt** (square root,  $\sqrt{x}$ ).

```
abs(c(2, -1, 0, -3, NA_real_))
[1] 2 1 0 3 NA
```

Here, *vectorised* means that instead of being defined to act on a single numeric value, the function of interest is applied on *each* element in a vector. The *i*-th resulting item is a transformed version of the *i*-th input:

$$|\pmb{x}| = (|x_1|, |x_2|, \dots, |x_n|).$$

Moreover, if an input is a missing value, the corresponding output will be marked as unknown as well.

Another example:

```
x <- c(4, 2, -1)
(y <- sqrt(x))
```

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```
Warning in sqrt(x): NaNs produced
[1] 2.0000 1.4142
```

To attract our attention to the fact that computing the square root of a negative value is a reckless act, R generated an informative warning. However, a warning is not an error: the result is being produced as usual. In this case, the ill value is marked as not-anumber.

Also, the fact that the irrational  $\sqrt{2}$  is displayed as 1.4142 does not mean that it is such a crude approximation to 1.414213562373095048801688724209698.... It was rounded when printing purely for aesthetic reasons. In fact, in Section 3.2.3, we will point out that the computer's floating-point arithmetic has roughly 16 decimal digits precision (but we shall see that the devil is in the detail).

```
print(y, digits=16) # display more significant figures
[1] 2.00000000000000 1.414213562373095
 NaN
```

#### Rounding 2.3.2

The following functions get rid of all or portions of fractional parts of numbers:

- **floor**(x) (rounds down to the nearest integer, denoted |x|),
- **ceiling**(x) (rounds up, denoted [x] = -|-x|),
- trunc(x) (rounds towards zero),
- round(x, digits=0) (rounds to the nearest number with digits decimal digits).

#### For instance:

```
x <- c(7.0001, 6.9999, -4.3149, -5.19999, 123.4567, -765.4321, 0.5, 1.5, 2.5)
floor(x)
[1]
 -5 -6 123 -766
ceiling(x)
[1] 8
 -4
 -5 124 -765 1 2
trunc(x)
[1]
 -5 123 -765
```

**Note** When we write that a function's usage is like round(x, digits=0), compare help("round"), we mean that the digits parameter is equipped with the default value of o. In other words, if rounding to o decimal digits is what we need, the second argument can be omitted.

<sup>&</sup>lt;sup>7</sup> There are a couple of settings in place that control the default behaviour of the print function; see width, digits, max.print, OutDec, scipen, etc. in help("options").

```
round(x) # the same as round(x, 0); round half to even

[1] 7 7 -4 -5 123 -765 0 2 2

round(x, 1) # round to tenths (nearest 0.1s)

[1] 7.0 7.0 -4.3 -5.2 123.5 -765.4 0.5 1.5 2.5

round(x, -2) # round to hundreds (nearest 100s)

[1] 0 0 0 0 100 -800 0 0
```

### 2.3.3 Natural exponential function and logarithm

Moreover:

- $\exp(x)$  outputs the natural exponential function,  $e^x$ , where Euler's number  $e \simeq 2.718$ ,
- log(x, base=exp(1)) computes, by default, the natural logarithm of x,  $log_e x$  (which is most often denoted simply as log x).

Recall that if  $x = e^y$ , then  $\log_e x = y$ , i.e., one is the inverse of the other.

```
log(c(0, 1, 2.7183, 7.3891, 20.0855)) # grows slowly

[1] -Inf 0 1 2 3

exp(c(0, 1, 2, 3)) # grows fast

[1] 1.0000 2.7183 7.3891 20.0855
```

These functions enjoy a number of very valuable identities and inequalities. In particular, we should know from school that  $\log(x \cdot y) = \log x + \log y$ ,  $\log(x^y) = y \log x$ , and  $e^{x+y} = e^x \cdot e^y$ .

For the logarithm to a different base, say,  $log_{10} x$ , we can call:

```
log(c(0, 1, 10, 100, 1000, 1e10), 10) # or log(..., base=10)
[1] -Inf 0 1 2 3 10
```

Recall that if  $\log_b x = y$ , then  $x = b^y$ , for any  $1 \neq b > 0$ .

**Example 2.4** Commonly, a logarithmic scale is used for variables that grow rapidly when expressed as functions of each other; see Figure 2.2.

```
x <- seq(0, 10, length.out=1001)
par(mfrow=c(1, 2)) # two plots in one figure (one row, two columns)
plot(x, exp(x), type="l") # left subplot
plot(x, exp(x), type="l", log="y") # log-scale on the y-axis; right subplot</pre>
```

Let us highlight that  $e^x$  on the log-scale is just a straight line. Such a transformation of the axes can only be applied in the case of values strictly greater than 0.

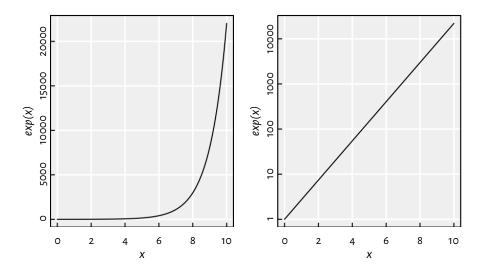


Figure 2.2. Linear- vs log-scale on the y-axis.

### 2.3.4 Probability distributions (\*)

It should come as no surprise that R offers extensive support for many univariate probability distribution families, including:

- continuous distributions, i.e., those whose support is comprised of uncountably many real numbers (e.g., some interval or the whole real line):
  - \*unif (uniform),
  - \*norm (normal),
  - \*exp (exponential),
  - \*gamma (gamma,  $\Gamma$ ),
  - \*beta (beta, B),
  - \*lnorm(log-normal),
  - \*t (Student),
  - \*cauchy (Cauchy-Lorentz),
  - \*chisq (chi-squared,  $\chi^2$ ),
  - \*f (Snedecor–Fisher),
  - \*weibull (Weibull);

with the prefix "\*" being one of:

- d (probability density function, PDF),

- p (cumulative distribution function, CDF; or survival function, SF),
- q (quantile function, being the inverse of the CDF),
- Γ (generation of random deviates; already mentioned above);
- discrete distributions, i.e., those whose possible outcomes can easily be enumerated (e.g., some integers):
  - \*binom (binomial),
  - \*geom (geometric),
  - \*pois (Poisson),
  - \*hyper (hypergeometric),
  - \*nbinom (negative binomial);

here, prefixes "p" and "r" have the same meaning as above, however:

- d now gives the probability mass function (PMF),
- q brings about the quantile function, defined as a generalised inverse of the CDF.

Each distribution is characterised by a set of underlying parameters. For instance, a normal distribution  $N(\mu,\sigma)$  can be pinpointed by setting its expected value  $\mu \in \mathbb{R}$  and standard deviation  $\sigma > 0$ . In R, these two have been named mean and sd, respectively; see **help**("dnorm"). Therefore, e.g., **dnorm**(x, 1, 2) computes the PDF of N(1,2) at x.

**Note** The parametrisations assumed in R can be subtly different from what we know from statistical textbooks or probability courses. For example, the normal distribution can be identified based on either standard deviation or variance, and the exponential distribution can be defined via expected value or its reciprocal. We thus advise the reader to study carefully the documentation of **help**("dnorm"), **help**("dunif"), **help**("dbinom"), and the like.

It is also worth knowing the typical use cases of each of the distributions listed, e.g., a Poisson distribution can describe the probability of observing the number of independent events in a fixed time interval (e.g., the number of users downloading a copy of R from CRAN per hour), and an exponential distribution can model the time between such events; compare [23].

**Exercise 2.5** A call to hist(x) draws a histogram, which can serve as an estimator of the underlying continuous probability density function of a given sample; see Figure 2.3 for an illustration.

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```
x <- seq(0, 1, length.out=101)</pre>
lines(x, dunif(x, 0, 1), lwd=2) # draw the true density function (PDF)
right subplot: normal N(0, 1)
hist(rnorm(10000, 0, 1), col="white", probability=TRUE, main="")
x <- seq(-4, 4, length.out=101)
lines(x, dnorm(x, 0, 1), lwd=2) # draw the PDF
```

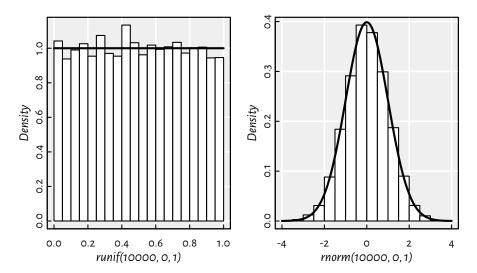


Figure 2.3. Example histograms of some pseudorandom samples and the true underlying probability density functions: the uniform distribution on the unit interval (left) and the standard normal distribution (right).

Draw a histogram of some random samples of different sizes n from the following distributions:

- **rnorm**(n,  $\mu$ ,  $\sigma$ ) normal  $N(\mu, \sigma)$  with expected values  $\mu \in \{-1, 0, 5\}$  (i.e.,  $\mu$  being equal to either -1, 0, or 5; read " $\in$ " as "belongs to the given set" or "in") and standard deviations  $\sigma \in \{0.5, 1, 5\}$ ;
- runif(n, a, b) uniform U(a,b) on the interval (a,b) with a=0 and b=1 as well as a = -1 and b = 1;
- **rbeta**(n, a,  $\beta$ ) beta B( $\alpha$ ,  $\beta$ ) with  $\alpha$ ,  $\beta \in \{0.5, 1, 2\}$ ;
- rexp(n,  $\lambda$ ) exponential E( $\lambda$ ) with rates  $\lambda \in \{0.5, 1, 10\}$ ;

Moreover, read about and play with the breaks, main, xlab, ylab, xlim, ylim, and col parameters; see help("hist").

**Example 2.6** We roll a six-sided dice twelve times. Let C be a random variable denoting the number of cases where the "1" face is thrown. C follows a binomial distribution Bin(n, p) with parameters n = 12 (the number of Bernoulli trials) and p = 1/6 (the probability of success in a single roll).

The probability mass function, **dbinom**, represents the probabilities that the number of "1"s rolled is equal to 0, 1, ..., or 12, i.e., P(C = 0), P(C = 1), ..., or P(C = 12), respectively:

```
round(dbinom(0:12, 12, 1/6), 2) # PMF at 13 different points
[1] 0.11 0.27 0.30 0.20 0.09 0.03 0.01 0.00 0.00 0.00 0.00 0.00
```

On the other hand, the probability that we throw no more than three "1"s,  $P(C \le 3)$ , can be determined by means of the cumulative distribution function, **pbinom**:

```
pbinom(3, 12, 1/6) # pbinom(3, 12, 1/6, lower.tail=FALSE)
[1] 0.87482
```

The smallest c such that  $P(C \le c) \ge 0.95$  can be computed based on the quantile function:

```
qbinom(0.95, 12, 1/6)
[1] 4
pbinom(3:4, 12, 1/6) # for comparison: 0.95 is in-between
[1] 0.87482 0.96365
```

In other words, at least 95% of the time, we will be observing no more than four successes.

Also, here are 30 pseudorandom realisations (simulations) of the random variable C:

```
rbinom(30, 12, 1/6) # how many successes in 12 trials, repeated 30 times ## [1] 1 3 2 4 4 0 2 4 2 2 4 2 3 2 0 4 1 0 1 4 4 3 2 6 2 3 2 2 1 1
```

## 2.3.5 Special functions (\*)

Within mathematical formulae and across assorted application areas, certain functions appear more frequently than others. Hence, for the sake of notational brevity and computational precision, many of them have been assigned special names. For instance, the following functions may be mentioned in the definitions related to some of the probability distributions listed above:

```
• gamma(x) for x > 0 computes \Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt,
```

• beta(a, b) for 
$$a,b>0$$
 yields  $B(a,b)=rac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}=\int_0^1 t^{a-1}(1-t)^{b-1}\,dt$ .

Why do we have **beta** if it is merely a mix of **gammas**? A specific, tailored function is expected to be faster and more precise than its DIY version; its underlying implementation does not have to involve any calls to **gamma**.

```
beta(0.25, 250) # okay
[1] 0.91213
gamma(0.25)*gamma(250)/gamma(250.25) # not okay
[1] NaN
```

The  $\Gamma$  function grows so rapidly that already **gamma**(172) gives rise to Inf. It is due to the fact that a computer's arithmetic is not infinitely precise; compare Section 3.2.3.

Special functions are plentiful; see the open-access NIST Digital Library of Mathematical Functions [51] for one of the most definitive references (and also [2] for its predecessor). R package **gsl** [33] provides a vectorised interface to the GNU GSL [28] library, which implements many of such routines.

**Exercise 2.7** The Pochhammer symbol,  $(a)_x = \Gamma(a+x)/\Gamma(a)$ , can be computed via a call to gsl::poch(a, x), i.e., the poch function from the gsl package:

```
call install.packages("gsl") first
library("gsl") # load the package
poch(10, 3:6) # calls gsl_sf_poch() from GNU GSL
[1] 1320 17160 240240 3603600
```

Read the documentation of the corresponding **gsl\_sf\_poch** function in the GNU GSL manual<sup>8</sup>. And when you are there, do not hesitate to go through the list of all functions, including those related to statistics, permutations, combinations, and so forth.

Many functions also have their logarithm-of versions; see, e.g., lgamma and lbeta. Also, for instance, dnorm and dbeta have the log parameter. Their classical use case is the (numerical) maximum likelihood estimation, which involves the sums of the *logarithms* of densities.

## 2.4 Arithmetic operations

## 2.4.1 Vectorised arithmetic operators

R features the following binary arithmetic operators:

- `+` (addition) and `-` (subtraction),
- `\*` (multiplication) and `/` (division),
- `%**/**%` (integer division) and `%%` (modulo, division remainder),
- `^` (exponentiation; synonym: `\*\*`).

They are all *vectorised*: they take two vectors on input and produce another vector on output.

```
c(1, 2, 3) * c(10, 100, 1000)
[1] 10 200 3000
```

The operation was performed in an *elementwise* fashion on the *corresponding* pairs of elements from both vectors. The first element in the left sequence was multiplied by

<sup>8</sup> https://www.gnu.org/software/gsl/doc/html

the *corresponding* element in the right vector, and the result was stored in the first element of the output. Then, the second element in the left... all right, we get it.

Other operators behave similarly:

```
0:10 + seq(0, 1, 0.1)

[1] 0.0 1.1 2.2 3.3 4.4 5.5 6.6 7.7 8.8 9.9 11.0

0:7 / rep(3, length.out=8) # division by 3

[1] 0.00000 0.33333 0.66667 1.00000 1.33333 1.66667 2.00000 2.33333

0:7 %/% rep(3, length.out=8) # integer division

[1] 0 0 0 1 1 1 2 2

0:7 %% rep(3, length.out=8) # division remainder

[1] 0 1 2 0 1 2 0 1
```

Operations involving missing values also yield NAs:

```
c(1, NA_real_, 3, NA_real_) + c(NA_real_, 2, 3, NA_real_)
[1] NA NA 6 NA
```

#### 2.4.2 Recycling rule

Some of the above statements can be written more concisely. When the operands are of different lengths, the shorter one is *recycled* as many times as necessary, as in rep(y, length.out=length(x)). For example:

```
0:7 / 3

[1] 0.00000 0.33333 0.66667 1.00000 1.33333 1.66667 2.00000 2.33333

1:10 * c(-1, 1)

[1] -1 2 -3 4 -5 6 -7 8 -9 10

2 ^ (0:10)

[1] 1 2 4 8 16 32 64 128 256 512 1024
```

We call this the recycling rule.

If an operand cannot be recycled in its entirety, a warning 9 is generated, but the output is still available.

```
c(1, 10, 100) * 1:8
Warning in c(1, 10, 100) * 1:8: longer object length is not a multiple of
shorter object length
[1] 1 20 300 4 50 600 7 80
```

Vectorisation and the recycling rule are perhaps most fruitful when applying binary operators on sequences of identical lengths or when performing vector-scalar (i.e., a sequence vs a single value) operations. However, there is much more: schemes like

<sup>&</sup>lt;sup>9</sup> A few functions do not warn us whatsoever when they perform incomplete recycling (e.g., paste) or can even give an error (e.g., as.data.frame.list). Consider this inconsistency an annoying bug and hope it will be fixed, in the next decade or so.

"every k-th element" appear in Taylor series expansions (multiply by  $\mathbf{c}(-1, 1)$ ), k-fold cross-validation, etc.; see also Section 11.3.4 for use cases in matrix/tensor processing.

Also, **pmin** and **pmax** return the *parallel* minimum and maximum of the corresponding elements of the input vectors. Their behaviour is the same as the arithmetic operators, but we call them as ordinary functions:

```
pmin(c(1, 2, 3, 4), c(4, 2, 3, 1))
[1] 1 2 3 1
pmin(3, 1:5)
[1] 1 2 3 3 3
pmax(0, pmin(1, c(0.25, -2, 5, -0.5, 0, 1.3, 0.99))) # clipping to [0, 1]
[1] 0.25 0.00 1.00 0.00 0.00 1.00 0.99
```

**Note** Some functions can be very *deeply* vectorised, i.e., with respect to multiple arguments. For example:

```
runif(3, c(10, 20, 30), c(11, 22, 33))
[1] 10.288 21.577 31.227
```

generates three random numbers uniformly distributed over the intervals (10, 11), (20, 22), and (30, 33), respectively.

## 2.4.3 Operator precedence

Expressions involving multiple operators need a set of rules governing the order of computations (unless we enforce it using round brackets). We have said that -1:10 means (-1):10 rather than -(1:10). But what about, say, 1+1+1+1+1+10 or 3\*2^0:5+10?

Let us list the operators mentioned so far *in their order of precedence*, from the least to the most binding (see also **help**("Syntax")):

```
 '<-` (right to left),
 '+` and `-` (binary),
 '*` and `/`,
 '%` and `%/%`,
 `:`,
 '+` and `-` (unary),
 '^` (right to left).
 Hence, -2^2/3+3*4 means ((-(2^2))/3)+(3*4) and not, e.g., -((2^(2/(3+3)))*4).
```

Notice that `+` and `-`, `\*` and `/`, as well as `\%\` and `\/\%` have the same priority. Expressions involving a series of operations in the same group are evaluated left to

right, with the exception of `^` and `<-`, which are performed the other way around. Therefore:

- 2\*3/4\*5 is equivalent to ((2\*3)/4)\*5,
- 2^3^4 is 2^(3^4) because, mathematically, we would write it as  $2^{3^4} = 2^{81}$ ,
- "x <- y <- 4\*3%8/2" binds both y and x to 6, not x to the previous value of y and then y to 6.

When in doubt, we can always *bracket* a subexpression to ensure it is executed in the intended order. It can also increase the readability of the code.

#### 2.4.4 Accumulating

The `+` and `\*` operators, as well as the pmin and pmax functions, implement element-wise operations that are applied on the corresponding elements taken from two given vectors. For instance:

$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{pmatrix} + \begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_n \end{pmatrix} = \begin{pmatrix} x_1 + y_1 \\ x_2 + y_2 \\ x_3 + y_3 \\ \vdots \\ x_n + y_n \end{pmatrix}.$$

However, we can also scan through all the values in a *single* vector and combine the successive elements that we inspect using the corresponding operation:

- cumsum(x) gives the cumulative sum of the elements in a vector,
- **cumprod**(x) computes the cumulative product,
- **cummin**(x) yields the cumulative minimum,
- **cummax**(x) breeds the cumulative maximum.

The i-th element in the output vector will consist of the sum/product/min/max of the first i inputs. For example:

cumsum 
$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} x_1 \\ x_1 + x_2 \\ x_1 + x_2 + x_3 \\ \vdots \\ x_1 + x_2 + x_3 + \dots + x_n \end{pmatrix}.$$

```
cumsum(1:8)
[1] 1 3 6 10 15 21 28 36
cumprod(1:8)
[1] 1 2 6 24 120 720 5040 40320
cummin(c(3, 2, 4, 5, 1, 6, 0))
```

(continues on next page)

```
[1] 3 2 2 2 1 1 0

cummax(c(3, 2, 4, 5, 1, 6, 0))

[1] 3 3 4 5 5 6 6
```

**Example 2.8** On a side note, **diff** can be considered an inverse to **cumsum**. It computes the iterated difference: subtracts the first two elements, then the second from the third one, the third from the fourth, and so on. In other words, **diff**(x) gives y such that  $y_i = x_{i+1} - x_i$ .

```
x <- c(-2, 3, 6, 2, 15)
diff(x)
[1] 5 3 -4 13
cumsum(diff(x))
[1] 5 8 4 17
cumsum(c(-2, diff(x))) # recreates x
[1] -2 3 6 2 15</pre>
```

Thanks to **diff**, we can compute the daily changes to the EUR/AUD forex rates studied earlier; see Figure 2.4.

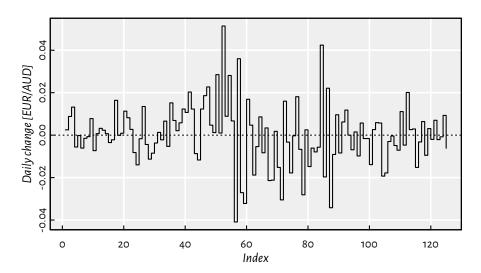


Figure 2.4. Iterated differences of the exchange rates (non-missing values only).

### 2.4.5 Aggregating

Continuing the operations mentioned in the previous section, if we are interested only in the last cumulant, which summarises *all* the inputs, we have the following<sup>10</sup> functions at our disposal:

- sum(x) computes the sum of elements in a vector,  $\sum_{i=1}^{n} x_i = x_1 + x_2 + \dots + x_n$ ,
- **prod**(x) outputs the product of all elements,  $\prod_{i=1}^{n} x_i = x_1 x_2 \cdots x_n$ ,
- min(x) determines the minimum,
- max(x) reckons the greatest value.

```
sum(1:8)
[1] 36
prod(1:8)
[1] 40320
min(c(3, 2, 4, 5, 1, 6, 0))
[1] 0
max(c(3, 2, 4, 5, 1, 6, 0))
[1] 6
```

The above functions form the basis for the popular summary statistics<sup>11</sup> (sample aggregates) such as:

- mean(x) gives the arithmetic mean, sum(x)/length(x),
- var(x) yields the (unbiased) sample variance,  $sum((x-mean(x))^2)/(length(x)-1)$ ,
- **sd**(x) is the standard deviation, **sqrt**(**var**(x)).

Furthermore, median(x) computes the sample median, i.e., the middle value in the sorted<sup>12</sup> version of x.

For instance:

```
x <- runif(1000)
c(min(x), mean(x), median(x), max(x), sd(x))
[1] 0.00046535 0.49727780 0.48995025 0.99940453 0.28748391</pre>
```

**Exercise 2.9** Let x be any vector of length n with positive elements. Compute its geometric and harmonic mean, which are given by, respectively,

$$\sqrt[n]{\prod_{i=1}^{n} x_i} = e^{\frac{1}{n} \sum_{i=1}^{n} \log x_i} \quad and \quad \frac{n}{\sum_{i=1}^{n} \frac{1}{x_i}}.$$

<sup>&</sup>lt;sup>10</sup> Chapter 7 will discuss the **Reduce** function, which generalises the above by allowing any binary operation to be propagated over a given vector.

<sup>&</sup>lt;sup>11</sup> Actually, var and median, amongst others, are defined by the stats package. But this one is automatically loaded by default, so let us not make a fuss about it now.

 $<sup>^{12}</sup>$  min, median, and max are special cases of quantile, which we will discuss much further (Section 4.4.3). It is because it returns a named vector.

When solving exercises like this one, it does not really matter what data you apply these functions on. We are being abstract in the sense that the  $\mathbf{x}$  vector can be anything: from the one that features very accurate socioeconomic predictions that will help make this world less miserable, through the data you have been collecting for the last ten years in relation to your super important PhD research, whatever your company asked you to crunch today, to something related to the hobby project that you enjoy doing after hours. But you can also just test the above on something like " $\mathbf{x} < -\mathbf{runif}(10)$ ", and move on.

All aggregation functions return a missing value if any of the input elements is unavailable. Luckily, they are equipped with the na.rm parameter, on behalf of which we can request the removal of NAs.

Otherwise, we could have called, e.g., mean(na.omit(x)).

**Note** In the documentation, we read that the usage of **sum**, **prod**, **min**, and **max** is like **sum**(..., na.rm=FALSE), etc. In this context, it means that they accept any number of input vectors, and each of them can be of arbitrary length. Therefore, **min**(1, 2, 3), **min**(c(1, 2, 3)) as well as **min**(c(1, 2), 3) all return the same result.

However, we also read that we have mean(x, trim=0, na.rm=FALSE, ...). This time, only one vector can be aggregated, and any further arguments (except trim and na.rm) are ignored.

The extra flexibility (which we do not have to rely on, ever) of the former group is due to their being associative operations. It holds, e.g., (2+3)+4=2+(3+4). Hence, these operations can be performed in any order, in any group. They are primitive operations: it is **mean** that is based on **sum**, not vice versa.

#### 2.5 Exercises

**Exercise 2.10** Answer the following questions.

- What is the meaning of the dot-dot-dot parameter in the definition of the c function?
- We say that the **round** function is vectorised. What does that mean?
- What is wrong with a call to c(sqrt(1), sqrt(2), sqrt(3))?
- What do we mean by saying that multiplication operates element by element?

- How does the recycling rule work when applying `+`?
- How to (and why) set the seed of the pseudorandom number generator?
- What is the difference between NA\_real\_ and NaN?
- How are default arguments specified in the manual of, e.g., the **round** function?
- Is a call to rep(times=4, x=1:5) equivalent to rep(4, 1:5)?
- List a few ways to generate a sequence like (-1, -0.75, -0.5, ..., 0.75, 1).
- Is -3:5 the same as -(3:5)? What about the precedence of operators in expressions such as 2^3/4\*5^6, 5\*6+4/17%%8, and 1+-2^3:4-1?
- If x is a numeric vector of length n (for some  $n \ge 0$ ), how many values will **sample**(x) output?
- Does **scan** support reading directly from compressed archives, e.g., .csv.gz files?

When in doubt, refer back to the material discussed in this chapter or the R manual.

**Exercise 2.11** The following code generates an example graph of arcsine and arccosine. Thanks to vectorisation, its implementation is quite straightforward.

```
x <- seq(-1, 1, length.out=11) # increase length.out for a smoother curve
plot(x, asin(x), # asin() computed for 11 points
 type="l", # lines
 ylim=c(-pi/2, pi), # y axis limits like c(y_min, y_max)
 ylab="asin(x), acos(x)") # y axis label
lines(x, acos(x), col="red", lty="dashed") # adds to the current plot
legend("topright", c("asin(x)", "acos(x)"),
 lty=c("solid", "dashed"), col=c("black", "red"), bg="white")</pre>
```

Inspired by the above, plot the following functions:  $|\sin x^2|$ ,  $|\sin |x|$ ,  $|\sin |x|$ , and  $1/(1 + e^{-x})$ . Recall that the documentation of **plot** can be viewed by calling **help**("plot.default").

**Exercise 2.12** It can be shown that:

$$4\sum_{i=1}^{n} \frac{(-1)^{i+1}}{2i-1} = 4\left(\frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \cdots\right)$$

slowly converges to  $\pi$  as n approaches  $\infty$ . Compute the above for n=1,000,000 and n=1,000,000,000 using the vectorised functions and operators discussed in this chapter, making use of the recycling rule as much as possible.

**Exercise 2.13** Let x and y be two vectors of identical lengths n, say:

```
x <- rnorm(100)
y <- 2*x+10+rnorm(100, 0, 0.5)
```

Compute the Pearson linear correlation coefficient given by:

$$r = \frac{\sum_{i=1}^{n} \left(x_i - \frac{1}{n} \sum_{j=1}^{n} x_j\right) \left(y_i - \frac{1}{n} \sum_{j=1}^{n} y_j\right)}{\sqrt{\sum_{i=1}^{n} \left(x_i - \frac{1}{n} \sum_{j=1}^{n} x_j\right)^2} \sqrt{\sum_{i=1}^{n} \left(y_i - \frac{1}{n} \sum_{j=1}^{n} y_j\right)^2}}.$$

To make sure you have come up with a correct implementation, compare your result to a call to cor(x, y).

**Exercise 2.14** (\*) Find an R package providing a function to compute moving (rolling) averages and medians of a given vector. Apply them on the EUR/AUD currency exchange data. Draw thus obtained smoothened versions of the time series.

**Exercise 2.15** (\*\*) Use a call to **convolve**(..., type="filter") to compute the k-moving average of a numeric vector.

In the next chapter, we will study operations that involve logical values.

# Logical vectors

#### 3.1 Creating logical vectors

R defines three(!) logical constants: TRUE, FALSE, and NA, which represent "yes", "no", and "???", respectively. Each of them, when instantiated, is an atomic vector of length one.

Some of the functions we introduced in the previous chapter can be used to generate logical vectors as well:

```
c(TRUE, FALSE, FALSE, NA, TRUE, FALSE)
[1] TRUE FALSE FALSE NA TRUE FALSE
rep(c(TRUE, FALSE, NA), each=2)
[1] TRUE TRUE FALSE FALSE NA NA
sample(c(TRUE, FALSE), 10, replace=TRUE, prob=c(0.8, 0.2))
[1] TRUE TRUE TRUE FALSE FALSE TRUE TRUE FALSE TRUE TRUE
```

**Note** By default, T is a synonym for TRUE and F stands for FALSE. However, these are not reserved keywords and can be reassigned to any other values. Therefore, we advise against relying on them: they are not used throughout the course of this course.

Also, notice that the logical missing value is spelled simply as NA, and not NA\_logical\_. Both the logical NA and the numeric NA\_real\_ are, for the sake of our widely-conceived wellbeing, both *printed* as "NA" on the R console. This, however, does not mean they are identical; see Section 4.1 for discussion.

## 3.2 Comparing elements

## 3.2.1 Vectorised relational operators

Logical vectors frequently come into being as a result of various *testing* activities. In particular, the binary operators:

```
• `<` (less than),
```

- `<=` (less than or equal),
- `>` (greater than),
- `>=` (greater than or equal)
- `==` (equal),
- `!=` (not equal),

compare the corresponding elements of two numeric vectors and output a logical vector.

```
1 < 3
[1] TRUE
c(1, 2, 3, 4) == c(2, 2, 3, 8)
[1] FALSE TRUE TRUE FALSE
1:10 <= 10:1
[1] TRUE TRUE TRUE TRUE FALSE FALSE FALSE FALSE
```

Thus, they operate in an elementwise manner. Moreover, the recycling rule is applied if necessary:

```
3 < 1:5 \# c(3, 3, 3, 3, 3) < c(1, 2, 3, 4, 5)
[1] FALSE FALSE FALSE TRUE TRUE
c(1, 4) == 1:4 \# c(1, 4, 1, 4) == c(1, 2, 3, 4)
[1] TRUE FALSE FALSE TRUE
```

Therefore, we can say that they are vectorised in the same manner as the arithmetic operators `+`, `\*`, etc.; compare Section 2.4.1.

#### Testing for NA, NaN, and Inf 3.2.2

Comparisons against missing values and not-numbers yield NAs. Instead of the incorrect "x == NA\_real\_", testing for missingness should rather be performed via a call to the vectorised is.na function.

```
is.na(c(NA_real_, Inf, -Inf, NaN, -1, 0, 1))
[1] TRUE FALSE FALSE TRUE FALSE FALSE
is.na(c(TRUE, FALSE, NA, TRUE)) # works for logical vectors too
[1] FALSE FALSE TRUE FALSE
```

Moreover, is.finite is noteworthy since it returns FALSE on Infs, NA\_real\_s and NaNs.

```
is.finite(c(NA_real_, Inf, -Inf, NaN, -1, 0, 1))
[1] FALSE FALSE FALSE TRUE TRUE TRUE
```

See also the more specific is.nan and is.infinite.

### 3.2.3 Dealing with round-off errors (\*)

In mathematics, real numbers are merely an idealisation. In practice, however, it is impossible to store them with infinite precision (think  $\pi=3.141592653589793...$ ): computer memory is limited, and our time is precious.

Therefore, a consensus had to be reached. In R, we rely on the *double-precision floating* point format. The floating point part means that the numbers can be both small (close to zero like  $\pm 2.23 \times 10^{-308}$ ) and large (e.g.,  $\pm 1.79 \times 10^{308}$ ).

#### Note

These two are quite distant.

Every numeric value takes 8 bytes (or, equivalently, 64 bits) of memory. We are, however, able to store only *about* 15-17 decimal digits:

```
print(0.12345678901234567890123456789012345678901234, digits=22) # 22 is max
[1] 0.1234567890123456773699
```

which limits the precision of our computations. The *about* part is, unfortunately, due to the numbers' being written in the computer-friendly *binary*, not the human-aligned *decimal* base. This can lead to unexpected outcomes.

In particular:

• 0.1 cannot be represented exactly for it cannot be written as a finite series of reciprocals of powers of 2 (it holds  $0.1 = 2^{-4} + 2^{-5} + 2^{-8} + 2^{-9} + ...$ ). This leads to surprising results such as:

```
0.1 + 0.1 + 0.1 == 0.3
[1] FALSE
```

Quite strikingly, what follows does not show anything suspicious:

```
c(0.1, 0.1 + 0.1 + 0.1, 0.3)
[1] 0.1 0.3 0.3
```

Printing involves rounding. In the above context, it is misleading. Actually, we experience something more like:

```
print(c(0.1, 0.1 + 0.1 + 0.1, 0.3), digits=22)
[1] 0.10000000000000055511 0.300000000000000444089
[3] 0.2999999999999888978
```

• All integers between  $-2^{53}$  and  $2^{53}$  all stored *exactly*. This is good news. However, the next integer is beyond the representable range:

```
2^53 + 1 == 2^53
[1] TRUE
```

• The above suggests that the order of operations might matter. In particular, the associativity property may be violated when dealing with numbers of contrasting orders of magnitude:

```
2^53 + 2^-53 - 2^53 - 2^-53 # should be == 0.0
[1] -1.1102e-16
```

Some numbers may just be too large, too small, or too close to zero to be represented exactly:

**Important** The double-precision floating point format (IEEE 754) is not specific to R. It is used by most other computing environments, including Python and C++.

For discussion, see [32, 35, 42]. Also, [31] can be of particular interest to the general statistical/data analysis audience.

Can we do anything about these issues?

Firstly, dealing with *integers* of a *reasonable* order of magnitude (e.g., various resource or case IDs in our datasets) is *safe*. Their comparison, addition, subtraction, and multiplication are always precise.

In all other cases (including applying other operations on integers, e.g., division or **sqrt**), we need to be very careful with comparisons, especially involving testing for

equality via `==`. The sole fact that  $\sin \pi = 0$ , mathematically speaking, does not mean that we should expect that:

```
sin(pi) == 0
[1] FALSE
```

Instead, they are so close that we can *treat the difference between them as negligible*. Thus, in practice, instead of testing if x = y, we will be considering:

- |x y| (absolute error), or
- $\frac{|x-y|}{|y|}$  (relative error; which takes the order of magnitude of the numbers into account but obviously cannot be applied if y is very close to 0),

and determining if these are less than an assumed error margin,  $\varepsilon>0$ , say,  $10^{-8}$  or  $2^{-26}$ . For example:

```
abs(sin(pi) - 0) < 2^-26
[1] TRUE</pre>
```

**Note** Rounding can sometimes have a similar effect as testing for almost equality in terms of the absolute error.

```
round(sin(pi), 8) == 0
[1] TRUE
```

**Important** The above recommendations are valid for the most popular applications of R, i.e., statistical and, more generally, scientific computing<sup>1</sup>. Our datasets usually do not represent accurate measurements. Bah, the world itself is far from ideal! Therefore, we do not have to lose sleep over our not being able to precisely pinpoint the *exact* solutions.

## 3.3 Logical operations

## 3.3.1 Vectorised logical operators

The relational operators such as == and > accept only *two* arguments. Their chaining is forbidden. A test that we would mathematically write as  $0 \le x \le 1$  (or  $x \in [0,1]$ )

<sup>&</sup>lt;sup>1</sup> However, in financial applications, we had rather rely on base-10 numbers (compare the problem with 0.1 above). There are some libraries implementing higher precision floating-point numbers or even interval arithmetic that keeps track of error propagation in operation chains.

cannot be expressed as "0 <= x <= 1" in R. Therefore, we need a way to combine two logical conditions so as to be able to state that " $x \ge 0$  and, at the same time,  $x \le 1$ ".

In such situations, the following logical operators and functions come in handy:

- `!` (not, negation; unary),
- `&` (and, conjunction; are both predicates true?),
- `I` (or, alternation; is at least one true?).
- xor (exclusive-or, exclusive disjunction, either-or; is one and only one of the predicates true?).

They again act elementwisely and implement the recycling rule if necessary (and applicable).

```
x < -c(-10, -1, -0.25, 0, 0.5, 1, 5, 100)
(x >= 0) & (x <= 1)
[1] FALSE FALSE FALSE TRUE TRUE TRUE FALSE FALSE
(x < 0) | (x > 1)
[1] TRUE TRUE TRUE FALSE FALSE TRUE TRUE
!((x < 0) | (x > 1))
[1] FALSE FALSE TRUE TRUE TRUE FALSE FALSE
xor(x >= -1, x <= 1)
[1] TRUE FALSE FALSE FALSE FALSE TRUE TRUE
```

**Important** The vectorised `&` and `|` operators should not be confused with their scalar, short-circuit counterparts, `&&` and `||`; see Section 8.1.4.

## 3.3.2 Operator precedence revisited

The operators introduced in this chapter have lower precedence than the arithmetic ones, including the binary `+` and `-`. Calling help("Syntax") reveals that we can extend our listing from Section 2.4.3 as follows:

```
1. `<-` (right to left; least binding),
2. `[`,
3. `&`,
4. `!` (unary),
5. `<`,`>`,`<=`,`>=`, and`!=`,
6. `+` and `-` (binary),
7. `*` and `/`.
8. ...
```

The order of precedence is quite intuitive, e.g., " $x+1 \le y \le y \le z-1 \mid x \le z$ " means "(((x+1) <= y) & ( $y \le (z-1)$ )) | ( $x \le z$ )".

#### 3.3.3 Dealing with missingness

Operations involving missing values follow the principles of Łukasiewicz's three-valued logic, which is based on common sense. For instance, "NA | TRUE" is TRUE because the alternative (or) needs at least one argument to be TRUE to generate a positive result. On the other hand, "NA | FALSE" is NA since the outcome would be different depending on what we substituted NA for.

Let us take a moment to contemplate the logical operations' *truth tables* for all the possible combinations of inputs:

```
u <- c(TRUE, FALSE, NA, TRUE, FALSE, NA,
 TRUE, FALSE, NA)
v <- c(TRUE, TRUE, TRUE, FALSE, FALSE, NA,
 NA)
! u
[1] FALSE TRUE
 NA FALSE TRUE
 NA FALSE TRUE
u & v
[1] TRUE FALSE NA FALSE FALSE
 NA FALSE
 NA
[1] TRUE TRUE TRUE TRUE FALSE
 NA TRUE
 NA
 NΔ
xor(u, v)
[1] FALSE TRUE
 NA TRUE FALSE
 NA
 NA
 NA
 NA
```

## 3.3.4 Aggregating with all, any, and sum

Just like in the case of numeric vectors, we can summarise the contents of logical sequences. **all** tests whether *every* element in a logical vector is equal to TRUE. **any** determines if there *exists* an element that is TRUE.

```
x <- runif(10000)
all(x <= 0.2) # are all values in x <= 0.2?
[1] FALSE
any(x <= 0.2) # is there at least one element in x that is <= 0.2?
[1] TRUE
any(c(NA, FALSE, TRUE))
[1] TRUE
all(c(TRUE, TRUE, NA))
[1] NA</pre>
```

**Note** all will frequently be used in conjunction with `==`. This is because the latter, as we have said above, is itself *vectorised*: it does *not* test whether a vector *as a whole* is equal to another one.

```
z <- c(1, 2, 3)
z == 1:3 # elementwise equal
[1] TRUE TRUE TRUE
all(z == 1:3) # elementwise equal summarised
[1] TRUE</pre>
```

However, let us keep in mind the warning about the testing for *exact* equality of floating-point numbers stated in Section 3.2.3. Sometimes, considering absolute or relative errors might be more appropriate.

```
z <- sin((0:10)*pi) # sin(0), sin(pi), sin(2*pi), ..., sin(10*pi)
all(z == 0.0) # danger zone! please don't...
[1] FALSE
all(abs(z - 0.0) < 1e-8) # are the absolute errors negligible?
[1] TRUE</pre>
```

We can also call **sum** on a logical vector. Taking into account that it interprets TRUE as numeric 1 and FALSE as 0 (more on this in Section 4.1), it will give us the number of elements equal to TRUE.

```
sum(x <= 0.2) # how many elements in x are <= 0.2?
[1] 1998</pre>
```

Also, by computing sum(x)/length(x), we can obtain the proportion (fraction) of values equal to TRUE in x. Equivalently:

```
mean(x <= 0.2) # proportion of elements <= 0.2
[1] 0.1998
```

Naturally, we *expect*  $mean(runif(n) \le 0.2)$  to be equal to 0.2 (20%), but with randomness, we can never be sure.

## 3.3.5 Simplifying predicates

Each aspiring programmer needs to become fluent with the rules governing the transformations of logical conditions, e.g., that the negation of "(x >= 0) & (x < 1)" is equivalent to " $(x < 0) \mid (x >= 1)$ ". Such rules are called *tautologies*. Here are a few of them:

- !(!p) is equivalent to p (double negation),
- !(p & q) holds if and only if !p | !q (De Morgan's law),
- !(p | q) is !p & !q (another De Morgan's law),
- all(p) is equivalent to !any(!p).

Various combinations thereof are, of course, possible. Further simplifications are enabled by other properties of the binary operations:

- commutativity (symmetry), e.g., a + b = b + a, a \* b = b \* a,
- associativity, e.g., (a + b) + c = a + (b + c),  $\max(\max(a,b),c) = \max(a,\max(b,c))$ ,
- distributivity, e.g., a \* b + a \* c = a \* (b + c), min(max(a, b), max(a, c)) = max(a, min(b, c)),

and relations, including:

• transitivity, e.g., if  $a \le b$  and  $b \le c$ , then surely  $a \le c$ .

**Exercise 3.1** Assuming that a, b, and c are numeric vectors, simplify the following expressions:

- !(b>a & b<c),
- !(a>=b & b>=c & a>=c),
- a>b & a<c | a<c & a>d,
- a>b | a<=b,</li>
- a<=b & a>c | a>b & a<=c,
- a<=b & (a>c | a>b) & a<=c,</li>
- !all(a > b & b < c).

## 3.4 Choosing elements with ifelse

The **ifelse** function is a vectorised version of the scalar **if**...**else** conditional statement, which we will forgo for as long as until Chapter 8. It permits us to select an element from one of two vectors based on some logical condition.

A call to **ifelse**(l, t, f), where l is a logical vector, returns a vector y such that:

$$y_i = \left\{ \begin{array}{ll} t_i & \text{if } l_i \text{ is TRUE,} \\ f_i & \text{if } l_i \text{ is FALSE.} \end{array} \right.$$

In other words, the *i*-th element of the result vector is equal to  $t_i$  if  $l_i$  is TRUE and to  $f_i$  otherwise. For example:

```
(z <- rnorm(6)) # example vector
[1] -0.560476 -0.230177 1.558708 0.070508 0.129288 1.715065
ifelse(z >= 0, z, -z) # like abs(z)
[1] 0.560476 0.230177 1.558708 0.070508 0.129288 1.715065
```

```
(x <- rnorm(6)) # example vector
[1] 0.46092 -1.26506 -0.68685 -0.44566 1.22408 0.35981
(y <- rnorm(6)) # example vector
[1] 0.40077 0.11068 -0.55584 1.78691 0.49785 -1.96662
ifelse(x >= y, x, y) # like pmax(x, y)
[1] 0.46092 0.11068 -0.55584 1.78691 1.22408 0.35981
```

We should not be surprised anymore that the recycling rule is fired up when necessary:

```
ifelse(x > 0, x^2, 0) # squares of positive xs and 0 otherwise
[1] 0.21244 0.00000 0.00000 0.00000 1.49838 0.12947
```

**Note** All arguments are evaluated in their entirety before deciding on which elements are selected. Therefore, the following call generates a warning:

```
ifelse(z >= 0, log(z), NA_real_)
Warning in log(z): NaNs produced
[1] NA NA 0.44386 -2.65202 -2.04571 0.53945
```

This is because, with **log**(z), we compute the logarithms of negative values anyway. To fix this, we can write:

```
log(ifelse(z >= 0, z, NA_real_))
[1] NA NA 0.44386 -2.65202 -2.04571 0.53945
```

In case we yearn for an **if...else if...else**-type expression, the calls to **ifelse** can naturally be nested.

**Example 3.2** A version of pmax(pmax(x, y), z) can be written as:

```
ifelse(x >= y,
 ifelse(z >= x, z, x),
 ifelse(z >= y, z, y)
)
[1] 0.46092 0.11068 1.55871 1.78691 1.22408 1.71506
```

However, determining three intermediate logical vectors is not necessary. We can save one call to `>=` by introducing an auxiliary variable:

```
xy <- ifelse(x >= y, x, y)
ifelse(z >= xy, z, xy)
[1] 0.46092 0.11068 1.55871 1.78691 1.22408 1.71506
```

**Exercise 3.3** Figure 3.1 depicts a realisation of the mixture Z = 0.2X + 0.8Y of two normal distributions  $X \sim N(-2, 0.5)$  and  $Y \sim N(3, 1)$ .

```
n <- 100000
z <- ifelse(runif(n) <= 0.2, rnorm(n, -2, 0.5), rnorm(n, 3, 1))
hist(z, breaks=101, probability=TRUE, main="", col="white")</pre>
```

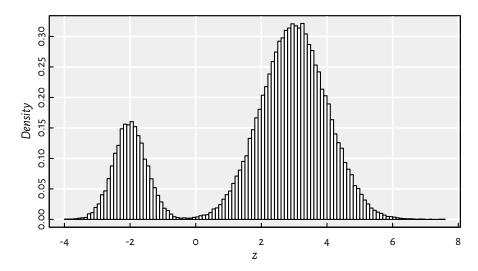


Figure 3.1. A mixture of two Gaussians generated with ifelse.

In other words, we generated a variate from the normal distribution that has the expected value of -2 with probability 20%, and from the one with the expectation of 3 otherwise.

*Inspired by the above, generate the following Gaussian mixtures:* 

- $\frac{2}{3}X + \frac{1}{3}Y$ , where  $X \sim N(100, 16)$  and  $Y \sim N(116, 8)$ ,
- 0.3X + 0.4Y + 0.3Z, where  $X \sim N(-10, 2)$ ,  $Y \sim N(0, 2)$ , and  $Z \sim N(10, 2)$ .

(\*) On a side note, knowing that if X follows N(0,1), then the scaled-shifted  $\sigma X + \mu$  is distributed  $N(\mu,\sigma)$ , the above can be equivalently written as:

```
w <- (runif(n) <= 0.2)
z <- rnorm(n, 0, 1)*ifelse(w, 0.5, 1) + ifelse(w, -2, 3)</pre>
```

#### 3.5 Exercises

**Exercise 3.4** *Answer the following questions.* 

• Why the statement "The Earth is flat or the smallpox vaccine is proven effective" is obviously true?

- What is the difference between NA and NA\_real\_?
- Why is "FALSE & NA" equal to FALSE, but "TRUE & NA" is NA?
- Why has **ifelse**(x>=0, **sqrt**(x), NA\_real\_) a tendency to generate warnings and how to rewrite it so as to prevent that from happening?
- What is the interpretation of **mean**( $x \ge 0 & x <= 1$ )?
- For some integer x and y, how to verify whether 0 < x < 100, 0 < y < 100, and x < y, all at the same time?
- Mathematically, for all real x, y > 0, it holds  $\log xy = \log x + \log y$ . Why then  $all(\log(x*y)) = \log(x) + \log(y)$  can sometimes return FALSE? How to fix this?
- Is x/y/z always equal to x/(y/z)? How to fix this?
- What is the purpose of very specific functions such as **log1p** and **expm1** (see their help page) and many others listed in, e.g., the GNU GSL library [28]? Is our referring to them a violation of the beloved "do not multiply entities without necessity" rule?
- If we know that x may be subject to error, how to test whether x > 0 in a robust manner?
- Is "y<-5" the same as "y <- 5" or rather "y < -5"?

Exercise 3.5 What is the difference between all and isTRUE? What about `==`, identical, and all.equal? Is the last one properly vectorised?

**Exercise 3.6** Compute the cross-entropy loss between a numeric vector p with values in the interval (0,1) and a logical vector y, both of length n (you can generate them randomly or manually, it does not matter, it is just an exercise):

$$\mathcal{L}(\boldsymbol{p},\boldsymbol{y}) = \frac{1}{n} \sum_{i=1}^{n} \ell_i,$$

where

$$\ell_i = \left\{ \begin{array}{ll} -\log p_i & \text{if } y_i \text{ is TRUE,} \\ -\log (1-p_i) & \text{if } y_i \text{ is FALSE.} \end{array} \right.$$

Interpretation: in classification problems,  $y_i \in \{FALSE, TRUE\}$  denotes the true class of the ith object (say, whether the i-th hospital patient is symptomatic) and  $p_i \in (0,1)$  is a machine learning algorithm's confidence that i belongs to class TRUE (e.g., how sure a decision tree model is that the corresponding person is unwell). Ideally, if  $y_i$  is TRUE,  $p_i$  should be close to 1 and to 0 otherwise. The cross-entropy loss quantifies by how much a classifier differs from the omniscient one. The use of the logarithm penalises strong beliefs in the wrong answer.

By the way, if we have solved any of the exercises encountered so far by referring to **if** statements, **for** loops, vector indexing like x[...], or any external R package, we recommend to go back and rewrite our code. Let us keep things simple (effective, readable) by only using *base* R's vectorised operations that we have introduced.

# Lists and attributes

After two brain-teasing chapters, it is time to cool it down a little. In this more technical part, we will introduce *lists*, which serve as universal containers for R objects of any size and type. Moreover, we will also show that each R object can be equipped with a number of optional *attributes*. Thanks to them, we will be able to label elements in any vector, and, in Chapter 10, introduce new complex data types such as matrices and data frames.

## 4.1 Type hierarchy and conversion

So far, we have been playing with three types of atomic vectors:

- 1. logical (Chapter 3),
- 2. numeric (Chapter 2),
- 3. character (which we have barely touched upon yet, but rest assured that they will be covered in detail very soon; see Chapter 6).

To determine the type of an object programmatically, we can call the **typeof** function.

```
typeof(c(1, 2, 3))
[1] "double"
typeof(c(TRUE, FALSE, TRUE, NA))
[1] "logical"
typeof(c("spam", "spam", "bacon", "eggs", "spam"))
[1] "character"
```

It turns out that we can easily convert between these types, either on our explicit demand (*type casting*) or on-the-fly (*coercion*, when we perform an operation that expects something different from the kind of input it was fed with).

**Note** (\*) Numeric vectors are reported as being either of the type double (double-precision floating-point numbers) or integer (32-bit; it is a subset of double); see Section 6.4.1. In most practical cases, this is a technical detail that we can risklessly ignore; compare also the **mode** function.

### 4.1.1 Explicit type casting

We can use functions such as **as.logical**, **as.numeric**<sup>1</sup>, and **as.character** to *convert* given objects to the corresponding types.

```
as.numeric(c(TRUE, FALSE, NA, TRUE, NA, FALSE)) # synonym: as.double
[1] 1 0 NA 1 NA 0
as.logical(c(-2, -1, 0, 1, 2, 3, NA_real_, -Inf, NaN))
[1] TRUE TRUE FALSE TRUE TRUE TRUE NA TRUE NA
```

**Important** It is easily seen that the rules are:

```
• TRUE \rightarrow 1,
```

- FALSE → O,
- NA → NA real ,

#### and:

- O → FALSE,
- NA\_real\_ and NaN → NA,
- anything else → TRUE.

The distinction between zero and non-zero is commonly applied in other programming languages as well.

Moreover, in the case of the conversion involving character strings, we have:

```
as.character(c(TRUE, FALSE, NA, TRUE, NA, FALSE))
[1] "TRUE" "FALSE" NA "TRUE" NA
 "FALSE"
as.character(c(-2, -1, 0, 1, 2, 3, NA_real_, -Inf, NaN))
 "-1" "O"
 "1"
 "2" "3" NA
[1] "-2"
 "-Inf" "NaN"
as.logical(c("TRUE", "True", "true", "T",
 "FALSE", "False", "false", "F",
 "anything other than these", NA_character_))
[1] TRUE TRUE TRUE TRUE FALSE FALSE FALSE
as.numeric(c("0", "-1.23e4", "pi", "2+2", "NaN", "-Inf", NA_character_))
Warning: NAs introduced by coercion
 NA
[1]
 0 -12300
 NaN
 -Inf
 NA
```

<sup>1 (\*)</sup> as.numeric is a built-in generic function identical to (synonymous with) as.double; see Section 10.2.3. is.numeric is generic too, and is more universal than is.double, which only verifies whether typeof returns "double". For instance, vectors of the type integer which we mention later are considered numeric as well.

#### 4.1.2 Implicit conversion (coercion)

Recall that we referred to the three vector types as *atomic* ones. They can only be used to store elements of the *same type*.

If we make an attempt at composing an object of mixed types with **c**, the common type will be determined in such a way that data are stored without information loss:

```
c(-1, FALSE, TRUE, 2, "three", NA)
[1] "-1" "FALSE" "TRUE" "2" "three" NA
c("zero", TRUE, NA)
[1] "zero" "TRUE" NA
c(-1, FALSE, TRUE, 2, NA)
[1] -1 0 1 2 NA
```

Hence, we see that logical is the most specialised of the tree, whereas character is the most general.

**Note** The logical NA is converted to NA\_real\_ and NA\_character\_ in the above examples. R users tend to rely on implicit type conversion when they write **c**(1, 2, NA, 4) rather than **c**(1, 2, NA\_real\_, 4). In most cases, this is fine, but it might make us less vigilant.

However, occasionally, it will be wiser to be more unequivocal. For instance, rep(NA\_real\_, 1e9) preallocates a long numeric vector instead of a logical one.

Some functions that expect vectors of specific types can apply coercion by themselves (or act as if they do so):

```
c(NA, FALSE, TRUE) + 10 # implicit conversion logical -> numeric
[1] NA 10 11
c(-1, 0, 1) & TRUE # implicit conversion numeric -> logical
[1] TRUE FALSE TRUE
sum(c(TRUE, TRUE, FALSE, TRUE, FALSE)) # same as sum(as.numeric(...))
[1] 3
cumsum(c(TRUE, TRUE, FALSE, TRUE, FALSE))
[1] 1 2 2 3 3
cummin(c(TRUE, TRUE, FALSE, TRUE, FALSE))
[1] 1 1 0 0 0
```

**Exercise 4.1** In one of the previous exercises, we computed the cross-entropy loss between a logical vector  $\mathbf{y} \in \{0,1\}^n$  and a numeric vector  $\mathbf{p} \in (0,1)^n$ . This measure can be equivalently defined as:

$$\mathcal{L}(\pmb{p},\pmb{y}) = -\frac{1}{n} \left( \sum_{i=1}^n y_i \log(p_i) + (1-y_i) \log(1-p_i) \right).$$

Implement the above formula (using vectorised operations, but not relying on **ifelse** this time)

and compute the cross-entropy loss between, for instance, " $y \leftarrow sample(c(FALSE, TRUE), n)$ " and " $p \leftarrow runif(n)$ " for some n. Note how seamlessly we translate between FALSE/TRUEs and o/1s in the above equation (in particular, where  $1 - y_i$  means the logical negation of  $y_i$ ).

#### 4.2 Lists

Lists are generalised vectors. They can be comprised of R objects of any kind, also other lists. It is why we classify them as *recursive* (and not atomic) objects. They are especially useful wherever there is a need to handle some *multitude* as a single entity.

#### 4.2.1 Creating lists

The most straightforward way to create a list is by means of the **list** function:

```
list(1, 2, 3)
[[1]]
[1] 1
##
[[2]]
[1] 2
##
[[3]]
[1] 3
```

Notice that the above is not the same as **c**(1, 2, 3). We got a sequence that wraps three numeric vectors, each of length one. More examples:

```
list(1:3, 4, c(TRUE, FALSE, NA, TRUE), "and so forth") # different types
[[1]]
[1] 1 2 3
##
[[2]]
[1] 4
##
[[3]]
[1] TRUE FALSE NA TRUE
##
[[4]]
[1] "and so forth"
list(list(c(TRUE, FALSE, NA, TRUE), letters), list(1:3)) # a list of lists
[[1]]
[[1]][[1]]
[1] TRUE FALSE
 NA TRUE
```

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```
##
[[1]][[2]]
[1] "a" "b" "c" "d" "e" "f" "g" "h" "i" "j" "k" "l" "m" "n" "o" "p" "q"
[18] "r" "s" "t" "u" "v" "w" "x" "y" "z"
##
##
##
##
##
##
[[2]]
[[2]][[1]]
[1] 1 2 3
```

The display of lists is (un)pretty bloated. However, the **str** function prints any R object in a more concise fashion:

```
str(list(list(c(TRUE, FALSE, NA, TRUE), letters), list(1:3)))
List of 2
$:List of 2
..$: logi [1:4] TRUE FALSE NA TRUE
..$: chr [1:26] "a" "b" "c" "d" ...
$:List of 1
..$: int [1:3] 1 2 3
```

**Note** In Section 4.1, we said that the **c** function, when fed with arguments of mixed types, tries to determine the common type that retains the sense of data. If coercion to an atomic vector is not possible, the result will be a list.

```
c(1, "two", identity) # `identity` is an object of the type "function"
[[1]]
[1] 1
##
[[2]]
[1] "two"
##
[[3]]
function (x)
x
<environment: namespace:base>
```

Thus, the **c** function can also be used to concatenate lists:

```
c(list(1), list(2), list(3)) # three lists -> one list
[[1]]
[1] 1
##
```

(continues on next page)

I DEEP

```
[[2]]
[1] 2
##
[[3]]
[1] 3
```

Lists can be repeated using **rep**:

```
rep(list(1:11, LETTERS), 2)

[[1]]

[1] 1 2 3 4 5 6 7 8 9 10 11

##

[[2]]

[1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q"

[13] "# [1] 1 2 3 4 5 6 7 8 9 10 11

##

[[4]]

[1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q"

[18] "R" "S" "T" "U" "V" "W" "X" "Y" "Z"
```

# 4.2.2 Converting to and from lists

The conversion of an atomic vector to a list of vectors of length one can be done via a call to as.list:

```
as.list(c(1, 2, 3)) # vector of length 3 -> list of 3 vectors of length 1
[[1]]
[1] 1
##
[[2]]
[1] 2
##
[[3]]
[1] 3
```

Unfortunately, calling, say, **as.numeric** on a list arouses an error, even if it is comprised of numeric vectors only. We can try flattening it to an atomic sequence by calling **unlist**:

```
unlist(list(list(1, 2), list(3, list(4:8)), 9))
[1] 1 2 3 4 5 6 7 8 9
(continues on next page)
```

(continued from previous page)

```
unlist(list(1, 2), list(3, list(4:8)), "spam"))
[1] "1" "2" "3" "4" "5" "6" "7" "8" "spam"
```

**Note** (\*) Chapter 11 will mention the **simplify2array** function, which generalises **unlist** in a way that can sometimes give rise to a matrix.

#### **4.3 NULL**

NULL, being the one and only instance of the eponymous type, can be used as a place-holder for an R object or designate the absence of any entities whatsoever.

```
list(NULL, NULL, month.name)
[[1]]
NULL
##
[[2]]
NULL
##
[[3]]
[1] "January"
 "March"
 "April"
 "May"
 "February"
[6] "June"
 "July"
 "September" "October"
 "August"
[11] "November"
 "December"
```

NULL is different from a vector of length zero because the latter has a type. However, NULL sometimes *behaves* like a zero-length vector. In particular, **length**(NULL) returns o. Also, **c** called with no arguments returns NULL.

Testing for NULL-ness can be done with a call to **is.null**.

**Important** NULL is not the same as NA or it is other-typed variants. The former cannot be emplaced in an atomic vector.

```
c(1, NA, 3, NULL, 5) # NULL behaves like a zero-length vector here ## [1] 1 NA 3 5
```

They have very distinct semantics (no value vs a missing value).

Later we will see that some functions return NULL invisibly when they have nothing interesting to report. This is the case of **print** or **plot**, which are called because of their side effects (printing and plotting).

Furthermore, in certain contexts, replacing content with NULL will actually result in its removal, e.g., when subsetting a list.

# 4.4 Object attributes

Lists can embrace many entities in the form of a single item sequence. Attributes, on the other hand, give means to inject *extra* data into an object.

Attributes are unordered key=value pairs, where key is a single string, and value is any R object except NULL. They can be introduced by calling, amongst others<sup>2</sup>, the **structure** function:

```
x_simple <- 1:10
x <- structure(
 x_simple, # the object to be equipped with attributes
 attribute1="value1",
 attribute2=c(6, 100, 324)
)</pre>
```

#### 4.4.1 Developing perceptual indifference to most attributes

Let us see how the above x is reported on the console:

```
print(x)
[1] 1 2 3 4 5 6 7 8 9 10
attr(,"attribute1")
[1] "value1"
attr(,"attribute2")
[1] 6 100 324
```

The object of concern, 1:10, was displayed first. We need to get used to that. Most of the time, we suggest to treat the "attr..." parts of the display as if they were printed in tiny font.

Equipping an object with attributes does not usually change its nature; see, however, Chapter 10 for a few exceptions. The above x is still treated as an ordinary sequence of numbers by most functions:

```
sum(x) # the same as sum(1:10); `sum` does not care about any attributes
[1] 55
typeof(x) # just a numeric vector, but with some perks
[1] "integer"
```

<sup>&</sup>lt;sup>2</sup> Other ways include the replacement versions of the attr and attributes functions; see Section 9.3.6.

**Important** Attributes are generally ignored by most functions unless they have specifically been programmed to pay attention to them.

#### 4.4.2 But there are a few use cases

Some R functions add attributes to the return value to sneak extra information that *might* be useful, just in case.

For instance, na.omit, whose main aim is to remove missing values from an atomic vector, yields:

```
y <- c(10, 20, NA, 40, 50, NA, 70)
(y_na_free <- na.omit(y))
[1] 10 20 40 50 70
attr(,"na.action")
[1] 3 6
attr(,"class")
[1] "omit"</pre>
```

We can enjoy the NA-free version of y in any further computations:

```
mean(y_na_free)
[1] 38
```

Additionally, the na.action attribute tells us where the missing observations were:

```
attr(y_na_free, "na.action") # read the attribute value
[1] 3 6
attr(,"class")
[1] "omit"
```

We ignore the class part until Chapter 10.

As another example, **gregexpr** discussed in Chapter 6 searches for a given pattern in a character vector:

```
needle <- "spam|durian" # pattern to search for: spam OR durian
haystack <- c("spam, bacon, and durian-flavoured spam", "spammer") # text
(pos <- gregexpr(needle, haystack, perl=TRUE))
[[1]]
[1] 1 18 35
attr(, "match.length")
[1] 4 6 4
attr(, "index.type")
[1] "chars"
attr(, "useBytes")</pre>
```

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```
[1] TRUE
##
[[2]]
[1] 1
attr(,"match.length")
[1] 4
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
```

We sought all occurrences of the pattern within two character strings. As their number may vary from string to string, wrapping the results in a list was a good design choice. Each list element gives the starting positions where matches can be found: there are three and one match(es), respectively. Moreover, every vector of positions has a designated match.length attribute (amongst others), in case we need it.

Exercise 4.2 Create a list with EUR/AUD, EUR/GBP, and EUR/USD exchange rates read from the euraud-\*.csv, eurgbp-\*.csv, and eurusd-\*.csv files in our data repository<sup>3</sup>. Each of its three elements should be a numeric vector storing the currency exchange rates. Furthermore, equip them with currency\_from, currency\_to, date\_from, and date\_to attributes. For example:

```
NA 1.6119 1.6251 1.6195 1.6193 1.6132
[1]
 NA 1.6006 1.6031
 NA
[11]
 NA
 NA 1.6117 1.6110 1.6188 1.6115 1.6122
 NA
attr(,"currency_from")
[1] "EUR"
attr(,"currency_to")
[1] "AUD"
attr(,"date_from")
[1] "2020-01-01"
attr(,"date_to")
[1] "2020-06-30"
```

Such an additional piece of information could be stored in a few separate variables (other vectors), but then it would not be as convenient to use as the above representation.

#### Special attributes 4.4.3

Attributes have great potential which is somewhat wasted, for R users rarely know:

- that attributes exist (pessimistic scenario), or
- how to handle them (realistic scenario).

But we know now.

<sup>3</sup> https://github.com/gagolews/teaching-data/tree/master/marek

What is more, certain attributes have been predestined to play a unique role in R. Namely, the most prevalent amongst the *special attributes* are:

- names, row.names, and dimnames are used to label the elements of atomic and generic vectors (see below) as well as rows and columns in matrices (Chapter 11) and data frames (Chapter 12),
- dim turns flat vectors into matrices and other tensors (Chapter 11),
- levels labels the underlying integer codes in factor objects (Section 10.3.2),
- class can be used to bring forth new complex data structures based on basic types (Chapter 10).

We call them *special* because:

- they cannot be assigned arbitrary values; for instance, we will soon see that names
  can accept a character vector of a specific length,
- they can be accessed via designated functions, e.g., names, class, dim, dimnames, levels, etc.,
- they are widely recognised by many other functions.

However, in spite of the above, special attributes can still be managed as ordinary ones.

**Exercise 4.3** comment is perhaps the most rarely used special attribute. Create an object (whatever) equipped with the comment attribute. Verify that assigning to it anything other than a character vector leads to an error. Read its value by calling the **comment** function. Display the object equipped with this attribute. Note that the **print** function ignores its existence whatsoever: this is how special it is.

**Important** (\*) The accessor functions such as names or class might return meaningful values, even if the corresponding attribute is not set explicitly; see, e.g., Section 11.1.5 for an example.

# 4.4.4 Labelling vector elements with the names attribute

The special attribute names labels atomic vectors' and lists' elements.

```
(x <- structure(c(13, 2, 6), names=c("spam", "sausage", "celery")))
spam sausage celery
13 2 6</pre>
```

The labels may improve the expressivity and readability of our code and data.

**Exercise 4.4** Verify that the above x is still an ordinary numeric vector by calling **typeof** and **sum** on it.

Let us stress that we can ignore the names attribute whatsoever. If we apply any operation discussed in Chapter 2, we will garner the same result regardless whether such extra information is present or not.

It is just the **print** function that changed its behaviour slightly. After all, it is a special attribute. Instead of reporting:

```
[1] 13 2 6
attr(,"names")
[1] "spam" "sausage" "celery"
```

we got a nicely formatted table-like display. Non-special attributes are still printed in the standard way:

```
structure(x, additional_attribute=1:10)
spam sausage celery
13 2 6
attr(,"additional_attribute")
[1] 1 2 3 4 5 6 7 8 9 10
```

**Note** Chapter 5 will also mention that some operations (such as indexing) gain superpowers in the presence of the names attribute.

This attribute can be read by calling:

```
attr(x, "names") # just like any other attribute
[1] "spam" "sausage" "celery"
names(x) # because it is so special
[1] "spam" "sausage" "celery"
```

Named vectors can be easily created with the **c** and **list** functions as well:

```
c(a=1, b=2)
a b
1 2
list(a=1, b=2)
$a
[1] 1
##
$b
[1] 2
c(a=c(x=1, y=2), b=3, c=c(z=4)) # this is smart
a.x a.y b c.z
1 2 3 4
```

Let us contemplate how a named list is printed on the console. Again, it is still a list, but with some extras.

**Exercise 4.5** A whole lot of functions return named vectors. Evaluate the following expressions and read the corresponding pages in their documentation:

- quantile(runif(100)),
- hist(runif(100), plot=FALSE),
- options (take note of the digits, scipen, max.print, and width options),
- capabilities.

**Note** (\*) Most of the time, lists are used merely as *containers* for other R objects. This is a boring yet essential role. However, let us just mention here that every data frame is, in fact, a generic vector (see Chapter 12). Each column corresponds to a named list element:

```
(df <- head(iris)) # some data frame</pre>
 Sepal.Length Sepal.Width Petal.Length Petal.Width Species
 5.1
1
 3.5
 1.4
 0.2 setosa
 4.9
2
 3.0
 1.4
 0.2 setosa
3
 4.7
 3.2
 1.3
 0.2 setosa
4
 4.6
 3.1
 1.5
 0.2 setosa
5
 5.0
 3.6
 1.4
 0.2 setosa
6
 5.4
 3.9
 1.7
 0.4 setosa
typeof(df) # it is just a list (with extras that will be discussed later)
[1] "list"
unclass(df) # how it is represented exactly (without the extras)
$Sepal.Length
[1] 5.1 4.9 4.7 4.6 5.0 5.4
##
$Sepal.Width
[1] 3.5 3.0 3.2 3.1 3.6 3.9
##
$Petal.Length
[1] 1.4 1.4 1.3 1.5 1.4 1.7
$Petal.Width
[1] 0.2 0.2 0.2 0.2 0.2 0.4
##
$Species
[1] setosa setosa setosa setosa setosa
Levels: setosa versicolor virginica
attr(,"row.names")
[1] 1 2 3 4 5 6
```

Therefore, the functions we discuss in this chapter are of use in processing such structured data too.

#### 4.4.5 Altering and removing attributes

We know that a single attribute can be read by calling attr. Their whole list is generated with a call to attributes.

```
(x <- structure(c("some", "object"), names=c("X", "Y"),</pre>
 attribute1="value1", attribute2="value2", attribute3="value3"))
##
 "some" "object"
##
attr(,"attribute1")
[1] "value1"
attr(, "attribute2")
[1] "value2"
attr(,"attribute3")
[1] "value3"
attr(x, "attribute1") # reads a single attribute, returns NULL if unset
[1] "value1"
attributes(x) # returns a named list with all attributes of an object
$names
[1] "X" "Y"
##
$attribute1
[1] "value1"
##
$attribute2
[1] "value2"
##
$attribute3
[1] "value3"
```

We can alter an attribute's value or add further attributes by referring to the structure function once again. Moreover, setting an attribute's value to NULL gets rid of it completely.

```
structure(x, attribute1=NULL, attribute4="added", attribute3="modified")
##
 Χ
 "some" "object"
attr(, "attribute2")
[1] "value2"
attr(, "attribute3")
[1] "modified"
```

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```
attr(,"attribute4")
[1] "added"
```

As far as the names attribute is concerned, we may generate an unnamed copy of an object by calling:

```
unname(x)
[1] "some" "object"
attr(,"attribute1")
[1] "value1"
attr(,"attribute2")
[1] "value2"
attr(,"attribute3")
[1] "value3"
```

In Section 9.3.6, we will introduce *replacement functions*. They will enable us to modify or remove an object's attribute by calling "attr(x, "some\_attribute") <- new\_value".

Moreover, Section 5.5 highlights that certain operations (such as vector indexing, elementwise arithmetic operations, and coercion) might not preserve all attributes of the objects that were given as their inputs.

#### 4.5 Exercises

**Exercise 4.6** *Provide an answer to the following questions.* 

- What is the meaning of c(TRUE, FALSE)\*1:10?
- What does **sum(as.logical**(x)) compute when x is a numeric vector?
- We said that atomic vectors of the type character are the most general ones. Therefore, is
   as.numeric(as.character(x)) the same as as.numeric(x), regardless of the type of x?
- What is the meaning of **as.logical**(x+y) if x and y are logical vectors? What about **as.** logical(x\*y), as.logical(1-x), and as.logical(x!=y)?
- What is the meaning of the following when x is a logical vector?
  - cummin(x) and cummin(!x),
  - cummax(x) and cummax(!x),
  - cumsum(x) and cumsum(!x),
  - cumprod(x) and cumprod(!x).
- Let x be a named numeric vector, e.g., "x <- quantile(runif(100))". What is the result
  of 2\*x, mean(x), and round(x, 2)?</li>

- What is the meaning of x == NULL?
- Give two ways to create a named character vector.
- Give two ways (discussed above; there are more) to remove the names attribute from an object.

**Exercise 4.7** There are a few peculiarities when joining or coercing lists. Compare the results generated by the following pairs of expressions:

```
1)
as.character(list(list(1, 2), list(3, list(4)), 5))
as.character(unlist(list(list(1, 2), list(3, list(4)), 5)))
2)
as.numeric(list(list(1, 2), list(3, list(4)), 5))
as.numeric(unlist(list(list(1, 2), list(3, list(4)), 5)))
3)
unlist(list(list(1, 2), sd))
list(1, 2, sd)
4)
c(list(c(1, 2), 3), 4, 5)
c(list(c(1, 2), 3), c(4, 5))
```

**Exercise 4.8** Given numeric vectors x, y, z, and w, how to combine x, y, and list(z, w) so as to obtain list(x, y, z, w)? More generally, given a set of atomic vectors and lists of atomic vectors, how to combine them to obtain a single list of atomic vectors (not a list of atomic vectors and lists, not atomic vectors unwound, etc.)?

**Exercise 4.9** readRDS serialises R objects and writes their snapshots to disk so that they can be restored via a call to **saveRDS** at a later time. Verify that this function preserves object attributes. Also, check out **dput** and **dget** which work with objects' textual representation in the form executable R code.

**Exercise 4.10** (\*) Use **jsonlite**::**fromJSON** to read a JSON file in the form of a named list.

In the extremely unlikely event of our finding the current chapter boring, let us rejoice: some of the exercises and remarks that we will encounter in the next part, which is devoted to vector indexing, will definitely be deliciously stimulating!

# Vector indexing

We now know plenty of ways to process vectors in their entirety, but how to extract and replace their specific parts? We will be collectively referring to such activities as indexing. This is because they are often performed through the index operator, `[`.

#### 5.1 head and tail

Let us begin with something more lightweight, though. The **head** function fetches a few elements from the beginning of a vector.

```
x <- 1:10
head(x) # head(x, 6)
[1] 1 2 3 4 5 6
head(x, 3) # get the first three
[1] 1 2 3
head(x, -3) # skip the last three
[1] 1 2 3 4 5 6 7</pre>
```

Similarly, tail extracts a few elements from the end of a sequence.

```
tail(x) # tail(x, 6)
[1] 5 6 7 8 9 10
tail(x, 3) # get the last three
[1] 8 9 10
tail(x, -3) # skip the first three
[1] 4 5 6 7 8 9 10
```

Both functions work on lists too<sup>1</sup>. They are useful, e.g., when we wish to preview the contents of a *big* object.

<sup>&</sup>lt;sup>1</sup> head and tail are actually S3 generics defined in the utils package. We will be able to call them on matrices and data frames as well; see Chapter 10.

#### 5.2 Subsetting and extracting from vectors

Given a vector x, x[i] returns its subset comprised of elements indicated by the indexer i, which can be a *single* vector of:

- nonnegative integers (gives the positions of elements to retrieve),
- negative integers (gives the positions to omit),
- logical values (states which items should be fetched or skipped),
- character strings (locates the elements with specific names).

#### 5.2.1 Nonnegative indexes

Consider the following example vectors:

```
(x <- seq(10, 100, 10))
[1] 10 20 30 40 50 60 70 80 90 100
(y <- list(1, 11:12, 21:23))
[1]]
[1] 1
##
[[2]]
[1] 11 12
##
[[3]]
[1] 21 22 23</pre>
```

The first element in a vector is at index 1. Hence:

```
x[1] # the first element
[1] 10
x[length(x)] # the last element
[1] 100
```

**Important** We might have wondered why "[1]" is displayed each time we print out an atomic vector on the console:

```
print((1:51)*10)
[1] 10 20 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170
[18] 180 190 200 210 220 230 240 250 260 270 280 290 300 310 320 330 340
[35] 350 360 370 380 390 400 410 420 430 440 450 460 470 480 490 500 510
```

It is merely a visual hint indicating which vector element we output first in each line.

Vectorisation is a universal feature of R. It comes as no surprise that the indexer can also be of length greater than one.

```
x[c(1, length(x))] # the first and the last
[1] 10 100
x[1:3] # the first three
[1] 10 20 30
```

Take note of the boundary cases:

```
x[c(1, 2, 1, 0, 3, NA_real_, 1, 11)] # repeated, 0, missing, out of bound
[1] 10 20 10 30 NA 10 NA
x[c()] # indexing by an empty vector
numeric(0)
```

When applied on lists, the index operator always returns a list as well, even if we ask for a single element:

```
y[2] # a list that includes the second element
[[1]]
[1] 11 12
y[c(1, 3)] # not the same as x[1, 3] (a different story)
[[1]]
[1] 1
##
[[2]]
[1] 21 22 23
```

If we wish to *extract* a component, i.e., to dig into what is inside a list at a specific location, we can refer to `[[`:

```
y[[2]] # extract the second element
[1] 11 12
```

This is exactly why R displays "[[1]]", "[[2]]", etc. when lists are printed.

On a side note, calling x[[i]] on an *atomic* vector, where i is a single value, has almost<sup>2</sup> the same effect as x[i]. However, [[i]] generates an error if the subscript is out of bounds.

**Important** Let us reflect on the operators' behaviour in the case of nonexistent items:

```
c(1, 2, 3)[4]
[1] NA
list(1, 2, 3)[4]
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```

<sup>&</sup>lt;sup>2</sup> See also Section 5.5 for the discussion on the preservation of object attributes.

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```
[[1]]
NULL
c(1, 2, 3)[[4]]
Error in c(1, 2, 3)[[4]]: subscript out of bounds
list(1, 2, 3)[[4]]
Error in list(1, 2, 3)[[4]]: subscript out of bounds
```

**Note** (\*) `[[` also supports multiple indexers.

```
y[[c(1, 3)]]
Error in y[[c(1, 3)]]: subscript out of bounds
```

Its meaning is different from y[c(1, 3)], though; we are about to extract a single value, remember? Here, indexing is applied recursively. Namely, the above is equivalent to y[[1]][[3]]. We got an error because y[[1]] is of a length smaller than three.

More examples:

```
y[[c(3, 1)]] # y[[3]][[1]]
[1] 21
list(list(7))[[c(1, 1)]] # 7, not list(7)
[1] 7
```

#### 5.2.2 Negative indexes

The indexer can also be a vector of negative integers. This way, we can exclude the elements at given positions:

```
y[-1] # all but the first
[[1]]
[1] 11 12
##
[[2]]
[1] 21 22 23
x[-(1:3)] # all but the first three
[1] 40 50 60 70 80 90 100
x[-c(1, 0, 2, 1, 1, 8:100)] # 0, repeated, out of bound indexes
[1] 30 40 50 60 70
```

**Note** Negative and positive indexes cannot be mixed.

```
x[-1:3] # recall that -1:3 == (-1):3
Error in x[-1:3]: only 0's may be mixed with negative subscripts
```

Also, NA indexes cannot be mixed with negative ones.

# 5.2.3 Logical indexer

A vector can also be subsetted by means of a logical vector. If they both are of identical lengths, the consecutive elements in the latter indicate whether the corresponding elements of the indexed vector are supposed to be selected (TRUE) or omitted (FALSE).

```
1*** 2 3 4 5*** 6*** 7 8*** 9? 10***

x[c(TRUE, FALSE, FALSE, TRUE, TRUE, FALSE, TRUE, NA, TRUE)]

[1] 10 50 60 80 NA 100
```

In other words, x[l], where l is a logical vector, returns all x[i] with i such that l[i] is TRUE. Above, we extracted the elements at indexes 1, 5, 6, 8, and 10.

**Important** Let us be careful: if the element selector is NA, the selected element will be set to a missing value (for atomic vectors) or NULL (for lists).

```
c("one", "two", "three")[c(NA, TRUE, FALSE)]
[1] NA "two"
list("one", "two", "three")[c(NA, TRUE, FALSE)]
[[1]]
NULL
##
[[2]]
[1] "two"
```

This, lamentably, comes with no warning, which might be problematic when indexers are generated programmatically. As a remedy, we sometimes pass the logical indexer to the **which** function first. It returns the indexes of the elements equal to TRUE, ignoring the missing ones.

```
which(c(NA, TRUE, FALSE, TRUE, FALSE, NA, TRUE))
[1] 2 4 7
c("one", "two", "three")[which(c(NA, TRUE, FALSE))]
[1] "two"
```

Recall that in Chapter 3, we discussed ample vectorised operations that generate logical vectors. Anything that yields a logical vector of the same length as x can be passed as an indexer.

