# **Deep R Programming**

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Weird is the world we live in, but the following had to be written.

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Anyway, any bug reports/corrections/feature requests are welcome. To make this text-book even better, please file them at https://github.com/gagolews/deepr.

Typeset with XeMEX. Please be understanding: it was an algorithmic process. Hence, the results are ∈ [good enough, perfect).

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Deep R Programming by Marek Gagolewski<sup>1</sup> is a **comprehensive course on one of the most popular languages in data science** (statistical computing, graphics, machine learning, data wrangling and analytics). It **introduces the base language** in-depth. It is aimed at ambitious students, practitioners, and researchers who want to become **independent users** of this powerful environment.

Although available online, this is a whole course. It should be read from the beginning to the end. In particular, refer to the *Preface* for general introductory remarks.

#### This early draft is distributed in the hope that it will be useful.

For many students around the world, educational resources are hardly affordable. Therefore, I have decided that this book should **remain an independent, non-profit, open-access project** (available both in PDF<sup>2</sup> and HTML<sup>3</sup> forms). Whilst, for some people, the presence of a "designer tag" from a major publisher might still be a proxy for quality, it is my hope that this publication will prove useful to those seeking knowledge for knowledge's sake.

**Please spread the news** about it by sharing the above URLs with your mates, peers, or students. Thank you.

Also, check out my other book, Minimalist data wrangling with Python<sup>4</sup> [25].

Any bug/typo reports/fixes are appreciated: please submit them via this project's Git-Hub repository<sup>5</sup>.

Consider citing this book as: Gagolewski M. (2023), *Deep R Programming*, Zenodo, Melbourne, DOI: 10.5281/zenodo.7490464<sup>6</sup>, ISBN: 978-0-6455719-2-9, URL: https://deepr.gagolewski.com/.

<sup>1</sup> https://www.gagolewski.com

<sup>&</sup>lt;sup>2</sup> https://deepr.gagolewski.com/deepr.pdf

<sup>3</sup> https://deepr.gagolewski.com/

<sup>4</sup> https://datawranglingpy.gagolewski.com/

<sup>&</sup>lt;sup>5</sup> https://github.com/gagolews/deepr/issues

<sup>6</sup> https://dx.doi.org/10.5281/zenodo.7490464

## Preface

#### 0.1 To R, or not to R

R [64] has been named the eleventh most dreaded programming language in the 2022 StackOverflow Developer Survey<sup>7</sup>.

Also, it is a free app, so there must be something wrong with it, right?

But whatever, R is deprecated anyway; the "modern" way is to use **tidyverse**.

Or we should all just switch to Python<sup>8</sup>.

Well, not really<sup>9</sup>.

## 0.2 R (GNU S) as a language and an environment

Let us get one thing straight: R is *not* just a *statistical package*. It is a general-purpose, high-level programming language that happens to be very powerful for numerical, data-intense computing activities of any kind. It offers extensive support for statistical, machine learning, data analysis, data wrangling, and data visualisation applications, but there is much more.

Initially, R<sup>10</sup> was written for statisticians, by statisticians. Therefore, it is a free, yet more capable alternative to Stata, SAS, SPSS, Statistica, Minitab, Weka, etc. (and without any strings attached). Unlike in some of them, in R, a spreadsheet-like GUI is not the main gateway for performing computations on data. Here, a user must *write code* to get things done. Despite the learning curve's being a little steeper for non-programmers, in the long run, it empowers their users because they are not limited only to the most common scenarios. If some functionality is missing or does not suit their needs, they can easily implement everything themselves.

It is thus very convenient for rapid prototyping. It helps turn our ideas into operational

<sup>&</sup>lt;sup>7</sup> https://survey.stackoverflow.co/2022/

<sup>8</sup> https://datawranglingpy.gagolewski.com/

<sup>&</sup>lt;sup>9</sup> Or, as Aussies would say, yeah, nah.

<sup>&</sup>lt;sup>10</sup> Or we should rather say: S, whose open-source reimplementation/dialect R is; see below for historical notes. Credit must be given where credit is due.

code that can be tested, extended, polished, run in production, and otherwise enjoyed. As an interpreted language, it can not only be executed in an interactive read-eval-print loop (command-result, question-answer, ...), but also in batch mode (running whole, standalone scripts).

Thus, we would rather position R amongst such tools/languages for numerical or scientific computing as Python with the NumPy ecosystem, Julia, GNU Octave, Scilab, MATLAB, etc. However, it is more *specialised* in data science applications than any of them. Hence, it provides a much smoother experience. This is why, over the years, R has become the de facto standard in statistics and many other related fields.

**Important** R is a whole ecosystem (environment). It not only consists of the R language interpreter, but also features advanced:

- graphics capabilities (see Chapter 13),
- a consistent, well-integrated help system (Section 1.4),
- ways for convenient interfacing with compiled code (Chapter 14),
- a package system and centralised package repositories (such as CRAN and Bioconductor; Section 7.3.1),
- a lively community of users and developers curious and passionate people, like you and me.

**Note** R is a free, open-source (licensed under the GNU General Public License v2) variation upon/dialect of the very popular S system designed in the mid-1970s by Rick A. Becker, John M. Chambers, and Allan R. Wilks at Bell Labs; see [3, 4, 5, 6] and its later revisions [7, 9, 13, 52].

Quoting [4]:

The design goal for S is, most broadly stated, to enable and encourage good data analysis, that is, to provide users with specific facilities and a general environment that helps them quickly and conveniently look at many displays, summaries, and models for their data, and to follow the kind of iterative, exploratory path that most often leads to a thorough analysis. The system is designed for interactive use with simple but general expressions for the user to type, and immediate, informative feedback from the system, including graphic output on any of a variety of graphical devices.

S became popular because it offered greater flexibility than the standalone statistical packages. It was praised for its high interactivity and array orientation that was known from APL, the familiar syntax of the C language that involves the use of {curly braces}, the ability to treat code as data known from Lisp (Chapter 15), the notion of lazy arguments (Chapter 17), and the ease of calling external C and FORTRAN routines (Chapter 14). Its newer versions were also somewhat object-oriented (Chapter 10).

However, S was a commercial system. To address this, R (GNU S) was developed in the mid-1990s<sup>11</sup>by Robert Gentleman and Ross Ihaka of the Statistics Department, University of Auckland, and many contributors; see [12, 36] for some historical notes. In essence, R was supposed to be backwards-compatible with S, but some design choices led to their evaluation models' being slightly different: its design was heavily inspired by Scheme (with its environment model of evaluation; see [1] and Chapter 16 for more details)

## 0.3 Aims, scope, and design philosophy

Many users were introduced to R by means of some very advanced operations involving data frames, formulae, and functions that rely on nonstandard evaluation (metaprogramming), like:

```
lm(
    Ozone~Solar.R+Temp,
    data=subset(airquality, Temp>60, select=-(Month:Day))
) |> summary()
```

This is horrible.

Another group was isolated from the base R through a thick layer of third-party packages that feature an overwhelming number of functions (every operation, regardless of its complexity, has a different name), often duplicate the core functionality, and sometimes are quite incompatible with our traditional system.

Both user families ought to be fine, as long as they limit themselves to solving only the simplest and most common data processing problems.

But we yearn for more. We do not want hundreds of prefabricated *recipes* for popular dishes that we can mindlessly apply without much understanding.

Our aim is to learn base R, which is supposed to be the common language (lingua franca)

<sup>&</sup>lt;sup>11</sup> R version 0.49 released in April 1997 (the first for which source code? is available on CRAN), was already quite feature-rich (e.g., implemented S3 methods, formulae, and data frames introduced in the 1991 version of S [13]).

<sup>11</sup> https://cloud.r-project.org/src/base/R-o/

for all R users. We want to write code that everybody *should* be able to understand; code that will work without modifications ten years from now (no slang!).

We want to be able to tackle *any* data-intense problem. Furthermore, we want to develop *transferable* skills so that learning new tools such as Python with NumPy and Pandas (e.g., [25]) or Julia will be much easier later (because R is not the only notable environment out there).

Anyway, enough preaching. This graduate 12-level textbook is for independent readers who:

- do not mind a slightly steeper learning curve at the beginning,
- can appreciate a more cohesively and comprehensively<sup>13</sup> organised material,
- would like to experience the joy of solving problems by programming,
- do not want to be made obsolete by artificial "intelligence" in the future.

Some will benefit from it as a first introduction to R (yet, without all the pampering). For others<sup>14</sup>, this will be a fine course from intermediate to advanced (do not skip the first chapters, though).

Either way, do not forget to solve *all* the prescribed exercises.

Good luck.

## 0.4 Classification of R data types and book structure

The most commonly used R data types can be classified as follows; see also Figure 1.

- 1. *Basic types* which we discuss in the first part of this book internal or built-in types, upon which more complex ones are hinged:
  - *atomic vectors* represent whole sequences of values, where every element is of the same type:
    - logical (Chapter 3) includes items that are TRUE ("yes", "present"), FALSE ("no", "absent"), or NA ("not available", "missing");

<sup>&</sup>lt;sup>12</sup> The author taught similar courses for his wonderfully ambitious undergraduate data/computer science and maths students at Warsaw University of Technology, where such an approach has proven not difficult at all. It requires a more independent, curious, and motivated mindset, though. And that's the way to go in the long run.