```
x > 60 # yes, it is a perfect indexer candidate
[1] FALSE FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE
x[x > 60] # select elements in `x` that are greater than 60
[1] 70 80 90 100
x[x < 30 | 70 < x] # elements not between 30 and 70
[1] 10 20 80 90 100
x[x < mean(x)] # elements smaller than the mean
[1] 10 20 30 40 50
x[x^2 > 7777 | log10(x) <= 1.6] # indexing via a transformed version of `x`
[1] 10 20 30 90 100
(z <- round(runif(length(x)), 2)) # ten pseudorandom numbers
[1] 0.29 0.79 0.41 0.88 0.94 0.05 0.53 0.89 0.55 0.46
x[z <= 0.5] # indexing based on `z`, not `x`: no problem
[1] 10 30 60 100</pre>
```

The indexer is always evaluated first and then passed to the subsetting operation. The index operator does not care how an indexer is generated.

Furthermore, the recycling rule is applied when necessary:

```
x[c(FALSE, TRUE)] # every second element

[1] 20 40 60 80 100

y[c(TRUE, FALSE)] # interestingly, there is no warning here

[1]]

[1] 1

##

[2]]

[1] 21 22 23
```

**Exercise 5.1** Consider a simple database about six people, their favourite dishes, and birth years.

```
name <- c("Graham", "John", "Terry", "Eric", "Michael", "Terry")
food <- c("bacon", "spam", "spam", "eggs", "spam", "beans")
year <- c(1941, 1939, 1942, 1943, 1943, 1940)
```

The consecutive elements in different vectors correspond to each other, e.g., Graham was born in 1941, and his go-to food was bacon.

- List the names of people born in 1941 or 1942.
- List the names of those who like spam.
- List the names of those who like spam and were born after 1940.
- Compute the average birth year of the lovers of spam.
- Give the average age, in 1969, of those who didn't find spam utmostly delicious.

The answers to the above must be provided programmatically, i.e., we do not just write "Eric"

and "Graham". The code must be generic enough so that it works in the case of any other database of this kind, no matter its size.

**Exercise 5.2** Remove missing values from a given vector without referring to **na.omit**.

#### 5.2.4 Character indexer

Let us consider a vector equipped with the names attribute:

```
x <- structure(x, names=letters[1:10]) # add names
print(x)
a b c d e f g h i j
10 20 30 40 50 60 70 80 90 100</pre>
```

These labels can be referred to when extracting the elements. To do this, we use an indexer that is a character vector:

```
x[c("a", "f", "a", "g", "z")]
a f a g <NA>
10 60 10 70 NA
```

**Important** We have said that special object attributes add *extra* functionality on top of the existing ones. Therefore, indexing by means of positive, negative, and logical vectors is still available:

```
x[1:3]

a b c

10 20 30

x[-(1:5)]

f g h i j

60 70 80 90 100

x[x > 70]

h i j

80 90 100
```

Lists can also be subsetted this way.

```
(y <- structure(y, names=c("first", "second", "third")))
$first
[1] 1
##
$second
[1] 11 12
##
$third</pre>
```

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```
[1] 21 22 23
y[c("first", "second")]
$first
[1] 1
##
$second
[1] 11 12
 # result is a list
y["third"]
$third
[1] 21 22 23
y[["third"]] # result is the specific element unwrapped
[1] 21 22 23
```

**Important** Labels do not have to be unique. When we have repeated names, the first matching element is extracted:

```
structure(c(1, 2, 3), names=c("a", "b", "a"))["a"]
a
1
```

There is no direct way to select all but given names, just like with negative integer indexers. For a workaround, see Section 5.4.1.

**Exercise 5.3** Rewrite the solution to the above spam-lovers exercise, assuming that we now have the three features wrapped inside a list.

```
(people <- list(</pre>
 Name=c("Graham", "John", "Terry", "Eric",
 "Michael", "Terry", "Steve"),
 Food=c("bacon", "spam", "spam", "eggs",
 "spam",
 "beans", "spam"),
 Year=c(1941,
 1939, 1942,
 1943,
 1943,
 1940,
 NA_real_)
))
$Name
[1] "Graham" "John" "Terry"
 "Eric"
 "Michael" "Terry"
 "Steve"
##
$Food
[1] "bacon" "spam" "spam" "eggs" "spam" "beans" "spam"
##
$Year
[1] 1941 1939 1942 1943 1943 1940
 NA
```

Do not refer to name, food, and year directly. Instead, use the full people[["Name"]] etc. accessors. There is no need to pout: it is just a tiny bit of extra work. Also, notice that Steve has joined the group; hello, Steve.

# 5.3 Replacing elements

#### 5.3.1 Modifying atomic vectors

There are also *replacement* versions of the above indexing schemes. They allow us to substitute some new content for the old one.

```
(x <- 1:12)
[1] 1 2 3 4 5 6 7 8 9 10 11 12
x[length(x)] <- 42 # modify the last element
print(x)
[1] 1 2 3 4 5 6 7 8 9 10 11 42</pre>
```

The principles of vectorisation, recycling rule, and implicit coercion are all in place:

```
x[c(TRUE, FALSE)] <- c("a", "b", "c")
print(x)
[1] "a" "2" "b" "4" "c" "6" "a" "8" "b" "10" "c" "42"
```

Long story long: first, to ensure that the new content can be poured into the old wine-skin, R coerced the numeric vector to a character one. Then, every second element therein, a total of six items, was replaced by a recycled version of the replacement sequence of length three. Finally, the name x was rebound to such a brought-forth object and the previous one became forgotten.

**Note** For more details on replacement functions in general, see Section 9.3.6. Such operations alter the state of the object they are called on (quite a rare behaviour in functional languages).

**Exercise 5.4** Replace missing values in a given numeric vector with the arithmetic mean of its well-defined observations.

# 5.3.2 Modifying lists

List contents can be altered as well. For modifying individual elements, the safest option is to use the replacement version of the `[[` operator:

```
y <- list(a=1, b=1:2, c=1:3)
y[[1]] <- 100:110
y[["c"]] <- -y[["c"]]
print(y)
$a
[1] 100 101 102 103 104 105 106 107 108 109 110
##</pre>
```

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I DEEP

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```
$b
[1] 1 2
##
$c
[1] -1 -2 -3
```

The replacement version of `[` modifies a whole sub-list:

```
y[1:3] <- list(1, c("a", "b", "c"), c(TRUE, FALSE))
print(y)
$a
[1] 1
##
$b
[1] "a" "b" "c"
##
$c
[1] TRUE FALSE
```

#### Moreover:

```
y[1] <- list(1:10) # replace one element with one object
y[-1] <- 10:11 # replace two elements with two singletons
print(y)
$a
 [1] 1 2 3 4 5 6 7 8 9 10
##
$b
[1] 10
##
$c
[1] 11
```

Note Let i be a vector of positive indexes of elements to be modified. Overall, calling "y[i] <- z" behaves as if we wrote:

```
1. y[[i[1]]] <- z[[1]],</pre>
2. y[[i[2]]] <- z[[2]],
3. y[[i[3]]] <- z[[3]],
```

and so forth.

Furthermore, z (but not i) will be recycled when necessary. In other words, we retrieve z[[j % length(z)]] for consecutive js from 1 to the length of i.

#### **Exercise 5.5** *Reflect on the results of the following expressions:*

```
y[1] <- c("a", "b", "c"),
y[[1]] <- c("a", "b", "c"),
y[[1]] <- list(c("a", "b", "c")),
y[1:3] <- c("a", "b", "c"),
y[1:3] <- list(c("a", "b", "c")),
y[1:3] <- list("a", "b", "c")),
y[1:3] <- list("a"),
y[c(1, 2, 1)] <- c("a", "b", "c").
```

**Important** Setting a list item to NULL removes it from the list completely.

```
y <- list(1, 2, 3, 4)
y[1] <- NULL # removes the first element (i.e., 1)
y[[1]] <- NULL # removes the first element (i.e., now 2)
y[1] <- list(NULL) # sets the first element (i.e., now 3) to NULL
print(y)
[[1]]
NULL
##
[[2]]
[1] 4</pre>
```

The same notation convention is used for dropping object attributes; see Section 9.3.6.

#### 5.3.3 Inserting new elements

New elements can be pushed at the end of the vector quite easily<sup>3</sup>.

```
(x <- 1:5)
[1] 1 2 3 4 5
x[length(x)+1] <- 6 # insert at the end
print(x)
[1] 1 2 3 4 5 6
x[10] <- 10 # insert at the end but add more items
print(x)
[1] 1 2 3 4 5 6 NA NA NA 10</pre>
```

The elements to be inserted can be named as well:

<sup>&</sup>lt;sup>3</sup> And often cheaply; see Section 8.3.5 for performance notes. Still, a warning can be generated on each size extension if the "check.bounds" flag is set; see help("options").

Note that x was not equipped with the names attribute before. The unlabelled elements were assigned blank labels (empty strings).

**Note** It is not possible to insert new elements at the beginning or in the middle of a sequence, at least not with the index operator. By writing "x[3:4] <- 1:5" we do not replace two elements in the middle with five other ones. However, we can always use the **c** function to slice parts of the vector and intertwine them with some new content:

```
x <- seq(10, 100, 10)
x <- c(x[1:2], 1:5, x[5:7])
print(x)
[1] 10 20 1 2 3 4 5 50 60 70</pre>
```

# 5.4 Functions related to indexing

Let us review a few operations which pinpoint interesting elements in a vector (or functions based on these).

# 5.4.1 Matching elements in another vector

We know that the = operator acts in an elementwise manner. It compares each element in a vector on its left side to the *corresponding* element in a vector on the right side. Thus, missing values and the recycling rule aside, if "z <- (x == y)", then z[i] is TRUE if and only if x[i] is equal to y[i].

The `**%in%**` operator<sup>4</sup> is vectorised differently. It checks whether each element on the left-hand side matches *one* of the elements on the right. Given "z <- (x %in% y)", z[i] is TRUE whenever x[i] is equal to y[j] for some j.

```
c("spam", "bacon", "spam", "eggs", "spam") %in% c("eggs", "spam", "ham")
[1] TRUE FALSE TRUE TRUE TRUE
```

<sup>&</sup>lt;sup>4</sup> A fantastic name; see Section 9.3.5.

**Example 5.6** Here is how we can remove the elements of a vector that have been assigned specified labels.

```
(x <- structure(1:12, names=month.abb)) # example vector

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec

1 2 3 4 5 6 7 8 9 10 11 12

x[!(names(x) %in% c("Jan", "May", "Sep", "Oct"))] # get rid of some elements

Feb Mar Apr Jun Jul Aug Nov Dec

2 3 4 6 7 8 11 12
```

More generally, match(x, y) gives us the index of the element in y that matches each x[i].

```
match(c("spam", "bacon", "spam", "eggs", "spam"), c("eggs", "spam", "ham"))
[1] 2 NA 2 1 2
match(month.abb, c("Jan", "May", "Sep", "Oct")) # is the month on the list?
[1] 1 NA NA NA 2 NA NA NA 3 4 NA NA
match(c("Jan", "May", "Sep", "Oct"), month.abb) # which month is it?
[1] 1 5 9 10
```

By default, a missing value denotes a no-match.

**Exercise 5.7** Check out the documentation of `**%in%**` to see how this operator is reduced to a call to **match**. Also, verify that it treats missing values as well-defined ones.

If the elements in y are not unique, the smallest index j such that x[i] == y[j] is returned. Therefore, for example, match(TRUE, l) fetches the index of the first occurrence of a positive value in a logical vector l.

```
(x <- round(runif(10), 2)) # example vector

[1] 0.29 0.79 0.41 0.88 0.94 0.05 0.53 0.89 0.55 0.46

match(TRUE, x>0.8) # index of the first value > 0.8 (from the left)

[1] 4
```

# 5.4.2 Assigning numbers into intervals

**findInterval** can come in handy where the assigning of numeric values into real intervals is needed. Namely, z <- **findInterval**(x, y) for increasing y gives z[i] being the index j such that x[i] is between y[j] (by default, inclusive) and y[j+1] (by default, exclusive).

For example, a sequence of five knots  $y = (-\infty, 0.25, 0.5, 0.75, \infty)$  splits the real line into the following four intervals:

$$[-\infty, 0.25)$$
  $[0.25, 0.5)$   $[0.5, 0.75)$   $[0.75, \infty)$ 

Hence, for instance:

```
findInterval(c(0, 0.2, 0.25, 0.4, 0.66, 1), c(-Inf, 0.25, 0.5, 0.75, Inf))
[1] 1 1 2 2 3 4
```

**Exercise 5.8** Refer to the manual of **findInterval** to verify the function's behaviour when we do not include  $\pm \infty$  as endpoints and how to make  $\infty$  classified as a member of the fourth interval.

**Exercise 5.9** Using a call to **findInterval**, compose a statement that generates a logical vector whose i-th element indicates whether x[i] is in the interval [0.25, 0.5]. Was this easier to write than an expression involving <= and >=?

### 5.4.3 Splitting vectors into subgroups

split(x, z) can take the output of match or findInterval (and many other operations) and divide the elements in a vector x into subgroups corresponding to identical zs.

For instance, we can assign people into groups determined by their favourite dish:

```
name <- c("Graham", "John", "Terry", "Eric",</pre>
 "Michael", "Terry")
food <- c("bacon", "spam", "spam", "eggs", "spam",</pre>
 "beans")
split(name, food) # group names with respect to food
$bacon
[1] "Graham"
##
$beans
[1] "Terry"
##
$eaas
[1] "Eric"
##
$spam
[1] "John"
 "Terry" "Michael"
```

The result is a named list with labels determined by the unique elements in the second vector.

Here is another example, where we pigeonhole some numbers into the four previously mentioned intervals:

```
x <- c(0, 0.2, 0.25, 0.4, 0.66, 1)
split(x, findInterval(x, c(-Inf, 0.25, 0.5, 0.75, Inf)))
$`1`
[1] 0.0 0.2
##
$`2`
[1] 0.25 0.40
##
$`3`</pre>
```

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```
[1] 0.66
##
$`4`
[1] 1
```

Items in the first argument that correspond to missing values in the grouping vector will be ignored. Also, unsurprisingly, the recycling rule is applied when necessary.

We can also split x into groups defined by a combination of levels of two or more variables z1, z2, etc., by calling **split**(x, **list**(z1, z2, ...)).

**Example 5.10** The ToothGrowth dataset is a named list (more precisely, a data frame; see Chapter 12) that represents the results of an experimental study involving 60 guinea pigs. The experiment's aim was to measure the effect of different vitamin C supplement types and doses on the growth of the rodents' teeth lengths:

```
ToothGrowth <- as.list(ToothGrowth) # it is a list, but with extra attribs
ToothGrowth[["supp"]] <- as.character(ToothGrowth[["supp"]]) # was: factor
print(ToothGrowth)
$len
[1] 4.2 11.5 7.3 5.8 6.4 10.0 11.2 11.2 5.2 7.0 16.5 16.5 15.2 17.3
[15] 22.5 17.3 13.6 14.5 18.8 15.5 23.6 18.5 33.9 25.5 26.4 32.5 26.7 21.5
[29] 23.3 29.5 15.2 21.5 17.6 9.7 14.5 10.0 8.2 9.4 16.5 9.7 19.7 23.3
[43] 23.6 26.4 20.0 25.2 25.8 21.2 14.5 27.3 25.5 26.4 22.4 24.5 24.8 30.9
[57] 26.4 27.3 29.4 23.0
##
$SUDD
[57] "OJ" "OJ" "OJ" "OJ"
##
$dose
[52] 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0
```

We can split len with respect to the combinations of supp and dose (also called interactions) by calling:

```
split(ToothGrowth[["len"]], ToothGrowth[c("supp", "dose")], sep="_")
$0J_0.5
[1] 15.2 21.5 17.6 9.7 14.5 10.0 8.2 9.4 16.5 9.7
##
(continues on next page)
```

```
$VC_0.5
##
 [1] 4.2 11.5 7.3 5.8 6.4 10.0 11.2 11.2 5.2 7.0
##
$0J 1
##
 [1] 19.7 23.3 23.6 26.4 20.0 25.2 25.8 21.2 14.5 27.3
##
$VC 1
 [1] 16.5 16.5 15.2 17.3 22.5 17.3 13.6 14.5 18.8 15.5
##
##
$0J 2
 [1] 25.5 26.4 22.4 24.5 24.8 30.9 26.4 27.3 29.4 23.0
##
$VC 2
 [1] 23.6 18.5 33.9 25.5 26.4 32.5 26.7 21.5 23.3 29.5
```

Other synonyms are, of course, possible, e.g., **split**(ToothGrowth[[1]], ToothGrowth[-1]) and **split**(ToothGrowth[[1]], **list**(ToothGrowth[[2]], ToothGrowth[[3]])). We recommend meditating upon our conscious use of double vs single square brackets here.

Functions such as **Map** (Section 7.2) will soon enable us to compute any summary statistics within groups, e.g., the group averages like those obtained by executing "SELECT AVG(len) FROM ToothGrowth GROUP BY supp, dose" in SQL. As an appetiser, let us pass a list of vectors to the **boxplot** function; see Figure 5.1.

boxplot(split(ToothGrowth[["len"]], ToothGrowth[c("supp", "dose")], sep="\_"))

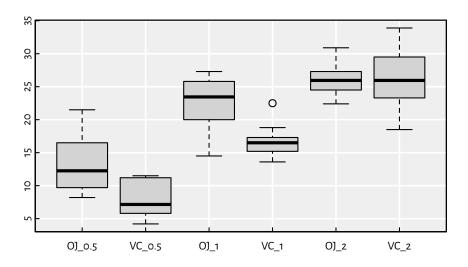


Figure 5.1. Box-and-whisker plots of len split by supp and dose in ToothGrowth.

**Note** unsplit revokes the effects of split. Later, we will get used to calling unsplit(Map(some\_transformation, split(x, z)), z) to modify the values in x independently in each group defined by z (e.g., standardise the variables within each class separately).

#### 5.4.4 Ordering elements

The **order** function finds the ordering permutation of a given vector, i.e., a sequence of indexes that leads to a sorted version thereof.

```
x <- c(1024, 7, 42, 666, 0, 32787)
(o <- order(x)) # the ordering permutation of x
[1] 5 2 3 4 1 6
x[o] # ordered version of x
[1] 0 7 42 666 1024 32787</pre>
```

Note that o[1] is the index of the smallest element in x, o[2] is the position of the second smallest, ..., and o[length(o)] is the index of the greatest value. Hence, e.g., x[o[1]] is equivalent to min(x).

Another example:

```
x <- c("b", "a", "abs", "bass", "aaargh", "aaargh", "aaaargh")
(o <- order(x))
[1] 2 7 5 6 3 1 4
x[o]
[1] "a" "aaaargh" "aaargh" "abs" "b" "bass"</pre>
```

Here, as x is a character vector, the ordering is lexicographical (like in a dictionary). This is exactly how `<=` on strings works.

**Note** The ordering permutation that **order** returns is unique (that is why we call it *the* permutation), even for inputs containing duplicated elements. Owing to the use of a *stable* sorting algorithm, ties (repeated elements) will be listed in the order of occurrence.

```
order(c(10, 20, 40, 10, 10, 30, 20, 10, 10))
[1] 1 4 5 8 9 2 7 6 3
```

Above we have, e.g., five 10s at positions 1, 4, 5, 8, and 9. These five indexes are guaranteed to be listed in this very order.

Ordering can also be performed in a nonincreasing manner:

```
x[order(x, decreasing=TRUE)]
[1] "bass" "b" "abs" "aargh" "aaargh" "a"
```

**Note** A call to sort(x) is equivalent to x[order(x)], but the former function can be faster in certain scenarios. For instance, one of its arguments can induce a *partially* sorted vector which can be helpful if we only seek a few order statistics (e.g., the seven smallest values). Speed is rarely a bottleneck in the case of sorting (when it is, we have a problem!). This is why we will not bother ourselves with such topics until the last part of this pleasant book. Currently, we aim at expanding our skill repertoire so that we can implement anything we can think of.

**Exercise 5.11** is.unsorted(x) determines if the elements in x are... not sorted with respect to `<=`. Write an R expression that generates the same result by referring to the order function. Also, assuming that x is numeric, do the same by means of a call to diff.

**order** also accepts one or more arguments via the dot-dot parameter, `...`. This way, we can sort a vector with respect to many criteria. If there are ties in the first variable, they will be resolved by the order of elements in the second variable. This is most useful for rearranging rows of a data frame, which we will exercise in Chapter 12.

```
x <- c(10, 20, 30, 40, 50, 60)
y1 <- c("a", "b", "a", "b", "b")
y2 <- c("w", "w", "v", "u", "v")
x[order(y1)]
[1] 10 30 40 20 50 60
x[order(y2)]
[1] 40 50 30 60 10 20
x[order(y1, y2)]
[1] 40 30 10 50 60 20
x[order(y2, y1)]
[1] 40 50 30 60 10 20</pre>
```

**Note** (\*) Calling **order** on a permutation (a vector that is an arbitrary arrangement of *n* consecutive natural numbers) determines its *inverse*.

```
x <- c(10, 30, 40, 20, 10, 10, 50, 30)
order(x)
[1] 1 5 6 4 2 8 3 7
order(order(x)) # inverse of the above permutation
[1] 1 5 7 4 2 3 8 6
(x[order(x)])[order(order(x))] # we get x again
[1] 10 30 40 20 10 10 50 30</pre>
```

Note that order(order(x)) can be considered as a way to rank all the elements in x. For

instance, the third value in  $\times$ , 40, is assigned rank 7: it is the seventh smallest value in this vector. This breaks the ties on a first-come, first-served basis. But we can also write:

```
order(order(x, runif(length(x)))) # ranks with ties broken at random
[1] 2 5 7 4 3 1 8 6
```

For different variations of these, see the rank function.

**Exercise 5.12** Recall that sample(x) returns a pseudorandom permutation of elements of a given vector unless x is a single positive number. Write an expression that always produces a proper rearrangement, regardless of the size of x.

#### 5.4.5 Identifying duplicates

Whether any element in a vector was already listed in the previous part of the sequence can be verified by calling:

```
x <- c(10, 20, 30, 20, 40, 50, 50, 50, 20, 20, 60)
duplicated(x)
[1] FALSE FALSE TRUE FALSE TRUE TRUE TRUE TRUE TRUE FALSE</pre>
```

This function can be used to remove repeated observations; see also **unique**. This function returns a value that is not guaranteed to be sorted (unlike in some other languages/libraries).

**Exercise 5.13** What can be the use case of a call to match(x, unique(x))?

**Exercise 5.14** Given two named lists x and y, which we treat as key-value pairs, determine their set-theoretic union (with respect to the keys). For example:

```
x <- list(a=1, b=2)
y <- list(c=3, a=4)
z <- ...to.do... # combine x and y
str(z)
List of 3
$ a: num 4
$ b: num 2
$ c: num 3</pre>
```

# 5.4.6 Counting index occurrences

**tabulate** takes a vector of values from a set of small positive integers (e.g., indexes) and determines their number of occurrences:

```
x <- c(2, 4, 6, 2, 2, 2, 3, 6, 6, 3)
tabulate(x)
[1] 0 4 2 1 0 3</pre>
```

In other words, there are 0 ones, 4 twos, ..., and 3 sixes.

**Exercise 5.15** Using a call to **tabulate** (amongst others), return a named vector with the number of occurrences of each unique element in a character vector. For example:

```
y <- c("a", "b", "a", "c", "a", "d", "e", "e", "g", "g", "c", "c", "g")
result <- ...to.do...
print(result)
a b c d e g
3 1 3 1 2 3</pre>
```

# 5.5 Preserving and losing attributes

Attributes are conceived of as *extra* data. It is thus up to a function's authors what they will decide to do with them. Generally, it is safe to assume that much thought has been put into the design of base R functions. Oftentimes, they behave quite reasonably. This is why we are now going to spend some time now exploring their approaches to the handling of attributes.

Namely, for functions and operators that aim at transforming vectors passed as their inputs, the assumed strategy may be to:

- · ignore the input attributes completely,
- · equip the output object with the same set of attributes, or
- take care only of a few special attributes, such as names, if that makes sense.

Below we explore some common patterns; see also Section 1.3 of [66].

#### 5.5.1

First, **c** drops<sup>5</sup> all attributes except names:

```
(x <- structure(1:4, names=c("a", "b", "c", "d"), attrib1="<3"))
a b c d
1 2 3 4
attr(,"attrib1")
[1] "<3"</pre>
(continues on next nose)
```

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 $<sup>^5</sup>$  To be precise, we mean the default S3 method of  ${f c}$  here; compare Section 10.2.4.

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```
c(x) # only `names` are preserved
a b c d
1 2 3 4
```

We can therefore end up calling this function chiefly for this nice side effect. Also, recall that unname drops the labels.

```
unname(x)
[1] 1 2 3 4
attr(,"attrib1")
[1] "<3"</pre>
```

#### 5.5.2 as.something

**as.vector**, **as.numeric**, and similar drop all attributes in the case where the output is an atomic vector, but it might not necessarily do so in other cases (because they are S3 generics; see Chapter 10).

```
as.vector(x) # drops all attributes if x is atomic
[1] 1 2 3 4
```

### 5.5.3 Subsetting

Subsetting with `[` (except where the indexer is not given) drops all attributes but names (as well as dim and dimnames; see Chapter 11), which is adjusted accordingly:

```
x[1] # subset of labels
a
1
x[[1]] # this always drops the labels (makes sense, right?)
[1] 1
```

The replacement version of the index operator modifies the values in an existing vector whilst preserving all the attributes. In particular, skipping the indexer replaces all the elements:

```
y <- x
y[] <- c("u", "v") # note that c("u", "v") has no attributes
print(y)
a b c d
"u" "v" "u" "v"
attr(, "attrib1")
[1] "<3"</pre>
```

#### 5.5.4 Vectorised functions

Vectorised unary functions tend to copy all the attributes.

```
round(x)
a b c d
1 2 3 4
attr(,"attrib1")
[1] "<3"
```

Binary operations are expected to get the attributes from the longer input. If they are of equal sizes, the first argument is preferred to the second.

```
y <- structure(c(1, 10), names=c("f", "g"), attrib1=":|", attrib2=":0")</pre>
y * x # x is longer
a b c d
1 20 3 40
attr(,"attrib1")
[1] "<3"
y[c("h", "i")] < -c(100, 1000) # add two new elements at the end
y * x
##
 f g h i
1 20 300 4000
attr(,"attrib1")
[1] ":|"
attr(,"attrib2")
[1] ":0"
x * v
a b c
1 20 300 4000
attr(,"attrib1")
[1] "<3"
attr(,"attrib2")
[1] ":0"
```

Also, Section 9.3.6 mentions a way to copy all attributes from one object to another.

**Important** Even in base R, the above rules are not enforced strictly. We consider them inconsistencies that should be, for the time being, treated as features (with which we need to learn to live as they have not been fixed for years, but hope springs eternal).

As far as third-party extension packages are concerned, suffice it to say that a lot of R programmers do not know what attributes are whatsoever. It is always best to refer to the documentation, perform a few experiments, and/or manually ensure the preservation of the data we care about.

#### 5.6 Exercises

**Exercise 5.17** *Answer the following questions (contemplate first, then use R to find the answer).* 

- What is the result of x[c()]? Is it the same as x[]?
- Is x[c(1, 1, 1)] equivalent to x[1]?
- Is x[1] equivalent to x["1"]?
- Is x[c(-1, -1, -1)] equivalent to x[-1]?
- What does x[c(0, 1, 2, NA)] do?
- What does x[0] return?
- What does x[1, 2, 3] do?
- What about x[c(0, -1, -2)] and x[c(-1, -2, NA)]?
- Why x[NA] is so significantly different from x[c(1, NA)]?
- What is x[c(FALSE, TRUE, 2)]?
- What will we obtain by calling x[x < min(x)]?
- What about x[length(x)+1]?
- Why x[min(y)] is most probably a mistake? What could it mean? How can it be fixed?
- Why cannot we mix indexes of different types and write x[c(1, "b", "c", 4)]? Or can we?
- Why would we call **as.vector(na.omit(**x)) instead of just **na.omit(**x)?
- What is the difference between **sort** and **order**?
- What is the type and the length of the object returned by a call to split(a, u)? What about split(a, c(u, v))?
- How to get rid of the seventh element from a list of ten elements?
- How to get rid of the seventh, eight, and ninth elements from a list with ten elements?
- How to get rid of the seventh element from an atomic vector of ten elements?
- If y is a list, by how many elements "y[c(length(y)+1, length(y)+1, length(y)+1)]
   list(1, 2, 3)" will extend it?
- What is the difference between x[x>0] and x[which(x>0)]?

**Exercise 5.18** If x is an atomic vector of length n, x[5:n] obviously extracts everything from the fifth element to the end. Does it, though? Check what happens when x is of length less than five, including 0. List different ways to correct this expression so that it makes (some) sense in the case of shorter vectors.

**Exercise 5.19** Similarly, x[length(x) + 1 - 5:1] is supposed to return the last five elements in x. Propose a few alternatives that are correct also for short xs.

**Exercise 5.20** Given a numeric vector, fetch its five largest elements. Ensure the code works for vectors of length less than five.

**Exercise 5.21** We can compute a trimmed mean of some x by setting the trimargument to the mean function. Compute a similar robust estimator of location – the p-winsorised mean,  $p \in [0,0.5]$  defined as the arithmetic mean of all elements in x clipped to the  $[Q_p,Q_{1-p}]$  interval, where  $Q_p$  is the vector's p-quantile; see quantile. For example, if x is (8,5,2,9,7,4,6,1,3), we have  $Q_{0.25} = 3$  and  $Q_{0.75} = 7$  and hence the 0.25-winsorised mean will be equal to the arithmetic mean of (7,5,3,7,7,4,6,3,3).

**Exercise 5.22** Let x and y be two vectors of the same length, n, and no ties. Implement the formula for the Spearman rank correlation coefficient:

$$\varrho(\mathbf{x}, \mathbf{y}) = 1 - \frac{6\sum_{i=1}^{n} d_i^2}{n(n^2 - 1)},$$

where  $d_i = r_i - s_i$ , i = 1, ..., n, and  $r_i$  and  $s_i$  denote the rank of  $x_i$  and  $y_i$ , respectively; see also **cor**.

**Exercise 5.23** (\*) Given two vectors x and y both of length n, a call to approx(x, y, ...) can be used to interpolate linearly between the points  $(x_1, y_1), (x_2, y_2), ..., (x_n, y_n)$ . We can use it whenever we wish to generate new ys for previously unobserved xs (somewhere "in-between" the data we already have). Moreover, spline(x, y, ...) can perform a cubic spline interpolation, which is smoother; see Figure 5.2.

Using a call to one of the above, impute missing data in euraud-20200101-20200630.cs $v^6$ , e.g., the blanks in (0.60, 0.62, NA, 0.64, NA, NA, 0.58) should be filled so as to obtain (0.60, 0.62, 0.63, 0.64, 0.62, 0.60, 0.58).

**Exercise 5.24** Given some  $1 \le from \le to \le n$ , use **findInterval** to generate a logical vector of length n with TRUE elements only at indexes between from and to, inclusive.

**Exercise 5.25** Implement expressions that give rise to the same results as calls to which, which. min, which.max, and rev functions. What is the difference between x[x>y] and x[which(x>y)]? What about which.min(x) vs which(x == min(x))?

<sup>&</sup>lt;sup>6</sup> https://github.com/gagolews/teaching-data/raw/master/marek/euraud-20200101-20200630.csv

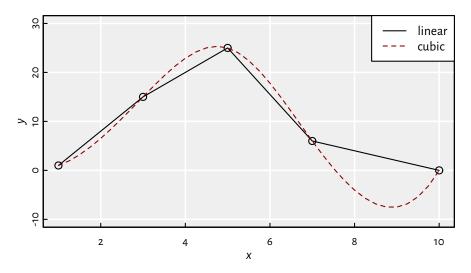


Figure 5.2. Piecewise linear and cubic spline interpolation.

**Exercise 5.26** Given two equal-length vectors x and y, fetch the value from the former that corresponds to the smallest value in the latter. Write three versions of such an expression, each dealing with potential ties in y differently. For example:

```
x <- c("a", "b", "c", "d", "e", "f")
y <- c(3, 1, 2, 1, 1, 4)
```

It should choose the first ("b"), last ("e"), or random element from x fulfilling the above property ("b", "d", or "e" with equal probability). Make sure your code works for x being of the type character or numeric as well as an empty vector.

**Exercise 5.27** Implement an expression that yields the same result as duplicated(x) for a numeric vector x, but using diff and order.

**Exercise 5.28** Based on match and unique, implement your versions of union(x, y), intersect(x, y), setdiff(x, y), is.element(x, y), and setequal(x, y) for x and y being nonempty numeric vectors.

# Character vectors

Text is a universal, portable, economical, and efficient means of interacting between humans and computers as well as exchanging data between programs or APIs. This book is 99% made of text. And, wow, how much valuable knowledge is in it, innit?

## 6.1 Creating character vectors

#### 6.1.1 Inputting individual strings

Specific character strings are delimited by a pair of either double or single quotes (apostrophes).

```
"a string"
[1] "a string"
'another string' # and, of course, neither 'like this" nor "like this'
[1] "another string"
```

The only difference between these two is that we cannot directly include, e.g., an apostrophe in a single quote-delimited string. On the other hand, "'tis good ol' spam" and 'I "love" bacon' are both okay.

However, to embrace characters whose inclusion might otherwise be difficult or impossible, we may always employ the so-called *escape sequences*.

R uses the backslash, "\", as the escape character. In particular:

- \" inputs a double quote,
- \' generates a single quote,
- \\ includes a backslash,
- \n endows a new line.

```
(x <- "I \"love\" bacon\n\\\"/")
[1] "I \"love\" bacon\n\\\"/"</pre>
```

The **print** function (which was implicitly called to display the above object) does not reveal the special meaning of the escape sequences. Instead, **print** outputs strings in

the same way that we ourselves would follow when inputting them. The number of characters in x is 18, and not 23:

```
nchar(x)
[1] 18
```

To display the string as-it-really-is, we call **cat**:

```
cat(x, sep="\n")
I "love" bacon
\"/
```

In raw character constants, the backslash character's special meaning is disabled. They can be entered using the notation like  $r"(...)", r"\{...\}", or r"[...]"$ ; see **help**("Quotes"). These can be useful when inputting regular expressions (Section 6.2.4).

```
x <- r"(spam\n\\\"maps)" # also: r"-(...)-", r"--(...)--", etc.
print(x)
[1] "spam\n\\\\"maps"
cat(x, sep="\n")
spam\n\\\"maps</pre>
```

Furthermore, the string version of the missing value marker is NA\_character\_.

**Note** (\*) The Unicode standard 15.0 (version dated September 2022) defines 149 186 characters, i.a., letters from different scripts, mathematical symbols, and emojis. Each is assigned a unique numeric identifier; see the Unicode Character Code Charts<sup>1</sup>. For example, the *inverted exclamation mark* (see the Latin-1 Supplement section therein) has been mapped to the hexadecimal code 0xA1 (or 161 decimally). Knowing this magic number permits us to specify a Unicode code point using one of the following escape sequences:

- \uxxxx codes using four hexadecimal digits,
- \Uxxxxxxx codes using eight hexadecimal digits.

For instance:

```
cat("!\u00a1!\U0000000a1!", sep="\n")
!;!;!
```

All R installations allow for working with Unicode strings. More precisely, they support dealing with *UTF-8*, being a super-encoding that is native to most UNIX-like boxes, including GNU/Linux and m\*\*OS. Other operating systems may use some 8-bit encoding as the system one (e.g., latin1 or cp1252), but they can be mixed with Unicode seamlessly; see help("Encoding"), help("iconv"), and [27] for discussion.

<sup>1</sup> https://www.unicode.org/charts

Nevertheless, certain output devices (web browsers, LaTeX renderers, text terminals) might be unable to display every possible Unicode character, e.g., due to some fonts' being missing. However, as far as processing character data is concerned, this does not matter because R does it with its eyes closed. For example:

```
cat("\U0001f642\u2665\u0bb8\U0001f923\U0001f60d\u2307", sep="\n")
00000
```

In the PDF version<sup>2</sup> of this adorable book, the Unicode glyphs are not rendered correctly for some reason. However, its HTML variant<sup>3</sup>, generated from the same source files, should be displayed by most web browsers properly.

**Note** (\*) Some output devices may support the following codes that control the position of the caret (text cursor):

- \b inserts a backspace (moves cursor one column to the left),
- \t implants a tabulator (advances to the next tab stop, e.g., a multiply of four or eight text columns),
- \r injects a carriage return (move to the beginning of the current line).

```
cat("abc\bd\tef\rg\nhij", sep="\n")
gbd ef
hij
```

These can be used on unbuffered outputs like **stderr** to display the status of the current operation, for instance, an animated textual progress bar, the print-out of the ETA, or the percentage of work completed.

Further, certain terminals can also understand the ECMA-48/ANSI-X3.64 escape sequences<sup>4</sup> of the form \u001b[... to control the cursor's position, text colour, and even style. For example, \u001b[1;31m outputs red text in bold font and \u001b[0m resets the settings to default. We recommend giving, e.g., cat("\u001b[1;31mspam\u001b[0m") or cat("\u001b[5;36m\u001b[Abacon\u001b[Espam\u001b[0m") a try.

## 6.1.2 Many strings, one object

Less trivial character vectors (meaning, of length greater than one) can be constructed by means of, e.g., c or rep<sup>5</sup>.

<sup>&</sup>lt;sup>2</sup> https://deepr.gagolewski.com/deepr.pdf

<sup>&</sup>lt;sup>3</sup> https://deepr.gagolewski.com/

<sup>4</sup> https://en.wikipedia.org/wiki/ANSI\_escape\_code

<sup>&</sup>lt;sup>5</sup> Internally, there is a string cache (a hash table). Multiple clones of the same string do not occupy more RAM than necessary.

```
(x <- c(rep("spam", 3), "bacon", NA_character_, "spam"))
[1] "spam" "spam" "bacon" NA "spam"</pre>
```

Thus, a character vector is, in fact, a sequence of sequences of characters<sup>6</sup>. As usual, the total number of strings can be fetched via the **length** function. However, the length of each string may be read with the vectorised **nchar**.

```
length(x) # how many strings?
[1] 6
nchar(x) # the number of code points in each string
[1] 4 4 4 5 NA 4
```

#### 6.1.3 Concatenating character vectors

paste can be used to concatenate (join) the corresponding elements of two or more character vectors:

```
paste(c("a", "b", "c"), c("1", "2", "3")) # sep=" " by default
[1] "a 1" "b 2" "c 3"
paste(c("a", "b", "c"), c("1", "2", "3"), sep="") # see also paste0
[1] "a1" "b2" "c3"
```

The function is deeply vectorised:

```
paste(c("a", "b", "c"), 1:6, c("!", "?")) # coercion of numeric to character
[1] "a 1 !" "b 2 ?" "c 3 !" "a 4 ?" "b 5 !" "c 6 ?"
```

We can also collapse (flatten, aggregate) a sequence of strings into a single string:

```
paste(c("a", "b", "c", "d"), collapse=",")
[1] "a,b,c,d"
paste(c("a", "b", "c", "d"), 1:2, sep="", collapse="")
[1] "a1b2c1d2"
```

Perhaps for convenience, alas, **paste** treats missing values differently from most other vectorised functions:

```
paste(c("A", NA_character_, "B"), "!", sep="")
[1] "A!" "NA!" "B!"
```

 $<sup>^6</sup>$  (\*) Chapter 14 will mention that objects of the type character are internally represented as objects with SEXPTYPE of STRSXP. They are arrays with elements whose SEXPTYPE is CHARSXP, each of which is a string of characters (char\*).

### 6.1.4 Formatting objects

Strings can also arise by converting other-typed R objects into text. For example, the quite customisable (see Chapter 10) **format** function prepares data for display in dynamically generated reports.

```
x <- c(123456.789, -pi, NaN)
format(x)
[1] "123456.7890" " -3.1416" " NaN"
cat(format(x, digits=8, scientific=FALSE, drop0trailing=TRUE), sep="\n")
123456.789
-3.1415927
NaN</pre>
```

Moreover, **sprintf** is a workhorse for turning possibly many atomic vectors into strings. Its first argument is a *format string*. Special escape sequences starting with the per cent sign, "%", serve as placeholders for the actual values. For instance, "%s" is replaced with a string and "%f" with a floating point value taken from further arguments.

```
sprintf("%s%s", "a", c("X", "Y", "Z")) # like paste(...)
[1] "aX" "aY" "aZ"
sprintf("key=%s, value=%f", c("spam", "eggs"), c(100000, 0))
[1] "key=spam, value=100000.000000" "key=eggs, value=0.000000"
```

The numbers' precision, strings' widths and justification, etc., can be customised, e.g., "%6.2f" is a number that, when converted to text, will occupy six text columns<sup>7</sup>, with two decimal digits of precision.

Also, e.g., "%1\$s", "%2\$s", ... inserts the first, second, ... argument as text.

```
sprintf("%1$s, %2$s, %1$s, and %1$s", "spam", "bacon") # numbered argument
[1] "spam, bacon, spam, and spam"
```

**Exercise 6.1** Read **help**("sprintf") (highly recommended!).

## 6.1.5 Reading text data from files

Given a raw text file, **readLines** loads it into memory and represents it as a character vector, with each line stored in a separate string.

<sup>&</sup>lt;sup>7</sup> This is only true for 8-bit native encodings or ASCII; see also **sprintf** from the **stringx** package, which takes the text width and not the number of bytes into account.

```
head(readLines(
 "https://github.com/gagolews/teaching-data/raw/master/README.md"
))
[1] "# Dr [Marek](https://www.gagolewski.com)'s Data for Teaching"
[2] ""
[3] "> *See the comment lines within the files themselves for"
[4] "> a detailed description of each dataset.*"
[5] ""
[6] "*Good* datasets are actually hard to find!"
```

writeLines is its counterpart. There is also an option to read or write parts of files at a time using file connections which we mention in Section 8.3.5. Moreover, cat(..., append=TRUE) can be used to create a text file incrementally.

## 6.2 Pattern searching

#### 6.2.1 Comparing whole strings

We have already reviewed a couple of ways to compare strings as a whole. For instance, the `==` operator implements elementwise testing:

```
c("spam", "spam", "bacon", "eggs") == c("spam", "eggs") # recycling rule
[1] TRUE FALSE FALSE TRUE
```

In Section 5.4.1, we introduced the **match** function and its derivative, the `**%in%**` operator. They are vectorised in a different way:

```
match(c("spam", "spam", "bacon", "eggs"), c("spam", "eggs"))
[1] 1 1 NA 2
c("spam", "spam", "bacon", "eggs") %in% c("spam", "eggs")
[1] TRUE TRUE FALSE TRUE
```

**Note** (\*) match relies on a simple, bytewise comparison of the corresponding code points. It might not be valid in natural language processing activities, e.g., where the German word *groß* should be equivalent to *gross* [18]. Moreover, in the rare situations where we read Unicode-unnormalised data, canonically equivalent strings may be considered different; see [17].

## 6.2.2 Partial matching

When only a consideration of the initial part of each string is required, we can call:

```
startsWith(c("s", "spam", "spamtastic", "spontaneous", "spoon"), "spam")
[1] FALSE TRUE TRUE FALSE FALSE
```

If we provide many prefixes, the above function will be applied elementwisely, just like the `==` operator.

On the other hand, **charmatch** performs a *partial matching* of strings. It is an each-vs-all version of **startsWith**:

Note that 0 designates that there was an ambiguous match.

**Note** (\*) In Section 9.4.7, we discuss match.arg, which a few R functions rely on when they need to select a value from a range of possible choices. Furthermore, Section 9.3.2 and Section 15.4.4 mention the (discouraged) partial matching of list labels and function argument names.

## 6.2.3 Matching anywhere within a string

Fixed patterns can also be searched for anywhere within character strings using grepl:

```
x <- c("spam", "y spammite spam", "yummy SPAM", "sram")
grepl("spam", x, fixed=TRUE) # fixed patterns, as opposed to regexes below
[1] TRUE TRUE FALSE FALSE</pre>
```

**Important** The order of arguments is like **grepl**(needle, haystack), not vice versa. Also, this function is not vectorised with respect to the first argument.

**Exercise 6.2** How the calls to grep(y, x, value=FALSE) and grep(y, x, value=TRUE) can be implemented based on grepl and other operations we are already familiar with?

**Note** (\*) As a curiosity, **agrepl** performs *approximate* matching, which can account for a smöll nmber of tpyos.

```
agrepl("spam", x)
[1] TRUE TRUE FALSE TRUE
agrepl("ham", x, ignore.case=TRUE)
[1] TRUE TRUE TRUE TRUE
```

It is based on *Levenshtein's edit distance* that measures the number of character insertions, deletions, or substitutions required to turn one string into another.

### 6.2.4 Using regular expressions (\*)

Setting perl=TRUE allows for identifying occurrences of patterns specified by *regular expressions* (regexes).

```
grepl("^spam", x, perl=TRUE) # strings that begin with `spam`
[1] TRUE FALSE FALSE
grepl("(?i)^spam|spam$", x, perl=TRUE) # begin or end; case ignored
[1] TRUE TRUE TRUE FALSE
```

**Note** For more details on regular expressions in general, see, e.g., [24]. The ultimate reference on the PCRE2 pattern syntax is the Unix man page  $pcre2pattern(3)^8$ . From now on, we assume that the reader is familiar with it.

Apart from the Perl-compatible regexes, R also gives access to the TRE library (ERE-like), which is the default one; see **help**("regex"). However, we discourage its use because it is feature-poorer.

**Exercise 6.3** The **list.files** function generates the list of file names in a given directory that match a given regular expression. For instance, the following gives all CSV files in a folder.

```
list.files("~/Projects/teaching-data/r/", "\\.csv$")
[1] "air_quality_1973.csv" "anscombe.csv" "iris.csv"
[4] "titanic.csv" "tooth_growth.csv" "trees.csv"
[7] "world_phones.csv"
```

Write a single regular expression that matches file names ending with ".csv" or ".csv.gz". Also, scribble a regex that matches CSV files whose names do not begin with "eurusd".

## 6.2.5 Locating pattern occurrences

**regexpr** finds the first occurrence of a pattern in each string:

```
regexpr("spam", x, fixed=TRUE)
[1] 1 3 -1 -1
attr(,"match.length")
[1] 4 4 -1 -1
attr(,"index.type")
[1] "chars"
(continues on next page)
```

<sup>8</sup> http://www.pcre.org/current/doc/html/pcre2pattern.html

(continued from previous page)

```
attr(,"useBytes")
[1] TRUE
```

In particular, there is a pattern occurrence starting at the third code point of the second string in x. Moreover, the last string has no pattern match, which is denoted with -1.

The match. length attribute is generally more informative when searching with regular expressions.

To locate all the matches, i.e., globally, we use **gregexpr**:

```
`spam` followed by 0 or more letters, case insensitively
gregexpr("(?i)spam\\p{L}*", x, perl=TRUE)
[[1]]
[1] 1
attr(,"match.length")
[1] 4
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
##
[[2]]
[1] 3 12
attr(,"match.length")
[1] 8 4
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
##
[[3]]
[1] 7
attr(,"match.length")
[1] 4
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
##
[[4]]
[1] -1
attr(,"match.length")
[1] -1
attr(,"index.type")
```

I DEEP

(continued from previous page)

```
[1] "chars"
attr(,"useBytes")
[1] TRUE
```

As we noted in Section 4.4.2, wrapping the results in a list was a clever choice for the number of matches can obviously vary between strings.

In Section 7.2, we will look at the Map function, which, along with substring introduced below, can aid in getting the most out of such data. Meanwhile, let us just mention that regmatches extracts the matching substrings:

```
regmatches(x, gregexpr("(?i)spam\\p{L}*", x, perl=TRUE))
[[1]]
[1] "spam"
##
[[2]]
[1] "spammite" "spam"
##
[[3]]
[1] "SPAM"
##
[[4]]
character(0)
```

**Note** (\*) Let us consider what happens when a regular expression contains parenthesised subexpressions (capture groups).

```
r <- "(?<basename>[^.]+)\\.(?<extension>[^]*)"
```

The above regex consists of two capture groups separated by a dot. The first one is labelled "basename". It comprises several arbitrary characters except for spaces and dots. The second group, named "extension", is a substring consisting of anything but spaces.

Such a pattern can be used for unpacking space-delimited lists of file names.

```
z <- "dataset.csv.gz something_else.txt spam"</pre>
regexpr(r, z, perl=TRUE)
[1] 1
attr(,"match.length")
[1] 14
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
```

(continued from previous page)

```
attr(,"capture.start")
##
 basename extension
 1
[1,]
attr(,"capture.length")
 basename extension
[1,]
 7
attr(,"capture.names")
[1] "basename" "extension"
gregexpr(r, z, perl=TRUE)
[[1]]
[1] 1 16
attr(,"match.length")
[1] 14 18
attr(,"index.type")
[1] "chars"
attr(,"useBytes")
[1] TRUE
attr(,"capture.start")
basename extension
[1,]
 1
[2,]
 16
 31
attr(,"capture.length")
basename extension
[1,]
 7 6
[2,]
 14
attr(,"capture.names")
[1] "basename" "extension"
```

The capture.\* attributes give us access to the matches to the individual capture groups, i.e., the basename and the extension.

**Exercise 6.4** (\*) Check out the difference between the results generated by **regexec** and **regexer** as well as between the outputs of **gregexec** and **gregexpr**.

## 6.2.6 Replacing pattern occurrences

**sub** and **gsub** can replace first and all, respectively, matches to a pattern:

**Note** (\*) If a regex defines capture groups, matches thereto can be mentioned not only in the pattern itself but also in the replacement string:

```
gsub("(\p{L})\p{L}\1", "\1", "aha egg gag NaN spam", perl=TRUE)
[1] "a egg g N spam"
```

The above matches in the following order: a letter (it is a capture group), another letter, and the former letter again. Each such palindrome of length three is replaced with just the repeated letter.

**Exercise 6.5** (\*) Display the source code of **glob2rx** by calling **print**(glob2rx) and study how this function converts wildcards such as file???..\* or \*.csv to regular expressions that can be passed to, e.g., list.files.

### Splitting strings into tokens

**strsplit** divides each string in a character vector into chunks.

```
strsplit(c("spam;spam;eggs;;bacon", "spam"), ";", fixed=TRUE)
[[1]]
[1] "spam" "spam" "eggs" ""
 "bacon"
[[2]]
[1] "spam"
```

Note that this time the search pattern specifying the token delimiter is given as the second argument (an inconsistency).

#### Other string operations 6.3

## 6.3.1 Extracting substrings

**substring** extracts parts of strings between given character position ranges.

```
substring("spammity spam", 1, 4) # from the first to the fourth character
[1] "spam"
substring("spammity spam", 10) # from the tenth to end
[1] "spam"
substring("spammity spam", c(1, 10), c(4, 14)) # vectorisation
[1] "spam" "spam"
substring(c("spammity spam", "bacon and eggs"), 1, c(4, 5))
[1] "spam" "bacon"
```

**Note** There is also a replacement (compare Section 9.3.6) version of the above:

```
x <- "spam, spam, bacon, and spam"
substring(x, 7, 11) <- "eggs"
print(x)
[1] "spam, eggs, bacon, and spam"</pre>
```

Unfortunately, the number of characters in the replacement string should not exceed the length of the part being substituted (try "chickpeas" instead of "eggs"). However, substring replacement can be written as a composition of substring extraction and concatenation:

```
paste(substring(x, 1, 6), "chickpeas", substring(x, 11), sep="")
[1] "spam, chickpeas, bacon, and spam"
```

**Exercise 6.6** Take the output generated by **regexpr** and apply **substring** to extract the pattern occurrences. If there is no match in a string, the corresponding output should be NA.

#### 6.3.2 Translating characters

tolower and toupper converts between lower and upper case:

```
toupper("spam")
[1] "SPAM"
```

**Note** Like many other string operations in base R, these functions perform very simple character substitutions. They might not be valid in natural language processing tasks. For instance, *groß* is *not* converted to *GROSS*, being the correct case folding in German.

Moreover, chartr translates individual characters:

```
chartr("\\", "/", "c:\\windows\\system\\cmd.exe") # chartr(old, new, x)
[1] "c:/windows/system/cmd.exe"
chartr("([S", ")]*", ":(:S :[")
[1] ":) :* :]"
```

In the first line, we replace each backslash with a slash. The second example replaces "(", "[", and "S" with ")", "]", and "\*", respectively.

## 6.3.3 Ordering strings

We have previously mentioned that operators and functions such as `<`, `>=`, sort, order, rank, and xtfrm<sup>9</sup> are based on the lexicographic ordering of strings.

```
sort(c("chłodny", "hardy", "chladný", "hladný"))
[1] "chladný" "chłodny" "hardy" "hladný"
```

It is worth noting that the ordering depends on the currently selected locale; see **Sys. getlocale**("LC\_COLLATE"). For instance, in the Slovak language setting, we would obtain "hardy" < "chladný" < "chladný" < "chlodny".

**Note** Many "structured" data items can be displayed or transmitted as humanreadable strings. In particular, we know that **as.numeric** can convert a string to a number. Moreover, Section 10.3.1 will discuss date-time objects such as "1970-01-01 00:00:00 GMT". We will be processing them with specialised functions such as **strptime** and **strftime**.

**Important** (\*) Many string operations in base R are not necessarily portable. The **stringx** package defines drop-in, "fixed" replacements therefor. They are based on the International Components for Unicode ( $ICU^{10}$ ) library, a de facto standard for processing Unicode text, and the R package **stringi**; see [27].

```
call install.packages("stringx") first
suppressPackageStartupMessages(library("stringx")) # load the package
sort(c("chlodny", "hardy", "chladný", "hladný"), locale="sk_SK")
[1] "hardy" "hladný" "chladný" "chlodny"
toupper("gro\u00DF") # compare base::toupper("gro\u00DF")
[1] "GROSS"
detach("package:stringx") # remove the package from the search path
```

## 6.4 Other atomic vector types (\*)

We have discussed four vector types: logical, double, character, and list. To get a more complete picture of the sequence-like types in R, let us briefly mention integer, complex, and raw atomic types so that we are not surprised when we encounter them.

<sup>&</sup>lt;sup>9</sup> See Section 12.3.1 for a use case.

<sup>10</sup> https://icu.unicode.org/

#### 6.4.1 Integer vectors (\*)

Integer scalars can be input manually by using the L suffix:

```
(x <- c(1L, 2L, -1L, NA_integer_)) # looks like numeric
[1] 1 2 -1 NA
typeof(x) # but is integer
[1] "integer"</pre>
```

Some functions return them in a few contexts<sup>11</sup>:

```
typeof(1:10) # seq(1, 10) as well, but not seq(1, 10, 1)
[1] "integer"
as.integer(c(-1.1, 0, 1.9, 2.1)) # truncate/round towards 0
[1] -1 0 1 2
```

In most expressions, integer vectors behave like numeric ones. They are silently coerced to double if need be. Usually, there is no practical<sup>12</sup> reason to distinguish between them. For example:

```
1L/2L # like 1/2 == 1.0/2.0
[1] 0.5
```

**Note** (\*) R integers are 32-bit signed types. In the double type, we can store more of them. The maximal contiguously representable integer is  $2^{31} - 1$  and  $2^{53}$ , respectively; see Section 3.2.3:

```
as.integer(2^31-1) + 1L # 32-bit integer overflow
Warning in as.integer(2^31 - 1) + 1L: NAs produced by integer overflow
[1] NA
as.integer(2^31-1) + 1 == 2^31 # integer+double == double - OK
[1] TRUE
(2^53 - 1) + 1 == 2^53 # OK
[1] TRUE
(2^53 + 1) - 1 == 2^53 # lost due to FP rounding; left side equals 2^53 - 1
[1] FALSE
```

**Note** Since R 3.0, there is support for vectors longer than  $2^{31} - 1$  elements. As there are no 64-bit integers in R, long vectors are indexed by doubles (we have been doing all this time). In particular, x[1.9] is the same as x[1], and x[-1.9] means x[-1], i.e.,

<sup>&</sup>lt;sup>11</sup> Actually, 1:10 returns an integer vector in a compact (ALTREP; see [55]) form; compare the results of the call to .Internal(inspect(1:10)) and .Internal(inspect(seq(1, 10, 1))). This way, the whole vector does not have to be allocated. This saves memory and time. At the R level, though, it behaves as any other integer (numeric) sequence.

<sup>&</sup>lt;sup>12</sup> They are of *internal* interest, e.g., when writing C/C++ extensions; see Chapter 14.

#### 6.4.2 Raw vectors (\*)

Vectors of the type raw can store bytes, i.e., unsigned 8-bit integers, whose range is 0–255. For example:

```
as.raw(c(-1, 0, 1, 2, 0xc0, 254, 255, 256, NA))
Warning: out-of-range values treated as 0 in coercion to raw
[1] 00 00 01 02 c0 fe ff 00 00
```

They are displayed as two-digit hexadecimal (base-16) numbers. There are no raw NAS.

Only a few functions deal with such vectors: e.g., readBin, charToRaw, and rawToChar.

Interestingly, the meaning of the logical operators differs for raw vectors; they denote bitwise operations. See also **bitwAnd**, **bitwOr** etc. that work on integer vectors.

```
xor(as.raw(0xf0), as.raw(0x0f))
[1] ff
bitwXor(0x0fff0f00, 0x0f00f0ff)
[1] 16777215
```

**Example 6.7** (\*) One use case of bitwise operations is for representing a selection of items in a small set of possible values. This can be useful for communicating with routines implemented in C/C++. For instance, let us define three flags:

```
HAS_SPAM <- 0x01 # binary 00000001
HAS_BACON <- 0x02 # binary 00000010
HAS_EGGS <- 0x04 # binary 00000100
```

Now a particular subset can be created using the bitwise OR:

```
dish <- bitwOr(HAS_SPAM, HAS_EGGS) # {spam, eggs}
```

Testing for inclusion is done via the bitwise AND:

```
as.logical(bitwAnd(dish, c(HAS_SPAM, HAS_BACON, HAS_EGGS)))
[1] TRUE FALSE TRUE
```

## 6.4.3 Complex vectors (\*)

We can also play with vectors of the type complex, with "1i" representing the imaginary unit,  $\sqrt{-1}$ . Complex numbers appear in quite a few engineering or scientific applications, e.g., in physics, electronics, or signal processing. They are (at least: ought to

be) part of introductory subjects or textbooks in university-level mathematics, including the statistics- and machine learning-orientated ones because of their heavy use of numerical computing; see e.g., [19, 30].

```
c(0, 1i, pi+pi*1i, NA_complex_)
[1] 0.0000+0.0000i 0.0000+1.0000i 3.1416+3.1416i NA
```

Apart from the basic operators, mathematical and aggregation functions, procedures like **fft**, **solve**, **qr**, or **svd** can be fed with or produce such data. For more details, see **help**("complex") and some matrix examples in Chapter 11.

#### 6.5 Exercises

Exercises marked with (\*) might require tinkering with regular expressions or third-party R packages.

**Exercise 6.8** Answer the following questions.

- How many characters are there in the string "ab\n\\\t\\\\""? What about r"-{ab\n\\\\\\"-}? "?
- What is the result of a call to paste(NA, 1:5, collapse="")?
- What is the meaning of the following **sprintf** format strings: "%s", "%20s", "%-20s", "%f", "%g", "%e", "%5f", "%5.2f%", "%.2f", "%0+5f", and "[%+-5.2f]"?
- What is the difference between regexpr and gregexpr? What does "g" in the latter function name stand for?
- What is the result of a call to **grepl**(c("spam", "spammity spam", "aubergines"), "spam")?
- Is it always the case that ""Aaron" < "Zorro""?
- Why "x < "10"" and "x < 10" may return different results?
- If x is a character vector, is "x == x" always equal to TRUE?
- If x and y are character vectors of lengths n and m, respectively, what is the length of the output of match(x, y)?
- If x is a named vector, why is there a difference between x[NA] and  $x[NA\_character\_]$ ?
- What is the difference between "x == y" and "x %in% y"?

**Exercise 6.9** Let x, y, and z be atomic vectors and a and b be single strings. Generate the same results as pastena(x, collapse=b), pastena(x, y, sep=a), pastena(x, y, sep=a), pastena(x, y, z, sep=a), pastena(x, y, z

**Exercise 6.10** Based on **list.files** and **glob2rx**, generate the list of all PDFs on your computer. Then, use **file.size** to filter out the files smaller than 10 MiB.

**Exercise 6.11** Read a text file that stores a long paragraph of some banal prose. Concatenate all the lines to form a single, long string. Using **strwrap** and **cat**, output the paragraph on the console, nicely formatted to fit a block of text of an aesthetic width, say, 60 columns.

**Exercise 6.12** (\*) Implement a simplified version of basename and dirname.

**Exercise 6.13** (\*) Implement an operation similar to **trimus** using the functions introduced in this chapter.

**Exercise 6.14** (\*) Write a regex that extracts all words from each string in a given character vector.

**Exercise 6.15** (\*) Write a regex that extracts, from each string in a character vector, all:

- integers numbers (signed or unsigned),
- floating-point numbers,
- numbers of any kind (including those in scientific notation),
- · #hashtags,
- email@address.es,
- hyperlinks of the form http://... and https://....

**Exercise 6.16** (\*) What do 42i, 42L, and 0x42 stand for?

Exercise 6.17 (\*) Check out stri\_sort in the stringi package (or sort.character in stringx) for a way to obtain an ordering like "a1" < "a2" < "a10" < "a11" < "a100".

**Exercise 6.18** (\*) In **sprintf**, the formatter "%20s" means that if a string is less than 20 bytes long, the remaining bytes will be replaced with spaces. Only for ASCII characters (English letters, digits, some punctuation marks, etc.), it is true that one character is represented by one byte. Other Unicode code points can take up between two and four bytes.

```
cat(sprintf("..%6s..", c("abc", "1!<", "aßc", "qß@")), sep="\n") # aligned?
.. abc..
.. 1!<..
.. aßc..
.. aße..</pre>
```

Use the **stri\_pad** function from the **stringi** package to align the strings aesthetically. Alternatively, check out **sprintf** from **stringx**.

**Exercise 6.19** (\*) Implement an operation similar to **stri\_pad** from **stringi** using the functions introduced in this chapter.

# **Functions**

R is a *functional* language, i.e., one where functions play first fiddle. Each action we perform reduces itself to a call to some function or a combination thereof.

So far, we have been tinkering with dozens of available functions which were mostly part of base R. They constitute the essential vocabulary that everyone *must* be able to speak fluently.

Any operation, be it **sum**, **sqrt**, or **paste**, when fed with a number of arguments, generates a (hopefully fruitful) return value.

```
sum(1:10) # invoking `sum` on a specific argument
[1] 55
```

From a user's perspective, each function is merely a tool. To achieve a goal at hand, we do not have to care about what is going on under its bonnet, i.e., how the inputs are being transformed so that, after a couple of nanoseconds or hours, we can relish what has been bred. This is very convenient: all we need to know is the function's specification which can be stated, for example, informally, in plain Polish or Malay, on its help page.

In this chapter, we will learn how to write our own functions. Using this skill is a good development practice when we expect that the same operations will need to be executed many times but perhaps on different data.

Also, some functions invoke other procedures, for instance, on every element in a list or every section of a data frame grouped by a qualitative variable. Thus, it is advisable to learn how we can specify a custom operation to be propagated thereover.

#### **Example 7.1** Given some objects (whatever):

```
x1 <- runif(16)
x2 <- runif(32)
x3 <- runif(64)
```

assume we want to apply the same action on different data, say, compute the root mean square. Then, instead of retyping almost identical expressions (or a bunch of them) over and over again:

```
sqrt(mean(x1^2)) # very fresh
[1] 0.6545
sqrt(mean(x2^2)) # the same second time; borderline okay
(continues on next page)
```

I DEEP

(continued from previous page)

```
[1] 0.56203
sqrt(mean(x3^2)) # third time the same; tedious, barbarous, and error-prone
[1] 0.57206
```

we can generalise the operation to any object like x:

```
bind the name `rms` to...
rms <-
 function(x)
 # a function that takes one parameter, `x`
 sqrt(mean(x^2)) # transforming the input to yield output this way
```

and then reuse it on different concrete data instances:

```
rms(x1)
[1] 0.6545
rms(x2)
[1] 0.56203
rms(x3)
[1] 0.57206
```

or even combine it with other function calls:

```
rms(sqrt(c(x1, x2, x3)))^2
[1] 0.50824
```

Thus, custom functions are very useful.

**Important** Does writing own functions equal reinventing the wheel? Can everything be found online these days (including on Stack Overflow, GitHub, or CRAN)? Luckily, it is not the case. Otherwise, data analysts', researchers', and developers' lives would be monotonous, dreary, and uninspiring. What is more, we might be able to compose a function from scratch much more quickly than to get through the whole garbage dump called the internet from where, only occasionally, we can dig out some pearls. Let us remember that we advocate for minimalism in this book. We will reflect on such issues in Chapter 9. There is also the personal growth side: we become better programmers by crunching those exercises.

#### Creating and invoking functions 7.1

## 7.1.1 Anonymous functions

Functions are usually created through the following notation:

```
function(args) body
```

First, args is a (possibly empty) list of comma-separated parameter names which act as *input* variables.

Second, body is a *single* R expression that is evaluated when the function is called. The value this expression yields will constitute the function's output.

For example, here is a definition of a function that takes no inputs and generates a constant output:

```
function() 1
function() 1
```

We thus created a *function* object. However, as we have not used it at all, it disappeared immediately thereafter.

Any function **f** can be *invoked*, i.e., evaluated on *concrete* data, using the syntax **f**(arg1, ..., argn). Here, arg1, ..., argn are expressions passed as *arguments* to **f**.

```
(function() 1)() # invoking f like f(); here, no arguments are expected
[1] 1
```

Only now have we obtained a return value.

**Note** (\*) Calling **typeof** on a function object will report "closure" (user-defined functions), "builtin", or "primitive" (built-in, base ones) for the reasons that we explain in more detail in Section 9.4.3 and Section 16.3.2. In our case:

```
typeof(function() 1)
[1] "closure"
```

#### 7.1.2 Named functions

Names can be bound to function objects. This way, we can refer to them multiple times:

```
one <- function() 1 # one <- (function() 1)</pre>
```

We created an object named **one** (we use bold font to indicate that it is of the type function for functions are so crucial in R). We are very familiar with such a notation, as not since yesterday we are used to writing "x <- 1", etc.

Invoking one, which can be done by writing one(), will generate a return value:

```
one() # (function() 1)()
[1] 1
```

This output can be used in further computations. For instance:

```
0:2 - one() # 0:2 - (function() 1)(), i.e., 0:2 - 1
[1] -1 0 1
```

#### 7.1.3 Passing arguments to functions

Functions with no arguments are kind of boring. Thus, let us distil a more highbrowed operation:

```
concat <- function(x, y) paste(x, y, sep="")</pre>
```

We created a mapping whose aim is to concatenate two objects using a specialised call to **paste**. Yours faithfully pleads guilty to multiplying entities needlessly: it *should* not be a problem for anyone to write **paste**(x, y, sep="") each time. Yet, 'tis merely an illustration.

The **concat** function has two *parameters*, x and y. Hence, calling it will require the provision of two *arguments*, which we put within round brackets and separate from each other by commas.

```
u <- 1:5
concat("spam", u) # i.e., concat(x="spam", y=1:5)
[1] "spam1" "spam2" "spam3" "spam4" "spam5"</pre>
```

**Important** Notice the distinction: *parameters* (*formal arguments*) are abstract, general, or symbolic; "something, anything that will be put in place of x when the function is invoked". Contrastingly, *arguments* (*actual parameters*) are concrete, specific, and real.

During the above call, x in the function's body is precisely "spam" and nothing else. Also, the u object from the caller's environment can be accessed via y in **concat**. Most of the time (yet, see Section 16.3), it is best to think of the function as being fed not with u per se but the value that u is bound to, i.e., 1:5.

Also:

```
x <- 1:5
y <- "spam"
concat(y, x) # concat(x="spam", y=1:5)
[1] "spam1" "spam2" "spam3" "spam4" "spam5"</pre>
```

This call is equivalent to **concat**(x=y, y=x). The argument x is assigned the value of y from the calling environment, "spam". Let us stress that one x is not the same as the other x; which is which is unambiguously defined by the context.

**Exercise 7.2** Write a function **standardise** that takes a numeric vector x as argument and re-

turns its standardised version, i.e., from each element in x, subtract the sample arithmetic mean and then divide it by the standard deviation.

**Note** Section 2.1.3 mentioned that, syntactically speaking, the following are perfectly valid alternatives to the positionally-matched call **concat**("spam", u):

```
concat(x="spam", y=u)
concat(y=u, x="spam")
concat("spam", y=u)
concat(u, x="spam")
concat(x="spam", u)
concat(y=u, "spam")
```

However, we recommend to avoid the last two for the sake of the readers' sanity. It is best to provide positionally-matched arguments before the keyword-based ones; see Section 15.4.4 for more details.

Also, Section 10.4 introduces the (overused) forward pipe operator, `|>`, which will enable us to write the above as ""spam" |> concat(u)".

### 7.1.4 Grouping expressions with curly braces, `{`

We have been informed that a function's body is a *single* R expression whose evaluated value is passed to the user as its output. This may sound restrictive and in contrast with what we have experienced so far. Rarely are we faced with such simple computing tasks, and we have already seen R functions performing quite sophisticated operations.

Grammatically, a single R expression can be arbitrarily complex (Chapter 15). We can use curly braces to group many calls that are to be evaluated one after another. For instance:

```
{
 cat("first expression\n")
 cat("second expression\n")
 # ...
 cat("last expression\n")
}
first expression
second expression
last expression
```

We used four spaces to visually indent the constituents for greater readability (some developers prefer tabs over spaces, others find two or three spaces more urbane, but we do not). This single (compound) expression can now play a role of a function's body.

**Important** The last expression evaluated in a curly-braces delimited block will be considered its output value.

```
x <- {
 1
 2
 3 # <--- last expression: will be taken as the output value
}
print(x)
[1] 3</pre>
```

The above code block can also be written more concisely by replacing newlines with semicolons, albeit with perhaps some loss in readability:

```
{1; 2; 3}
[1] 3
```

Section 9.3 will give a few more details about `{`.

**Example 7.3** Here is a version of the above **concat** function, which guarantees a more Chapter 2-style missing values' propagation:

```
concat <- function(a, b)
{
 z <- paste(a, b, sep="")
 z[is.na(a) | is.na(b)] <- NA_character_
 z # last expression in the block - return value
}</pre>
```

Example calls:

```
concat("a", 1:3)
[1] "a1" "a2" "a3"
concat(NA_character_, 1:3)
[1] NA NA NA
concat(1:6, c("a", NA_character_, "c"))
[1] "1a" NA "3c" "4a" NA "6c"
```

Let us appreciate the fact that we could keep the code brief thanks to **paste**'s and `**I**`'s implementing the recycling rule.

**Exercise 7.4** Write a function **normalise** that takes a numeric vector x and returns its version shifted and scaled to the [0,1] interval. To do so, subtract the sample minimum from each element, and then divide it by the range, i.e., the difference between the maximum and the minimum. Avoid computing min(x) twice.

Exercise 7.5 Write a function that applies the robust standardisation of a numeric vector: sub-

tract the median and divide it by the median absolute deviation, 1.4826 times the median of the absolute differences between the values and their median.

**Note** R is an open-source (free, libre) project distributed under the terms of the GNU General Public License version 2. Therefore, we are not only encouraged to run the software for whatever purpose, but also study and modify its source code without restrictions. To facilitate this, we can display all function definitions:

```
print(concat) # code of the above procedure
function(a, b)
{
 z <- paste(a, b, sep="")</pre>
 z[is.na(a) | is.na(b)] <- NA character
 z # last expression in the block - return value
}
print(union) # a built-in function
function (x, y)
{
 u <- as.vector(x)</pre>
##
 v <- as.vector(v)</pre>
##
 unique(c(u, v))
##
}
<environment: namespace:base>
```

Nevertheless, some functionality might be implemented in compiled programming languages such as C, C++, or Fortran; notice a call to .Internal in the source code of paste, .Primitive in list, or .Call in runif. Therefore, we will sometimes have to dig a bit deeper to access the underlying definition; see Chapter 14 for more details.

## 7.2 Functional programming

R is a *functional* programming language. As such, it shares several features with other languages that emphasise the role of function manipulation in software development (e.g., Common Lisp, Scheme, OCaml, Haskell, Clojure, F#). Let us explore these commonalities now.

## 7.2.1 Functions are objects

R functions were given the right to a fair go; they are what we refer to as first-class citizens. In other words, our interaction with them is not limited to their invocation; we treat them as any other language object.

• They can be stored inside list objects, which can embrace R objects of any kind:

```
list(identity, NROW, sum) # a list storing three functions
[[1]]
function (x)
x
<environment: namespace:base>
##
[[2]]
function (x)
if (length(d <- dim(x))) d[1L] else length(x)
<environment: namespace:base>
[[3]]
function (..., na.rm = FALSE) .Primitive("sum")
```

• They can be created and then called inside another function's body:

```
euclidean distance <- function(x, y)</pre>
{
 square <- function(z) z^2 # auxiliary/internal/helper function
 sqrt(sum(square(x-y))) # square root of the sum of squares
}
euclidean_distance(c(0, 1), c(1, 0)) # example call
[1] 1.4142
```

This is why we tend to classify functions as representatives of recursive types (compare is.recursive).

• They can be passed as arguments to other operations:

```
Replaces missing values with a given aggregate
of all non-missing elements:
fill_na <- function(x, filler_fun)</pre>
{
 missing ones <- is.na(x) # otherwise, we'd have to call is.na twice
 replacement value <- filler fun(x[!missing ones])</pre>
 x[missing_ones] <- replacement_value
 Х
}
fill_na(c(0, NA_real_, NA_real_, 2, 3, 7, NA_real_), mean)
[1] 0 3 3 2 3 7 3
fill_na(c(0, NA_real_, NA_real_, 2, 3, 7, NA_real_), median)
[1] 0.0 2.5 2.5 2.0 3.0 7.0 2.5
```

Procedures like this are called higher-order functions.

**Note** More advanced techniques, which we will discuss in the third part of the book, will let the functions be:

- returned as other function's outputs,
- equipped with auxiliary data,
- generated programmatically on the fly,
- modified at runtime.

Below we review the most basic higher-order functions, including do.call and Map.

#### 7.2.2 Calling on precomputed arguments with do.call

Notation like f(arg1, ..., argn) has no monopoly over how we call a function on a specific sequence of arguments. The list of actual parameters does not have to be hardcoded.

Here is an alternative. We can first prepare a number of objects to be passed as **f**'s inputs, wrap them in a list 1, and then invoke **do.call(f, 1)** to get the same result.

```
words <- list(
 c("spam",
 "bacon",
 "eggs"),
 c("buckwheat", "quinoa", "barley"),
 "spam",
 "spam")
 c("ham",
do.call(paste, words) # paste(words[[1]], words[[2]], words[[3]])
[1] "spam buckwheat ham" "bacon quinoa spam" "eggs barley spam"
do.call(cbind, words) # column-bind; returns a matrix (explained later)
 [,1]
 Γ,27
[1,] "spam" "buckwheat" "ham"
[2,] "bacon" "quinoa"
 "spam"
[3,] "eggs" "barley"
 "spam"
do.call(rbind, words) # row-bind (explained later)
 [,1]
 [,2]
 Γ,37
[1,] "spam"
 "bacon" "eaas"
[2,] "buckwheat" "quinoa" "barley"
[3,] "ham"
 "spam"
 "spam"
```

The length and content of the list passed as the second argument of **do.call** can be arbitrary (possibly unknown at the time of writing the code). See Section 12.1.2 for more use cases, e.g., ways to concatenate a list of data frames (perhaps produced by some complex chain of commands) into a single data frame.

If elements of the list are named, they will be matched to the corresponding keyword arguments.

```
x <- 2^(seq(-2, 2, length.out=101))
plot_opts <- list(col="red", lty="dashed", type="l")
do.call(plot, c(list(x, log2(x), xlab="x", ylab="log2(x)"), plot_opts))
(plot display suppressed)</pre>
```

Notice that our favourite plot\_opts can now be reused in further calls to graphics functions. This is very convenient as it avoids repetitions.

#### 7.2.3 Common higher-order functions

There is an important class of higher-order functions that permit us to apply custom operations on consecutive elements of sequences without relying on loop-like statements, at least explicitly. They can be found in all functional programming languages (e.g., Lisp, Haskell, Scala) and have been ported to various add-on libraries (**functools** in Python, more recent versions of the C++ Standard Library, etc.) or frameworks (Apache Spark and the like). Their presence reflects the obvious truth that certain operations occur more frequently than others. In particular:

- Map calls a function on each element of a sequence in order to transform:
  - their individual components (just like sqrt, round, or the unary `!` operator in R), or
  - the corresponding elements of many sequences so as to vectorise a given operation elementwisely (compare the binary `+` or paste),
- Reduce (also called accumulate) applies a binary operation to combine consecutive elements in a sequence, e.g., to generate the aggregates, like, totally (compare sum, prod, all, max) or cumulatively (compare cumsum, cummmin),
- Filter creates a subset of a sequence that is comprised of elements that enjoy a given property (which we typically achieve in R by means of the `[` operator),
- **Find** locates the first element that fulfils some logical condition (compare **which**).

Below we will only focus on the Map function. The inspection of the remaining ones is left as an exercise. This is because, oftentimes, we can be better off with their more R-ish versions (e.g., using the subsetting operator, `[`).

## 7.2.4 Vectorising functions with Map

In data-centric computing, we are frequently faced with tasks that involve processing each vector element independently, one after another. Such use cases can benefit from vectorised operations like those discussed in Chapter 2, Chapter 3, and Chapter 6.

Unfortunately, most of the functions that we introduced so far cannot be applied on lists. For instance, if we try calling **sqrt** on a generic vector, we will get an error, even if it is a list of numeric sequences only. One way to compute the square root of all elements would be to invoke **sqrt(unlist(...))**. It is a go-to approach if we wish to

treat all the list's elements as one sequence. However, this comes at the price of losing the list's structure.

We have also discussed a few operations that are not vectorised with respect to all their arguments, even though they could have been designed this way, e.g., grepl.

The Map function<sup>1</sup> applies an operation on each element in a vector or the corresponding elements in a number of vectors. In many situations, it may be used as a more elegant alternative to **for** loops that we will introduce in the next chapter.

First<sup>2</sup>, a call to Map(f, x) yields a list whose *i*-th element is equal to f(x[[i]]) (recall that [[x]]) works on atomic vectors too). For example:

```
x <- list(# an example named list
 x1=1:3.
 x2=seq(0, 1, by=0.25),
 x3=c(1, 0, NA_real_, 0, 0, 1, NA_real_)
Map(sqrt, x) # x is named, hence the result will be named as well
$x1
[1] 1.0000 1.4142 1.7321
$x2
[1] 0.00000 0.50000 0.70711 0.86603 1.00000
##
$x3
[1] 1 0 NA 0 0 1 NA
Map(length, x)
$x1
[11 3
##
$x2
[1] 5
##
$x3
[1] 7
unlist(Map(mean, x)) # compute three aggregates, convert to an atomic vector
x1 x2 x3
2.0 0.5 NA
Map(function(n) round(runif(n, -1, 1), 1), c(2, 4, 6)) # x is atomic now
[[1]]
[1] 0.4 0.8
```

(continues on next page)

<sup>&</sup>lt;sup>1</sup> Yes, the author is aware that **Map** was implemented using the slightly more primitive **mapply** but we are not fond of the latter function's having the SIMPLIFY argument set to TRUE by default.

<sup>&</sup>lt;sup>2</sup> This use case scenario can also be programmed using lapply; lapply(x, f, ...) is equivalent to Map(f, x, MoreArgs=list(...)).

```
##
[[2]]
[1] 0.5 0.8 -0.1 -0.7
##
[[3]]
[1] -0.3 0.0 0.5 1.0 -0.9 -0.7
```

Next, we can vectorise a given function over several parameters. A call to, e.g., Map(f, x, y, z) breeds a list whose *i*-th element is equal to f(x[[i]], y[[i]], z[[i]]). Like in the case of, e.g., paste, the recycling rule will be applied if necessary.

For example, the following generates list(seq(1, 6), seq(11, 13), seq(21, 29)):

```
Map(seq, c(1, 11, 21), c(6, 13, 29))

[[1]]

[1] 1 2 3 4 5 6

##

[[2]]

[1] 11 12 13

##

[[3]]

[1] 21 22 23 24 25 26 27 28 29
```

Moreover, we can get list(seq(1, 40, length.out=10), seq(11, 40, length.out=5), seq(21, 40, length.out=10), seq(31, 40, length.out=5)) by calling:

```
Map(seq, c(1, 11, 21, 31), 40, length.out=c(10, 5))
[[1]]
[1] 1.0000 5.3333 9.6667 14.0000 18.3333 22.6667 27.0000 31.3333
[9] 35.6667 40.0000
##
[[2]]
[1] 11.00 18.25 25.50 32.75 40.00
##
[[3]]
[1] 21.000 23.111 25.222 27.333 29.444 31.556 33.667 35.778 37.889 40.000
##
[[4]]
[1] 31.00 33.25 35.50 37.75 40.00
```

**Note** If we have some additional arguments to be passed to the function applied (which it does not have to be vectorised over), we can wrap them inside a separate list and toss it via the MoreArgs argument (à la do.call).

```
unlist(Map(mean, x, MoreArgs=list(na.rm=TRUE))) # mean(..., na.rm=TRUE)
x1 x2 x3
2.0 0.5 0.4
```

Alternatively, we can always construct a custom anonymous function:

```
unlist(Map(function(xi) mean(xi, na.rm=TRUE), x))
x1 x2 x3
2.0 0.5 0.4
```

**Exercise 7.6** Here is an example list of files (see our teaching data repository<sup>3</sup>) with daily Forex rates:

```
file_names <- c(
 "euraud-20200101-20200630.csv",
 "eurgbp-20200101-20200630.csv",
 "eurusd-20200101-20200630.csv"
)</pre>
```

Call Map to read them with scan. Determine each series' minimal, mean, and maximal value.

**Exercise 7.7** Implement your version of the **Filter** function based on a call to **Map**.

## 7.3 Accessing third-party functions

When we indulge in the writing of a software piece, a few questions naturally arise. Is the problem we are facing fairly complex? Has it already been successfully addressed in its entirety? If not, can it, or its parts, be split into manageable chunks? Can it be constructed based on some readily available nontrivial components?

A smart developer is independent but knows when to stand on the shoulders to cry on. Let us explore a few ways to reuse the existing function libraries.

## 7.3.1 Using R packages

Most contributed R extensions come in the form of add-on packages, which can include:

- reusable code (e.g., new functions),
- data (which we can exercise on),
- documentation (manuals, vignettes, etc.);

see Section 9.2.2 for more and Writing R Extensions [63] for all the details.

<sup>&</sup>lt;sup>3</sup> https://github.com/gagolews/teaching-data/tree/master/marek

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Most packages are published in the moderated repository that is part of the Comprehensive R Archive Network (CRAN<sup>4</sup>). However, there are also other popular sources such as Bioconductor<sup>5</sup> which specialises in bioinformatics.

We call install.packages("pkg") to fetch a package pkg from a repository (CRAN by default; see, however, the repos argument).

A call to library("pkg") loads an indicated package and makes the exported objects available to the user (i.e., attaches it to the search path; see Section 16.2.6).

For instance, in one of the previous chapters, we have mentioned the **gsl** package:

```
call install.packages("gsl") first
library("gsl") # load the package
poch(10, 3:6) # calls gsl sf poch() from GNU GSL
[1]
 1320
 17160 240240 3603600
```

Here, **poch** is an object exported by package **gsl**. If we did not call **library**("gsl"), trying to access the former would raise an error.

We could have also accessed the above function without attaching it to the search path using the **pkg**::object syntax, namely, **gsl**::**poch**.

**Note** For more information about any R extension, call help(package="pkg"). Also, it is advisable to visit the package's CRAN entry at an address like https://CRAN.Rproject.org/package=pkg to access additional information, e.g., vignettes. Why waste our time and energy by querying a web search engine that will likely lead us to a dodgy middleman when we can acquire authoritative knowledge directly from the source?

Moreover, it is worth exploring various CRAN Task Views<sup>6</sup> that group the packages into topics such as Genetics, Graphics, and Optimisation. They are curated by experts in their relevant fields.

Important Frequently, R packages are written in their respective authors' free time, many of whom are volunteers. Neither get they paid for this, nor do it as part of the so-called their job. Yes, not everyone is driven by money or fame.

Someday, when we come up with something valuable for the community, we will become one of them. Before this happens, we can show appreciation for their generosity by, e.g., spreading the word about their software by citing it in publications (see citation(package="pkg")), talking about them during lunchtime, or mentioning them in (un)social media. We can also help them improve the existing code base by reporting

<sup>4</sup> https://cloud.r-project.org/

<sup>&</sup>lt;sup>5</sup> https://bioconductor.org/

<sup>6</sup> https://cloud.r-project.org/web/views

bugs, polishing documentation, proposing new features, or cleaning up the redundant fragments of their APIs.

### Default packages

The **base** package is omnipresent. It provides us with the most crucial functions such as the vector addition, **c**, **Map**, and **library**. Certain other extensions are also loaded by default:

```
getOption("defaultPackages")
[1] "datasets" "utils" "grDevices" "graphics" "stats"
[6] "methods"
```

This list can, theoretically, be changed<sup>7</sup>. However, in this book, we assume that the above are always attached because it is reasonable to do so. This is why in Section 2.4.5, there was no need to call, for example, **library**("stats") before referring to the **var** and **sd** functions.

On a side note, grDevices and graphics will be discussed in Chapter 13. methods will be mentioned in Section 10.5. datasets brings a few example R objects on which we can exercise our skills. The functions from utils, graphics, and stats already appeared here and there.

**Exercise 7.8** Use the **find** function to determine which packages define **mean**, **var**, **find**, and **Map**. Recall from Section 1.4 where such information can be found in these objects' manual pages.

### Source vs binary packages (\*)

R is an open environment. Therefore, its packages are published primarily in the source form. This way, anyone can study how they work and improve them or reuse parts thereof in different projects.

If we call **install.packages**("path", repos=NULL, type="source"), we should be able to install a package from sources: path can be pinpointing either a directory or a source tarball (most often as a compressed pkg\_version.tar.gz file; see **help**("untar")).

Note that type="source" is the default unless one is on a W\*\*\*\*ws or m\*\*OS box; see **getOption**("pkgType"). This is because these two operating systems require additional build tools, especially if a package relies on C or C++ code; see Chapter 14 and Section C.3 of [65]:

- RTools<sup>8</sup> on W\*\*\*\*ws,
- Xcode Command Line Tools<sup>9</sup> on m\*\*OS.

These systems are less developer-orientated. Thus, as a courtesy to their users, CRAN

<sup>7 (\*)</sup> R is greatly configurable: we can have custom ~/.Renviron and ~/.Rprofile files that are processed on R's startup; see help("Startup").

<sup>8</sup> https://cran.r-project.org/bin/windows/Rtools

<sup>9</sup> https://developer.apple.com/xcode/resources

also distributes the platform-specific binary versions of the packages (.zip or .tgz files). install.packages will try to fetch them by default.

**Example 7.9** GitLab and GitHub are quite popular hosting platforms. It is very easy to retrieve a package's source directly from them. At the time of writing this, the relevant links were, respectively:

- https://gitlab.com/user/repo/-/archive/branch/repo-branch.zip,
- https://github.com/user/repo/archive/branch.zip.

For example, to download the contents of the master branch in the GitHub repository rpackagedemo owned by gagolews, we can call:

```
f <- tempfile() # download destination: a temporary file name
download.file("https://github.com/gagolews/rpackagedemo/archive/master.zip",
 destfile=f)</pre>
```

Next, the contents can be extracted with **unzip**:

```
t <- tempdir() # temporary directory for extracted files
(d <- unzip(f, exdir=t)) # returns extracted file paths</pre>
```

The path where the files were extracted can be passed to **install.packages**:

```
install.packages(dirname(d)[1], repos=NULL, type="source")
file.remove(c(f, d)) # clean up
```

**Exercise 7.10** Use the **git2r** package to clone the **git** repository located at https://github.com/gagolews/rpackagedemo.git and install the package published therein.

### Managing dependencies (\*)

By calling **update.packages**, all installed add-on packages may be upgraded to their most recent versions available on CRAN or other indicated repository.

As a general rule, the more experienced we become, the less excited we get about the *new*. Sure, bug fixes and well-thought-out additional features are usually welcome. Still, just we wait until someone updates a package's API for the n-th time,  $n \geq 2$ , breaking our so-far flawless program.

Hence, when designing software projects (see Chapter 9 for more details), we must ask ourselves the ultimate question: do we really need to import that package with lots of dependencies from which we will just use only about 3–5 functions? Wouldn't it be better to write our own version of some functionality (and learn something new, exercise our brain, etc.), or call a mature terminal-based tool?

Otherwise, as all the historical versions of the packages are archived on CRAN<sup>10</sup>,

<sup>10</sup> https://cran.r-project.org/src/contrib/Archive

simple software dependency management can be conducted by storing different releases of packages in different directories. This way, we can create an isolated environment for the add-ons. To fetch the locations where packages are sought (in this very order), we call:

```
.libPaths()
[1] "/home/gagolews/R/x86_64-pc-linux-gnu-library/4.3"
[2] "/usr/local/lib/R/site-library"
[3] "/usr/lib/R/site-library"
[4] "/usr/lib/R/library"
```

The same function can add new folders to the search path; see also the environment variable R\_LIBS\_USER that we can set using **Sys.setenv**. The **install.packages** function will honour them as target directories; see its lib parameter for more details. Note that only one version of a package can be loaded at a time, though.

Moreover, the packages may deposit auxiliary data on the user's machine. Therefore, it might be worthwhile to set the following directories (via the corresponding environment variables) relative to the current project:

```
tools::R_user_dir("pkg", "data") # R_USER_DATA_DIR
[1] "/home/gagolews/.local/share/R/pkg"
tools::R_user_dir("pkg", "config") # R_USER_CONFIG_DIR
[1] "/home/gagolews/.config/R/pkg"
tools::R_user_dir("pkg", "cache") # R_USER_CACHE_DIR
[1] "/home/gagolews/.cache/R/pkg"
```

### 7.3.2 Calling external programs

Many tasks can be accomplished by calling external programs. Such an approach is particularly natural on UNIX-like systems, which classically follow modular, minimalist design patterns. There are many tools at a developer's hand and each tool is specialised at solving a single, well-defined problem.

Apart from the many standard UNIX commands<sup>11</sup>, we may consider the following:

- pandoc<sup>12</sup> converts documents between markup formats, e.g., Markdown, HTML, reStructuredText, and LaTeX and can generate LibreOffice Writer documents, EPUB or PDF files, or slides;
- jupyter-nbconvert converts Jupyter<sup>13</sup> notebooks (see Section 1.2.5) to other formats such as LaTeX, HTML, Markdown, etc.;
- convert (from ImageMagick<sup>14</sup>) applies various operations on bitmap graphics (scaling, cropping, conversion between formats);

<sup>11</sup> https://en.wikipedia.org/wiki/List\_of\_Unix\_commands

<sup>12</sup> https://pandoc.org/

<sup>13</sup> https://jupyter.org/

<sup>14</sup> https://imagemagick.org/

- graphviz<sup>15</sup> and PlantUML<sup>16</sup> draws graphs and diagrams;
- python, perl, ... can be called to perform tasks that can be expressed more easily in languages other than R.

The good news is that we are not limited to calling R from the system shell in the interactive or batch mode; see Section 1.2. Our environment serves well as a glue language too.

The system2 function invokes a system command. Communication between such programs may be done using, e.g., intermediate text, JSON, CSV, XML, or any other files. The stdin, stdout, and stderr arguments control the redirection of the standard I/O streams.

```
system2("pandoc", "-s input.md -o output.html")
system2("bash", "-c 'for i in `seq 1 2 10`; do echo $i; done'", stdout=TRUE)
[1] "1" "3" "5" "7" "9"
system2("python3", "-", stdout=TRUE,
 input=c(
 "import numpy as np",
 "print(repr(np.arange(5)))"
))
[1] "array([0, 1, 2, 3, 4])"
```

On a side note, the current working directory can be read and changed through a call to getwd and setwd, respectively. By default, it is the directory where the current R session was started.

**Important** Relying on system2 assumes that the commands it refers to are available on the target platform. Hence, it might not be portable unless additional assumptions are made, e.g., that a user runs a UNIX-like system and that certain libraries are available. We strongly recommend GNU/Linux or FreeBSD for both software development and production use, as they are free, open, developer-friendly, user-loving, reliable, ethical, and sustainable. Users of other operating systems are missing out on so many good features.

### Interfacing C, C++, Fortran, Python, Java, etc. (\*\*)

Most standalone data processing algorithms are implemented in compiled, slightly lower-level programming languages. This usually makes them faster and more reusable in other environments. For instance, an industry-standard library might be written in very portable C, C++, or Fortran and define bindings for easier access from within R, Python, Julia, etc. It is the case with FFTW, LIBSVM, mlpack, OpenBLAS,

<sup>15</sup> https://graphviz.org/

<sup>16</sup> https://plantuml.com/

ICU, and GNU GSL, amongst many others. Chapter 14 explains basic ways to refer to such compiled code.

Also, the **rJava** package can dynamically create JVM objects and access their fields and methods. Similarly, **reticulate** can be used to access Python objects, including **numpy** arrays and **pandas** data frames (but see also the **rpy2** package for Python).

**Important** We should not feel obliged to use R in all parts of a data processing pipeline. Some activities can be expressed more naturally in other languages or environments (e.g., parse raw data and create a SQL database in Python but visualise it in R).

#### 7.4 Exercises

**Exercise 7.11** Answer the following questions.

- What is the result of " $\{x < "x"; x < function(x) x; x(x)\}$ "?
- How to compose a function that returns two objects?
- What is a higher-order function?
- What are the use cases of do.call?
- Why a call to **Map** is redundant in the expression Map(paste, x, y, z)?
- What is the difference between Map(mean, x, na.rm=TRUE) and Map(mean, x, More-Args=list(na.rm=TRUE))?
- What do we mean when we write **stringx**::**sprintf**?
- How to get access to the vignettes (tutorials, FAQs, etc.) of the **data.table** and **dplyr** packages? Why perhaps 95% of R users would just googleit, and what is suboptimal about this strategy?
- What is the difference between a source and a binary package?
- How to update the **base** package?
- How to ensure that we will always run an R session with only specific versions of a set of packages?

**Exercise 7.12** Write a function that computes the Gini index of a vector of positive integers x, which, assuming  $x_1 \le x_2 \le ... \le x_n$ , is equal to:

$$G(x_1, \dots, x_n) = \frac{\sum_{i=1}^n (n-2i+1)x_i}{(n-1)\sum_{i=1}^n x_i}.$$

**Exercise 7.13** Implement a function **between**(x, a, b) that verifies whether each element in x is in the [a, b] interval. Return a logical vector of the same length as x. Ensure the function is correctly vectorised with respect to all the arguments and handles missing data correctly.

**Exercise 7.14** Write your version of the **strrep** function called **dup**.

```
dup <- ...to.do...
dup(c("a", "b", "c"), c(1, 3, 5))
[1] "a" "bbb" "ccccc"
dup("a", 1:3)
[1] "a" "aa" "aaa"
dup(c("a", "b", "c"), 4)
[1] "aaaa" "bbbb" "cccc"
```

**Exercise 7.15** Given a list x, generate its sublist with all the elements equal to NULL removed.

**Exercise 7.16** Implement your version of the **sequence** function.

**Exercise 7.17** Using Map, how can we generate window indexes like below?

```
[[1]]
[1] 1 2 3
##
[[2]]
[1] 2 3 4
##
[[3]]
[1] 3 4 5
##
[[4]]
[1] 4 5 6
```

Write a function windows(k, n) that yields index windows of length k with elements between 1 and n (the above example is for k = 3 and k = 6).

**Exercise 7.18** Write a function to extract all q-grams,  $q \geq 1$ , from a given character vector. Return a list of character vectors. For example, bigrams (2-grams) in "abcd" are: "ab", "bc", "cd"`.

**Exercise 7.19** Implement a function **movstat**(f, x, k) that computes, using **Map**, a given aggregate  $\mathbf{f}$  of each k consecutive elements in x. For instance:

```
movstat <- ...to.do...
x <- c(1, 3, 5, 10, 25, -25) # example data
movstat(mean, x, 3) # 3-moving mean
[1] 3.0000 6.0000 13.3333 3.3333
movstat(median, x, 3) # 3-moving median
[1] 3.0000 6.0000 13.3333 3.3333
```

**Exercise 7.20** Recode a character vector with a small number of distinct values to a vector where

each unique code is assigned a positive integer from 1 to k. Here are example calls and the corresponding expected results:

```
recode <- ...to.do...

recode(c("a", "a", "a", "b", "b"))

[1] 1 1 1 2 2

recode(c("x", "z", "y", "x", "y", "x"))

[1] 1 3 2 1 2 1
```

**Exercise 7.21** Implement a function that returns the number of occurrences of each unique element in a given atomic vector. The return value should be a numeric vector equipped with the names attribute. Hint: use **match** and **tabulate**.

```
count <- ...to.do...
count(c(5, 5, 5, 5, 42, 42, 954))
5 42 954
4 2 1
count(c("x", "z", "y", "x", "y", "x", "w", "x", "x", "y", NA_character_))
w x y z <NA>
1 5 3 1 1
```

**Exercise 7.22** Extend the built-in **duplicated** function. For each vector element, indicate which occurrence of a repeated value is it (starting from the beginning of the vector).

```
duplicatedn <- ...to.do...
duplicatedn(c("a", "a", "b", "b"))
[1] 1 2 3 1 2
duplicatedn(c("x", "z", "y", "x", "y", "x", "w", "x", "x", "y", "z"))
[1] 1 1 1 2 2 3 1 4 5 3 2</pre>
```

**Exercise 7.23** Based on a call to **Map**, implement your version of **split** that takes two atomic vectors as arguments. Then, extend it to handle the second argument being a list of the form **list**(y1, y2, ...) representing the product of many levels. If the ys are of different lengths, apply the recycling rule.

**Exercise 7.24** Implement  $my\_unsplit$  being your version of unsplit. For any x and g of the same lengths, ensure that  $my\_unsplit(split(x, g), g)$  is equal to x.

**Exercise 7.25** Write a function that takes as arguments: (a) an integer n, (b) a numeric vector x of length k and no duplicated elements, (c) a vector of probabilities p of length k. Verify that  $p_i \geq 0$  for all i and  $\sum_{i=1}^k p_i \approx 1$ . Based on a random number generator from the uniform distribution on the unit interval, generate n independent realisations of a random variable X such that  $\Pr(X = x_i) = p_i$  for  $i = 1, \ldots, k$ . To obtain a single value:

- 1. generate  $u \in [0,1]$ ,
- 2. find  $m \in \{1, \dots, k\}$  such that  $u \in \left(\sum_{j=1}^{m-1} p_j, \sum_{j=1}^m p_j\right]$ ,
- 3. the result is then  $x_m$ .

**Exercise 7.26** Write a function that takes as arguments: (a) an increasingly sorted vector x of length n, (b) any vector y of length n, (c) a vector z of length k and elements in  $[x_1, x_n)$ . Let f be the piecewise linear spline that interpolates the points  $(x_1, y_1), \dots, (x_n, y_n)$ . Return a vector w of length k such that  $w_i = f(z_i)$ .

Exercise 7.27 (\*) Write functions dpareto, ppareto, apareto, and rpareto that implement the basic functions related to the Pareto distribution; compare Section 2.3.4.

# Flow of execution

The **ifelse** and **Map** functions are potent. However, they allow us to process only the *consecutive* elements in a vector.

Thus, let us (finally!) discuss different ways to alter a program's control flow manually, based on some criterion, and to evaluate the same expression many times, but perhaps on different data. Before proceeding any further, let us, however, contemplate the fact that we have managed without them for such a long time, despite the fact that the data processing exercises we learnt to solve were far from trivial.

### 8.1 Conditional evaluation

Life is full of surprises, so it would be nice if we were able to adapt to any future challenges.

The following evaluates a given expression if and only if a logical condition is true.

```
if (condition) expression
```

When performing some other\_expression is preferred rather than doing nothing in the case of the condition's being false, we can write:

```
if (condition) expression else other_expression
```

For instance:

```
(x <- runif(1)) # to spice things up
[1] 0.28758
if (x > 0.5) cat("head\n") else cat("tail\n")
tail
```

Many expressions can, of course, be grouped with curly braces, `{`.

(continued from previous page)

```
} else { # do not put newline before else!
 cat("tail\n")
 x <- 0
}
tail
print(x)
[1] 0
```

**Important** At the top level, we should not put a new line before **else**. Otherwise, we will get an error like Error: unexpected 'else' in "else". This is because the interpreter enthusiastically executes the statements read line by line as soon as it regards them as standalone expressions. In this case, we first get an **if** without **else**, and then, separately, a dangling else without the preceding if.

This is not an issue when a conditional statement is part of an expression group as the latter is read in its entirety.

```
function (x)
{ # opening bracket - start
 if (x > 0.5)
 cat("head\n")
 # not dandling because {...} is read as a whole
 else
 cat("tail\n")
} # closing bracket - expression ends
```

As an exercise, try removing the curly braces and see what happens.

#### Return value 8.1.1

`if` is a function (compare Section 9.3). Hence, it has a return value: the result of evaluating the conditional expression.

```
(x <- runif(1))
[1] 0.28758
y <- if (x > 0.5) "head" # no else
print(y)
NULL
y <- if (x > 0.5) "head" else "tail"
print(v)
[1] "tail"
```

This is particularly useful when a call to `if` is the last expression in a curly bracedelimited code block that constitutes a function's body.

```
mint <- function(x)
{
 cond <- (x > 0.5) # could be something more sophisticated
 if (cond) # the last expression in the code block
 "head" # this can be the return value...
 else
 "tail" # or this one, depending on the condition
}

mint(x)
[1] "tail"
unlist(Map(mint, runif(5)))
[1] "tail" "head" "tail" "head" "head"
```

**Example 8.1** Add-on packages can be loaded using **requireNamespace**. Contrary to **library**, the former does not fail when a package is not available. Also, it does not attach it to the search path; see Section 16.2.6. Instead, it returns a logical value indicating if the package is available for use. This can be helpful in situations where the availability of some features depends on the user environment's configuration:

```
process_data <- function(x)
{
 if (requireNamespace("some_extension_package", quietly=TRUE))
 some_extension_package::very_fast_method(x)
 else
 normal_method(x)
}</pre>
```

#### 8.1.2 Nested ifs

If more than two test cases are possible, i.e., when we need to go beyond either condition or !condition, then we can use the following construction:

```
if (a) {
 expression_a
} else if (b) {
 expression_b
} else if (c) {
 expression_c
} else {
 expression_else
}
```

This evaluates all conditions a, b, ... (in this order) until the first positive case is found and then executes the corresponding expression.

It is worth stressing that the above is nothing else than a series of nested **if** statements but written in a more readable<sup>1</sup> manner:

```
if (a) {
 expression_a
} else {
 if (b) {
 expression_b
 } else {
 if (c) {
 expression_c
 } else {
 expression_else
 }
 }
}
```

**Exercise 8.2** Write a function named **sign** that determines if a given numeric value is "positive", "negative", or "zero".

#### 8.1.3 Condition: Either TRUE or FALSE

**if** expects a condition that is a single, well-defined logical value, either TRUE or FALSE. Thence, problems may arise when this is not the case.

If the condition is of length not equal to one, we get an error:

```
if (c(TRUE, FALSE)) cat("spam\n")
Error in if (c(TRUE, FALSE)) cat("spam\n"): the condition has length > 1
if (logical(0)) cat("bacon\n")
Error in if (logical(0)) cat("bacon\n"): argument is of length zero
```

We cannot pass a missing value either:

```
if (NA) cat("ham\n")
Error in if (NA) cat("ham\n"): missing value where TRUE/FALSE needed
```

**Important** If we think that we are immune to writing code violating the above constraints, just we wait until the condition becomes a function of data for which there is no sanity-checking in place.

<sup>&</sup>lt;sup>1</sup> (\*) Somewhat related is the **switch** function which relies on the lazy evaluation of its arguments (Chapter 17). However, it can always be replaced by a series of **if**s.

(continued from previous page)

```
mint(0.25)
[1] "tail"
mint(runif(5))
Error in if (x > 0.5) "head" else "tail": the condition has length > 1
mint(log(rnorm(1))) # not obvious, only triggered sometimes
Warning in log(rnorm(1)): NaNs produced
Error in if (x > 0.5) "head" else "tail": missing value where TRUE/FALSE
needed
```

In Chapter 9, we will be particularly interested in ways to ensure input data integrity so that such cases will either fail gracefully or succeed bombastically. In the above example, we should probably ensure that x is a single finite numeric value. Alternatively, we might need to apply **ifelse**, **all**, or **any**.

Interestingly, conditions other that logical are coerced:

```
x <- 1:5
if (length(x)) # i.e., length(x) != 0, but way less readable
 cat("length is not zero\n")
length is not zero</pre>
```

Recall that coercion of numeric to logical yields FALSE if and only if the original value is zero.

#### 8.1.4 Short-circuit evaluation

Especially for formulating logical conditions in **if** and **while** (see below), we have the *scalar* `||` (alternative) and `&&` (conjunction) operators.

```
FALSE || TRUE
[1] TRUE
NA || TRUE
[1] TRUE
```

Contrary to their vectorised counterparts (`|` and `&`), the scalar operators are lazy (Chapter 17) in the sense that they evaluate the first operand and then determine if the computing of the second one is necessary (because, e.g., FALSE && whatever is always FALSE anyway).

Therefore,

```
if (a && b)
expression
```

is equivalent to:

```
if (a) {
 if (b) { # compute b only if a is TRUE
 expression
 }
}
```

and:

```
if (a || b)
 expression
```

corresponds to:

```
if (a) {
 expression
} else if (b) { # compute b only if a is FALSE
 expression
}
```

For instance, "is.vector(x) && length(x) > 0 && x[[1]] > 0" is a risk-free test. It takes into account that x[[1]] has the desired meaning only for objects that are nonempty vectors.

Some other examples:

```
{cat("spam"); FALSE} || {cat("ham"); TRUE} || {cat("cherries"); FALSE}
spamham
[1] TRUE
{cat("spam"); TRUE} && {cat("ham"); FALSE} && {cat("cherries"); TRUE}
spamham
[1] FALSE
```

Recall that the expressions within the curly braces are evaluated one after another and that the result is determined by the last value in the series.

**Exercise 8.3** Study the source code of **isTRUE** and **isFALSE** and determine if these functions could be useful in formulating the conditions within the **if** expressions.

### 8.2 Exception handling

Exceptions are exceptional, but they may happen and break stuff. For instance, we are in deep skit when the internet connection drops while we try to download a file, an optimisation algorithm fails to converge, or:

```
read.csv("/path/to/a/file/that/does/not/exist")
Warning in file(file, "rt"): cannot open file '/path/to/a/file/that/does/
not/exist': No such file or directory
Error in file(file, "rt"): cannot open the connection
```

Three types of *conditions* are frequently observed:

- errors stop the flow of execution,
- warnings are not critical, but can be turned into errors (see warn in option),
- messages transmit diagnostic information.

They can be manually triggered using the **stop**, warning, and message functions.

Errors (but warnings too) can be handled by means of the **tryCatch** function, amongst others.

```
tryCatch({
 # block of expressions to execute, until an error occurs
 cat("a...\n")
 stop("b!")
 # error - breaks the linear control flow
 cat("c?\n")
 },
 error = function(e) { # executed immediately on an error
 cat(sprintf("[error] %s\n", e[["message"]]))
 }.
 finally = { # always executed at the end, regardless of error occurrence
 cat("d.\n")
 }
)
a...
[errorl b!
d.
```

The two other conditions can be ignored by calling **suppressWarnings** and **suppress-Messages**.

```
log(-1)
Warning in log(-1): NaNs produced
[1] NaN
suppressWarnings(log(-1)) # yeah, yeah, we know what we're doing
[1] NaN
```

**Exercise 8.4** At the time of writing this book, when the **data.table** package is attached, it emits a message. Call **suppressMessages** to silence it. Note that consecutive calls to **library** do not reload an already loaded package. Therefore, the message will only be seen once per R session.

Related functions include **stopifnot** discussed in Section 9.1 and **on.exit** mentioned in Section 17.4; see Section 9.2.4 for some code debugging tips.

#### Repeated evaluation 8.3

And now for something completely different... time for the elephant in the room!

We have been able to manage without loops so far (and will be quite all right in the second part of the book too). This is because many data processing tasks can be written in terms of vectorised operations such as `+`, sqrt, sum, `[`, Map, and Reduce. Oftentimes, compared to their loop-based counterparts, they are more readable and efficient. We will explore this in the exercises below.

However, at times, using an explicit while or for loop might be the only natural way to solve a problem, for instance, when processing chunks of data streams. Also, an explicitly "looped" algorithm may occasionally have better<sup>2</sup> time or memory complexity.

#### 8.3.1 while

if considers a logical condition provided and determines whether to execute a given statement. On the other hand:

```
while (condition) # single TRUE or FALSE, as in `if`
 expression
```

evaluates a given expression as long as the logical condition is true. Therefore, it is advisable to make the condition dependent on some variable that the expression can modify.

```
i <- 1
while (i <= 3) {
 cat(sprintf("%d, ", i))
 i < -i + 1
}
1, 2, 3,
```

Nested loops are possible too:

```
i <- 1
while (i <= 2) {
 j <- 1
 while (j <= 3) {
 cat(sprintf("%d %d, ", i, j))
 j < -j + 1
 }
 cat("\n")
 i < -i + 1
```

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<sup>&</sup>lt;sup>2</sup> In such a case, rewriting it in C or C++ might be beneficial; see Chapter 14.

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```
}
1 1, 1 2, 1 3,
2 1, 2 2, 2 3,
```

**Example 8.5** Implement a simple linear congruential pseudorandom number generator that, given some seed  $X_0 \in [0, m)$ , outputs a sequence  $(X_1, X_2, ...)$  defined by:

$$X_i = (aX_{i-1} + c) \mod m,$$

with, e.g., a = 75, c = 74, and  $m = 2^{16} + 1$  (here, mod is the division remainder, `%%`). This generator has poor statistical properties and its use in practice is discouraged. In particular, after a rather small number of iterations k, we will find a cycle such that  $X_k = X_1$ ,  $X_{k+1} = X_2$ , ....

#### 8.3.2 for

The for-each loop:

```
for (name in vector)
 expression
```

takes each element, from the beginning to the end, in a given vector, assigns it some name, and evaluates the expression. For example:

```
fridge <- c("spam", "spam", "bacon", "eggs")
for (food in fridge)
 cat(sprintf("%s, ", food))
spam, spam, bacon, eggs,</pre>
```

Another example:

```
for (i in 1:length(fridge)) # better: seq_along(fridge), see below
 cat(sprintf("%s, ", fridge[i]))
spam, spam, bacon, eggs,
```

One more:

```
for (i in 1:2) {
 for (j in 1:3)
 cat(sprintf("%d %d, ", i, j))
 cat("\n")
}
1 1, 1 2, 1 3,
2 1, 2 2, 2 3,
```

The iterator still exists after the loop's watch has ended:

```
print(i)
[1] 2
print(j)
[1] 3
```

### Important Writing:

```
for (i in 1:length(x))
 print(x[i])
```

is reckless. If x is an empty vector, then we will observe undesired behaviour because we ask to iterate over 1:0:

```
x <- logical(0)</pre>
for (i in 1:length(x))
 print(x[i])
[1] NA
logical(0)
```

Recall from Chapter 5 that x[1] tries to access an out-of-bounds element here, and x[0] returns nothing.

We generally suggest replacing 1: length(x) with  $seq_along(x)$  or  $seq_len(length(x))$ . wherever possible.

**Note** The above model **for** loop is roughly equivalent to:

```
name <- NULL
tmp_vector <- vector</pre>
tmp iter <- 1
while (tmp_iter <= length(tmp_vector)) {</pre>
 name <- tmp_vector[[tmp_iter]]</pre>
 expression
 tmp iter <- tmp iter + 1
}
```

Note that the tmp\_vector is determined before the loop itself. Hence, any changes to the vector will not influence the execution flow. Furthermore, due to the use of `[[`, the loop can also be applied on lists.

**Example 8.6** Let x be a list and f be a function. The following code generates the same result as Map(f, x):

```
n <- length(x)
ret <- vector("list", n) # a new list of length `n`
for (i in seq_len(n))
 ret[[i]] <- f(x[[i]])</pre>
```

**Example 8.7** Let x and y be two lists and f be a function. Here is the most basic version of Map(f, x, y).

```
nx <- length(x)
ny <- length(y)
n <- max(nx, ny)
ret <- vector("list", n)
for (i in seq_len(n))
 ret[[i]] <- f(x[[((i-1)%%nx)+1]], y[[((i-1)%%ny)+1]])</pre>
```

Note that x and y might be of different lengths. Feel free to upgrade the above code by adding a warning like the longer argument is not a multiple of the length of the shorter one. Also, rewrite it without using the modulo operator, `%.`

#### 8.3.3 break and next

**break** can be used to escape the current loop. **next** skips the remaining expressions and advances to the next iteration (where the testing of the logical condition occurs).

Here is a rather random example:

```
x <- c(10, 0.03, 0.04, 1, 0.001, 0.05)
s <- 0
for (e in x) {
 if (e > 0.1) # skip the current element if it is greater than 0.1
 next

 print(e)
 if (e < 0.01) # stop at the first element less than 0.01
 break

 s <- s + e
}
[1] 0.03
[1] 0.04
[1] 0.001
print(s)
[1] 0.07</pre>
```

We have used a frequently occurring design pattern:

which is equivalent to:

```
for (e in x) {
 if (!condition) {
 many_statements...
 }
}
```

but which avoids introducing a nested block of expressions.

**Note** (\*) There is a third loop type,

```
repeat expression
```

which is a shorthand for

```
while (TRUE)
expression
```

i.e., it is a possibly infinite loop. Such constructs are invaluable when expressing situations like *repeat*-something-*until*-success, e.g., when we want to execute a command at least once.

```
i <- 1
repeat { # while (TRUE)
 # simulate dice casting until we throw "1"
 if (runif(1) < 1/6) break # repeat until this
 i <- i+1 # how many times until success
}
print(i)
[1] 6</pre>
```

### **Exercise 8.8** What is wrong with the following code?

```
j < -1
while (j <= 10) {
 if (j \%\% 2 == 0) next

(continues on next page)
```

(continued from previous page)

```
print(j)
 j <- j + 1
}</pre>
```

#### **Exercise 8.9** What about this one?

#### 8.3.4 return

**return**, when called from within a function, immediately yields a specified value and goes back to the caller.

For example, here is a simple recursive function that flattens a given list:

```
my_unlist <- function(x)
{
 if (is.atomic(x))
 return(x)

so if we are here, x is definitely not atomic
 out <- NULL
 for (e in x)
 out <- c(out, my_unlist(e))

 out # or return(out); not necessary as it's the last expression
}

my_unlist(list(list(list(1, 2), 3), list(4, list(5, list(6, 7:10)))))
[1] 1 2 3 4 5 6 7 8 9 10</pre>
```

**return** is a function: the round brackets are obligatory.

## 8.3.5 Time and space complexity of algorithms (\*)

Analysis of algorithms can give us a rough estimate of their run time or memory consumption as a function of the input problem size, especially for *big* data (e.g., [14, 43]).

In scientific computing and data science, we often deal with vectors (sequences) or matrices/data frames (tabular data). Therefore, we might be interested in determining how many *primitive operations* need to be performed as a function of their length n or the number of rows n and columns m, respectively.

The O (Big-Oh) notation can express the upper bounds for time/resource consumption in asymptotic cases. For instance, we say that the time complexity is  $O(n^2)$ , if for large

n, the number of operations to perform or memory cells to use will be proportional to at most the square of the vector size (more precisely, there exists m and C > 0 such that for all n > m, the number of operations is  $\leq Cn^2$ ).

Therefore, if we have two algorithms that solve the same task, one that has  $O(n^2)$  time complexity, and other of  $O(n^3)$ , it is better to choose the former. For large problem sizes, we expect it to be faster.

Moreover, whether time grows proportionally to  $\log n$ ,  $\sqrt{n}$ , n,  $n \log n$ ,  $n^2$ ,  $n^3$ , or  $2^n$ , can be informative in predicting how big the data can be if we have a fixed deadline or not enough space left on the disk.

**Exercise 8.10** The **hclust** function determines a hierarchical clustering of a dataset. It is fed with an object that stores the distance between all the pairs of input points. There are n(n-1)/2 (i.e.,  $O(n^2)$ ) unique point pairs for any given n. One numeric scalar (double type) takes 8 bytes of storage. If you have 16 GiB of RAM, what is the largest dataset that you can process on your machine using this function?

Oftentimes, we can learn about the time or memory complexity of the functions we use from their documentation; see, e.g., help("findInterval").

**Example 8.11** A course in data structures in algorithms, which this one is not, will give us plenty of opportunities to implement many algorithms ourselves. This way, we can gain a lot of insights and intuitions.

For instance, this is a O(n)-time algorithm:

```
for (i in seq_len(n))
 expression
```

and this is one runs in  $O(n^2)$  time:

```
for (i in seq_len(n))
 for (j in seq_len(n))
 expression
```

as long as, of course, the expression is rather primitive (e.g., operations on scalar variables).

R is a very expressive language. Hence, quite complex and lengthy operations can look pretty innocent. After all, it is a glue language for rapid prototyping.

For example:

```
for (i in seq_len(n))
 for (j in seq_len(n))
 z <- z + x[[i]] + y[[j]]</pre>
```

can be seen as  $O(n^3)$  if each element in the lists x and y as well as z itself are atomic vectors of length n.

Similarly,

```
Map(mean, x)
```

is  $O(n^2)$  if x is a list of n atomic vectors, each of length n.

**Note** A quite common statistical scenario involves generating a data buffer of a fixed size:

```
ret <- c() # start with an empty vector
for (i in seq_len(n))
 ret[[i]] <- generate_data(i) # here: ret[[length(ret)+1]] <- ...</pre>
```

This notation, however, involves growing the ret array in each iteration. Luckily, since R version 3.4.0, each such size extension has amortised O(1) time as some more memory is internally reserved for its prospective growth (dynamic arrays; see, e.g., Chapter 17 of [14]).

However, it is better to preallocate the output vector of the desired final size. We can construct vectors of specific lengths and types in an efficient way (more efficient than with **rep**) by calling:

```
numeric(3)
[1] 0 0 0
numeric(0)
numeric(0)
logical(5)
[1] FALSE FALSE FALSE FALSE
character(2)
[1] "" ""
vector("numeric", 8)
[1] 0 0 0 0 0 0 0 0
vector("list", 2)
[[1]]
NULL
##
[[2]]
NULL
```

**Note** Not all data fit into memory, but it does not mean that we should start installing Apache Hadoop and Spark immediately. Some datasets can be processed chunk by chunk. R enables data stream handling (some can be of infinite length) through file connections. For example:

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```
i <- 0
while (TRUE) {
 few_lines <- readLines(f, n=4) # reads only four lines at a time
 if (length(few_lines) == 0) break
 i <- i + length(few_lines)</pre>
}
close(f)
print(i) # the number of lines
[1] 90
```

Many functions support reading from/writing to already established connections of different types, e.g., file, gzfile, textConnection, batch by batch.

A frequent scenario involves reading a very large CSV, JSON, or XML file only by thousands of lines/records at a time, parsing and cleansing them, and exporting them to SQL databases (which we will exercise in Chapter 12).

#### **Exercises** 8.4

From now on, we must stay alert. Many, if not all, of the following tasks, can still be implemented without the explicit use of the R loops but based only on the operations covered in the previous chapters. If this is the case, try composing both the looped and loop-free versions. Use **proc.time** to compare their run times<sup>3</sup>.

**Exercise 8.12** *Answer the following questions.* 

- Let x be a numeric vector. When does "if(x > 0) ..." yield a warning? When does it give an error? How to guard ourselves against them?
- What is a dangling **else**?
- What happens if you put **if** as the last expression in a curly braces block within a function's body?
- Why do we say that `&&` and `\(\begin{aligned}
  \) are lazy? What are their use cases?
- What is the difference between `&&` and `&`?
- Can **while** always be replaced with **for**? What about the other way around?
- What is wrong with "return (1+2)\*3"?

**Exercise 8.13** Verify which of the following can be safely used as logical conditions in **if** state-

<sup>&</sup>lt;sup>3</sup> It might be the case that a **for**-based solution is faster (e.g., for larger objects) because of the use of a more efficient algorithm. Such cases will benefit from a rewrite in C or C++ (Chapter 14).

ments. If that is not the case for all x, y, ..., determine the additional conditions that must be imposed to make them valid.

```
 x == 0,
 x[y] > 0,
 any(x>0),
 match(x, y),
 any(x %in% y).
```

**Exercise 8.14** What can go wrong in the following code chunk, depending on the type and form of x? Consider as many scenarios as possible.

```
count <- 0
for (i in 1:length(x))
 if (x[i] > 0)
 count <- count + 1</pre>
```

**Exercise 8.15** Implement  $shift_left(x, n)$  and  $shift_right(x, n)$ . The former function gets rid of the first n observations in x and adds n missing values at the end of the resulting vector, e.g.,  $shift_left(c(1, 2, 3, 4, 5), 2)$  is c(3, 4, 5, NA, NA). On the other hand,  $shift_right(c(1, 2, 3, 4, 5), 2)$  is c(NA, NA, 1, 2, 3).

**Exercise 8.16** Implement your version of diff.

**Exercise 8.17** Write a function that determines the longest ascending trend in a given numeric vector, i.e., the length of the longest subsequence of consecutive increasing elements. For example, the input c(1, 2, 3, 2, 1, 2, 3, 4, 3) should yield 4.

**Exercise 8.18** Implement the functions that round down and round up each element in a numeric vector to a number of decimal digits.

This concludes the first part of this magnificent book.

Part II

Deeper

# Designing functions

In Chapter 7, we learnt how to compose simple functions. This skill is vital to enforcing the good development practice of avoiding code repetition: running the same command sequence on different data.

This chapter is devoted to designing reusable methods so that they are easier to use, test, and maintain. We also provide more technical details about functions. They were not of the highest importance during our first exposure to this topic but are crucial to our better understanding of how R works.

## 9.1 Managing data flow

A function, most of the time, can and should be treated as a black box. Its callers do not have to care what it hides inside. After all, they are supposed to *use* it. Given some *inputs*, they expect well-defined *outputs* that are explained in detail in the function's manual.

## 9.1.1 Checking input data integrity and argument handling

A function takes R objects of any kind as arguments, but it does not mean feeding it with everything is healthy for its guts.

When designing functions, it is best to handle the inputs in a manner similar to base R's behaviour. This will make our contributions easier to work with.

Lamentably, base functions frequently do not process arguments of a similar *kind* fully consistently. Such variability might be due to many reasons and, in essence, is not necessarily bad. Usually, there might be many possible behaviours and choosing one over another would make a few users unhappy anyway. Some choices might not be optimal, but they are for historical compatibility (e.g., with S). Of course, it might also happen that something is poorly designed or there is a bug (but the likelihood is low).

This is why it is better to keep the vocabulary quite restricted Even if there are exceptions to the general rules, with fewer functions, they are easier to remember. We advocate for such minimalism in this book.

Consider the following case study, illustrating that even the extremely simple scenario dealing with a single positive integer is not necessarily straightforward.

**Exercise 9.1** In mathematical notation, we usually denote the number of objects in a collection with the famous "n". It is implicitly assumed that such n is a single natural number (albeit whether this includes 0 or not should be specified at some point). The functions **runif**, **sample**, **seq**, **rep**, **strrep**, and **class**: **:knn** take it as arguments. Nonetheless, nothing stops us from trying to challenge them by passing:

```
2.5, -1, 0, 1-1e-16 (non-positive numbers, non-integers);
NA_real_, Inf (not finite);
1:5 (not of length 1; after all, there are no scalars in R);
numeric(0) (an empty vector);
TRUE, NA, c(TRUE, FALSE, NA), "1", c("1", "2", "3") (non-numeric, but coercible to);
```

- list(1), list(1, 2, 3), list(1:3, 4) (non-atomic);
- "Spanish Inquisition" (unexpected nonsense);
- as.matrix(1), factor(7), factor(c(3, 4, 2, 3)), etc. (compound types; Chapter 10).

Read the aforementioned functions' reference manuals and call them on different inputs. Notice how differently they handle such atypical arguments.

Sometimes we will rely on other functions to check data integrity for us.

**Example 9.2** Let us consider the following function that generates n pseudorandom numbers from the unit interval rounded to d decimal digits. We strongly believe or at least hope (the good faith and high competence assumption) that its author knew what he was doing when he wrote:

```
round_rand <- function(n, d)
{
 x <- runif(n) # runif will check if `n` makes sense
 round(x, d) # round will determine the appropriateness of `d`
}</pre>
```

What constitutes correct n and d and how the function behaves when not provided with positive integers is determined by the two underlying functions, **runif** and **round**:

```
round_rand(4, 1) # the expected use case
[1] 0.3 0.8 0.4 0.9
round_rand(4.8, 1.9) # 4, 2
[1] 0.94 0.05 0.53 0.89
round_rand(4, NA)
[1] NA NA NA NA
round_rand(0, 1)
numeric(0)
```

Some design choices can be defended if they are well thought out and adequately documented. Certain programmers will opt for high uniformity/compatibility across numerous tools, as there are cases where diversity does more good than harm.

Our functions might become part of a more complicated data flow pipeline. Let us think what happens when another procedure generates a value that we did not expect (due to a bug or because we did not study its manual). The problem arises when this *unthinkable* value is passed to our function. In our case, this would correspond to the said *n*'s or *d*'s being determined programmatically.

**Example 9.3** Continuing the previous example, the following might be somewhat challenging with regard to our being flexible and open-minded:

```
round_rand(c(100, 42, 63, 30), 1) # n=length(c(...))
[1] 0.7 0.6 0.1 0.9
round_rand("4", 1) # n=as.numeric("4")
[1] 0.2 0.0 0.3 1.0
```

Sure, it is quite convenient. Nevertheless, it might lead to problems that are hard to diagnose.

Also, note the not so informative error messages in cases like:

```
round_rand(NA, 1)
Error in runif(n): invalid arguments
round_rand(4, "1")
Error in round(x, d): non-numeric argument to mathematical function
```

*Defensive design* strategies are always welcome, especially if they lead to constructive error messages.

**Important stopifnot** gives a convenient means to assert the enjoyment of our expectations about a function's arguments (or intermediate values). A call to **stopifnot**(cond1, cond2, ...) is more or less equivalent to:

```
if (!(is.logical(cond1) && !any(is.na(cond1)) && all(cond1)))
 stop("`cond1` are not all TRUE")
if (!(is.logical(cond2) && !any(is.na(cond2)) && all(cond2)))
 stop("`cond2` are not all TRUE")
...
```

Thus, if all the elements in the given logical vectors are TRUE, nothing happens. We can move on with certainty.

### **Example 9.4** We can rewrite the above function as follows:

```
round_rand2 <- function(n, d)
{
 stopifnot(
 is.numeric(n), length(n) == 1,
 is.finite(n), n > 0, n == floor(n),
 is.numeric(d), length(d) == 1,
 (continues on next page)
```

II DEEPER

```
is.finite(d), d > 0, d == floor(d)
)
x <- runif(n)
round(x, d)
}

round_rand2(5, 1)
[1] 0.7 0.7 0.5 0.6 0.3
round_rand2(5.4, 1)
Error in round_rand2(5.4, 1): n == floor(n) is not TRUE
round_rand2(5, "1")
Error in round_rand2(5, "1"): is.numeric(d) is not TRUE</pre>
```

It is the strictest test for "a single positive integer" possible. In the case of any violation of the underlying condition, we get a very informative error message.

**Example 9.5** At other times, we might be interested in a more liberal yet still foolproof argument checking like:

```
if (!is.numeric(n))
 n <- as.numeric(n)
if (length(n) > 1) {
 warning("only the first element will be used")
 n <- n[1]
}
n <- floor(n)
stopifnot(is.finite(n), n > 0)
```

This way, "4" and c(4.9, 100) will all be accepted as  $4^1$ .

We see that there is always a tension between being generous/flexible and precise/restrictive. Also, because of their particular use cases, for certain functions, it will be better to behave differently from the others. Excessive uniformity is as bad as chaos. We are always expected to rely on common sense. Let us not be boring bureaucrats.

Still, it is our duty to be explicit about all the assumptions we make or exceptions we tolerate (by writing comprehensive documentation; see Section 9.2.2).

**Note** (\*) Example exercises related to improving the consistency of base R's argument handling in different domains include the **vctrs** and **stringx** packages. Can these contributions be justified?

<sup>&</sup>lt;sup>1</sup> We rely on the S3 generics is.numeric and as.numeric here; see Section 10.2.3.

**Exercise 9.6** Reflect on how you would respond to miscellaneous boundary cases in the following scenarios (and how base R and other packages or languages you know deal with them):

- a vectorised mathematical function (empty vector? non-numeric input? what if it is equipped
  with the names attribute? what if it has other ones?);
- an aggregation function (what about missing values? empty vector?);
- a function vectorised with regard to two arguments (elementwise vectorisation? recycling rule? only scalar vs vector, or vector vs vector of the same length allowed? what if one argument is a row vector and the other is a column vector?);
- a function vectorised with respect to all arguments (really all? maybe some exceptions are necessary?);
- a function vectorised with respect to the first argument but not the second (why such a restriction? when?).

Find a few functions that match each case.

### 9.1.2 Putting outputs into context

Our functions do not exist in a vacuum. We should put them into a much broader context: how can they be combined with other tools?

As a general rule, we ought to generate outputs of a *predictable* kind. This way, we can easily deduce what will happen in the code chunks that utilise them.

**Example 9.7** Some base R functions do not adhere to this rule for the sake of (questionable) users' convenience. We will meet a few of them in Chapter 11 and Chapter 12. In particular, **sapply** and the underlying **simplify2array**, can return a list, an atomic vector, or a matrix.

Further, the index operator with drop=TRUE, which is the default, may output an atomic vector. However, it may as well yield a matrix or a data frame.

```
(A <- matrix(1:6, nrow=3)) # an example matrix
[,1] [,2]
```

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```
[1,]
 1
 4
[2,] 2
 5
[3,]
 3
A[1,] # vector
[1] 1 4
A[1:2,] # matrix
[,1] [,2]
[1,] 1 4
[2,] 2
A[1, , drop=FALSE] # matrix with 1 row
[,1] [,2]
[1,]
 1
```

We proclaim that, if there are many options, the default functions' behaviour should be to return the object of the most generic kind possible, even when it is not the most convenient form. Then, either:

- we equip the function with a further argument which must be explicitly set if we really wish to simplify the output, or
- we ask the user to call a simplifier explicitly after the function call; in this case, if
  the simplifier cannot neaten the object, it should probably fail by issuing an error or at least try to apply some brute force solution (e.g., "fill the gaps" somehow
  itself, preferably with a warning).

#### For instance:

```
as.numeric(A[1:2,]) # always returns a vector
[1] 1 2 4 5
stringi::stri_list2matrix(list(1, 3:4)) # fills the gaps with NAs
[,1] [,2]
[1,] "1" "3"
[2,] NA "4"
```

Ideally, a function is expected to perform one (and only one) well-defined task. If it tends to generate objects of different kinds, depending on the arguments provided, it might be better to compose two or more separate procedures instead.

**Exercise 9.8** Functions such as **rep**, **seq**, and **sample** do not perform a single task. Or do they?

**Note** (\*) In a purely functional programming language, we can assume the so-called *referential transparency*: a call to a *pure function* can always be replaced with the *value* it generates. If this is true, then for the same set of argument values, the output is always the same. Furthermore, there are no side effects. In R, it is not exactly the case:

• a call can introduce/modify/delete variables in other environments (see Chapter 16), e.g., the state of the random number generator,

- due to lazy evaluation, functions are free to interpret the argument forms (passed expressions, i.e., not only: values) however they like; see Section 9.4.7, Section 12.3.9, and Section 17.5,
- printing, plotting, file writing, and database access have apparent consequences with regard to the state of certain external devices or resources.

**Important** Each function *must* return a value. However, in several instances (e.g., plotting, printing) this does not necessarily make sense. In such a case, we may consider returning **invisible**(NULL), a NULL whose *first* printing will be suppressed. Compare the following:

```
f <- function() invisible(NULL)
f() # printing suppressed
x <- f() # by the way, assignment also returns an invisible value
print(x) # no longer invisible
NULL</pre>
```

## 9.2 Organising and maintaining functions

#### 9.2.1 Function libraries

Definitions of frequently-used functions or datasets can be emplaced in separate source files (.R extension) for further reference.

Such libraries can be executed by calling:

```
source("path_to_file.R")
```

**Exercise 9.9** Create a source file (script) named mylib.R, where you define a function called *nlargest* which returns a few largest elements in a given atomic vector.

From within another script, call **source**("mylib.R"); note that relative paths refer to the current working directory (Section 2.1.6). Then, write a few lines of code where you test **nlargest** on some example inputs.

## 9.2.2 Writing R packages (\*)

When a function library grows substantially, there is a need for equipping its contents with the relevant help pages, or we wish to rely on compiled code, turning it into an R package might be worth considering.

**Important** Packages can be written only for ourselves or a small team's purpose. We *do not have to* publish them on CRAN<sup>2</sup>. Let us have mercy on the busy CRAN maintainers and do not contribute to the information overload unless we have come up with something potentially of service<sup>3</sup> for other R users. Packages can always be hosted on and installed from GitLab or GitHub.

#### Package structure (\*)

A source package is a directory containing the following special files and subdirectories:

- DESCRIPTION a text file that gives the name of the project, its version, authors, dependencies on other packages, license, etc.;
- NAMESPACE a text file containing directives stating which objects are available to the package users and which names are imported from other packages;
- R a directory with R scripts (.R files), which define, e.g., functions, example datasets, etc.;
- man a directory with R documentation files (.Rd), describing at least all the exported objects (Section 9.2.2);
- src optional; compiled code (Chapter 14);
- tests optional; tests to run on the package check (Section 9.2.4).

See Section 1 of Writing R Extensions [63] for more details and other options. We do not need to repeat the information from the official manual as all readers can read it themselves.

**Exercise 9.10** Inspect the source code of the example package available for download from https://github.com/gagolews/rpackagedemo.

### Building and installing (\*)

Recall from Section 7.3.1 that a source package can be built and installed by calling:

```
install.packages("pkg_directory", repos=NULL, type="source")
```

Then it can be used as any other R package (Section 7.3.1). In particular, it can be loaded and attached to the search path (Section 16.2.6) via a call to:

```
library("pkg")
```

<sup>&</sup>lt;sup>2</sup> Always consult the CRAN Repository Policy at https://cran.r-project.org/web/packages/policies.html.

<sup>&</sup>lt;sup>3</sup> Let us make it less about ourselves and more about the community. Developing expertise in any complex area takes years of hard work. In the meantime, we can help open-source projects by spreading the good word about them, submitting bug fixes, extending documentation, supporting other users through their journey, etc.

All the exported objects mentioned in its NAMESPACE file are now available to the user; see also Section 16.3.5.

**Exercise 9.11** Create a package mypkg with the solutions to the exercises listed in the previous chapter. When in doubt, refer to the official manual [63].

**Note** (\*) The building and installing of packages also be done from the command line:

```
R CMD build pkg_directory # creates a distributable source tarball (.tar.gz)
R CMD INSTALL pkg-version.tar.gz
R CMD INSTALL --build pkg_directory
```

Also, some users may benefit from authoring Makefiles that help automate the processes of building, testing, checking, etc.

#### Documenting (\*)

Documenting functions and commenting code thoroughly is critical, even if we just write for ourselves. Most programmers sooner or later will notice that they find it hard to determine what a piece of code is doing after they took a break from it. In some sense, we always communicate with external audiences, which includes our future selves.

The help system is one of the stronger assets of the R environment. By far, we most likely have interacted with many documentation pages and got a general idea of what constitutes an informative documentation piece.

From the technical side, documentation (.Rd) files are located in the man subdirectory of a source package. All exported objects (e.g., functions) should be described clearly. Additional topics can be covered too.

During the package installation, the .Rd files are converted to various output formats, e.g., HTML or plain text, and displayed on a call to the well-known **help** function.

Documentation files use a LaTeX-like syntax, which looks quite obscure to an untrained eye. The relevant commands are explained in very detail in Section 2 of [63].

**Note** The process of writing .Rd files by hand might be tedious, especially keeping track of the changes to the \usage and \arguments commands. Rarely do we recommend the use of external packages for base R facilities are usually sufficient. But **roxygen2** might be worth a try because it makes the developers' lives easier. Most importantly, it allows the documentation to be specified alongside the functions' definitions, which is much more natural.

**Exercise 9.12** Add a few manual pages to your example R package.

## 9.2.3 Writing standalone programs (\*\*)

Section 7.3.2 mentioned how to call external programs using system2.

On UNIX-like operating systems, it is easy to turn our R scripts into standalone tools that can be run from the terminal. We have already touched upon this topic in Section 1.2.3.

The **commandArgs** function returns the list of arguments passed from the command line to our script in the form of a character vector. Whatever we do with them is up to us. Moreover, **q** can terminate a script, yielding any integer return code. By convention, anything other than 0 indicates an error.

**Example 9.13** Say we have the following script named testfile in the current directory:

```
#!/bin/env -S Rscript --vanilla

argv <- commandArgs(trailingOnly=TRUE)
cat("commandArgs:\n")
print(argv)

if (length(argv) == 0) {
 cat("Usage: testfiles file1 file2 ...\n")
 q(save="no", status=1) # exit with code 1
}

if (!all(file.exists(argv))) {
 cat("Some files do not exist.\n")
 q(save="no", status=2) # exit with code 2
}

cat("All files exist.\n")

exits with code 0 (success)</pre>
```

Example interactions with this program from a UNIX-like shell (bash):

```
chmod u+x testfiles # add permission to execute
./testfiles
commandArgs:
character(0)
Usage: testfiles file1 file2 ...
./testfiles spanish_inquisition
commandArgs:
[1] "spanish_inquisition"
Some files do not exist.
./testfiles spam bacon eggs spam
commandArgs:
```

```
[1] "spam" "bacon" "eggs" "spam"
All files exist.
```

**stdin**, **stdout**, and **stderr** represent the always-open connections mapped to the standard input ("keyboard"), as well as the normal and error output. They can be read from or written to using functions such as **scan** or **cat**.

During run time, we can redirect **stdout** and **stderr** to different files or even strings using **sink**.

# 9.2.4 Assuring quality code

Below we mention some good development practices related to maintaining quality code. This is an important topic, but writing about them is tedious to the same extent that reading about them is dull. It is the more *artistic* part of software engineering as such heuristics are learnt best by observing and mimicking what more skilled programmers are doing (the exercises below aim to make up for our not having them at hand at the moment).

#### Managing changes and working collaboratively

We are recommended to employ a source code version control system, such as **git**, to keep track of the changes made to the software.

**Note** It is worth investing time and effort to learn how to use **git** from the command line; see https://git-scm.com/doc.

There are a few hosting providers for **git** repositories, with GitLab and GitHub being particularly popular among open-source software developers. They support working collaboratively on the projects and are equipped with additional tools for reporting bugs, suggesting feature requests, etc.

**Exercise 9.14** Find source code of your favourite R packages or other projects. Explore the corresponding repositories, feature trackers, wikis, discussion boards, etc. Each community is different and is governed by varied, sometimes contrasting guidelines; after all, we come from all corners of the world.

## Test-driven development and continuous integration

It is often hygienic to include some principles of *test-driven development*.

**Exercise 9.15** Assume that, for some reason, we were asked to compose a function to compute the root mean square (quadratic mean) of a given numeric vector. Before implementing the actual routine, we need to reflect upon what we want to achieve, especially how we want our function to behave in certain boundary cases.

**stopifnot** gives simple means to ensure that a given assertion is fulfilled. If that is the case, it will move forward without fuss.

Let us say we have come up with the following set of expectations:

```
stopifnot(all.equal(rms(1), 1))
stopifnot(all.equal(rms(1:100), 58.16786054171151931769))
stopifnot(all.equal(rms(rep(pi, 10)), pi))
stopifnot(all.equal(rms(numeric(0)), 0))
```

Write a function **rms** that fulfils the above assertions.

**Exercise 9.16** Implement your version of the **sample** function (assuming replace=TRUE), using calls to **runif**. Start by writing a few unit tests.

A couple of R packages support writing and executing unit tests, including **testthat**, **tinytest**, **RUnit**, or **realtest**. However, in the most typical use cases, relying on **stopi-fnot** is powerful enough.

**Exercise 9.17** (\*) Consult the Writing R Extensions manual [63] about where and how to include unit tests in your example package.

**Note** (\*) R can check a couple of code quality areas: running R CMD check pkg\_directory from the command line (preferably using the most recent version of the environment) will suggest several improvements.

Also, it is possible to use various continuous integration techniques that are automatically triggered when pushing changes to our software repositories; see GitLab CI or GitHub Actions. For instance, we can run a package build, install, and check process is possible on every **git** commit. Also, CRAN deploys continuous integration services, including checking the package on various platforms.

#### Debugging

For all his life, the current author has been debugging his programs primarily by manually printing the state of the suspicious variables (**printf** and the like) in different code areas. This is old-school but weirdly efficient.

R has an interactive debugger; see the **browser** function and Section 9 of [67] for more details. Some IDEs (e.g., **RStudio**) also support this feature; see their corresponding documentation.

## **Profiling**

Typically, a program spends relatively long time executing only a small portion of code. The **Rprof** function can be a helpful tool to identify which chunks might need a rewrite, for instance, using a compiled language (Chapter 14).

Please remember, though, that bottlenecks are not only formed by using algorithms

with high computational complexity, but also data input and output (such as reading files from disk, printing messages on the console, querying Web APIs, etc.).

# 9.3 Special functions: Syntactic sugar

Some functions, such as `\*`, are somewhat special. They can be referred to using *infix* syntax which, for obvious reasons, most of us accepted as the default one. However, below we will reveal, amongst others, that "5 \* 9" reduces to an ordinary function *call*:

```
`*`(5, 9) # a call to `*` with two arguments, equivalent to 5 * 9 ## [1] 45
```

#### 9.3.1 Backticks

In Section 2.2, we mentioned that via `<-` we can assign *syntactically valid names* to our objects. Most identifiers comprised of letters, digits, dots, and underscores can be used directly in R code.

Nevertheless, it is possible to label our objects however we like. Not syntactically valid (nonstandard) identifiers just need to be enclosed in backticks (back quotes, grave accents):

```
`42 a quite peculiar name :0` <- c(a=1, `b c`=2, `42`=3, `!`=4)
1/(1+exp(-`42 a quite peculiar name :0`))
a b c 42 !
0.73106 0.88080 0.95257 0.98201
```

Such names are less convenient but backticks let us refer to them in any setting.

# 9.3.2 Dollar, `\$` (\*)

The dollar operator, `\$`, can be an alternative accessor to a single element in a named list<sup>4</sup>. If a label is a syntactically valid name, then x\$label does the same job as x[["label"]] (saving five keystrokes: such a burden!).

```
x <- list(spam="a", eggs="b", `eggs and spam`="c", best.spam.ever="d")
x$eggs
[1] "b"
x$best.spam.ever # recall that a dot has no special meaning in most contexts
[1] "d"</pre>
```

Nonstandard names must still be enclosed in backticks:

<sup>&</sup>lt;sup>4</sup> And hence also in data frames.

```
x$`eggs and spam` \# x[\lceil"eggs \ and \ spam"]] is okay as usual
[1] "c"
```

We are minimalist by design here. Thence, we will avoid this operator for it does not increase the expressive power of our function repertoire. Also, it does not work on atomic vectors nor matrices. Furthermore, it does not support names that are generated programmatically:

```
what <- "spam"
x$what # the same as x[["what"]]; we do not want this
NULL
x[[what]] # works fine
[1] "a"
```

The support for the partial matching of element names has been added to provide users working in interactive programming sessions with some relief in the case where they find typing the whole label daunting:

```
x$s
Warning in x$s: partial match of 's' to 'spam'
[1] "a"
```

#### Compare:

```
x[["s"]] # no warning here...
NULL
x[["s", exact=FALSE]]
[1] "a"
```

Partial matching is generally a rubbishy programming practice. The result depends on the names of other items in x (which might change later) and can decrease code readability. The only reason why we obtained a warning message was because this book enforces the options (warnPartialMatchDollar=TRUE) setting, which, sadly, is not the default.

Note the behaviour on an ambiguous partial match:

```
x$eqq # ambiguous resolution
NULL
```

as well as on an element assignment:

```
x$s <- "e"
str(x)
List of 5
 : chr "a"
$ spam
$ eggs
 : chr "b"
 (continues on next page)
```

```
$ eggs and spam : chr "c"

$ best.spam.ever: chr "d"

$ s : chr "e"
```

It did not modify spam but added a new element, s. Confusing? Just let us not use the dollar operator and we will have one less thing to worry about.

## 9.3.3 Curly braces, `{`

A block of statements grouped with curly braces, `{`, corresponds to a function call. When we write:

```
{
 print(TRUE)
 cat("two")
 3
}
[1] TRUE
two
[1] 3
```

The parser translates it to a call to:

```
`{`(print(TRUE), cat("two"), 3)
[1] TRUE
two
[1] 3
```

When the above is executed, every argument to  $\hat{I}$  is evaluated one by one. Then, the last value is returned as the result of that call.

## 9.3.4 `if`

**if** is a function too. As mentioned in Section 8.1, it returns the value corresponding to the expression that is evaluated conditionally. Hence, we may write:

```
if (runif(1) < 0.5) "head" else "tail"
[1] "head"</pre>
```

but also:

```
`if`(runif(1) < 0.5, "head", "tail")
[1] "head"</pre>
```

**Note** A call like `if` (test, what\_if\_true, what\_if\_false) can only work correctly because of the lazy evaluation of function arguments; see Chapter 17.

On a side note, while, for, repeat can also be called that way, but they return invisible(NULL).

#### 9.3.5 Operators are functions

#### Calling built-in operators as functions

Every arithmetic, logical, and relational operator is translated to a call to the corresponding function. For instance:

```
`<`(`+`(`*`(`-`(3), 4)), 5) # 2+(-3)*4 < 5
[1] TRUE
```

Also, x[i] is equivalent to [(x, i)] and x[[i]] maps to [(x, i)].

Knowing this will not only enable us to manipulate unevaluated R code (Chapter 15) or access the corresponding manual pages (see, e.g., help("[")), but also verbalise certain operations more concisely. For instance:

```
x <- list(1:5, 11:17, 21:23)
unlist(Map(`[`, x, 1)) # 1 is a further argument passed to `[`
[1] 1 11 21</pre>
```

is equivalent to a call to Map(function(e) e[1], x).

**Note** Unsurprisingly, the assignment operator, `<-`, is also a function. It returns the assigned value invisibly.

`<-` binds right to left (compare help("Syntax")). Thus, the expression "a <- b <- 1" assigns 1 to both b and a. It is equivalent to `<- `("a", `<- `("b", 1)) and `<- `("b", 1) returns 1.

Owing to the pass-by-value-like semantics (Section 9.4.1), we can also expect that we will be assigning a *copy* of the value on the right side of the operator (with the exception of environments; Chapter 16).

```
x <- 1:6
y <- x # makes a copy (but delayed, on demand, for performance reasons)
y[c(TRUE, FALSE)] <- NA_real_ # modify every second element
print(y)
[1] NA 2 NA 4 NA 6
print(x) # state of x has not changed; x and y are different objects
[1] 1 2 3 4 5 6</pre>
```

This is especially worth pointing out to Python (amongst others) programmers, where the above assignment would mean that x and y both refer to the same (shared) object in the computer's memory.

However, with no harm done to semantics, copying x is postponed until absolutely necessary (Section 16.1.4). This is efficient both time- and memory-wisely.

#### Defining binary operators

We can also introduce custom binary operators named like `myopname\*`:

```
`%:)%` <- function(e1, e2) (e1+e2)/2
5 %:)% 1:10
[1] 3.0 3.5 4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5
```

Recall that `%%`, `%/%`, and `%in%` are built-in operators denoting division remainder, integer division, and testing for set inclusion. Also, in Chapter 11, we will learn about `%\*%`, which implements matrix multiplication.

**Note** Chapter 10 notes that most existing operators can be overloaded for objects of custom types.

# 9.3.6 Replacement functions

Functions generally do not change the state of their arguments. However, there is some syntactic sugar that permits us to replace objects or their parts with new content. We call them *replacement functions*.

For instance, three of the following calls *replace* the input x with its modified version:

```
x <- 1:5 # example input
x[3] <- 0 # replace the third element with 0
length(x) <- 7 # "replace" length
names(x) <- LETTERS[seq_along(x)] # replace the names attribute
print(x) # `x` is now different
A B C D E F G
1 2 0 4 5 NA NA</pre>
```

# **Creating replacement functions**

A replacement function is a mapping named like `f<-` with at least two parameters:

- x (the object to be modified),
- ... (possible further arguments),
- value (as the last parameter; the object on the right-hand side of the `<-` operator).

We will most often interact with existing replacement functions, not create our own ones. But knowing how to do the latter is vital to understanding this language feature. For example:

```
`add<-` <- function(x, where=TRUE, value)
{
 x[where] <- x[where] + value
 x # the modified object that will replace the original one
}
```

The above aims to add a value to a subset of the input vector x (by default, to each element therein). Then, it returns its altered version.

```
y <- 1:5
 # example vector
add(y) < -10
 # calls y <- `add<-`(y, value=10)
print(y)
 # y has changed
[1] 11 12 13 14 15
add(y, 3) <- 1000 # calls y <- `add<-`(y, 3, value=1000)
print(y)
 # y has changed again
[1] 11 12 1013 14
 15
```

Thus, invoking "add(y, w) <- v" is equivalent to "y <- `add<-`(y, w, value=v)".

**Note** (\*) According to [67], a call "add(y, 3) <- 1000" is a syntactic sugar precisely for:

```
`*tmp*` <- y # temporary substitution</pre>
y <- `add<-`(`*tmp*`, 3, value=1000)</pre>
rm("*tmp*") # remove the named object from the current scope
```

This has at least two implications. First, in the unlikely event that a variable `\*tmp\*` existed before the call to the replacement function, it will be no more, it will cease to be. It will be an ex-variable. Second, the temporary substitution guarantees that y must exist before the call (due to lazy evaluation, a function's body does not have to refer to all the arguments passed).

## Substituting parts of vectors

The replacement versions of the index-like operators are named as follows:

- `[<-` is used in substitutions like "x[i] <- value",
- `[[<-` is called when we perform "x[[i]] <- value",
- `\$<-` is used whilst calling "x\$i <- value".

```
x <- 1:5
`[<-`(x, c(3, 5), NA_real_) # returns a new object
```

```
[1] 1 2 NA 4 NA
print(x) # does not change the original input
[1] 1 2 3 4 5
```

**Exercise 9.18** Write a function `extend<-`, which pushes new elements at the end of a given vector, modifying it in place.

```
`extend<-` <- function(x, value) ...to.do...
```

Example use:

```
x <- 1
extend(x) <- 2 # push 2 at the back
extend(x) <- 3:10 # add 3, 4, ..., 10
print(x)
[1] 1 2 3 4 5 6 7 8 9 10</pre>
```

#### Replacing attributes

There are many replacement functions to reset object attributes (Section 4.4). In particular, each special attribute has its replacement procedure, e.g., `names<-`, `class<-`, `dim<-`, `levels<-`, etc.

```
x <- 1:3
names(x) <- c("a", "b", "c") # change the `names` attribute
print(x) # x has been altered
a b c
1 2 3</pre>
```

Individual (arbitrary, including non-special ones) attributes can be set using `attr<-`, and all of them can be established via a single call to `attributes<-`.

```
x <- "spam"
attributes(x) <- list(shape="oval", smell="meaty")
attributes(x) <- c(attributes(x), taste="umami")
attr(x, "colour") <- "rose"
print(x)
[1] "spam"
attr(, "shape")
[1] "oval"
attr(, "smell")
[1] "meaty"
attr(, "taste")
[1] "umami"</pre>
```

(continues on next page)

```
attr(,"colour")
[1] "rose"
```

Also, setting an attribute to NULL results, by convention, in its removal:

```
attr(x, "taste") <- NULL # it is tasteless now</pre>
print(x)
[1] "spam"
attr(,"shape")
[1] "oval"
attr(,"smell")
[1] "meaty"
attr(,"colour")
[1] "rose"
attributes(x) <- NULL # remove all
print(x)
[1] "spam"
```

Which can be worthwhile in contexts such as:

```
x <- structure(c(a=1, b=2, c=3), some_attrib="value")</pre>
y <- `attributes<-`(x, NULL)</pre>
```

y is a version of x with metadata removed. The latter remains unchanged.

#### Compositions of replacement functions (\*)

Updating only selected names like:

```
x <- c(a=1, b=2, c=3)
names(x)[2] \leftarrow "spam"
print(x)
##
 a spam c
 1 2
 3
```

is possible due to the fact that "names(x)[i] <- v" is equivalent to:

```
old_names <- names(x)</pre>
new_names <- `[<-`(old_names, i, value=v)</pre>
x <- `names<-`(x, value=new_names)</pre>
```

**Important** More generally, a composition of replacement calls "g(f(x, a), b) < y" yields a result equivalent to "x <- f<-(x, a, value=g<-(f(x, a), b, value=y))". Both **f** and `**f**<-` need to be defined, but having **g** is not necessary.

**Exercise 9.19** (\*) What is " $h(g(f(x, a), b), c) \leftarrow y$ " equivalent to?

**Exercise 9.20** Write a (convenient!) function `recode<-` which replaces specific elements in a character vector with other ones, allowing the following interface:

```
`recode<-` <- function(x, value) ...to.do...
x <- c("spam", "bacon", "eggs", "spam", "eggs")
recode(x) <- c(eggs="best spam", bacon="yummy spam")
print(x)
[1] "spam" "yummy spam" "best spam" "spam" "best spam"</pre>
```

We see that the named character vector gives a few from="to" pairs, e.g., all eggs are to be replaced by best spam. Determine which calls are equivalent to the following:

```
x <- c(a=1, b=2, c=3)
recode(names(x)) <- c(c="z", b="y") # or equivalently = ... ?
print(x)
a y z
1 2 3
y <- list(c("spam", "bacon", "spam"), c("spam", "eggs", "cauliflower"))
recode(y[[2]]) <- c(cauliflower="broccoli") # or = ... ?
print(y)
[1] "spam" "bacon" "spam"
##
[[2]]
[1] "spam" "eggs" "broccoli"</pre>
```

**Exercise 9.21** (\*) Consider the `recode<-` function from the previous exercise.

Here is an example matrix with the dimnames attribute whose names attribute is set (more details in Chapter 11):

```
(x <- Titanic["Crew", , "Adult",])</pre>
##
 Survived
Sex
 No Yes
Male
 670 192
 Female
 3 20
recode(names(dimnames(x))) <- c(Sex="sex", Survived="survived")</pre>
print(x)
##
 survived
sex
 No Yes
Male 670 192
Female 3 20
```

This changes the x object. For each of the following subtasks, compose a single call that alters names(dimnames(x)) without modifying x in place but returning a recoded copy of:

```
 names(dimnames(x)),
```

- dimnames(x),
- x

**Exercise 9.22** (\*) Consider the `recode<-` function again but now let an example object be a data frame with a column of the factor class:

```
x <- iris[c(1, 2, 51, 101),]
recode(levels(x[["Species"]])) <- c(</pre>
 setosa="SET", versicolor="VER", virginica="VIR"
)
print(x)
##
 Sepal.Length Sepal.Width Petal.Length Petal.Width Species
1
 5.1
 1.4
 0.2
 3.5
2
 4.9
 3.0
 1.4
 0.2
 SET
51
 7.0
 3.2
 4.7
 1.4
 VER
101
 6.3
 3.3
 6.0
 2.5
 VTR
```

How to change levels(x[["Species"]]) and return an altered copy of:

- levels(x[["Species"]]),
- x[["Species"]],
- · x

without modifying x in place?

# 9.4 Arguments and local variables

## 9.4.1 Call by "value"

As a general rule, functions cannot change the state of their arguments<sup>5</sup>. We can think of them as being passed by *value*, i.e., as if their copy was made.

```
test_change <- function(y)
{
 y[1] <- 7
 y
}

x <- 1:5
test_change(x)

(continues on next page)</pre>
```

<sup>&</sup>lt;sup>5</sup> With the exception of objects of the type environment, which are passed by reference; see Chapter 16. Also, the fact that we have access to unevaluated R expressions can cause further deviations to this rule because, actually, R implements the *call-by-need* strategy; see Chapter 17.

```
[1] 7 2 3 4 5
print(x) # same
[1] 1 2 3 4 5
```

If the above statement was not true, the state of x would change after the call.

## 9.4.2 Variable scope

Function arguments and any other variables we create inside a function's body are *relative* to each call to that function.

Both x and z are local variables. They only live whilst our function is being executed. The former temporarily *masks*<sup>6</sup> the object of the same name from the caller's context.

**Important** It is a good development practice to refrain from referring to objects not created within the current function, especially to "global" variables. We can always pass an object as an argument explicitly.

**Note** It is a function call as such, not curly braces per se that form a local scope. When we run " $x < \{ y < 1; y + 1 \}$ ", y is not an temporary variable. It is an ordinary named object created alongside x.

On the other hand, in "x <- (function() { z <- 1; z + 1 })()", z will not be available thereafter.

<sup>&</sup>lt;sup>6</sup> Chapter 16 discusses this topic in-depth: names are bound to objects within environment frames. Moreover, R uses lexical (static) scoping, which is not necessarily intuitive, especially taking into account that a function's environment can always be changed.

## 9.4.3 Closures (\*)

Most user-defined functions are, in fact, instances of the so-called *closures*; see Section 16.3.2 and [1]. They not only consist of an R expression to evaluate but also can carry auxiliary data.

For instance, given two numeric vectors x and y of the same length, a call to **approx-fun**(x, y) returns a *function* that linearly interpolates between the consecutive points  $(x_1, y_1)$ ,  $(x_2, y_2)$ , etc., so that a corresponding y can be determined for any x.

```
x <- seq(0, 1, length.out=11)
f1 <- approxfun(x, x^2)
f2 <- approxfun(x, x^3)
f1(0.75) # check that it is quite close to the true 0.75^2
[1] 0.565
f2(0.75) # compare with 0.75^3
[1] 0.4275</pre>
```

Let us inspect the source code of the above functions:

```
print(f1)
function (v)
.approxfun(x, y, v, method, yleft, yright, f, na.rm)
<environment: 0x561e197cb5a0>
print(f2)
function (v)
.approxfun(x, y, v, method, yleft, yright, f, na.rm)
<environment: 0x561e198361c8>
```

We might wonder how they can produce different results. It is evident that they are identical. It turns out, however, that they internally store additional data that are referred to when they are called:

```
environment(f1)[["y"]]
[1] 0.00 0.01 0.04 0.09 0.16 0.25 0.36 0.49 0.64 0.81 1.00
environment(f2)[["y"]]
[1] 0.000 0.001 0.008 0.027 0.064 0.125 0.216 0.343 0.512 0.729 1.000
```

We will explore these concepts in detail in the third part of this book.

# 9.4.4 Default arguments

We often need to find a sweet spot between being generous, mindful of the diverse needs of our users, and making the API neither overwhelming nor oversimplistic. We have established that it is best if a function performs a single, well-specified task. However, we are always delighted when it also lets us tweak its behaviour should we wish to do so. The use of default arguments can facilitate this principle.

For instance, log computes logarithms, by default, the natural ones.

```
log(2.718) # the same as log(2.718, base=exp(1)), i.e., default base, e
[1] 0.9999
log(4, base=2) # different base
[1] 2
```

**Exercise 9.23** Study the documentation of the following functions and note the default values they define: **round**, **hist**, **grep**, and **download**. **file**.

Let us create a function equipped with such recommended settings:

```
test_default <- function(x=1) x

test_default() # use default
[1] 1
test_default(2) # use something else
[1] 2</pre>
```

Most often, default arguments are just constants, e.g., 1. Generally, though, they can be any R expressions, also ones that include a reference to other arguments passed to the same function; see Section 17.2.

Default arguments usually appear at the end of the parameter list, but see Section 9.3.6 (on replacement functions) for a well-justified exception.