<sup>&</sup>lt;sup>13</sup> Yours truly is neither a historian, a stenographer, nor a grammarian. We allow ourselves to make a few noninvasive idealisations for didactic purposes. Languages evolve over time, R is now different from what it used to be, and we can shape it (slowly, because we value its stable API) to become something even better in the future.

<sup>&</sup>lt;sup>14</sup> It might also happen that for some, this will not be an appropriate course at all, either at this stage of their career (come back later) or in general (no dramas). This is a non-profit, open-access project, but it does not mean it is ideal for everyone – in such a case, give other sources a try, e.g., [8, 10, 15, 42, 53, 55, 56, 63], etc. Some of them are freely available.



Figure 1: An overview of the most prevalent R data types; see Figure 17.2 for a more comprehensive list

- numeric (Chapter 2) features real numbers, such as 1, 3.14, -0.0000001, etc.;
- character (Chapter 6) contains strings of characters, e.g., "groß",
   "123", от "Добрий день";
- function (Chapter 7) used to group a series of expressions (code lines) so
  that they can be applied on different kinds of input data to generate the
  (hopefully) desired outcomes, for instance, cat, print, plot, sample, and sum;
- list (generic vector; Chapter 4) can store elements of mixed types;

The above will be complemented with a discussion on vector indexing (Chapter 5) and ways to control the program flow (Chapter 8).

- 2. Compound types discussed in the second part wrappers around objects of basic types that might behave differently from the underlying primitives thanks to the dedicated operations overloaded for them. They are:
  - factor (Section 10.3.2) a vector-like object that represents qualitative data (on a nominal or an ordered scale);
  - matrix (Chapter II) stores tabular data, i.e., arranged into rows and columns, where each cell is usually of the same type;
  - data.frame (Chapter 12) also used for depositing tabular data, but this time such that each column can be of a different type;
  - and many more, which we can arbitrarily define using, amongst others, the principles of S3-style object-oriented programming (Chapter 10).

In this part of the book, we also discuss the principles of sustainable coding (Chapter 9) as well as introduce the basic ways to prepare publication-quality graphics (Chapter 13).

- 3. Some more advanced material is discussed in the third part. In most cases, we can (and often should) easily do without it, but it is still essential to gain a complete understanding of and control over our environment. This includes, amongst others, the following data types:
  - externalptr (sec:xptr) provides the ability to store/pass any C/C++ objects between function calls:
  - symbol (name), call, expression (Chapter 15) objects representing unevaluated R expressions that can be freely manipulated and executed if needed;
  - environment (Chapter 16) hashmaps that store named objects and which form the basis of the environment model of evaluation:
  - formula (Section 17.6) used by some functions to specify supervised learning models or define operations to be performed within data subgroups, amongst others.

We should not be surprised that we did not list any data types defined by a few trendy<sup>15</sup> third-party packages. We will later see that we can most often do without them. If that is not the case, we will become skilled enough to learn them quickly ourselves.

#### 0.5 About the author

I, Marek Gagolewski<sup>16</sup> (pronounced like Ma'rek Gong-olive-ski), am currently a Senior Lecturer in Data Science/Applied AI at Deakin University in Melbourne, VIC, Australia, and an Associate Professor at the Systems Research Institute of the Polish Academy of Sciences.

My research interests are related to data science, in particular: modelling complex phenomena, developing usable, general-purpose algorithms, studying their analytical properties, and finding out how people use, misuse, understand, and misunderstand methods of data analysis in research, commercial, and decision-making settings. I'm an author of 90+ publications, including journal papers in outlets such as Proceedings of the National Academy of Sciences (PNAS), Journal of Statistical Software, The R Journal, Information Fusion, International Journal of Forecasting, Statistical Modelling, Physica A: Statistical Mechanics and its Applications, Information Sciences, Knowledge-Based Systems, IEEE Transactions on Fuzzy Systems, and Journal of Informetrics.

In my "spare" time, I write books for my students (also check out my Minimalist data

<sup>&</sup>lt;sup>15</sup> Which does not automatically mean *good*. For instance, sugar, salt, and some drugs are very popular, but it does not make them healthy.

<sup>16</sup> https://www.gagolewski.com

wrangling with Python<sup>17</sup> [25]) and develop open-source (libre) data analysis software, such as **stringi**<sup>18</sup> (one of the most often downloaded R packages), **genieclust**<sup>19</sup> (a fast and robust clustering algorithm in both Python and R), and many others<sup>20</sup>.

## 0.6 Acknowledgements

R, and its predecessor S, is the result of a collaborative effort of many programmers<sup>21</sup>. Without their generous intellectual contributions, the landscape of data analysis would not be as beautiful as it is now. R is distributed under the terms of the GNU General Public license version 2, and we occasionally display fragments of its source code for didactic purposes.

We describe and use R version 4.3.0 (2023-04-21). However, we expect 99.9% of the material covered here to be valid in future releases (consider filing a bug report if you discover this is not the case).

Deep R Programming is based on the author's experience as an R user (since ~2003), developer of open-source packages (mentioned above), tutor/lecturer (since ~2008), and an author of a quite successful Polish textbook Programowanie w języku R (see [24]) which was published by PWN (1st ed. 2014, 2nd ed. 2016). Even though the current book is an entirely different work, its predecessor served as an excellent testbed for many ideas conveyed here.

In particular, the teaching style exercised in this book has proven successful in many similar courses that yours truly has been responsible for, including at Warsaw University of Technology, Data Science Retreat (Berlin), and Deakin University (Melbourne). I thank all my students and colleagues for the feedback given over the last 15-odd years.

However, this book received no funding, administrative, technical, or editorial support from Deakin University, Warsaw University of Technology, Polish Academy of Sciences, or any other source.

This book was prepared in a Markdown superset called MyST<sup>22</sup>, Sphinx<sup>23</sup>, and TeX (XeLaTeX). Code chunks were processed with the R package knitr [58]. All figures were plotted with the low-level graphics package using the author's own style template. A little help from Makefiles, custom shell scripts, and Sphinx plugins (sphinxcontrib-bibtex<sup>24</sup>, sphinxcontrib-proof<sup>25</sup>) dotted the j's and crossed the f's.

<sup>17</sup> https://datawranglingpy.gagolewski.com/

<sup>18</sup> https://stringi.gagolewski.com

<sup>19</sup> https://genieclust.gagolewski.com

<sup>20</sup> https://github.com/gagolews

<sup>&</sup>lt;sup>21</sup> https://www.r-project.org/contributors.html

<sup>&</sup>lt;sup>22</sup> https://myst-parser.readthedocs.io/en/latest/index.html

<sup>23</sup> https://www.sphinx-doc.org/

<sup>24</sup> https://pypi.org/project/sphinxcontrib-bibtex/

<sup>&</sup>lt;sup>25</sup> https://pypi.org/project/sphinxcontrib-proof/

The **Ubuntu** Mono<sup>26</sup> font is used for the display of code. Typesetting of the main text relies upon the  $Alegreya^{27}$  and  $Lato^{28}$  typefaces.

#### 0.7 You can make this book better

Open, non-profit projects such as this have to rely on the generosity of the readers' community when it comes to quality assurance.

If you find a typo, a bug, or a passage that could be rewritten or extended for better readability/clarity, do not hesitate to report it via the *Issues* tracker available at https://github.com/gagolews/deepr/issues/.

Please consider "starring" the book's *GitHub* repository<sup>29</sup>. Some people (weirdly) use the number of "stars" as a proxy for quality.

Also, please spread the news about this book by sharing https://deepr.gagolewski.com/ with your mates, peers, or students. You may also generously cite it in your publications. Thank you.

<sup>&</sup>lt;sup>26</sup> https://design.ubuntu.com/font/

<sup>&</sup>lt;sup>27</sup> https://www.huertatipografica.com/en

<sup>28</sup> https://www.latofonts.com/

<sup>&</sup>lt;sup>29</sup> https://github.com/gagolews/deepr/

Part I

Deep

## Introduction

#### 1.1 Hello, world!

Traditionally, every programming journey starts with the printing of a "Hello, World"-like greeting. Let's then get it over with asap:

```
cat("My hovercraft is full of eels.\n") # `\n` == newline
## My hovercraft is full of eels.
```

By calling (invoking) the **cat** function, we printed out a given character string that we enclosed in double-quote characters.

Documenting code is a good development practice. It is thus worth knowing that any text followed by a hash sign (that is not part of a string) is a *comment*. It ignored by the interpreter.

```
# This is a comment.
# This is another comment.
cat("I cannot wait", "till lunchtime.\n") # two arguments (another comment)
## I cannot wait till lunchtime.
cat("# I will not buy this record.\n# It is scratched.\n")
## # I will not buy this record.
## # It is scratched.
```

By convention, in this book, the textual outputs generated by R itself are always preceded by two hashes. This makes copy-pasting all code chunks easier in the case where the kind readers would like to experiment with them by themselves (which is always highly encouraged).