## 9.4.5 Lazy vs eager evaluation

In some languages, function arguments are always evaluated prior to a call. In R, though, they are only computed when actually needed. We call it *lazy* or *delayed* evaluation. Recall that in Section 8.1.4, we introduced the short-circuit evaluation operators `||` (or) and `&&` (and). They can do their job precisely thanks to this mechanism.

**Example 9.24** In the following example, we do not use the function's argument at all:

```
lazy_test1 <- function(x) 1 # x is not used

lazy_test1({cat("and now for something completely different!"); 7})
[1] 1</pre>
```

Otherwise, we would see a message being printed out on the console.

**Example 9.25** *Next, let us use x amidst other expressions in the body:* 

```
lazy_test2 <- function(x)
{
 cat("it's... ")
 y <- x+x # using x twice
 cat(" a man with two noses")
 y
 (continues on next page)</pre>
```

```
lazy_test2({cat("and now for something completely different!"); 7})
it's... and now for something completely different! a man with two noses
[1] 14
```

An argument is evaluated once, and its value is stored for further reference. If that was not the case, we would see two messages like "and now...".

We will elaborate on this in Chapter 17.

# 9.4.6 Ellipsis, `...`

Let us start with an exercise.

**Exercise 9.26** Notice the presence of `...` in the parameter list of **c**, list, structure, cbind, rbind, cat, Map (and the underlying mapply), lapply (a specialised version of Map), optimise, optim, uniroot, integrate, outer, aggregate. What purpose does it serve, according to these functions' documentation pages?

We can create a *variadic function* by including `...` (dot-dot-dot, ellipsis; see **help**("dots")) somewhere in its parameter list. The ellipsis serves as a placeholder for all objects passed to the function but not matched by any formal (named) parameters.

The easiest way to process arguments passed via `...` programmatically (see also Section 17.3) is by redirecting them to **list**.

```
test_dots <- function(...)
 list(...)

test_dots(1, a=2)
[[1]]
[1] 1
##
$a
[1] 2</pre>
```

Such a list can be processed just like... any other generic vector. What we can do with these arguments is only limited by our creativity (in particular, recall from Section 7.2.2 the very powerful do.call function). There are two primary use cases of the ellipsis<sup>7</sup>:

• create a new object by combining an arbitrary number of other objects:

```
c(1, 2, 3) # three arguments
[1] 1 2 3

(continues on next page)
```

<sup>&</sup>lt;sup>7</sup> Which is somewhat similar to Python's \*args and \*\*kwargs in a function's parameter list.

```
c(1:5, 6:7) # two arguments
[1] 1 2 3 4 5 6 7
structure("spam") # no additional arguments
[1] "spam"
structure("spam", color="rose", taste="umami") # two further arguments
[1] "spam"
attr(,"color")
[1] "rose"
attr(,"taste")
[1] "umami"
cbind(1:2, 3:4) # two
##
 \lceil,1\rceil \lceil,2\rceil
[1,] 1 3
[2,]
 2
cbind(1:2, 3:4, 5:6, 7:8) # four
[,1] [,2] [,3] [,4]
[1,] 1 3 5 7
[2,] 2 4 6 8
sum(1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 42) # twelve
[1] 108
```

pass further arguments (as-is) to other methods:

**Example 9.27** The documentation of **lapply** states that this function is defined like **lapply**(X, FUN, ...). Here, the ellipsis is a placeholder for a number of optional arguments that can be passed to **FUN**. Hence, if we denote the i-th element of a vector X by X[[i]], calling **lapply**(X, FUN, ...) will return a list whose i-th element will be equal to **FUN**(X[[i]], ...).

**Exercise 9.28** Using a single call to **lapply**, generate a list with three numeric vectors of lengths 3, 9, and 7, respectively, drawn from the uniform distribution on the unit interval. Then, upgrade your code to get numbers sampled from the interval [-1, 1].

**Example 9.29** Chapter 4 mentioned that concatenating a mix of lists and atomic vectors with **c**, unfortunately, unrolls the latter:

```
str(c(u=list(1:2), v=list(a=3:4, b=5:6), w=7:8)) (continues on next page)
```

```
List of 5
$ u : int [1:2] 1 2
$ v.a: int [1:2] 3 4
$ v.b: int [1:2] 5 6
$ w1 : int 7
$ w2 : int 8
```

Let us implement a fix:

```
as.list2 <- function(x) if (is.list(x)) x else list(x)
clist <- function(...) do.call(c, lapply(list(...), as.list2))
str(clist(u=list(1:2), v=list(a=3:4, b=5:6), w=7:8))
List of 4
$ u : int [1:2] 1 2
$ v.a: int [1:2] 3 4
$ v.b: int [1:2] 5 6
$ w : int [1:2] 7 8</pre>
```

## 9.4.7 Metaprogramming (\*)

We can access *expressions* passed as a function's arguments *without evaluating them*. In particular, a call to the composition of **deparse** and **substitute** converts them to a character vector.

```
test_deparse_substitute <- function(x)
 deparse(substitute(x)) # does not evaluate whatever is behind `x`

test_deparse_substitute(testing+1+2+3)
[1] "testing + 1 + 2 + 3"
test_deparse_substitute(spam & spam^2 & bacon | grilled(spam))
[1] "spam & spam^2 & bacon | grilled(spam)"</pre>
```

**Exercise 9.30** Check out the y-axis label generated by **plot.default**((1:100)^2). Inspect its source code. Notice a call to the two aforementioned functions.

Similarly, call **shapiro.test(log(rlnorm**(100))) and take note of the "data:" field.

A function is free to do with such an expression whatever it likes. For instance, it can modify the expression and then evaluate it in a very different context. Such a language feature allows certain operations to be expressed much more compactly. In theory, it is a potent tool. Alas, it is easy to find many practical examples where it was over/misused and made learning or using R confusing.

**Example 9.31** (\*) In Section 12.3.9 and Section 17.5, we explain that **subset** and **transform** use metaprogramming techniques to specify basic data frame transformations. For instance:

```
transform(
 subset(
 iris.
 Sepal.Length>=7.7 & Sepal.Width >= 3.0, # huh?
 select=c(Species, Sepal.Length:Sepal.Width) # le what?
),
 Sepal.Length.mm=Sepal.Length/10 # pardon my French, but pardon?
)
##
 Species Sepal.Length Sepal.Width Sepal.Length.mm
118 virginica
 7.7
 3.8
 0.77
132 virginica
 7.9
 0.79
 3.8
136 virginica
 7.7
 3.0
 0.77
```

None of the arguments (except iris) makes sense outside of the function's call. In particular, neither Sepal.Length nor Sepal.Width exists as a standalone variable.

The two functions took the liberty to interpret the arguments passed how they felt. They created their own virtual reality within our well-defined world. The reader must refer to their documentation to discover the meaning of such special syntax.

**Note** (\*) Some functions have rather peculiar default arguments. For instance, in the manual page of **prop.test**, we read that the alternative parameter defaults to **c**("two.sided", "less", "greater") but that "two.sided" is actually the default one.

If we call **print(prop.test)**, we will find the code line responsible for this behaviour: "alternative <- **match.arg**(alternative)". Consider the following example:

```
test_match_arg <- function(x=c("a", "b", "c")) match.arg(x)

test_match_arg() # missing argument; choose first
[1] "a"
test_match_arg("c") # one of the predefined options
[1] "c"
test_match_arg("d") # unexpected setting
Error in match.arg(x): 'arg' should be one of "a", "b", "c"</pre>
```

In this setting, match.arg only allows an actual parameter from a given set of choices but selects the first option if the argument is missing.

Unfortunately, we have to learn this behaviour by heart because looking at the above source code gives us no clue about this being possible. If such an expression was normally evaluated, we would use either the default argument or whatever the user passed as x (but then the function would not know the range of possible choices). A call to match.arg(x, c("a", "b", "c")) could guarantee the desired functionality and would be much more readable. Instead, metaprogramming techniques enabled

match.arg to access the enclosing function's default argument list without explicitly referring to them.

One may ask: why is it so? The only sensible answer to this will be "because its programmer decided it must be this way". Let us contemplate this for a while. In cases like these, we are not dealing with some base R language design choice that we might like or dislike, but which we should just accept as an inherent feature. Instead, we are struggling intellectually because of some programmers' (mis)use (in good faith...) of R's flexibility itself. They have introduced a slang/dialect on top of our mother tongue, whose meaning is valid only within this function. Blame the middleman, not the environment, please.

This is why we generally advocate for avoiding metaprogramming-based techniques wherever possible. We shall elaborate on this topic in the third part of this book.

# 9.5 Principles of sustainable design (\*)

Fine design is more art than science. As usual in real life, we will need to make many compromises. This is because improving things with regard to one criterion sometimes makes them worse with respect to other aspects<sup>8</sup> (also those that we are not aware of). Moreover, not everything that counts can nor will be counted.

We do not want to be considered heedless enablers who say that if anything is possible, it should be done. Therefore, below we serve some food for thought. However, as there is no accounting for taste, the kind readers might as well decide to skip this spicy meal.

#### 9.5.1 To write or abstain

Our functions can often be considered merely creative combinations of the building blocks available in base R or a few high-quality add-on packages. Some are simpler than others. Thus, there is a question if a new operation should be introduced at all: whether we are faced with the case of multiplying entities without necessity.

On the one hand, the DRY (don't repeat yourself) principle tells us that the most frequently used code chunks (say, called at least thrice) should be generalised in the form of a new function. As far as *complex* operations are concerned, this is definitely a correct approach.

On the other hand, not every generalisation is necessarily welcome. Let us say we are tired of writing  $\mathbf{g}(\mathbf{f}(\mathbf{x}))$  for the n-th time,  $n \geq 2$ . Why not introduce  $\mathbf{h}$  defined as a combination of  $\mathbf{g}$  and  $\mathbf{f}$ ? This might seem like a clever idea, but let us not take it for granted. Being tired might be an indication that we need a rest. Being lazy can be a call

<sup>&</sup>lt;sup>8</sup> Compare the notion of Pareto efficiency.

for more self-discipline (not an overly popular word these days, but still, an endearing trait).

**Example 9.32** paste0 is a specialised version of paste, but has the sep argument hardcoded to an empty string.

- Even if this might be the most often applied use case, is the introduction of a new function justifiable? Is it so hard to write sep=""each time?
- Would changing **paste**'s default argument be better? That, of course, would harm backward compatibility, but what strategies could we apply to make the transition as smooth as possible?
- What about introducing a new version of **paste** with sep defaulting to "", and informing the users that the old version is deprecated and will be removed in, say, two years? (or maybe one month is better? or five?)

**Example 9.33** R 4.0 defined a new function called **deparse1**. It is nothing but a combination of **deparse** and **paste**:

```
print(deparse1)
function (expr, collapse = " ", width.cutoff = 500L, ...)
paste(deparse(expr, width.cutoff, ...), collapse = collapse)
<environment: namespace:base>
```

Let us say this covers 90% of use cases: was introducing it a justified idea then? What if that number was 99%? Might it lead to new users' not knowing that the more primitive operations are available?

Overall, more functions contribute to information overload. We do not want our users to be overwhelmed by unreasonably many choices. Luckily, nothing is cemented once and for all. Had we made bad design choices resulting in our API's being bloated, we could always cancel those that no longer spark joy.

# 9.5.2 To pamper or challenge

We should think about the kind of audience we would like to serve: is it our team only, students, professionals, certain client groups, etc.? Do they have mathematical, programming, engineering, or scientific background?

Not everything appropriate for one cohort will be valuable for another.

Not everything pleasing some *now* will benefit them in the long run: people (their skills, attitudes, etc.) change.

**Example 9.34** Assume we are writing a friendly package for novices who would like to grasp the basics of data analysis as quickly as possible. Without much effort, it could enable them to solve 80–95% of the most common, easy problems.

 $Think of introducing \ the \ students \ to \ a \ function \ that \ returns \ the \ five \ largest \ observations \ in \ a \ given$ 

vector. Let us call it **nlargest**. So pleasant. It makes the students feel empowered and improves their retention9.

However, when faced with the remaining 5–20% of tasks, they will have to learn another, more advanced, generic, and capable tool anyway (in our case, the base R itself). Are they determined and skilled enough to do that? Some might, unfortunately, say: "it is not my problem, I made sure everyone was happy at that time". Due to this shortsightedness, it is our problem now.

Recall that it took us some time to arrive at **order** and subsetting via  $\hat{I}$ . Assuming that we read this book from the beginning to the end and solve all the exercises, which we should, we are now able to author the said **nlargest** (and lots of other functions) ourselves, using a single line of code. This will also pay off in many scenarios that we will be facing in the future, e.g., when we consider matrices and data frames.

Yes, everyone will be reinventing their own **nlargest** this way. But this constitutes a great exercise: by our being immoderately nice (spoonfeeding), some might have lost an opportunity to learn a new. more universal skill.

Although most users would love to minimise the effort put into all their activities, ultimately, they sometimes need to learn new things. Let us thus not be afraid to teach them stuff.

Furthermore, we do not want to discourage experts (or experts to-be) by presenting them with overly simplified solutions that keep their hands tied when something more ambitious needs to be done.

#### To build or reuse 9.5.3

The fail-fast philosophy encourages us to build applications using prefabricated components. This is fantastic at the early stage of their life cycles. Nonetheless, if we construct something uncomplicated or whose only purpose is to illustrate an idea, educate, or show off, let us be explicit about it so that other users do not feel obliged to treat our product (exercise) seriously.

In the (not so likely, probabilistically speaking) event of its becoming successful, we are expected to start thinking about the project's long-term stability and sustainability. After all, relying on third-party functions, packages, or programs makes our software projects less... independent. This may be problematic because:

- the dependencies might not be available on every platform or may behave differently across various system configurations,
- they may be huge (and can depend on other external software too),
- their APIs may be altered, which can cause our code to break,
- their functionality can change, which can lead to unexpected behaviour.

<sup>&</sup>lt;sup>9</sup> Brought to the extreme, this strategy is employed by certain companies (and drug dealers): make the introductory experience smooth and fun. At the same time, do not permit your users to become independent too easily. Instead, make them rely on your product lines/proprietary solutions/payable services, etc.

Hence, it might be better to rewrite some parts from scratch on our own.

**Exercise 9.35** Identify a few R packages on CRAN with many dependencies. See what functions they import from other packages. How often do they only borrow a few lines of code?

The UNIX philosophy emphasises building and using minimalist yet nontrivial, single-purpose, high-quality pieces of software that can work as parts of more complex pipelines. R serves as a glue language quite well.

In the long run, our software project might converge to such a tool. Thus, we might have to standardise its API (e.g., make it available from the command line; Section 1.2) so that the users of other languages can benefit from our work.

**Important** If our project is merely a modified interface/front-end to a standalone program developed by others, we should be humble about it. We should strive to ensure we are not the ones who get all the credit for other people's work. Also, we must clearly state how the original tools can be used to achieve the same goals, e.g., when working from the command line. In other words, let us not be selfish jerks.

#### 9.5.4 To revolt or evolve

The wise, gradual improving of things is generally welcome. It gives everyone time to adjust.

Some projects, however, are governed in a compulsive way, reinforced by neurotic thinking that "stakeholders need to be kept engaged or we're going to lose popularity". It is not a sustainable strategy. Less is better, even though slightly more challenging. Put good engineering first.

It might even happen that we realise that "everything so far was wrong and we need a global reset". But if we become very successful, we will cause a *divide* in the community. Especially when we decide to duplicate the existing, base functionality, we should note that some users will be introduced to the system through the supplementary interface and they will not be familiar with the classic one. Others will have to learn the added syntax to be able to communicate with the former group. This gives rise to a whole new set of issues (how to make all the functions interoperable with each other seamlessly, etc.). Such moves are sometimes necessary, but let us not treat them lightly; it is a great responsibility.

#### 9.6 Exercises

**Exercise 9.36** Answer the following questions.

• Will stopifnot(1) stop? What about stopifnot(NA), stopifnot(TRUE, FALSE), and stopifnot(c(TRUE, TRUE, NA))?

- What does the `if` function return?
- Does `attributes<-`(x, NULL) modify x?</li>
- When can we be interested in calling `[` and `[<-` as functions (and not as operators) directly?
- How to define a new binary operator? Can it be equipped with default arguments?
- What are the main use cases of the ellipsis?
- What is wrong with **transform**, **subset**, and **match.arg**?
- When a call like **f**(-1, **do\_something\_that\_takes\_a\_million\_years**()) does not necessarily have to be a regrettable action?
- What is the difference between "names(x)[1] <- new name" and "names(x[1]) <new name"?
- What might be the form of x if it is legit to call it like x[[c(1, 2)]]()()()[[1]]()()?

**Exercise 9.37** *Consider the following function.* 

```
f <- function(x)</pre>
 for (e in x)
 print(e)
```

What is the return value of a call to f(list(1, 2, 3))? Is it NULL, invisible(NULL), x[[length(x)]], or invisible(x[[length(x)]])? Does it change relative to whether x is empty or not?

**Exercise 9.38** The split function also has its replacement version. Study its documentation to learn how it works.

**Exercise 9.39** A call to **ls**(envir=**baseenv**()) returns all objects defined in the **base** package (see Chapter 16). List the names corresponding to replacement functions.

**Important** Apply the principle of test-driven development when solving the remaining exercises.

**Exercise 9.40** Implement your version of the **Position** and **Find** functions. Evaluation should stop as soon as the first element fulfilling a given predicate has been found.

**Exercise 9.41** Implement your version of the **Reduce** function.

**Exercise 9.42** Write a function slide(f, x, k, ...) which returns a list y with **length**(x)-k+1 elements such that y[[i]] = f(x[i:(i+k-1)], ...)

```
unlist(slide(sum, 1:5, 1))
[1] 1 2 3 4 5
unlist(slide(sum, 1:5, 3))
[1] 6 9 12
```

(continues on next page)

```
unlist(slide(sum, 1:5, 5))
[1] 15
```

**Exercise 9.43** Using **slide** defined above, write another function that counts how many increasing pairs of numbers are in a given numeric vector. For instance, in (0, 2, 1, 1, 0, 1, 6, 0), there are three such pairs: (0, 2), (0, 1), (1, 6).

**Exercise 9.44** (\*) Write your version of **tools**::package\_dependencies with reverse=TRUE based on information extracted by calling utils::available.packages.

**Exercise 9.45** (\*\*) Write a standalone program which can be run from the system shell and which computes the total size of all the files in directories given as the script's arguments (via *commandArgs*).

# S3 classes

Let x be a randomly generated matrix with 1 000 000 rows and 1 000 columns, y be a data frame with results from the latest survey indicating that things are way more complicated than what most people think, and z be another matrix, this time with many zeroes.

The human brain is not capable of dealing with excessive data that are immoderately specific. This is why we have a natural tendency to *group* different entities based on their similarities. This way, we form more abstract classes of objects.

Also, many of us are inherently lazy. Oftentimes we take shortcuts to minimise energy (at a price to be paid later).

Printing out a matrix, a data frame, and a time series are all instances of the displaying of things, although they undoubtedly differ in detail. By now, we have probably forgotten which objects are hidden behind x, y, and z that we introduced above. Being able to simply call **print**(y) without having to recall that, yes, y is a data frame, might seem quite appealing.

This chapter introduces S3 classes [13]. They provide a lightweight object-orientated programming (OOP) approach for automated dispatching calls to *generics* of the type **print**(y) to concrete *methods* such as **print.data.frame**(y), based on the *class* of the object they are invoked on.

We shall see that S3 classes in their essence are beautifully simple<sup>1</sup>. Ultimately, *generics* and *methods* are ordinary R functions (Chapter 7) and *classes* are merely additional object attributes (Section 4.4).

Of course, this does not mean that wrapping our heads around them will be effortless. However, unlike other "class systems"<sup>2</sup>, S3 is ubiquitous in most R programming projects. Suffice it to say that factors, matrices, and data frames discussed in the following chapters are quite straightforward, S3-based extensions of the concepts we introduce below.

<sup>&</sup>lt;sup>1</sup> They were built on top of the ordinary ("old S") R so they have inherent limitations that we discuss in the sequel: classes cannot be formally defined (often we will use named lists for representing objects, and we know we cannot be any more flexible than this), and method dispatching can only be based on the class of one of the arguments (usually the first one, but, e.g., binary operators take both types into account).

<sup>&</sup>lt;sup>2</sup> Other class systems may give an impression that they are alien implants which were forcefully added to our language to solve a specific, rather narrow class of problems; e.g., S4 (Section 10.5), reference classes (Section 16.1.5), and other ones proposed by third-party packages.

#### Object type vs class 10.1

Recall that **typeof** (introduced in Section 4.1) returns the internal type of an object. So far, we were mostly focused on atomic and generic vectors; compare Figure 1 in the Preface.

```
typeof(NULL)
[1] "NULL"
typeof(c(TRUE, FALSE, NA))
[1] "logical"
typeof(c(1, 2, 3, NA_real_))
[1] "double"
typeof(c("a", "b", NA_character_))
[1] "character"
typeof(list(list(1, 2, 3), LETTERS))
[1] "list"
typeof(function(x) x)
[1] "closure"
```

The number of admissible types is small<sup>3</sup>, but they open the world of endless possibilities<sup>4</sup>. They provide a basis for more complex data structures. This is thanks to the fact that they can be equipped with arbitrary attributes (Section 4.4).

Most compound types constructed using the mechanisms discussed in this chapter only pretend they are something different from what they actually are. Still, they often do their job very well. By looking under their bonnet, we will be able to manipulate their state outside of the prescribed use cases.

**Important** Setting the class attribute might make some objects behave differently in certain scenarios.

**Example 10.1** Let us equip two identical objects with different class attributes.

```
xt <- structure(123, class="POSIXct") # POSIX calendar time
xd <- structure(123, class="Date")</pre>
```

Both objects are represented using numeric vectors:

```
c(typeof(xt), typeof(xd))
[1] "double" "double"
```

However, when printed, they are decoded quite differently:

<sup>&</sup>lt;sup>3</sup> Their list is hardcoded at the C language level; see the list of SEXPTYPEs in Table 14.1 and [66].

<sup>&</sup>lt;sup>4</sup> In particular, Section 14.2.8 mentions externalptrs which are simple pointers to memory blocks that can be instances of any C structs or C++ classes. This makes R a very extensible language.

```
print(xt)
[1] "1970-01-01 10:02:03 AEST"
print(xd)
[1] "1970-05-04"
```

In the former case, 123 is understood as the number of seconds since the UNIX epoch, 1970-01-01T00:00:00+0000. The latter is deciphered as the number of days since the said timestamp.

Therefore, we expect that there must exist a mechanism that calls a version of **print** dependent on an object's virtual class.

That it only relies on the class attribute, which might be set, unset, or reset quite freely, is emphasised below.

```
attr(xt, "class") <- "Date" # change class from POSIXct to Date
print(xt) # same 123, but now interpreted as Date
[1] "1970-05-04"
as.numeric(xt) # drops all attributes
[1] 123
unclass(xd) # drops the class attribute; `attr<-`(xd, "class", NULL)
[1] 123</pre>
```

We are having so much fun that one more illustration can only increase our joy.

#### **Example 10.2** Consider an example data frame:

It is an object of the following class (an object whose class attribute is set to):

```
attr(x, "class")
[1] "data.frame"
```

Some may say, and they are absolutely right, that we have not covered data frames yet. After all, they are the topic of Chapter 12, which is still ahead of us. However, from the current perspective, we should know that R data frames are nothing but lists of vectors of the same lengths equipped with the names and row. names attributes.

```
##
$Sepal.Width
[1] 3.5 3.0 3.2
##
attr(,"row.names")
[1] 1 2 3
print(x)
 Sepal.Length Sepal.Width
 5.1
 3.5
2
 4.9
 3.0
3
 4.7
 3.2
```

**Important** Revealing how x is actually represented enables us to process it using the extensive skill set that we have already<sup>5</sup> developed by studying the material covered in the previous part of our book (including all the exercises). This fact is noteworthy because some built-in and third-party data types are not particularly well-designed.

Let us underline again that attributes are simple additions to R objects. However, as we said in Section 4.4.3, certain attributes are special, and class is one of them. In particular, we can only set class to be a character vector (possibly of length greater than one; see Section 10.2.5).

```
x <- 12345
attr(x, "class") <- 1 # character vectors only</pre>
Error in attr(x, "class") <- 1: attempt to set invalid 'class' attribute
```

Furthermore, the class function can read the value of the class attribute. Its replacement version is also available.

```
class(x) <- "Date" # set; the same as attr(x, "class") <- "Date"</pre>
class(x) # get; here, it is the same as attr(x, "class")
[1] "Date"
```

**Important** The class function always yields a value, even if the corresponding attribute is not set. We call it an implicit class. Compare the following and the outputs generated by **typeof**:

```
class(NULL) # no `class` set because NULL cannot have any attributes
[1] "NULL"
class(c(TRUE, FALSE, NA)) # no attributes so class is implicit (= typeof)
 (continues on next page)
```

<sup>&</sup>lt;sup>5</sup> For instance, consider once again the example from Section 5.4.3 that applies the **split** function on a data frame reduced to a list.

```
[1] "logical"
class(c(1, 2, 3, NA_real_)) # typeof returns "double"
[1] "numeric"
class(c("a", "b", NA_character_))
[1] "character"
class(list(list(1, 2, 3), LETTERS))
[1] "list"
class(function(x) x) # typeof gives "closure"
[1] "function"
```

Also, Chapter 11 will explain that any object equipped with the dim attribute also has an implicit class:

```
(x <- as.matrix(c(1, 2, 3)))
[,1]
[1,] 1
[2,] 2
[3,] 3
attributes(x) # `class` is not amongst the attributes
$dim
[1] 3 1
class(x) # implicit class
[1] "matrix" "array"
typeof(x) # it is still a numeric vector (under the bonnet)
[1] "double"</pre>
```

# 10.2 Generics and method dispatching

# 10.2.1 Generics, default, and custom methods

Let us inspect the source code of the **print** function:

```
print(print) # sic!
function (x, ...)
UseMethod("print")
<environment: namespace:base>
```

Any function like the above 6 we will call from now on a generic (an S3 generic, from S ver-

<sup>&</sup>lt;sup>6</sup> Some functions can have a version of **UseMethod** hidden at the C language level (internally); see Section 10.2.3.

sion 3 [13]). Its only job is to invoke **UseMethod**("print"). It dispatches the control flow to another function, referred to as a *method*, based on the class of the first argument.

**Important** All arguments passed to the generic will also be available in the method dispatched to.

For example, let us define an object of the class categorical (a name that we have just come up with; we could have called it cat, CATEGORICAL, or SpanishInquisition as well). It will be our version of the factor type that we discuss later.

```
x <- structure(
 c(1, 3, 2, 1, 1, 1, 3),
 levels=c("a", "b", "c"),
 class="categorical"
)</pre>
```

We assume that such an object is a sequence of small positive integers (codes). It is equipped with the levels attribute, which is a character vector of length not less than the maximum of the said integers. In particular, the first level deciphers the meaning of the code 1. Hence, the above vector represents a sequence *a*, *c*, *b*, *a*, *a*, *a*, *a*.

There is no special method for displaying objects of the categorical class. Hence, when we call **print**, the *default* (fallback) method is invoked:

```
print(x)
[1] 1 3 2 1 1 1 3
attr(,"levels")
[1] "a" "b" "c"
attr(,"class")
[1] "categorical"
```

This is the standard function for displaying numeric vectors. We are well familiar with it. Its name is **print.default**, and we can always call it directly:

```
print.default(x) # the default print method
[1] 1 3 2 1 1 1 3
attr(,"levels")
[1] "a" "b" "c"
attr(,"class")
[1] "categorical"
```

However, we can introduce a designated method for printing categorical objects. Its name must precisely be **print.categorical**:

<sup>&</sup>lt;sup>7</sup> However, it cannot be implied by reading the above source code. **UseMethod** heavily relies on some obscure hacks. We may only call it inside a function's body. Once invoked, it does not return to the generic. Before dispatching to a particular method, it creates a couple of hidden variables which give more detail on the operation conveyed, e.g., `.Generic` or `.Class`; see **help**("UseMethod") and Section 5 of [67].

```
print.categorical <- function(x, ...)
{
 x_character <- attr(x, "levels")[unclass(x)]
 print(x_character) # calls `print.default`
 cat(sprintf("Categories: %s\n",
 paste(attr(x, "levels"), collapse=", ")))
 invisible(x) # this is what all print methods do; see help("print")
}</pre>
```

Calling **print** automatically dispatches the control flow to the above method:

```
print(x)
[1] "a" "c" "b" "a" "a" "c"
Categories: a, b, c
```

Of course, the default method can still be called. Referring to **print.default**(x) directly will output the same result as the one a few chunks above.

**Note print.categorical** has been equipped with the dot-dot-dot attribute since the generic **print** had one too<sup>8</sup>.

## 10.2.2 Creating generics

Introducing new S3 generics is as straightforward as defining a function that calls **Use-Method**. For instance, here is a dispatcher which creates new objects of the categorical class based on other objects:

```
as.categorical <- function(x, ...)
UseMethod("as.categorical") # synonym: UseMethod("as.categorical", x)</pre>
```

We always need to define the default method:

```
as.categorical.default <- function(x, ...)
{
 if (!is.character(x))
 x <- as.character(x)
 xu <- unique(sort(x)) # drops NAs
 structure(
 match(x, xu),
 class="categorical",
 levels=xu
)
}</pre>
```

<sup>&</sup>lt;sup>8</sup> (\*) Ensuring S3 generic/method consistency is part of R package check.

Testing:

```
as.categorical(c("a", "c", "a", "d", "c"))
[1] "a" "c" "a" "d" "c"
Categories: a, c, d
as.categorical(c(3, 6, 4, NA, 9, 9, 6, NA, 3))
[1] "3" "6" "4" NA "9" "9" "6" NA "3"
Categories: 3, 4, 6, 9
```

The above method is already quite flexible. It handles a wide variety of data types because it relies on the *built-in generic* **as.character** (Section 10.2.3).

**Example 10.3** We might want to forbid the conversion from lists because it does not necessarily make sense:

```
as.categorical.list <- function(x, ...)
 stop("conversion of lists to categorical is not supported")</pre>
```

The users can always be instructed in the method's documentation that they are responsible for converting lists to another type prior to a call to **as.categorical**.

**Example 10.4** *The default method deals with logical vectors perfectly fine:* 

```
as.categorical(c(TRUE, FALSE, NA, NA, FALSE)) # as.categorical.default
[1] "TRUE" "FALSE" NA NA "FALSE"
Categories: FALSE, TRUE
```

However, we might still want to introduce its specialised version. This is because we know a slightly more efficient algorithm (and we have nothing better to do) based on the fact that FALSE and TRUE converted to numeric yield 0 and 1, respectively:

```
as.categorical.logical <- function(x, ...)
{
 if (!is.logical(x))
 x <- as.logical(x) # or maybe stopifnot(is.logical(x))?
 structure(
 x + 1, # only 1, 2, and NAs will be generated
 class="categorical",
 levels=c("FALSE", "TRUE")
)
}</pre>
```

It spawns the same result as the default method but is slightly faster.

```
as.categorical(c(TRUE, FALSE, NA, NA, FALSE)) # as.categorical.logical
[1] "TRUE" "FALSE" NA NA "FALSE"
Categories: FALSE, TRUE
```

We performed some argument consolidation at the beginning because a user is always able to call

a method directly on an R object of any kind (which is a good thing; see Section 10.2.4). In other words, there is no guarantee that the argument x must be of type logical.

#### 10.2.3 Built-in generics

Many<sup>9</sup> functions and operators we have introduced so far are, in fact, S3 generics: print, head, `[`, `[[`, `[<-`, `[[<-`, length, `+`, `<=`, is.numeric, as.numeric, is. character, as.character, as.list, round, log, sum, rep, c, and na.omit, to name a few.

**Example 10.5** Let us overload the **as.character** method. The default one does not make much sense for the objects of our custom type:

```
as.character(x)
[1] "1" "3" "2" "1" "1" "3"
```

So:

```
as.character.categorical <- function(x, ...)
attr(x, "levels")[unclass(x)]</pre>
```

And now:

```
as.character(x)
[1] "a" "c" "b" "a" "a" "c"
```

**Exercise 10.6** Overload the **unique** and **rep** methods for objects of the class categorical.

**Example 10.7** New types ought to be designed carefully. For instance, if we forget to overload the to-numeric converter, some users might be puzzled  $^{10}$  when they see:

```
(x <- as.categorical(c(4, 9, 100, 9, 9, 100, 42, 666, 4)))
[1] "4" "9" "100" "9" "9" "100" "42" "666" "4"
Categories: 100, 4, 42, 666, 9
as.double(x) # synonym: as.numeric(x); here, it calls as.double.default(x)
[1] 2 5 1 5 5 1 3 4 2
```

<sup>&</sup>lt;sup>9</sup> Generating the list of all S3 generics is somewhat tricky but at least the internal ones are enumerated in help("InternalMethods") and help("groupGeneric"); compare `.knownS3Generics` and also `. S3\_methods\_table`. Some of them do not even call UseMethod explicitly; they dispatch internally at the Clanguage level. This is quite unfortunate as it decreases transparency. Instead of simply inspecting a function's source code (compare, e.g., cbind), we need to look this information up in the documentation. Also, methods may be hardcoded internally, and thus be unoverloadable. However, sometimes these design choices can be defended because they improve execution speed or memory consumption.

<sup>&</sup>lt;sup>10</sup> It is a different story if we *really* want this behaviour. Provided that we document it *thoroughly* (see how **help**("factor") discusses the behaviour of a to-numeric conversion), we can start holding the users responsible for their feeling confused (those who have experience in teaching others will certainly agree how complex this matter is). Remember that we can never make an API fully foolproof and that there will always be someone to challenge/stress-test our ideas. Bad design is always wrong, but being overprotective or too defensive also has its cons. We should maintain our audience wisely. Users of open-source software are not our *clients*. We do not work *for* them. We are in this *together*.

Hence, we might want to introduce a new method:

```
as.double.categorical <- function(x, ...) # not: as.numeric.categorical
{
 # actually: as.double.default(as.character.categorical(x))
 as.double(as.character(x))
}</pre>
```

It now yields:

```
as.double(x) # or as.numeric(x); calls as.double.categorical(x)
[1] 4 9 100 9 9 100 42 666 4
```

**Note** We can still use **unclass** to fetch the codes:

```
unclass(x)
[1] 2 5 1 5 5 1 3 4 2
attr(,"levels")
[1] "100" "4" "42" "666" "9"
```

It is because the above returns a class-free object, which is now guaranteed to be processed by the default methods (**print**, subsetting, **as.character**, etc.).

Exercise 10.8 What would happen if we used as.numeric instead of unclass in print. categorical and as.character.categorical?

**Exercise 10.9** Update the above methods so that we can also create named objects of the class categorical (i.e., equipped with the names attribute).

**Exercise 10.10** The levels of x are sorted lexicographically, not numerically. Introduce a single method that would make the above code (when rerun without any alterations) generate a more natural result.

## 10.2.4 First-argument dispatch and calling S3 methods directly

With S3, dispatching is most often done based on the class of only one  $^{11}$  argument: by default, the first one from the parameter list.

For example, the **c** function is a generic that dispatches on the first argument's class. Let us overload it for categorical objects. In other words, we will create a function to be called by the generic when it is invoked on a series of objects whose first element is of the said class.

<sup>&</sup>lt;sup>11</sup> There are many exceptions to this rule. They were made for the (debatable) sake of the R users' convenience. In particular, in Section 12.1.2 we mention that **cbind** and **rbind** will dispatch to the data. frame method if at least one argument is a data frame (and others are unclassed). Binary operators consider the type of both operands; see Section 10.2.6. Furthermore, it is worth noting that the S4 class system (Section 10.5) allows for dispatching based on the classes many arguments.

```
c.categorical <- function(...)
 as.categorical(
 unlist(
 lapply(list(...), as.character)
)
)</pre>
```

It converts each argument to a character vector, relying on the generic **as.character** to take care of the details. It works because **unlist** converts a list of such atomic vectors to a single sequence of strings.

Calling **c** with the first argument of the class categorical dispatches to the above method:

```
x <- c(9, 5, 7, 7, 2)
xc <- as.categorical(x)
c(xc, x) # c.categorical
[1] "9" "5" "7" "7" "2" "9" "5" "7" "7" "2"
Categories: 2, 5, 7, 9</pre>
```

However, if the first argument is, say, unclassed, the default method will be consulted:

```
c(x, xc) # default c
[1] 9 5 7 7 2 4 2 3 3 1
```

It ignored the class attribute and saw xc as it is, a bareboned numeric vector:

```
`attributes<-`(xc, NULL) # the underlying codes
[1] 4 2 3 3 1
```

It is not a bug. It is a well-documented (and now explained) behaviour. After all, compound types (classed objects) are emulated through the basic ones.

**Important** In most cases, S3 methods can be called directly to get the desired outcome:

```
c.categorical(x, xc) # force a call to the specific method
[1] "9" "5" "7" "7" "2" "9" "5" "7" "7" "2"
Categories: 2, 5, 7, 9
```

We said in most cases because methods can be:

• hardcoded at the C language level (e.g., there is no c.default defined at all<sup>12</sup>),

<sup>&</sup>lt;sup>12</sup> Dispatching to internal methods can also be done... internally. For instance, overloading `<.character` (or Compare.character; see below) will have no effect unless the base `<` is replaced with a custom one that makes an explicit call to UseMethod. Most often, we can expect that the built-in types (e.g., atomic vectors), factors, data frames, and matrices and other arrays might be treated specially.

- - hidden (defined in a package's namespace but not exported; Section 16.3.6),
  - overloaded as a group; see Section 10.2.6 and help("groupGeneric").

**Example 10.11** Just for fun, let us find a partition of the iris dataset into three clusters using the k-means algorithm:

```
res <- kmeans(iris[-5], centers=3, nstart=10)
print(res)
K-means clustering with 3 clusters of sizes 50, 62, 38
##
Cluster means:
Sepal.Length Sepal.Width Petal.Length Petal.Width
1
 5.0060 3.4280 1.4620 0.2460
2
 5.9016
 2.7484
 4.3935
 1.4339
3
 6.8500
 3.0737
 5.7421
 2.0711
##
Clustering vector:
[reached getOption("max.print") -- omitted 51 entries]
##
Within cluster sum of squares by cluster:
[1] 15.151 39.821 23.879
(between_SS / total_SS = 88.4 %)
##
Available components:
##
[1] "cluster"
 "centers"
 "totss"
 "withinss"
[5] "tot.withinss" "betweenss" "size"
 "iter"
[9] "ifault"
```

The above is an object of the class:

```
class(res)
[1] "kmeans"
```

which, in fact, is a:

```
typeof(res)
[1] "list"
```

The underlying list looks like:

```
unclass(res)
$cluster
(continues on next page)
```

```
[reached getOption("max.print") -- omitted 51 entries]
##
$centers
 Sepal.Length Sepal.Width Petal.Length Petal.Width
1
 5.0060
 3.4280
 1.4620
 0.2460
 5.9016
 2.7484
 4.3935
 1.4339
2
3
 6.8500
 3.0737
 5.7421
 2.0711
##
Stotss
[1] 681.37
##
$withinss
[1] 15.151 39.821 23.879
##
$tot.withinss
[1] 78.851
##
$betweenss
[1] 602.52
##
$size
[1] 50 62 38
##
Siter
[1] 2
##
$ifault
[1] 0
```

We already know that res was displayed in a fancy way only because there is a **print** method overloaded for objects of the kmeans class.

But is there?

```
print.kmeans
Error in eval(expr, envir, enclos): object 'print.kmeans' not found
```

Even though the method is hidden (internal) in the stats package's namespace, from Section 16.3.6 we will learn that it can be accessed by calling getS3method("print", "kmeans") or referring to stats:::print.kmeans (note the triple colon).

#### 10.2.5 Multi-class-ness

The class attribute can be instantiated as a character vector of any length. For example:

```
(t1 <- Sys.time())
[1] "2023-06-28 15:20:49 AEST"
(t2 <- strptime("2021-08-15T12:59:59+1000", "%Y-%m-%dT%H:%M:%S%z"))
[1] "2021-08-15 12:59:59"
```

Let us inspect the classes of these two objects:

```
class(t1)
[1] "POSIXct" "POSIXt"
class(t2)
[1] "POSIXlt" "POSIXt"
```

Section 10.3.1 will discuss date-time classes in more detail. It will highlight that the former is represented as a numeric vector, while the latter is a list. Thus, these two should primarily be seen as instances of two distinct types.

However, both of them have a lot in common. Hence, it was a wise design choice to allow them to be seen also as the representatives of the same generic category of POSIX time objects.

**Important** When calling a generic function<sup>13</sup> **f** on an object x of the classes<sup>14</sup> class1, class2, ..., classK (in this order), UseMethod(f, x) dispatches to the method determined as follows:

- 1. if **f.class1** is available 15, call it;
- 2. otherwise, if **f.class2** is available, call this one;
- 3. ...;
- 4. otherwise, if **f.classK** is available, invoke it;
- 5. otherwise, refer to the fallback **f.default**.

**Example 10.12** There is a method **diff** for objects of the class POSIXt that carries a statement:

```
r <- if (inherits(x, "POSIXIt")) as.POSIXct(x) else x</pre>
```

This way, we can process both POSIXct and POSIXlt instances using the same procedure.

Let us see no magic in this simple scheme. It is nothing more than what we described

<sup>&</sup>lt;sup>13</sup> The case of binary operators is handled differently; see Section 10.2.6.

<sup>&</sup>lt;sup>14</sup> UseMethod dispatches on the implicit class as determined by the class function. Note that the class attribute does not necessarily have to be set in order for class to return a sensible answer.

<sup>&</sup>lt;sup>15</sup> For more details on S3 method lookup, see Section 16.3.6.

above: a way to determine which method to call for a particular R object. It can be used as a mechanism to mimic the idea of inheritance in object-orientated programming languages. However, the S3 system does not allow for defining classes in any formal manner.

For example, we cannot say that objects of the class POSIXct inherit from POSIXt. Neither can we say that each object of the class POSIXct is also an instance of POSIXt. The class attribute can still be set arbitrarily on a per-object basis. We can create ones whose class is simply POSIXct (without the POSIXt part) or even c("POSIXt", "POSIXct") (in this order).

**Note** In any method, it is possible to call the method corresponding to the next class by calling **NextMethod**.

For instance, if we are in **f.class1**, a call to **NextMethod**(f) will try invoking **f.class2**. If such a method does not exist, further methods in the search chain will be probed, falling back to the default method if necessary. We will give an illustration later.

#### 10.2.6 Operator overloading

Operators are ordinary functions (Section 9.3.5). Even though what follows can partially be implied by what we have said above, as usual in R, there will be some oddities.

For example, let us overload the index operator for objects of the class categorical. Looking at **help**("["), we see that the default method has two arguments: x (the categorical object being sliced) and i (the indexer). Ours will have the same interface then:

```
`[.categorical` <- function(x, i)
{
 structure(
 unclass(x)[i], # `[`(unclass(x), i)
 class="categorical",
 levels=attr(x, "levels") # the same levels as input
)
}</pre>
```

The default S3 method, `[.default`, is hardcoded at the C language level and we cannot refer to it directly. This is why we called unclass instead. Alternatively, we can also invoke NextMethod:

```
levels=attr(x, "levels") # the same levels as input
)
}
```

We can also introduce the replacement version of this operator:

```
`[<-.categorical` <- function(x, i, value)
{
 levels <- attr(x, "levels")</pre>
 value <- match(value, levels) # integer codes corresponding to levels
 structure(
 NextMethod("[<-"), # call default method, passing `x`, `i`, `values`
 class="categorical",
 levels=levels # same levels as input
)
 # # or, equivalently:
 # structure(
 `[<-`(unclass(x), i, value=match(value, attr(x, "levels"))),
 class="categorical",
 levels=attr(x, "levels")
 #)
}
```

#### Testing:

```
x <- as.categorical(c(3, 6, 4, NA, 9, 9, 6, NA, 3))
x[1:4]
[1] "3" "6" "4" NA
Categories: 3, 4, 6, 9
x[1:4] <- c("6", "7")
print(x)
[1] "6" NA "6" NA "9" "9" "6" NA "3"
Categories: 3, 4, 6, 9
```

Notice how we handled the case of nonexistent levels and that the recycling rule has been automagically inherited (amongst other features) from the default index operator.

**Exercise 10.13** Do these two operators preserve the names attribute of x? Is indexing with negative integers or logical vectors supported as well? Why is that/is that not the case?

Furthermore, let us overload the `==` operator. Assume<sup>16</sup> that we would like two cat-

<sup>&</sup>lt;sup>16</sup> There are, of course, many possible ways to implement the `==` operator for the discussed objects. For instance, it may return either a single TRUE or FALSE depending on if two objects are identical (although probably overloading all.equal would be a better idea). We could also compare the corresponding underlying integer codes instead of the labels, etc.

egorical objects to be compared based on the actual labels they encode, in an elementwise manner:

```
`==.categorical` <- function(e1, e2)
 as.character(e1) == as.character(e2)</pre>
```

We are feeling lucky: by not performing any type checking, we rely on the particular **as.character** methods corresponding to the types of e1 and e2. Also, assuming that **as.character** always<sup>17</sup> returns a character object, we dispatch to the default method for `==` (which handles atomic vectors).

Some examples:

```
as.categorical(c(1, 3, 5, 1)) == as.categorical(c(1, 3, 1, 1))
[1] TRUE TRUE FALSE TRUE
as.categorical(c(1, 3, 5, 1)) == c(1, 3, 1, 1)
[1] TRUE TRUE FALSE TRUE
c(1, 3, 5, 1) == as.categorical(c(1, 3, 1, 1))
[1] TRUE TRUE FALSE TRUE
```

**Important** In the case of binary operators, dispatching is done based on the classes of both arguments. In all three example calls above, we call `==.categorical`, regardless of whether the classed object is the first or the second operand.

If two operands are classed, and different methods are overloaded for both, a warning will be generated, and the default internal method will be called.

```
`==.A` <- function(e1, e2) "A"

`==.B` <- function(e1, e2) "B"

structure(c(1, 2, 3), class="A") == structure(c(2, NA, 3), class="B")

Warning: Incompatible methods ("==.A", "==.B") for "=="

[1] FALSE NA TRUE</pre>
```

**Note** (\*) By creating a single **Ops** method, we can define the meaning of all binary operators at once.

<sup>&</sup>lt;sup>17</sup> Which, of course, does not have to be the case; it is merely an assumption based on our belief in the common sense of other developers.

```
NextMethod(.Generic) # dispatch to the default method (for character)
}
as.categorical(c(1, 3, 5, 1)) > c(1, 2, 4, 2)
[1] FALSE TRUE TRUE FALSE
```

Here, `.Generic` is a variable representing the name of the operator (generic) being invoked: see Section 16.3.6.

Other group generics are: Summary (including functions such as min, sum, and all), Math (abs, log, round, etc.), and Complex (e.g., Re, Im); see help("groupGeneric") for more details.

Sometimes we must rely on registerS3method to force R to recognise a custom method related to such generics.

#### Common built-in S3 classes

Let us discuss a few noteworthy classes, including those representing date-time information and factors (ordered or not).

Classes representing tabular data will be dealt with in separate parts, owing to their importance and ubiquity. Namely, matrices and other arrays are covered in Chapter 11, and data frames are discussed in Chapter 12.

Inspecting other<sup>18</sup> interesting compound types is left as a simple exercise for the studious reader.

#### 10.3.1 Date, time, etc.

The Date class represents... dates (calendar ones, not fruits).

```
(x <- c(Sys.Date(), as.Date(c("1969-12-31", "1970-01-01", "2023-02-29"))))
[1] "2023-06-28" "1969-12-31" "1970-01-01" NA
class(x)
[1] "Date"
```

Complex types are built on basic ones. Underneath, what we deal with here is:

```
typeof(x)
[1] "double"
 (continues on next page)
```

<sup>&</sup>lt;sup>18</sup> unique(.S3\_methods\_table[, 2]) approximates the list of available classes.

```
unclass(x)
[1] 19536 -1 0 NA
```

which is the number of days since the *UNIX epoch*, 1970-01-01T00:00:00+0000 (midnight GMT/UTC).

The POSIXct (calendar time) class represents date-time objects:

```
(x <- Sys.time())
[1] "2023-06-28 15:20:49 AEST"
class(x)
[1] "POSIXct" "POSIXt"
typeof(x)
[1] "double"
unclass(x)
[1] 1687929650</pre>
```

Underneath, it is the number of seconds since the UNIX epoch. By default, whilst printing, the current default timezone is used (see **Sys.timezone**). However, such objects can be equipped with the tzone attribute.

```
structure(1, class=c("POSIXct", "POSIXt")) # using current default timezone
[1] "1970-01-01 10:00:01 AEST"
structure(1, class=c("POSIXct", "POSIXt"), tzone="UTC")
[1] "1970-01-01 00:00:01 UTC"
```

In both cases, the time is 1 second after the beginning of the UNIX epoch. On the author's PC, the former is displayed in the current local timezone, though.

**Exercise 10.14** Use **ISOdatetime** to inspect how midnights are displayed in different timezones.

The POSIXIt (local time) class is represented using a list of atomic vectors<sup>19</sup>.

<sup>19</sup> Which was inspired by struct tmin C's <time.h>.

```
$ mday : int [1:2] 1 31
##
$ mon : int [1:2] 0 11
 $ year : Named int [1:2] 70 130
 ..- attr(*, "names")= chr [1:2] "a" "b"
##
$ wday : int [1:2] 4 2
$ vday : int [1:2] 0 364
$ isdst : int [1:2] 0 1
$ zone : chr [1:2] "AEST" "AEDT"
$ gmtoff: int [1:2] NA NA
- attr(*, "tzone")= chr [1:3] "" "AEST" "AEDT"
- attr(*, "balanced")= logi TRUE
```

**Exercise 10.15** Read about the meaning of each named element, especially mon and year; see help("DateTimeClasses").

The manual states that POSIXIt is supposedly closer to human-readable forms than POSIXct, but it is a matter of taste. Some R functions return the former, and other output the latter type.

**Exercise 10.16** The two main functions for date formatting and parsing, strftime and strp**time**, use special field formatters (similar to **sprintf**). Read about them in the R manual. What type of inputs do they accept? What outputs do they produce?

There are several methods overloaded for objects of the said classes. In fact, the first call in this section already involved the use of **c.Date**.

**Exercise 10.17** Play around with the overloaded versions of seq. rep, and as.character.

A specific number of days or seconds can be added to or subtracted from a date or time, respectively. However, `-` (see also diff) can also be applied on two date-time objects, which yields an object of the class difftime.

```
Sys.Date() - (Sys.Date() - 1)
Time difference of 1 days
Sys.time() - (Sys.time() - 1)
Time difference of 1 secs
```

**Exercise 10.18** Check out how objects of the class difftime are internally represented.

Applying other arithmetic operations on date-time objects raises an error. Because date-time objects are just numbers, they can be compared to each other using binary operators<sup>20</sup>. Also, methods such as **sort** and **order**<sup>21</sup> could be applied on them.

Exercise 10.19 Check out the stringx package, which replaces the base R date-time processing functions with their more portable counterparts.

<sup>&</sup>lt;sup>20</sup> The overloaded group generic **0ps** prevents us from adding or multiplying two dates and defines the meaning of the relational operators. As an exercise, check out its source code.

<sup>&</sup>lt;sup>21</sup> See an exercise below on the use of xtfrm.

**Exercise 10.20** *proc. time* can be used to measure the time to execute a given expression:

```
t0 <- proc.time() # timer start
... to do - something time-consuming ...
sum(runif(1e7)) # whatever, just testing
[1] 4999488
print(proc.time() - t0) # elapsed time
user system elapsed
0.229 0.029 0.258</pre>
```

The function returns an object of the class proc time. Inspect how it is represented internally.

#### 10.3.2 Factors

The factor class is often used to represent qualitative data, e.g., species, groups, types. In fact, categorical (the example class that we played with above) was inspired by the built-in factor.

```
(x <- c("spam", "spam", "bacon", "sausage", "spam", "bacon"))
[1] "spam" "spam" "bacon" "sausage" "spam" "bacon"
(f <- factor(x))
[1] spam spam bacon sausage spam bacon
Levels: bacon sausage spam</pre>
```

Note how factors are printed. There are no double quote characters around the labels. The list of levels is given at the end.

Internally, such objects are represented as integer vectors (Section 6.4.1) with elements between 1 and k. They are equipped with the special (as in Section 4.4.3) levels attribute, which is a character vector of length  $k^{22}$ .

```
class(f)
[1] "factor"
typeof(f)
[1] "integer"
unclass(f)
[1] 3 3 1 2 3 1
attr(, "levels")
[1] "bacon" "sausage" "spam"
attr(f, "levels") # also: levels(f)
[1] "bacon" "sausage" "spam"
```

<sup>&</sup>lt;sup>22</sup> [67] states: Factors are currently implemented using an integer array to specify the actual levels and a second array of names that are mapped to the integers. Rather unfortunately users often make use of the implementation in order to make some calculations easier. This, however, is an implementation issue and is not guaranteed to hold in all implementations of R. Still, fortunately, this has been a de facto standard for factors for a very long time.

Factors are often used instead of character vectors defined over a small number of unique labels<sup>23</sup>, where there is a need to manipulate their levels conveniently.

```
attr(f, "levels") <- c("a", "b", "c") # also levels(f) <- c(....new...)
print(f)
[1] c c a b c a
Levels: a b c</pre>
```

The underlying integer codes remain the same.

Certain operations on vectors of small integers are relatively easy to express, especially those concerning element grouping: splitting, counting, and plotting (e.g., Figure 13.17). It is because the integer codes can naturally be used whilst indexing other vectors. Section 5.4 mentioned a few functions related to this, such as match, split, findInterval, and tabulate. Specifically, the latter can be implemented like "for each i, increase count[factor\_codes[i]] by one".

**Exercise 10.21** Study the source code of the **factor** function. Note the use of **as.character**, **unique**, **order**, and **match**.

**Exercise 10.22** Implement a simplified version of **table** based on **tabulate**. It should work for objects of the class factor and return a named numeric vector.

**Exercise 10.23** Implement a version of cut based on findInterval.

**Important** The **as.numeric** method has not been overloaded for factors. Therefore, when we call the generic, the default method is used: it returns the underlying integer codes as-is. This can surprise unaware users when they play with factors representing integer numbers:

```
(g <- factor(c(11, 15, 16, 11, 13, 4, 15))) # converts numbers to strings
[1] 11 15 16 11 13 4 15
Levels: 4 11 13 15 16
as.numeric(g) # the underlying codes
[1] 2 4 5 2 3 1 4
as.numeric(as.character(g)) # to get the numbers encoded
[1] 11 15 16 11 13 4 15
```

Alas, support for factors is often hardcoded at the C language level. From the end user perspective, it makes this class behave less predictably. In particular, the manual overloading of certain methods for factor objects might have no effect.

**Important** If f is a factor, then x[f] does not behave like x[as.character(f)], i.e., it is not indexing by labels using the names attribute. Instead, we get x[as.numeric(f)]; the underlying codes determine the positions.

<sup>&</sup>lt;sup>23</sup> Recall that there is a global (internal) string cache. Hence, having many duplicated strings is not a burden on the computer's memory.

```
h <- factor(c("a", "b", "a", "c", "a", "c"))
levels(h)[h] # the same as c("a", "b", "c")[c(1, 2, 1, 3, 1, 3)]
[1] "a" "b" "a" "c"
c(b="x", c="y", a="z")[h] # names are not used whilst indexing
b c b a b a
"x" "y" "x" "z" "x" "z"
c(b="x", c="y", a="z")[as.character(h)] # names are used now
a b a c a c
"z" "x" "z" "y" "z" "y"</pre>
```

More often than not, indexing by factors will happen "accidentally"<sup>24</sup>, leaving us slightly puzzled. In particular, factors look much like character vectors when they are carried in data frames:

```
(df <- data.frame(A=c("x", "y", "z"), B=factor(c("x", "y", "z"))))
A B
1 x x
2 y y
3 z z
class(df[["A"]])
[1] "character"
class(df[["B"]])
[1] "factor"</pre>
```

**Important** Be careful when combining factors and not-factors:

```
x <- factor(c("A", "B", "A"))
c(x, "C")
[1] "1" "2" "1" "C"
c(x, factor("C"))
[1] A B A C
Levels: A B C</pre>
```

**Exercise 10.24** When subsetting a factor object, the result will inherit the levels attribute in its entirety:

```
f[c(1, 2)] # drop=FALSE
[1] c c
Levels: a b c
```

<sup>&</sup>lt;sup>24</sup> (\*) Up until R 4.0, many functions (including data.frame and read.csv) had the stringsAsFactors option set to TRUE; see help("options"). It resulted in all character vectors' being automatically converted to factors, e.g., when creating data frames (compare Section 12.1.5). Luckily, this is no longer the case. However, factor objects can still be encountered; for instance, check the class of iris[["Species"]].

However:

```
f[c(1, 2), drop=TRUE]
[1] c c
Levels: c
```

Implement your version of the **droplevels** function, which removes the unused attributes.

**Exercise 10.25** The replacement version of the index operator does not automatically add new levels to the modified object:

```
x <- factor(c("A", "B", "A"))
`[<-`(x, 4, value="C") # like in x[4] <- "C"
Warning in `[<-.factor`(x, 4, value = "C"): invalid factor level, NA
generated
[1] A B A <NA>
Levels: A B
```

Implement a version of `[<-.factor` that has such a capability.

#### 10.3.3 Ordered factors

When creating factors, we can enforce a particular ordering and the number of levels:

```
x <- c("spam", "spam", "bacon", "sausage", "spam", "bacon")
factor(x, levels=c("eggs", "bacon", "sausage", "spam"))
[1] spam spam bacon sausage spam bacon
Levels: eggs bacon sausage spam</pre>
```

If we want the arrangement of the levels to define a linear ordering relation over the set of labels, we can call:

```
(f <- factor(x, levels=c("eggs", "bacon", "sausage", "spam"), ordered=TRUE))
[1] spam spam bacon sausage spam bacon
Levels: eggs < bacon < sausage < spam
class(f)
[1] "ordered" "factor"</pre>
```

It yields an ordered factor, which enables comparisons like:

```
f[f >= "bacon"] # what's not worse than bacon?
[1] spam spam bacon sausage spam bacon
Levels: eggs < bacon < sausage < spam</pre>
```

How is that possible? Well, based on information provided in this chapter, it will come as no surprise that it is because... someone has created a relational operator for objects of the class ordered.

#### 10.3.4 Formulae (\*)

Formulae are created using the `~` operator. Some R users employ them to specify widely-conceived *statistical models* in functions such as lm (e.g., linear regression), glm (generalised linear models like logistic regression etc.), aov (analysis of variance), wilcox.test (the two-sample Mann–Whitney–Wilcoxon test), aggregate (computing aggregates within data groups), boxplot (box-and-whisker plots for a variable split by a combination of factors), or plot (scatter plots); see also Chapter 11 of [57]. For instance, formulae can be used to describe symbolic relationships such as:

- "y as a linear combination of x1, x2, and x3",
- "y grouped/split by a combination of x1 and x2",

where y, x1, etc., are, for example, column names in a data frame.

Formulae are interpreted by the corresponding functions, and not the R language itself. Thus, programmers are free to assign them any meaning. As their syntax is quite esoteric, beginners might find them confusing. Hence, we will postpone discussing them until Section 17.6. Luckily, the use of formulae can usually quite easily be avoided<sup>25</sup>.

## 10.4 (Over)using the forward pipe operator, `|>` (\*)

The OOP paradigm is utile when we wish to define a new data type, perhaps even a hierarchy of types. Many development teams find it an efficient tool to organise larger pieces of software. However, in the data science and numerical computing domains, more often than not, we are the *consumers* of object orientation rather than class *designers*.

Thanks to the S3 method dispatch mechanism, our language is easily extensible. Something that mimics a new data type can easily be introduced. Most importantly, methods can be added or removed during runtime, e.g., when importing external packages.

However, R is still a functional programming language, where functions are not just first-class citizens: they are privileged.

In functional programming, the emphasis is on operations (verbs), not data (nouns). It leads to a very readable syntax. For example, assuming that **square**, x, and y are sensibly defined, the mean squared difference can be written as:

mean(square(x-y)) # read: mean of squares of differences

<sup>&</sup>lt;sup>25</sup> For example, lm.fit can be used instead of lm. It is slightly more difficult to learn, but it has the added benefit of ensuring the user knows that the emergence of all model variables is not magical (especially the nonlinear/mixed effect terms).

**Example 10.26** Base R is extremely flexible. We can introduce new vocabulary as we please. In Section 12.3.7, we will study an example where we define:

- **group\_by** (a function that splits a data frame with respect to a combination of levels in given named columns and returns a list of data frames with class list\_dfs),
- aggregate.list\_dfs (which applies an aggregation function on every column of all data frames in a given list), and
- mean.list\_dfs (a specialised version of the former that calls mean).

The specifics do not matter now. Let us just consider the notation we use when the operations are chained:

The functional syntax is very reader-centric. We compute the mean in groups defined by Species in a subset of the iris data frame. All verbs appear on the left side of the expression, with the final (the most important?) operation being listed first.

By the way, self-explanatory variable names and rich comments are priceless.

Nonetheless, when implementing more complex data processing pipelines, *programmers* think in different categories: "first, we need to do this, then we need to do that, and afterwards...". When they write their ideas down, they have to press Home and End or arrow keys a few times to move the caret to the right places:

```
finally(thereafter(then(first(x))))
```

As we are inherently lazy, we might want to "optimise" our workflow to save a bit of energy.

In more traditional object-orientated programming languages, either the method list is sealed inside<sup>26</sup> the class' definition (like in C++), or peculiar patches must be applied to inject a method (like in Python)<sup>27</sup>. There, it is *the objects* that are *told* what to do. They are treated as black boxes.

Many popular languages rely on message-passing syntax, where operations are

 $<sup>^{26}</sup>$  When methods are parts of particular classes, there can be a lot of duplicated code. Functional OOP can be more developer-friendly as we can provide all methods related to roughly the same functionality in one spot.

<sup>&</sup>lt;sup>27</sup> See also the concept of extension methods in C# or Kotlin and, to some extent, of class inheritance.

propagated (and written) left-to-right instead of inside-out. For instance, obj. method1().method2() might mean "call method1 on obj and then call method2 on the result".

Since R 4.1.0, there is a *pipe operator*<sup>28</sup>, `**|>**`. It is merely syntactic sugar for translating between the message-passing and function-centric notion. In a nutshell, writing:

```
x |> f() |> g(y) |> h()
(x-y) |> square() |> mean()
```

is equivalent, respectively, to:

```
h(g(f(x), y))
mean(square(x-y))
```

This syntax is developer-centric. It emphasises the order in which the operations are executed, something that could always be achieved with the function-centric form and perhaps a few auxiliary variables.

The placeholder `\_` can be used on the right side of the pipe operator (only once) to indicate that the left side must be matched with a specific *named* argument of the function to be called. Otherwise, the left side is always passed as the first argument.

Therefore, the two following expressions are equivalent:

```
x |> median() |> `-`(e1=x, e2=_) |> abs() |> median()
median(abs(x-median(x)))
```

**Example 10.27** The pipe operator version of the above ir is aggregation exercise would look like:

```
iris_subset |> group_by("Species") |> mean()
```

Expressions on the right side of the pipe operator must always be proper calls. Therefore, the use of round brackets is obligatory. Thus, when passing anonymous functions, we must write:

```
runif(10) |> (function(x) mean((x-mean(x))^2))() # note the "()" at the end
[1] 0.078184
```

Peculiarly, in R 4.1.0, a "shorthand" notation for creating functions was introduced. We can save seven keystrokes and scribble " $\setminus(\ldots)$  expr" instead of "function(...) expr".

```
runif(10) |> (\(x) mean((x-mean(x))^2))() # again: "()" at the end
[1] 0.078184
```

<sup>&</sup>lt;sup>28</sup> It was inspired by `|` in Bash and `|-@` in F# and Julia (which are part of the language specification). Also, there is a `%-%` operator (and related ones) in the R package magrittr.

There is nothing that cannot be achieved without the pipe operator. As this book is minimalist by design, we refrain ourselves from using it.

**Note** When writing code interactively, we may sometimes benefit from using the rightward `->` operator. Suffice it to say that "name <- value" and "value -> name" are synonymous.

This way, we can type some lengthy code, store the result in an intermediate variable, and then continue in the next line (possibly referring to that auxiliary value more than once). For instance:

```
runif(10) -> .
mean((.-mean(.))^2)
[1] 0.078184
```

Recall that `.` is as valid a variable name as any other one. Another example:

## 10.5 S4 classes (\*)

The S3-style OOP is based on a brilliantly simple idea: calling a generic f(x) dispatches automatically to a method  $f.class_of_x(x)$  or f.default(x) in the case where the former does not exist. Naturally, S3 has the following inherent limitations:

- classes cannot be formally defined; the class attribute may be assigned arbitrarily to any object<sup>29</sup>,
- argument dispatch is performed only  $^{30}$  with regard to one data type  $^{31}$ .

<sup>&</sup>lt;sup>29</sup> A partial solution to this could involve defining a method like validate.class\_name, which is called frequently and which checks whether a given object enjoys a few desirable constraints.

<sup>&</sup>lt;sup>30</sup> Certain functions implement ad hoc workarounds (see, e.g., cbind, which dispatches to cbind.data. frame if one argument is a data frame and the remaining ones are vectors or matrices). Also, we said in the previous chapter that binary operators consider the classes of both operands.

<sup>&</sup>lt;sup>31</sup> Hypothetically, we can imagine an OOP system relying on methods named like method.class\_name1. class\_name2 where dispatching is based on two argument types. This would be beautiful, but it is not the case in R.

In most cases, and with an appropriate level of mindfulness, they are not a problem at all. However, it is a typical condition of programmers who come to our world from more mainstream languages (e.g., C++ or Java; yours truly included) until they appreciate the true beauty of R's being somewhat different. Before they fully develop such an acquired taste, though, they grow restless as "R is has no real OOP because it lacks polymorphism, encapsulation, formal inheritance, and so on, and something must be done about it!". The truth is that it had not had to, but with high probability, it would have anyway in one way or another.

And so the fourth version of the S language was introduced in 1998 (see [9]). It brought a new object-orientated system, which we are used to referring to as S4. Its R version is defined by the **methods** package. Below we discuss it briefly. For more details, see **help**("Classes Details") and **help**("Methods Details") as well as [10] and [11].

**Note** (\*) S4 was loosely inspired by the Common Lisp Object System (with its defclass, defmethod, etc.; see, e.g., [20]). In the current author's opinion, the S4 system is somewhat of an afterthought. Due to appendages like this, R seems like a patchwork language. Suffice it to say that it was not the last attempt to introduce a "real" OOP in the overall functional R: the story will resume in Section 16.1.5.

The main issue with all the supplementary OOP approaches is that each of them is parallel to S3 which never lost its popularity and is still in the very core of our language. We are thus covering them only for the sake of completeness for the readers might come across such objects. In particular, below we explain the meaning of a notation like x@slot. Moreover, in Section 11.4.7 we mention the Matrix class which is perhaps the most prominent showcase of S4.

Nonetheless, the current author advises taking with a pinch of salt statements such as for new projects, it is recommended to use the more flexible and robust S4 scheme provided in the **methods** package mentioned in **help**("UseMethod").

## 10.5.1 Defining S4 classes

An S4 class can be formally registered through a call to **setClass**. For instance:

```
library("methods") # in the case where it is not auto-loaded
setClass("qualitative", slots=c(data="integer", levels="character"))
```

We defined a class named qualitative (similarity to our own categorical and the built-in factor S3 classes is intended). It has two slots: data and levels being integer and character vectors, respectively. This notation is already quite peculiar. There is no assignment suggesting that we have introduced something novel.

An object of the above class can be instantiated by calling new:

```
An object of class "qualitative"
Slot "data":
[1] 1 2 2 1 1
##
Slot "levels":
[1] "a" "b"
```

That z is of this class can be verified by calling is.

```
is(z, "qualitative")
[1] TRUE
class(z) # also: attr(z, "class")
[1] "qualitative"
attr(,"package")
[1] ".GlobalEnv"
```

**Important** A few R packages import the **methods** package only to get access the handy **is** function. It does not mean they are defining new S4 classes.

**Note** S4 objects are marked as being of the following basic type:

```
typeof(z)
[1] "54"
```

See Section 1.12 of [66] for technical details on how they are internally represented. In particular, in our case, all the slots are simply stored as object attributes:

```
attributes(z)
$data
[1] 1 2 2 1 1
##
$levels
[1] "a" "b"
##
$class
[1] "qualitative"
attr(,"package")
[1] ".GlobalEnv"
```

#### 10.5.2 Accessing slots

Reading or writing slot contents can be done via the `@` operator and the **slot** function or their replacement versions.

```
z@data # or slot(z, "data")
[1] 1 2 2 1 1
z@levels <- c("A", "B")</pre>
```

**Note** The `@` operator can only be used on S4 objects, and some sanity checks are automatically performed:

```
z@unknown <- "spam"
Error in (function (cl, name, valueClass) : 'unknown' is not a slot in
class "qualitative"
z@data <- "spam"
Error in (function (cl, name, valueClass) : assignment of an object of
class "character" is not valid for @'data' in an object of class
"qualitative"; is(value, "integer") is not TRUE</pre>
```

## 10.5.3 Defining methods

For the S4 counterparts of the S3 generics (Section 10.2), see help("setGeneric"). Luckily, there is a reasonable degree of interoperability between the S3 and S4 systems.

Let us start by introducing a new method for the well-known as.character generic. Instead of defining as.character.qualitative, we need to register a new routine with setMethod.

Testing:

```
as.character(z)
[1] "A" "B" "A" "A"
```

**show** is the S4 counterpart of **print**:

```
setMethod(
(continues on next page)
```

Interestingly, it is involved automatically on a call to **print**:

```
print(z) # calls `show` for `qualitative`
[1] "A" "B" "A" "A"
Categories: A, B
```

Methods that dispatch on the type of multiple arguments are also possible. For example:

```
setMethod(
 "split",
 c(x="ANY", f="qualitative"),
 function (x, f, drop=FALSE, ...)
 split(x, as.character(f), drop=drop, ...)
)
```

It permits the first argument to be of any type (like a default method). Moreover, here is its version tailored for matrices (see Chapter 11).

```
setMethod(
 "split",
 c(x="matrix", f="qualitative"),
 function (x, f, drop=FALSE, ...)
 lapply(
 split(seq_len(NROW(x)), f, drop=drop, ...), # calls the above
 function(i) x[i, , drop=FALSE])
)
```

Some tests:

```
A <- matrix(1:35, nrow=5) # whatever

split(A, z) # matrix, qualitative

$A

[,1] [,2] [,3] [,4] [,5] [,6] [,7]
```

```
[1,] 1 6 11 16 21
 26
 31
[2,] 4 9 14 19 24
 29
 34
[3,]
 5 10 15 20 25
 30 35
##
$B
##
 [,1] [,2] [,3] [,4] [,5] [,6] [,7]
[1,7
 7 12 17 22 27
[2,]
 3
 8
 13
 18 23
 28
 33
split(1:5, z) # ANY, qualitative
$A
[1] 1 4 5
##
$B
[1] 2 3
```

**Exercise 10.28** Overload the `[` operator for the qualitative class.

## 10.5.4 Defining constructors

We can also overload the initialize method, which is automatically called by new:

This constructor yields instances of the class qualitative based on an object coercible to a character vector. For example:

```
w <- new("qualitative", c("a", "c", "a", "d", "c"))
print(w)
[1] "a" "c" "a" "a" "d" "c"
Categories: a, c, d</pre>
```

**Exercise 10.29** Set up a validating method for our class; see **help**("setValidity").

#### 10.5.5 Inheritance

New S4 classes can be derived from existing ones. For instance:

```
setClass("binary", contains="qualitative")
```

It is a child class that inherits all slots from its parent. We can overload its initialisation method:

```
setMethod(
 "initialize",
 "binary",
 function(.0bject, x)
{
 if (!is.logical(x))
 x <- as.logical(x)
 x <- as.character(as.integer(x))
 xu <- c("0", "1")
 .0bject@data <- match(x, xu)
 .0bject levels <- xu
 .0bject
 }
)</pre>
```

Testing:

```
new("binary", c(TRUE, FALSE, TRUE, FALSE, NA, TRUE))
[1] "1" "0" "1" "0" NA "1"
Categories: 0, 1
```

We can still use the **show** method of the parent class.

#### 10.6 Exercises

**Exercise 10.30** *Answer the following questions.* 

- How to display the source code of the default methods for **head** and **tail**?
- Can there be, at the same time, one object of the class **c**("A", "B") and another one of the class **c**("B", "A")?
- If f is a factor, what are the relationships between as.character(f), as.numeric(f), as.character(as.numeric(f)), and as.numeric(as.character(f))?
- If x is a named vector and f is a factor, is x[f] equivalent to x[as.character(f)] or rather x[as.numeric(f)]?

#### Exercise 10.31 A user calls:

```
plot(x, y, col="red", ylim=c(1, max(x)), log="y")
```

where x and y are numeric vectors. Consult **help**("plot") for the meaning of the ylim and log arguments. Was that straightforward?

**Exercise 10.32** *Explain why the two following calls return significantly different results.* 

```
c(Sys.Date(), "1970-01-01")
[1] "2023-06-28" "1970-01-01"
c("1970-01-01", Sys.Date())
[1] "1970-01-01" "19536"
```

Propose a workaround.

**Exercise 10.33** Write methods **head** and **tail** for our example categorical class.

**Exercise 10.34** (\*) Write an R package that defines S3 class categorical. Add a few methods for this class. Note the need to use the S3method directive in the NAMESPACE file; see [63].

**Exercise 10.35** Inspect the result of a call to **binom.test**(79, 100) and to rle(c(1, 1, 1, 4, 3, 3, 3, 3, 3, 2, 2)). Find the methods responsible for such objects' pretty-printing.

**Exercise 10.36** Read more about the connection class. In particular, see the Value section of *help("connections")*.

**Exercise 10.37** Read about the subsetting operators overloaded for the package\_version class; see **help**("numeric\_version").

**Exercise 10.38** There are **xtfrm** methods overloaded for classes such as numeric\_version, difftime, Date, and factor. Find out how they work and where they might be of service (especially in relation to **order** and **sort**; see also Section 12.3.1).

**Exercise 10.39** Give an example where split(x, list(y1, y2)) (with default arguments) will fail to generate the correct result.

**Exercise 10.40** Write a function that determines the mode, i.e., the most frequently occurring value in a given object of the class factor. If the mode is not unique, return a randomly chosen one (each with the same probability).

**Exercise 10.41** Implement your version of the **gl** function.

# Matrices and other arrays

When we equip an atomic or generic vector with the dim attribute, it automatically becomes an object of the S3 class array. In particular, two-dimensional arrays (primary S3 class matrix) allow us to represent *tabular* data where items are aligned into rows and columns:

```
structure(1:6, dim=c(2, 3)) # a matrix with two rows and three columns
[,1] [,2] [,3]
[1,] 1 3 5
[2,] 2 4 6
```

Combined with the fact that there are many functions overloaded for the matrix class, we have just opened up a whole world of new possibilities, which we explore in this chapter.

In particular, we discuss how to perform basic algebraic operations such as matrix multiplication, transpose, finding eigenvalues, and performing various decompositions. We also cover data wrangling operations such as array subsetting and columnand rowwise aggregation.

**Important** Oftentimes, a numeric matrix with n rows and m columns is used to represent n points (samples) in an m-dimensional space (with m numeric features or variables),  $\mathbb{R}^m$ .

Furthermore, in the next chapter, we will introduce data frames: matrix-like objects whose columns can be of any (not necessarily the same) type.

# 11.1 Creating arrays

## 11.1.1 matrix and array

A matrix can be conveniently created using the following function.

```
(A <- matrix(1:6, byrow=TRUE, nrow=2))
[,1] [,2] [,3]
```

```
[1,]
[2,1
 5
```

It converted an atomic vector of length six to a matrix with two rows. The number of columns was determined automatically (ncol=3 could have been passed to get the same result).

**Important** By default, the elements of the input vector are read column by column:

```
matrix(1:6, ncol=3) # byrow=FALSE
 [,1] [,2] [,3]
[1,] 1 3 5
[2,]
 2
 4
```

A matrix can be equipped with an attribute that defines dimension names, being a list of two character vectors of appropriate sizes which label each row and column:

```
matrix(1:6, byrow=TRUE, nrow=2, dimnames=list(c("x", "y"), c("a", "b", "c")))
a b c
x 1 2 3
v 4 5 6
```

Alternatively, to create a matrix, we can use the array function. It requires the number of rows and columns to be specified explicitly.

```
array(1:6, dim=c(2, 3))
 [,1] [,2] [,3]
[1,] 1 3 5
[2,]
 2
 4
```

The elements were consumed in the column-major order.

Arrays of other dimensionalities are also possible. Let us define a one-dimensional array:

```
array(1:6, dim=6)
[1] 1 2 3 4 5 6
```

When printed, it is indistinguishable from an atomic vector (but the class attribute is still set to array).

And now for something completely different: a three-dimensional array of size  $3\times4\times2$ :

```
array(1:24, dim=c(3, 4, 2))
, , 1
```

It can be thought of as two matrices of size  $3 \times 4$  (because how else can we print out a 3D object on a 2D console?).

The array function can be fed with the dimnames argument too. For instance, the above three-dimensional hypertable would require a list of three character vectors of sizes 3, 4, and 2, respectively.

**Exercise 11.1** Verify that 5-dimensional arrays can also be created.

## 11.1.2 Promoting and stacking vectors

We can promote an ordinary vector to a *column vector*, i.e., a matrix with one column, by calling:

```
as.matrix(1:2)

[,1]

[2,] 2

cbind(1:2)

[,1]

[,1]

[2,] 2
```

and to a row vector:

```
t(1:3) # transpose

[,1] [,2] [,3]

[1,] 1 2 3

rbind(1:3)

[,1] [,2] [,3]

[1,] 1 2 3
```

Actually, **cbind** and **rbind** stand for column- and row-bind. They permit multiple vectors and matrices to be stacked one after/below another:

and so forth. Unfortunately, the *generalised* recycling rule is not implemented in full:

```
cbind(1:4, 5:8, cbind(9:10, 11)) # different from cbind(1:4, 5:8, 9:10, 11)
Warning in cbind(1:4, 5:8, cbind(9:10, 11)): number of rows of result is
not a multiple of vector length (arg 1)
[,1] [,2] [,3] [,4]
[1,] 1 5 9 11
[2,] 2 6 10 11
```

Note that the first two arguments were of length four.

## 11.1.3 Simplifying lists

**simplify2array** is an extension of the **unlist** function. Given a list of atomic vectors, each of length one, it will return a flat atomic vector. However, if longer vectors of the same lengths are given, they will be converted to a matrix.

```
simplify2array(list(1, 11, 21)) # each of length one
[1] 1 11 21
simplify2array(list(1:3, 11:13, 21:23, 31:33)) # each of length three
 [,1] [,2] [,3] [,4]
##
[1,]
 1 11 21 31
[2,]
 2
 12
 22
 32
 13
 23
[3,]
 3
 33
simplify2array(list(1, 11:12, 21:23)) # no can do (without warning!)
[[1]]
[1] 1
##
[[2]]
 (continues on next page)
```

```
[1] 11 12
##
[[3]]
[1] 21 22 23
```

In the second example, each vector becomes a separate column of the resulting matrix, which can easily be justified by the fact that matrix elements are stored in a columnwise order.

**Example 11.2** Quite a few functions call the above automatically; compare the simplify argument to **apply**, **sapply**, **tapply**, or **replicate**, and the SIMPLIFY(sic!) argument to **mapply**. For instance, **sapply** combines **lapply** with **simplify2array**:

Take note of what constitutes the columns of the return matrix.

**Exercise 11.3** Inspect the behaviour of **as.matrix** on list arguments. Write your version of **sim-plify2array** named **as.matrix.list** that always returns a matrix. If a list of non-equisized vectors is given, fill the missing cells with NAs and generate a warning.