Whenever a call to some function is to be made, the round brackets are obligatory. All objects within the parentheses (they are separated by commas) constitute the input data to be consumed by the operation. Thus, the syntax is: some\_function\_to\_be\_called(argument1, argument2, etc.).

## 1.2 Setting up the development environment

#### 1.2.1 Installing R

It is quite natural to pine for the ability to execute the above code ourselves – we cannot learn programming without getting our hands dirty.

The official precompiled binary distributions of R can be downloaded from https://cran.r-project.org/.

For serious programming work<sup>1</sup>, we recommend, sooner rather than later, switching to<sup>2</sup> one of the UNIX-like operating systems. This includes the free, open-source (== good) variants of GNU/Linux, amongst others, or the proprietary (== very far from good) m\*\*OS. The users thereof might employ their favourite package manager (e.g., apt, dnf, pacman, or Homebrew) to install R.

Users of other operating systems (such as Wi\*\*\*ws) might consider installing Anaconda or Miniconda if they require some level of interoperability with the Python environment, e.g., they would like to work with the Jupyter environment (Section 1.2.5).

Below we review several ways in which we can write and execute R code. It is up to the benign readers to research, set up, and learn the development environment that suits their needs. As usual in real life, there is no single universal approach that always works best in all scenarios.

#### 1.2.2 Interactive mode

R's read-eval-print loop (REPL) can give us instant gratification whenever we would like to compute something quickly, e.g., determine basic aggregates of a few numbers entered by hand or evaluate a mathematical expression like "2+2".

How to start the R console varies from system to system, e.g., users of UNIX-like boxes can simply execute **R** from the terminal (shell). Wi\*\*\*ws folks can fire up the **RGui** from the *Start* menu.

**Important** When working interactively, the default<sup>3</sup> command prompt, ">", means: *I am awaiting orders*. Moreover, "+" denotes: *Please continue*. In such a case, we should either complete the unfinished expression or cancel the operation by pressing ESC or CTRL+C (depending on the operating system).

> cat("And now

(continues on next page)

<sup>&</sup>lt;sup>1</sup> For instance, when interoperability with other programming languages/environments is required or when we think about scheduling jobs on Linux-based computing/container clusters.

<sup>&</sup>lt;sup>2</sup> Or at least trying out – by installing a copy of GNU/Linux on a virtual machine (VM).

<sup>&</sup>lt;sup>3</sup> It can be changed; see **help**("options").

(continued from previous page)

```
+ for something
+ completely different
+
+ it is an unfinished expression...
+ awaiting another double quote character and then the closing bracket...
+
+ press ESC or CTRL+C to abort input
>
```

For readability, we never print out the command prompt characters in this book.

### 1.2.3 Batch mode: Working with R scripts (\*\*)

The interactive mode of operation is unsuitable for more complicated tasks, though.

The users of UNIX-like operating systems will be interested in another extreme, which involves writing standalone R scripts that can be executed line by line without any user intervention.

To do so, in the terminal (command line, shell), we can invoke:

```
Rscript file.R
```

where file. R is the path to some source file.

**Exercise 1.1** (\*\*) In your favourite text editor (e.g., **Notepad++**, **Kate**, **vi**, **Emacs**, **RStudio**, or **VSCodium**), create a file named test.R. Write a few calls to the **cat** function. Then, execute this script from the terminal by invoking the **Rscript** program.

## 1.2.4 Weaving: Automatic report generation (\*\*)

Reproducible data analysis<sup>4</sup> requires us to keep the results (text, tables, plots, auxiliary files) synchronised with their generating code and data.

utils::Sweave (the Sweave function from the utils package) and knitr [58] are two example template processors that evaluate R code chunks within documents written in LaTeX, HTML, or other markup languages. The chunks are replaced by the outputs they yield.

This book is a showcase of such an approach – all the results, including Figure 2.3 and the above "Hello, World", were generated programmatically. Thanks to its being written in the highly universal Markdown<sup>5</sup> language, it could be easily converted to a single

<sup>&</sup>lt;sup>4</sup> The idea dates back to Knuth's literate programming concept; see [37].

<sup>&</sup>lt;sup>5</sup> https://daringfireball.net/projects/markdown/

PDF document<sup>6</sup> as well as the whole website<sup>7</sup>. Tools like **pandoc** and **docutils** facilitate such operations.

**Exercise 1.2** (\*\*) Install the **knitr** package by calling **install.packages**("knitr") from within an R session. Then, create a text file named test. Rmd with the following content:

```
# Hello, Markdown!

This is my first automatically generated report,
where I print messages and stuff.

```{r}
print("G'day!")
print(2+2)
plot((1:10)^2)

```
Thank you for your attention.
```

Assuming that the file is located in the current working directory (compare Section 7.3.3), call **knitr::knit**("test.Rmd") from the R console or run the following in the terminal:

```
Rscript -e 'knitr::knit("test.Rmd")'
```

Then, inspect the generated Markdown file, test.md.

Furthermore, if you have the **pandoc** tool installed, to generate a standalone HTML file, execute in the terminal:

```
pandoc test.md --standalone -o test.html
```

Alternatively, for ways to call external programs from R, see Section 7.3.3.

# 1.2.5 Semi-interactive modes (Jupyter Notebooks, sending code to an associated R console. etc.)

The nature of the most frequent use cases of R encourages a semi-interactive workflow, where we progress with prototyping fast by trial-and-error.

In this mode, we write a series of short code fragments inside a standalone R script.

Each fragment implements a simple, well-defined task, such as the loading of data files, data cleansing, feature visualisation, computations of some information aggregates, etc.

Importantly, any code chunk can be sent to the associated R console and executed

<sup>6</sup> https://deepr.gagolewski.com/deepr.pdf

<sup>7</sup> https://deepr.gagolewski.com

therein. This way, we can inspect the results it generates at any time. If we are not happy with the outcome, we can apply any corrections that are necessary.

There are quite a few integrated development environments (IDEs; sometimes requiring additional plugins) that enable such a workflow, including JupyterLab, Emacs, RStudio, and VSCodium.

Executing an individual code line or a whole text selection is usually done by pressing (configurable) keyboard shortcuts such as Ctrl+Enter or Shift+Enter.

**Exercise 1.3** (\*) **Jupy terLab**<sup>8</sup> is a development environment that runs in a web browser. It was programmed in Python, but supports many programming languages. Thanks to **IRkernel**<sup>9</sup>, we can use it with R.

- 1. Install **JupyterLab** and **IRkernel** (for instance, if you use Anaconda, run conda install -c r r-essentials).
- 2. From the File menu, select Create a new R source file and save it as, e.g., test.R.
- 3. From the File menu, select Create a new console for the editor running the R kernel.
- 4. Type some print "Hello, World"-like calls.
- 5. Press Shift+Enter (whilst working in the editor) to send different code fragments onto the console and execute them. Inspect the results.

See Figure 1.1 for an illustration.



Figure 1.1: JupyterLab: a source file editor and the associated R console, where we can run arbitrary code fragments

<sup>8</sup> https://jupyterlab.readthedocs.io/en/stable/

<sup>9</sup> https://irkernel.github.io/

**Example 1.4** (\*) The Jupyter project, whose **JupyterLab** is part of, also supports the handling of dedicated Notebooks. There, editable and executable code chunks and results they generate can be kept together in a single. ipynb (JSON) file; see Figure 1.2 for an illustration and Chapter 1 of [25] for a quick introduction (from the Python language kernel perspective).

This environment is quite convenient for live coding (e.g., for teachers) or performing exploratory data analyses. However, for more serious programming work, the code can get quite messy (luckily, there is always an option to export a notebook to an executable, plain text R script).

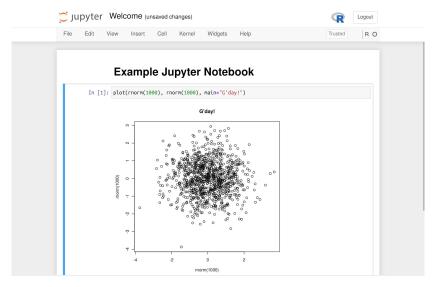


Figure 1.2: An example Jupyter Notebook, where we can keep the code and the results together

## 1.3 Atomic vectors at a glance

After the printing of the "Hello, World" message, a typical programming course would normally proceed with the discussion on basic data types for storing individual numeric or logical values. Next, we would be introduced to arithmetic and relational operations on such *scalars*, followed by the definition of whole arrays or other collections of such values, complemented by the methods to iterate over them, one element after another.

In R, no separate types representing individual values have been defined. Instead, what seems to be a single datum, is already a *vector* (sequence, array) of length 1.

```
2.71828 # input a number (here: the same as print(2.71828))
## [1] 2.7183

(continues on next page)
```

(continued from previous page)

```
length(2.71828) # it is a vector featuring one element
## [1] 1
```

To create a vector of any length, we can call the **c** function, which combines given arguments into a single sequence:

```
c(1, 2, 3) # three vectors of length 1 -> one vector of length 3
## [1] 1 2 3
length(c(1, 2, 3))
## [1] 3
```

In Chapter 2, Chapter 3, and Chapter 6, we will discuss the most prevalent types of atomic vectors: numeric, logical, and character ones, respectively.

We call them *atomic*, because they can only group together values of the same type. Lists, which we will discuss in Chapter 4, are, on the other hand, referred to as *generic* vectors – they can be used for storing items of mixed types – other lists as well.

**Note** Not having separate scalar types greatly simplifies the programming of numerical computing tasks. Vectors are prevalent in our main areas of interest – statistics, simulations, data science, machine learning, and all other data-oriented computing. For example, columns and rows in tables (values of different features describing clients, ratings of items given by users) or time series (stock market prices, readings from temperature sensors) are all best represented by means of such sequences.

Moreover, the fact that vectors are the core part of the R language makes their use very natural — as opposed to the languages that require special add-ons for vector processing, e.g., numpy for Python [33]. By learning different ways to process them *as a whole* (instead of one element at a time), we will ensure that our ideas can quickly be turned into working code (rapid prototyping). For instance, computing summary statistics such as, say, the mean absolute deviation of some sequence x, will be as effortless as writing mean(abs(x-mean(x))). Such a code is not only easy to read and maintain, but it is also fast to run.

### 1.4 Getting help

Our aim is to become independent, advanced R programmers.

Independent, however, does not mean omniscient. The *R help system* is the authoritative source of knowledge about specific functions or more general topics. To open a help page, we call:

```
help("topic") # equivalently: ?"topic"
```

**Exercise 1.5** Sight (without going into detail) the manual on the **length** function by calling **help**("length"). Note that most help pages are structured as follows:

- 1. Header: "package:base" means that the function is a base one (see Section 7.3.1 for more details on the R package system);
- 2. Title:
- 3. Description: a short description of what the function does;
- 4. Usage: the list of formal arguments (parameters) to the function;
- 5. Arguments: the meaning of each formal argument explained;
- 6. Details: technical information;
- 7. Value: return value explained;
- 8. References: further reading;
- 9. See Also: links to other help pages;
- 10. Examples: R code that is worth running and studying by yourself.

We can also search within all the installed help pages by calling:

```
help.search("vague topic") # equivalently: ??"vague topic"
```

This way, we will be able to find answers to our questions more reliably than when asking DuckDuckGo or G\*\* gle, which commonly feature many low-quality/irrelevant/distracting results from splogs (they can make us lose the sacred code writer's flow).

**Important** All code chunks, including code comments and textual outputs, form an integral part of this book's text. They should not be skipped by the reader. On the contrary, they must become objects of our intense reflection and thorough investigation.

For instance, whenever we introduce a few functions, it may be a clever idea to look it up in the help system. Moreover, playing with the presented code (running, modifying, experimenting, etc.) is also very beneficial. We should develop the habit of asking

ourselves questions like "What would happen if...", and then finding the answers on our own.

We are now ready to discuss the most significant operations on numeric vectors, which constitute the main theme of the next chapter. See you there.

#### 1.5 Exercises

**Exercise 1.6** What are the three most important types of atomic vectors?

**Exercise 1.7** According to the classification of the R data types we introduced in the previous chapter, are atomic vectors basic or compound types?

## Numeric vectors

In this chapter, we discuss the uttermost common operations on numeric vectors. They are so fundamental that we will also find them in other scientific computing environments, including Python with NumPy or TensorFlow, Julia, MATLAB, GNU Octave, or Scilab.

At first blush, the number of functions we are going to explore may seem quite large. Still, the reader is kindly asked to place some trust (a rare thing these days) in yours truly. It is because our selection is comprised only of the most representative and educational amongst the plethora of possible choices. More complex building blocks can often be reduced to a creative combination of the former. Also, sometimes they may easily found in a number of additional packages or libraries (e.g., the GNU GSL [27]).

A solid understanding of base R programming is crucial for dealing with popular packages (such as **data.table**, **dplyr**, or **caret**). Most importantly, base R's API is *stable*. Hence, the code we write today will most likely work the same way in ten years. It is often not the case when we rely on third-party add-ons.

In the sequel, we will be advocating a minimalist, keep-it-simple approach to the art of programming data processing pipelines, one that is a healthy balance between "doing it all by oneself", "minimising the information overload", "being lazy", and "standing on the shoulders of giants".

**Note** The exercises that we suggest below are all self-contained unless explicitly stated otherwise. The use of language constructs that are yet to be formally introduced (in particular, **if**, **for**, and **while** explained in Chapter 8) is not just unnecessary: it is discouraged. Moreover, we recommend against taking shortcuts by looking up partial solutions on the internet. Rather, to get the most out of this course, the reader should be seeking relevant information within the current and preceding chapters as well as the R help system.

## 2.1 Creating numeric vectors

#### 2.1.1 Numeric constants

The simplest numeric vectors are those of length one:

```
-3.14
## [1] -3.14
1.23e-4
## [1] 0.000123
```

The latter is in what we call *scientific notation*, which is a convenient means of entering numbers of very large or small orders of magnitude. Here, "e" stands for "... times 10 to the power of...". Therefore, 1.23e-4 is equal to  $1.23 \times 10^{-4} = 0.000123$ . In other words, given 1.23, we move the decimal separator by 4 digits towards the left.

In real life, some information items may be inherently or temporarily missing, unknown, or Not Available. R is data processing-oriented. Hence, it is equipped with a special indicator:

```
NA_real_ # numeric NA (missing value)
## [1] NA
```

It is similar to the *Null* marker in database query languages such as SQL. Note that NA\_real\_is displayed simply as "NA", chiefly for readability.

Moreover, Inf denotes infinity ( $\infty$ ; a value that is larger than the largest representable double precision – 64 bit – floating point number) and NaN stands for *not-a-number* (it is returned as the result of some illegal operations, e.g., 0/0 or  $\infty - \infty$ ).

## 2.1.2 Concatenating vectors with c

Let us provide some ways to create numeric vectors with possibly more than one element.

First, the **c** function that we introduced in the previous chapter can be used to combine (concatenate) many numeric vectors, each of any length, so as to form a single object:

```
c(1, 2, 3) # 3 vectors of length 1 -> 1 vector of length 3
## [1] 1 2 3
c(1, c(2, NA_real_, 4), 5, c(6, c(7, Inf)))
## [1] 1 2 NA 4 5 6 7 Inf
```

**Note** Running help("c"), we will see that its usage is like "c(...)". In the current context, this means that the c function takes an arbitrary number of arguments. In Section 9.5.6, we will study the dot-dot-dot (ellipsis) parameter in more detail.

## 2.1.3 Repeating entries with rep

Second, **rep** replicates the elements in a given vector a given number of times.

```
rep(1, 5)

## [1] 1 1 1 1 1

rep(c(1, 2, 3), 4)

## [1] 1 2 3 1 2 3 1 2 3 1 2 3
```

In the second case, the whole vector (1, 2, 3) has been *recycled* (tiled) four times. Interestingly, if the second argument was a vector of the same length as the first one, the behaviour would be quite different:

```
rep(c(1, 2, 3), c(2, 1, 4))
## [1] 1 1 2 3 3 3 3
rep(c(1, 2, 3), c(4, 4, 4))
## [1] 1 1 1 1 2 2 2 2 3 3 3 3
```

Here, each element is repeated the corresponding number of times.

If we call help("rep"), we will come across the notion like "rep(x, ...)" in the *Usage* section. It is rather peculiar. However, reading further, we discover the dot-dot stands for one of the following further parameters (see the *Arguments* section):

- times,
- length.out,
- · each.

So far, we have been playing with times, which is listed second in the parameter list (after x – the vector whose elements are to be repeated).

**Important** It turns out that the following function calls are all equivalent:

```
rep(c(1, 2, 3), 4) # positional matching of arguments: `x`, then `times` rep(c(1, 2, 3), times=4) # `times` is the second argument rep(x=c(1, 2, 3), times=4) # keyword arguments of the form name=value rep(times=4, x=c(1, 2, 3)) # keyword arguments can be given in any order rep(times=4, c(1, 2, 3)) # mixed positional and keyword arguments
```

We can also pass each or length.out (a dot has no special meaning in R; see Section 2.2), but their names must be mentioned explicitly:

```
rep(c(1, 2, 3), length.out=7)
## [1] 1 2 3 1 2 3 1
rep(c(1, 2, 3), each=3)
## [1] 1 1 1 2 2 2 3 3 3
rep(c(1, 2, 3), length.out=7, each=3)
## [1] 1 1 1 2 2 2 3
```

**Note** Whether it was a good programming practice to actually implement a range of varied behaviours inside a single function is a matter of taste. On the one hand, in all of the examples above, we do repeat the input elements somehow, so remembering just one function name is really convenient. Nevertheless, a drastic change in the repetition pattern depending, e.g., on the length of the times argument can be bug-prone. Anyway, we have been warned<sup>1</sup>.

Zero-length vectors are possible, too:

```
rep(c(1, 2, 3), 0)
## numeric(0)
```

Even though their handling might be a little tricky (compare Chapter 9), we will see later that they are indispensable in contexts like "create an empty data frame with a specific column structure".