**Important** Sometimes a call to **do.call(cbind,** x) might be a better idea than a referral to **simplify2array**. Provided that x is a list of atomic vectors, it *always* returns a matrix: shorter vectors are recycled (which might be welcome, but not necessarily).

```
do.call(cbind, list(a=c(u=1), b=c(v=2, w=3), c=c(i=4, j=5, k=6)))
Warning in (function (..., deparse.level = 1): number of rows of result
is not a multiple of vector length (arg 2)
a b c
i 1 2 4
j 1 3 5
k 1 2 6
```

**Example 11.4** Consider a toy named list of numeric vectors:

```
x <- list(a=runif(10), b=rnorm(15))</pre>
```

Compare the results generated by **sapply** (which calls **simplify2array**):

```
sapply(x, function(e) c(Mean=mean(e)))
a.Mean b.Mean
0.57825 0.12431
sapply(x, function(e) c(Min=min(e), Max=max(e)))
 а
Min 0.045556 -1.9666
Max 0.940467 1.7869
```

with its version based on do.call and cbind:

```
sapply2 <- function(...)</pre>
 do.call(cbind, lapply(...))
sapply2(x, function(e) c(Mean=mean(e)))
##
 а
Mean 0.57825 0.12431
sapply2(x, function(e) c(Min=min(e), Max=max(e)))
 а
Min 0.045556 -1.9666
Max 0.940467 1.7869
```

Notice that **sapply** may return an atomic vector with somewhat surprising names.

See Section 12.3.7 for a few more examples.

#### Beyond numeric arrays 11.1.4

Arrays based on non-numeric vectors are also possible. For instance, we will later stress that matrix comparisons are performed elementwisely. They spawn logical matrices:

```
A >= 3
[,1] [,2] [,3]
[1,] FALSE FALSE TRUE
[2,] TRUE TRUE TRUE
```

Matrices of character strings can be useful too:

```
matrix(strrep(LETTERS[1:6], 1:6), ncol=3)
 [,1] [,2] [,3]
[1,] "A" "CCC" "EEEEE"
[2,] "BB" "DDDD" "FFFFFF"
```

And, of course, complex matrices:

```
A + 1i
[,1] [,2] [,3]
```

```
[1,] 1+1i 2+1i 3+1i
[2,] 4+1i 5+1i 6+1i
```

We are not limited to *atomic* vectors. Lists can be a basis for arrays as well:

```
matrix(list(1, 11:21, "A", list(1, 2, 3)), nrow=2)
[,1] [,2]
[1,] 1 "A"
[2,] integer,11 list,3
```

Certain elements are not *displayed* correctly, but they *are* still there.

#### 11.1.5 Internal representation

An object of the S3 class array is an atomic vector or a list equipped with the dims attribute being a vector of nonnegative integers. Interestingly, we do not have to set the class attribute explicitly: the accessor function **class** will return an implicit<sup>1</sup> class anyway.

```
class(1) # atomic vector
[1] "numeric"
class(structure(1, dim=rep(1, 1))) # 1D array (vector)
[1] "array"
class(structure(1, dim=rep(1, 2))) # 2D array (matrix)
[1] "matrix" "array"
class(structure(1, dim=rep(1, 3))) # 3D array
[1] "array"
```

Note that a two-dimensional array is additionally of the matrix class.

Optional dimension names are represented by means of the dimnames attribute, which is a list of d character vectors, where d is the array's dimensionality.

<sup>&</sup>lt;sup>1</sup> See Section 10.1. Interestingly, calling **unclass** on a matrix has no effect.

```
[[2]]
[1] "A" "B" "C"
```

**Important** Internally, elements in an array are stored in the column-major (Fortran) order:

```
as.numeric(A) # drop all attributes to reveal the underlying numeric vector
[1] 1 2 3 4 5 6
```

Setting byrow=TRUE in a call to the matrix function only affects the order in which this constructor reads a given source vector, not the resulting column/row-majorness.

```
(B <- matrix(1:6, ncol=3, byrow=TRUE))
[,1] [,2] [,3]
[1,] 1 2
[2,] 4 5
as.numeric(B)
[1] 1 4 2 5 3 6
```

The two said special attributes can be modified through the replacement functions `dim<-` and `dimnames<-` (and, of course, `attr<-` as well). In particular, changing dim does not alter the underlying atomic vector. It only affects how other functions, including the corresponding **print** method, interpret their placement on a virtual grid:

```
`dim<-`(A, c(3, 2)) # not the same as the transpose of `A`
[,1] [,2]
[1,] 1 4
 2
[2,]
[3,] 3 6
```

We obtained a different view of the same flat data vector. Also, the dimnames attribute was dropped because its size became incompatible with the newly requested dimensionality.

Exercise 11.5 Study the source code of the nrow, NROW, ncol, NCOL, rownames, row.names, and colnames functions.

Interestingly, for one-dimensional arrays, the names function returns a reasonable value (based on the dimnames attribute, which is a list with one character vector), despite the names attribute's not being set.

What is more, the dimnames attribute itself can be named:

```
names(dimnames(A)) <- c("ROWS", "COLUMNS")</pre>
print(A)
```

```
COLUMNS
ROWS A B C
a 1 3 5
b 2 4 6
```

It is still a numeric matrix, but its presentation has been slightly prettified.

**Exercise 11.6 outer** applies an elementwisely vectorised function on each pair of elements from two vectors, forming a two-dimensional result grid. Implement it yourself based on two calls to **rep**. Some examples:

```
outer(c(x=1, y=10, z=100), c(a=1, b=2, c=3, d=4), "*") # multiplication
a b c d
x 1 2 3 4
y 10 20 30 40
z 100 200 300 400
outer(c("A", "B"), 1:8, paste, sep="-") # concatenate strings
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] "A-1" "A-2" "A-3" "A-4" "A-5" "A-6" "A-7" "A-8"
[2,] "B-1" "B-2" "B-3" "B-4" "B-5" "B-6" "B-7" "B-8"
```

**Exercise 11.7** Show how match(y, z) can be implemented using outer. Is its time and memory complexity optimal, though?

**Exercise 11.8 table** creates a contingency matrix/array that counts the number of unique elements or unique pairs of corresponding items from one or more vectors of equal lengths. Write its one- and two-argument version based on **tabulate**. For example:

```
tips <- read.csv(paste0("https://github.com/gagolews/teaching-data/raw/",
 "master/other/tips.csv"), comment.char="#") # a data.frame (list)
table(tips[["day"]])
##
##
 Fri Sat Sun Thur
 87
 76 62
table(tips[["smoker"]], tips[["day"]])
##
 Fri Sat Sun Thur
##
 No
 4 45 57
 45
##
 Yes 15 42 19
```

# 11.2 Array indexing

Array subsetting can be performed by means of the overloaded<sup>2</sup> `[` method.

### 11.2.1 Arrays are built on basic vectors

Consider the two following example matrices:

Subsetting based on one indexer (as in Chapter 5) will refer to the underlying flat vector. For instance:

```
A[6]
[1] 10
```

It is the element in the third row, second column. Recall that values are stored in the column-major order.

# 11.2.2 Selecting individual elements

Our example  $3 \times 4$  real matrix  $\mathbf{A} \in \mathbb{R}^{3 \times 4}$  is like:

$$\mathbf{A} = \left[ \begin{array}{cccc} a_{1,1} & a_{1,2} & a_{1,3} & a_{1,4} \\ a_{2,1} & a_{2,2} & a_{2,3} & a_{2,4} \\ a_{3,1} & a_{3,2} & a_{3,3} & a_{3,4} \end{array} \right] = \left[ \begin{array}{cccc} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{array} \right].$$

Matrix elements are aligned in a two-dimensional grid. Hence, we can pinpoint a cell using two indexes. In mathematical notation,  $a_{i,j}$  refers to the i-th row and the j-th column. Similarly in R:

<sup>&</sup>lt;sup>2</sup> Hidden deeply at the C language level; see help("[").

```
A[3, 2] # the third row, the second column
[1] 10
B["c", "y"] # using dimnames == B[3, 2]
[1] 10
```

### 11.2.3 Selecting rows and columns

Some textbooks, and we are fond of this notation here as well, mark with  $\mathbf{a}_{i,\cdot}$  a vector that consists of all the elements in the *i*-th row and with  $\mathbf{a}_{\cdot,j}$  all items in the *j*-th column. In R, this corresponds to one of the indexers being left out.

```
A[3,] # the third row

[1] 9 10 11 12

A[, 2] # the second column

[1] 2 6 10

B["c",] # or B[3,]

x y z w

9 10 11 12

B[, "y"] # or B[, 2]

a b c

2 6 10
```

Let us stress that A[1], A[1, ], and A[, 1] have different meanings. Also, we see that the results' dimnames are adjusted accordingly; see also unname, which can take care of them once and for all.

**Exercise 11.9** Use **duplicated** to remove repeating rows in a given numeric matrix (see also **unique**).

# 11.2.4 Dropping dimensions

Extracting an individual element or a single row/column from a matrix brings about an atomic vector. If the resulting object's dim attribute consists of 1s only, it will be removed whatsoever; see also the **drop** function which removes the dimensions with only one level.

In order to obtain proper row and column vectors, we can request the preservation of the dimensionality of the output object (and, more precisely, the length of dim). This can be done by passing drop=FALSE to `[`.

```
A[1, 2, drop=FALSE] # the first row, second column
[,1]
[1,] 2
A[1, , drop=FALSE] # the first row
[,1] [,2] [,3] [,4]
[1,] 1 2 3 4
```

(continues on next page)

```
A[, 2, drop=FALSE] # the second column
[,1]
[1,] 2
[2,] 6
[3,] 10
```

**Important** Unfortunately, the drop argument defaults to TRUE. Many bugs could be avoided otherwise, primarily when the indexers are generated programmatically.

**Note** For list-based matrices, we can also use a multi-argument version of `[[` to extract the individual elements.

# 11.2.5 Selecting submatrices

Indexing based on two vectors, both of length two or more, extracts a sub-block of a given matrix.

```
A[1:2, c(1, 2, 4)] # rows 1 and 2, columns 1, 2, and 4
[,1] [,2] [,3]
[1,] 1 2 4
[2,] 5 6 8
B[c("a", "b"), -3] # some rows, omit the third column
x y w
a 1 2 4
b 5 6 8
```

Note again that we have drop=TRUE by default, which affects the operator's behaviour if one of the indexers is a scalar.

```
A[c(1, 3), 3]
[1] 3 11
(continues on next page)
```

```
A[c(1, 3), 3, drop=FALSE]

[,1]

[2,] 11
```

**Exercise 11.10** Define the **split** method for the matrix class that returns a list of n matrices when given a matrix with n rows and an object of the class factor of length n (or a list of such objects). For example:

### 11.2.6 Selecting elements based on logical vectors

Logical vectors can also be used as indexers, with consequences that are not hard to guess:

```
A[c(TRUE, FALSE, TRUE), -1] # select 1st and 3rd row, omit 1st column

[,1] [,2] [,3]

[1,] 4 7 10

[2,] 6 9 12

B[B[, "x"]>1 & B[, "x"]<=9,] # all rows where x's contents are in (1, 9]

x y z w

b 5 6 7 8

c 9 10 11 12

A[2, colMeans(A)>6, drop=FALSE] # 2nd row and the columns whose means > 6

[,1] [,2]

[1,] 8 11
```

**Note** Section 11.3 notes that comparisons involving matrices are performed in an elementwise manner. For example:

```
A>7
[,1] [,2] [,3] [,4]
(continues on next page)
```

```
[1,] FALSE FALSE TRUE
[2,] FALSE FALSE TRUE TRUE
[3,] FALSE FALSE TRUE TRUE
```

Such logical matrices can be used to subset other matrices of the same size. This kind of indexing always gives rise to a (flat) vector:

```
A[A>7]
[1] 8 9 10 11 12
```

It is nothing else than the single-indexer subsetting involving two flat vectors (a numeric and a logical one). The dim attributes are not considered here.

Exercise 11.11 Implement your versions of max.col, lower.tri, and upper.tri.

### 11.2.7 Selecting based on two-column numeric matrices

We can also index a matrix A by a two-column matrix of positive integers I. For instance:

```
(I <- cbind(
	c(1, 3, 2, 1, 2),
	c(2, 3, 2, 2, 4)
))
[,1] [,2]
[1,] 1 2
[2,] 3 3
[3,] 2 2
[4,] 1 2
[5,] 2 4
```

Now A[I] gives easy access to:

```
A[I[1, 1], I[1, 2]],
A[I[2, 1], I[2, 2]],
A[I[3, 1], I[3, 2]],
```

and so forth. In other words, each row of I gives the coordinates of the elements to extract. The result is always a flat vector.

```
A[I]
[1] 4 9 5 4 11
```

This is exactly A[1, 2], A[3, 3], A[2, 2], A[1, 2], A[2, 4].

**Note** which can also return a list of index matrices:

Moreover, arrayInd converts flat indexes to multidimensional ones.

**Exercise 11.12** Implement your version of **arrayInd** and a function performing the inverse operation.

**Exercise 11.13** Write your version of diag.

### 11.2.8 Higher-dimensional arrays

For d-dimensional arrays, indexing can involve up to d indexes. It is particularly valuable for arrays with the dimnames attribute set representing contingency tables over a Cartesian product of multiple factors. The **datasets**::Titanic object is an exemplary four-dimensional table:

```
str(dimnames(Titanic)) # for reference (note that dimnames are named)
List of 4
$ Class : chr [1:4] "1st" "2nd" "3rd" "Crew"
$ Sex : chr [1:2] "Male" "Female"
$ Age : chr [1:2] "Child" "Adult"
$ Survived: chr [1:2] "No" "Yes"
```

Here is the number of adult male crew members who survived the accident:

```
Titanic["Crew", "Male", "Adult", "Yes"]
[1] 192
```

Moreover, let us fetch a slice corresponding to adults travelling in the premium class:

```
Titanic["1st", , "Adult",]

Survived

Sex No Yes

Male 118 57

Female 4 140
```

**Exercise 11.14** Check if the above four-dimensional array can be indexed using matrices with four columns.

### 11.2.9 Replacing elements

Generally, subsetting drops all attributes except names, dim, and dimnames (unless it does not make sense otherwise). The replacement variant of the index operator modifies vector values but generally preserves all the attributes. This enables transforming matrix elements like:

**Exercise 11.15** Given a character matrix with entities that can be interpreted as numbers like:

```
(X <- rbind(x=c(a="1", b="2"), y=c("3", "4")))
a b
x "1" "2"
y "3" "4"
```

convert it to a numeric matrix with a single line of code. Preserve all attributes.

# 11.3 Common operations

# 11.3.1 Matrix transpose

The matrix *transpose*, mathematically denoted with  $\mathbf{A}^T$ , is available via a call to  $\mathbf{t}$ :

```
(A <- matrix(1:6, byrow=TRUE, nrow=2))

[,1] [,2] [,3]

[1,] 1 2 3

[2,] 4 5 6

t(A)

[,1] [,2]

[1,] 1 4

[2,] 2 5

[3,] 3 6
```

Hence, if  $\mathbf{B} = \mathbf{A}^T$ , then it is a matrix such that  $b_{i,j} = a_{j,i}$ . In other words, in the transposed matrix, rows become columns, and columns become rows.

For higher-dimensional arrays, a generalised transpose can be obtained through **aperm** (try permuting the dimensions of Titanic). Also, the conjugate transpose of a complex matrix  $\mathbf{A}$  is done via  $\mathbf{Conj(t(A))}$ .

### 11.3.2 Vectorised mathematical functions

Vectorised functions such as **sqrt**, **abs**, **round**, **log**, **exp**, **cos**, **sin**, etc., operate on each array element<sup>3</sup>.

```
A <- matrix(1/(1:6), nrow=2)
round(A, 2) # rounds every element in A

[,1] [,2] [,3]

[1,] 1.0 0.33 0.20

[2,] 0.5 0.25 0.17
```

**Exercise 11.16** Using a single call to **matplot**, which allows the yargument to be a matrix, draw a plot of  $\sin(x)$ ,  $\cos(x)$ ,  $|\sin(x)|$ , and  $|\cos(x)|$  for  $x \in [-2\pi, 6\pi]$ ; see Section 13.3 for more details.

### 11.3.3 Aggregating rows and columns

When we call an aggregation function on an array, it will reduce all elements to a single number:

The apply function may be used to summarise individual rows or columns in a matrix:

- apply(A, 1, f) applies a given function **f** on each *row* of a matrix A (over the first axis),
- apply(A, 2, f) applies f on each column of A (over the second axis).

For instance:

```
apply(A, 1, mean) # synonym: rowMeans(A)
[1] 2.5 6.5 10.5

(continues on next page)
```

 $<sup>^3</sup>$  They are simply applied on each element of the underlying flat vector. Section 5.5 mentioned that unary functions preserve all attributes of their inputs, hence also dim and dimnames.

```
apply(A, 2, mean) # synonym: colMeans(A)
[1] 5 6 7 8
```

The function being applied does not have to return a single number:

```
apply(A, 2, range) # min and max
 [,1] [,2] [,3] [,4]
[1,]
 1
 2
 3
[2,]
 9
 10
 11
 12
apply(A, 1, function(row) c(Min=min(row), Mean=mean(row), Max=max(row)))
 [,1] [,2] [,3]
 1.0 5.0 9.0
Min
Mean 2.5 6.5 10.5
Max 4.0 8.0 12.0
```

Take note of the columnwise order of the output values.

apply also works on higher-dimensional arrays:

```
apply(Titanic, 1, mean) # over the first axis, "Class" (dimnames work too)
 2nd
 40.625 35.625 88.250 110.625
apply(Titanic, c(1, 3), mean) # over c("Class", "Age")
##
 Age
Class Child Adult
##
 1st 1.50 79.75
 2nd 6.00 65.25
##
 3rd 19.75 156.75
##
##
 Crew 0.00 221.25
```

#### Binary operators 11.3.4

In Section 5.5, we stated that binary elementwise operations, such as addition or multiplication, preserve the attributes of the longer input or both (with the first argument preferred to the second) if they are of equal sizes. Taking into account that:

- an array is simply a flat vector equipped with the dim attribute, and
- we refer to the respective default methods when applying binary operators,

we can deduce how `+`, `<=`, `&`, etc. behave in several different contexts.

Array-array. First, let us note what happens when we operate on two arrays of identical dimensionalities.

```
(A <- rbind(c(1, 10, 100), c(-1, -10, -100)))
[,1] [,2] [,3]
[1,] 1 10 100
[2,] -1 -10 -100
(B <- matrix(1:6, byrow=TRUE, nrow=2))
[,1] [,2] [,3]
[1,] 1 2 3
[2,] 4 5
A + B # elementwise addition
[,1] [,2] [,3]
[1,] 2 12 103
[2,] 3 -5 -94
A * B # elementwise multiplication (not: algebraic matrix multiply)
[,1] [,2] [,3]
[1,] 1 20 300
[2,] -4 -50 -600
```

They are simply the addition and multiplication of the corresponding elements of two given matrices.

**Array-scalar**. Second, we can apply matrix-scalar operations:

```
(-1)*B

[,1] [,2] [,3]

[1,] -1 -2 -3

[2,] -4 -5 -6

A^2

[,1] [,2] [,3]

[1,] 1 100 10000

[2,] 1 100 10000
```

They multiplied each element in B by -1 and squared every element in A, respectively. The behaviour of relational operators is of course similar:

```
A >= 1 & A <= 100

[,1] [,2] [,3]

[1,] TRUE TRUE TRUE

[2,] FALSE FALSE FALSE
```

**Array-vector**. Next, based on the recycling rule and the fact that matrix elements are ordered columnwisely, we have that:

```
B * c(10, 100)
[,1] [,2] [,3]
(continues on next page)
```

```
[1,] 10 20 30
[2,] 400 500 600
```

It multiplied every element in the first *row* by 10 and each element in the second row by 100.

If we wish to multiply each element in the first, second, ..., etc. *column* by the first, second, ..., etc. value in a vector, we should *not* call:

```
B * c(1, 100, 1000)

[,1] [,2] [,3]

[1,] 1 2000 300

[2,] 400 5 6000
```

but rather:

```
t(t(B) * c(1, 100, 1000))

[,1] [,2] [,3]

[1,] 1 200 3000

[2,] 4 500 6000
```

or:

**Exercise 11.17** Write a function that standardises the values in each column of a given matrix: for all elements in each column, subtract their mean and then divide them by the standard deviation. Try to implement it in a few different ways, including via a call to **apply**, **sweep**, **scale**, or based solely on arithmetic operators.

**Note** Some sanity checks are done on the dimattributes, so not every configuration is possible. Notice the following peculiarities:

```
A + t(B) # 'dim' equal to c(2, 3) vs c(3, 2)

Error in A + t(B): non-conformable arrays

A * cbind(1, 10, 100) # this is too good to be true

Error in A * cbind(1, 10, 100): non-conformable arrays

A * rbind(1, 10) # but A * c(1, 10) works...

Error in A * rbind(1, 10): non-conformable arrays

A + 1:12 # 'A' has six elements

Error in eval(expr, envir, enclos): dims [product 6] do not match the

length of object [12]
```

```
A + 1:5 # partial recycling is okay

Warning in A + 1:5: longer object length is not a multiple of shorter

object length

[1,1] [,2] [,3]

[1,] 2 13 105

[2,] 1 -6 -99
```

# 

Many data analysis and machine learning algorithms, in their essence, involve rather straightforward matrix algebra and numerical mathematics. Suffice it to say that anyone serious about data science and scientific computing should learn the necessary theory; see, for example, [30] and [31].

R is a convenient interface to the stable and well-tested algorithms from, amongst others, LAPACK and BLAS<sup>4</sup>. Below we mention a few of them. External packages implement hundreds of algorithms tackling differential equations, constrained and unconstrained optimisation, etc.; CRAN Task Views<sup>5</sup> provide a good overview.

# 11.4.1 Matrix multiplication

`\*` performs elementwise multiplication. For what we call the (algebraic) matrix multiplication, we use the `%\*%` operator. It can only be performed on two matrices of compatible sizes: the number of columns in the left matrix must match the number of rows in the right operand.

Given  $\mathbf{A} \in \mathbb{R}^{n \times p}$  and  $\mathbf{B} \in \mathbb{R}^{p \times m}$ , their multiply is a matrix  $\mathbf{C} = \mathbf{A}\mathbf{B} \in \mathbb{R}^{n \times m}$  such that  $c_{i,j}$  is the dot product of the *i*-th row in  $\mathbf{A}$  and the *j*-th column in  $\mathbf{B}$ :

$$c_{i,j} = \mathbf{a}_{i,\cdot} \cdot \mathbf{b}_{\cdot,j} = \sum_{k=1}^{p} a_{i,k} b_{k,j},$$

for i = 1, ..., n and j = 1, ..., m. For instance:

```
(A <- rbind(c(0, 1, 3), c(-1, 1, -2)))

[,1] [,2] [,3]

[1,] 0 1 3

[2,] -1 1 -2
```

(continues on next page)

<sup>&</sup>lt;sup>4</sup> (\*) We can select the underlying implementation of BLAS at R's compile time; see Section A.3 of [65]. Some of them are faster than others.

<sup>&</sup>lt;sup>5</sup> https://cran.r-project.org/web/views

```
(B <- rbind(c(3, -1), c(1, 2), c(6, 1)))

[,1] [,2]

[2,] 1 2

[3,] 6 1

A %*% B

[,1] [,2]

[1,] 19 5

[2,] -14 1
```

**Note** When applying `%\*%` on one or more flat vectors, their dimensionality will be promoted automatically to make the operation possible. However,  $\mathbf{c}(a, b)$  %\*%  $\mathbf{c}(c, d)$  gives a scalar ac + bd, and not a  $2 \times 2$  matrix.

Further, crossprod(A, B) yields  $A^TB$  and tcrossprod(A, B) determines  $AB^T$  more efficiently than relying on `%\*%`. We can omit the second argument and get  $A^TA$  and  $AA^T$ , respectively.

```
crossprod(c(2, 1)) # Euclidean norm squared
[,1]
[1,] 5
crossprod(c(2, 1), c(-1, 2)) # dot product of two vectors
[,1]
[1,] 0
crossprod(A) # same as t(A) %*% A, i.e., dot products of all column pairs
[,1] [,2] [,3]
[1,] 1 -1 2
[2,] -1 2 1
[3,] 2 1 13
```

Recall that if the dot product of two vectors equals 0, we say that they are orthogonal (perpendicular).

**Exercise 11.18** (\*) Write your versions of **cov** and **cor**: functions to compute the covariance and correlation matrices. Make use of the fact that the former can be determined with **crossprod** based on a centred version of an input matrix.

# 11.4.2 Solving systems of linear equations

The **solve** function can be used to determine the solution to m systems of n linear equations of the form  $\mathbf{A}\mathbf{X} = \mathbf{B}$ , where  $\mathbf{A} \in \mathbb{R}^{n \times n}$  and  $\mathbf{X}, \mathbf{B} \in \mathbb{R}^{n \times m}$  (via the LU decomposition with partial pivoting and row interchanges).

#### 11.4.3 Norms and metrics

Given an  $n \times m$  matrix **A**, calling norm(A, "1"), norm(A, "2"), and norm(A, "I"), we can compute the operator norms:

$$\begin{array}{lcl} \|\mathbf{A}\|_1 & = & \max_{j=1,\dots,m} \sum_{i=1}^n |a_{i,j}|, \\ \|\mathbf{A}\|_2 & = & \sigma_1(\mathbf{A}) = \sup_{\mathbf{0} \neq \mathbf{x} \in \mathbb{R}^m} \frac{\|\mathbf{A}\mathbf{x}\|_2}{\|\mathbf{x}\|_2} \\ \|\mathbf{A}\|_I & = & \max_{i=1,\dots,n} \sum_{j=1}^m |a_{i,j}|, \end{array}$$

where  $\sigma_1$  gives the largest singular value (see below).

Also, passing "F" as the second argument yields the Frobenius norm,  $\|\mathbf{A}\|_F = \sqrt{\sum_{i=1}^n \sum_{j=1}^m a_{i,j}^2}$ , and "M" computes the maximum norm,  $\|\mathbf{A}\|_M = \max_{\substack{i=1,\dots,n\\j=1,\dots,m}} |a_{i,j}|$ .

If **A** is a column vector, then  $\|\mathbf{A}\|_F$  and  $\|\mathbf{A}\|_2$  are equivalent. They are referred to as the Euclidean norm. Moreover,  $\|\mathbf{A}\|_M = \|\mathbf{A}\|_I$  gives the supremum norm and  $\|\mathbf{A}\|_1$  outputs the Manhattan (taxicab) one.

**Exercise 11.19** Given an  $n \times m$  matrix  $\mathbf{A}$ , normalise each column so that it becomes a unit vector, i.e., whose Euclidean norm equals 1.

Further, **dist** determines all pairwise distances between a set of n vectors in  $\mathbb{R}^m$ , written as an  $n \times m$  matrix. For example, let us consider three vectors in  $\mathbb{R}^2$ :

Thus, the Euclidean distance between the first and the third vector,  $\|\mathbf{x}_{1,\cdot} - \mathbf{x}_{3,\cdot}\|_2 = \sqrt{(x_{1,1} - x_{3,1})^2 + (x_{1,2} - x_{3,2})^2}$ , is roughly 1.41421. The maximum, Manhattan, and Canberra distances/metrics are also available, amongst others.

**Exercise 11.20** dist returns an object of the S3 class dist. Inspect how it is represented.

**Example 11.21** *adist* implements a couple of string metrics. For example:

(continues on next page)

It gave the Levenshtein distances between each pair of strings. In particular, we need two edit operations (character insertions, deletions, or replacements) to turn "eggs" into "legs" (add l and remove g).

**Example 11.22** Objects of the class dist can be used to find a hierarchical clustering of a dataset. For example:

```
h <- hclust(as.dist(d), method="average") # see also: plot(h, labels=x)
cutree(h, 3)
spam bacon eggs spa spams legs
1 2 3 1 1 3</pre>
```

It determined three clusters using the average linkage strategy ("legs" and "eggs" are grouped together, "spam", "spa", "spams" form another cluster, and "bacon" is a singleton).

### 11.4.4 Eigenvalues and eigenvectors

**eigen** returns a sequence of eigenvalues  $(\lambda_1, \dots, \lambda_n)$  ordered nondecreasingly w.r.t.  $|\lambda_i|$ , and a matrix **V** whose columns define the corresponding eigenvectors (scaled to the unit length) of a given matrix **X**. By definition, for all j, it holds that  $\mathbf{X}\mathbf{v}_{\cdot,j} = \lambda_j \mathbf{v}_{\cdot,j}$ .

**Example 11.23** (\*) Here are the eigenvalues and the corresponding eigenvectors of the matrix defining the rotation in the xy-plane about the origin (0,0) by the counterclockwise angle  $\pi/6$ :

```
(R <- rbind(c(cos(pi/6), sin(pi/6)),
 c(-sin(pi/6), cos(pi/6))))
##
 \lceil,1\rceil
 [,2]
[1,] 0.86603 0.50000
[2,] -0.50000 0.86603
eigen(R)
eigen() decomposition
$values
[1] 0.86603+0.5i 0.86603-0.5i
##
$vectors
##
 [,1]
 \Gamma, 27
[1,] 0.70711+0.00000i 0.70711+0.00000i
[2,] 0.00000+0.70711i 0.00000-0.70711i
```

The complex eigenvalues are  $e^{-\pi/6i}$  and  $e^{\pi/6i}$  and we have  $|e^{-\pi/6i}| = |e^{\pi/6i}| = 1$ .

**Example 11.24** (\*) Consider a pseudorandom sample that we depict in Figure 11.1:

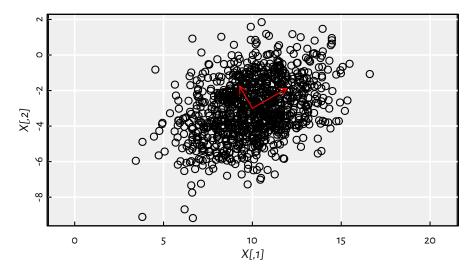


Figure 11.1. A sample from a bivariate normal distribution and its principal axes.

**X** was created by generating a realisation of a two-dimensional standard normal vector **Z**, scaling it by  $(\sqrt{5}, \sqrt{2})$ , rotating by the counterclockwise angle  $\pi/6$ , and shifting by (10, -3), which we denote with  $\mathbf{X} = \mathbf{Z}\mathbf{S}\mathbf{R} + \boldsymbol{\mu}^T$ . It can be shown that **X** follows a bivariate normal distribution centred at  $\boldsymbol{\mu} = (10, -3)$  and with the covariance matrix  $\boldsymbol{\Sigma} = (\mathbf{S}\mathbf{R})^T(\mathbf{S}\mathbf{R})$ :

```
crossprod($ %*% R) # covariance matrix
[,1] [,2]
[1,] 4.250 1.299
[2,] 1.299 2.750
cov(X) # compare: sample covariance matrix (estimator)
[,1] [,2]
[1,] 4.1965 1.2386
[2,] 1.2386 2.7973
```

<sup>&</sup>lt;sup>6</sup> For drawing random samples from any multivariate distribution, refer to the theory of copulas, e.g., [49]. There are a few R packages on CRAN that implement the most popular models.

It is known that eigenvectors of the covariance matrix correspond to the principal components of the original dataset. Furthermore, its eigenvalues give the variances explained by each of them.

```
eigen(cov(X))
eigen() decomposition
$values
[1] 4.9195 2.0744
##
$vectors
[,1] [,2]
[1,] -0.86366 0.50408
[2,] -0.50408 -0.86366
```

It roughly corresponds to the principal directions ( $\cos \pi/6$ ,  $\sin \pi/6$ )  $\simeq (0.866, 0.5)$  and the thereto-orthogonal ( $-\sin \pi/6$ ,  $\cos \pi/6$ )  $\simeq (-0.5, 0.866)$  (up to an orientation inverse) with the corresponding variances of 5 and 2 (i.e., standard deviations of  $\sqrt{5}$  and  $\sqrt{2}$ ), respectively. Note that this method of performing principal component analysis, i.e., recreating the scale and rotation transformation applied on  $\mathbf Z$  based only on  $\mathbf X$ , is not particularly numerically stable; see below for an alternative.

### 11.4.5 QR decomposition

We say that a real  $n \times m$  matrix  $\mathbf{Q}$ ,  $n \ge m$ , is *orthogonal*, whenever  $\mathbf{Q}^T \mathbf{Q} = \mathbf{I}$  (identity matrix). This is equivalent to  $\mathbf{Q}$ 's columns' being orthogonal unit vectors. Also, if  $\mathbf{Q}$  is a square matrix, then  $\mathbf{Q}^T = \mathbf{Q}^{-1}$  if and only if  $\mathbf{Q}^T \mathbf{Q} = \mathbf{Q} \mathbf{Q}^T = \mathbf{I}$ .

Let **A** be a real<sup>7</sup>  $n \times m$  matrix with  $n \ge m$ . Then **A** = **QR** is its QR decomposition (in the so-called narrow form), if **Q** is an orthogonal  $n \times m$  matrix and **R** is an upper triangular  $m \times m$  one.

The **qr** function returns an object of the S3 class qr from which we can extract the two components; see the **qr.Q** and **qr.R** functions.

**Example 11.25** Let **X** be an  $n \times m$  data matrix, representing n points in  $\mathbb{R}^m$ , and a vector  $\mathbf{y} \in \mathbb{R}^n$  of the desired outputs corresponding to each input. For fitting a linear model  $\mathbf{x}^T \boldsymbol{\theta}$ , where  $\boldsymbol{\theta}$  is a vector of m parameters, we can use the method of least squares, which minimises:

$$\mathcal{L}(\boldsymbol{\theta}) = \sum_{i=1}^{n} \left( \mathbf{x}_{i,\cdot}^T \boldsymbol{\theta} - y_i \right)^2 = \| \mathbf{X} \boldsymbol{\theta} - \mathbf{y} \|_2^2.$$

It might be shown that if  $\mathbf{X} = \mathbf{Q}\mathbf{R}$ , then  $\boldsymbol{\theta} = (\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^T\mathbf{y} = \mathbf{R}^{-1}\mathbf{Q}^T\mathbf{y}$ , which can conveniently be determined via a call to **qr.coef**.

In particular, we can fit a simple linear regression model y = ax + b by considering  $\mathbf{X} = (x, 1)$  and  $\boldsymbol{\theta} = (a, b)$ . For instance (see Figure 11.2):

 $<sup>^7</sup>$  If  ${\bf A}$  is a complex matrix, its QR decomposition spawns  ${\bf Q}$  that is a unitary matrix.

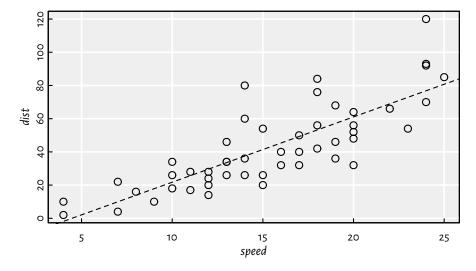


Figure 11.2. The cars dataset and the fitted regression line.

**solve** with one argument determines the inverse of a given matrix. The fitted model is y = 3.93241x - 17.5791.

The same approach is used by **Im.fit**, the workhorse behind the **Im** method accepting an R formula (which some readers might be familiar with; compare Section 17.6).

# 11.4.6 SVD decomposition

Given a real  $n \times m$  matrix **X**, its singular value decomposition (SVD) is given by **X** =  $\mathbf{UDV}^T$ , where **D** is a  $p \times p$  diagonal matrix (with the singular values of **X**,  $d_{1,1} \ge ... \ge$ 

 $d_{p,p} \ge 0, p = \min\{n, m\}$ ), and **U** and **V** are orthogonal matrices of dimensions  $n \times p$  and  $m \times p$ , respectively.

**svd** may not only be used to determine the solution to linear regression<sup>8</sup> but also to perform the principal component analysis<sup>9</sup>. Namely, **V** gives the eigenvectors of  $\mathbf{X}^T\mathbf{X}$ . Assuming that **X** is centred at 0, the latter is precisely its scaled covariance matrix.

**Example 11.26** (\*) Continuing the example featuring a bivariate normal sample, we can determine the principal directions also by calling:

```
Xc <- t(t(X)-colMeans(X)) # centred version of X
svd(Xc)[["v"]]
[,1] [,2]
[1,] -0.86366 -0.50408
[2,] -0.50408 0.86366</pre>
```

### 11.4.7 A note on the Matrix package

The Matrix package is perhaps the most widely known showcase of the S4 object orientation (Section 10.5). It defines classes and methods for dense and sparse matrices, including rectangular, symmetric, triangular, band, and diagonal ones.

For instance, large graph (e.g., in network sciences) or preference (e.g., in recommender systems) data can be represented using sparse matrices, i.e., those with many zeroes. After all, it is much more likely for two vertices in a network *not* to be joined by an edge than to be connected. For example:

We created a real diagonal matrix of size  $5 \times 5$ ; 20 elements equal to zero are specially marked. Moreover:

<sup>&</sup>lt;sup>8</sup> As the pseudoinverse  $\mathbf{X}^+ = (\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^T = \mathbf{V}\mathbf{D}^+\mathbf{U}^T = \mathbf{R}^{-1}\mathbf{Q}^T$ , with  $\mathbf{X}^+\mathbf{X} = \mathbf{I}$ . Here,  $\mathbf{D}^+$  is a transposed version of  $\mathbf{D}$  carrying the reciprocals of its non-zero elements.

<sup>&</sup>lt;sup>9</sup> See the source code of **getS3method**("prcomp", "default").

```
5 x 5 sparse Matrix of class "dgCMatrix"

[1,] 1 7 . . .

[2,] . 2 . . .

[3,] . . 3 . .

[4,] 42 . . 4 .

[5,] 5
```

It yielded a general sparse real matrix in the CSC (compressed, sparse, column-orientated) format.

For more information on this package, see vignette(package="Matrix").

### 11.5 Exercises

**Exercise 11.27** *Let X be a matrix with dimnames set. For instance:* 

Explain the meaning of the following expressions involving matrix subsetting. Note that a few of them are invalid.

```
X[1,],
X[, 3],
X[, 3, drop=FALSE],
X[3],
X[, "a"],
X[, c("a", "b", "c")],
X[, -2],
X[X[,1] > 5,],
X[X[,1]>5, c("a", "b", "c")],
X[X[,1]>5 & X[,1]<=10,],
```

- X[X[,1]>=5 & X[,1]<=10, c("a", "b", "c")],
- X[, c(1, "b", "d")].

**Exercise 11.28** Assuming that X is an array, what is the difference between the following operations involving indexing?

- X["1", ] vs X[1, ],
- X[, "a", "b", "c"] vs X["a", "b", "c"] vs X[, c("a", "b", "c")] vs X[c("a", "b", "c")],
- X[1] vs X[, 1] vs X[1, ],
- X[X>0] vs X[X>0, ] vs X[, X>0],
- X[X[, 1]>0] vs X[X[, 1]>0,] vs X[,X[,1]>0],
- X[X[, 1]>5, X[1, ]<10] vs X[X[1, ]>5, X[, 1]<10].

### **Exercise 11.29** *Give a few ways to create a matrix like:*

```
[,1] [,2]
##
[1,]
 1
 1
[2,]
 1
 2
[3,]
 1
 3
[4,]
 2
 1
[5,]
 2
[6,]
 2
 3
```

and one like:

```
##
 [,1] [,2] [,3]
 [1,]
 1
 1
##
 [2,]
 1
 1
 2
##
 [3, 7]
 2
##
 1
[4,]
 2
 2
 1
[5,]
 3
 1
[6,]
 1
 3
 2
[7,]
 2
 1
 1
[8,]
 2
 1
 2
[9,]
 1
 2
 2
 2
[10,]
[11,]
 2
 3
 1
[12,]
```

**Exercise 11.30** For a given real  $n \times m$  matrix  $\mathbf{X}$ , encoding n input points in an m-dimensional space, determine their bounding hyperrectangle, i.e., return a  $2 \times m$  matrix  $\mathbf{B}$  with  $b_{1,j} = \min_i x_{i,j}$  and  $b_{2,j} = \max_i x_{i,j}$ .

**Exercise 11.31** Let **t** be a vector of n integers in  $\{1, ..., k\}$ . Write a function to one-hot encode

each  $t_i$ . Return a 0–1 matrix **R** of size  $n \times k$  such that  $r_{i,j} = 1$  if and only if  $j = t_i$ . For example, if  $\mathbf{t} = [1, 2, 3, 2, 4]$  and k = 4, then:

$$\mathbf{R} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right].$$

On a side note, such a representation is beneficial when solving, e.g., a multiclass classification problem by means of k binary classifiers.

Then, compose another function, but this time setting  $r_{i,j} = 1$  if and only if  $j \ge t_i$ , e.g.:

$$R = \left[ \begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{array} \right].$$

**Important** As usual, try to solve all the exercises without using explicit **for** and **while** loops (provided that it is possible).

**Exercise 11.32** Given an  $n \times k$  real matrix, apply the softmax function on each row, i.e., map  $x_{i,j}$  to  $\frac{\exp(x_{i,j})}{\sum_{l=1}^k \exp(x_{i,l})}$ . Then, one-hot decode the values in each row, i.e., find the column number with the greatest value. Return a vector of size n with elements in  $\{1,\ldots,k\}$ .

**Exercise 11.33** Assume that an  $n \times m$  real matrix  $\mathbf{X}$  represents n points in  $\mathbb{R}^m$ . Write a function (but do not refer to dist) that determines the pairwise Euclidean distances between all the n points and a given  $\mathbf{y} \in \mathbb{R}^m$ . Return a vector  $\mathbf{d}$  of length n with  $d_i = ||\mathbf{x}_{i,\cdot} - \mathbf{y}||_2$ .

**Exercise 11.34** Let **X** and **Y** be two real-valued matrices of sizes  $n \times m$  and  $k \times m$ , respectively, representing two sets of points in  $\mathbb{R}^m$ . Return an integer vector **r** of length k such that  $r_i$  indicates the index of the point in **X** with the least distance to (the closest to) the i-th point in **Y**, i.e.,  $r_i = \arg\min_i \|\mathbf{x}_{i,\cdot} - \mathbf{y}_{i,\cdot}\|_2$ .

Exercise 11.35 Write your version of utils::combn.

**Exercise 11.36** Time series are vectors or matrices of the class ts equipped with the tspattribute, amongst others. Refer to **help**("ts") for more information about how they are represented and what S3 methods have been overloaded for them.

**Exercise 11.37** (\*) Numeric matrices can be stored in a CSV file, amongst others. Usually, we will be loading them via *read.csv*, which returns a data frame (see Chapter 12). For example:

II DEEPER

(continued from previous page)

```
"raw/master/marek/eurxxx-20200101-20200630.csv"
),
comment.char="#",
sep=","
))
```

Write a function <code>read\_numeric\_matrix(file\_name, comment, sep)</code> which is based on a few calls to <code>scan</code> instead. Use <code>file</code> to establish a file connection so that you can ignore the comment lines and fetch the column names before reading the actual numeric values.

**Exercise 11.38** (\*) Using **readBin**, read the t10k-images-idx3-ubyte.gz from the MNIST database homepage<sup>10</sup>. The output object should be a three-dimensional,  $10000 \times 28 \times 28$  array with real elements between 0 and 255. Refer to the File Formats section therein for more details.

**Exercise 11.39** (\*\*) Circular convolution of discrete-valued multidimensional signals can be performed by means of **fft** and matrix multiplication, whereas affine transformations require only the latter. Apply various image transformations such as sharpening, shearing, and rotating on the MNIST digits and plot the results using the **image** function.

**Exercise 11.40** (\*) Using constrOptin, find the minimum of the Constrained Betts Function  $f(x_1, x_2) = 0.01x_1^2 + x_2^2 - 100$  with linear constraints  $2 \le x_1 \le 50, -50 \le x_2 \le 50$ , and  $10x_1 \ge 10 + x_2$ . (\*\*) Also, use solve. QP from the quadprog package to find the minimum.

<sup>&</sup>lt;sup>10</sup> https://web.archive.org/web/20211107114045/http://yann.lecun.com/exdb/mnist

# Data frames

Most matrices are built on top of atomic vectors. Hence, only items of the same type can be arranged into rows and columns. On the other hand, *data frames* (objects of the S3 class data.frame, first introduced in [13]) are *collections* of vectors of the same lengths or matrices with identical row counts. Hence, they represent structured<sup>1</sup> data of possibly *heterogeneous* types. For instance:

```
class(iris) # `iris` is an example data frame
[1] "data.frame"
iris[c(1, 51, 101),] # three chosen rows from `iris`
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
1
 5.1
 3.5
 1.4
 setosa
51
 4.7
 1.4 versicolor
 7.0
 3.2
101
 6.3
 3.3
 6.0
 2.5 virginica
```

It is a mix of numeric and factor-type data.

The good news is that not only are data frames built on *named lists* (e.g., to extract a column, we can refer to `[[`), but also many functions consider them *matrix-like* (e.g., to select specific rows and columns, two indexes can be passed to `[` like in the example above). Hence, it will soon turn out that we already know a lot about performing basic data wrangling activities, even if we do not fully realise it now.

# 12.1 Creating data frames

#### 12.1.1 data.frame and as.data.frame

Most frequently, we create data frames based on a series of logical, numeric, or character vectors of identical lengths. In such a scenario, the data.frame function is particularly worthwhile.

<sup>&</sup>lt;sup>1</sup> We are already highly skilled in dealing with unstructured data and turning them into something that is much more regular. The numerous functions, which we have covered in the first part of this book, let us extract meaningful data from text, handle missing values, engineer features, and so forth.

The shorter vectors were recycled. We can verify that the diverse column types were retained and no coercion was made by calling:

```
str(x)
'data.frame': 6 obs. of 4 variables:
$ a: logi TRUE FALSE TRUE FALSE
$ b: int 1 2 3 4 5 6
$ c: num 0.774 0.197 0.978 0.201 0.361 ...
$ d: chr "spam" "spam" "eggs" "spam" ...
```

**Important** For many reasons (see, e.g., Section 12.1.5 and Section 12.1.6), we recommend having the type of each column always checked, e.g., by calling the **str** function.

Many objects, such as matrices, can easily be coerced to data frames using particular as.data.frame methods. Here is an example matrix:

Let us convert it to a data frame:

```
as.data.frame(A) # as.data.frame.matrix
u v
1 1 4

(continues on next page)
```

```
2 2 5
3 3 6
```

Note that a matrix with no row labels is printed slightly differently than a data frame with (as it will soon turn out) the default row.names.

Named lists are amongst other aspirants to a meaningful conversion. Consider an example list where all elements are vectors of the same length:

```
(l <- Map(
 function(x) {
 c(Min=min(x), Median=median(x), Mean=mean(x), Max=max(x))
 split(iris[["Sepal.Length"]], iris[["Species"]])
))
$setosa
##
 Min Median
 Mean
 Max
4.300 5.000 5.006 5.800
##
$versicolor
 Min Median
 Mean
 Max
4.900 5.900 5.936 7.000
$virginica
 Min Median
 Mean
 Max
4.900 6.500 6.588 7.900
```

Each list element will be turned into a separate column:

```
as.data.frame(l) # as.data.frame.list
##
 setosa versicolor virginica
 4.900
Min
 4.300
 4.900
Median 5.000
 5.900
 6.500
Mean
 5.006
 5.936
 6.588
 5.800
Max
 7.000
 7.900
```

Sadly, **as.data.frame.list** is not particularly fond of lists of vectors of incompatible lengths:

```
as.data.frame(list(a=1, b=11:12, c=21:23))
Error in (function (..., row.names = NULL, check.rows = FALSE, check.names
= TRUE, : arguments imply differing number of rows: 1, 2, 3
```

The above vectors could have been recycled with a warning. But they were not.

```
as.data.frame(list(a=1:4, b=11:12, c=21)) # recycling rule okay

a b c

1 1 11 21

2 2 12 21

3 3 11 21

4 4 12 21
```

The method for the S3 class table (mentioned in Chapter 11) can be helpful as well. Here is an example contingency table together with its *unstacked* (wide) version.

```
(t <- table(mtcars[["vs"]], mtcars[["cyl"]]))</pre>
##
 4 6 8
##
##
 0 1 3 14
 1 10 4 0
##
as.data.frame(t) # as.data.frame.table; see the stringsAsFactors note below!
 Var1 Var2 Freq
1
 0
 4
 1
2
 1
 4
 10
3
 0
 6
 3
4
 1
 6
 4
 0
 8
5
 14
6
```

**as.data.frame.table** is so handy that we might want to call it directly on any array. This way, we can convert it from the wide format to the long (tall) one; see Section 12.3.6 for more details.

**Note** The above method is based on **expand.grid**, which determines all combinations of a given series of vectors.

```
expand.grid(1:2, c("a", "b", "c")) # see the stringsAsFactors note below!
##
 Var1 Var2
1
 1
2
 2
3
 1
 Ь
4
 2
 Ь
5
 1
 c
6
 2
 c
```

Overall, many classes of objects can be included<sup>2</sup> in a data frame. The popular choices include Date, POSIXct, and factor.

<sup>&</sup>lt;sup>2</sup> The attributes of objects stored as columns will generally be preserved (even if they are not displayed by **print**; see **str** though).

**Example 12.1** It is worth noting that **format** is used whilst printing the columns. Here is its custom method for what we would like to call from now on the S3 class spam:

```
format.spam <- function(x, ...)
paste0("<", x, ">")
```

Testing data frame printing:

#### 12.1.2 cbind.data.frame and rbind.data.frame

There are data frame-specific versions of **cbind** or **rbind** (which we discussed in the context of stacking matrices; Section 11.1.2). They are used quite eagerly: **help**("cbind") states that they will be referred to if at least<sup>3</sup> one of its arguments is a data frame, and the other arguments are atomic vectors or lists (possibly with the dim attribute). For example:

```
x <- iris[c(1, 51, 101), c("Sepal.Length", "Species")] # whatever
cbind(Yummy=c(TRUE, FALSE, TRUE), x)
Yummy Sepal.Length Species
1 TRUE 5.1 setosa
51 FALSE 7.0 versicolor
101 TRUE 6.3 virginica</pre>
```

It added a new column to a data frame x. Moreover:

It added a new row. Note that columns are of different types. Hence, the values to rowbind had to be provided as a list.

<sup>&</sup>lt;sup>3</sup> This is a clear violation of the rule that an S3 generic dispatches on the type of only one argument (usually: the first). It is an exception made for the sake of the questionable user *convenience*. Also, note that there is no **cbind.default** method available: it is hardcoded at the C language level.

The generic vector used as a new row specifier can also be named. It can consist of sequences of length greater than one that are given in any order:

```
rbind(x, list(
 Species=c("virginica", "setosa"),
 Sepal.Length=c(42, 7)
))
 Sepal.Length Species
##
 5.1
1
 setosa
51
 7.0 versicolor
101
 6.3 virginica
11
 42.0 virginica
2
 7.0
 setosa
```

A direct referral to **cbind.data.frame** and **rbind.data.frame** will sometimes be necessary. Consider an example list of atomic vectors:

```
x <- list(a=1:3, b=11:13, c=21:23)
```

First, we call the generic, which dispatches to the default method:

It created a matrix. If we want to ensure we garner a data frame, we need to write:

```
do.call(cbind.data.frame, x)
a b c
1 1 11 21
2 2 12 22
3 3 13 23
```

This is useful for fetching outputs from Map et al., as they are wrapped inside a list. Here is a fancy way to obtain an illustrative list:

```
str(l)
List of 3
$:List of 3
 ..$ Sepal.Length: num 5.01
 ..$ Sepal.Width : num 3.43
 : Factor w/ 3 levels "setosa", "versicolor",..: 1
##
 ..$ Species
$:List of 3
 ..$ Sepal.Length: num 5.94
##
 ..$ Sepal.Width : num 2.77
..$ Species
 : Factor w/ 3 levels "setosa", "versicolor",... 2
$:List of 3
##
 ..$ Sepal.Length: num 6.59
 ..$ Sepal.Width : num 2.97
##
 ..$ Species : Factor w/ 3 levels "setosa", "versicolor",...: 3
##
```

We may now turn it into a data frame by calling:

On the other hand, do.call(rbind, 1) does not return an amiable object type:

Despite the pretty face, it is a matrix... over a list:

```
str(do.call(rbind, l))
List of 9
$: num 5.01
$: num 5.94
$: num 6.59
$: num 3.43
$: num 2.77
$: num 2.97
$: Factor w/ 3 levels "setosa", "versicolor",..: 1
$: Factor w/ 3 levels "setosa", "versicolor",..: 2
$: Factor w/ 3 levels "setosa", "versicolor",..: 3
- attr(*, "dim")= int [1:2] 3 3
```

```
- attr(*, "dimnames")=List of 2
..$: NULL
..$: chr [1:3] "Sepal.Length" "Sepal.Width" "Species"
```

### 12.1.3 Reading data frames

Structured data can be imported from external sources, such as CSV/TSV (comma/tab-separated values) or HDF5 files, relational databases supporting SQL (see Section 12.1.4), web APIs (e.g., through the **curl** and **jsonlite** packages), spreadsheets [64], and so on.

In particular, **read.csv** and the like fetch data from plain text files consisting of records, where commas, semicolons, tabs, etc. separate the fields. For instance:

```
x <- data.frame(a=runif(3), b=c(TRUE, FALSE, TRUE)) # example data frame
f <- tempfile() # temporary file name
write.csv(x, f, row.names=FALSE) # export</pre>
```

It created a CSV file that looks like:

```
cat(readLines(f), sep="\n") # print file contents
"a","b"
0.287577520124614, TRUE
0.788305135443807, FALSE
0.4089769218117, TRUE
```

The above can be read by calling:

```
read.csv(f)

a b

1 0.28758 TRUE

2 0.78831 FALSE

3 0.40898 TRUE
```

**Exercise 12.2** Check out **help**("read. table") for a long list of tunable parameters, especially: sep, dec, quote, header, comment.char, and row.names. Further, note that reading from compressed files and interned URLs is supported directly.

**Important** CSV is the most portable and user-friendly format for exchanging matrix-like objects between different programs and computing languages (Python, Julia, LibreOffice Calc, etc.). Such files can be opened in any text editor.

Also, as mentioned in Section 8.3.5, we can process data frames chunk by chunk. This is beneficial especially when data do not fit into memory (compare the nrows argument to read.csv).

### 12.1.4 Interfacing relational databases and querying with SQL (\*)

The **DBI** package provides a universal interface for many database management systems whose drivers are implemented in add-ons such as **RSQLite**, **RMariaDB**, **RPostgr-eSQL**, etc., or, more generally, **RODBC** or **odbc**. For more details, see Section 4 of [64].

**Example 12.3** Let us play with an in-memory (volatile) instance of an SQLite database.

```
library("DBI")
con <- dbConnect(RSQLite::SQLite(), ":memory:")</pre>
```

It returned an object representing a database connection which we can refer to in further communication. An easy way to create a database table is to call:

```
dbWriteTable(con, "mtcars", mtcars) # `mtcars` is a toy data frame
```

Alternatively, **dbExecute** could have been called to send SQL statements such as "CREATE TABLE ..." followed by a series of "INSERT INTO ...". Some data retrieval can now follow:

It gave us an ordinary R data frame. We can process it in the same fashion as any other object of this kind.

At the end, the database connection must be closed.

```
dbDisconnect(con)
```

**Exercise 12.4** Database passwords must never be stored in plain text files, let alone in R scripts in version-controlled repositories. Consider a few ways to fetch credentials programmatically:

- using environment variables (see help("Sys.getenv")),
- using the keyring package,
- calling **system2** (Section 7.3.2) to retrieve it from the system keyring (e.g., the **keyring** package for Python provides a platform-independent command-line utility).

### 12.1.5 Strings as factors?

Some functions related to data frames automatically convert character vectors to factors. This behaviour is frequently controlled by and argument named stringsAs-Factors. It can be particularly problematic because, when printed, factor and character columns look identical:

```
(x <- data.frame(a=factor(c("U", "V")), b=c("U", "V")))
a b
1 U U
2 V V</pre>
```

We recall from Section 10.3.2 that factors can be nasty. For example, passing factors as indexers in `[` or converting them with as.numeric might give counterintuitive results. Also, when we want to extend factors by previously unobserved data, new levels must be added manually. This can cause unexpected behaviour in contexts such as:

Therefore, always having the data types checked is a praiseworthy habit. For instance:

```
str(x)
'data.frame': 2 obs. of 2 variables:
$ a: Factor w/ 2 levels "U","V": 1 2
$ b: chr "U" "V"
```

Before R 4.0, certain functions, including data.frame and read.csv had the stringsAsFactors argument defaulting to TRUE. It is no longer the case. However, exceptions to this rule still exist, e.g., including as.data.frame.table and expand.grid. Besides, some example data frames continue to enjoy factor-typed columns, e.g.:

```
class(iris[["Species"]])
[1] "factor"
```

In particular, adding a new flower variety might be oblique:

```
101 6.3 3.3 6 2.5 virginica
3 6 3 2 <NA>
```

Compare the above to:

```
levels(iris2[["Species"]])[nlevels(iris2[["Species"]])+1] <- "croatica"</pre>
rbind(iris2, c(6, 3, 3, 2, "croatica"))
##
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
1
 3.5
 1.4
 setosa
101
 6.3
 3.3
 6
 2.5 virainica
3
 6
 3
 3
 2 croatica
```

### 12.1.6 Internal representation

Objects of the S3 class data.frame are erected on lists of vectors of the same length or matrices with identical row counts. Each list element defines a column or column group.

Apart from class, data frames must be equipped with the following special attributes:

- names a character vector (as usual in any named list) that gives the column labels,
- row.names a character or integer vector with no duplicates nor missing values, doing what is advertised.

Therefore, a data frame can be created from scratch by calling, for example:

```
structure(
 list(a=11:13, b=21:23), # sets the `names` attribute
 row.names=1:3,
 class="data.frame"
)
a b
1 11 21
2 12 22
3 13 23
```

Here is a data frame based on a list of length five, a matrix with five rows, and a numeric vector with five items. We added some fancy row names on top:

```
class="data.frame"
)
##
 a b.u b.v
spam
 1 11 21 0.28758
bacon
 1, 2 12 22 0.78831
 1, 2, 3 13 23 0.40898
eggs
 14 24 0.88302
aubergine -4, -3, -2, -1 15 25 0.94047
```

In general, the columns of the type list can contain anything, e.g., other lists or R functions. Including atomic vectors of varying lengths, just like above, permits us to create something à la ragged arrays.

The issue with matrix entries, on the other hand, is that they appear as if they were many columns. Still, as it will turn out in the sequel, they are often treated as a single complex column, e.g., by the index operator (see Section 12.2). Therefore, from this perspective, the above data frame has three columns, not four. Such compound columns can be output by aggregate (see Section 12.3), amongst others. They are valuable in certain contexts: the column groups can be easily accessed as a whole and batchprocessed in the same way.

**Important** Alas, data frames with list or matrix columns cannot be created with the data.frame nor cbind functions. This might explain why they are less popular. This behaviour is dictated by the underlying as.data.frame methods, which they both call. As a curiosity, see help("I"), though.

**Exercise 12.5** Verify that if a data frame carries a matrix column, this matrix does not need to have any column names (the second element of dimnames).

The names and row.names attributes are special in the sense of Section 4.4.3. In particular, they can be accessed or modified via the dedicated functions.

It is worth noting that row.names(df) always returns a character vector, even when attr(df, "row.names") is integer. Further, calling "row.names(df) <- NULL" will reset<sup>4</sup> this attribute to the most commonly desired case of consecutive natural numbers. For example:

```
(x \leftarrow iris[c(1, 51, 101),]) # comes with some sad row names
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
1
 5.1
 3.5
 1.4
 0.2
 setosa
 4.7
51
 7.0
 3.2
 1.4 versicolor
101
 6.3
 3.3
 6.0
 2.5 virainica
```

(continues on next page)

<sup>&</sup>lt;sup>4</sup> `attr<-`(df, "row.names", value) does not run the same sanity checks as `row.names<-`(df, value). For instance, it is easy to corrupt a data frame by setting too short a row.names attribute.

```
`row.names<-`(x, NULL) # reset to seq_len(NROW(x))
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
 3.5
 1.4
1
 5.1
 setosa
2
 7.0
 3.2
 4.7
 1.4 versicolor
 3.3
3
 6.3
 6.0
 2.5 virginica
```

**Exercise 12.6** Implement your version of **expand.grid**.

**Exercise 12.7** Write a version of **xtabs** that does not rely on a formula interface (compare Section 10.3.4). Allow three parameters: a data frame, the name of the "counts" column, and the names of the cross-classifying factors. Hence, **my\_xtabs**(x, "Freq", **c**("Var1", "Var2")) should be equivalent to **xtabs**(Freq~Var1+Var2, x).

# 12.2 Data frame subsetting

#### 12.2.1 Data frames are lists

A data frame is a named list whose elements represents individual columns. Therefore<sup>5</sup>, **length** yields the number of columns and **names** gives their respective labels.

Let us play with the following data frame:

```
(x <- data.frame(</pre>
 a=runif(6),
 b=rnorm(6),
 c=LETTERS[1:6],
 d1=c(FALSE, TRUE, FALSE, NA, FALSE, NA),
 d2=c(FALSE, TRUE, FALSE, TRUE, FALSE, TRUE)
))
##
 b c
 d1
1 0.287578 0.070508 A FALSE FALSE
2 0.788305 0.129288 B TRUE
3 0.408977 1.715065 C FALSE FALSE
 NA TRUE
4 0.883017 0.460916 D
5 0.940467 -1.265061 E FALSE FALSE
6 0.045556 -0.686853 F
 NA TRUE
typeof(x) # each data frame is a list
[1] "list"
length(x) # the number of columns
```

(continues on next page)

<sup>&</sup>lt;sup>5</sup> This is a strong word. This implication relies on an implicit assumption that the primitive functions **length** and **names** have not been contaminated by treating data frames differently from named lists. Luckily, that is indeed not the case. Even though we have the index operators specially overloaded for the data. frame class, they behave quite reasonably. As we will see, they support a mix of list- and matrix-like behaviours.

```
[1] 5
names(x) # column labels
[1] "a" "b" "c" "d1" "d2"
```

The one-argument versions of extract and index operators behave as expected. `[[` fetches (looks inside) the contents of a given column:

```
x[["a"]] # or x[[1]]
[1] 0.287578 0.788305 0.408977 0.883017 0.940467 0.045556
```

`[` returns a data frame (a list with extras):

```
x["a"] # or x[1]; a data frame with one column

a

1 0.287578

2 0.788305

3 0.408977

4 0.883017

5 0.940467

6 0.045556

x[c(TRUE, TRUE, FALSE, TRUE, FALSE)]

a b d1

1 0.287578 0.070508 FALSE

2 0.788305 0.129288 TRUE

3 0.408977 1.715065 FALSE

4 0.883017 0.460916 NA

5 0.940467 -1.265061 FALSE

6 0.045556 -0.686853 NA
```

Just like with lists, the replacement versions of these operators can add new columns or modify existing ones.

```
(y <- head(x, 1)) # example data frame
a b c d1 d2
1 0.28758 0.070508 A FALSE FALSE
y[["a"]] <- round(y[["a"]], 1) # replaces the column with new content
y[["b"]] <- NULL # removes the column, like, totally
y[["e"]] <- 10*y[["a"]]^2 # adds a new column at the end
print(y)
a c d1 d2 e
1 0.3 A FALSE FALSE 0.9</pre>
```

**Example 12.8** Some spam for thought to show how much we already know. Here are a few common scenarios involving indexing.

```
(y <- head(x, 1)) # example data frame
a b c d1 d2
1 0.28758 0.070508 A FALSE FALSE
```

Move the column a to the end:

```
y[unique(c(names(y), "a"), fromLast=TRUE)]
b c d1 d2 a
1 0.070508 A FALSE FALSE 0.28758
```

Remove the columns a and c:

```
y[-match(c("a", "c"), names(y))] # or y[setdiff(names(y), c("a", "c"))]
b d1 d2
1 0.070508 FALSE FALSE
```

Select all columns between a and c:

Fetch the columns with names starting with d:

```
y[grep("^d", names(y), perl=TRUE)]
d1 d2
1 FALSE FALSE
```

Change the name of column c to z:

Change names: d2 to u and d1 to v:

**Note** Some users prefer the `\$` operator over `[[`, but we do not. By default, the former supports partial matching of column names which might be appealing when R is used interactively. Nonetheless, it does not work on matrices nor it allows for

programmatically generated names. It is also trickier to use on not syntactically valid labels; compare Section 9.3.1.

**Exercise 12.9** Write a function **rename** that changes the names of columns based on a translation table given in a from=to fashion (we have already solved a similar exercise in Chapter 9). For instance:

```
rename <- function(x, ...) ...to.do...

rename(head(x, 1), c="new_c", a="new_a")

new_a b new_c d1 d2

1 0.28758 0.070508 A FALSE FALSE
```

#### 12.2.2 Data frames are matrix-like

Data frames can be considered "generalised" matrices. They store data of any kind (possibly mixed) organised in a *tabular* fashion. A few functions mentioned in the previous chapter are overloaded for the data frame case. They include: dim (despite the lack of the dim attribute), NROW, NCOL, and dimnames (which is, of course, based on row. names and names). For example:

```
(x <- data.frame(</pre>
 a=runif(6),
 b=rnorm(6).
 c=LETTERS[1:6],
 d1=c(FALSE, TRUE, FALSE, NA, FALSE, NA),
 d2=c(FALSE, TRUE, FALSE, TRUE, FALSE, TRUE)
))
##
 bc d1
1 0.287578 0.070508 A FALSE FALSE
2 0.788305 0.129288 B TRUE TRUE
3 0.408977 1.715065 C FALSE FALSE
4 0.883017 0.460916 D NA TRUE
5 0.940467 -1.265061 E FALSE FALSE
6 0.045556 -0.686853 F NA TRUE
dim(x) # the number of rows and columns
[1] 6 5
dimnames(x) # row and column labels
[[1]]
[1] "1" "2" "3" "4" "5" "6"
##
[[2]]
[1] "a" "b" "c" "d1" "d2"
```

In addition to the list-like behaviour, which only allows for dealing with particular columns or their groups, the `[` operator can also take two indexers:

```
x[1:2,] # first two rows

a b c d1 d2

1 0.28758 0.070508 A FALSE FALSE

2 0.78831 0.129288 B TRUE TRUE

x[x[["a"]] >= 0.3 & x[["a"]] <= 0.8, -2] # or use x[, "a"]

a c d1 d2

2 0.78831 B TRUE TRUE

3 0.40898 C FALSE FALSE
```

Recall the drop argument to `[` and its effects on matrix indexing (Section 11.2.4). In the current case, its behaviour will be similar with regard to the operations on individual columns:

When we extract a single row and more than one column, drop does not apply. It is because columns (unlike in matrices) can potentially be of different types:

```
x[1, 1:2] # two numeric columns but the result is still a numeric
a b
1 0.28758 0.070508
```

#### However:

```
x[1, 1] # a single value
[1] 0.28758
x[1, 1, drop=FALSE] # a data frame with one row and one column
a
1 0.28758
```

**Note** Once again, let us take note of logical indexing in the presence of missing values:

The default behaviour is consistent with many other R functions. It explicitly indicates that something is missing. After all, when we select a "don't know", the result is unknown as well. Regretfully, this comes with no warning. As we rarely manually check missing values in the outputs, our absent-mindedness can lead to code bugs.

By far, we might have already noted that the index operator adjusts (not: resets) the row.names attribute. For instance:

It is a version of x comprised of the top three values in the a column. Indexing by means of character vectors will refer to row.names and names:

```
xs["5", c("a", "b")]
a b
5 0.94047 -1.2651
```

It is not the same as xs[5, c("a", "b")], even though row.names is formally an integer vector here.

Regarding the replacement version of the two-indexer variant of the `[` operator, it is a quite flexible tool. It permits the new content to be a vector, a data frame, a list, or even a matrix. Verifying this is left as an exercise.

**Note** If a data frame carries a matrix, to access a specific sub-column, we need to use the index/extract operator twice:

In other words, neither x[["Sepal.Length.Min"]] nor x[, "Sepal.Length.Min"] works.

**Exercise 12.10** Write two replacement functions<sup>6</sup>. First, author **set\_row\_names** which replaces the row.names of a data frame with the contents of a specific column. For example:

```
(x <- aggregate(iris[1], iris[5], mean)) # an example data frame
 Species Sepal.Length
##
1
 setosa
2 versicolor
 5.936
3 virginica
 6.588
set_row_names(x) <- "Species"</pre>
print(x)
##
 Sepal.Length
setosa
 5.006
versicolor
 5.936
virginica
 6.588
```

Second, implement **reset\_row\_names** which converts row.names to a standalone column of a given name. For instance:

```
reset_row_names(x) <- "Type"
print(x)
Sepal.Length Type
1 5.006 setosa
2 5.936 versicolor
3 6.588 virginica</pre>
```

These two functions may be handy for they enable writing x[something, ] instead of x[x[["column"]] %in% something, ].

# 12.3 Common operations

Below we review the most commonly applied operations related to data frame wrangling. We have a few dedicated functions or methods overloaded for the data. frame class. However, we have already mastered most skills to deal with such objects effectively. Let us repeat: data frames are just lists exhibiting matrix-like behaviour.

# 12.3.1 Ordering rows

Ordering rows in a data frame with respect to different criteria can be easily achieved through the **order** function and the two-indexer version of `[`.

<sup>&</sup>lt;sup>6</sup> (\*) Compare pandas.DataFrame.set\_index and pandas.DataFrame.reset\_index in Python.

For instance, here are the six fastest cars from mtcars in terms of the time (in seconds) to complete a 402-metre race:

```
mtcars6 <- mtcars[order(mtcars[["qsec"]])[1:6], c("qsec", "cyl", "gear")]</pre>
(mtcars6 <- `row.names<-`(cbind(model=row.names(mtcars6), mtcars6), NULL))</pre>
 model qsec cyl gear
1 Ford Pantera L 14.50
2 Maserati Bora 14.60
 5
3
 Camaro Z28 15.41
 3
 8
4 Ferrari Dino 15.50
 5
 6
 Duster 360 15.84
 3
5
 8
6
 Mazda RX4 16.46
```

**order** uses a stable sorting algorithm. Therefore, any sorting with respect to a different criterion will not break the *relative* ordering of qsec in row groups with ties:

```
mtcars6[order(mtcars6[["cyl"]]),]
##
 model asec cyl gear
 Ferrari Dino 15.50
4
 6
 Mazda RX4 16.46
6
 4
1 Ford Pantera L 14.50
 8
 5
2 Maserati Bora 14.60
 5
 Camaro Z28 15.41
 3
3
 8
 Duster 360 15.84
5
 3
```

qsec is still increasing in each of the two cyl groups.

**Example 12.11** Notice the difference between ordering by cyl and gear:

```
mtcars6[order(mtcars6[["cyl"]], mtcars6[["gear"]]),]
##
 model qsec cyl gear
6
 Mazda RX4 16.46
 Ferrari Dino 15.50
 5
4
 6
 Camaro Z28 15.41
 3
3
5
 Duster 360 15.84 8
 .3
1 Ford Pantera L 14.50
 5
2 Maserati Bora 14.60
 5
```

vs gear and cyl:

```
mtcars6[order(mtcars6[["gear"]], mtcars6[["cyl"]]),]
##
 model gsec cyl gear
3
 Camaro Z28 15.41
 Duster 360 15.84
 3
5
 8
 6
6
 Mazda RX4 16.46
 4
 Ferrari Dino 15.50
 5
4
 6
1 Ford Pantera L 14.50
 5
 8
2 Maserati Bora 14.60
 5
```

**Note** Mixing increasing and decreasing ordering is tricky as the decreasing argument to **order** currently does not accept multiple flags in all the contexts. Perhaps the easiest way to change the ordering direction is to use the unary minus operator on the column(s) to be sorted decreasingly.

```
mtcars6[order(mtcars6[["gear"]], -mtcars6[["cyl"]]),]
##
 model qsec cyl gear
3
 Camaro Z28 15.41
 Duster 360 15.84
5
 3
6
 Mazda RX4 16.46
1 Ford Pantera L 14.50
 5
2 Maserati Bora 14.60
 5
4 Ferrari Dino 15.50
 5
```

For factor and character columns, **xtfrm** can convert them to sort keys first.

```
mtcars6[order(mtcars6[["cyl"]], -xtfrm(mtcars6[["model"]])),]
##
 model qsec cyl gear
6
 Mazda RX4 16.46
4
 Ferrari Dino 15.50
 5
2 Maserati Bora 14.60
 5
1 Ford Pantera L 14.50
 5
5
 Duster 360 15.84
 8
 3
3
 3
 Camaro Z28 15.41
```

Both of the above behave *like* the unsupported decreasing=**c**(FALSE, TRUE).

**Exercise 12.12** Write a method **sort.data.frame** that orders a data frame with respect to a given set of columns.

```
sort.data.frame <- function(x, decreasing=FALSE, cols) ...to.do...</pre>
sort(mtcars6, cols=c("cyl", "model"))
##
 model gsec cyl gear
 Ferrari Dino 15.50
4
6
 Mazda RX4 16.46
 4
3
 Camaro Z28 15.41
 3
 Duster 360 15.84
 3
1 Ford Pantera L 14.50
 5
2 Maserati Bora 14.60
 5
```

Unfortunately, that decreasing must be of length one and be placed as the second argument is imposed by the **sort** S3 generic.

**duplicated**, **anyDuplicated**, and **unique** have methods overloaded for the data.frame class. They can be used to indicate, get rid of, or replace the repeating rows.

### 12.3.3 Joining (merging) data frames

The **merge** function can perform the *join* operation that some readers might know from SQL<sup>7</sup>. It matches the items in the columns that two given data frames somewhat share. Then, it returns the combination of the corresponding rows.

**Example 12.13** Two calls to *merge* could be used to match data on programmers (each identified by developer\_id and giving such details as their name, location, main skill, etc.) with the information about the open-source projects (each identified by project\_id and informing us about its title, scope, website, and so forth) they are engaged in (based on a third data frame defining developer id and project id pairs).

As a simple illustration, consider the two following objects:

```
A <- data.frame(
 u=c("b0", "b1", "b2", "b3"),
 v=c("a0", "a1", "a2", "a3")
)

B <- data.frame(
 v=c("a0", "a2", "a2", "a4"),
 w=c("c0", "c1", "c2", "c3")
)</pre>
```

The two *common* columns, i.e., storing data of similar nature (a-something strings), are both named v.

First is the inner (natural) join, where we list only the matching pairs:

```
merge(A, B) # x=A, y=B, by="v", all.x=FALSE, all.y=FALSE
v u w
1 a0 b0 c0 (continues on next page)
```

<sup>&</sup>lt;sup>7</sup> Join is the reverse operation to data normalisation from relational database theory. It reduces data redundancy and increases their integrity. What data scientists need in data analysis, visualisation, and processing activities is sometimes the opposite of what the art of data management focuses on, i.e., efficient collection and storage of information. The readers are encouraged to learn about various normalisation forms from, e.g., [16] or any other course covering this topic.

```
2 a2 b2 c1
3 a2 b2 c2
```

The common column is included in the result only once.

Next, the *left join* guarantees that all elements in the first data frame will be included in the result:

The right join includes all records in the second argument:

```
merge(A, B, all.y=TRUE) # by="v", all.x=FALSE

v u w

1 a0 b0 c0

2 a2 b2 c1

3 a2 b2 c2

4 a4 <NA> c3
```

Lastly, the full outer join is their set-theoretic union:

Joining on more than one common column is also supported.

**Exercise 12.14** Show how match (Section 5.4.1) can help author a very basic version of merge.

**Exercise 12.15** Implement a version of match that allows the x and table arguments to be data frames with the same number of columns so that also the matching of pairs, triples, etc. is possible.

# 12.3.4 Aggregating and transforming columns

It might be tempting to try aggregating data frames with apply. Sadly, currently, this function coerces its argument to a matrix. Hence, we should refrain from applying it

### **Example 12.16** Let us consider an example data frame:

```
(iris_sample <- iris[sample(NROW(iris), 6),])</pre>
##
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
 5.2
 3.5
 1.5
28
 0.2
 setosa
80
 5.7
 2.6
 3.5
 1.0 versicolor
101
 6.3
 3.3
 6.0
 2.5 virginica
111
 6.5
 3.2
 5.1
 2.0 virginica
 6.3
 3.4
 5.6
 2.4 virginica
137
133
 6.4
 2.8
 5.6
 2.2 virginica
```

To get the class of each column, we can call:

```
sapply(iris_sample, class) # or unlist(Map(class, iris))
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
"numeric" "numeric" "numeric" "factor"
```

Next, here is a way to compute some aggregates of the numeric columns:

```
unlist(Map(mean, Filter(is.numeric, iris_sample)))
Sepal.Length Sepal.Width Petal.Length Petal.Width
6.0667 3.1333 4.5500 1.7167
```

or:

```
sapply(iris_sample[sapply(iris_sample, is.numeric)], mean)
Sepal.Length Sepal.Width Petal.Length Petal.Width
6.0667 3.1333 4.5500 1.7167
```

We can also fetch more than a single summary of each column:

```
as.data.frame(Map(
 function(x) c(Min=min(x), Max=max(x)),
 Filter(is.numeric, iris_sample)
))
 Sepal.Length Sepal.Width Petal.Length Petal.Width
##
Min
 5.2
 2.6
 1.5
 0.2
Max
 6.5
 3.5
 6.0
 2.5
```

or:

```
sapply(iris_sample[sapply(iris_sample, is.numeric)], quantile, c(0, 1))
Sepal.Length Sepal.Width Petal.Length Petal.Width
0% 5.2 2.6 1.5 0.2
100% 6.5 3.5 6.0 2.5
```

The latter called **simplify2array** automatically. Thus, the result is a matrix.

On the other hand, the standardisation of all numeric features can be performed, e.g., via a call:

```
iris_sample[] <- Map(function(x) {</pre>
 if (!is.numeric(x)) x else (x-mean(x))/sd(x)
}, iris_sample)
print(iris_sample)
 Sepal.Length Sepal.Width Petal.Length Petal.Width
 Species
28
 -1.70405
 1.03024
 -1.76004
 -1.65318
 setosa
80
 -0.72094
 -1.49854
 -0.60591
 -0.78117 versicolor
 0.45878
 0.46829
 0.83674
 0.85384 virginica
101
111
 0.85202
 0.18732
 0.31738
 0.30884 virginica
 0.74484 virainica
137
 0.45878
 0.74927
 0.60591
133
 0.65540
 -0.93659
 0.60591
 0.52684 virainica
```

### 12.3.5 Handling missing values

The is.na method for objects of the class data. frame returns a logical matrix of the same dimensionality<sup>8</sup>, indicating whether the corresponding items are missing or not. Of course, the default method can still be called on individual columns.

Further, **na.omit** gets rid of *rows* with missing values.

**Exercise 12.17** Given a data frame, use **is.na** and other functions such as **apply** or **approx** to:

- 1. remove all rows that bear at least one missing value,
- 2. remove all rows that only consist of missing values,
- 3. remove all columns that carry at least one missing value,
- 4. for each column, replace all missing values with the column averages,
- 5. for each column, replace all missing values with values that linearly interpolate between the preceding and succeeding well-defined observations (which is of use in time series processing), e.g., the blanks in c(0.60, 0.62, NA, 0.64, NA, NA, 0.58) should be filled to obtain c(0.60, 0.62, 0.63, 0.64, 0.62, 0.60, 0.58).

# 12.3.6 Reshaping data frames

Consider an example matrix:

<sup>(</sup>continues on next page)

<sup>&</sup>lt;sup>8</sup> Provided that a data frame does not carry a matrix column.

```
names(dimnames(A)) <- c("Row", "Col")
print(A)
Col
Row u v
X 0.29 0.88
Y 0.79 0.94
Z 0.41 0.05</pre>
```

The as.data.frame method for the table class can be called directly on any array-like object:

```
as.data.frame.table(A, responseName="Val", stringsAsFactors=FALSE)

Row Col Val

1 X u 0.29

2 Y u 0.79

3 Z u 0.41

4 X v 0.88

5 Y v 0.94

6 Z v 0.05
```

It is an instance of array *reshaping*. More precisely, we call it *stacking*. We converted from a *wide* (okay, in this example, not so wide, as we only have two columns) to a *long* (tall) format.

The above can also be achieved by means of the **reshape** function which is more flexible and operates directly on data frames (but is harder to use):

```
(df <- `names<-`(
 data.frame(row.names(A), A, row.names=NULL),
 c("Row", "Col.u", "Col.v")))
##
 Row Col.u Col.v
1 X 0.29 0.88
 Y 0.79 0.94
2
3 Z 0.41 0.05
(stacked <- reshape(df, varying=2:3, direction="long"))</pre>
 Row time Col id
##
1.u
 X
 и 0.29 1
2.u
 u 0.79 2
3.u Z
 u 0.41 3
1.v X
 v 0.88 1
2.v Y
 v 0.94 2
3.v Z
 v 0.05 3
```

Maybe the default column names are not superb, but we can adjust them manually afterwards.