Also, note that R often allows for partial matching of named arguments, but its use is a bad programming practice; see Section 15.4.4 for more details.

```
rep(c(1, 2, 3), len=7) # not recommended (see later)
## Warning in rep(c(1, 2, 3), len = 7): partial argument match of 'len' to
## 'length.out'
## [1] 1 2 3 1 2 3 1
```

The only reason we see the warning message is that we have manually set **options**(warnPartialMatchArgs=TRUE) in our environment. It is not set by default.

## 2.1.4 Generating arithmetic progressions with seq and `:`

Third, we can call the **seq** function to create a sequence of equally-spaced numbers (on a linear scale, i.e., an arithmetic progression).

```
seq(1, 15, 2)
## [1] 1 3 5 7 9 11 13 15
```

From the function's help page, we discover that it features the from, to, by, length.out parameters, amongst others.

Thus, the above call is equivalent to:

 $<sup>^1</sup>$  Some "caring" R users might be tempted to introduce two new functions now, one for generating (1, 2, 3, 1, 2, 3, ...) only and the other outputting patterns like (1, 1, 1, 2, 2, 2, ...). They would most likely wrap them in a new package and announce that on Twitter or Mastodon. But this is nothing else than a multiplication of entities without actual necessity. This way, we would end up with three functions. First, the original one, rep, which everyone ought to know anyway because it is so basic and has been and will be used everywhere by almost everybody so far. Second and third, the two redundant ones, whose user-friendliness is only illusory. See also Chapter 9 for a discussion on the design of functions.

```
seq(from=1, to=15, by=2)
## [1] 1 3 5 7 9 11 13 15
```

Note that to actually means "up to":

```
seq(from=1, to=16, by=2)
## [1] 1 3 5 7 9 11 13 15
```

We can also pass length.out instead of by. In such a case, the increments or decrements will be computed via the formula ((to - from)/(length.out - 1)); this *default* value is reported in the *Usage* section in **help**("seq").

```
seq(1, 0, length.out=5)
## [1] 1.00 0.75 0.50 0.25 0.00
```

Also, this:

```
seq(length.out=5) # default `from` is 1
## [1] 1 2 3 4 5
```

Arithmetic progressions with steps equal to 1 or -1 can also be generated via the `:` operator.

```
1:10  # seq(1, 10) or seq(1, 10, 1)

## [1] 1 2 3 4 5 6 7 8 9 10

-1:10  # seq(-1, 10) or seq(-1, 10, 1)

## [1] -1 0 1 2 3 4 5 6 7 8 9 10

-1:-10  # seq(-1, -10) or seq(-1, -10, -1)

## [1] -1 -2 -3 -4 -5 -6 -7 -8 -9 -10
```

Let us highlight the order of precedence of this operator: "-1:10" means "(-1):10" and not "-(1:10)"; compare Section 2.4.3.

**Exercise 2.1** Take a look at the manual page of **seq\_along** and **seq\_len**. Determine whether they can easily be done without having **seq**<sup>2</sup> at hand.

## 2.1.5 Generating pseudorandom numbers

We can also generate sequences drawn independently from a range of univariate probability distributions.

```
runif(7) # uniform U(0, 1)
## [1] 0.287578 0.788305 0.408977 0.883017 0.940467 0.045556 0.528105
rnorm(7) # normal N(0, 1)
## [1] 1.23950 -0.10897 -0.11724 0.18308 1.28055 -1.72727 1.69018
```

<sup>&</sup>lt;sup>2</sup> Certain configurations of **seq** and its variants might return vectors of the type integer instead of double, some of them in a compact (ALTREP) form; see Section 6.4.1.

These correspond to seven pseudorandom deviates following the uniform distribution on the unit interval (i.e., (0,1)) and the standard normal distribution (i.e., with expectation 0 and standard deviation 1), respectively; compare Figure 2.3.

For more *named* distribution classes (frequently occurring in various real-world statistical modelling exercises), see Section 2.3.4.

Another worthwhile function samples a number of values from a given vector, either with or without replacement:

```
sample(1:10, 20, replace=TRUE) # 20 with replacement (allow repetitions)
## [1] 3 3 10 2 6 5 4 6 9 10 5 3 9 9 9 3 8 10 7 10
sample(1:10, 5, replace=FALSE) # 5 without replacement (do not repeat)
## [1] 9 3 4 6 1
```

The distribution of the sampled values does not need to be uniform; the prob argument may be fed with a vector of the corresponding probabilities. For example, here are 20 independent realisations of the random variable X such that Pr(X=0)=0.9 (the probability that we obtain 0 is equal to 90%) and Pr(X=1)=0.1:

```
sample(0:1, 20, replace=TRUE, prob=c(0.9, 0.1))
## [1] 0 0 0 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1
```

**Note** If n is a single number (a numeric vector of length 1), then sample(n, ...) is equivalent to sample(1:n, ...). Similarly, seq(n) is a synonym for seq(1, n) or seq(1, length(n)), depending on the length of n. This is a dangerous behaviour that can occasionally backfire and lead to bugs (check what happens when n is, e.g., o). Nonetheless, we have been warned. From now on, we are going to be extra careful (but are we really?). Read more at help("sample") and help("seq").

Let us stress that the numbers we obtain are merely *pseudo*random because they are generated algorithmically. R uses the Mersenne-Twister MT19937 method [43] by default; see **help**("RNG") and [21, 28, 39]. By setting the *seed* of the random number generator, i.e., resetting its state to a given one, we can obtain results that are *reproducible*.

```
set.seed(12345) # seeds are specified with integers
sample(1:10, 5, replace=TRUE) # a,b,c,d,e
## [1] 3 10 8 10 8
sample(1:10, 5, replace=TRUE) # f,g,h,i,j
## [1] 2 6 6 7 10
```

Setting the seed to the one used previously gives:

```
set.seed(12345)
sample(1:10, 5, replace=TRUE) # a,b,c,d,e
## [1] 3 10 8 10 8
```

We did not(?) expect that! And now for something completely different:

```
set.seed(12345)
sample(1:10, 10, replace=TRUE) # a,b,c,d,e,f,g,h,i,j
## [1] 3 10 8 10 8 2 6 6 7 10
```

Reproducibility is a crucial feature of each truly scientific experiment. The same initial condition (here: the same seed) leads to exactly the same outcomes.

**Note** Some claim that the only unsuspicious seed is 42, but each programmer can have their own picks. Yours truly, for example, uses 123, 1234, and 12345 as well. When performing many runs of Monte Carlo experiments, it may be a clever idea to call **set. seed(i)** in the i-th iteration of a simulation we are trying to program.

Anyhow, we should ensure that our seed settings are applied consistently across all our scripts. Otherwise, we might be accused of tampering with evidence. For instance, here is the ultimate proof that we are very lucky today:

This is exactly why reproducible scripts and auxiliary data should be published alongside all research reports or papers. Only open, transparent science can be fully trustworthy.

If **set.seed** is not called explicitly, and the random state is not restored from the previously saved R session (see Chapter 16), then the random generator is initialised based on the current wall time and the identifier of the running R instance (PID). This may give the impression that the numbers we generate are surprising.

To understand the "pseudo" part of the said randomness better, in Section 8.3, we will build a very simple random generator ourselves.

## 2.1.6 Reading data with scan

The example text file named euraud-20200101-20200630.csv<sup>3</sup> gives the EUR to AUD exchange rates (how many Australian Dollars can one buy for 1 Euro) from 1 January to 30 June 2020 (remember COVID-19?). Let us preview the first couple of lines:

```
# EUR/AUD Exchange Rates
# Source: Statistical Data Warehouse of the European Central Bank System
# https://www.ecb.europa.eu/stats/policy_and_exchange_rates/
# (provided free of charge)
NA
```

(continues on next page)

<sup>&</sup>lt;sup>3</sup> https://github.com/gagolews/teaching-data/raw/master/marek/euraud-20200101-20200630.csv

```
1.6006
1.6031
NA
```

The four first lines that begin with "#" merely serve as comments for us humans. They should be ignored by the interpreter. The first "real" value, NA, corresponds to 1 January (Wednesday, New Year's Day; Forex markets were closed, hence a missing observation).

The **scan** function can be used to read all the inputs and convert them to a single numeric vector:

```
scan(paste0("https://github.com/gagolews/teaching-data/raw/",
   "master/marek/euraud-20200101-20200630.csv"), comment.char="#")
## [1]
          NA 1.6006 1.6031
                             NA NA 1.6119 1.6251 1.6195 1.6193 1.6132
## [11]
                 NA 1.6117 1.6110 1.6188 1.6115 1.6122
                                                                NA 1.6154
                                           NA 1.6291 1.6290 1.6299 1.6412
## [21] 1.6177 1.6184 1.6149 1.6127 NA
                 NA
                        NA 1.6521 1.6439 1.6299 1.6282 1.6417
## [31] 1.6494
## [41] 1.6373 1.6260 1.6175 1.6138 1.6151
                                           NA
                                                   NA 1.6129 1.6195 1.6142
## [51] 1.6294 1.6363 NA
                              NA 1.6384 1.6442 1.6565 1.6672 1.6875
          NA 1.6998 1.6911 1.6794 1.6917 1.7103
                                                  NA
                                                         NA 1.7330 1.7377
                                     NA 1.8198 1.8287 1.8568 1.8635 1.8226
## [71] 1.7389 1.7674 1.7684
                              NA
                 NA 1.8586 1.8315 1.7993 1.8162 1.8209
## [81]
                                                         NA
                                                                NA 1.8021
## [91] 1.7967 1.8053 1.7970 1.8004 NA
                                           NA 1.7790 1.7578 1.7596
## [ reached getOption("max.print") -- omitted 83 entries ]
```

We used the **paste0** function to concatenate two long (too long to fit a single line of code) strings to form a single URL; see Section 6.1.3.

We can also read the files located on our computer, for example:

```
scan("~/Projects/teaching-data/marek/euraud-20200101-20200630.csv",
    comment.char="#")
```

uses an absolute file path that starts at the user's home directory, denoted "~": yours truly's case is /home/gagolews/.

**Note** For portability reasons, we suggest slashes, "/", as path separators (but see help("file.path") and help(".Platform")). These are not only recognised by all UNIX-like boxes but also by other popular operating systems. Note that URLs (such as https://www.r-project.org/) consist of slashes as well.

Paths can also be relative to the current working directory, denoted ".". It can be read via a call to **getwd**. Usually, it is the directory from where the R session has been started.

For instance, if the working directory was /home/gagolews/Projects/teaching-data/

marek, we could have written the file path equivalently as ./euraud-20200101-20200630.csv or even euraud-20200101-20200630.csv.

On as side note, ... / would mark the parent directory of the current working directory. For instance, ... /r/iris.csv would be equivalent to /home/gagolews/Projects/teaching-data/r/iris.csv.

**Exercise 2.2** Read the help page about **scan**. Take note of the following formal arguments and their meaning: dec, sep, what, comment.char, and na. strings.

Later we will discuss the **read.table** and **read.csv**, which are wrappers around **scan** that can be used to read tabular data. Also, **write** can be used to export an atomic vector's contents to a text file.

**Example 2.3** Figure 2.1 shows the graph of the aforementioned exchange rates, which was generated by calling:

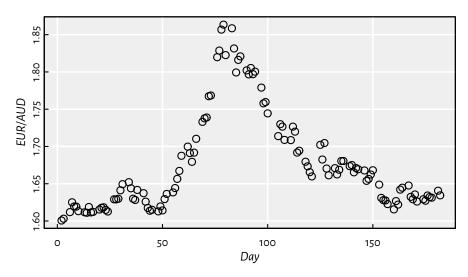


Figure 2.1: EUR/AUD exchange rates from 2020-01-01 (day 1) to 2020-06-30 (day 182)

Somewhat misleadingly (and for reasons that will become apparent later), the documentation of **plot** can be accessed by calling **help**("plot.default"). Read about, and experiment with, different values of the main, xlab, ylab, type, col, pch, cex, lty, and lwdarguments. More plotting routines will be discussed in Chapter 13.

### 2.2 Creating named objects

Often, the objects we bring forth will need to be memorised so that they can be referred to in further computations. The assignment operator, `<-`, can be used for this very purpose:

```
x <- 1:3 # creates a numeric vector and binds the name `x` to it
```

The now-named object can be recalled<sup>4</sup> and dealt with as we please:

```
print(x) # or just `x` in the R console
## [1] 1 2 3
sum(x) # example operation: compute the sum of all elements in `x`
## [1] 6
```

**Important** In R, all names are *case-sensitive*. Hence, x and x can coexist peacefully: when set, they refer to two different objects. Also, if we tried to call Print(x) above, we would get an error.

Typically, we will be using what we refer to as *syntactic names* (see Section 9.4.1 for an exception). In the R help system (see help("make.names") and also help("Quotes")), we read: A syntactically valid name consists of letters, numbers and the dot or underline characters and starts with a letter or the dot not followed by a number. Names such as . 2way are not valid, and neither are the reserved words. For the list of the latter, see help("Reserved").

A fine name is self-explanatory and thus reader-friendly: patients, mean, and average\_scores are way better (if they are what they claim they are) than xyz123, crap, or spam. Also, it might not be such a bad idea to get used to denoting:

- vectors with x, y, z,
- matrices (and matrix-like objects) with A, B, ..., X, Y, Z,
- integer indexes with letters i, j, k, l,
- object sizes with n, m, d, p or nx, ny, etc.,

especially when they are only of temporary nature (for storing some auxiliary results, iterating over collections of objects, etc.).

There are numerous naming conventions that we can adopt, but most often they are a matter of taste; snake\_case, lowerCamelCase, UpperCamelCase, flatcase, or dot. case are equally sound as long as they are used coherently (for instance, some use snake\_case for vectors and UpperCamelCase for functions). It may even be the case that

<sup>&</sup>lt;sup>4</sup> Names are bound in environment frames; see Chapter 16.

we have little choice but to adhere to the naming conventions agreed upon in the project we are about to contribute to.

**Note** Let us stress that a dot, ".", has no special meaning (however, see Chapter 10 and Chapter 16 for some asterisks); na.omit is as appropriate a name as na\_omit, naOmit, NAOMIT, naomit, and NaOmit. Users coming from some other (C, C++, Java, Python, etc.) programming languages will need to habituate themselves to this convention.

R, as a dynamic language, allows for introducing new variables at any time. Moreover, existing names can be rebound to new values. For instance:

Now x refers to a verbatim copy of y.

**Note** Objects are automatically destroyed when there are no more names bound to them. By now, the *garbage collector* is likely to have got rid of the 1:3 vector begotten above (to which the name x was bound previously). See sec:memory-management for more details on memory management.

#### 2.3 Vectorised mathematical functions

Mathematically, we will be denoting a given vector  $\mathbf{x}$  of length n with  $(x_1, x_2, \dots, x_n)$ . In other words, its i-th element is equal to  $x_i$ .

Let us review some ubiquitous operations in numerical computing.

#### 2.3.1 abs and sqrt

R implements *vectorised* versions of the most popular mathematical functions, e.g., **abs** (absolute value, |x|) and **sqrt** (square root,  $\sqrt{x}$ ).

```
abs(c(2, -1, 0, -3, NA_real_))
## [1] 2 1 0 3 NA
```

Here, *vectorised* means that instead of being defined to act on a single numeric value, the function of interest is applied on each element in a vector. The *i*-th resulting item

is a transformed version of the *i*-th input. If an input is a missing value, the corresponding output will be marked as "don't know" as well.

Another example:

```
x <- c(4, 2, -1)
(y <- sqrt(x))
## Warning in sqrt(x): NaNs produced
## [1] 2.0000 1.4142 NaN</pre>
```

To attract our attention to the fact that computing the square root of a negative value yields a not-a-number, R generated an informative warning. A warning is not an error: the result is being reckoned as usual.

Also the fact that the irrational  $\sqrt{2}$  is  $displayed^5$  as 1.4142 does not mean that it is such a crude approximation to 1.414213562373095048801688724209698 ...; it is only rounded when printing for aesthetic reasons. In fact, in Section 3.2.3, we will point out that the computer's floating-point arithmetic allows for roughly 16 decimal digits precision (but we shall see that the devil is in the detail).

```
print(y, digits=16) # display more significant figures
## [1] 2.00000000000000 1.414213562373095 NaN
```

### 2.3.2 Rounding

The following functions get rid of all or portions of fractional parts of numbers:

- **floor**(x) (rounds down to the nearest integer, denoted  $\lfloor x \rfloor$ ),
- **ceiling**(x) (rounds up, denoted  $\lceil x \rceil$ ),
- trunc(x) (rounds towards zero), and
- round(x, digits=0) (rounds to the nearest number with digits decimal digits).

For instance:

**Note** If we call **help**("round"), we will read that its usage is like round(x, digits=0),

<sup>&</sup>lt;sup>5</sup> There are a couple of settings in place that control the default behaviour of the **print** function; see width, digits, max.print, OutDec, scipen, etc. in **help**("options").

which means that the digits parameter is equipped with the *default value* of 0. In other words, if rounding to 0 decimal digits is what we need, the second argument can be omitted.

```
round(x) # the same as round(x, 0)

## [1] 7 7 -4 -5 123 -765 0 2 2

round(x, 1)

## [1] 7.0 7.0 -4.3 -5.2 123.5 -765.4 0.5 1.5 2.5

round(x, -2)

## [1] 0 0 0 0 100 -800 0 0 0
```

### 2.3.3 Natural exponential function and logarithm

Moreover:

- exp(x) outputs the natural exponential function,  $e^x$ , where the Euler's number  $e \simeq 2.718$ ,
- log(x, base=exp(1)) computes, by default, the natural logarithm of x,  $log_e x$  (which is most often denoted simply as log x).

Recall that if  $x = e^y$ , then  $\log_e x = y$ , i.e., one is the inverse of the other.

```
log(c(0, 1, 2.7183, 7.3891, 20.0855)) # grows slowly
## [1] -Inf 0 1 2 3
exp(c(0, 1, 2, 3)) # grows fast
## [1] 1.0000 2.7183 7.3891 20.0855
```

**Note** These functions enjoy a number of very valuable identities and inequalities, including:

- $\log(x \cdot y) = \log x + \log y$ ,
- $\log(x^y) = y \log x$ ,
- $e^{x+y} = e^x \cdot e^y$ .