The reverse operation is called *unstacking*:

```
reshape(stacked, idvar="Row", timevar="time", drop="id", direction="wide")
Row Col.u Col.v
1.u X 0.29 0.88
2.u Y 0.79 0.94
3.u Z 0.41 0.05
```

**Exercise 12.18** Given a named numeric vector, convert it to a data frame with two columns. For instance:

```
convert <- function(x) ...to.do...
x <- c(spam=42, eggs=7, bacon=3)
convert(x)
key value
1 spam 42
2 eggs 7
3 bacon 3</pre>
```

**Exercise 12.19** Stack the WorldPhones dataset. Then, unstack it back. Furthermore, unstack the stacked set but first remove<sup>9</sup> five random rows from it and then randomly permute all the remaining rows. Fill in the missing entries with NAs.

**Exercise 12.20** Implement a basic version of **as.data.frame.table** manually (using **rep** etc.). Also, write a function **as.table.data.frame** that computes its reverse. Make sure both functions are compatible with each other.

**Exercise 12.21** *Titanic* is a four-dimensional array. Convert it to a long data frame.

**Exercise 12.22** *Perform what follows on the data frame defined below:* 

- 1. convert the second column to a list of character vectors (split at ", ");
- 2. extract the first elements from each of such vectors;
- 3. extract the last elements:
- 4. (\*) unstack the split data frame;
- 5. (\*) stack it back to a data frame that carries a list;
- 6. convert the list back to a character column (concatenate with ", " as separator).

(continues on next page)

<sup>9</sup> The original dataset can be thought of as representing a fully crossed design experiment (all combinations of two grouping variables are present). Its truncated version is like an incomplete crossed design.

```
3 Jo
4 Mary eggs,spam,spam,lollipops
```

**Exercise 12.23** Write a function that converts all matrix-based columns in a given data frame to separate atomic columns. Furthermore, author a function that does the opposite, i.e., groups all columns with similar prefixes and turns them into matrices.

### 12.3.7 Aggregating data in groups

We can straightforwardly apply various transforms on data groups determined by a factor-like variable or their combination thanks to the **split.data.frame** method, which returns a list of data frames. For example:

```
x <- data.frame(</pre>
 40,
 20,
 30,
 50),
 u=c("spam", "spam", "eggs", "spam", "eggs"),
 1,
 2,
 1,
)
split(x, x["u"]) # i.e., split.data.frame(x, x["u"]) or x[["u"]]
$eggs
##
 a uv
3 30 eggs 1
5 50 eggs 1
##
$spam
a u v
1 10 spam 1
2 20 spam 2
4 40 spam 1
```

It split x with respect to the u column, which served as the grouping variable. On the other hand:

```
split(x, x[c("u", "v")]) # sep="."
$eggs.1
a u v
3 30 eggs 1

$spam.1
a u v
1 10 spam 1
4 40 spam 1

$eggs.2
```

(continues on next page)

```
[1] a u v
<0 rows> (or 0-length row.names)
##
$spam.2
a u v
2 20 spam 2
```

It partitioned with respect to a combination of two factor-like sequences. A nonexistent level pair (eggs, 2) resulted in an empty data frame.

**Exercise 12.24** split.data.frame (when called directly) can also be used to break a matrix into a list of matrices (rowwisely). Given a matrix, perform its train-test split: allocate, say, 70% of the rows at random into one matrix and the remaining 30% into another.

sapply is quite convenient if we need to aggregate grouped numeric data. To recall, it is a combination of lapply (one-vector version of Map) and simplify2array (Section 11.1.3).

If the function to apply returns more than a single value, **sapply** will not return too informative a result. The list of matrices converted to a matrix will not have the row. names argument set:

```
MinMax <- function(x) c(Min=min(x), Max=max(x))</pre>
sapply(split(iris[1:2], iris[5]), sapply, MinMax)
 setosa versicolor virainica
[1,]
 4.3
 4.9
 4.9
[2,]
 5.8
 7.0
 7.9
[3,]
 2.3
 2.0
 2.2
[4.]
 4.4
 3.4
 3.8
```

As a workaround, we either call **simplify2array** explicitly, or pass simplify="array" to **sapply**:

```
(res <- sapply(
 split(iris[1:2], iris[5]),
 sapply,
 MinMax,
 simplify="array"
)) # or simplify2array(lapply(...) or Map(...) etc.)
, , setosa
##</pre>
```

```
Sepal.Length Sepal.Width
##
Min
 4.3
 2.3
 5.8
 4.4
Max
##
, , versicolor
##
##
 Sepal.Length Sepal.Width
Min
 4.9
 2.0
 7.0
 3.4
Max
##
, , virginica
##
##
 Sepal.Length Sepal.Width
 4.9
 2.2
Min
Max
 7.9
 3.8
```

It produced a three-dimensional array, which is particularly handy if we now wish to access specific results by name:

```
res[, "Sepal.Length", "setosa"]
Min Max
4.3 5.8
```

The previously mentioned **as.data.frame.table** method will work on it like a charm (up to the column names, which we can change):

```
as.data.frame.table(res, stringsAsFactors=FALSE)
 Var2
##
 Var1
 Var3 Frea
1 Min Sepal.Length
 setosa 4.3
 setosa 5.8
2 Max Sepal.Length
3 Min Sepal.Width
 setosa 2.3
4 Max Sepal.Width
 setosa 4.4
5 Min Sepal.Length versicolor 4.9
6 Max Sepal.Length versicolor 7.0
7 Min Sepal.Width versicolor 2.0
8 Max Sepal.Width versicolor 3.4
9 Min Sepal.Length virginica 4.9
10 Max Sepal.Length virginica 7.9
11 Min Sepal.Width virginica 2.2
12 Max Sepal.Width virginica 3.8
```

**Note** If the grouping (by) variable is a list of two or more factors, the combined levels will be concatenated to a single string. This behaviour yields a result that may be deemed convenient in some contexts but not necessarily so in other ones.

The name of the aggregated column (len) has been included, because **sapply** simplifies the result to a flat vector too eagerly.

**aggregate** can assist us when a single function is to be applied on all columns in a data frame.

```
aggregate(iris[-5], iris[5], mean) # neither iris[[5]] nor iris[, 5]
##
 Species Sepal.Length Sepal.Width Petal.Length Petal.Width
 5.006
1
 setosa
 3.428
 1.462
 0.246
2 versicolor
 5.936
 4.260
 1.326
 2.770
 2.026
3 virginica
 6.588
 2.974
 5.552
aggregate(ToothGrowth["len"], ToothGrowth[c("supp", "dose")], mean)
 supp dose
 len
 OJ 0.5 13.23
1
 VC 0.5 7.98
2
 OJ 1.0 22.70
3
4 VC 1.0 16.77
5
 OJ 2.0 26.06
6
 VC 2.0 26.14
```

The second argument, by, must be list-like (this includes data frames). Neither a factor nor an atomic vector is acceptable. Also, if the function being applied returns many values, they will be wrapped into a matrix column:

(continues on next page)

```
Min Max
##
[1,] 2.3 4.4
[2,] 2.0 3.4
[3,] 2.2 3.8
```

It is actually handy: by referring to x[["Sepal.Width"]], we access all the stats for this column. Further, if many columns are being aggregated simultaneously, we can process all the summaries in the same way.

**Exercise 12.25** Check out the **by** function, which supports basic split-apply-bind use cases. Note the particularly peculiar behaviour of the **print** method for the by class.

The most flexible scenario involves applying a custom function returning any set of aggregates in the form of a list and then row-binding the results to obtain a data frame.

**Example 12.26** The following implements an R version of what we would express in SQL as:

```
SELECT supp, dose, AVG(len) AS ave_len, COUNT(*) AS count
FROM ToothGrowth
GROUP BY supp, dose
```

Ad rem:

```
do.call(rbind.data.frame, lapply(
 split(ToothGrowth, ToothGrowth[c("supp", "dose")]),
 function(df) list(
 supp=df[1, "supp"],
 dose=df[1, "dose"],
 ave_len=mean(df[["len"]]),
 count=NROW(df)
)
))
 supp dose ave len count
##
0J.0.5 0J 0.5 13.23
 10
VC.0.5 VC 0.5 7.98
 10
 OJ 1.0 22.70
0J.1
 10
VC.1
 VC 1.0 16.77
 10
0J.2
 OJ 2.0 26.06
 10
 VC 2.0 26.14
VC.2
 10
```

**Exercise 12.27** Many aggregation functions are idempotent, which means that when they are fed with a vector with all the elements being identical, the result is exactly that unique element: min, mean, median, and max behave this way.

Overload the mean and median methods for character vectors and factors. They should return NA and give a warning for sequences where not all elements are the same. Otherwise, they are expected to output the unique value.

```
mean.character <- function(x, na.rm=FALSE, ...) ...to.do...
mean.factor <- function(x, na.rm=FALSE, ...) ...to.do...
```

This way, we can also aggregate the grouping variables conveniently:

**Example 12.28** As an exercise, let us study a function that takes a named list x (can be a data frame) and a sequence of col=f pairs and applies the function f (or each function from a list of functions f) on the element named col in x:

```
napply \leftarrow function(x, ...)
{
 fs <- list(...)
 cols <- names(fs)</pre>
 stopifnot(is.list(x), !is.null(names(x)))
 stopifnot(all(cols %in% names(x)))
 do.call(
 c, # concatenates lists
 lapply(
 structure(seg along(fs), names=cols),
 function(i)
 { # always returns a list
 y <- x[[cols[i]]]</pre>
 if (is.function(fs[[i]]))
 list(fs[[i]](y))
 else
 lapply(fs[[i]], function(f) f(y))
 }
)
)
}
```

For example:

```
first \leftarrow function(x, ...) head(x, n=1L, ...) # helper function napply(ToothGrowth, supp=first, dose=first, len=list(ave=mean, count=length) (continues on next page)
```

```
$supp
[1] VC
Levels: 0J VC
##
$dose
[1] 0.5
##
$len.ave
[1] 18.813
##
$len.count
[1] 60
```

It applied **first** on both ToothGrowth[["supp"]] and ToothGrowth[["dose"]] as well as **mean** and **length** on ToothGrowth[["len"]]. We included list names for a more dramatic effect. And now:

```
do.call(
 rbind.data.frame,
 lapply(
 split(ToothGrowth, ToothGrowth[c("supp", "dose")]),
 napply,
 supp=first, dose=first, len=list(ave=mean, count=length)
)
)
 supp dose len.ave len.count
##
0J.0.5 0J 0.5 13.23
 10
VC.0.5 VC 0.5
 7.98
 10
0J.1
 OJ 1.0 22.70
 10
VC.1
 VC 1.0 16.77
 10
 OJ 2.0
OJ.2
 26.06
 10
VC.2
 VC 2.0
 26.14
 10
```

or even:

(continues on next page)

```
...
))
```

And now:

```
gapply(iris, "Species", Sepal.Length=mean, Sepal.Width=list(min, max))
 Species Sepal.Length Sepal.Width1 Sepal.Width2
 5.006
 2.3
setosa
 setosa
 4.4
versicolor versicolor
 5.936
 2.0
 3.4
virginica
 virginica
 6.588
 2.2
 3.8
gapply(ToothGrowth, c("supp", "dose"), len=list(ave=mean, count=length))
 supp dose len.ave len.count
0J.0.5
 OJ 0.5
 13.23
VC.0.5
 VC 0.5
 7.98
 10
0J.1
 OJ 1.0 22.70
 10
VC.1
 VC 1.0 16.77
 10
OJ.2
 OJ 2.0
 26.06
 10
VC.2
 VC 2.0
 26.14
 10
```

This brings fun back to R programming in the sad times when many things are given to us on a plate (the thorough testing of the above is left as an exercise).

**Example 12.29** In Section 10.4, we mentioned (without giving the implementation) the **group\_by** function returning a list of the class list\_dfs. It splits a data frame into a list of data frames with respect to a combination of levels in given named columns:

```
group_by <- function(df, by)
{
 stopifnot(is.character(by), is.data.frame(df))
 df <- droplevels(df) # factors may have unused levels
 structure(
 split(df, df[names(df) %in% by]),
 class="list_dfs",
 by=by
)
}</pre>
```

The next function applies a set of aggregates on every column of each data frame in a given list (two nested *lapply*s plus cosmetic additions):

```
aggregate.list_dfs <- function(x, FUN, ...)
{
 aggregates <- lapply(x, function(df) {
 is_by <- names(df) %in% attr(x, "by")
 res <- lapply(df[!is_by], FUN, ...)
 res_mat <- do.call(rbind, res)
 (continues on next page)</pre>
```

```
if (is.null(dimnames(res_mat)[[2]]))
 dimnames(res_mat)[[2]] <- paste0("f", seq_len(NCOL(res_mat)))</pre>
 cbind(
 `row.names<-`(df[1, is_by, drop=FALSE], NULL),
 x=row.names(res mat).
 `row.names<-`(res_mat, NULL)
 7)
 combined_aggregates <- do.call(rbind.data.frame, aggregates)</pre>
 `row.names<-`(combined_aggregates, NULL)
}
aggregate(group_by(ToothGrowth, c("supp", "dose")), range)
 supp dose x f1 f2
1 OJ 0.5 len 8.2 21.5
2 VC 0.5 len 4.2 11.5
3 OJ 1.0 len 14.5 27.3
 VC 1.0 len 13.6 22.5
4
5 OJ 2.0 len 22.4 30.9
6 VC 2.0 len 18.5 33.9
```

We really want our API to be bloated. Hence, let us introduce a convenience function, which is a specialised version of the above:

```
mean.list_dfs <- function(x, ...)</pre>
 aggregate.list_dfs(x, function(y) c(Mean=mean(y, ...)))
mean(group_by(iris[51:150, c(2, 3, 5)], "Species"))
 Species
1 versicolor Sepal.Width 2.770
2 versicolor Petal.Length 4.260
3 virginica Sepal.Width 2.974
4 virginica Petal.Length 5.552
```

#### Transforming data in groups 12.3.8

Variables will sometimes need to be transformed relative to what is happening in a dataset's subsets. This is the case, e.g., where we decide that missing values should be replaced by the corresponding within-group averages or want to compute the relative ranks or z-scores.

If the loss of the original ordering of rows is not an issue, the standard split-apply-bind will suffice. Here is an example data frame:

```
(x <- data.frame(</pre>
 a=c(10, 1, NA, NA, NA,
 4),
 b=c(-1, 10, 40, 30,
 1,
 20),
 (continues on next page)
```

```
c=runif(6),
 d=c("v", "u", "u", "v", "u")
))
a b c d
1 10 -1 0.52811 v
2 1 10 0.89242 u
3 NA 40 0.55144 u
4 NA 30 0.45661 u
5 NA 1 0.95683 v
6 4 20 0.45333 u
```

Some operations:

And now:

```
x_groups <- lapply(</pre>
 split(x, x["d"]),
 function(df) {
 df[["a"]] <- fill_na(df[["a"]])</pre>
 df[["b"]] <- rank(df[["b"]])</pre>
 df[["c"]] <- standardise(df[["c"]])</pre>
 df
 }
)
do.call(rbind.data.frame, x groups)
 a b
u.2 1.0 1 1.46357 u
u.3 2.5 4 -0.17823 u
u.4 2.5 3 -0.63478 u
u.6 4.0 2 -0.65057 u
v.1 10.0 1 -0.70711 v
v.5 10.0 2 0.70711 v
```

Only the *relative* ordering of rows within groups has been retained. Overall, the rows are in a different order. If this is an issue, we can use the **unsplit** function:

```
5 10.0 2 0.70711 v
6 4.0 2 -0.65057 u
```

**Exercise 12.30** Show how we can do the above also via the replacement version of **split**.

**Example 12.31** (\*) Recreating the previous ordering can be done manually too. It is because the split operation behaves as if we first ordered the data frame with respect to the grouping variable(s) (using a stable sorting algorithm). Here is a transformation of an example data frame split by a combination of two factors:

```
(x <- `row.names<-`(ToothGrowth[sample(NROW(ToothGrowth), 10),], NULL))</pre>
##
 len supp dose
1
 23.0
 OJ 2.0
2
 23.3
 OJ 1.0
3 29.4
 OJ 2.0
4 14.5
 OJ 1.0
5
 11.2
 VC 0.5
 OJ 1.0
6 20.0
7 24.5
 OJ 2.0
8 10.0
 OJ 0.5
 9.4
 OJ 0.5
9
10 7.0
 VC 0.5
(y <- do.call(rbind.data.frame, lapply(</pre>
 split(x, x[c("dose", "supp")]), # two grouping variables
 function(df) {
 df[["len"]] <- df[["len"]] * 100^df[["dose"]] * # whatever
 ifelse(df[["supp"]] == "OJ", -1, 1)
 # do not overthink it
 df
 }
)))
##
 len supp dose
 - 100
 OJ 0.5
0.5.0J.8
0.5.0J.9
 -94
 OJ 0.5
1.0J.2
 -2330
 OJ 1.0
1.0J.4
 OJ 1.0
 -1450
1.0J.6
 -2000
 OJ 1.0
2.0J.1
 -230000
 OJ 2.0
2.0J.3
 -294000
 OJ 2.0
2.0J.7
 OJ 2.0
 -245000
0.5.VC.5
 VC 0.5
 112
0.5.VC.10
 VC 0.5
```

Section 5.4.4 mentioned that by calling **order**, we can determine the inverse of a given permutation. Hence, we can call:

```
y[order(order(x[["supp"]], x[["dose"]])),] # not: dose, supp
 len supp dose
2.0J.1
 -230000
 OJ 2.0
1.0J.2
 -2330
 OJ 1.0
2.0J.3
 OJ 2.0
 -294000
1.0J.4
 -1450
 OJ 1.0
0.5.VC.5
 112
 VC 0.5
 OJ 1.0
1.0J.6
 -2000
2.0J.7
 -245000
 OJ 2.0
0.5.0J.8
 OJ 0.5
 -100
0.5.0J.9
 - 94
 OJ 0.5
0.5.VC.10
 70
 VC 0.5
```

Additionally, we can manually restore the original row.names, et voilà.

### 12.3.9 Metaprogramming-based techniques (\*)

Section 9.4.7 mentioned a few functions that provide *convenient* interfaces to some common data frame operations. These include **transform**, **subset**, **with**, and basically every procedure accepting a formula. The popular **data.table** and **dplyr** packages also belong to this class (Section 12.3.10).

Unfortunately, each method relying on metaprogramming must be studied separately because it is free to interpret the *form* of the passed arguments arbitrarily, without taking into account their *real* meaning. As we are interested in developing a more universal skill set, we avoid<sup>10</sup> them in this course. They do not offer anything more than what we have learnt so far.

Withal, they are thought-provoking on their own. Furthermore, they are quite popular in other users' code. Thus, after all, they deserve the honourable mention.

**Example 12.32** Let us consider an example call to the **subset** function:

```
subset(iris, Sepal.Length<4.5, -(Sepal.Width:Petal.Width))
Sepal.Length Species
9 4.4 setosa
14 4.3 setosa
39 4.4 setosa
43 4.4 setosa</pre>
```

Neither the second nor the third argument makes sense as a standalone R expression. We have not defined the named variables used there:

<sup>&</sup>lt;sup>10</sup> We are not alone in our calling to refrain from using them. help("subset") warns (and help("transform") quite similarly): This is a convenience function intended for use interactively. For programming, it is better to use the standard subsetting functions like `[`, and in particular the nonstandard evaluation of argument subset can have unanticipated consequences. The same in help("with"): For interactive use, this is very effective and nice to read. For programming however, i.e., in one's functions, more care is needed, and typically one should refrain from using with, as, e.g., variables in data may accidentally override local variables.

```
Sepal.Length<4.5 # utter nonsense

Error in eval(expr, envir, enclos): object 'Sepal.Length' not found
-(Sepal.Width:Petal.Width) # gibberish

Error in eval(expr, envir, enclos): object 'Sepal.Width' not found
```

Only from **help**("subset") we can learn that this tool assumes that the expression passed as the second argument plays the role of a row selector. Moreover, the third one is meant to remove all the columns between the two given ones.

In our course, we pay attention to developing transferable skills. We believe that R is not the only language we will learn during our long and happy lives. It is much more likely that in the next environment, we will become used to writing something of the more basic form:

**Example 12.33** With **transform**, we can add, modify, and remove columns in a data frame. Existing features can be referred to as if they were ordinary variables:

```
(mtcars4 <- mtcars[sample(seq_len(NROW(mtcars)), 4), c("hp", "am", "mpg")])</pre>
##
 hp am mpg
 335 1 15.0
Maserati Bora
Cadillac Fleetwood 205 0 10.4
 52 1 30.4
Honda Civic
Merc 450SLC
 180 0 15.2
transform(mtcars4, log hp=log(hp), am=2*am-1, hp=NULL, fcon=235/mpg)
 am mpg log hp
 fcon
Maserati Bora
 1 15.0 5.8141 15.6667
Cadillac Fleetwood -1 10.4 5.3230 22.5962
Honda Civic
 1 30.4 3.9512 7.7303
Merc 450SLC
 -1 15.2 5.1930 15.4605
```

Similarly, **attach** adds any named list to the search path (see Section 16.2.6) but it does not support altering their contents. As an alternative, **within** may be called:

```
within(mtcars4, {
 log_hp <- log(hp)
 fcon <- 235/mpg
 am <- factor(am, levels=c(0, 1), labels=c("no", "yes"))
 hp <- NULL</pre>
```

(continues on next page)

```
})
am mpg fcon log_hp
Maserati Bora yes 15.0 15.6667 5.8141
Cadillac Fleetwood no 10.4 22.5962 5.3230
Honda Civic yes 30.4 7.7303 3.9512
Merc 450SLC no 15.2 15.4605 5.1930
```

Those who find writing mtcars4[["name"]] instead of name too exhausting, can save a few keystrokes.

**Example 12.34** As mentioned in Section 10.3.4 (see Section 17.6 for more details), formulae are special objects that consist of two unevaluated expressions separated by a tilde, `~`. Functions can support formulae and do what they please with them. However, a popular approach is to allow them to express "something grouped by something else" or "one thing as a function of other things".

```
do.call(rbind.data.frame, lapply(split(ToothGrowth, ~supp+dose), head, 1))
 len supp dose
0J.0.5 15.2
 OJ 0.5
VC.0.5 4.2
 VC 0.5
OJ.1
 19.7
 OJ 1.0
VC.1
 16.5
 VC 1.0
0J.2 25.5 0J 2.0
VC.2
 23.6
 VC 2.0
aggregate(cbind(mpg, log_hp=log(hp))~am:cyl, mtcars, mean)
 am cvl
 mpg log hp
 4 22.900 4.4186
1 0
2 1 4 28.075 4.3709
3 0 6 19.125 4.7447
 6 20.567 4.8552
5 0 8 15.050 5.2553
6 1 8 15.400 5.6950
head(model.frame(mpg+hp\sim log(hp)+I(1/qsec), mtcars))
##
 mpg + hp log(hp)
 I(1/qsec)
Mazda RX4
 131.0 4.7005 0.060753....
Mazda RX4 Wag
 131.0 4.7005 0.058754....
Datsun 710
 115.8 4.5326 0.053734....
Hornet 4 Drive
 131.4 4.7005 0.051440....
Hornet Sportabout
 193.7 5.1648 0.058754....
Valiant
 123.1 4.6540 0.049455....
```

If these examples seem esoteric, it is because it is precisely the case. We need to consult the corresponding functions' manuals to discover what they do. And, as we do not recommend their use by beginner programmers, we will not explain them here. Don't trip.

**Exercise 12.35** In the last example, the peculiar printing of the last column is due to which method's being overloaded?

In the third part of this book, we will return to these functions for they will serve as an amusing illustration of how to indite our own procedures that rely on metaprogramming techniques.

### 12.3.10 A note on the dplyr (tidyverse) and data. table packages (\*)

data.table and dplyr are very popular packages that implement common data frame transformations. In particular, the latter is part of an immerse system of interdependent extensions called **tidyverse** which became quite invasive over the last few years. They both heavily rely on metaprogramming.

They introduce entirely new APIs featuring hundreds of functions for the operations we already know well how to perform (the calamity of superabundance). Still, their users must remember that they will *need* to rely on base functions when the processing of other prominent data structures is required, e.g., of fancy lists and matrices.

Base R (and its predecessor, S) has long ago proven to be a versatile tool for rapid prototyping, calling specialised procedures written in C or Java, and wrangling data that fit into memory. Even though some operations from the mentioned packages may be much faster for larger datasets, the speed is less often an issue in practice than what most users might think.

For larger problems, techniques for working with batches of data, sampling methods, or aggregating data stored elsewhere are often the way to go, especially when building machine learning models or visualisation<sup>11</sup> is required. Usually, the most recent data will be stored in external, normalised databases, and we will need to join a few tables to fetch something interesting from the perspective of the current task's context.

Thus, we cannot stress enough that, in many situations, SQL, not the other tools, is the most powerful interface to more considerable amounts of data. Learning it will give us the skills we can use later in other programming environments.

Note Of course, certain functions from tidyverse and related packages we will find very helpful after all. Quite annoyingly, they tend to return objects of the class tibble (tbl\_df) (e.g., haven::read.xpt that reads SAS data files). Luckily, they are subclasses of data.frame; we can always use as.data.frame to get our favourite objects back.

<sup>11</sup> For example, drawing scatter plots of billions of points makes little sense as they may result in unreadable images of large file sizes. The points need to be sampled or summarised somehow (e.g., binned); see Chapter 13.

### 12.4 Exercises

**Exercise 12.36** *Answer the following questions.* 

- What attributes a data frame is equipped with?
- If row. names is an integer vector, how to access rows labelled 1, 7, and 42?
- How to create a data frame that carries a column that is a list of character vectors of different lengths?
- How to create a data frame that includes a matrix column?
- How to convert all numeric columns in a data frame to a numeric matrix?
- Assuming that x is an atomic vector, what is the difference between as.data.frame(x), as. data.frame(as.list(x)), as.data.frame(list(a=x)), and data.frame(a=x)?

**Exercise 12.37** Assuming that x is a data frame, what is the meaning of/difference between the following:

- x["u"] vs x[["u"]] vs x[, "u"]?
- x["u"][1] vs x[["u"]][1] vs x[1, "u"] vs x[1, "u", drop=FALSE]?
- x[which(x[[1]] > 0), ]vsx[x[[1]] > 0, ]?
- x[grep("^foo", names(x))]?

**Exercise 12.38** We have a data frame with columns named like: ID (character), checked (logical, possibly with missing values), category (factor), x0, ..., x9 (ten separate numeric columns), y0, ..., y9 (ten separate numeric columns), coords (numeric matrix with two columns named lat and long), and features (list of character vectors of different lengths).

- How to extract the rows where checked is TRUE?
- How to extract the rows for which ID is like three letters and then five digits (e.g., XYZ12345)?
- How to select all the numeric columns in one go?
- How to extract a subset comprised only of the ID and x-something columns?
- How to get rid of all the columns between x3 and y7?
- Assuming that the IDs are like three letters and then five digits, how to add two columns: ID3
  (the letters) and ID5 (the five digits)?
- How to check where both lat and long in coords are negative?
- How to add the column indicating the number of features?
- How to extract the rows where "spam" is amongst the features?
- How to convert it to a long data frame with two columns: ID and feature (individual strings)?

- How to change the name of the ID column to id?
- How to make the y-foo columns appear before the x-bar ones?
- How to order the rows with respect to checked (FALSE first, then TRUE) and IDs (decreasingly)?
- How to remove rows with duplicate IDs?
- How to determine how many entries correspond to each category?
- How to compute the average lat and long in each category?
- How to compute the average lat and long for each category and checked combined?

**Exercise 12.39** Consider the flights<sup>12</sup> dataset. Give some ways to select all rows between March and October (regardless of the year).

Exercise 12.40 In this task, you will be working with a version of a dataset on 70k+ Melbourne trees (urban forest $^{13}$ ).

- 1. Load the downloaded dataset by calling the **read.csv** function.
- 2. Fetch the IDs (CoM. ID) and trunk diameters (Diameter. Breast. Height) of the horse chestnuts with five smallest diameters at breast height. The output data frame must be sorted with respect to Diameter. Breast. Height, decreasingly.
- 3. Create a new data frame that gives the number of trees planted in each year.
- 4. Compute the average age (in years, based on Year. Planted) of the trees of genera (each genus separately): Eucalyptus, Platanus, Ficus, Acer, and Quercus.

Exercise 12.41 (\*) Consider the historic data dumps of Stack Exchange<sup>14</sup> available here<sup>15</sup>. Export these CSV files to an SQLite database. Then, write some R code that corresponds to the following SQL queries. Use **dbGetQuery** to verify your results.

First:

```
SELECT
 Users.DisplayName,
 Users.Age,
 Users. Location,
 SUM(Posts.FavoriteCount) AS FavoriteTotal,
 Posts. Title AS MostFavoriteQuestion,
 MAX(Posts.FavoriteCount) AS MostFavoriteQuestionLikes
FROM Posts
JOIN Users ON Users. Id=Posts. OwnerUserId
WHERE Posts.PostTypeId=1
GROUP BY OwnerUserId
```

(continues on next page)

<sup>12</sup> https://github.com/gagolews/teaching-data/blob/master/other/flights.csv

<sup>13</sup> https://github.com/gagolews/teaching-data/raw/master/marek/urban\_forest.csv.gz

<sup>14</sup> https://travel.stackexchange.com/

<sup>15</sup> https://github.com/gagolews/teaching-data/tree/master/travel\_stackexchange\_com\_2017

```
ORDER BY FavoriteTotal DESC
LIMIT 10
```

Second:

```
SELECT
 Posts.ID,
 Posts. Title,
 Posts2.PositiveAnswerCount
FROM Posts
JOIN (
 SELECT
 Posts.ParentID,
 COUNT(*) AS PositiveAnswerCount
 FROM Posts
 WHERE Posts.PostTypeID=2 AND Posts.Score>0
 GROUP BY Posts.ParentID
) AS Posts2
 ON Posts. ID=Posts2. ParentID
ORDER BY Posts2. PositiveAnswerCount DESC
LIMIT 10
```

Third:

```
SELECT
 Posts. Title,
 UpVotesPerYear. Year,
 MAX(UpVotesPerYear.Count) AS Count
FROM (
 SELECT
 PostId,
 COUNT(*) AS Count,
 STRFTIME('%Y', Votes.CreationDate) AS Year
 FROM Votes
 WHERE VoteTypeId=2
 GROUP BY PostId, Year
) AS UpVotesPerYear
JOIN Posts ON Posts.Id=UpVotesPerYear.PostId
WHERE Posts.PostTypeId=1
GROUP BY Year
```

Fourth:

```
SELECT
Questions.Id,
```

```
Questions. Title,
 BestAnswers.MaxScore,
 Posts. Score AS AcceptedScore,
 BestAnswers.MaxScore-Posts.Score AS Difference
FROM (
 SELECT Id, ParentId, MAX(Score) AS MaxScore
 FROM Posts
 WHERE PostTypeId==2
 GROUP BY ParentId
) AS BestAnswers
JOIN (
 SELECT * FROM Posts
 WHERE PostTypeId==1
) AS Questions
 ON Questions. Id=BestAnswers. ParentId
JOIN Posts ON Questions. Accepted Answer Id=Posts. Id
WHERE Difference>50
ORDER BY Difference DESC
```

## Fifth:

```
SELECT
 Posts. Title,
 CmtTotScr.CommentsTotalScore
FROM (
 SELECT
 PostID,
 UserID,
 SUM(Score) AS CommentsTotalScore
 FROM Comments
 GROUP BY PostID, UserID
) AS CmtTotScr
JOIN Posts ON Posts.ID=CmtTotScr.PostID
 AND Posts.OwnerUserId=CmtTotScr.UserID
WHERE Posts.PostTypeId=1
ORDER BY CmtTotScr.CommentsTotalScore DESC
LIMIT 10
```

#### Sixth:

```
SELECT DISTINCT
 Users. Id,
 Users.DisplayName,
 Users.Reputation,
 Users.Age,
 (continues on next page)
```

```
Users.Location

FROM (

SELECT

Name, UserID

FROM Badges

WHERE Name IN (

SELECT

Name

FROM Badges

WHERE Class=1

GROUP BY Name

HAVING COUNT(*) BETWEEN 2 AND 10

)

AND Class=1

) AS ValuableBadges

JOIN Users ON ValuableBadges.UserId=Users.Id
```

#### Seventh:

```
SELECT
 Posts. Title,
 VotesByAge2.OldVotes
FROM Posts
JOIN (
 SELECT
 PostId,
 MAX(CASE WHEN VoteDate = 'new' THEN Total ELSE @ END) NewVotes,
 MAX(CASE WHEN VoteDate = 'old' THEN Total ELSE 0 END) OldVotes,
 SUM(Total) AS Votes
 FROM (
 SELECT
 PostId,
 CASE STRFTIME('%Y', CreationDate)
 WHEN '2017' THEN 'new'
 WHEN '2016' THEN 'new'
 ELSE 'old'
 END VoteDate.
 COUNT(*) AS Total
 FROM Votes
 WHERE VoteTypeId=2
 GROUP BY PostId, VoteDate
) AS VotesByAge
 GROUP BY VotesByAge.PostId
 HAVING NewVotes=0
) AS VotesByAge2 ON VotesByAge2.PostId=Posts.ID
```

WHERE Posts.PostTypeId=1
ORDER BY VotesByAge2.OldVotes DESC
LIMIT 10

**Exercise 12.42** (\*) Generate a CSV file that stores some random data arranged in a few columns of a size at least two times larger than your available RAM. Then, export the CSV file to an SQLite database. Use file connections (Section 8.3.5) and the nrowargument to **read. table** to process it chunk by chunk. Determine whether setting colclasses in **read. table** speeds up the reading of large CSV files significantly or not.

**Exercise 12.43** (\*) Export the whole XML data dump of StackOverflow<sup>16</sup> published at https://archive.org/details/stackexchange (see also https://data.stackexchange.com/) to an SQLite database.

<sup>16</sup> https://stackoverflow.com/

# Graphics

The R project homepage advertises our free software as an *environment for statistical* computing and graphics. Hence, had we not dealt with the latter use case, our course would have been incomplete.

R is nowadays equipped with the two following independent (incompatible, yet coexisting) systems for graphics generation; see Figure 13.1.

- 1. The (historically) newer one, **grid** (e.g., [48]), is very flexible but might seem quite complicated. Some readers might have come across the **lattice** [53] and **ggplot2** [58, 61] packages before. They are built on top of **grid**.
- 2. On the other hand, its traditional (S-style) counterpart, base graphics (e.g., [7]), is much easier to master. It still gives their users complete control over the drawing process. It is simple, fast, and minimalist, which makes it very attractive from the perspective of this course's philosophy.

This is why we only cover the second system here.

**Note** All figures in this book were generated using **graphics** and its dependants. They are sufficiently aesthetic, aren't they? Form precedes essence.

# 13.1 Graphics primitives

In **graphics**, we do not choose from a superfluity of virtual objects to be placed on an abstract canvas, letting some algorithm decide how and when to delineate them. We *just draw*. We do so by calling functions that plot the following *graphics primitives* (see, e.g., [36, 44]):

- symbols (e.g., pixels, circles, stars) of different shapes and colours,
- line segments of different styles (e.g., solid, dashed, dotted),
- polygons (optionally filled),
- text (using available fonts),
- raster images (bitmaps).



Figure 13.1. Relation between the graphics subsystems.

That's it. It will turn out that *all* other shapes (smooth curves, circles) may be easily approximated using the above.

Of course, in practice, we do not always have to be so low-level. There are many functions that provide the most popular chart types: histograms, bar plots, dendrograms, etc. They will suit our basic needs. We will review them in Section 13.3.

The more basic routines we discuss next will still be of service for fine-tuning our figures and adding further details. However, if the prefabricated components are not what we are after, we will be able to create any drawing from scratch.

**Important** In **graphics**, most of the function calls have immediate effects. Objects are drawn on the active plot one by one, and their state cannot be modified later.

**Example 13.1** Figure 13.2 depicts some graphics primitives, which we plotted using the following program. We will detail the meaning of all the functions in the next sections, but they should be self-explanatory enough for us to be able to find the corresponding shapes in the plot.

```
par(mar=rep(0.5, 4)) # small plot margins (bottom, left, top, right)
plot.new() # start a new plot
plot.window(c(0, 6), c(0, 2), asp=1) # x range: 0-6, y: 0-2; proportional
x \leftarrow c(0, 0, NA, 1, 2, 3, 4, 4, 5, 6)
y \leftarrow c(0, 2, NA, 2, 1, 2, 2, 1, 0.25, 0)
points(x[-(1:6)], y[-(1:6)]) # symbols
lines(x, y) # line segments
text(c(0, 6), c(0, 2), c("(0, 0)", "(6, 2)"), col="red") # two text labels
rasterImage(
 matrix(c(1, 0, # 2x3 pixel "image"; 0=black, 1=white
 0, 0), byrow=TRUE, ncol=2),
 5, 0.5, 6, 2, # position: xleft, ybottom, xright, ytop
 interpolate=FALSE
)
polygon(
 c(4, 5, 5.5, 4), # x coordinates of the vertices
 c(0, 0, 1, 0.75), # y coordinates
 lty="dotted", # border style
 col="#ffff0044" # fill colour: semi-transparent yellow
)
```

# 13.1.1 Symbols (points)

The **points** function can draw a series of symbols (by default, circles) on the twodimensional plot region, relative to the user coordinate system.

We specify the points' coordinates using the x and y arguments (two vectors of equal lengths; no recycling). Alternatively, we may give a matrix or a data frame with two



Figure 13.2. Graphics primitives: plotting symbols, line segments, polygons, text labels, and bitmaps. Objects are added one after another, with newer ones drawn *over* the already existing shapes.

columns: its first column (regardless of how and if it is named) defines the abscissae, and the second column determines the ordinates.

This function permits us to plot each point differently if this is what we desire. Thus, it is ideal for drawing scatter plots, possibly for grouped data (see Figure 13.17 below). It is vectorised with respect to, amongst others, the col (colour; see Section 13.2.1), cex (scale, defaults to 1), and pch (plotting character or symbol, defaults to 1, i.e., a circle) arguments.

**Example 13.2** Figure 13.3 gives an overview of the plotting symbols available. The most often used ones are:

- NA\_integer\_ no symbol,
- 0, ..., 14 and 15, ..., 18 unfilled and filled symbols, respectively;
- 19, ..., 25 filled symbols with a border of width lwd; for codes 21, ..., 25, the fill colour is controlled separately by the bg parameter,
- ". " a tiny point (a "pixel"),
- "a", "1", etc. a single character (not all Unicode characters can be drawn); strings longer than one will be truncated.

```
par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0.9, 9.1), c(0.9, 4.1))
points(
 cbind(1:9, 1), # or x=1:9, y=rep(1, 9); bottom row
 col="red",
 pch=c("A", "B", "a", "b", "Spanish Inquisition", "*", "!", ".", "9")
)

xy <- expand.grid(1:9, 4:2)
text(xy, labels=0:(NROW(xy)-1), pos=1, cex=0.89, offset=0.75, col="darkgray")
points(xy, pch=0:(NROW(xy)-1), bg="yellow")
Warning in plot.xy(xy.coords(x, y), type = type, ...): unimplemented pch
value '26'</pre>
```

	0	Δ	+	×	$\Diamond$	$\nabla$		*
0	1	2	3	4	5	6	7	8
$\Phi$	<b>⊕</b>	ΧX	Ħ	8			•	<b>A</b>
9	10	11	12	13	14	15	16	17
<b>♦</b>	•	•	0		<b>\Q</b>	Δ	$\nabla$	
18	19	20	21	22	23	24	25	26
Α	В	a	Ь	S	*	!		

Figure 13.3. Plotting characters and symbols (pch).

### 13.1.2 Line segments

**lines** can draw connected line segments whose mid- and endpoints are given in a similar manner as in the **points** function. A series of segments can be interrupted by defining an endpoint whose coordinate is a missing value; compare Figure 13.2.

Actually, **points** and **lines** are wrappers around the same function, **plot.xy**, which we usually do not call directly. Their type arguments determine the object to draw; the only difference is that by default the former uses type="p" whilst the latter relies on type="l". Changing these to type="b" (both) or type="o" (overplot) will give their combination. Moreover, type="s" and type="S" creates step functions (with post- and pre-increments, respectively), and type="h" draws bar plot-like vertical lines. See Figure 13.4 for an illustration (implement something similar yourself as an exercise).

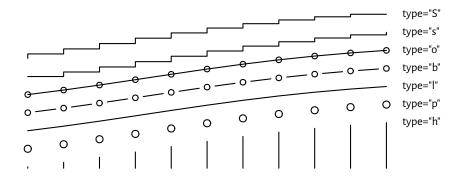


Figure 13.4. Different type argument settings in **lines** or **points**.

The col argument controls the line colour (see Section 13.2.1), and lwd determines the line width (1 by default). Six named line types (lty) are available, which can also be specified via their respective numeric identifiers, lty=1, ..., lty=6; see Figure 13.5 (implementing a similar plot is left as an exercise). Additionally, custom dashes can be defined using strings of up to eight hexadecimal digits. Consecutive digits give the lengths of the dashes and blanks (alternating). For instance, lty="1343" yields a dash of length 1, followed by a space of length 3, then a dash of length 4, followed by a blank of length 3. The whole sequence will be recycled for as long as necessary.

 "dashed", "44", or 2	 "solid" or 1
 "dotdash", "1343", or 4	 "dotted", "13", or 3
 "twodash", "2262", or 6	 "longdash", "73", or 5
 "9515"	 "5515"
 "4484C4"	 "19"

Figure 13.5. Line types (lty).

**Example 13.3 lines** can be used for plotting empirical cumulative distribution functions (we will suggest it as an exercise later), regression models (e.g., lines, splines of different degrees), time series, and any other mathematical functions, even when they are smooth and curvy. The naked eye cannot tell the difference between a densely sampled piecewise linear approximation of an object and its original version. The code below illustrates this (sad for the high-hearted idealists) truth using the sine function; see Figure 13.6.

```
ns <- c(seq(3, 25, by=2), 50, 100)
par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, length(ns)*pi), c(-1, 1))
for (i in seq_along(ns)) {
 x <- seq((i-1)*pi, i*pi, length.out=ns[i])
 lines(x, sin(x))
 text((i-0.5)*pi, 0, ns[i], cex=0.89)
}</pre>
```



Figure 13.6. The sine function approximated with line segments. Sampling more densely gives the illusion of smoothness.

**Exercise 13.4** Implement your version of the **segments** function using a call to **lines**.

**Exercise 13.5** (\*) Implement a simplified version of the **arrows** function, where the length of edges of the arrowhead is given in user coordinates (and not inches; you will be equipped with skills to achieve this later; see Section 13.2.4). Use the ljoin and lend arguments (see **help**("par") for admissible values) to change the line end and join styles (from the default rounded caps).

## 13.1.3 Polygons

**polygon** draws a polygon with a border of specified colour and line type (border, lty, lwd). If the col argument is not missing, the polygon is filled (or hatched; cf. the density and angle arguments).

**Example 13.6** Let us draw a few regular (equilateral and equiangular) polygons; see Figure 13.7. By increasing the number of sides, we can obtain an approximation to a circle.

```
regular_poly <- function(x0, y0, r, n=101, ...)
{
 theta <- seq(0, 2*pi, length.out=n+1)[-1]
 polygon(x0+r*cos(theta), y0+r*sin(theta), ...)
}

par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, 9.5), c(-1, 1), asp=1)
 regular_poly(1, 0, 1, n=3)
 regular_poly(3.5, 0, 1, n=7, density=15, angle=45, col="tan", border="red")
 regular_poly(6, 0, 1, n=10, density=8, angle=-60, lty=3, lwd=2)
 regular_poly(8.5, 0, 1, n=100, border="brown", col="lightyellow")</pre>
```

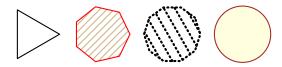


Figure 13.7. Regular polygons drawn using polygon.

Note the asp=1 argument to the **plot.window** function (which we detail below) that guarantees the same scaling of the x- and y-axes. This way, the circle looks like one and not an oval.

Notice that the last vertex adjoins the first one. Also, if we are absent-minded (or particularly creative), we can produce self-intersecting or otherwise degenerate shapes.

**Exercise 13.7** Implement your version of the **rect** function using a call to **polygon**.

#### 13.1.4 Text

A call to **text** draws arbitrary strings (newlines and tabs are supported) centred at the specified points. Moreover, by setting the pos argument, the labels may be placed below, to the left of, etc., the pivots. Some further position adjustments are also possible (adj, offset); see Figure 13.8.



Figure 13.8. The positioning of text with **text** (plotting symbols added for reference).

col specifies the colour, cex affects the size, and srt changes the rotation of the text.

On many graphics devices, we have little but crude control over the font face used: family chooses a generic font family ("sans", "serif", "mono"), and font selects between the normal variant (1), bold (2), italic (3), or bold italic (4). See, however, Section 13.2.6 for some workarounds.

**Note** (\*) There is limited support for basic mathematical symbols and formulae. It relies on some quirky syntax that we enter using unevaluated R expressions (Chapter 15). Still, it should be enough to meet our most basic needs. For instance, passing **quote**(beta[i]^j) as the labels argument to **text** will output " $\beta_i^j$ ". See **help**("plotmath") for more details.

For more sophisticated mathematical typesetting, see the **tikzDevice** graphics device mentioned in Section 13.2.6. It outputs plot specifications that can be rendered by the LaTeX typesetting system.

### 13.1.5 Raster images (bitmaps) (\*)

Raster images are encoded in the form of bitmaps, i.e., matrices whose elements represent pixels (see Figure 13.2 for an example). They can be used for drawing heat maps or backgrounds of contour plots; see Section 13.3.4.

**Example 13.8** Optionally, bilinear interpolation can be applied if the drawing area is larger than the true bitmap size, and we would like to smoothen the colour transitions out. Figure 13.9 presents a very stretched  $4 \times 3$  pixel image, with and without interpolation.



Figure 13.9. Example bitmaps drawn with rasterImage, with (left) and without (right) colour interpolation.

# 13.2 Graphics settings

par can be used to query and modify (as long as they are not read-only) many graphics options. For instance, we have several parameters related to the current page or device settings, e.g., the plot's margins (see Section 13.2.2) or user coordinates (see Section 13.2.3). The reference list of available parameters is given in help("par"). Below we discuss the most noteworthy ones.

Moreover, some functions source<sup>1</sup> the values of their default arguments by querying par. This is the case of, e.g., col, pch, lty in the points and lines function.

**Exercise 13.9** *Study the following pseudocode.* 

```
lines(x, y) # use the default `lty`, i.e., par("lty") == "solid"

old_settings <- par(lty="dashed") # change setting, save old for reference
lines(x, y) # use the new default `lty`, i.e., par("lty") == "dashed"
lines(x, y, lty=3) # use the given `lty`, but only for this call
lines(x, y) # default lty="dashed" again
par(old_settings) # restore the previous settings
lines(x, y) # lty="solid" now</pre>
```

#### 13.2.1 Colours

Many functions allow for customising colours of the plotted objects or their parts; compare, e.g., col and border arguments to **polygon**, or col and bg to **points**.

There are a few ways to specify colours (see the *Colour Specification* section of help("par") for more details).

• We can use a "colour name" string, being one of the 657 predefined tags known to the **colours** function:

• We can pass a "#rrggbb" string, which specifies a position in the RGB colour space: three series of hexadecimal numbers of two digits each, i.e., between  $oo_{hex} = 0$  (off) and  $FF_{hex} = 255$  (full on), giving the intensity of the red, green, and blue channels<sup>2</sup>.

<sup>&</sup>lt;sup>1</sup> Alas, it is not as straightforward as that. For instance, **polygon** is unaffected by the col setting, **axis** uses col.axis instead, etc. We should always consult the documentation.

<sup>&</sup>lt;sup>2</sup> From school, we probably know the *subtractive* CMY (cyan, magenta, yellow) model, where we obtain, e.g., a green colour by using blue-ish and yellow crayons (subtracting certain wavelengths from white light). The RGB model, on the other hand, corresponds to the three photoreceptor/cone cells in the retinas of the human eyes. Nonetheless, it is *additive* and, therefore, less intuitive: total darkness emerges when we emit no light, yellow emerges when mixing red and green beams, etc.

In practice, the **col2rgb** and **rgb** functions can convert between the decimal and hexadecimal representations:

```
C <- c("black", "red", "green", "blue", "cyan", "magenta",
 "yellow", "grey", "lightgrey", "pink") # example colours
(M <- structure(col2rgb(C), dimnames=list(c("R", "G", "B"), C)))</pre>
 black red green blue cyan magenta yellow grey lightgrey pink
 0 255
 255
 255 190
R
 0
 211 255
 255
 255
 0
 255 190
 211
G
 0
 192
 0 190
B
 0 255 255
 255
 211 203
structure(rgb(M[1,], M[2,], M[3,], maxColorValue=255), names=C)
 black
 red
 blue
 green
 cyan
 magenta
 yellow
"#000000" "#FF0000" "#00FF00" "#000FF" "#00FFFF" "#FF00FF" "#FFF00"
 grey lightgrey
 pink
"#BEBEBE" "#D3D3D3" "#FFC0CB"
```

• An "#rrggbbaa" string is similar, but has the added alpha channel (two additional hexadecimal digits): from  $oo_{hex} = 0$  denoting fully transparent, to  $FF_{hex} = 255$  indicating fully visible (lit) colour; see Figure 13.2 for an example.

Semi-transparency (translucency) can significantly enhance the expressivity of our data visualisations; see Figure 13.18 and Figure 13.19.

• We can rely on an integer index to select an item from the *current palette* (with recycling), which we can get or set by a call to **palette**. Moreover, 0 identifies the background colour, **par**("bg").

Integer colour specifiers are particularly valuable when plotting data in groups defined by factor objects. The underlying integer level codes can be mapped to consecutive colours from any palette; see Figure 13.17 below for an example.

#### **Example 13.10** We recommend memorising the colours in the default palette:

```
palette() # default palette
[1] "#000000F0" "#DF536BF0" "#61D04FF0" "#2297E6F0" "#28E2E5F0"
[6] "#CD0BBCF0" "#F5C710F0" "#999999F0"
```

These are<sup>3</sup>, in order: black, red, green, blue, cyan, magenta, yellow, and grey; see<sup>4</sup> Figure 13.10.

```
k \leftarrow length(palette())

par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, k+1), c(0, 1))

points(1:k, rep(0.5, k), col=1:k, pch=16, cex=3)
```

(continues on next page)

<sup>&</sup>lt;sup>3</sup> Actually, red-ish, green-ish, etc. The choice is more aesthetic than when pure red, green, etc. was used (before R 4.0.0). It is also expected to be more friendly to people who have colour vision deficiencies. We know that roughly every 1 in 12 men (8%) and 1 in 200 women (0.5%), especially in the red-green or blue-yellow spectrum; see [50] for more details.

<sup>&</sup>lt;sup>4</sup> The readers of the printed version of this book should know that its online version displays this figure (and all others) in full colour. See you there.

(continued from previous page)

```
text(1:k, 0.5, palette(), pos=rep(c(1, 3), length.out=k), col=1:k, offset=1)
text(1:k, 0.5, 1:k, pos=rep(c(3, 1), length.out=k), col=1:k, offset=1)
```



Figure 13.10. The default colour palette.

Choosing usable colours requires talents that most programmers lack. Therefore, we will find ourselves relying on the built-in colour sets. **palette.pals** and **hcl.pals** return the names of the available *discrete* (qualitative) palettes. Then, **palette.colors** and **hcl.colors** (note the American spelling) can generate a given number of colours from a particular named set.

Continuous (quantitative) palettes are also available, see rainbow, heat.colors, terrain. colors, topo.colors, cm.colors, and gray.colors. They transition smoothly between predefined pivot colours, e.g., from blue through green to brown (like in a topographic map with elevation colouring). They may be of use, e.g., when drawing contour plots; compare Figure 13.27.

**Exercise 13.11** Create a demo of the aforementioned palettes in a similar (or nicer) style to that in Figure 13.11.

# 13.2.2 Plot margins and clipping regions

A device (page) region represents a single plot window, one raster image file, or a page in a PDF document (see Section 13.2.6 for more information on graphics devices). As we will learn from Section 13.2.5, it is capable of holding many figures.

Usually, however, we draw *one figure per page*. In such a case, the device region is divided into the following parts:

- 1) outer margins, which can be set via, e.g., the oma graphics parameter (in text lines, based on the height of the default font); by default, they are equal to 0;
- figure region:
  - a) inner (plot) margins, by default mar=c(5.1, 4.1, 4.1, 2.1) text lines (bottom, left, top, right, respectively); this is where we usually emplace the figure title, axes labels, etc.
  - b) plot region, where we draw graphics primitives positioned relative to the user coordinates.

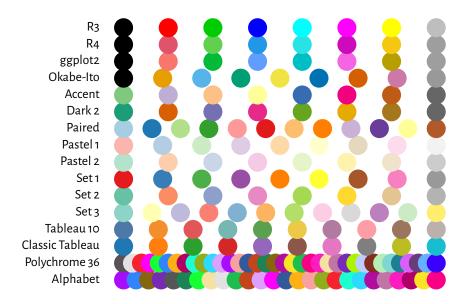


Figure 13.11. Qualitative colour palettes in **palette.pals**; R4 is the default one, as seen in Figure 13.10.

**Note** Typically, all drawings are *clipped* to the plot region, but this can be changed with the xpd parameter; see also the more flexible **clip** function.

**Example 13.12** Figure 13.12 shows the default page layout. In the code chunk below, note the use of mtext to print a text line in the inner margins, box to draw a rectangle around the plot or figure region, axis to add the two axes (labels and tick marks), and title to print the descriptive labels.

(continued from previous page)

```
rect(-10, -10, 10, 10, col="lightgray") # rectangle (clipped to plot region)
text(0, 0, "Plot region")
lines(c(-3, 0, 3), c(-2, 2, -2)) # standard clipping (plot region)
lines(c(-3, 0, 3), c(-2, 1.25, -2), xpd=TRUE, lty=3) # clip to figure region
```

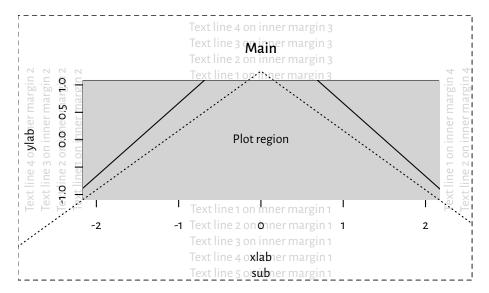


Figure 13.12. Figure layout with default inner and outer margins (mar=c(5.1, 4.1, 4.1, 2.1)) and oma=c(0, 0, 0, 0) text lines, respectively). We see that a lot of space is wasted and hence some tweaking might be necessary to suit our needs better. Note the clipping of the solid line to the grey plot region.

#### 13.2.3 User coordinates and axes

**plot.window** sets the user coordinates. It accepts the following parameters:

- xlim, ylim vectors of length two giving the minimal and maximal ranges on the respective axes; by default, they are extended by 4% in each direction for aesthetic reasons (see, e.g., Figure 13.12) but we can disable this behaviour by setting the xaxs and yaxs graphics parameters;
- asp aspect ratio (y/x); defaults to NA, i.e., no adjustment; use asp=1 for circles to look like ones, and not ovals;
- log logarithmic scaling on particular axes: "" (none; default), "x", "y", or "xy".

**Example 13.13** The graphics parameter us r can be used to read (and set) the extremes of the user coordinates in the form  $(x_1, x_2, y_1, y_2)$ .

```
plot.new()
(continues on next page)
```

```
(continued from previous page)
```

```
plot.window(c(-1, 1), c(1, 1000), log="y", yaxs="i")
par("usr")
[1] -1.08 1.08 0.00 3.00
```

Indeed, the x-axis range was extended by 4% in each direction (xaxs="r"). We have turned this behaviour off for the y-axis (yaxs="i"), which uses the base-10 logarithmic scale. In this case, its actual range is  $10^{\text{par}}("usr")[3:4]$  because  $\log_{10} 1 = 0$  and  $\log_{10} 1000 = 3$ .

**Exercise 13.14** Implement your version of the **abline** function using **lines**.

Even though axes (labels and tick marks) can be drawn manually using the aforementioned graphics primitives, it is usually too tedious a work.

This is why we tend to rely on the axis function, which draws the object on one of the plot sides (as usual, 1=bottom, ..., 4=right).

Once **plot.window** is called, **axTicks** can be called to guesstimate the tasteful (round) locations for the tick marks relative to the current plot size. By default, they are based on the xaxp and yaxp graphics parameters, which give the axis ranges and the number of intervals between the tick marks.

```
plot.new(); plot.window(c(-0.9, 1.05), c(1, 11))
par("usr") # (x1, x2, y1, y2)
[1] -0.978 1.128 0.600 11.400
par("yaxp") # (y1, y2, n)
[1] 2 10 4
axTicks(2) # left y-axis
[1] 2 4 6 8 10
par("xaxp") # (x1, x2, n)
[1] -0.5 1.0 3.0
axTicks(1) # bottom x-axis
[1] -0.5 0.0 0.5 1.0
par(xaxp=c(-0.9, 1.0, 5)) # change
axTicks(1)
[1] -0.90 -0.52 -0.14 0.24 0.62 1.00
```

axis relies on the same algorithm as axTicks. Alternatively, we can provide custom tick locations and labels.

**Example 13.15** Most of the plots in this book use the following graphics settings (except las=1 to axis(2)); see Figure 13.13. Check out help("par"), help("axis"), etc. and tune them up to suit your needs.

```
par(mar=c(2.2, 2.2, 1.2, 0.6))
par(tcl=0.25) # the length of the tick marks (fraction of text line height)
par(mgp=c(1.1, 0.2, 0)) # axis title, axis labels, and axis line location
 (continues on next page)
```

(continued from previous page)

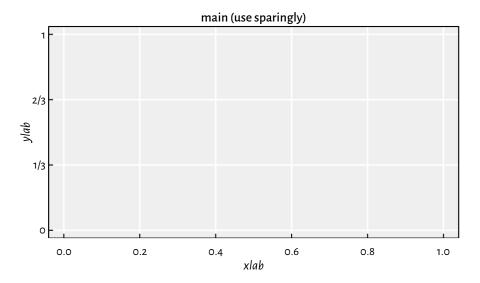


Figure 13.13. Custom axes and other settings.

### 13.2.4 Plot dimensions (\*)

Certain sizes can be read or specified in inches (1" is exactly 25.4 mm):

- pin plot dimensions (width, height),
- fin figure region dimensions,
- din page (device) dimensions,
- mai plot (inner) margin size,

- omi outer margins,
- cin the size of the "default" character (width, height).

If the figure is scaled, the *virtual* inch (the one reported by R) will not match the physical one (e.g., the actual size in the printed version of this book or on the computer screen).

**Important** Most objects' positions are specified in *virtual* user coordinates, as given by usr. They are automatically mapped to the *physical* device region, taking into account the page size, outer and inner margins, etc.

Knowing the above, some basic scaling can be used to convert between the user and physical sizes (in inches). It is based on the ratios (usr[2]-usr[1])/pin[1] and (usr[4]-usr[3])/pin[2]; compare the **xinch** and **yinch** functions.

**Example 13.16** (\*) Figure 13.14 shows how we can pinpoint the edges of the figure and device region in user coordinates.

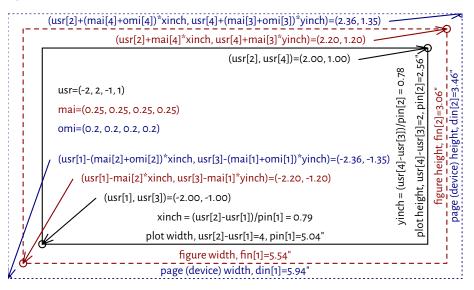


Figure 13.14. User vs device coordinates. Note that the virtual inch does not correspond to the physical one, as some scaling was applied.

**Exercise 13.17** (\*) We cannot use **mtext** to print text on the right inner margin rotated by 180 degrees compared to what we see in Figure 13.12. Write your version of this function that will allow you to do so. Hint: use **text**, the cin graphics parameter, and what you can read from Figure 13.14.

# 13.2.5 Many figures on one page (subplots)

It is possible to create many figures on one page. In such a case, each subplot has its own inner margins and plot region.

A call to par(mfrow=c(nr, nc)) or par(mfcol=c(nr, nc)) splits the page into a regular grid with nr rows and nc columns. Each invocation of plot.new starts a new figure. Consecutive figures are either placed in a rowwise manner (mfrow) or the columnwise one (mfcol). Alternatively, the mfg parameter can enforce a custom order.

**Example 13.18** Figure 13.15 depicts an example page with four figures aligned on a  $2 \times 2$  grid.

```
par(oma=rep(1.2, 4)) # outer margins (default 0)
par(mfrow=c(2, 2)) # a 2x2 plot grid
for (i in 1:4) {
 plot.new()
 par(mar=c(3, 3, 2, 2)) # each subplot will have the same inner margins
 plot.window(c(i-1, i+1), c(-1, 1)) # separate user coordinates for each
 text(i, 0, sprintf("Plot region (plot %d)\n(%d, %d)", i,
 par("mfg")[1], par("mfg")[2]))
 box("figure", lty="dashed") # a box around the figure region
 box("plot") # a box around the plot region
 axis(1) # horizontal axis (bottom)
 axis(2) # vertical axis (left)
}
box("outer", lty="dotdash") # a box around the whole page
for (i in 1:4)
 mtext(sprintf("Outer margin %d", i), side=i, outer=TRUE)
```

Thanks to mfrow and mfcol, we can create a scatter plot matrix or different trellis plots. If an irregular grid is required, we can call the slightly more sophisticated **layout** function (which is incompatible with mfrow and mfcol). Examples will follow later; see Figure 13.24 and Figure 13.26.

Certain grid sizes might affect the mex and cex parameters and hence the default font sizes (amongst others). Refer to the documentation of par for more details.

# 13.2.6 Graphics devices

Where our plots are *displayed* depends on our development environment (Section 1.2). Users of **JupyterLab** see the plots embedded into the current notebook, consumers of **RStudio** display them in a dedicated *Plots* pane, working from the console opens a new graphics window (unless we work in a text-only environment), whereas compiling **utils::Sweave** or **knitr** markup files brings about an image file that will be included in the output document.

In practice, we might be interested in exercising our creative endeavours on different devices. For instance, to draw something in a PDF file, we can call:

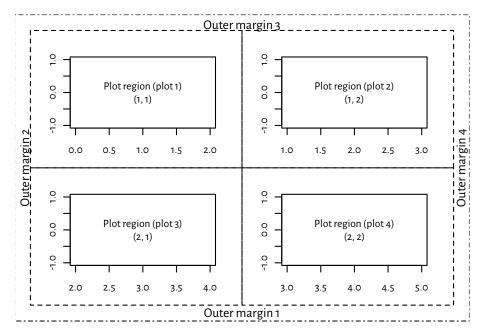


Figure 13.15. A page with four figures created using **par**(mfrow=**c**(2, 2)).

```
cairo_pdf("figure.pdf", width=6, height=3.5) # open "device"
... calls to plotting functions...
dev.off() # save file, close device
```

Similarly, a call to png or svg creates a PNG or a SVG file. In both cases, as we rely on the Cairo library, we can customise the font family by calling Cairo::CairoFonts.

**Note** Typically, web browsers can display JPEG, PNG, and SVG files. PDF is a popular choice in printed publications (e.g., articles or books).

It is worth knowing that PNG and JPEG are raster graphics formats, i.e., they store figures as bitmaps (pixel matrices). They are fast to render, but the file sizes might become immense if we want decent image quality (high resolution). Most importantly, they should not be scaled: it is best to display them at their original widths and heights. However, JPEG uses lossy compression. Therefore, it is not a particularly fortunate file format for data visualisations. It does not support transparency either.

On the other hand, SVG and PDF files store vector graphics, where all primitives are described geometrically. This way, the image can be redrawn at any size and is always expected to be aesthetic. Unfortunately, scatter plots with millions of points will result in considerable files size and relatively slow rendition times (but there are tricks to remedy this).

Users of TeX might be interested in **tikzDevice::tikz**, which creates TikZ files that can be rendered as standalone PDF files or embedded in LaTeX documents (and its variants). It allows for typesetting beautiful equations using the standard "\$...\$" syntax within any R string.

Many other devices are listed in help("Devices").

**Note** (\*) The opened graphics devices form a stack. Calling **dev.off** will return to the last opened device (if any). See **dev.list** and other functions listed in its help page for more information.

Each device has separate graphics parameters. When opening a new device, we start with default settings in place.

Also, dev.hold and dev.flush can suppress the immediate display of the plotted objects, which might increase the drawing speed on certain interactive devices.

The current plot can be copied to another device (e.g., a PDF file) using **dev.print**.

**Exercise 13.19** (\*) Create an animated PNG displaying a large point sliding along the sine curve. Generate a series of video frames like in Figure 13.16. Store each frame in a separate PNG file. Then, use **ImageMagick**<sup>5</sup> (compare Section 7.3.2 or rely on another tool) to combine these files as a single animated PNG.

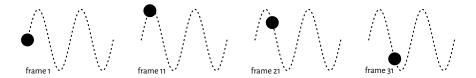


Figure 13.16. Selected frames of an example animation. They can be stored in separate files and then combined as a single animated PNG.

# 13.3 Higher-level functions

Higher-level plotting commands call **plot.new**, **plot.window**, **axis**, **box**, **title**, etc., and draw graphics primitives on our behalf. They provide ready-to-use implementations of the most common data visualisation tools, e.g., box-and-whisker plots, histograms, pairs plots, etc.

Below we review a few of them. We also show how they can be customised or even rewritten from scratch if we are not completely happy with them. They will inspire us to practice lower-level graphics programming.

<sup>5</sup> https://imagemagick.org/

**Exercise 13.20** Check out the meaning of the ask, new, xaxt, yaxt, and ann graphics parameters and how they affect plot.new, axis, title, and so forth.

### 13.3.1 Scatter and function plots with plot. default and matplot

The default method for the S3 generic **plot** is a convenient wrapper around **points** and **lines**.

**Example 13.21 plot. default** can draw a scatter plot of a set of points in  $\mathbb{R}^2$  possibly grouped by another categorical variable. From Section 10.3.2 we know that a factor is represented as a vector of small natural numbers. Therefore, its underlying level codes can be used directly as col or pch specifiers; see Figure 13.17 for a demonstration. Take note of a call to the **legend** function.

```
plot(
 jitter(iris[["Sepal.Length"]]), # x (it is a numeric vector)
 jitter(iris[["Petal.Width"]]), # y (it is a numeric vector)
 col=as.numeric(iris[["Species"]]), # colours (integer codes)
 pch=as.numeric(iris[["Species"]]), # plotting symbols (integer codes)
 xlab="Sepal length", ylab="Petal width",
 asp=1 # y/x aspect ratio
)
legend(
 "bottomright",
 legend=levels(iris[["Species"]]),
 col=seq_along(levels(iris[["Species"]])),
 pch=seq_along(levels(iris[["Species"]])),
 bg="white"
)
```

**Exercise 13.22** Pass ann=FALSE and axes=FALSE to **plot** to suppress the addition of axes and labels. Then, draw them manually using the functions discussed in the previous section.

**Exercise 13.23** Draw a plot of the  $y = \sin x$  function using **plot**. Then, call **lines** to add  $y = \cos x$ . Later, do the same using a single reference to **matplot**. Include a legend.

**Example 13.24** Semi-transparency may convey additional information. Figure 13.18 shows two scatter plots of adult females' weights vs heights. If the points are fully opaque, we cannot judge the density around them. On the other hand, translucent symbols somewhat imitate the two-dimensional histograms that we will later depict in Figure 13.29.

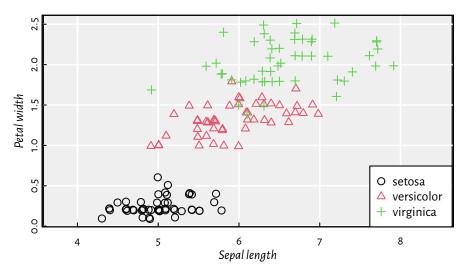


Figure 13.17. **as.numeric** can define different plotting styles for each factor level.

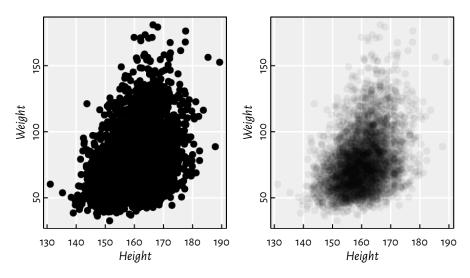


Figure 13.18. Semi-transparent symbols can reflect the points' distribution density.

**Example 13.25** Figure 13.19 depicts the average monthly temperatures in your next holiday destination: Warsaw, Poland (a time series). Note that the translucent ribbon representing the low-high average temperature intervals was added using a call to **polygon**.

```
Warsaw monthly temperatures; source: https://en.wikipedia.org/wiki/Warsaw high <- c(0.6, 1.9, 6.6, 13.6, 19.5, 21.9, 24.4, 23.9, 18.4, 12.7, 5.9, 1.6)

mean <- c(-1.8, -0.6, 2.8, 8.7, 14.2, 17.0, 19.2, 18.3, 13.5, 8.5, 3.3, -0.7)

low <- c(-4.2, -3.6, -0.6, 3.9, 8.9, 11.8, 13.9, 13.1, 9.1, 4.8, 0.6, -3.0)

matplot(1:12, cbind(high, mean, low), type="o", col=c(2, 1, 4), lty=1, xlab="month", ylab="temperature [°C]", xaxt="n", pch=16, cex=0.5)

axis(1, at=1:12, labels=month.abb, line=-0.25, lwd=0, lwd.ticks=1)

polygon(c(1:12, rev(1:12)), c(high, rev(low)), border=NA, col="#ffff0033")

legend("bottom", c("average high", "mean", "average low"), lty=1, col=c(2, 1, 4), bg="white")
```

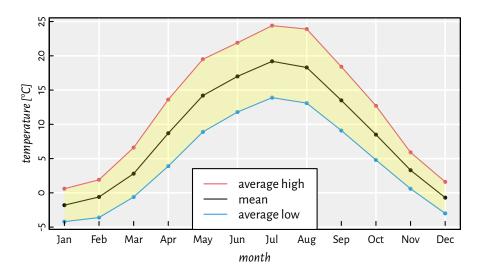


Figure 13.19. Example time series. A semi-transparent ribbon was added by calling **polygon** to highlight the area between the low-high ranges (intervals).

**Example 13.26** Figure 13.20 depicts a scatter plot similar to Figure 13.18, but now with the points' hue being a function of a third variable.

```
midpoints <- function(x) 0.5*(x[-1]+x[-length(x)])
z <- nhanes[["waistcirc"]]
breaks <- seq(min(z), max(z), length.out=10)
zf <- cut(z, breaks, include.lowest=TRUE)
```

(continues on next page)

(continued from previous page)

```
col <- hcl.colors(nlevels(zf), "Viridis", alpha=0.5)
layout(matrix(c(1, 2), nrow=1), # two plots in one page
 widths=c(1, lcm(3))) # second one is of width "3cm" (scaled)
first subplot:
plot(nhanes[["height"]], nhanes[["weight"]], col=col[as.numeric(zf)],
 pch=16, xlab="Height", ylab="Weight")
second subplot:
par(mar=c(2.2, 0.6, 2.2, 0.6))
plot.new(); plot.window(c(0, 1), c(0, nlevels(zf)))
rasterImage(as.matrix(rev(col)), 0, 0, 1, nlevels(zf), interpolate=FALSE)
text(0.5, 1:nlevels(zf)-0.5, sprintf("%3.0f", midpoints(breaks)))
mtext("Waist 0", side=3)</pre>
```

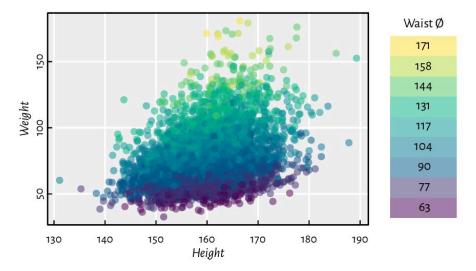


Figure 13.20. A 2D scatter plot with a third variable represented by colours.

**Exercise 13.27** Implement your version of **pairs**, being the function to draw a scatter plot matrix (a pairs plot).

**Exercise 13.28 ecdf** returns an object of the S3 classes ecdf and stepfun. There are **plot** methods overloaded for them. Inspect their source code. Then, inspired by this, create a function to compute and display the empirical cumulative distribution function corresponding to a given numeric vector.

**Exercise 13.29 spline** performs cubic spline interpolation, whereas **smooth.spline** determines a smoothing spline of a given two-dimensional dataset. Plot different splines for cars[["dist"]] as a function of cars[["speed"]]. Which of these two functions is more appropriate for depicting this dataset?

### 13.3.2 Bar plots and histograms

A bar plot is drawn using a series of rectangles (i.e., certain polygons) of different heights (or widths, if we request horizontal alignment).

**Example 13.30** Let us visualise the dataset<sup>6</sup> listing the most frequent causes of medication errors (data are fabricated):

```
cat_med = c(
 "Unauthorised drug", "Wrong IV rate", "Wrong patient", "Dose missed",
 "Underdose", "Wrong calculation", "Wrong route", "Wrong drug",
 "Wrong time", "Technique error", "Duplicated drugs", "Overdose"
)
counts_med = c(1, 4, 53, 92, 7, 16, 27, 76, 83, 3, 9, 59)
```

A Pareto chart combines a bar plot featuring bars of decreasing heights with a cumulative percentage curve; see Figure 13.21.

```
o <- order(counts_med)</pre>
cato med <- cat med[o]
pcto med <- counts med[o]/sum(counts med)*100</pre>
cumpcto_med <- rev(cumsum(rev(pcto_med)))</pre>
bar plot of percentages
par(mar=c(2.2, 0.6, 2.2, 6.6)) # wide left margin
midp <- barplot(pcto_med, horiz=TRUE, xlab="%",</pre>
 col="white", xlim=c(0, 25), xaxs="r", yaxs="r", yaxt="n",
 width=3/4, space=1/3)
text(pcto_med, midp, sprintf("%.1f%", pcto_med), pos=4, cex=0.89)
axis(4, at=midp, labels=cato_med, las=1)
box()
cumulative percentage curve in a new coordinate system
par(usr=c(-4, 104, par("usr")[3], par("usr")[4])) # 0-100 with 4% addition
lines(cumpcto_med, midp, type="o", col=4, pch=18)
axis(3, col=4)
mtext("cumulative %", side=3, line=1.2, col=4)
text(cumpcto_med, midp, sprintf("%.1f%", cumpcto_med), cex=0.89, col=4,
 pos=c(4, 2)[(cumpcto_med>80)+1], offset=0.5)
```

Note that **barplot** returned the midpoints of the bars, which we put in good use. By default, it sets the xaxs="i" graphics parameter and thus does not extend the x-axis range by 4% on both sides. This would not make us happy here, therefore we needed to change it manually.

**Exercise 13.31** Draw a bar plot summarising, for each passenger class and sex, the number of adults who did not survive the sinking of the deadliest 1912 cruise; see Figure 13.22 and the Titanic dataset.

<sup>6</sup> https://www.cec.health.nsw.gov.au/CEC-Academy/quality-improvement-tools/pareto-charts

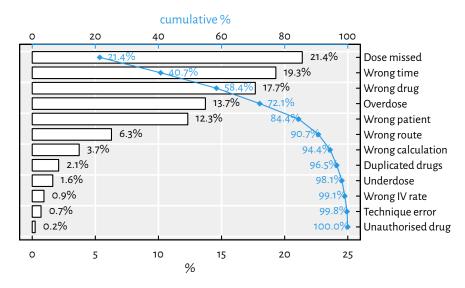


Figure 13.21. An example Pareto chart (a fancy bar plot). Double axes have a general tendency to confuse the reader.

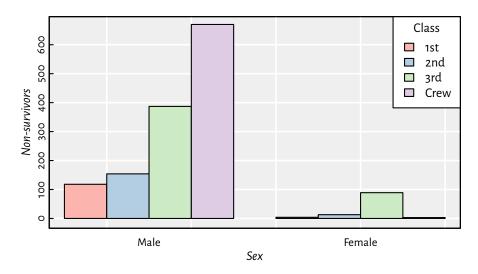


Figure 13.22. An example bar plot representing a two-way contingency table.

**Exercise 13.32** Implement your version of **barplot**, but where the bars are placed precisely at the positions specified by the user, e.g., allowing the bar midpoints to be consecutive integers.

We will definitely not cover the (in)famous pie charts in our book. The human brain is not very skilled at judging the relative differences between the areas of geometric objects. Also, they are ugly.

Moving on: a histogram is a simple density estimator for continuous data. It can be thought of as a bar plot with bars of heights proportional to the number of observations falling into the corresponding disjoint intervals. Most often, there is no space between the bars to emphasise that the intervals cover the whole data range.

A histogram can be computed and drawn using the high-level function **hist**; see Figure 13.23.

```
par(mfrow=c(1, 2))
for (breaks in list("Sturges", 25)) {
 # Sturges (a heuristic) is the default; any value is merely a suggestion
 hist(iris[["Sepal.Length"]], probability=TRUE, xlab="Sepal length",
 main=NA, breaks=breaks, col="white")
 box() # weirdly, we need to add it manually
}
```

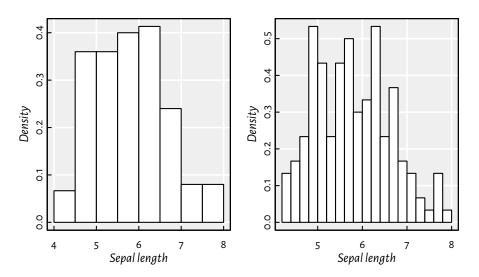


Figure 13.23. Example histograms for the same dataset.

**Exercise 13.33** Study the source code of **hist.default**. Note the invisibly-returned list of the S3 class histogram. Then, study **graphics:::plot.histogram**. Implement similar functions yourself.

**Exercise 13.34** Modify your function to draw a scatter plot matrix so that it gives the histograms of the marginal distributions on its diagonal.

**Example 13.35** Using **layout** mentioned in Section 13.2.5, we can draw a scatter plot with marginal histograms; see Figure 13.24. Note that we split the page into four plots of unequal sizes, but the upper right part of the grid is unused. We use **hist** for binning only (plot=FALSE). Then, **barplot** is utilised for drawing as it gives greater control over the process (e.g., supports vertical layout).

```
layout(matrix(
 c(1, 1, 1, 0, # first row: first plot of width 3 and nothing
 3, 3, 2, # three rows: square third plot and a tall second
 3, 3, 3, 2,
 3, 3, 3, 2), nrow=4, byrow=TRUE))
par(mex=1, cex=1) # the layout function changed this!
x <- jitter(iris[["Sepal.Length"]])</pre>
y <- jitter(iris[["Sepal.Width"]])</pre>
first subplot (top)
par(mar=c(0.2, 2.2, 0.6, 0.2), ann=FALSE)
hx \leftarrow hist(x, plot=FALSE, breaks=seq(min(x), max(x), length.out=20))
barplot(hx[["density"]], space=0, axes=FALSE, col="#00000011")
second subplot (right)
par(mar=c(2.2, 0.2, 0.2, 0.6), ann=FALSE)
hy <- hist(y, plot=FALSE, breaks=seq(min(y), max(y), length.out=20))</pre>
barplot(hy[["density"]], space=0, axes=FALSE, horiz=TRUE, col="#00000011")
third subplot (square)
par(mar=c(2.2, 2.2, 0.2, 0.2), ann=TRUE)
plot(x, y, xlab="Sepal length", ylab="Sepal width",
 xlim=range(x), ylim=range(y)) # default xlim, ylim
```

**Example 13.36** (\*) Kernel density estimators (KDEs) are another way to guesstimate the data distribution. The **density** function, for a given numeric vector, returns a list with, amongst others, the x and y coordinates of the points that we can pass directly to the **lines** function. Below we depict the KDEs of data split into three groups; see Figure 13.25.