For more properties like these, take a glance at Chapter 4 of the freely available hand-book [47].

For the logarithm to a different base, say,  $\log_{10} x$ , we can call:

```
log(c(0, 1, 10, 100, 1000, 1e10), 10) # or log(..., base=10)
## [1] -Inf 0 1 2 3 10
```

Note that if  $\log_b x = y$ , then  $x = b^y$ , for any  $1 \neq b > 0$ .

**Note** Commonly, a logarithmic scale is used for variables that grow rapidly when expressed as functions of each other; see Figure 2.2.

```
x <- seq(0, 10, length.out=1001)
par(mfrow=c(1, 2)) # two plots in one figure (1 row, 2 columns)
plot(x, exp(x), type="l")
plot(x, exp(x), type="l", log="y") # log-scale on the y-axis</pre>
```

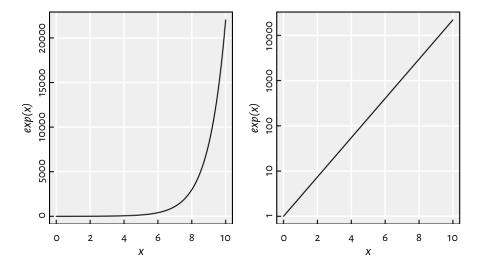


Figure 2.2: Linear- vs log-scale on the y-axis

Let us highlight that  $e^x$  on the log-scale is just a straight line. Also, keep in mind that such a transformation of the axes can only be applied in the case of values strictly greater than 0.

### 2.3.4 Probability distributions (\*)

It should come as no surprise that R offers extensive support for many univariate probability distribution families, including:

- continuous distributions, which take values being arbitrary real numbers (over the whole possible range or in some interval):
  - \*unif (uniform),
  - \*norm (normal),
  - \*exp (exponential),
  - \*gamma (gamma,  $\Gamma$ ),

- \*beta (beta, B),
- \*lnorm (log-normal),
- \*t (Student),
- \*cauchy (Cauchy-Lorentz),
- \*chisq (chi-squared,  $\chi^2$ ),
- \*f (Snedecor-Fisher),
- \*weibull (Weibull);

with the prefix "\*" being one of:

- "d" (probability density function, PDF),
- "p" (cumulative distribution function, CDF; or survival function, SF),
- "q" (quantile function, being the inverse of the CDF),
- "Γ" (generation of random deviates; already mentioned);
- discrete distributions, i.e., those whose possible outcomes can be easily enumerated (e.g., some integers).
  - \*binom (binomial),
  - \*geom (geometric),
  - \*pois (Poisson),
  - \*hyper (hypergeometric),
  - \*nbinom (negative binomial);

here, prefixes "p" and "r" have the same meaning as above, however:

- "d" now gives the probability mass function (PMF),
- "q" yields the quantile function, but one that is defined as a *generalised* inverse of the CDF.

Each distribution is characterised by a set of underlying parameters. For instance, a normal distribution  $N(\mu, \sigma)$  can be pinpointed by setting its expected value  $\mu \in \mathbb{R}$  and standard deviation  $\sigma > 0$ . In R, these two have been named mean and sd, respectively; see **help**("dnorm").

**Note** The parametrisations assumed in R can be subtly different from what we know from statistical textbooks or probability courses. For example, the normal distribution can be parameterised based on either standard deviation or variance, and the exponential distribution can be defined via its expected value or the reciprocal thereof. We thus advise the reader to study carefully the documentation of **help**("dnorm"), **help**("dunif"), **help**("dexp"), **help**("dbinom"), and the like.

It is also worth knowing the typical use cases of each of the distributions listed, e.g.,

a Poisson distribution can describe the probability of observing the number of independent events in a fixed time interval (e.g., the number of users downloading a copy of R from CRAN per hour), and an exponential distribution can model the time between such events; compare [22].

**Exercise 2.4** A call to **hist**(x) draws a histogram, which can serve as an estimator of the underlying continuous probability density function of a given sample; see Figure 2.3 for an illustration.

```
par(mfrow=c(1, 2)) # 2 plots in 1 figure
# Uniform U(0, 1)
hist(runif(10000, 0, 1), col="white", probability=TRUE, main="")
x <- seq(0, 1, length.out=101)
lines(x, dunif(x, 0, 1), lwd=2) # draw the true density function (PDF)
# Normal N(0, 1)
hist(rnorm(10000, 0, 1), col="white", probability=TRUE, main="")
x <- seq(-4, 4, length.out=101)
lines(x, dnorm(x, 0, 1), lwd=2) # draw the PDF</pre>
```

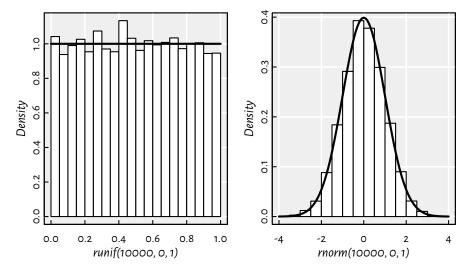


Figure 2.3: Example histograms of some pseudorandom samples and the true underlying probability density functions: the uniform distribution on the unit interval (left) and the standard normal distribution (right)

Draw a histogram of some random samples of different sizes n from the following distributions:

• rnorm(n,  $\mu$ ,  $\sigma$ ) – normal N( $\mu$ ,  $\sigma$ ) with expected values  $\mu \in \{-1, 0, 5\}$  (i.e.,  $\mu$  being equal to either -1, 0, or 5; read " $\in$ " as "belongs to the given set" or "in") and standard deviations  $\sigma \in \{0.5, 1, 5\}$ ;

- runif(n, a, b) uniform U(a, b) on the interval (a, b) with a = 0 and b = 1 as well as a = -1 and b = 1;
- rbeta(n, a,  $\beta$ ) beta B( $\alpha$ ,  $\beta$ ) with  $\alpha$ ,  $\beta \in \{0.5, 1, 2\}$ ;
- $rexp(n, \lambda)$  exponential  $E(\lambda)$  with rates  $\lambda \in \{0.5, 1, 10\}$ ;

Moreover, read about and play with the breaks, main, xlab, ylab, xlim, ylim, and colparameters; see **help**("hist").

**Example 2.5** We roll a six-sided dice twelve times. Let C be a random variable denoting the number of cases where the "1" face is thrown. C follows a binomial distribution Bin(n,p) with parameters n=12 (the number of Bernoulli trials) and p=1/6 (the probability of success in a single roll).

The probabilities that the number of "1"s rolled will be equal to 0, 1, ..., 4, i.e., P(C = 0), P(C = 1), ..., P(C = 4), respectively, can be computed based on the probability mass function (**dbinom**):

```
dbinom(0:4, 12, 1/6) # probability mass function at 5 different points ## [1] 0.112157 0.269176 0.296094 0.197396 0.088828
```

On the other hand, the probability that we throw more than three "1"s,  $P(C > 3) = 1 - P(C \le 3)$ , can be determined by means of the cumulative distribution function (**pbinom**) or survival function (**pbinom**(..., lower.tail=FALSE)):

```
1-pbinom(3, 12, 1/6) # pbinom(3, 12, 1/6, lower.tail=FALSE)
## [1] 0.12518
```

The smallest c such that  $P(C \le c) \ge 0.95$  can be computed based on the quantile function:

```
qbinom(0.5, 12, 1/6)
## [1] 2
pbinom(3:4, 12, 1/6) # for comparison: 0.95 is in-between
## [1] 0.87482 0.96365
```

In other words, at least 95% of the time, we will be observing no more than four successes.

Also, here are some pseudorandom realisations of C – the number of "1"s in 30 simulations of 12 independent dice rolls each:

```
rbinom(30, 12, 1/6)
## [1] 1 3 2 4 4 0 2 4 2 2 4 2 3 2 0 4 1 0 1 4 4 3 2 6 2 3 2 2 1 1
```

### 2.3.5 Special functions (\*)

Within mathematical formulae and across assorted application areas, certain functions appear more frequently than others. Hence, for the sake of notational brevity and computational precision, many of them have been assigned special names. For

instance, the following may be mentioned in the definitions related to some of the probability distributions listed above:

- gamma(x) for x>0 computes  $\Gamma(x)=\int_0^\infty t^{x-1}e^{-t}\,dt$  ,
- beta(a, b) for a,b>0 yields  $B(a,b)=rac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}=\int_0^1 t^{a-1}(1-t)^{b-1}\,dt$ .

Why do we have **beta** if it is merely a mix of **gammas**? A specific, tailored function is expected to be faster and more precise than its DIY version; its underlying implementation does not have to involve any calls to **gamma** at all.

```
beta(0.25, 250) # okay
## [1] 0.91213
gamma(0.25)*gamma(250)/gamma(250.25) # not okay
## [1] NaN
```

The  $\Gamma$  function grows so rapidly that already **gamma** (172) yields Inf. It is due to the fact that a computer's arithmetic is not infinitely precise; compare Section 3.2.3.

Special functions are plentiful; see the open-access [47] for one of the most definitive references (and also [2] for its predecessor). R package **gsl** [32] provides a vectorised interface to the GNU GSL [27] library, which implements many of such routines.