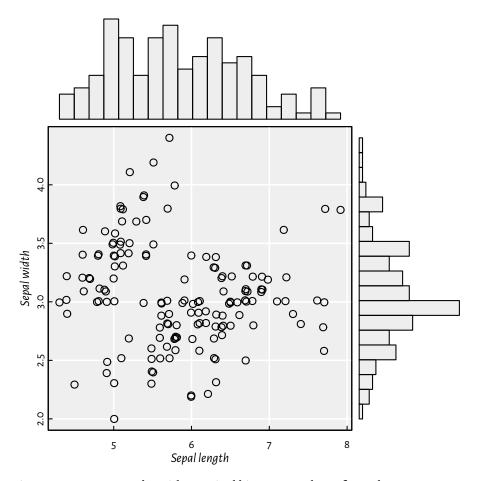


Figure 13.24. A scatter plot with marginal histograms: three (four) plots on one page, but on a nonuniform grid created using **layout**.

**Exercise 13.37** (\*) Implement a function that draws kernel density estimators for a given numeric variable split by a combination of three factor levels; see Figure 13.26 for an example.

```
grid_kde <- function(data, values, x, y, hue) ...to.do...</pre>
tips <- read.csv("~/Projects/teaching-data/other/tips.csv", comment.char="#",
 stringsAsFactors=TRUE) # see https://github.com/gagolews/teaching-data
head(tips, 3) # preview an example dataset
 total bill tip
 sex smoker day
1
 16.99 1.01 Female
 No Sun Dinner
2
 10.34 1.66
 Male
 No Sun Dinner
 3
3
 21.01 3.50
 Male
 No Sun Dinner
grid_kde(tips, values="tip", x="smoker", y="time", hue="sex")
```

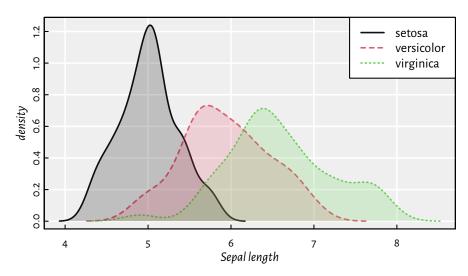


Figure 13.25. Kernel density estimators of sepal length split by species in the iris dataset. Note the semi-transparent polygons (again).

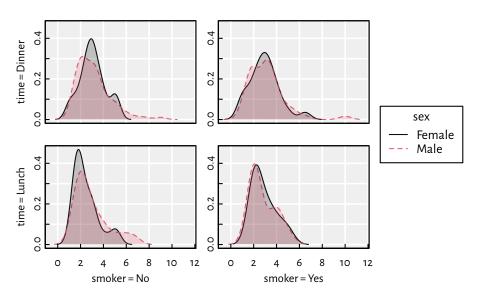


Figure 13.26. An example grid plot (also known as a trellis, panel, conditioning, or lattice plot) with kernel density estimators for a numeric variable (amount of tip in a US restaurant) split by a combination of three factor levels (smoker, time, sex).

### Box-and-whisker plots

We have already seen a chart generated by the **boxplot** function in Figure 5.1. Tinkering with it will give us robust practice, which in turn shall make us perfect.

**Exercise 13.38** Modify the code generating Figure 5.1 so that:

- 1. same doses are grouped together (more space between different doses added; also, on the xaxis, only unique doses are printed),
- 2. different supps have different colours (add a legend explaining them).

**Exercise 13.39** Write a function for drawing box plots using graphics primitives.

**Exercise 13.40** (\*) Write a function for drawing violin plots. They are similar to box plots but use kernel density estimators.

**Exercise 13.41** (\*) Implement a bag plot, which is a two-dimensional version of a box plot. Use **chull** to compute the convex hull of a point set.

### 13.3.4 Contour plots and heat maps

When plotting a function of two variables like z = f(x, y), the magnitude of the z component can be expressed using colour brightness or hue.

image is a convenient wrapper around rasterImage, which can draw contour plots, two-dimensional histograms, heatmaps, etc.

**Example 13.42** Figure 13.27 presents a filled contour plot of Himmelblau's function, f(x,y) = $(x^2 + y - 11)^2 + (x + y^2 - 7)^2$ , for  $x \in [-5, 5]$  and  $y \in [-4, 4]$ . A call to **contour** adds labelled contour lines (which is actually a nontrivial operation).

```
x \leftarrow seq(-5, 5, length.out=250)
y <- seq(-4, 4, length.out=200)</pre>
z \leftarrow outer(x, y, function(xg, yg) (xg^2 + yg - 11)^2 + (xg + yg^2 - 7)^2)
image(x, y, z, col=grey(seq(1, 0, length.out=16)))
contour(x, y, z, nlevels=16, add=TRUE)
```

In **image**, the number of rows in z matches the length of x, whereas the number of columns is equal to the size of y. This might be counterintuitive; if z is printed, the image is its 90-degree rotated version.

**Example 13.43** Figure 13.28 presents an example heatmap depicting Pearson's correlations between all pairs of variables in the nhanes data frame which we loaded some time ago.

```
o <- c(6, 5, 1, 7, 4, 2, 3) # order of rows/cols (by similarity)
R <- cor(nhanes[o, o])</pre>
par(mar=c(2.8, 7.6, 1.2, 7.6), ann=FALSE)
image(1:NROW(R), 1:NCOL(R), R,
 ylim=c(NROW(R)+0.5, 0.5),
 zlim=c(-1, 1),
```

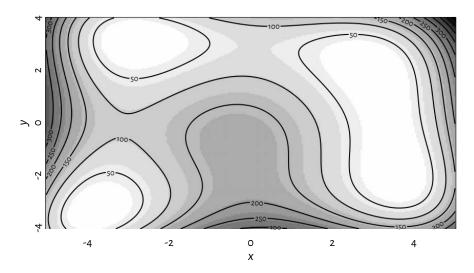


Figure 13.27. A filled contour plot with labelled contour lines.

(continued from previous page)

```
col=hcl.colors(20, "BluGrn", rev=TRUE),
 xlab=NA, ylab=NA, asp=1, axes=FALSE)
axis(1, at=1:NROW(R), labels=dimnames(R)[[1]], las=2, line=FALSE, tick=FALSE)
axis(2, at=1:NCOL(R), labels=dimnames(R)[[2]], las=1, line=FALSE, tick=FALSE)
text(arrayInd(seq_along(R), dim(R)),
 labels=sprintf("%.2f", R),
 col=c("white", "black")[abs(R<0.8)+1],</pre>
 cex=0.89)
```

**Exercise 13.44** Check out the **heatmap** function, which uses hierarchical clustering to find an aesthetic reordering of the matrix's items.

**Example 13.45** Figure 13.29 depicts a two-dimensional histogram. It approaches the idea of reflecting the points' density quite differently from the semi-transparent symbols in Figure 13.18.

```
histogram_2d \leftarrow function(x, y, k=25, ...)
ſ
 breaksx <- seq(min(x), max(x), length.out=k)</pre>
 fx <- cut(x, breaksx, include.lowest=TRUE)</pre>
 breaksy <- seq(min(y), max(y), length.out=k)</pre>
 fy <- cut(y, breaksy, include.lowest=TRUE)</pre>
 C <- table(fx, fy)</pre>
 image(midpoints(breaksx), midpoints(breaksy), C,
 xaxs="r", yaxs="r", ...)
```

hipcirc	1.00	0.88	0.94	0.83	0.24	-0.15	-0.44
armcirc	0.88	1.00	0.94	0.82	0.21	0.12	-0.29
weight	0.94	0.94	1.00	0.92	0.45	0.16	-0.24
waistcirc	0.83	0.82	0.92	1.00	0.63	0.35	-0.00
leglen	0.24	0.21	0.45	0.63	1.00	0.66	0.36
height	-0.15	0.12	0.16	0.35	0.66	1.00	0.80
armlen	-0.44	-0.29	-0.24	-0.00	0.36	0.80	1.00
	hipcirc	armcirc	weight	waistcirc	leglen	height	armlen

Figure 13.28. A correlation heatmap drawn using image.

(continued from previous page)

**Exercise 13.46** (\*) Implement some two-dimensional kernel density estimator and plot it using **contour**.

### 13.4 Exercises

**Exercise 13.47** Answer the following questions.

- Can functions from the **graphics** package be used to adjust the plots generated by **lattice** and **ggplot2**?
- What are the most common graphics primitives?
- Can all high-level functions be implemented using low-level ones? As an example, discuss the key ingredients used in **barplot**.

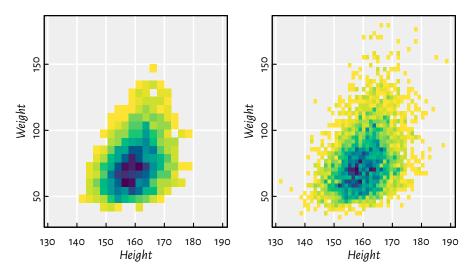


Figure 13.29. Two-dimensional histograms with different numbers of bins, where the bin count is reflected by the colour.

- Some high-level functions discussed in this chapter carry the add parameter. What is its purpose?
- What are the admissible values of pch and Lty? Also, in the default palette, what is the meaning of colours 1, 2, ..., 16? Can their meaning be changed?
- Can all graphics parameters be changed?
- What is the difference between passing xaxt="n" to plot.default vs setting it with par, and then calling plot.default?
- Which graphics parameters are set by plot.window?
- What is the meaning of the usr parameter when using the logarithmic scale on the x-axis?
- (\*) How to place a plotting symbol exactly 1 centimetre from the top-left corner of the current page (following the page's diagonal)?
- Semi-transparent polygons are nice, right?
- Can an ellipse be drawn using polygon?
- What happens when we set the graphics parameter mfrow=c(2, 2)?
- How to export the current plot to a PDF file?

**Exercise 13.48** Draw the 2022 BTC-to-USD close rates<sup>7</sup> time series. Then, add the 7- and 30-day moving averages. (\*) Also, fit a local polynomial (moving) regression model using the Savitzky–Golay filter (see **loess**).

<sup>&</sup>lt;sup>7</sup> https://github.com/gagolews/teaching-data/raw/master/marek/btcusd\_close\_2022.csv

**Exercise 13.49** (\*) Draw (from scratch) a candlestick plot for the 2022 BTC-to-USD rates<sup>8</sup>.

**Exercise 13.50** (\*) Create a function to draw a normal quantile-quantile (Q-Q) plot, i.e., for inspecting whether a numeric sample might come from a normal distribution.

**Exercise 13.51** (\*) Draw a map of the world, where each country is filled with a colour whose brightness or hue is linked to its Gini index of income inequality. You can easily find the data on Wikipedia. Try to find an open dataset that gives the borders of each country as vertices of a polygon (e.g., in the form of a (geo)JSON file).

**Exercise 13.52** Next time you see a pleasant data visualisation somewhere, try to reproduce it using base *graphics*.

For further information on graphics generation in R, see, e.g., Chapter 12 of [57], [48], and [52]. In this chapter, we were only interested in *static* graphics, e.g., for use in printed publications or plain websites. Interactive plots that a user might tinker with in a web browser are a different story.

And so the second part of our mind-blowing course is ended.

<sup>8</sup> https://github.com/gagolews/teaching-data/raw/master/marek/btcusd\_ohlc\_2022.csv

Part III

Deepest

# *Interfacing compiled code (\*\*)*

R is an effective *glue* language. It is suitable for composing whole data wrangling pipelines: from data import through processing, analysis, and visualisation to export. It makes using and connecting larger *building blocks* very convenient.

R is also a competent tool for developing quick and dirty prototypes of standalone, general-purpose algorithms, especially if they are of *numerical* nature. Nevertheless, for performance reasons, we may consider rewriting computing-intensive tasks in C or  $C++^1$ . Such a move can be beneficial if we need a method that:

- has higher memory or time complexity when programmed using vectorised R functions than its straightforward implementation,
- has an iterative or recursive nature, e.g., involving unvectorisable for or while loops,
- relies on complicated dynamic data structures (e.g., hash maps, linked lists, or trees),
- needs methods provided elsewhere and not available in R (e.g., other C or C++ libraries).

In the current chapter, we will demonstrate that R works very well as a user-friendly interface to compiled code.

This topic is overall very technical. The definitive reference is the *Writing R Extensions* manual [63], but see also Chapter 11 of [10]. Furthermore, R's source code provides many working examples of how to deal with R objects in C.

Here, we will only cover the most important basics. We will focus on writing or interfacing *portable*<sup>2</sup> function libraries that only rely on *simple*<sup>3</sup> data structures (e.g., arrays of the type double and int). Thanks to this, we will be able to reuse them in other environments such as Python (e.g., via Cython) or Julia. Let us remember that R is one of *many* languages out there.

<sup>&</sup>lt;sup>1</sup> Plain C and C++ are as fast as we can get without applying fancy CPU-specific optimisations or similar hacks. Fortran is also supported but will not be covered in this book because of its smaller popularity. Additionally, certain external packages are gateways to other languages, such as Java.

Nevertheless, D.E. Knuth once said: "The real problem is that programmers have spent far too much time worrying about efficiency in the wrong places and at the wrong times; premature optimisation is the root of all evil (or at least most of it) in programming" [39].

<sup>&</sup>lt;sup>2</sup> Hence, we are not interested in the overall very convenient **Rcpp** or **cpp11** packages. They define C++ classes that make interacting with R objects more pleasant for some users.

<sup>&</sup>lt;sup>3</sup> Thus, we will not discuss the ALTREP [55] representation of objects, ways to deal with environments or pairlists, etc.

We assume basic knowledge of the C language; see [38]. The reader can skip this chapter now and return to it later. The remaining material is not contingent on the current one.

From now on, we take for granted that our environment can successfully build a source package with C code, as mentioned in Section 7.3.1. In particular, W\*\*\*\*ws and m\*\*OS should install, respectively, RTools and Xcode.

**Note** To avoid ambiguity, in the main text, calls to C functions will be denoted with the "C::" prefix, e.g., C::spanish\_inquisition().

#### C and C++ code in R 14.1

#### Source files for compiled code in R packages 14.1.1

Perhaps the most versatile way to interact with portable C code is via standalone R packages. For the purpose of the current chapter, we created a demo project available at https://github.com/gagolews/cpackagedemo.

**Exercise 14.1** Inspect the structure of **cpackagedemo**. Note that C source files are located in the src/subdirectory. Build and install the package using install.packages or the "R CMD IN-STALL" command. Then, load the package in R and call my\_sum defined there on some numeric vector.

The package provides an R interface to one C function, C::my\_c\_sum, written in the most portable fashion possible. Its declaration is included in the src/cfuns.h file:

```
#ifndef __CFUNS_H
#define __CFUNS_H
#include <stddef.h>
double my_c_sum(const double* x, size_t n);
#endif
```

The function accepts a pointer to the start of a numeric sequence and its size, which is a standard<sup>4</sup> way of representing an array of doubles.

Its definition is given in src/cfuns.c. We see that it is nothing more than a simple sum of all the elements in an array:

<sup>4 (\*)</sup> A slightly more sophisticated representation (used, e.g., in GNU GSL and numpy) deals with a sliced array, where we additionally store the so-called stride. Instead of inspecting elements one after another, we advance the iterator by a given step size. This way, we could apply the same function on selected rows of a matrix (if it is in the column-major order).

```
#include "cfuns.h"

/* computes the sum of all elements in an array x of size n */
double my_c_sum(const double* x, size_t n)
{
 double s = 0.0;
 for (size_t i = 0; i < n; ++i) {
 /* this code does not treat potential missing values specially
 (they are kinds of NaNs); to fix this, add:
 if (ISNA(x[i])) return NA_REAL; // #include <R.h> */
 s += x[i];
 }
 return s;
}
```

To make **C::my\_c\_sum** available in R, we will have to introduce a wrapper around it that works with the data structures from the first part of this jolly book. We know that an R function accepts objects of *any* kind on input and yields *anything* as a result. In the next section, we will explain that we get access to R objects via special pointers of the type SEXP (S expressions).

And so we declare our R-callable wrapper in src/rfuns.h:

```
#ifndef __RFUNS_H
#define __RFUNS_H
#include <R.h>
#include <Rinternals.h>
#include <Rmath.h>

SEXP my_c_sum_wrapper(SEXP x);
#endif
```

The actual definition is included in src/rfuns.c:

```
#include "rfuns.h"
#include "cfuns.h"

/* a wrapper around my_c_sum callable from R */
SEXP my_c_sum_wrapper(SEXP x)
{
 double s;

 if (!Rf_isReal(x)) {
 /* the caller is expected to prepare the arguments
```

(continues on next page)

```
(doing it at the C level is tedious work) */
 Rf error("'x' should be a vector of the type 'double'");
 }
 s = my_c_sum(REAL(x), (size_t)XLENGTH(x));
 return Rf_ScalarReal(s);
}
```

The arguments could be, technically speaking, prepared at the C level. For instance, if x turned out to be an integer vector, we could have converted it to the double one (they are two different types; see Section 6.4.1). Nevertheless, overall, it is very burdensome. It is easier to use pure R code to ensure that the arguments are of the correct form as well as to beautify the outputs.

This explains why we only assert the enjoyment of C::Rf\_isReal(x). It guarantees that the C::REAL and C::XLENGTH functions correctly return the pointer to the start of the sequence and its length, respectively.

Once C::my\_c\_sum is called, we must convert it to an R object so that it can be returned to our environment. Here, it is a newly allocated numeric vector of length one. We did this by calling C::Rf\_ScalarReal.

Although optional (see Section 5.4 of [63]), we will register C::my\_c\_sum\_wrapper as a callable function explicitly. This way, R will not be struggling to find the specific entry point in the resulting dynamically linked library (DLL). We do this in src/ cpackagedemo.c:

```
#include <R_ext/Rdynload.h>
#include "rfuns.h"
/* the list of functions available in R via a call to .Call():
 each entry is like {exported_name, fun_pointer, number_of_arguments} */
static const R_CallMethodDef cCallMethods[] = {
 {"my_c_sum_wrapper", (DL_FUNC)&my_c_sum_wrapper, 1},
 {NULL, NULL, 0} // the end of the list (sentinel)
};
/* registers the list of callable functions */
void R_init_cpackagedemo(DllInfo *dll)
{
 R_registerRoutines(dll, NULL, cCallMethods, NULL, NULL);
 R_useDynamicSymbols(dll, FALSE);
}
```

The function can be invoked from R using .Call. Here are the contents of R/my\_sum.R:

```
my_sum <- function(x)
{
 # prepare input data:
 if (!is.double(x))
 x <- as.double(x)

s <- .Call("my_c_sum_wrapper", x, PACKAGE="cpackagedemo")

some rather random postprocessing:
 attr(s, "what") <- deparse(substitute(x))
 s
}</pre>
```

And, finally, here is the package NAMESPACE file responsible for registering the exported R names and indicating the DLL to use:

```
export(my_sum)
useDynLib(cpackagedemo)
```

Once the package is built and installed (e.g., by running "R CMD INSTALL <pkgdir>" in the terminal or calling install.packages), we can test it by calling:

```
library("cpackagedemo")
my_sum(runif(100)/100)
[1] 0.49856
attr(,"what")
[1] "runif(100)/100"
```

**Exercise 14.2** Extend the package by adding a function to compute the index of the greatest element in a numeric vector. Note that C uses 0-based array indexing whereas in R, the first element is at index 1. Compare its run time against which.max using proc.time.

### 14.1.2 R CMD SHLIB

The "R CMD SHLIB <files>" shell command compiles one or more source files without the need for turning them into standalone packages; see [63]. Then, dyn.load loads the resulting DLL.

**Exercise 14.3** (\*) Compile src/cfuns.c and src/rfuns.c from our demo package using "R CMD SHLIB". Call dyn.load. Write an R function that uses .Call to invoke C::my\_c\_sum\_wrapper from the second source file.

The direct SHLIB approach is convenient for learning C programming, including running simple examples. We will thus use it for didactic reasons in this chapter. The inst/examples/csource.R file in our demo package includes the implementation of an R function called **csource**. It compiles a given C source file, and loads the resulting

DLL. It also extracts and executes a designated R code chunk preferably defining a function that refers to .Call.

Here is an example source file, inst/examples/helloworld.c in the cpackagedemo source code repository:

Let us compile it and call the R function defined above.

```
source("~/R/cpackagedemo/inst/examples/csource.R") # defines csource
csource("~/R/cpackagedemo/inst/examples/helloworld.c")
hello()
The mill's closed. There's no more work. We're destitute.
I'm afraid I've no choice but to sell you all for scientific experiments.
```

**Exercise 14.4** (\*) C++ is also supported. It can be thought of as a superset of the C language, but the devil is in the detail. Change the name of the above file to helloworld2.cpp, add extern "C" before the function declaration, and compile it.

**Exercise 14.5** (\*) Verify that C and C++ source files can coexist in R packages.

**Example 14.6** (\*) It might be very educative to study the implementation of **csource**. We should be able to author such functions ourselves now (a few hours' worth of work), let alone read with understanding.

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```
shlibargs=character(),
 headers=paste0(
 "#include <R.h>\n",
 "#include <Rinternals.h>\n",
 "#include <Rmath.h>\n"
 R=file.path(R.home(), "bin/R")
)
{
 stopifnot(file.exists(fname))
 stopifnot(is.character(shlibargs))
 stopifnot(is.character(headers))
 stopifnot(is.character(R), length(R) == 1)
 if (is.null(libname))
 libname <- regmatches(basename(fname),</pre>
 regexpr("[^.]*(?=\\..*)", basename(fname), perl=TRUE))
 stopifnot(is.character(libname), length(libname) == 1)
 # read the source file:
 f <- paste(readLines(fname), collapse="\n")</pre>
 # set up output file names:
 tmpdir <- normalizePath(tempdir(), winslash="/") # tempdir on Win uses \
 dynlib ext <- .Platform[["dynlib.ext"]]</pre>
 libpath <- file.path(tmpdir, sprintf("%s%s", libname, dynlib ext))</pre>
 cfname <- file.path(tmpdir, basename(fname))</pre>
 rfname <- sub("\\..*?$", ".R", cfname, perl=TRUE) # .R extension
 # separate the /* R \ldots < R code> \ldots R * / chunk from the source file:
 rpart <- regexec("(?smi)^/\|* R\\s?(.*)R */$", f, perl=TRUE)[[1]]
 rpart start <- rpart
 rpart_len <- attr(rpart, "match.length")</pre>
 if (rpart_start[1] < 0 || rpart_len[1] < 0)</pre>
 stop("enclose R code between /* R ... and ... R */")
 rcode <- substr(f, rpart_start[2], rpart_start[2]+rpart_len[2]-1)</pre>
 cat(rcode, file=rfname, append=FALSE)
 # write the C/C++ file:
 ccode <- paste(
 headers.
 substr(f, 1, rpart_start[1]-1),
```

```
substr(f, rpart_start[1]+rpart_len[1], nchar(f)),
 collapse="\n"
 cat(ccode, file=cfname, append=FALSE)
 # prepare the "R CMD SHLIB ..." command:
 shlibargs <- c(
 "CMD", "SHLIB",
 sprintf("-o %s", libpath),
 cfname,
 shlibargs
)
 # compile and load the DLL, run the extracted R script:
 retval <- FALSE
 oldwd <- setwd(tmpdir)</pre>
 tryCatch({
 if (libpath %in% sapply(getLoadedDLLs(), `[[`, "path"))
 dyn.unload(libpath)
 stopifnot(system2(R, shlibargs) == 0) # 0 == success
 dyn.load(libpath)
 source(rfname)
 retval <- TRUE
 }, error=function(e) {
 cat(as.character(e), file=stderr())
 7)
 setwd(oldwd)
 if (!retval) stop("error compiling file or executing R code therein")
 invisible(TRUE)
}
```

## Handling basic types

### 14.2.1 SEXPTYPES

All R objects are stored as instances of the C language structure SEXPREC. Usually, we access them via pointers, which are of the type SEXP (S expression).

A C function referred to via .Call takes the very generic SEXPs on input. It outputs another SEXP. Importantly, one of the said structure's fields represents the actual R object type (SEXPTYPE numbers); see Table 14.1 for a selection.

SEXPTYPE	Type in R (typeof)	Test in C	
NILSXP	NULL	$Rf_{isNull}(x)$ (true for $R_NilValue$ only)	
RAWSXP	raw	TYPEOF(x) == RAWSXP	
LGLSXP	logical	Rf_isLogical(x)	
INTSXP	integer	Rf_isInteger(x)	
REALSXP	double	$Rf_isReal(x)$	
CPLXSXP	complex	$Rf_isComplex(x)$	
STRSXP	character	Rf_isString(x)	
VECSXP	list	<pre>Rf_isVectorList(x)</pre>	
CHARSXP	char (scalar string; internal)	TYPEOF(x) == CHARSXP	
EXTPTRSXP	externalptr (internal)	TYPEOF(x) == EXTPTRSXP	

Table 14.1. Basic R types in C.

**Example 14.7** To illustrate that any R object is available as a SEXP, let us consider the inst/examples/sexptype.c file from **cpackagedemo**:

### Example calls:

```
csource("~/R/cpackagedemo/inst/examples/sexptype.c")
test_sexptype(1:10)
type of x: integer (SEXPTYPE=13)
test_sexptype(NA)
type of x: logical (SEXPTYPE=10)
test_sexptype("spam")
type of x: character (SEXPTYPE=16)
```

We should refer to particular SEXPTYPEs via their descriptive names (constants; e.g., STRSXP), not their numeric identifiers (e.g., 16); see Section 1.1 of [66] for the complete list $^5$ .

<sup>5</sup> src/include/Rinternals.h in R's source code repository; see, e.g., https://svn.r-project.org/R/trunk.

### 14.2.2 Accessing elements in simple atomic vectors

Table 14.2 gives the most important vector-like SEXPTYPEs (atomic and generic), the C types of their elements, and the functions to access the underlying array pointers. A call to C::XLENGTH returns the length of a given sequence.

We have already seen an example function that processes a numeric vector; see C::my\_c\_sum\_wrapper above.

Let us stress that writing functions that accept only int and double array pointers and their lengths makes them easily reusable in other environments. In many data analysis applications, we do not need much more.

SEXPTYPE	Array element type	Pointer access
RAWSXP	typedef unsigned char Rbyte;	RAW(x)
LGLSXP	int (use the FALSE, TRUE, and NA_LOGICAL constants)	LOGICAL(x)
INTSXP	int	INTEGER(x)
REALSXP	double	REAL(x)
CPLXSXP	<pre>typedef struct { double r; double i; } Rcomplex;</pre>	COMPLEX(x)
STRSXP	SEXP (array of SEXPs of the type CHARSXP)	(not directly)
VECSXP	SEXP (array of SEXPs of any SEXPTYPE)	(not directly)
CHARSXP	const char* (read-only; trailing 0; check encoding)	CHAR(x)

Table 14.2. Basic array-like R types and their elements in C.

**Important** With raw, logical, integer, floating-point, and complex vectors, we get direct access to data that might be shared amongst many objects (compare Section 16.1.4). SEXPRECS are simply passed by pointers (since SEXPs are exactly them). We must thus refrain from modifying the objects passed as function arguments. See below for ways to create new vectors, e.g., for storing auxiliary or return values.

### **Example 14.8** Consider inst/examples/sharedmem.c:

```
SEXP C_test_sharedmem(SEXP x)
{
 if (!Rf_isReal(x) || XLENGTH(x) == 0)
 Rf_error("`x` should be a non-empty vector of the type 'double'");

REAL(x)[0] = REAL(x)[0]+1; // never do it; always make a copy;
 // the underlying array `x` may be shared by many objects

return R_NilValue;
}
```

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<sup>&</sup>lt;sup>6</sup> (\*) Unless we know what we are doing, e.g., we are certain that we deal with a local variable in an R function that invokes our .call.

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```
/* R
test_sharedmem <- function(x)
 invisible(.Call("C_test_sharedmem", x, PACKAGE="sharedmem"))
R */</pre>
```

Calling the above function on an example vector:

```
csource("~/R/cpackagedemo/inst/examples/sharedmem.c")
y <- 1
z <- y
test_sharedmem(y)
print(c(y, z))
[1] 2 2</pre>
```

modifies y and z in place! It is not the same semantics as the one we got used to when interacting with R. Hence, we must always make a copy.

### 14.2.3 Representation of missing values

Most languages do not support the notion of missing values out of the box. Therefore, in R, they have to be emulated. Table 14.3 lists the relevant constants and the conventional ways for testing for missingness.

SEXPTYPE	Missing value	Testing
RAWSXP	(none)	(none)
LGLSXP	NA_LOGICAL (equal to INT_MIN)	el == NA_LOGICAL
INTSXP	NA_INTEGER (equal to INT_MIN)	el == NA_INTEGER
REALSXP	NA_REAL (a special NaN)	ISNA(el)
CPLXSXP	a pair of NA_REALs	ISNA(el.r)
STRSXP	NA_STRING (a CHARSXP object)	el == NA_STRING

Table 14.3. Representation of missing values.

In logical and integer vectors, NAs are represented as the smallest 32-bit signed integer. Thus, we need to be careful when performing any operations on these types: testing for missingness must be performed first.

The case of doubles is slightly less irksome, for a missing value is represented as a special not-a-number. Many arithmetic operations on NaNs return NaNs as well, albeit there is no guarantee<sup>7</sup> that they will be of precisely the same type as NA\_REAL. Thus, manual testing for missingness is also advised.

 $<sup>^7</sup>$  (\*\*) Namely, NAs are encoded as un-signalling NaNs 0x7ff00000000007A2 of the type double (the lower 32 payload bits are equal to 1954, decimally); see src/arithmetic.c in R's source code. The payload propagation is not fully covered by the current IEEE 754 floating point standard; see [22] for discussion. Reliance on

**Example 14.9** The inst/examples/mean\_naomit.c file defines a function to compute the arithmetic mean of an int or a double vector:

```
SEXP C_mean_naomit(SEXP x)
{
 double ret = 0.0;
 size_t k = 0;
 if (Rf_isInteger(x)) {
 const int* xp = INTEGER(x);
 size_t n = XLENGTH(x);
 for (size_t i=0; i<n; ++i)</pre>
 if (xp[i] != NA_INTEGER) { // NOT: ISNA(xp[i])
 ret += (double)xp[i];
 k++;
 }
 }
 else if (Rf isReal(x)) {
 const double* xp = REAL(x);
 size_t n = XLENGTH(x);
 for (size_t i=0; i<n; ++i)</pre>
 if (!ISNA(xp[i])) { // NOT: xp[i] == NA_REAL
 ret += xp[i];
 k++;
 }
 }
 else
 Rf_error("`x` should be a numeric vector");
 return Rf_ScalarReal((k>0)?(ret/(double)k):NA_REAL);
}
/* R
mean_naomit <- function(x)</pre>
{
 if (!is.numeric(x)) # neither integer nor double
 x \leftarrow as.numeric(x) + convert to double (the same as as.double)
 .Call("C_mean_naomit", x, PACKAGE="mean_naomit")
}
R */
```

There is some inherent code duplication but int and double are distinct types. Thus, they need to be handled separately (we could have convert them to doubles at the R level too). Some tests:

such behaviour will thus make our code platform-dependent. R itself sometimes does that; theoretically, this may cause NAs to be converted to (other) NaNs.

```
csource("~/R/cpackagedemo/inst/examples/mean_naomit.c")
mean_naomit(c(1L, NA_integer_, 3L, NA_integer_, 5L))
[1] 3
mean_naomit(rep(NA_real_, 10))
[1] NA
```

**Exercise 14.10** Implement all and any in C. Add the na. rm argument.

### 14.2.4 Memory allocation

R implements a simple yet effective garbage collector that relies on reference counting. Occasionally<sup>8</sup>, memory blocks that can no longer be reached are either freed or marked as reusable.

To allocate a new vector of length one and set its only element, we can call C::ScalarLogical, C::ScalarInteger, C::ScalarReal, etc. We have already used these functions for returning R "scalars".

Vectors of arbitrary lengths can be created using **C**::**Rf\_allocVector**(sexptype, size). Note that this function does not initialise the elements of logical and numeric sequences (amongst others). They will need to be set manually after creation.

**Important** All allocated vectors must be manually protected from garbage collection. To guard against premature annihilation, R maintains a stack<sup>9</sup> of objects. **C::PROTECT**(sexp) pushes a given object pointer onto the top of the list. **C::UNPROTECT**(n) pops the last *n* elements therefrom (in a last-in-first-out manner). At the end of a .Call, R checks if the number of protects matches that of unprotects. If it is not the case, a warning is generated.

Protection is not needed:

- for arguments to functions referred to by .Call, as they are already in use and hence protected;
- for objects assigned as list or character vectors' elements using C::SET\_VECTOR\_ELT and C::SET\_STRING\_ELT (see below); when the container is protected, so are its components;
- when we return the allocated vector to R immediately after creating it (like in return Rf\_ScalarReal(val) in a C function invoked by .Call).

**Example 14.11** Here is a function to compute the square of each element in a numeric vector. Note that the new vector must be protected from garbage collection while data are being prepared.

 $<sup>^8</sup>$  A safe strategy is to assume that any call to a function from R's API may trigger the memory cleanup. On a side note, we may call the gc function in R to enforce rubbish removal. It also reports the current memory usage.

<sup>9 (\*\*)</sup> C::R\_PreserveObject protects an arbitrary SEXP until C::R\_ReleaseObject is called manually. With this mechanism, objects are not automatically released at the end of a .Call.

```
SEXP C square1(SEXP x)
{
 // no need to call PROTECT(x), it is already in use
 if (!Rf_isReal(x)) Rf_error("`x` should be of the type 'double'");
 size_t n = XLENGTH(x);
 const double* xp = REAL(x);
 SEXP y = PROTECT(Rf_allocVector(REALSXP, n)); // won't be GC'd
 double* yp = REAL(y);
 for (size_t i=0; i<n; ++i) {</pre>
 if (ISNA(xp[i])) yp[i] = xp[i]; // NA_REAL
 else
 yp[i] = xp[i]*xp[i];
 }
 UNPROTECT(1); // pops one object from the protect stack;
 // does not trigger garbage collection, so we can return `y` now
 return y; // R will retrieve and protect it
}
/* R
square1 <- function(x)</pre>
{
 if (!is.double(x)) x <- as.double(x)</pre>
 .Call("C_square1", x, PACKAGE="square1")
}
R */
```

As an alternative, in this case, we may use C:: Rf\_duplicate:

```
SEXP C square2(SEXP x)
ſ
 if (!Rf_isReal(x)) Rf_error("`x` should be of the type 'double'");
 x = PROTECT(Rf_duplicate(x)); // OK; just replaces the pointer (address)
 size_t n = XLENGTH(x);
 double* xp = REAL(x);
 for (size_t i=0; i<n; ++i)</pre>
 if (!ISNA(xp[i])) xp[i] = xp[i]*xp[i];
 UNPROTECT(1);
 return x;
}
```

(continued from previous page)

```
/* R
square2 <- function(x)
{
 if (!is.double(x)) x <- as.double(x)
 .Call("C_square2", x, PACKAGE="square2")
}
R */</pre>
```

Some tests:

```
csource("~/R/cpackagedemo/inst/examples/square1.c")
square1(c(-2, -1, 0, 1, 2, 3, 4, NA_real_))
[1] 4 1 0 1 4 9 16 NA
csource("~/R/cpackagedemo/inst/examples/square2.c")
square2(c(-2, -1, 0, 1, 2, 3, 4, NA_real_))
[1] 4 1 0 1 4 9 16 NA
```

We can claim auxiliary memory from the heap during a function's runtime using the well-known C::malloc (or new in C++). We are of course fully responsible for releasing it via C::free (or delete).

**Example 14.12** Here is our version of the which function.

```
SEXP C which1(SEXP x)
₹
 if (!Rf_isLogical(x)) Rf_error("`x` should be of the type 'logical'");
 size_t n = XLENGTH(x), i, k;
 const int* xp = LOGICAL(x);
 size_t* d = (size_t*)malloc(n*sizeof(size_t)); // conservative size
 if (!d) Rf_error("memory allocation error");
 for (i=0, k=0; i<n; ++i)</pre>
 if (xp[i] != NA_LOGICAL && xp[i])
 d\lceil k++\rceil = i;
 // Rf allocVector can longjmp, memory leak possible...
 SEXP y = PROTECT(Rf_allocVector(REALSXP, k));
 double* yp = REAL(y); // yes, the type is double; ready for long vectors
 for (i=0; i<k; ++i)
 yp[i] = (double)d[i]+1; // R uses 1-based indexing
 free(d);
 (continues on next page)
```

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```
UNPROTECT(1);
 return y;
}
/* R
which1 <- function(x)</pre>
 if (!is.logical(x)) x <- as.logical(x)</pre>
 .Call("C_which1", x, PACKAGE="which1")
7
R */
```

Some tests:

```
csource("~/R/cpackagedemo/inst/examples/which1.c")
which1(c(TRUE, FALSE, TRUE, NA, TRUE))
[1] 1 3 5
```

Exercise 14.13 R's which returns either an int or a double vector, depending on the size of the input vector (whether it is shorter than  $2^{31} - 1$ ). Rewrite the above to take that into account: integer arithmetic is slightly faster.

(\*) R's exception handling uses a long jump<sup>10</sup>. Therefore, when calling C::Rf\_error (whether directly or not) normal stack unwinding will not occur. This is particularly important when using C++ objects which deallocate memory in their destructors as they might not be invoked whatsoever.

In the above example, a call to C::Rf\_allocVector may trigger a long jump, e.g., if we run out of available memory. In such a case, d will not be freed.

Thus, care should be taken to make sure there are no memory leaks. We can sometimes switch to C::R\_alloc(n, size) which allocates n\*size bytes. The memory it requests will automatically be garbage-collected at the end of a .Call.

Otherwise, we should ensure that blocks relying on manual memory allocation are not mixed with the calls to R API functions. In our C::which1, it would be better to determine the desired size of y and allocate it before calling **C**::malloc.

**Example 14.14** (\*) If we do not like that we are potentially wasting memory in the case of sparse logical vectors, we can rely on dynamically growable arrays. Below is a C++ rewrite of the above function using deque (double-ended queue) from the language's standard library.

```
#include <deque>
 (continues on next page)
```

<sup>10</sup> https://en.wikipedia.org/wiki/Setjmp.h

(continued from previous page)

```
extern "C" SEXP C_which2(SEXP x)
{
 if (!Rf_isLogical(x)) Rf_error("`x` should be of the type 'logical'");
 size_t n = XLENGTH(x), i, k=0;
 const int* xp = LOGICAL(x);
 // precompute k, Rf_allocVector can do a longjmp
 for (i=0; i<n; ++i) if (xp[i] != NA_LOGICAL && xp[i]) k++;</pre>
 SEXP y = PROTECT(Rf_allocVector(REALSXP, k));
 double* yp = REAL(y); // ready for long vectors
 std::deque<size_t> d; // allocates memory
 for (i=0; i<n; ++i)
 if (xp[i] != NA LOGICAL \&\& xp[i])
 d.push_back(i);
 i=0;
 for (size_t e : d)
 yp[i++] = (double)e+1; // R uses 1-based indexing
 UNPROTECT(1);
 return y; // d's destructor will be called automatically
}
/* R
which2 <- function(x)</pre>
ſ
 if (!is.logical(x)) x <- as.logical(x)
 .Call("C which2", x, PACKAGE="which2")
7
R */
```

### Example calls:

```
csource("~/R/cpackagedemo/inst/examples/which2.cpp")
x <- (runif(10) > 0.5)
stopifnot(which(x) == which1(x))
stopifnot(which(x) == which2(x))
```

Alternatively, we could have used C::realloc to extend an initially small buffer created using C::malloc by, say, 50% whenever it is about to overflow.

### 14.2.5 Lists

For safety reasons<sup>11</sup>, we do not get access to the underlying pointers in lists and character vectors. List items can be read by calling **C**::**VECTOR\_ELT**(x, index) and can be set with **C**::**SET\_VECTOR\_ELT**(x, index, newval).

Note that lists (VECSXPs) are comprised of SEXPs of any type. Hence, after extracting an element, its SEXPTYPE needs to be tested using one of the functions listed in Table 14.1. This can be tiresome.

**Example 14.15** Here is a rather useless function that fetches the first and the last element in a given numeric vector or a list. However, if the latter case, we apply the function recursively on all its elements.

```
SEXP C firstlast(SEXP x)
ſ
 if (!Rf_isVector(x) || XLENGTH(x) == 0)
 Rf error("`x` must be a non-empty vector (atomic or generic)");
 else if (Rf isReal(x)) {
 SEXP y = PROTECT(Rf_allocVector(REALSXP, 2));
 // first
 REAL(y)[0] = REAL(x)[0];
 REAL(y)[1] = REAL(x)[XLENGTH(x)-1]; // last
 UNPROTECT(1);
 return y;
 else if (Rf_isVectorList(x)) {
 SEXP y = PROTECT(Rf_allocVector(VECSXP, 2));
 // VECTOR_ELT(x, i) is PROTECTEd by the container;
 // SET_VECTOR_ELT does not trigger GC; no need to call PROTECT
 // on the result of C_firstlast(...) in this context
 SET_VECTOR_ELT(y, 0, C_firstlast(VECTOR_ELT(x, 0)));
 SET_VECTOR_ELT(y, 1, C_firstlast(VECTOR_ELT(x, XLENGTH(x)-1)));
 UNPROTECT(1);
 return y;
 7
 else
 Rf_error("other cases left as an exercise");
 return R_NilValue; // avoid compiler warning
}
firstlast <- function(x)</pre>
 .Call("C_firstlast", x, PACKAGE="firstlast")
R */
```

 $<sup>^{11}</sup>$  To get the object reference counting right, C::SET\_VECTOR\_ELT needs to unprotect the old element and start protecting the new one.

Testing:

```
csource("~/R/cpackagedemo/inst/examples/firstlast.c")
firstlast(c(1, 2, 3))
[1] 1 3
firstlast(list(c(1, 2, 3), c(4, 5), 6))
[[1]]
[1] 1 3
##
[[2]]
[1] 6 6
firstlast(list(c(1, 2, 3), 4, 5, list(6, c(7, 8), c(9, 10, 11))))
[[1]]
[1] 1 3
##
[[2]]
[[2]][[1]]
[1] 6 6
[[2]][[2]]
[1] 9 11
```

**Exercise 14.16** Implement a C function that returns the longest vector in a given list. Use C::Rf\_isVector to check whether a given object is an atomic or a generic vector, and hence if C::XLENGTH can be called thereon.

**Exercise 14.17** Inscribe your version of **unlist**. Consider scanning the input list twice. First, determine the size of the output vector. Second, fill the return object with the un-listed values.

**Exercise 14.18** Write a C function that takes a list of numeric vectors of identical lengths. Return their elementwise sum: the first element of the output should be the sum of the first elements in every input vector, and so forth.

## 14.2.6 Character vectors and individual strings (\*)

Character vectors (STRSXPs) are similar to VECSXPs except that they only carry individual strings which are represented using a separate data type, CHARSXP. C::STRING\_ELT(x, index) and C::SET\_STRING\_ELT(x, index, newval) play the role of the element getters and setters.

**Important** If we are not interested in text processing but rather in handling *categorical* data or defining grouping variables, we should consider converting character vectors to *factors* before issuing a .Call. Comparing small integers is much faster than strings; see below for more details.

Because of R's string cache, there are no duplicate strings in the memory. However, this feature could only be guaranteed by making data in CHARSXPs read-only. We can

access the underlying const char\* pointer by calling **C**::**CHAR**(s). As typical in C, a string is terminated by byte o.

**Note** R strings may be of different encodings; compare Section 6.1.1. For portability and peace of mind, it is best to preprocess the arguments to .Call using enc2utf8, which converts all strings to UTF-8<sup>12</sup>.

Despite being the most universal encoding, UTF-8 does not represent each code point using a fixed number of bytes. For instance, computing the string length requires iterating over all its elements. For CHARSXPS, **C**::**XLENGTH** returns the number of *bytes*, not including the trailing o.

It is thus best to leave the processing of strings to the dedicated libraries, e.g., ICU<sup>13</sup> or rely on functions from the **stringi** package [27] at the R level.

C strings can be converted to CHARSXPs by calling C::Rf\_mkCharCE(stringbuf, CE\_UTF8) or C::Rf\_mkCharLenCE(stringbuf, buflen, CE\_UTF8). If we are sure that a string is in ASCII (a subset of UTF-8), we can also call C::Rf\_mkChar(stringbuf).

We should never return CHARSXPs as results to R. They are for internal use only. They must be wrapped inside a character vector, e.g., using C::Rf\_ScalarString.

## 14.2.7 Calling R functions from C (\*\*)

Section 5.11 of [63] discusses ways to call R functions in C. To understand them, we will first need to study the material from the remaining chapters of our book, i.e., environments and the related evaluation model. They can be useful, e.g., when calling optimisation algorithms implemented in C on objective functions written in R.

## 14.2.8 External pointers (\*\*)

For storing arbitrary C pointers, there is a separate basic R type named externalptr (SEXPTYPE of EXTPTRSXP); see Section 5.13 of [63] for more details.

We can use them to maintain dynamic data structures or resource handlers between calls to R functions. The problem with these is that pointers are passed as... pointers. They can easily break R's pass-by-value-like semantics, where changes to the state of the referenced object will be visible outside the call.

Furthermore, pointers are not serialisable. They cannot be saved for use in another R session.

**Example 14.19** (\*\*) inst/examples/stack.cpp provides a C++ implementation of the stack data structure, being a last-in-first-out container of arbitrary R objects:

<sup>&</sup>lt;sup>12</sup> Take care when calling **C::Rprintf**, though. It should only be used to output messages in the *native* encoding, which does not necessarily have to be UTF-8, although this landscape is slowly changing. Sticking to ASCII is a safe choice.

<sup>13</sup> https://icu.unicode.org/

```
#include <deque>
class S : public std::deque<SEXP>
{
 public: ~S()
 { // destructor: release all SEXPs so that they can be GC'd
 while (!this->empty()) {
 SEXP obj = this->front();
 this->pop_front();
 R_ReleaseObject(obj);
 }
 }
};
S* get_stack_pointer(SEXP s, bool check_zero=true) // internal function
ſ
 if (TYPEOF(s) != EXTPTRSXP)
 Rf error("not an external pointer");
 SEXP tag = R_ExternalPtrTag(s); // our convention, this can be anything
 if (TYPEOF(tag) != CHARSXP || strcmp(CHAR(tag), "stack") != 0)
 Rf_error("not a stack");
 S* sp = (S*)R_ExternalPtrAddr(s);
 if (check_zero && !sp)
 Rf_error("address is 0");
 return sp;
}
void stack_finaliser(SEXP s) // internal function
{
 // called during garbage collection
 S* sp = get stack pointer(s, false);
 if (sp) {
 delete sp; // destruct S, release SEXPs
 R_ClearExternalPtr(s);
 }
}
extern "C" SEXP C_stack_create()
{
 S* sp = new S(); // stack pointer
 SEXP s = PROTECT(
 R_MakeExternalPtr((void*)sp, /*tag*/mkChar("stack"), R_NilValue)
 (continues on next page)
```

```
);
 R_RegisterCFinalizerEx(s, stack_finaliser, TRUE); // auto-called on GC
 UNPROTECT(1);
 return s;
}
extern "C" SEXP C_stack_empty(SEXP s)
ſ
 S* sp = get_stack_pointer(s);
 return Rf_ScalarLogical(sp->empty());
7
extern "C" SEXP C_stack_push(SEXP s, SEXP obj)
 S* sp = get stack pointer(s);
 R_PreserveObject(obj);
 sp->push_front(obj);
 return R_NilValue;
}
extern "C" SEXP C_stack_pop(SEXP s)
{
 S* sp = get_stack_pointer(s);
 if (sp->empty())
 Rf_error("stack is empty");
 SEXP obj = sp->front();
 sp->pop_front();
 R_ReleaseObject(obj);
 return obj;
7
/* R
stack_create <- function()</pre>
 .Call("C_stack_create", PACKAGE="stack")
stack_empty <- function(s)</pre>
 .Call("C_stack_empty", s, PACKAGE="stack")
stack_push <- function(s, obj)</pre>
 .Call("C_stack_push", s, obj, PACKAGE="stack")
stack pop <- function(s)</pre>
 .Call("C_stack_pop", s, PACKAGE="stack")
R */
```

Note how we preserve R objects from garbage collection. Some tests:

```
csource("~/R/cpackagedemo/inst/examples/stack.cpp")
s <- stack_create()
print(s)
<pointer: 0x556ded58c520>
typeof(s)
[1] "externalptr"
for (i in c("one", "two", "Spanish Inquisition"))
 stack_push(s, i)
while (!stack_empty(s))
 print(stack_pop(s))
[1] "Spanish Inquisition"
[1] "two"
[1] "one"
```

## 14.3 Dealing with compound types

### 14.3.1 Reading and setting attributes

From Chapter 10, we know that compound types such as matrices, factors, or data frames are represented using basic data structures. Usually, they are atomic vectors or lists organised in a predefined manner.

C::Rf\_getAttrib(x, attrname) and C::Rf\_setAttrib(x, attrname, newval) gets and sets specific attributes of an object x. Their second argument, attrname, should be a one-element STRSXP. For convenience, the constants R\_ClassSymbol, R\_DimNamesSymbol, R\_DimSymbol, R\_LevelsSymbol, R\_NamesSymbol, and R\_RowNamesSymbol can be used instead of the STRSXP versions of the "class", "dimnames", "dim", "levels", "names", and "row.names" strings.

**Example 14.20** Consider a function for testing whether an object is of a given class:

(continued from previous page)

```
const char* c = CHAR(STRING_ELT(class, 0)); // class arg as a C string
 size_t n = XLENGTH(xclass);
 for (size_t i=0; i<n; ++i)</pre>
 if (strcmp(CHAR(STRING_ELT(xclass, i)), c) == 0)
 return Rf_ScalarLogical(TRUE);
 return Rf_ScalarLogical(FALSE);
7
/* R
isofclass <- function(x, class)</pre>
 .Call("C isofclass", x, class, PACKAGE="isofclass")
```

Some tests:

```
csource("~/R/cpackagedemo/inst/examples/isofclass.c")
isofclass(Sys.time(), "POSIXct")
[1] TRUE
isofclass(cbind(1:5, 11:15), "matrix")
[1] FALSE
```

Note that a matrix has an implicit class (reported by the **class** function), but its class attribute does not have to be set. Hence the negative result.

**Example 14.21** Write a function that fetches a particular named element in a list.

#### **Factors** 14.3.2

Factors (Section 10.3.2) are represented as integer vectors with elements in the set {1, 2, ..., k, NA\_integer\_} for some k. They are equipped with the levels attribute, being a character vector of length k. Their class attribute is set to factor.

**Example 14.22** An example implementation of a function to compute the number of occurrences of each factor level is given below.

```
SEXP C_table1(SEXP x)
ſ
 if (!Rf_isFactor(x)) Rf_error("`x` is not a 'factor' object");
 size_t n = XLENGTH(x);
 const int* xp = INTEGER(x); // `x` is INTSXP
 SEXP levels = Rf_getAttrib(x, R_LevelsSymbol); // `levels` is a STRSXP
 size_t k = XLENGTH(levels);
```

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```
SEXP y = PROTECT(Rf_allocVector(REALSXP, k));
 double* vp = REAL(v);
 for (size_t i=0; i<k; ++i)</pre>
 yp[i] = 0.0;
 for (size_t j=0; j<n; ++j) {</pre>
 if (xp[j] != NA_INTEGER) {
 if (xp[j] < 1 || xp[j] > k)
 Rf_error("malformed factor"); // better safe than sorry
 yp[xp[j]-1] += 1.0; // levels are 1..k, but C needs 0..k-1
 }
 7
 Rf_setAttrib(y, R_NamesSymbol, levels); // set names attribute
 UNPROTECT(1);
 return y;
}
/* R
table1 <- function(x)
€
 if (!is.factor(x)) x <- as.factor(x)</pre>
 .Call("C_table1", x, PACKAGE="table1")
7
R */
```

Testing:

```
csource("~/R/cpackagedemo/inst/examples/table1.c")
table1(c("spam", "bacon", NA, "spam", "eggs", "bacon", "spam", "spam"))
bacon eggs spam
2 1 4
```

**Exercise 14.23** Create a function to compute the most frequently occurring value (mode) in a given factor. Return a character vector. If a mode is ambiguous, return all the possible candidates.

### 14.3.3 Matrices

Matrices (Chapter 11) are *flat* atomic vectors or lists with the dim attribute being a vector of length two. The class attribute does not have to be set (but the **class** function returns matrix and array).

Matrices are so important in data analysis that they have been blessed with a few dedicated functions available at the C level. C::Rf\_isMatrix tests if a given object meets the criteria mentioned above.

R relies on the Fortran order of matrix elements, i.e., it uses the column-major

alignment. Let A be a matrix with n rows and m columns (compare  $C::Rf_nrows$  and  $C::Rf_ncols$ ). Then, the element in the i-th row and the j-th column is at A[i+n\*j].

**C::Rf\_allocMatrix**(sexptype, n, m) allocates a new matrix. The dimnames attributes must be handled manually, though.

**Example 14.24** Here is a function to compute the transpose of a numeric matrix:

```
SEXP C_transpose(SEXP x)
{
 if (!Rf_isMatrix(x) || !Rf_isReal(x))
 Rf_error("`x` must be a real matrix");
 size_t n = Rf nrows(x);
 size_t m = Rf_ncols(x);
 const double* xp = REAL(x);
 SEXP y = PROTECT(Rf_allocMatrix(REALSXP, m, n));
 double* yp = REAL(y);
 for (size_t i=0; i<n; ++i)</pre>
 for (size_t j=0; j<m; ++j)</pre>
 yp[j+m*i] = xp[i+n*j];
 SEXP dimnames = Rf_getAttrib(x, R_DimNamesSymbol);
 if (!Rf_isNull(dimnames)) {
 SEXP tdimnames = PROTECT(Rf_allocVector(VECSXP, 2));
 SET_VECTOR_ELT(tdimnames, 0, VECTOR_ELT(dimnames, 1));
 SET_VECTOR_ELT(tdimnames, 1, VECTOR_ELT(dimnames, 0));
 Rf_setAttrib(y, R_DimNamesSymbol, tdimnames); // set dimnames
 UNPROTECT(1);
 // dimnames may have the names attribute too (left as an exercise)
 }
 UNPROTECT(1);
 return y;
}
/* R
transpose <- function(x)</pre>
{
 if (!is.matrix(x)) x <- as.matrix(x)</pre>
 if (!is.double(x)) x[] <- as.double(x) # preserves attributes
 .Call("C_transpose", x, PACKAGE="transpose")
}
R */
```

```
csource("~/R/cpackagedemo/inst/examples/transpose.c")
transpose(cbind(c(1, 2, 3, 4), c(5, 6, 7, 8)))
[,1] [,2] [,3] [,4]
[1,] 1 2 3 4
[2,] 5 6 7 8
transpose(Titanic[, "Male", "Adult",])
1st 2nd 3rd Crew
No 118 154 387 670
Yes 57 14 75 192
```

**Exercise 14.25** Author a C function named **table2** that computes a two-way contingency table.

### 14.3.4 Data frames

Data frames (Chapter 12) are lists of m vectors of identical lengths n or matrices of n rows for some n and m. The character vectors stored in the row.names and names attributes give the n row and m column labels. They are objects of the S3 class data. frame.

We process data frames as ordinary lists. However, assuming we only want to process numeric data, we can extract the columns of interest and put them inside a matrix at the R level. If element grouping is required, they can be accompanied by a factor or a list of factor variables. In many applications, this is a good-enough strategy. Let us not complicate our lives beyond what is necessary.

## 14.4 Using existing function libraries

## 14.4.1 Checking for user interrupts

Long computations may lead to R's becoming unresponsive. The user may always request to cancel the evaluation of the current expression by pressing Ctrl+C.

To process the event queue, we should occasionally call C::R\_CheckUserInterrupt(), e.g., in every iteration of a complex for loop. Note that R might decide never to return to our function. Thus, we have to prevent memory leaks, e.g., by preferring C::R\_alloc over C::malloc.

## 14.4.2 Generating pseudorandom numbers

**C::unif\_rand** returns a single pseudorandom deviate from the uniform distribution on the unit interval. It is the basis for generating numbers from all other supported distributions (Section 6.7.1 of [63]).

It uses the same pseudorandom generator as we described in Section 2.1.5. To read and memorise its seed (the `.Random.seed` object in the global environment), we have

to call C::GetRNGstate() and C::PutRNGstate() at the beginning and the end of our function, respectively.

**Example 14.26** Below is a function to generate a pseudorandom bit sequence:

```
SEXP C_randombits(SEXP n)
{
 if (!Rf_isInteger(n) || XLENGTH(n) != 1)
 Rf_error("`n` should be a single integer");
 int _n = INTEGER(n)[0];
 if (_n == NA_INTEGER |/ _n < 1)</pre>
 Rf error("incorrect `n`");
 SEXP y = PROTECT(Rf_allocVector(INTSXP, _n));
 int* yp = INTEGER(y);
 GetRNGstate();
 for (int i=0; i<_n; ++i)</pre>
 yp[i] = (int)(unif_rand()>0.5); // not the best way to sample bits
 PutRNGstate();
 UNPROTECT(1);
 return y;
}
/* R
randombits <- function(n)</pre>
{
 if (!is.integer(n)) n <- as.integer(n)</pre>
 .Call("C randombits", n, PACKAGE="randombits")
7
R */
```

Let us play with the above:

```
csource("~/R/cpackagedemo/inst/examples/randombits.c")
set.seed(123); randombits(10)
[1] 0 1 0 1 1 0 1 1 1 0
randombits(10)
[1] 1 0 1 1 0 1 0 0 0 1
set.seed(123); randombits(20)
[1] 0 1 0 1 1 0 1 1 1 0 1 0 1 0 0 0 1
set.seed(123); as.integer(runif(20)>0.5) # it's the same "algorithm"
[1] 0 1 0 1 1 0 1 1 1 0 1 0 1 1 0 0 0 1
```

**Exercise 14.27** Create a function to compute the most frequently occurring value (mode) in a given factor object. In the case of ambiguity, return a randomly chosen candidate.

### 14.4.3 Mathematical functions from the R API

Section 6.7 of [63] lists the available statistical distribution functions, mathematical routines and constants, and other numerical utilities.

### 14.4.4 Header files from other R packages (\*)

A package may use header files from another package. For this to be possible, it must include the dependency name in the LinkingTo field of its DESCRIPTION file; see [63] for discussion.

**Exercise 14.28** The **BH** package on CRAN gives access to Boost, the header-only C++ libraries that define many useful algorithms and data structures. Create an R package that calls **C++::boost::math::gcd** after issuing the #include <boost/math/common\_factor.hpp> directive.

### 14.4.5 Specifying compiler and linker flags (\*\*)

We can pass arbitrary flags to the compiler or linker, e.g., to use any library installed on our system.

Basic configuration can be set via Makevars (or Makevars.win on  $W^{****}ws$ ), e.g., by setting PKG\_CFLAGS or PKG\_LIBS variables.

For maximum portability across different platforms, which is overall challenging to ensure if we do not wish to exclude W\*\*\*\*ws users, we might be required to author custom configure (and configure.win) scripts.

For more information, see [63]. In particular, it discusses how to use  $OpenMP^{14}$  in our projects.

### 14.5 Exercises

**Exercise 14.29** Answer the following questions about the C language API for R.

- What are the most common SEXPTYPEs?
- How are missing values represented?

<sup>&</sup>lt;sup>14</sup> Most R functions are single-threaded by design. It is up to the user to decide whether and how they would like their code to be parallelised. More often than not, computations in the data science domain are naïvely parallelisable (e.g., Monte Carlo simulations, exhaustive grid search, etc.). In such cases, the R package parallel might be helpful: it defines parallel versions of lapply and apply. However, for serious jobs, running multiple single-threaded R instances via, e.g., the slurm workload manager might be a better idea than starting a process that spawns many child threads.

- - How can we check if an int is a missing value? What about a double?
  - How to prevent SEXPs from being garbage-collected?
  - · How are character vectors represented? What is the difference between a CHARSXP and a STRSXP?
  - Why is it better to handle factor objects rather than raw character vectors if we merely would like to define grouping variables?
  - How are R matrices represented in C? Does R use the C or Fortran order of matrix elements?
  - How are R data frames handled in C?

Exercise 14.30 Implement the C versions of the rep, seq, rle, match, findInterval, sample, order, unique, and split functions.

**Exercise 14.31** (\*) Read Writing R Extensions [63] in its entirety.

**Exercise 14.32** (\*) Download R's source code from CRAN<sup>15</sup> or its **Subversion**<sup>16</sup> (SVN) repository. Explore the header files in the src/include subdirectory. They are part of the callable API.

<sup>15</sup> https://stat.ethz.ch/R/daily

<sup>16</sup> https://svn.r-project.org/R/trunk

# Unevaluated expressions (\*)

In this and the remaining chapters, we will learn some hocus-pocus that should only be of interest to the advanced-to-be<sup>1</sup> and open-minded R programmers who would like to understand what is going on under our language's bonnet. In particular, we will inspect the mechanisms behind why certain functions act differently from what we would expect them to do if a *standard* evaluation scheme was followed (compare **subset** and **transform** mentioned in Section 12.3.9).

Namely, in normal programming languages, when we execute something like:

```
plot(x, exp(x))
```

the expression  $\exp(x)$ , is evaluated *first* and its value<sup>2</sup> (in this case: probably a numeric vector) is only then passed to the **plot** function as the actual parameter. Thus, if x is set to be  $\sec(0, 10, \end{tension})$ , the above never means anything else than:

```
plot(c(0.00, 0.01, 0.02, 0.03, ...), c(1.0000, 1.0101, 1.0202, 1.0305, ...))
```

But R was heavily inspired by the S language from which it has taken the notion of lazy arguments (Chapter 17). It is thus equipped with the ability to apply a set of techniques referred to as *metaprogramming* (computing on the language, reflection). With it, we can define functions that do not take their arguments for granted and clearly see the code fragments passed to them. Having access to such *unevaluated expressions*, we can do to them whatever we please: print, modify, evaluate on different data, or ignore whatsoever.

In theory, this enables implementing many potentially helpful<sup>3</sup>, beginner-friendly features and express certain requests in a more concise manner. For instance, that the y-axis labels in Figure 2.2 could be generated automatically is precisely because **plot** was able to see not only a vector like c(1.0000, 1.0101, 1.0202, 1.0305, ...) but also the expression that generated it, exp(x).

<sup>&</sup>lt;sup>1</sup> Remember that this book is supposed to be read from the beginning to the end. Also, if you have not tested yourself against all the 300-odd exercises suggested so far, please do it before proceeding with the material presented here. Only practice makes perfect, and nothing is built in a day. Give yourself time: you can always come back later.

<sup>&</sup>lt;sup>2</sup> Or a reference/pointer to an object that stores the said value.

<sup>&</sup>lt;sup>3</sup> The original authors of R (R. Ihaka and R. Gentleman), in [37], mention: "A policy of *lazy arguments* is very useful because it means that, in addition to the value of an argument, its symbolic form can be made available in the function being called. This can be very useful for specifying functions or models in symbolic form."

Nonetheless, as a form of *untamed freedom of expression*<sup>4</sup>, metaprogramming has the endless potential to arouse chaos, confusion, and division in the user community. In particular, we can introduce a dialect *within* our language that people outside our circle will not be able to understand. Once it becomes a dominant one, other users will feel excluded.

Cursed be us, for we are about to start eating from the tree of the knowledge of good and evil. But remember: with great power comes great fun (and responsibility).

## 15.1 Expressions at a glance

At the most general level, *expressions* (statements) in a language like R can be classified into two groups:

- simple expressions:
  - constants (e.g., 3.14, 2i, 42L, NA\_real\_, Inf, NaN, NA, FALSE, TRUE, "character string", NULL, -1.3e-16, and 0x123abc),
  - names (symbols, identifiers; e.g., x, iris, sum, data.frame, spam, `+`, `[<-`, and spanish\_inquisition),</li>
- *compound expressions* combinations of n + 1 expressions (simple or compound) of the form:

$$(f,e_1,e_2,\dots,e_n).$$

As we will soon see, compound expressions represent a *call* to f (an *operator*) on a sequence of arguments  $e_1, e_2, \ldots, e_n$  (*operands*). It is why, equivalently, we denote them with  $f(e_1, e_2, \ldots, e_n)$ .

On the other hand, *names* have no meaning without an explicitly stated context, which we will explore in Chapter 16. Prior to that, we treat them as *meaning-less*.

Hence, for the time being, we are only interested in the *syntax* or *grammar* of our language, not the *semantics*. We are abstract in the sense that, in the expression mean(rates)+2, which we know from Section 9.3.5 that we can equivalently express as `+`(mean(rates), 2), neither mean, x, nor even `+` have the *usual* sense. Therefore, we should treat them as equivalent to, say, f(g(x), 2) or  $nobody(expects(spanish_inquisition), 2)$ .

<sup>&</sup>lt;sup>4</sup> In the current author's opinion, R (as a whole, in the sense of R (GNUS) as a language and an environment) would be better off if an ordinary programmer was not exposed so much to functions heavily relying on metaprogramming. A healthy user can perfectly manage without (and thus refrain from using) them. The fact that we call them advanced will not make us cool if we start horsing around with nonstandard evaluation. Perverse is perhaps a better label.

## 15.2 Language objects

There are three types of language objects in R:

- name (symbol) represents object names in the sense of simple expressions: names in Section 15.1;
- call stores unevaluated function calls in the sense of *compound expressions* above;
- expression, quite confusingly, represents a *sequence* of simple or compound expressions (constants, names, or calls).

One way to create a simple or compound expression is by *quoting*, where the R interpreter is asked to refrain from evaluating a given command:

```
quote(spam) # name (symbol)
spam
quote(f(x)) # call
f(x)
quote(1+2+3*pi) # another call
1 + 2 + 3 * pi
```

None of the above was executed. In particular, spam has no sense in the current context (whichever that is). It is not the meaning that we are after now.

Single strings can be converted to names by calling:

```
as.name("spam")
spam
```

Calls can be built programmatically by invoking:

```
call("sin", pi/2)
sin(1.5707963267949)
```

Sometimes we would rather have the arguments quoted:

```
call("sin", quote(pi/2))
sin(pi/2)
call("c", 1, exp(1), quote(exp(1)), pi, quote(pi))
c(1, 2.71828182845905, exp(1), 3.14159265358979, pi)
```

Objects of the type expression can be thought of as list-like sequences that consist of simple or compound expressions.

```
(exprs <- expression(1, spam, mean(x)+2))
expression(1, spam, mean(x) + 2)</pre>
```

All arguments were quoted. We can select or subset the individual statements using the extraction or index operators:

```
exprs[-1]
expression(spam, mean(x) + 2)
exprs[[3]]
mean(x) + 2
```

**Exercise 15.1** Check the type of the object returned by a call to c(1, "two", sd, list(3, 4:5), expression(3+3)).

There is also an option to *parse* a given text fragment or a whole source file:

```
parse(text="mean(x)+2")
expression(mean(x) + 2)
parse(text=" # two code lines (comments are ignored by the parser)
 x <- runif(5, -1, 1)
 print(mean(x)+2)
")
expression(x <- runif(5, -1, 1), print(mean(x) + 2))
parse(text="2+") # syntax error - unfinished business
Error in parse(text = "2+"): <text>:2:0: unexpected end of input 1: 2+ ^
```

**Important** The **deparse** function converts language objects to character vectors, e.g.:

```
deparse(quote(mean(x+2)))
[1] "mean(x + 2)"
```

This function has the nice side effect of tidying up the code formatting:

```
exprs <- parse(text=
 "`+`(x, 2)->y; if(y>0) print(y**10|>log()) else { y<--y; print(y)}")</pre>
```

Let us print them out:

```
for (e in exprs)
 cat(deparse(e), sep="\n")
y <- x + 2
if (y > 0) print(log(y^10)) else {
y <- -y
print(y)
}</pre>
```

**Note** Calling **class** on objects of the three aforementioned types yields name, call, and expression, whereas **typeof** returns symbol, language, and expression, respectively.

## 15.3 Calls as combinations of expressions

We have mentioned that calls (compound expressions) are combinations of simple or compound expressions of the form  $(f, e_1, \dots, e_n)$ . The first expression on the list, denoted above with f, plays a special role. It is precisely seen in the following examples:

```
as.call(expression(f, x))
f(x)
as.call(expression(`+`, 1, x)) # `+`(1, x)
1 + x
as.call(expression(`while`, i < 10, i <- i + 1))
while (i < 10) i <- i + 1
as.call(expression(function(x) x**2, log(exp(1))))
(function(x) x^2)(log(exp(1)))
as.call(expression(1, x, y, z)) # utter nonsense, but syntactically valid
1(x, y, z)</pre>
```

Recall from Section 9.3 that operators and language constructs such as **if** and **while** are ordinary functions.

Furthermore, keyword arguments will result in the underlying sequence's being named:

```
expr <- quote(f(1+2, a=1, b=2))
length(expr) # three arguments -> length-4 sequence
[1] 4
names(expr) # NULL if no arguments are named
[1] "" "" "a" "b"
```

## 15.3.1 Browsing parse trees

Square brackets give us access to the individual expressions constituting an object of the type call. For example:

```
expr <- quote(1+x)
expr[[1]]
`+`
expr[c(1, 3, 2)]</pre>
```

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```
x + 1
expr[c(2, 3, 1, 3)]
1(x, `+`, x)
```

A compound expression was defined recursively: it may consist of other compound expressions. For instance, the following statement:

```
expr <- quote(
 while (i < 10) {</pre>
 cat("i = ", i, "\n", sep="")
 i <- i+1
 }
)
```

can be rewritten<sup>5</sup> using the f(...) notation like:

```
quote(
 `while`(
 `<`(i, 10),
 `{`(cat("i = " , i, "\n", sep=""), `<-`(i, `+`(i, 1)))
)
)
```

We can dig into all the subexpressions using a series of extractions:

```
expr[[2]][[1]] # expr[[c(2, 1)]]
expr[[3]][[3]][[3]] # expr[[c(3, 3, 3)]]
i + 1
expr[[3]][[3]][[3]][[1]] # expr[[c(3, 3, 3, 1)]]
`+`
```

```
(this is not valid R syntax)
(
 `while`,
 (`<`, i, 10),
 `{`,
 (cat, "i = ", i, "\n", sep=""),
 `<-`,
 (`+`, i, 1)
)
)
```

<sup>&</sup>lt;sup>5</sup> (\*) Equivalently, in the fully parenthesised Polish notation (f,...) (the prefix notation; traditionally used in source code s-expressions in Lisp), we would express it like:

#### **Example 15.2** We can even compose a recursive function to traverse the whole parse tree:

```
recapply <- function(expr)</pre>
{
 if (is.call(expr)) lapply(expr, recapply)
 else expr
}
str(recapply(expr))
List of 3
$: symbol while
$:List of 3
 ..$: symbol <
##
##
 ..$: symbol i
..$: num 10
$:List of 3
 ..$: symbol {
..$:List of 5
 $: symbol cat
 $: chr "i = "
##
 $: symbol i
##
##
 $: chr "\n"
 $ sep: chr ""
##
 ..$:List of 3
##
 $: symbol <-
##
 $: symbol i
##
##
 $:List of 3
 $: symbol +
 $: symbol i
##
 $: num 1
```

# 15.3.2 Manipulating calls

The R language is *homoiconic*: it can treat code as data. This includes the ability to manipulate it on the fly. This is because, just like on lists, we can freely use the replacement versions of `[` and `[[` on objects of the type call.

```
expr[[2]][[1]] <- as.name("<=") # was: `<`
expr[[3]] <- quote(i <- i * 2) # was: {...}
print(expr)
while (i <= 10) i <- i * 2</pre>
```

We are only limited by our imagination. We should spend some time and contemplate how powerful this is, knowing that soon we will become able to evaluate any expression in different contexts.

# 15.4 Inspecting function definition and usage

# 15.4.1 Getting the body and formal arguments

Consider the following function:

```
test <- function(x, y=1)
 x+y # whatever</pre>
```

We know from the first part of this book that calling **print** on a function reveals its source code. But there is more. We can fetch its formal parameters in the form of a named list<sup>6</sup>:

```
formals(test)
$x
##
##
##
$y
[1] 1
```

Note that the expressions corresponding to the default arguments are stored as ordinary list elements (for more details, see Section 17.2).

Furthermore, we can access the function's body:

```
body(test)
x + y
```

It is an object of the now well-known class call. Thus, we can customise it as we please:

<sup>&</sup>lt;sup>6</sup> (\*) Actually, a special internal datatype called pairlist, which is rarely seen at the R level; see [66] and [63] for information on how to deal with them in C. In the current context, seeing pairlists as named lists is perfectly fine.

### 15.4.2 Getting the expression passed as an actual argument

A call to **substitute** reveals the expression passed as a function's argument.

```
test <- function(x) substitute(x)</pre>
```

Some examples:

```
test(1)
[1] 1
test(2+spam)
2 + spam
test(test(test(!!7)))
test(test(!!7))
test() # it is not an error
```

Chapter 17 notes that arguments are evaluated only on demand (lazily): **substitute** triggers no computations. This opens the possibility to author functions that interpret their input whichever way they like; see Section 9.4.7, Section 12.3.9, and Section 17.5 for examples.

**Example 15.3** *library* (see Section 7.3.1) specifies the name of the package to be loaded both in the form of a character string and a name:

```
library("gsl") # preferred
library(gsl) # discouraged; via as.character(substitute(package))
```

A user saves two keystrokes at the cost of not being able to prepare the package name programmatically before the call:

```
which_package <- "gsl"
library(which_package) # library("which_package")
Error in library(which_package): there is no package called
'which_package'</pre>
```

In order to make the above possible, we need to alter the function's character.only argument (which defaults to FALSE):

```
library(which_package, character.only=TRUE) # OK
```

**Exercise 15.4** In many functions, we can see a call like **deparse(substitute(**arg)) or **as. character(substitute(**arg)). Study the source code of **plot.default**, **hist.default**, **prop.test**, **wilcox.test.default** and the aforementioned **library**. Explain why they do that. Propose a solution to achieve the same functionality without using reflection techniques.

# 15.4.3 Checking if an argument is missing

missing checks whether an argument was provided:

```
test <- function(x) missing(x)</pre>
test(1)
[1] FALSE
test()
[1] TRUE
```

Exercise 15.5 Study the source code of sample, seq. default, plot. default, matplot, and t. test.default. Determine the role of a call to missing. Would introducing a default argument *NULL* and testing its value with **is.null** constitute a reasonable alternative?

#### Determining how a function was called

Even though this somewhat touches on the topics discussed in the two following chapters, it is worth knowing that sys.call can look at the call stack and determine how the current function was invoked.

Moreover, match.call takes us a step further: it returns a call with argument names matched to a function's formal parameters list. For instance:

```
test <- function(x, y, ..., a="yes", b="no")</pre>
{
 print(sys.call()) # sys.call(0)
 print(match.call())
}
x <- "maybe"
test("spam", "bacon", "eggs", u = "ham"<"jam", b=x)</pre>
test("spam", "bacon", "eggs", u = "ham" < "jam", b = x)
test(x = "spam", y = "bacon", "eggs", u = "ham" < "jam", b = x)
```

In both cases, the results are objects of the type call. We know how to manipulate them already.

Another example where we see that we can access the call stack much more deeply:

```
f <- function(x)
{
 g <- function(y)</pre>
 {
 cat("g:\n")
 print(sys.call(0))
 print(sys.call(-1)) # go back one frame
 У
 }
 cat("f:\n")
```

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```
print(sys.call(0))
 g(x+1)
}

f(1)
f:
f(1)
g:
g(x+1)
f(1)
f(1)
[1] 2
```

**Note** Let us formalise the order of matching function parameters *to* the passed arguments. As described in Section 4.3 of [67], it proceeds as follows.

- 1. First, keyword arguments with names are matched exactly. Each name is matched at most once.
- 2. Then, we take the remaining keyword arguments, but with the partial matching of names listed before the ellipsis, `...`. Each match must be unambiguous.
- 3. Third, we apply the positional matching to the remaining parameters.
- 4. Last, the ellipsis (if present) consumes all the remaining arguments (named or not).

For instance:

```
test <- function(spam, jasmine, jam, ..., option=NULL)
 print(match.call())</pre>
```

#### Example calls:

```
test(1, 2, 3, 4, option="yes")
test(spam = 1, jasmine = 2, jam = 3, 4, option = "yes")
test(1, 2, jasmine="no", sp=4, ham=7)
Warning in test(1, 2, jasmine = "no", sp = 4, ham = 7): partial argument
match of 'sp' to 'spam'
Warning in match.call(definition, call, expand.dots, envir): partial
argument match of 'sp' to 'spam'
test(spam = 4, jasmine = "no", jam = 1, 2, ham = 7)
test(1, 2, ja=7) # ambiguous match
Warning in test(1, 2, ja = 7): partial argument match of 'ja' to 'jasmine'
Error in test(1, 2, ja = 7): argument 3 matches multiple formal arguments
test(o=7) # partial matching of `option` failed - `option` is after `...`
test(o = 7)
```

Note again that our environment uses **options**(warnPartialMatchArgs=TRUE).

**Exercise 15.6** A function can<sup>7</sup> see how it was defined by its maker. Call **sys.function** inside its body to reveal that.

Exercise 15.7 Execute match.call(sys.function(-1), sys.call(-1)) in the g function above.

#### 15.5 Exercises

**Exercise 15.8** *Answer the following questions.* 

- What is a simple expression? What is a compound expression? Give a few examples.
- What is the difference between an object of the type call and that of the type expression?
- What do **formals** and **body** return when called on a function object?
- How to test if an argument to a function was given? Provide a use case for such a verification step.
- Give a few ways to create an unevaluated call.
- What is the purpose of **deparse(substitute(...))?** Give a few examples of functions that use this technique.
- What is the difference between sys.call and match.call?

**Exercise 15.9** Write a function that takes the dot-dot argument. Using match.call (amongst others), determine the list of all the expressions passed via `...`. Allow some of them to be named (just like in one of the above examples). The solution will be given in Section 17.3.

**Exercise 15.10** Write a function  $check_if_calls(f, fun_list)$  that takes another function f on input. Then, it verifies if f calls any of the functions (referred to by their names) from a character vector f unlist.

<sup>&</sup>lt;sup>7</sup> Therefore, it is possible to have a function that returns a modified version of itself.

# *Environments and evaluation (\*)*

In the first part of our book, we discussed the most crucial *basic* object types: numeric, logical, and character vectors, lists (generic vectors), and functions.

In this chapter, we introduce another basic type: *environments*. Like lists, they can be classified as recursive data structures; compare the diagram in Figure 17.2.

**Important** Each object of the type environment consists of:

- a *frame*<sup>1</sup> (Section 16.1), which stores a set of *bindings* that associate variable names with their corresponding values; it can be thought of as a container of named R objects of any type;
- a reference to an *enclosing environment*<sup>2</sup> (Section 16.2.2), which might be inspected (recursively!) when a requested named variable is not found in the current frame.

Even though we rarely interact with them directly (unless we need a hash table-like data structure with a quick by-name element lookup), they are crucial for the R interpreter itself. Namely, we shall soon see that they form the basis of the *environment model of evaluation*, which governs how expressions are computed (Section 16.2).

# 16.1 Frames: Environments as object containers

To create a new, empty environment, we can call the new.env function:

```
e1 <- new.env()
typeof(e1)
[1] "environment"</pre>
```

In this section, we treat environments merely as containers for named objects of any kind, i.e., we deal with the *frame* part thereof.

<sup>&</sup>lt;sup>1</sup> Not to be confused with a *data frame*, i.e., an object (list) of the S3 class data.frame; see Chapter 12.

<sup>&</sup>lt;sup>2</sup> Some also call it a *parent* environment, but we will not. We will try following the nomenclature established in Section 3.2 of [1]. Note that there is a bit of a mess in the R documentation regarding how enclosing environments are referred to.

Let us insert a few elements into e1:

```
e1[["x"]] <- "x in e1"
e1[["y"]] <- 1:3
e1[["z"]] <- NULL # unlike in the case of lists, creates a new element
```

The `[[` operator provides us with a *named list-*like behaviour also in the case of element extraction:

```
e1[["x"]]
[1] "x in e1"
e1[["spam"]] # does not exist
NULL
(e1[["y"]] <- e1[["y"]]*10) # replace with new content
[1] 10 20 30
```

#### 16.1.1 Printing

Printing an environment leads to a quite awkward result:

```
print(e1) # same with str(e1)
<environment: 0x557efb009ab8>
```

It is the address where e1 is stored in the computer's memory. It can serve as the environment's unique identifier.

As we have said, these objects are of rather internal interest. Thus, such an esoteric message was perhaps a good design choice; it wards off novices. However, we can easily get the list of objects stored inside the container by calling names:

```
names(e1) # but attr(e1, "names") is not set
[1] "x" "y" "z"
```

Moreover, **length** gives the number of bindings in the frame:

```
length(e1)
[1] 3
```

#### Environments vs named lists 16.1.2

Environment frames, in some sense, can be thought of as named lists, but the set of admissible operations is severely restricted. In particular, we cannot extract more than one element at the same time using the index operator:

```
e1[c("x", "y")] # but see the `mget` function
Error in e1[c("x", "y")]: object of type 'environment' is not subsettable
```

nor can we refer to the elements by position:

```
e1[[1]] <- "bad key"
Error in e1[[1]] <- "bad key": wrong args for environment subassignment
```

**Exercise 16.1** Check if **lapply** and **Map** can be applied directly on environments. Also, can we iterate over their elements using a **for** loop?

Still, named lists can be converted to environments and vice versa using **as.list** and **as.environment**.

```
as.list(e1)
$x
[1] "x in e1"
##
$y
[1] 10 20 30
##
$z
NULL
as.environment(list(u=42, whatever="it's not going to be printed anyway"))
<environment: 0x557efabc2a18>
as.list(as.environment(list(x=1, y=2, x=3))) # no duplicates allowed
$y
[1] 2
##
$x
[1] 3
```

# 16.1.3 Hash maps: Fast element lookup by name

Environment frames are internally implemented using hash tables (hash maps; see, e.g., [14, 41]) with character string keys.

**Important** A *hash table* is a data structure that implements a very quick<sup>3</sup> lookup and insertion of individual elements *by name*.

The above comes at a price, including what we have already observed above:

- the elements are not ordered in any particular way: they cannot be referred to via a numeric index;
- all element names must be unique.

**Note** A list may be considered a *sequence*, but an environment frame is only, in fact, a *set* (a bag) of *key-value pairs*. In most numerical computing applications, we would rather

<sup>&</sup>lt;sup>3</sup> In hash tables, element lookup, insertion, and deletion take amortised O(1) time.

store, iterate over, and process all the elements *in order*, hence the greater prevalence of the former. Lists still implement the element lookup by name, even though it is slightly slower<sup>4</sup>. However, they are much more universal.

**Example 16.2** A natural use case of manually-created environment frames deals with grouping a series of objects identified by character string keys. Consider a simple pseudocode for counting the number of occurrences of objects in a given container:

```
for (key in some_container) {
 if (!is.null(counter[["key"]]))
 counter[["key"]] <- counter[["key"]]+1
 else
 counter[["key"]] <- 1
}</pre>
```

Let us assume that some\_container is large, e.g., it is generated on the fly by reading a data stream of size n. The runtime of the above algorithm will depend on the data structure used. If the counter is a list, then, theoretically, the worst-case performance will be  $O(n^2)$  (if all keys are unique). On the other hand, for environments, it will be faster by one order magnitude: down to amortised O(n).

**Exercise 16.3** Implement a test function according to the above pseudocode and benchmark the two data structures using **proc.time** on example data.

**Exercise 16.4** (\*) Determine the number of unique text lines in a huge file (assuming that the set of unique text lines fits into memory, but the file itself does not). Also, determine the five most frequently occurring text lines.

# 16.1.4 Call by value, copy on demand: Not for environments

Given any object x, when we issue:

```
y <- x
```

its copy<sup>5</sup> is made so that y and x are independent. In other words, any change to the state of x (or y) is not reflected in y (or x). For instance:

```
x <- list(a=1)
y <- x
y[["a"]] <- y[["a"]]+1
print(y)
$a
[1] 2</pre>
```

(continues on next page)

<sup>&</sup>lt;sup>4</sup> Accessing elements by position (numeric index) in lists takes O(1) time. The worst-case scenario for the element lookup by name is linear with respect to the container size (when the item is not found). Also, inserting new elements at the end takes amortised O(1) time.

<sup>&</sup>lt;sup>5</sup> Delayed (on demand); see below.

(continued from previous page)

```
print(x) # not affected: `x` and `y` are independent
$a
[1] 1
```

The same happens with arguments that we pass to the functions:

```
mod <- function(y, key) # it is like: local_y <- passed_argument
{
 y[[key]] <- y[[key]]+1
 y
}
mod(x, "a")[["a"]] # returns a modified copy of `x`
[1] 2
x[["a"]] # not affected
[1] 1</pre>
```

We can thus say that R imitates the *pass-by-value* strategy here.

**Important** Environments are the only<sup>6</sup> objects that follow the assign- and pass-by-reference strategies.

In other words, if we perform:

```
x <- as.environment(x)
y <- x</pre>
```

then the names x and y are bound to the same object in the computer's memory:

```
print(x)
<environment: 0x557efa2bd1b8>
print(y)
<environment: 0x557efa2bd1b8>
```

Therefore:

```
y[["a"]] <- y[["a"]]+1
print(y[["a"]])
[1] 2
print(x[["a"]]) # `x` is `y`, `y` is `x`
[1] 2</pre>
```

<sup>&</sup>lt;sup>6</sup> We do not count all the tricks we can do at the C language level (Chapter 14). In R, the distinction between pass-by-value and pass-by-reference is slightly more complicated because of the lazy evaluation of arguments (the call-by-need strategy; Chapter 17). We are making an idealisation for didactic purposes here.

The same happens when we pass an environment to a function:

```
mod(y, "a")[["a"]] # pass-by-reference (`y` is `x`, remember?)
[1] 3
x[["a"]] # `x` has changed
[1] 3
```

Thus, any changes we make to an environment passed as an argument to a function will be visible *outside* the call. This minimises time and memory use in certain situations.

**Note** (\*) For efficiency reasons, when we write "y <- x", a copy of x (unless it is an environment) is created only if it is absolutely necessary.

Here is some benchmarking of the *copy-on-demand* mechanism.

```
n <- 100000000 # like, a lot
```

Creation of a new large numeric vector:

```
t0 <- proc.time(); x <- numeric(n); proc.time() - t0
user system elapsed
0.853 1.993 2.852</pre>
```

Creation of a (delayed) copy is instant:

We definitely did not duplicate the n data cells.

Copy-on-demand is implemented using some simple *reference counting*; compare Section 14.2.4. We can inspect that x and y point to the same address in memory by calling:

```
.Internal(inspect(x)) # internal function - do not use it
@7efba1134010 14 REALSXP g0c7 [REF(2)] (len=1000000000, tl=0) 0,0,0,0,...
.Internal(inspect(y))
@7efba1134010 14 REALSXP g0c7 [REF(2)] (len=1000000000, tl=0) 0,0,0,0,...
```

The actual copying is only triggered when we try to modify x or y. This is when they need to be separated.

```
t0 <- proc.time(); y[1] <- 1; proc.time() - t0

user system elapsed

1.227 1.910 3.142
```

Now x and y are different objects.

```
.Internal(inspect(x))
@7efba1134010 14 REALSXP g0c7 [MARK,REF(1)] (len=1000000000, tl=0) 0,0,...
.Internal(inspect(y))
@7ef9c43ce010 14 REALSXP g0c7 [MARK,REF(1)] (len=1000000000, tl=0) 1,0,...
```

The elapsed time is similar to that needed to create x from scratch. Further modifications will already be quick:

### 16.1.5 A note on reference classes (\*\*)

In Section 10.5, we briefly mentioned the S4 system for object-orientated programming. We also have access to its variant, called *reference classes*<sup>7</sup>, which was first introduced in R version 2.12.0. Reference classes are implemented using S4 classes, with the data part being of the type environment. They give a more typical OOP experience, where methods can modify the data they act on in place.

They are theoretically interesting concepts on their own and may be quite appealing to package developers with C++ or Java background. Nevertheless, in the current author's opinion, such classes are alien citizens of our environment, violating its *functional* nature. Therefore, we will not be discussing them here.

A curious reader is referred to **help**("ReferenceClasses") and Chapters 9 and 11 of [11] for more details.

#### 16.2 The environment model of evaluation

In Chapter 15, we said that there are three types of expressions: constants (e.g., 1 and "spam"), names (e.g., x, +, and spam), and calls (like f(x, 1)).

**Important** Names (symbols) have no meaning by themselves. The *meaning* of a name always depends on the context, which is specified by an environment.

Consider a simple expression that merely consists of the name x:

```
expr_x <- quote(x)
```

<sup>&</sup>lt;sup>7</sup> Some call them R5, but we will not.

Let us define two environments that bind the name x to two different constants.

```
e1 <- as.environment(list(x=1))</pre>
e2 <- as.environment(list(x="spam"))</pre>
```

**Important** An expression is evaluated within a specific environment.

Let us call eval on the above.

```
eval(expr_x, envir=e1) # evaluate `x` within environment e1
[1] 1
eval(expr_x, envir=e2) # evaluate the same `x` within environment e2
[1] "spam"
```

The very same expression has two different meanings, depending on the context. This is quite like in the so-called real life: "I'm good" can mean "I don't need anything" but also "My virtues are plentiful". It all depends on who and when is asking, i.e., in which environment we evaluate the said sentence.

We call this the environment model of evaluation, a notion that R authors have borrowed from a Lisp-like language called Scheme<sup>8</sup> (see Section 3.2 of [1] and Section 6 of [67]).

## 16.2.1 Getting the current environment

By default, expressions are evaluated in the *current* environment, which can fetch by calling:

```
sys.frame(sys.nframe()) # get the current environment
<environment: R_GlobalEnv>
```

We are working on the R console. Hence, the current one is the global environment (user workspace). We can access it from anywhere by calling **globalenv** or referring to the `.GlobalEnv` object.

**Example 16.5** Calling any operation, for instance<sup>9</sup>:

```
x <- "spammity spam"
```

means evaluating it within the current environment:

```
eval(quote(x <- "spammity spam"), envir=sys.frame(sys.nframe()))</pre>
```

<sup>&</sup>lt;sup>8</sup> That is why everyone serious about R programming should add the Structure and Interpretation of Computer Programs [1] to their reading list. Also, R is not the only known marriage between statistics and Lisp-like languages; see also LISP-STAT [54].

<sup>9</sup> Let us, for now, take for granted that `<-` is accessible from the current context and denotes the assignment.

Here, we bound the name x to the string "spammity spam" in the current environment's frame:

```
sys.frame(sys.nframe())[["x"]] # yes, `x` is in the current environment now
[1] "spammity spam"
globalenv()[["x"]] # because the global environment is the current one here
[1] "spammity spam"
```

Therefore, when we now refer to x (from within the current environment):

```
x # eval(quote(x), envir=sys.frame(sys.nframe()))
[1] "spammity spam"
```

precisely the above named object is fetched.

**Exercise 16.6** save.image saves the current workspace, i.e., the global environment, by default, to the file named .Rdata. Test this function in combination with load.

**Note** Names starting with a dot are *hidden*. **ls**, a function to fetch all names registered within a given environment, does not list them by default.

```
.test <- "spam"
ls() # list all names in the current environment, i.e., the global one
[1] "e1" "e2" "expr_x" "mod" "x" "y"</pre>
```

Compare the above with:

On a side note, `.Random.seed` stores the current pseudorandom number generator's seed; compare Section 2.1.5.

#### 16.2.2 Enclosures, enclosures thereof, etc.

To show that there is much more to the environment model of evaluation than what we mentioned above, let us try to evaluate an expression featuring two names:

```
e2 <- as.environment(list(x="spam")) # once again (a reminder)
expr_comp <- quote(x < "eggs")
eval(expr_comp, envir=e2) # "spam" < "eggs"
Error in x < "eggs": could not find function "<"</pre>
```

The meaning of any constant (here, "spam") is context-independent. The environment provided specifies the name x but does not define `<`. Hence the error.

Nonetheless, we feel that we know the meaning of `<`. It is a relational operator, obvi-

ously, isn't it? To increase the confusion, let us highlight that our experience-grounded intuition is true in the following context:

```
e3 <- new.env()
e3[["x"]] <- "bacon"
eval(expr_comp, envir=e3) # "bacon" < "eggs"</pre>
[1] TRUE
```

So where does the name `<` come from? It is neither included in e2 nor e3:

```
e2[["<"]]
NULL
e3[["<"]]
NUI I
```

Is `<` hardcoded somewhere? Or is it also dependent on the context? Why is it visible when evaluating an expression within e3 but not in e2?

Studying help("[[") (see the Environments section), we discover that e3[["<"]] is equivalent to a call to get("<", envir=e3, inherits=FALSE). In help("get"), we read that if the inherits argument is set to TRUE (which is the default in get), then the enclosing frames of the given environment are searched as well.

Continuing the example from the previous subsection:

```
get("<", envir=e2) # inherits=TRUE</pre>
Error in get("<", envir = e2): object '<' not found
get("<", envir=e3) # inherits=TRUE</pre>
function (e1, e2) .Primitive("<")</pre>
```

And indeed, we see that `<` is reachable from e3 but not from e2. It means that e3 points to another environment where further information should be sought if the current container is left empty-handed.

**Important** The reference (pointer) to the *enclosing environment* is integral to each environment (alongside a frame of objects). It can be fetched and set using the parent.env function.

# Missing names are sought in enclosing environments

To understand the idea of enclosing environments better, let us create two new environments whose enclosures are explicitly set as follows:

```
(e4 <- new.env(parent=e3))</pre>
<environment: 0x557efa536b20>
```

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(continued from previous page)

```
(e5 <- new.env(parent=e4))
<environment: 0x557efa4af9e8>
```

To verify that everything is in order, let us inspect the following:

```
print(e3) # this is the address of e3
<environment: 0x557efac569f0>
parent.env(e4) # e3 is the enclosing environment of e4
<environment: 0x557efac569f0>
parent.env(e5) # e4 is the enclosing environment of e5
<environment: 0x557efa536b20>
```

Also, let us bind two different objects to the name y in e5 and e3.

```
e5[["y"]] <- "spam"
e3[["y"]] <- function() "a function `y` in e3"
```

The current state of matters is depicted in Figure 16.1.

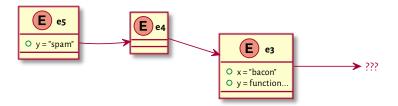


Figure 16.1. Example environments and their enclosures (original setting).

Let us evaluate the y name in the above environments:

```
expr_y <- quote(y)
eval(expr_y, envir=e3)
function() "a function `y` in e3"
eval(expr_y, envir=e5)
[1] "spam"</pre>
```

No surprises yet. However, evaluating it in e4, which does not define y, yields:

```
eval(expr_y, envir=e4)
function() "a function `y` in e3"
```

It returned y from e4's enclosure, e3.

Let us play about with the enclosures of e5 and e4 so that we obtain the setting depicted in Figure 16.2:

```
parent.env(e5) <- e3</pre>
parent.env(e4) <- e5
```

```
O v = "spam"
 > ???
 v = function
```

Figure 16.2. Example environments and their enclosures (after the change made).

Evaluating y again in the same e4 nourishes a very different result:

```
eval(expr_y, envir=e4)
[1] "spam"
```

Important Names referred to in an expression but missing in the current environment will be sought in their enclosure(s) *until* successful.

**Note** Here are the functions related to searching within and modifying environments that optionally allow for continuing explorations in the enclosures until successful:

- inherits=TRUE by default:
  - exists,
  - get,
- inherits=FALSE by default:
  - assign,
  - rm (remove).

# 16.2.4 Looking for functions

Interestingly, if a name is used instead of a function to be called, the object sought is always<sup>10</sup> of the mode function.

Consider an expression similar to the above, but this time including the name y playing a different role:

<sup>&</sup>lt;sup>10</sup> This is why we can write "c < -c(1, 2)" and then still be able to call c to create another vector.

```
expr_y2 <- quote(y()) # a call to something named `y`
eval(expr_y2, envir=e4)
[1] "a function `y` in e3"</pre>
```

In other words, what we used here was not:

```
get("y", envir=e4)
[1] "spam"
```

but:

```
get("y", envir=e4, mode="function")
function() "a function `y` in e3"
```

**Note** name(), "name"(), and `name`() are synonymous. However, the first expression is acceptable only if name is syntactically valid.

#### 16.2.5 Inspecting the search path

Going back to our expression involving a relational operator:

```
expr_comp
x < "eggs"</pre>
```

Why does the following work as expected?

```
eval(expr_comp, envir=e3) # "bacon" < "eggs"
[1] TRUE</pre>
```

Well, we have gathered all the bits to understand it now. Namely, `<` is a function that is looked up in the following way:

```
get("<", envir=e3, inherits=TRUE, mode="function")
function (e1, e2) .Primitive("<")</pre>
```

It is reachable from e3, which means that e3 also has an enclosing environment.

```
parent.env(e3)
<environment: R_GlobalEnv>
```

This is our global namespace, which was the current environment when e3 was created. Still, we did not define `<` there. It means that the global environment also has an enclosure.

We can explore the whole *search path* by starting at the global environment and following the enclosures recursively.

```
ecur <- globalenv() # starting point</pre>
repeat {
 cat(paste0(format(ecur), " (", attr(ecur, "name"), ")")) # pretty-print
 if (exists("<", envir=ecur, inherits=FALSE)) # look for `<`</pre>
 cat(strrep(" ", 25), "`<` found here!")</pre>
 cat("\n")
 ecur <- parent.env(ecur) # advance to its enclosure
}
<environment: R_GlobalEnv> ()
<environment: 0x557efae53ac0> (.marekstuff)
<environment: package:stats> (package:stats)
<environment: package:graphics> (package:graphics)
<environment: package:grDevices> (package:grDevices)
<environment: package:utils> (package:utils)
<environment: package:datasets> (package:datasets)
<environment: package:methods> (package:methods)
<environment: 0x557ef8ebd960> (Autoloads)
<environment: base> ()
 `<` found here!
<environment: R_EmptyEnv> ()
Error in parent.env(ecur): the empty environment has no parent
```

Underneath the global environment, there is a whole list of attached packages:

- 1. packages attached by the user (.marekstuff is used internally in the process of evaluating code in this book),
- 2. default packages (Section 7.3.1),
- 3. (\*\*) **Autoloads** (for the promises-to-load R packages; compare **help**("autoload"); it is a technicality we may safely ignore here),
- 4. the **base** package, which we can access directly by calling **baseenv**; it is where most of the *fundamental* functions from the previous chapters reside,
- 5. the *empty* environment (**emptyenv**), which is the only one followed by nil (the loop would turn out endless otherwise).

It comes at no surprise that the `<` operator has been found in the base package.

**Note** On a side note, the reason why this operation failed:

```
e2 <- as.environment(list(x="spam")) # to recall
eval(expr_comp, envir=e2)
Error in x < "eggs": could not find function "<"</pre>
```

is because as.environment sets the enclosing environment to:

```
parent.env(e2)
<environment: R_EmptyEnv>
```

See also list2env which gives greater control over this (cf. its parent argument).

#### 16.2.6 Attaching to and detaching from the search path

In Section 7.3.1, we mentioned that we can access the objects exported by a package without attaching them to the search path by using the pkg::object syntax, which loads the package if necessary. For instance:

```
tools::toTitleCase("`tools` not attached to the search path")
[1] "`tools` not Attached to the Search Path"
```

#### However:

```
toTitleCase("nope")
Error in toTitleCase("nope"): could not find function "toTitleCase"
```

It did not work because **toTitleCase** is not reachable from the current environment.

Let us inspect the current search path:

```
search()
[1] ".GlobalEnv" ".marekstuff" "package:stats"
[4] "package:graphics" "package:grDevices" "package:utils"
[7] "package:datasets" "package:methods" "Autoloads"
[10] "package:base"
```

Some might find writing "pkg::" inconvenient. Thus, we can call library to attach the package to the search path immediately below the global environment.

```
library("tools")
```

The search path becomes (see Figure 16.3 for an illustration):

Therefore, what follows, now works as expected:

```
toTitleCase("Nobody expects the Spanish Inquisition")
[1] "Nobody Expects the Spanish Inquisition"
```

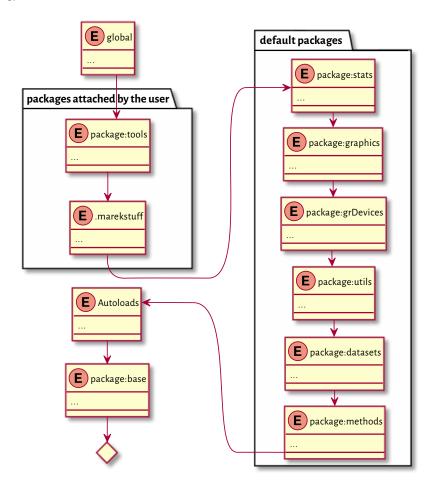


Figure 16.3. The search path after attaching the **tools** package.

We can use **detach**<sup>11</sup> to remove an item from the search path.

<sup>&</sup>lt;sup>11</sup> Which does not unload the package from memory, though; see unload (possibly combined with library.dynam.unload).

**Note** We can also plug arbitrary environments<sup>12</sup> and named lists into the search path. Recalling that data frames are built on the latter (Section 12.1.6), some users rely on this technique save a few keystrokes.

```
attach(iris)
head(search(), 3)
[1] ".GlobalEnv" "iris" ".marekstuff"
```

The iris list was converted to an environment, and the necessary enclosures were set accordingly:

```
str(parent.env(globalenv()))
<environment: 0x557efafd2db8>
- attr(*, "name")= chr "iris"
str(parent.env(parent.env(globalenv())))
<environment: 0x557efae53ac0>
- attr(*, "name")= chr ".marekstuff"
```

We can now write:

```
head(Petal.Width/Sepal.Width) # iris[["Petal.Width"]]/iris[["Sepal.Width"]]
[1] 0.057143 0.066667 0.062500 0.064516 0.055556 0.102564
```

Overall, attaching data frames is discouraged, especially outside the interactive mode. Let us not be too lazy.

```
detach(iris) # such a relief
```

# 16.2.7 Masking (shadowing) objects from down under

An assignment via `<-` creates a binding in the *current* environment. Therefore, even if the name to bind exists somewhere on the search path, it will not be modified. Instead, a new name will be created.

```
eval(quote("spam" < "eggs"))
[1] FALSE</pre>
```

Here, we rely on `<` from the base environment. Withal, we can create an object of the same name in the current (global) context:

<sup>&</sup>lt;sup>12</sup> Or we should rather say, environment frames. When an environment is attached to the search path, it is duplicated so that the changes made to the original environment are not reflected in the copy. Then, its previous enclosure is discarded. After all, we want a series of recursive calls to parent.env to form the whole search path.

```
`<` <- function(e1, e2)
{
 warning("This is not the base `<`, mate.")
 NA
}</pre>
```

Now we have two different functions of the same name. When we evaluate an expression within the current environment or any of its descendants, the new name *shadows* the base one:

```
"spam" < "eggs" # evaluate in the global environment
Warning in "spam" < "eggs": This is not the base `<`, mate.
[1] NA
eval(quote("spam" < "eggs"), envir=e5) # its enclosure's enclosure is global
Warning in "spam" < "eggs": This is not the base `<`, mate.
[1] NA</pre>
```

But we can still call the original function directly:

```
base::`<`("spam", "eggs")
[1] FALSE
```

It is also reachable from within the current environment's ancestors:

```
eval(quote("spam" < "eggs"), envir=parent.env(globalenv()))
[1] FALSE</pre>
```

Before proceeding any further, let us clean up after ourselves. Otherwise, we will be asking for trouble.

```
rm("<") # removes `<` from the global environment
```

An attached package may introduce some object names that are also available elsewhere. For instance:

```
library("stringx")
Attaching package: 'stringx'
The following objects are masked from 'package:base': casefold, chartr,
endsWith, gregexec, gregexpr, grep, grepl, gsub, ISOdate, ISOdatetime,
nchar, nzchar, paste, paste0, regexec, regexpr, sprintf, startsWith,
strftime, strptime, strrep, strsplit, strtrim, strwrap, sub, substr,
substr<-, substring, substring<-, Sys.time, tolower, toupper, trimws,
xtfrm, xtfrm.default</pre>
```

Therefore, in the current context, we have what follows:

```
toupper("Groß") # stringx::toupper
[1] "GROSS"
base::toupper("Groß")
[1] "GROß"
```

Sometimes<sup>13</sup>, we can use **assign**(..., inherits=TRUE) or its synonym, `<<-`, to modify the *existing* binding. A new binding is only created if necessary.

**Note** Let us attach the iris data frame (named list) to the search path again:

```
attach(iris)
Sepal.Length[1] <- 0</pre>
```

We did not modify the original iris nor its converted-to-an-environment copy that we can find in the search path. Instead, a new vector named Sepal. Length was created in the current environment:

```
exists("Sepal.Length", envir=globalenv(), inherits=FALSE) # it is in global ## [1] TRUE Sepal.Length[1] # global ## [1] 0
```

We can verify the above statement as follows:

```
rm("Sepal.Length") # removes the one in the global environment
Sepal.Length[1] # `iris` from the search path
[1] 5.1
iris[["Sepal.Length"]][1] # the original `iris`
[1] 5.1
```

However, we can write:

```
Sepal.Length[1] <<- 0 # uses assign(..., inherits=TRUE)</pre>
```

We changed the state of the environment on the search path.

```
exists("Sepal.Length", envir=globalenv(), inherits=FALSE) # not in global
[1] FALSE
Sepal.Length[1] # `iris` from the search path
[1] 0
```

Yet, the original iris object is left untouched. There is no mechanism in place that would *synchronise* the original data frame and its independent copy on the search path.

 $<sup>^{13}</sup>$  We normally cannot modify package namespaces. As we will mention in Section 16.3.5, they are automatically locked.

```
iris[["Sepal.Length"]][1] # the original `iris`
[1] 5.1
```

It is best to avoid attach to avoid confusion.

#### Closures 16.3

So far, we have only covered the rules of evaluating standalone R expressions. In this section, we look at what happens *inside* the invoked functions.

#### Local environment 16.3.1

When we call a function, a new temporary environment is created. It is where all argument values<sup>14</sup> and local variables are emplaced. This environment is the current one while the function is being evaluated. After the call, it ceases to exist, and we return to the previous environment from the call stack.

Consider the following function:

```
test <- function(x)
{
 print(ls()) # list object names in the current environment
 y <- x^2 # creates a new variable
 print(sys.frame(sys.nframe())) # get the ID of the current environment
 str(as.list(sys.frame(sys.nframe()))) # display its contents
}
```

First call:

```
test(2)
[1] "x"
<environment: 0x557efb2e7fb8>
List of 2
$ y: num 4
$ x: num 2
```

Second call:

```
test(3)
[1] "x"
<environment: 0x557efbb35898>
 (continues on next page)
```

<sup>&</sup>lt;sup>14</sup> Function arguments are initially unevaluated; see Chapter 17.

(continued from previous page)

```
List of 2
$ y: num 9
$ x: num 3
```

Each time, the current environment is different. This is why we do not see the y variable at the start of the second call. It is a brilliantly simple implementation of the storage for local variables.

#### 16.3.2 Lexical scope and function closures

We were able to access the **print** function (amongst others) in the above example. This should make us wonder what the enclosing environment of that local environment is.

```
print_enclosure <- function()
 print(parent.env(sys.frame(sys.nframe())))

print_enclosure()
<environment: R_GlobalEnv>
```

It is the global environment. Let us invoke the same function from another one:

```
call_print_enclosure <- function()
 print_enclosure()

call_print_enclosure()
<environment: R_GlobalEnv>
```

It is the global environment again. If R used the so-called *dynamic scoping*, we would see the local environment of the function that invoked the one above. If this was true, we would have access to the caller's local variables from within the callee. But this is not the case.

**Important** Objects of the type closure, i.e., user-defined<sup>15</sup> functions, consist of three components:

- a list of formal arguments (compare **formals** in Section 15.4.1);
- an expression (see **body** in Section 15.4.1);
- a reference to the *associated environment* where the function might store data for further use (see **environment**).

By default, the associated environment is set to the current environment where the function was created.

<sup>15</sup> There are two other types of functions: a special is an internal function that does not necessarily evaluate its arguments (e.g., switch, if, or quote; compare also Chapter 17), whereas a builtin always evaluates its actual parameters, e.g., sum.

A local environment created during a function's call has this associated environment as its closure.

Due to this, we say that R has lexical (static) scope.

Thence, in the above example, we have:

```
environment(print_enclosure) # print the associated environment
<environment: R_GlobalEnv>
```

**Example 16.7** Consider the following function that prints out x defined outside of its scope:

```
test <- function() print(x)</pre>
```

Now:

```
x <- "x in global"
test()
[1] "x in global"</pre>
```

It printed out x from the user workspace as it is precisely the environment associated with the function. However, setting the associated environment to another one that also happens to define x will give a different result:

```
environment(test) <- e3 # defined some time ago
test()
[1] "bacon"</pre>
```

### **Example 16.8** Consider the following example:

```
test <- function()
{
 cat(sprintf("test: current env: %s\n", format(sys.frame(sys.nframe()))))
 subtest <- function()
 {
 e <- sys.frame(sys.nframe())
 cat(sprintf("subtest: enclosing env: %s\n", format(parent.env(e))))
 cat(sprintf("x = %s\n", x))
 }

 x <- "spam"
 subtest()
 environment(subtest) <- globalenv()
 subtest()
}</pre>
```

(continued from previous page)

```
x <- "bacon"
test()
test: current env: <environment: 0x557efaf317f8>
subtest: enclosing env: <environment: 0x557efaf317f8>
x = spam
subtest: enclosing env: <environment: R_GlobalEnv>
x = bacon
```

Here is what happened.

- 1. A call to **test** creates a local function **subtest**, whose associated environment is set to the local frame of the current call. It is precisely the current environment where **subtest** was created (because R has lexical scope).
- 2. The above explains why **subtest** can access the local variable x inside its maker.
- 3. Then we change the environment associated with **subtest** to the global one.
- 4. In the next call to **subtest**, unsurprisingly, we gain access to x in the user workspace.

**Note** In lexical (static) scoping, which variables a function refers to can be deduced by reading the function's body only and not how it is called in other contexts. This is the theory. Nevertheless, the fact that we can freely modify the associated environment anywhere can complicate the program analysis greatly.

If we find the rules of lexical scoping complicated, we should refrain from referring to objects outside of the current scope ("global" or "non-local" variables") except for the functions defined as top-level ones or imported from external packages. It is what we have been doing most of the time anyway.

# 16.3.3 Application: Function factories

As closures are functions with associated environments, and the role of environments is to store information, we can consider closures = functions + data. We have already seen that in Section 9.4.3, where we mentioned **approxfun**. To recall:

```
x <- seq(0, 1, length.out=11)
f1 <- approxfun(x, x^2)
print(f1)
function (v)
.approxfun(x, y, v, method, yleft, yright, f, na.rm)
<environment: 0x557efb3b24b8>
```

The variables x, y, etc., that **f1**'s source code refers to, are stored in its associated environment:

```
ls(envir=environment(f1))
[1] "f"
 "method" "na.rm" "x"
 "yleft" "yright"
```

Important Routines that return functions whose non-local variables are memorised in their associated environments are referred to as function factories.

**Example 16.9** *Consider the following function factory:* 

```
gen_power <- function(p)</pre>
 function(x) x^p \# p references a non-local variable
```

A call to **gen\_power** creates a local environment that defines one variable,  $\rho$ , where the argument's value is stored. Then, we create a function whose associated environment (remember that R uses lexical scoping) is that local one. It is where the reference to the non-local p in its body will be resolved. This new function is returned by **gen\_power** to the caller. Normally, the local environment would be destroyed, but it is still used after the call. Thus, it will not be garbage-collected.

Example calls:

```
(square <- gen_power(2))</pre>
function(x) x^p
<environment: 0x557efa995f20>
(cube <- gen_power(3))</pre>
function(x) x^p
<environment: 0x557efa9f64b8>
square(2)
[1] 4
cube(2)
[1] 8
```

The underlying environment can, of course, be modified:

```
assign("p", 7, envir=environment(cube))
cube(2) # so much for the cube
[1] 128
```

**Example 16.10** *Negate* is another example of a function factory. The function it returns stores **f** passed as an argument.

```
notall <- Negate(all)</pre>
notall(c(TRUE, TRUE, FALSE))
[1] TRUE
```

Study its source code:

```
print(Negate)
function (f)
{
f <- match.fun(f)
function(...) !f(...)
}
<environment: namespace:base>
```

#### **Example 16.11** *In* [37], the following example is given:

```
account <- function(total)
 list(
 balance = function() total,
 deposit = function(amount) total <<- total+amount,
 withdraw = function(amount) total <<- total-amount
)

Robert <- account(1000)
Ross <- account(500)
Robert$deposit(100)
Ross$withdraw(150)
Robert$balance()
[1] 1100
Ross$balance()
[1] 350</pre>
```

We can now fully understand why the above code does what it does. The return list consists of three functions whose enclosing environment is the same. account somewhat resembles the definition of a class with three methods and one data field. No wonder why reference classes (Section 16.1.5) were introduced at some point: they are based on the same concept.

**Exercise 16.12** Write a function factory named **gen\_counter** which implements a simple counter that is increased by one on each call thereto.

```
gen_counter <- function() ...to.do...
c1 <- gen_counter()
c2 <- gen_counter()
c(c1(), c1(), c2(), c1(), c2())
[1] 1 2 1 3 2</pre>
```

Moreover, compose a function that resets a given counter to zero.

```
reset_counter <- function(counter_fun) ...to.do...
reset_counter(c1)
c1()
[1] 1</pre>
```

#### 16.3.4 Accessing the calling environment

We know that the environment associated with a function is not necessarily the same as the environment from which the function was called, sometimes quite confusingly referred to as the *parent frame*.

R maintains a whole *frame stack*. The global environment is assigned the number 0. Each call to a function increases the stack by one frame, whereas returning from a call decreases the counter. To get the current frame number, we call **sys.nframe**. This is why **sys.frame**(sys.nframe()) returns the current environment.

We can fetch the calling environment by referring to parent.frame() or sys.frame(sys.parent()), amongst others<sup>16</sup>. Thanks to parent.frame, we may evaluate arbitrary expressions in (on behalf of) the calling environment. Normally, we should never be doing that. However, a few functions rely on this feature, hence our avid interest in this possibility.

#### 16.3.5 Package namespaces (\*)

An R package pkg defines two environments:

- namespace:pkg is where all objects are defined (functions, vectors, etc.); it is the
  enclosing environment of all closures in the package;
- package:pkg contains selected<sup>17</sup> objects from namespace:pkg that can be accessed by the user; it can be attached to the search path.

As an illustration, we will use the example package discussed in Section 7.3.1.

```
library("rpackagedemo") # https://github.com/gagolews/rpackagedemo/
Loading required package: tools
```

Here is its DESCRIPTION file:

Package: rpackagedemo

Type: Package

Title: Just a Demo R Package

Version: 1.0.2 Date: 1970-01-01

Author: Anonymous Llama

Maintainer: Unnamed Kangaroo <roo@inthebush.au>

Description: Provides a function named bamboo(), just give it a shot.

License: GPL (>= 2)
Imports: stringx
Depends: tools

<sup>&</sup>lt;sup>16</sup> In **help**("sys.parent"), we read that the parent frame number, as returned by **sys.parent**(), is not necessarily equal to **sys.nframe**()-1. It is certainly true if we are at the top (global) level.

<sup>&</sup>lt;sup>17</sup> Exported using the export or exportPattern directive in the package's NAMESPACE file; see Section 1 of [63].

The Import and Depends fields specify which packages (apart from **base**) ours depends on. As we can see above, all items in the latter list are attached to the search path on a call to **library**.

The NAMESPACE file specifies the names imported from other packages and those that are expected to be visible to the user:

```
importFrom(stringx, sprintf)
importFrom(tools, toTitleCase)
S3method(print, koala)
S3method(print, kangaroo, .a_hidden_method_to_print_a_roo)
export(bamboo)
```

Thus, our package exports one object, a function named **bamboo** (we will discuss the S3 methods in the next section). It is included in the package:rpackagedemo environment attached to the search path:

```
ls(envir=as.environment("package:rpackagedemo")) # ls("package:rpackagedemo")
[1] "bamboo"
```

Let us give it a shot:

```
bamboo("spanish inquisition") # rpackagedemo::bamboo
G'day, Spanish Inquisition!
```

We did not expect this at all, nor that its source code looks like:

```
print(bamboo)
function (x = "world")
cat(prepare_message(toTitleCase(x)))
<environment: namespace:rpackagedemo>
```

We see a call to **toTitleCase** (most likely from **tools**, and this is indeed the case). Also, **prepare\_message** is invoked but it is not listed in the package's imports (see the NAMESPACE file). We definitely cannot access it directly:

```
prepare_message
Error in eval(expr, envir, enclos): object 'prepare_message' not found
```

It is the package's *internal* function, which is included in the namespace:rpackagedemo environment.

```
(e <- environment(rpackagedemo::bamboo)) # or getNamespace("rpackagedemo")
<environment: namespace:rpackagedemo>
ls(envir=e)
[1] "bamboo" "prepare_message" "print.koala"
```

We can fetch it via the `:::` operator:

```
print(rpackagedemo:::prepare_message)
function (x)
sprintf("G'day, %s!\n", x)
<environment: namespace:rpackagedemo>
```

All functions defined in a package have the corresponding namespace as their associated environment. As a consequence, **bamboo** can refer to **prepare\_message** directly.

It will be educative to inspect the enclosure of namespace: rpackagedemo:

```
(e <- parent.env(e))
<environment: 0x557efaf66b38>
attr(,"name")
[1] "imports:rpackagedemo"
ls(envir=e)
[1] "sprintf" "toTitleCase"
```

It is the environment carrying the bindings to all the imported objects. This is why our package can also refer to **stringx::sprintf** and **tools::toTitleCase**. Its enclosure is the *namespace* of the **base** package (not to be confused with package:base):

```
(e <- parent.env(e))
<environment: namespace:base>
```

The next enclosure is, interestingly, the global environment:

```
(e <- parent.env(e))
<environment: R_GlobalEnv>
```

Then, of course, the whole search path follows; see Figure 16.4 for an illustration.

**Note** (\*\*) All environments related to packages are locked, which means that we cannot change any bindings inside their frames; compare **help**("lockEnvironment"). In the extremely rare event of our needing to *patch* an existing function within an already loaded package, we can call **unlockBinding** followed by **assign** to change its definition.

```
new_message <- function (x) sprintf("Nobody expects %s!\n", x)
e <- getNamespace("rpackagedemo")
environment(new_message) <- e # set enclosing environment (very important!)
unlockBinding("prepare_message", e)
assign("prepare_message", new_message, e)
rm("new_message")
bamboo("the spanish inquisition")
Nobody expects The Spanish Inquisition!</pre>
```

R is indeed a quite hackable language (except in the cases where it is not).

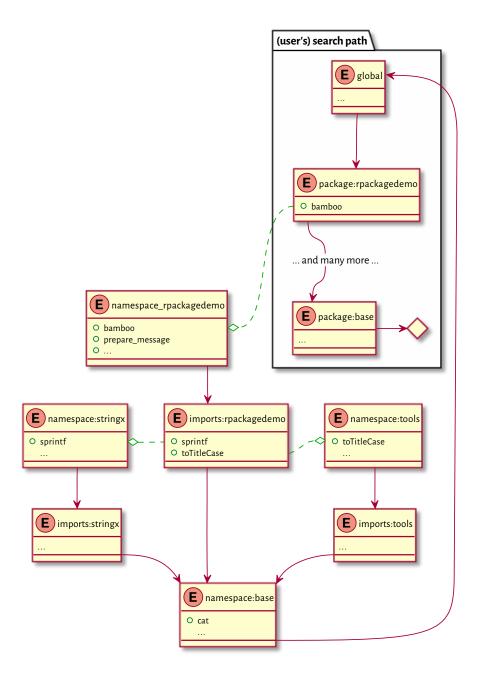


Figure 16.4. A search path for an example package. Dashed lines represent environments associated with closures, whereas solid lines denote enclosing environments. References to objects within each package are resolved inside their respective namespaces.

**Exercise 16.13** (\*\*) A function or a package might register certain functions (hooks) to be called on various events, e.g., attaching a package to the search patch; see **help**("setHook") and **help**(".onAttach").

- 1. Inspect the source code of **plot.new** and notice a reference to a hook named "before.plot. new". Try setting such a hook yourself (e.g., one that changes some of the graphics parameters discussed in Section 13.2) and see what happens on each call to a plotting function.
- 2. Define the .onLoad, .onAttach, .onUnload, and .onDetach functions in your own R package and take note of when they are invoked.

**Exercise 16.14** (\*\*) For the purpose of this book, we have registered a custom "before.plot. new" hook that sets our favourite graphics parameters that we listed in Section 13.2.3. Moreover, to obtain a white grid on a grey background, e.g., in Figure 13.13, we modified **plot.window** slightly. Apply similar hacks to the **graphics** package so that its outputs suit your taste better.

### 16.3.6 S3 method lookup by UseMethod (\*)

Let us go back to the **rpackagedemo** example. Inspecting the NAMESPACE file, we see that the package defines two **print** methods for objects of the classes koala and kangaroo.

The package is still attached to the search path. Therefore, we can access these methods via a call to the corresponding generic:

```
print(structure("Tiny Teddy", class="koala"))
This is a cute koala, Tiny Teddy
print(structure("Moike", class="kangaroo"))
This is a very naughty kangaroo, Moike
```

The package does not make the definitions of these S3 methods available to the user, at least not directly. It is not the first time when we have experienced such an obscuration. In the first case, the method is simply hidden in the package namespace because it was not marked for exportation in the NAMESPACE file. However, it is still available under the expected name:

```
rpackagedemo:::print.koala
function (x, ...)
cat(sprintf("This is a cute koala, %s\n", x))
<environment: namespace:rpackagedemo>
```

In the second case, the method appears under a very different identifier:

```
rpackagedemo:::.a_hidden_method_to_print_a_roo
function (x, ...)
cat(sprintf("This is a very naughty kangaroo, %s\n", x))
<environment: namespace:rpackagedemo>
```

Since the base UseMethod is still able to find them, we suspect that there must be a

global register of all S3 methods. And this is indeed the case. We can use **getS3method** to get access to what is available via **UseMethod**:

```
getS3method("print", "kangaroo")
function (x, ...)
cat(sprintf("This is a very naughty kangaroo, %s\n", x))
<environment: namespace:rpackagedemo>
```

**Important** Overall, the search for methods is performed in two places:

1. in the environment where the generic is called (the current environment); this is why defining **print.kangaroo** in the current scope will use this method instead of the one from the package:

```
print.kangaroo <- function(x, ...) cat("Nobody expects", x, "\n")
print(structure("the Spanish Inquisition", class="kangaroo"))
Nobody expects the Spanish Inquisition</pre>
```

2. in the internal S3 methods table (registration database).

See help("UseMethod") for more details. Also, recall that in Section 10.2.3, we said that UseMethod is not the only way to perform method dispatching. There are also internal generics and group generic functions; see help("InternalMethods") and help("groupGeneric").

**Exercise 16.15** (\*) Study the source code of **getS3method**. Note the reference to the base::`. \_\_\_S3MethodsTable\_\_.` object which is for R's internal use (we ought not to tinker with it directly). Moreover, study the **registerS3method** function with which we can define new S3 methods not necessarily following the **generic.classname** convention.

#### 16.4 Exercises

**Exercise 16.16** Asking too many questions is not very charismatic, but challenge yourself by trying to find the answer to the following.

- What is the role of a frame in an environment?
- What is the role of an enclosing environment? How to read it or set it?
- What is the difference between a named list and an environment?
- What functions and operators work on named lists but cannot be applied on environments?
- What do we mean by saying that environments are not passed by value to R functions?
- What do we mean by saying that objects are sometimes copied on demand?

- What happens if a name listed in an expression to be evaluated is not found in the current environment?
- How and what kind of objects can we attach to the search path?
- What happens if we have two identical object names on the search path?
- What do we mean by saying that package namespaces are locked when loaded?
- What is the current environment when we evaluate an expression "on the console"?
- What is the difference between `<-` and `<<-`?
- Do packages have their own search paths?
- What is a function closure?
- What is the difference between the dynamic and the lexical scope?
- When evaluating a function, how is the enclosure of the current (local) environment determined? Is it the same as the calling environment? How to get it/them programmatically?
- How and why function factories work?
- (\*) What is the difference between the package: pkg and namespace: pkg environments?
- How do we fetch the definition of an S3 method that does not seem to be available directly via the standard accessor **generic.classname**?
- (\*) base::print.data.frame calls base::format.data.frame (directly). Will the introduction of print.data.frame in the current environment affect how data frames are printed?
- (\*) On the other hand, **base::format.data.frame** calls the generic **base::format** on all the input data frame's columns. Will the overloading of the particular methods affect how data frames are printed?

## Exercise 16.17 Calling:

```
pkg <- available.packages()
pkg[, "Package"] # a list of the names of available packages
pkg[, "Depends"] # dependencies</pre>
```

gives the list of available packages and their dependencies. Convert the dependency lists to a list of character vectors (preferably using regular expressions; see Section 6.2.4).

Then, generate a list of reverse dependencies: what packages depend on each given package.

Use an object of the type environment (a hash table) to map the package names to numeric IDs (indexes). It will significantly speed up the whole process (compare it to a named list-based implementation).

Exercise 16.18 According to [67], compare also Section 9.3.6, a call to:

```
add(x, f(x)) \ll v
```

translates to:

```
`*tmp*` <- get(x, envir=parent.env(), inherits=TRUE)</pre>
x <<- `add<-`(`*tmp*`, f(x), v) # note: not f(`*tmp*`)</pre>
rm(`*tmp*`)
```

Given:

```
`add<-` <- function(x, where=TRUE, value)
 x[where] <- x[where] + value
 x # the modified object that will replace the original one
}
y < -1:5
f <- function() { y <- -(1:5); add(y, y==-3) <<- 1000; y }</pre>
```

explain why we get the following results:

```
f()
[1] -1 -2 -3 -4 -5
print(y)
[1] 1 2 1003 4 5
```

# Lazy evaluation (\*\*)

The ability to create, store, and manipulate unevaluated expressions so that they can be computed later is not particularly special. Many languages enjoy such *metaprogramming* (computing *on* the language, reflection) capabilities, e.g., Lisp, Scheme, Wolfram, Julia, amongst many others.

However, R inherited from its predecessor, the S language, a variation of lazy¹ (nonstrict, noneager, delayed) evaluation of function arguments. They are only computed when their *values* are first needed. As we can take the expressions used to generate them (via **substitute**; see Section 15.4.2), we shall see that we can ignore their meaning in the original (caller's) context and compute them in a very different one.

# 17.1 Evaluation of function arguments

We know that calls such as `if`(test, ifyes, ifno), `||`(mustbe, maybe), or `&&`(mustbe, maybe) do not have to evaluate all their arguments.

```
{cat(" first "); FALSE} && {cat(" second "); FALSE}
first
[1] FALSE
{cat(" first "); TRUE } && {cat(" Spanish Inquisition "); FALSE}
first Spanish Inquisition
[1] FALSE
```

We can compose such functions ourselves. For instance:

```
test <- function(a, b, c) a + c # b is unused
test({cat("spam\n"); 1}, {cat("eggs\n"); 10}, {cat("salt\n"); 100})
spam
salt
[1] 101</pre>
```

The second argument was not referred to in the function's body. Therefore, it was not evaluated (no printing of *eggs* occurred).

<sup>&</sup>lt;sup>1</sup> Call-by-need but without the memoisation of results generated by expressions which is available, e.g., in Haskell. In other words, in an expression like c(f(x), f(x)), the call f(x) will still be performed twice.

# **Example 17.1** Study the following very carefully.

```
test <- function(a, b, c)
{
 cat("Arguments passed to `test` (expressions): \n")
 cat("a = ", deparse(substitute(a)), "\n")
 cat("b = ", deparse(substitute(b)), "\n")
 cat("c = ", deparse(substitute(c)), "\n")
 subtest <- function(x, y, z)</pre>
 ſ
 cat("Arguments passed to `subtest` (expressions): \n")
 cat("x = ", deparse(substitute(x)), "\n")
 cat("y = ", deparse(substitute(y)), "\n")
 cat("z = ", deparse(substitute(z)), "\n")
 cat("Using x and z... ")
 retval <- x + z # does not refer to `y`
 cat("Cheers!\n")
 retval
 }
 cat("Using c... ")
 c # force evaluation; we do not even have to be particularly creative
 subtest(a, \sim!\sim b*2 := headache \rightarrow ha@x$y, c*10) # no evaluation yet!
}
environment(test) <- new.env() # to spice things up</pre>
test(
 {testx <- "goulash"; cat("spam\n"); 1},
 {testy <- "kabanos"; cat("eggs\n"); MeAn(egGs+whatever&!!weird[stuff])},
 {testx <- "kransky"; cat("salt\n"); 100}</pre>
)
Arguments passed to `test` (expressions):
 testx <- "goulash" cat("spam\n") 1 }
testy <- "kabanos" cat("eggs\n") MeAn(egGs + whatever ...
a = {
b = {
 testx <- "kransky" cat("salt\n") 100 }
c = {
Using c... salt
Arguments passed to `subtest` (expressions):
x = a
y = := (~!~b * 2, ha@x$y <<- headache)
z = c * 10
Using x and z... spam
Cheers!
[1] 1001
```

```
print(testx)
[1] "goulash"
print(testy)
Error in eval(expr, envir, enclos): object 'testy' not found
```

On a side note, the `~` (formula) operator will be discussed in Section 17.6. Furthermore, the `:=` operator was used in an ancient version of R for assignments. The parser still recognises it, yet now it has no associated meaning.

## **Important** We note what follows.

• Either the evaluation of an argument does not happen, or is triggered only once (in which case the result is cached).

This is why, in our example, *salt* was printed once.

• Evaluation is *delayed* until the very first request for the underlying value. We call it *lazy evaluation*.

It can be delayed forever; eggs is never printed and testy is undefined.

- Evaluation takes place in the calling environment (parent frame). testx is equal to *goulash* after all.
- Merely passing arguments further to another function usually does not trigger the evaluation.

We wrote *usually* because functions of the type builtin (e.g., c, list, sum, `+`, `&`, and `:`) always evaluate the arguments. There is no lazy evaluation in the case of the arguments passed to group generics; see help("groupGeneric") and Section 10.2.6. Furthermore, replacement functions' values arguments (Section 9.3.6) are computed eagerly.

• Fetching the expression passed as an argument using **substitute** (Section 15.4.2) or checking if an argument was provided with **missing** (Section 15.4.3) does not trigger the evaluation.

We see *spam* printed much later.

**Exercise 17.2** Study the source code of **system.time** and notice the use of delayed evaluation to measure the duration of the execution of a given expression. Note that **on.exit** (Section 17.4) reacts to possible exceptions.

**Example 17.3** It turns out that the role of **substitute** is broader than just getting the expression passed as an argument. We can actually replace each occurrence of every name from a given dictionary (a named list or an environment). For instance:

```
test <- function(x)
ſ
 subtest <- function(y)</pre>
 {
 ex <- substitute(x, env=parent.frame()) # substitute(x) is just `x`</pre>
 ev <- substitute(v)</pre>
 cat("ex =", deparse(ex), "\n")
 cat("ey =", deparse(ey), "\n")
 # not: eval(substitute(ey, list(x=ex)))
 eval(as.call(list(substitute, ey, list(x=ex))))
 }
 subtest(spam(!xx))
7
test(eels@hovercraft)
ex = eels@hovercraft
ey = spam(!xx)
spam(!eels@hovercrafteels@hovercraft)
```

We fetched the expression passed as the x argument to the calling function. Then, we replaced every occurrence of x in the expression ey. On a side note, as **substitute** does not evaluate its first argument, if we called **substitute(ey, ...)** in the last expression of **subtest**, we would treat ey as a quoted name.

### **Exercise 17.4** Study the source code of replicate:

```
print(replicate)
function (n, expr, simplify = "array")
sapply(integer(n), eval.parent(substitute(function(...) expr)),
##
 simplify = simplify)
<environment: namespace:base>
```

It creates a function that evaluates expr inside its local environment, which is new every time. Note that **eval.parent**(expr) is a shorthand for **eval**(expr, **parent.frame**()).

Note (\*) Internally, lazy evaluation of arguments is implemented using the so-called promises, compare [67], which consist of:

- an expression (which we can access by calling **substitute**);
- an environment where the expression is to be evaluated (once this happens, it is set to NULL);
- a cached value (computed on demand, once).

This interface is not really visible from within R, but see help("delayedAssign").

**Exercise 17.5** Inspect the definition of match.fun. Why is it called by, e.g., apply, Map, or outer? Note that it uses eval.parent(substitute(substitute(FUN))) to fetch the expression representing the argument passed by the calling function (but it is probably very rarely needed there). Compare:

**Exercise 17.6** (\*) *Implement your version of the* **bquote** *function*.

# 17.2 Evaluation of default arguments

As we know from Section 9.4.4, default arguments are special expressions specified in a function's parameter list.

**Important** When a function's body requires the value of an argument that the caller did not provide, the default expression will be evaluated in the current (local) environment of the function.

It is thus different from the case of normally passed arguments, which are interpreted in the context of the calling environment.

**Example 17.7** Study the following very carefully.

```
x <- "banana"

test <- function(y={cat("spam\n"); x})
{
 cat(deparse(substitute(y)), "\n")
 cat("bacon\n")
 x <- "rotten potatoes"
 (continues on next page)</pre>
```

```
cat(y, y, "\n")
}
test({cat("spam\n"); x})
{ cat("spam\n") x }
bacon
spam
banana banana
```

As usual, the evaluation is triggered only once, where it was explicitly requested, and only when needed. y was bound to the value of x from the calling environment (banana in the global one).

```
test()
{ cat("spam\n") x }
bacon
spam
rotten potatoes rotten potatoes
```

The expression for the default y was evaluated in the local environment. It happened after the creation of the local x.

**Example 17.8** *Consider the following example from [37]:* 

```
sumsq <- function(y, about=mean(y), na.rm=FALSE)</pre>
ſ
 if (na.rm)
 y \leftarrow y[!is.na(y)]
 sum((y - about)^2)
}
y <- c(1, NA_real_, NA_real_, 2)
sumsq(y, na.rm=TRUE)
[1] 0.5
```

In the case where we rely on the default argument, the computation of the mean may take into account the request for missing value removal. Still, the following will not work as intended:

```
sumsq(y, mean(y), na.rm=TRUE) # we should rather pass mean(y, na.rm=TRUE)
[1] NA
```

However, as the idea of lazy evaluation of arguments is alien to most programmers (especially those coming from different languages), it might be better to rewrite the above using a call to missing (Section 15.4.3):

```
sumsq <- function(y, about, na.rm=FALSE)</pre>
{
 (continues on next page)
```

or hetter even:

```
sumsq <- function(y, about=NULL, na.rm=FALSE)
{
 if (na.rm)
 y <- y[!is.na(y)]
 if (is.null(about))
 about <- mean
 sum((y - about(y))^2)
}
sumsq(y, na.rm=TRUE)
[1] 0.5</pre>
```

Exercise 17.9 The default arguments to do.call, list2env, and new.env are set to parent. frame. What does that mean?

**Exercise 17.10** Study the source code of the **local** function:

```
print(local)
function (expr, envir = new.env())
eval.parent(substitute(eval(quote(expr), envir)))
<environment: namespace:base>
```

# 17.3 Ellipsis revisited

If our function has the dot-dot parameter, `...`, whatever we pass through it is packed into a pairlist of promise expressions. Thus, we can relish the benefits of lazy evaluation. In particular, we can redirect all `...`-fed arguments to another call as-is.

```
test <- function(...)
{</pre>
```

(continues on next page)

```
subtest <- function(x, ...)</pre>
 {
 cat("x = "); str(x)
 cat("... = "); str(list(...))
 }
 subtest(...)
}
test({cat("eggs! "); 1}, {cat("spam! "); 2}, z={cat("rice! "); 3})
x = eggs! num 1
... = spam! rice! List of 2
$: num 2
$ z: num 3
```

Exercise 17.11 In the documentation of lapply, we read that this function is called like lap**ply**(X, FUN, ...), where `...` are optional arguments to **FUN**. Verify that whatever is passed via the ellipsis is evaluated only once and not on each application of **FUN** on the elements of X.

**Example 17.12** We know from Chapter 13 that many high-level graphics functions rely on multiple calls to more primitive routines that allow for setting a variety of parameters (e.g., via par). A common scenario is for a high-level function to pass all the arguments down. Each underlying procedure can then decide by itself which items it is interested in.

```
test <- function(...)</pre>
₹
 subtest1 <- function(..., a=1) c(a=a)</pre>
 subtest2 <- function(..., b=2) c(b=b)</pre>
 subtest3 <- function(..., c=3) c(c=c)</pre>
 c(subtest1(...), subtest2(...), subtest3(...))
}
test(a="A", b="B", d="D")
a b
"A" "B" "3"
```

Here, for instance, **subtest1** only consumes the value of a and ignores all other arguments whatsoever. **plot.default** (amongst others) relies on such a design pattern.

`...length` fetches the number of items passed via the ellipsis, `...names` retrieves their names (in the case they are given as keyword arguments), and `...elt`(i) gives with `...elt`(1), `...elt`(2), etc.

```
test <- function(...)</pre>
 (continues on next page)
```

```
{
 cat("length:", ...length(), "\n")
 cat("names: ", paste(...names(), collapse=", "), "\n")
 for (i in seq_len(...length()))
 cat(i, ":", ...elt(i), "\n")
 print(substitute(...elt(i)))
}

test(u={cat("honey! "); "a"}, {cat("gravy! "); "b"}, w={cat("bacon! "); "c"})
length: 3
names: u, , w
honey! 1: a
gravy! 2: b
bacon! 3: c
...elt(3L)
```

Note that `...elt`(i) triggers the evaluation of the respective argument. Unfortunately, we cannot use **substitute** to fetch the underlying expression. Instead, we can rely on match.call discussed in Section 15.4.4:

```
test <- function(a, b, ..., z=1)
{
 e <- match.call()[-1]
 as.list(e[!(names(e) %in% names(formals(sys.function())))])
}

str(test(1+1, 2+2, 3+3, 4+4, a=2, z=8, w=4))
List of 4
$: language 2 + 2
$: language 3 + 3
$: language 4 + 4
$ w: num 4</pre>
```

**Note** Objects passed via `...`, even if they are specified as keyword arguments, cannot be referred to by their name as if they were local variables:

```
test <- function(...) zzz
test(zzz=3)
Error in test(zzz = 3): object 'zzz' not found</pre>
```

In other words, no assignment in the local environment is triggered.

Exercise 17.13 Implement your version of the switch function.

Exercise 17.14 Write your version of the stopifnot function.

# 17.4 on.exit(\*)

**on.exit** registers an expression to be evaluated at the very end of a call, regardless of whether the function exited due to an error or not. It might be used to reset the temporarily modified graphics parameters (see **par**) and system options (**options**) or clean up the allocated resources (e.g., close all open file connections). For instance:

```
test <- function(reset=FALSE, error=FALSE)</pre>
{
 on.exit(cat("eggs\n"))
 on.exit(cat("bacon\n")) # replace
 on.exit(cat("spam\n"), add=TRUE) # add
 cat("roti canai\n")
 if (reset)
 on.exit() # cancels all (replace by nothing)
 if (error)
 stop("aaarrgh!")
 cat("end\n")
 "return value"
}
test()
roti canai
end
bacon
spam
[1] "return value"
test(reset=TRUE)
roti canai
end
[1] "return value"
test(error=TRUE)
roti canai
Error in test(error = TRUE): aaarrgh!
bacon
spam
```

We can always manage without **on.exit**, e.g., by applying exception handling techniques; see Section 8.2.

**Exercise 17.15** In the definition of scan, notice the call to:

```
on.exit(close(file))
```

*Is its purpose to close the file on exit?* 

**Exercise 17.16** Why does **graphics**::**barplot.default** call the following expressions?

```
dev.hold()
opar <- if (horiz) par(xaxs="i", xpd=xpd) else par(yaxs="i", xpd=xpd)
on.exit({
 dev.flush()
 par(opar)
})</pre>
```

# 17.5 Metaprogramming and laziness in action: Examples (\*)

Due to lazy evaluation, we can define functions that permit any random syntactically valid gibberish to be fed as their arguments. Nothing but basic decency stops us from interpreting them in any way we want. Each such function can become a microverse (a microlanguage?) by itself. This will surely confuse<sup>2</sup> our users, as they will have to analyse every procedure's behaviour separately.

In this section, we extend on our notes from Section 9.4.7 and Section 12.3.9. We look at a few functions relying on metaprogramming and laziness, mostly because studying them is a good exercise. It can help extend our programming skills and deepen our understanding of the concepts discussed in this part of the book. By no means is it an invitation to use them in practice. Nevertheless, R's computing on the language capabilities might interest some advanced programmers (e.g., package developers).

#### 17.5.1 match.arg

match.arg was mentioned in Section 9.4.7. When called normally, it matches a string against a set of possible choices, similarly to pmatch:

```
choices <- c("spam", "bacon", "eggs")
match.arg("spam", choices)
[1] "spam"
match.arg("s", choices) # partial matching
[1] "spam"
match.arg("eggplant", choices) # no match
Error in match.arg("eggplant", choices): 'arg' should be one of "spam",
"bacon", "eggs"</pre>
```

(continues on next page)

<sup>&</sup>lt;sup>2</sup> Novices are prone to overgeneralising when they learn new material that they are still far from comfortable with. Such exceptions go against this natural coping strategy of theirs.

```
match.arg(choices, choices) # match first
[1] "spam"
```

However, skipping the second argument, this function will fetch the choices from the default argument of the function it is enclosed in!

```
test <- function(x=c("spam", "bacon", "eggs"))</pre>
 match.arg(x)
test("spam")
[1] "spam"
test("s")
[1] "spam"
test("eggplant")
Error in match.arg(x): 'arg' should be one of "spam", "bacon", "eggs"
test()
[1] "spam"
```

**Exercise 17.17** Inspect the source code of **stats**::**binom.test**, which looks like:

```
function(..., alternative = c("two.sided", "less", "greater"))
{
 # ...
 alternative <- match.arg(alternative)</pre>
}
```

Read the description of the alternative argument in the documentation.

**Exercise 17.18** Study the source code of match.arg. In particular, notice the following fragment:

```
if (missing(choices)) {
 formal.args <- formals(sys.function(sysP <- sys.parent()))</pre>
 choices <- eval(
 formal.args[[as.character(substitute(arg))]],
 envir=sys.frame(sysP)
}
```

#### 17.5.2 curve

The **curve** function can be called, e.g., like:

```
curve(sin(1/x^2), 1/pi, 3, 1001, lty=2)
```

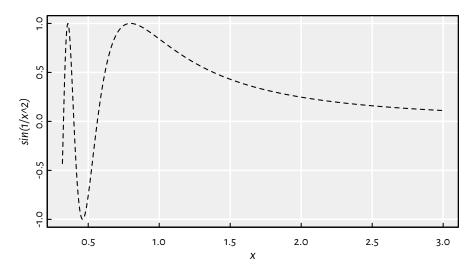


Figure 17.1. An example plot generated by calling **curve**.

It results in Figure 17.1. Wait a minute... We did not define x as a sequence ranging between about 0.3 and 3!

**Exercise 17.19** Study the source code of *curve*. Take note of the following code fragment:

```
function(expr, from=NULL, to=NULL, n=101, xlab="x", type="l", ...)
{
 # ...
 expr <- substitute(expr)
 ylab <- deparse(expr)
 x <- seq.int(from, to, length.out=n)
 ll <- list(x=x)
 y <- eval(expr, envir=ll, enclos=parent.frame())
 plot(x=x, y=y, type=type, xlab=xlab, ylab=ylab, ...)
 # ...
}</pre>
```

#### 17.5.3 with and within

Environments and named lists (and hence data frames) are similar (Section 16.1.2). Due to this, the envir argument to **eval** can be set to either. Therefore, for instance:

```
eval(quote(head(Sepal.Length)), envir=iris)
[1] 5.1 4.9 4.7 4.6 5.0 5.4
```

It evaluates the given expression in something like list2env(iris, parent=parent.

**frame())**. Thus, even though Sepal. Length is not a standalone variable, it is treated as one *inside* the iris data frame.

Moreover, the enclosure is set to the calling frame. Hence, we can successfully refer to the **head** function located somewhere on the search path. This is somewhat similar to **attach** (Section 16.2.6) but without modifying the search path.

The with function does exactly the above:

```
print(with.default)
function (data, expr, ...)
eval(substitute(expr), data, enclos = parent.frame())
<environment: namespace:base>
```

### Example use:

```
with(iris, {
 mean(Sepal.Length) # `Sepal.Length` is in `iris`
})
[1] 5.8433
```

As we evaluate the above in the local (temporary) environment, we cannot modify the existing columns of the data frame this way. However, the within function includes a way to detect and apply any changes made.

```
within(iris, {
 Sepal.Length <- Sepal.Length/1000
 Spam <- "yum!"
}) -> iris2
head(iris2, 3)
 Sepal.Length Sepal.Width Petal.Length Petal.Width Species Spam
 3.5
 1.4
 0.2 setosa vum!
1
 0.0051
2
 0.0049
 3.0
 1.4
 0.2 setosa yum!
3
 0.0047
 3.2
 1.3
 0.2 setosa yum!
```

# **Exercise 17.20** Study the source code of within:

```
print(within.data.frame)
function (data, expr, ...)
{
 parent <- parent.frame()</pre>
##
 e <- evalq(environment(), data, parent)</pre>
##
 eval(substitute(expr), e)
##
##
 l <- as.list(e, all.names = TRUE)</pre>
##
 l <- l[!vapply(l, is.null, NA, USE.NAMES = FALSE)]</pre>
 nl <- names(l)</pre>
##
 del <- setdiff(names(data), nl)</pre>
##
 data[nl] <- l
##
```

(continues on next page)

```
data[del] <- NULL
data
}
<environment: namespace:base>
```

Note that evalq(expr, ...) is equivalent to eval(quote(expr), ...). Also, vapply(X, FUN, NA, ...) is like a call to sapply, but it guarantees that the result is a logical vector.

#### 17.5.4 transform

We can call **transform** to modify/add columns in a data frame using vectorised functions. For instance:

```
head(transform(mtcars, log_hp=log(hp), am=2*am-1, hp=NULL), 3)
##
 mpg cyl disp drat
 wt qsec vs am gear carb log_hp
Mazda RX4
 21.0 6 160 3.90 2.620 16.46 0 1
 4
 4 4.7005
Mazda RX4 Wag 21.0 6 160 3.90 2.875 17.02 0
 1
 4
 4 4.7005
 4 108 3.85 2.320 18.61 1 1
Datsun 710
 22.8
 1 4.5326
```

If we suspect that this function evaluates all expressions passed as `...` within the data frame, we are brilliantly right. Furthermore, there must be a mechanism to detect newly created variables so that new columns can be added.

#### Exercise 17.21 Study the source code of transform:

```
print(transform.data.frame)
function (`_data`, ...)
{
 e <- eval(substitute(list(...)), `_data`, parent.frame())</pre>
##
 tags <- names(e)
##
 inx <- match(tags, names(` data`))</pre>
##
 matched <- !is.na(inx)</pre>
##
##
 if (any(matched)) {
##
 ` data`[inx[matched]] <- e[matched]
 ` data` <- data.frame(` data`)
##
##
 if (!all(matched))
##
##
 do.call("data.frame", c(list(`_data`), e[!matched]))
##
 else ` data`
}
<environment: namespace:base>
```

In particular, note that e is a named list.

#### 17.5.5 subset

The **subset** function selects rows and columns of a data frame that meet certain criteria. For instance:

The second argument, the row selector, must definitely be evaluated within the data frame. We expect it to reduce itself to a logical vector which can then be passed to the index operator.

The "select all columns except those between the given ones" part can be implemented by assigning each column a consecutive integer and then treating them as numeric indexes.

#### **Exercise 17.22** Study the source code of **subset**:

```
print(subset.data.frame)
function (x, subset, select, drop = FALSE, ...)
{
##
 chkDots(...)
 r <- if (missing(subset))</pre>
##
 rep_len(TRUE, nrow(x))
##
 else {
##
 e <- substitute(subset)</pre>
##
##
 r <- eval(e, x, parent.frame())</pre>
 if (!is.logical(r))
##
##
 stop("'subset' must be logical")
 r & !is.na(r)
##
##
 vars <- if (missing(select))</pre>
##
 rep len(TRUE, ncol(x))
##
##
 else {
 nl <- as.list(seg along(x))</pre>
##
 names(nl) <- names(x)
##
 eval(substitute(select), nl, parent.frame())
##
##
 x[r, vars, drop = drop]
##
}
<environment: namespace:base>
```

# 17.5.6 Forward pipe operator

Section 10.4 mentioned the pipe operator, `|>`. We can compose its simplified version manually:

```
`%>%` <- function(e1, e2)
{
 e2 <- as.list(substitute(e2))
 e2 <- as.call(c(e2[[1]], substitute(e1), e2[-1]))
 eval(e2, envir=parent.frame())
}</pre>
```

This function imputes e1 as the first argument in a call e2 and then evaluates the new expression.

Example calls:

```
x <- c(1, NA_real_, 2, 3, NA_real_, 5)
x %>% mean # mean(x)
[1] NA
x %>% `-`(1) # x-1
[1] 0 NA 1 2 NA 4
x %>% na.omit %>% mean # mean(na.omit(x))
[1] 2.75
x %>% mean(na.rm=TRUE) # mean(x, na.rm=TRUE)
[1] 2.75
```

Moreover, we can memorise the value of e1 so that it can be referred to in the expression on the right side of the operator. This comes at a cost of forcing the evaluation of the left-hand side argument and thus losing the potential benefits of laziness, including access to the generating expression.

```
`%.>%` <- function(e1, e2)
{
 env <- list2env(list(.=e1), parent=parent.frame())
 e2 <- as.list(substitute(e2))
 e2 <- as.call(c(e2[[1]], quote(.), e2[-1]))
 eval(e2, envir=env)
}</pre>
```

This way, we can refer to the value of the left side multiple times in a single call. For instance:

```
runif(5) %.>% `[`(.>0.5) # x[x>0.5] with x=runif(5)
[1] 0.78831 0.88302 0.94047
```

This is crazy, I know. I made this. Your author. One more then:

I cannot wait for someone to put this operator into a new R package (it is a brilliant idea, by the way, isn't it?) and then confuse thousands of users ("What is this thing?").

# 17.5.7 Other ideas (\*\*)

Why stop ourselves here? We can create way more invasive functions that read the local variables in the calling functions (unless they are primitive; in R, there are often exceptions to general rules...). Here is an operator which helps select a range of columns in a data frame between two given labels:

```
`%:%` <- function(e1, e2)
{
 # get the `x` argument in the caller (hoping its `[`)
 x <- get("x", envir=sys.frame(sys.nframe()-1))</pre>
 n < -names(x)
 from <- pmatch(substitute(e1), n)</pre>
 to <- pmatch(substitute(e2), n)
 from: to
}
head(iris[, Sepal.W%:%Petal.W])
 Sepal.Width Petal.Length Petal.Width
 3.5
 1.4
1
 0.2
2
 3.0
 1.4
 0.2
 3.2
 1.3
 0.2
3
 3.1
 1.5
4
 0.2
 3.6
 1.4
5
 0.2
 3.9
6
 1.7
 0.4
```

This operator relies on the assumption that it is called in the expression passed as an argument to a non-primitive function which also takes a named vector x as an actual parameter. So ugly, but saves a few keystrokes. We will not be using it because it is not good for us.

**Exercise 17.23** *Make the above more foolproof:* 

- if `%:%` is used outside of `[` or `[<-`, raise a polite error,
- permit x to be a matrix (is it possible?),
- prepare better for the case of less expected inputs.

**Exercise 17.24** *Modify the definition of the above operator so that both:* 

```
iris[, -Sepal.W%:%Petal.W]
iris[, -(Sepal.W%:%Petal.W)]
```

mean "select everything except".

**Exercise 17.25** Define `%:%` for data frames so that:

- x[%:%3, ] means "select the first three rows",
- x[3%:%, ] means "select from the third to the end",
- x[-3%:%, ] means "select from the third last to the end",
- x[%:%-10, ] means "select all but the last nine".

You can go one step further and redefine `[` entirely to support such kinds of indexers.

The ceiling is the limit. Please, do not use the above in production.

# 17.6 Processing formulae, `~` (\*)

Formulae were introduced to S in the early 1990s [13]. Their original raison d'être was to specify *statistical models*; compare Section 10.3.4.

From the language perspective, they are merely unevaluated calls to the `~` (tilde) operator. When creating them, we do not even have to apply **quote** explicitly. For instance:

```
f <- (y ~ x1 + x2) # or: `~`(y, x1+x2)
mode(f)
[1] "call"
class(f)
[1] "formula"</pre>
```

Hence, formulae are compound objects in the sense given in Chapter 10. Usually, they are equipped with an additional attribute:

```
attr(f, ".Environment") # environment active when the formula was created
<environment: R_GlobalEnv>
```

**Exercise 17.26** Write a function that generates a list of formulae of the form " $y \sim x1+x2+...+xk$ ", for all possible combinations x1, x2, ..., xk (of any cardinality) of elements in a given set of xs. For instance:

```
formula_allcomb <- function(y, xs, env=parent.frame()) ...to.do...
str(formula_allcomb("len", c("supp", "dose")))
List of 3</pre>
```

(continues on next page)

```
$:Class 'formula' language len ~ supp + dose
....- attr(*, ".Environment")=<environment: R_GlobalEnv>
$:Class 'formula' language len ~ dose
 ...- attr(*, ".Environment")=<environment: R_GlobalEnv>
##
$:Class 'formula' language len ~ supp
 - attr(*, ".Environment")=<environment: R_GlobalEnv>
str(formula allcomb(
 "y",
 c("x1", "x2", "x3"),
 env=NULL
))
List of 7
$:Class 'formula' language y ~ x1 + x2 + x3
$:Class 'formula' language y ~ x2 + x3
$:Class 'formula' language y ~ x1 + x3
$:Class 'formula' language y ~ x3
$:Class 'formula' language y ~ x1 + x2
$:Class 'formula' language y ~ x2
$:Class 'formula' language y ~ x1
```

As they are unevaluated calls, functions can assign any fantastic meaning to formulae. We cannot really do anything about this freedom of expression. However, many functions, especially in the **stats** and **graphics** packages, rely on a call to **model.frame** and related routines. Thanks to this, we can at least find a few behavioural patterns. In particular, **help**("formula") lists the typical meanings of operators that can be used in a formula.

**Example 17.27** Here are a few examples (executing the expressions below is left as an exercise).

Draw a box-and-whisker plot for iris[["Sepal.Length"]] split by iris[["Species"]]:

```
boxplot(Sepal.Length~Species, data=iris)
```

 Draw a box plot for ToothGrowth[["len"]] split by a combination of levels in Tooth-Growth[["supp"]] and ToothGrowth[["dose"]]:

```
boxplot(len~supp:dose, data=ToothGrowth)
```

• Split the given data frame by a combination of values in two specified columns therein:

```
split(ToothGrowth, ~supp:dose)
```

• Fit a linear regression model of the form y = a + bx, where y is iris[["Sepal.Length"]] and x is iris[["Petal.Length"]]:

```
lm(Sepal.Length~Petal.Length, data=iris)
```

• Fit a linear regression model without the intercept term of the form z = ax + by, where z is iris[["Sepal.Length"]], x is iris[["Petal.Length"]], and y is iris[["Sepal.Width"]]:

```
lm(Sepal.Length~Petal.Length+Sepal.Width+0, data=iris)
```

• Fit a linear regression model of the form z = a + bx + cy + dxy, where z is iris[["Sepal. Length"]]+e (with e fetched from the associated environment), and x and y are like above:

```
e <- rnorm(length(iris[["Sepal.Length"]]), 0, 0.05)
lm(I(Sepal.Length+e)~Petal.Length*Sepal.Width, data=iris)
```

• Draw scatter plots of warpbreaks[["breaks"]] vs their indexes for data grouped by a combination of warpbreaks[["wool"]] and warpbreaks[["tension"]]:

```
Index <- seq_len(NROW(warpbreaks))
coplot(breaks ~ Index / wool * tension, data=warpbreaks)</pre>
```

From the perspective of this book, which focuses on more universal aspects of the R language, formulae are not interesting enough to describe them in any more detail. However, the tender-hearted reader is now equipped with all the necessary knowledge to solve the following very educative exercises.

Exercise 17.28 Study the source code of graphics:::boxplot.formula, stats::Im, and stats:::t.test.formula and notice how they prepare and process the calls to model.frame, model.matrix, model.response, model.weights, etc. Note that their main aim is to prepare data to be passed to boxplot.default, lm.fit (it is just a function with such a name, not an S3 method), and t.test.default

**Exercise 17.29** Write a function similar to *curve*, but one that lets us specify the function to plot using a formula.

# 17.7 Exercises

**Exercise 17.30** *Answer the following questions.* 

- What is the role of promises?
- Why do we generally discourage the use of functions relying on metaprogramming?
- How are default arguments evaluated?
- Is there anything special about formulae from the language perspective?

Revaluates function arguments lazily. Does it mean that "y[c(length(y)+1, length(y)+1, length(y)+1)] <- list(1, 2, 3)" extends a list y by three elements? Or are there cases where evaluation is eager?</li>

**Exercise 17.31** Why the two following calls yield different results?

```
test <- function(x, y=deparse(substitute(x)), force_first=FALSE)
{
 if (force_first) y # just force the evaluation of `y` here
 x <- x**2
 print(y)
}
test(1:5)
[1] "c(1, 4, 9, 16, 25)"
test(1:5, force_first=TRUE)
[1] "1:5"</pre>
```

### 17.8 Outro

Recall our first approximation to the classification of R data types that we presented in the *Preface*. To summarise what we have covered in this book, let us contemplate Figure 17.2, which gives a much broader picture.

If we omitted something, it was most likely on purpose: either we can now study it on our own easily, it is not really worth our attention, or it violates our *minimalist* design principles that we explained in the *Preface*.

Now that we have reached the end of this course, we might be interested in reading:

- R Language Definition [67],
- R Internals [66],
- Writing R Extensions [63],
- R's source code available at https://cran.r-project.org/src/base.

What is more, the NEWS files available at https://cran.r-project.org/doc/manuals/r-release will keep us updated with fresh features, bug fixes, and newly deprecated functionality; see also the **news** function.

Please spread the news about this book. Also, check out another open-access work by yours truly, *Minimalist Data Wrangling with Python*<sup>3</sup> [26]. Thank you.

Good luck with your further projects!

<sup>&</sup>lt;sup>3</sup> https://datawranglingpy.gagolewski.com/

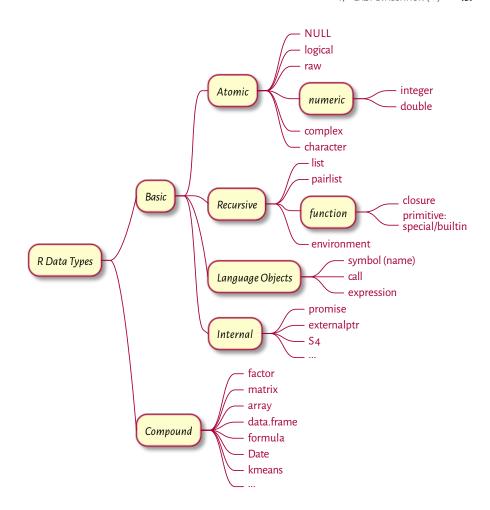


Figure 17.2. R data types.

# Changelog

**Important** Any bug/typo reports/fixes<sup>4</sup> are appreciated. The most up-to-date version of this book can be found at https://deepr.gagolewski.com/.

Below is the list of the most noteworthy changes:

- under development (v1.0.0.9xxx):
  - Printed (paperback) version can now be ordered from Amazon<sup>5</sup>.
  - Minor extensions.
  - (...) to do (...) work in progress (...)
- 2023-06-28 (V1.O.O):
  - Final proofreading and copyediting.
  - Minor extensions.
- 2023-05-19 (vo.9.0):
  - Chapter on interfacing compiled code drafted.
  - Minor extensions.
- **2023-04-27** (vo.2.1):
  - Chapter on graphics drafted.
- 2023-04-09 (vo.2.0):
  - New HTML theme (with light and dark modes).
  - Chapter on unevaluated expressions drafted.
  - Chapter on environments and evaluation drafted.
  - Chapter on lazy evaluation drafted.
- 2022-12-29 (VO.1.12):
  - First public release at https://deepr.gagolewski.com/.

<sup>4</sup> https://github.com/gagolews/deepr/issues

<sup>5</sup> https://www.amazon.com/dp/064557192X

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- Chapters 1–12 (basic and compound types, functions, control flow, etc.) drafted.
- Preface drafted.
- ISBN 978-0-6455719-2-9 reserved.
- Cover.

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