**Exercise 2.6** The Pochhammer symbol,  $(a)_x = \Gamma(a+x)/\Gamma(a)$ , can be computed via a call to gsl::poch(a, x) (i.e., the poch function from the gsl package; see Section 7.3.1):

```
# call install.packages("gsl") first
library("gsl") # load the package
poch(10, 3:6) # calls gsl_sf_poch() from GNU GSL
## [1] 1320 17160 240240 3603600
```

Read the documentation of the corresponding **gsl\_sf\_poch** function in the GNU GSL manual available here<sup>6</sup>.

And since you are there, do not hesitate to go through the list of all the other functions, including those related to statistics, permutations, combinations, and so forth.

Many functions also have their logarithm-of versions; see, e.g., lgamma and lbeta. Also, for instance, dnorm and dbeta have the log parameter. Its classical use case is the (numerical) maximum likelihood estimation, which involves the sums of the *logarithms* of densities.

<sup>6</sup> https://www.gnu.org/software/gsl/doc/html/

### 2.4 Arithmetic operations

### 2.4.1 Vectorised arithmetic operators

R features the following arithmetic operators:

- `+` (addition) and `-` (subtraction),
- `\*` (multiplication) and `/` (division),
- `%/%` (integer division) and `%%` (modulo, division remainder),
- `^` (exponentiation; synonym: `\*\*`).

They are all *vectorised*: they take two vectors on input and yield another vector in the result.

```
c(1, 2, 3) * c(10, 100, 1000)
## [1] 10 200 3000
```

The multiplication was performed in an *elementwise* fashion. The first element in the left vector was multiplied by the *corresponding* element in the right vector, and the result was stored in the first element of the output Then, the second element in the left... all right, we get the point.

Other operators are vectorised in the same manner:

```
0:10 + seq(0, 1, 0.1)

## [1] 0.0 1.1 2.2 3.3 4.4 5.5 6.6 7.7 8.8 9.9 11.0

0:7 / rep(3, length.out=8) # division by 3

## [1] 0.00000 0.33333 0.66667 1.00000 1.33333 1.66667 2.00000 2.33333

0:7 %/% rep(3, length.out=8) # integer division

## [1] 0 0 0 1 1 1 2 2

0:7 %% rep(3, length.out=8) # division remainder

## [1] 0 1 2 0 1 2 0 1
```

Operations involving missing values also yield NAs:

```
c(1, NA_real_, 3, NA_real_) + c(NA_real_, 2, 3, NA_real_)
## [1] NA NA 6 NA
```

### 2.4.2 Recycling rule

Some of the above statements can be written more concisely. When the operands are of different lengths, the shorter one is recycled (think: rep(y, length.out=length(x))) as many times as necessary.

```
0:7 / 3

## [1] 0.00000 0.33333 0.66667 1.00000 1.33333 1.66667 2.00000 2.33333

1:10 * c(-1, 1)

## [1] -1 2 -3 4 -5 6 -7 8 -9 10

2 ^ (0:10)

## [1] 1 2 4 8 16 32 64 128 256 512 1024
```

We call this the recycling rule.

If an operand cannot be recycled in its entirety, a warning $^{7}$  is generated, but the output is still available.

```
c(1, 10, 100) * 1:8
## Warning in c(1, 10, 100) * 1:8: longer object length is not a multiple of
## shorter object length
## [1] 1 20 300 4 50 600 7 80
```

**Note** Some functions are also deeply vectorised, i.e., with respect to multiple arguments. For example,

```
runif(3, c(10, 20, 30), c(11, 22, 33))
## [1] 10.288 21.577 31.227
```

generates three random numbers uniformly distributed over the intervals (10, 11), (20, 22), and (30, 33), respectively.

Also, **pmin** and **pmax** return the *parallel* minimum and maximum of the corresponding elements of the input vectors:

```
pmin(c(1, 2, 3, 4), c(4, 2, 3, 1))
## [1] 1 2 3 1
pmin(3, 1:5)
## [1] 1 2 3 3 3
pmax(0, pmin(1, c(0.25, -2, 5, -0.5, 0, 1.3, 0.99))) # clipping to [0, 1]
## [1] 0.25 0.00 1.00 0.00 0.00 1.00 0.99
```

**Note** Vectorisation and the recycling rule are perhaps most fruitful when applying binary operators on sequences of identical lengths or when performing vector-scalar (i.e., a sequence vs a single value) operations. However, there is much more: schemes like "every k-th element" appear in Taylor series expansions (multiply by  $\mathbf{c}(-1, 1)$ ),

<sup>&</sup>lt;sup>7</sup> A few built-in functions do not warn at all when incomplete recycling is performed (e.g., paste) or can even give an error (e.g., as.data.frame.list). Consider this inconsistency an annoying bug and hope it will be fixed, in the next decade or so.

k-fold cross-validation, etc.; see also Section 11.3.4 for use cases in matrix/tensor processing.

#### 2.4.3 Operator precedence

Apart from the seven binary arithmetic operators, other noteworthy, already mentioned ones include: the unary `-` (change of sign), `:` (sequence generation), and `<-` (assignment).

Expressions involving multiple operations need a set of rules governing the order of computations (unless we enforce it using round brackets). We have said that "-1:10" means "(-1):10" rather than "-(1:10)". But what about, say, "1+1+1+1+1\*0" or "3\*2^0:5+10"?

Let us list the aforementioned operators in their order of precedence, from the least to the most binding (see also help("Syntax")):

```
1. `<-` (right-to-left),
```

- 2. `+` and `-`,
- 3. `\*` and `/`,
- 4. `%%` and `%/%`,
- 5. `**:**`,
- 6. `+` and `-` (unary),
- 7. `^` (right-to-left).

Hence, " $-2^2/3+3*4$ " means "(( $-(2^2))/3$ )+(3\*4)" and not, for example,  $-((2^2/(2/3+3)))*4$ ).

Notice that `+` and `-`, `\*` and `/`, as well as `\%\` and `\/\%` have the same priority. Expressions involving a series of operations in the same group are evaluated left to right, with the exception of `^` and `<-`, which are performed from right to left.

#### Therefore:

- "2\*3/4\*5" is equivalent to "((2\*3)/4)\*5",
- "2^3^4" is the same as "2^(3^4)" (which, mathematically, we would write as  $2^{3^4} = 2^{81}$ ),
- "x <- y <- 4\*3%8/2" binds both y and x with 6 and not x with the previous value of y.

And let us remember: when in doubt, we can always bracket a subexpression to ensure it is executed in the intended order (which can also increase the readability of the code).

### 2.4.4 Accumulating

The `+` and `\*` operators, as well as the pmin and pmax functions, implement element-wise operations that are applied on the corresponding elements taken from two given vectors:

$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{pmatrix} + \begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_n \end{pmatrix} = \begin{pmatrix} x_1 + y_1 \\ x_2 + y_2 \\ x_3 + y_3 \\ \vdots \\ x_n + y_n \end{pmatrix}.$$

However, we can also scan through all the values in a *single* vector and combine the successive elements that we inspect using the corresponding operation:

- cumsum(x) gives the cumulative sum of the elements in a vector,
- **cumprod**(x) computes the cumulative product,
- **cummin**(x) yields the cumulative minimum,
- **cummax**(x) generates the cumulative maximum.

The i-th element in the output vector will consist of the sum/product/min/max of the first i inputs:

cumsum 
$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} x_1 \\ x_1 + x_2 \\ x_1 + x_2 + x_3 \\ \vdots \\ x_1 + x_2 + x_3 + \dots + x_n \end{pmatrix}.$$

For example:

```
cumsum(1:8)
## [1] 1 3 6 10 15 21 28 36
cumprod(1:8)
## [1] 1 2 6 24 120 720 5040 40320
cummin(c(3, 2, 4, 5, 1, 6, 0))
## [1] 3 2 2 2 1 1 0
cummax(c(3, 2, 4, 5, 1, 6, 0))
## [1] 3 3 4 5 5 6 6
```

If we are interested only in the last cumulant, summarising all the inputs, we have the following functions at our disposal:

- sum(x) computes the sum of elements in a vector,  $\sum_{i=1}^{n} x_i = x_1 + x_2 + \dots + x_n$ ,
- **prod**(x) outputs the product of all elements,  $\prod_{i=1}^n x_i = x_1 x_2 \cdots x_n$ ,
- min(x) computes the minimum,
- max(x) reckons the greatest value.

For example:

```
sum(1:8)
## [1] 36
prod(1:8)
## [1] 40320
min(c(3, 2, 4, 5, 1, 6, 0))
## [1] 0
max(c(3, 2, 4, 5, 1, 6, 0))
## [1] 6
```

**Note** Chapter 7 will discuss the **Reduce** function, which generalises the above by allowing any binary operation to be propagated over a given vector.

**Example 2.7** diff can be considered an inverse to cumsum: it computes the iterated difference. Namely, it subtracts the first two elements, then the second from the third one, the third from the fourth, and so on. In other words, diff(x) gives y such that  $y_i = x_{i+1} - x_i$ .

```
x <- c(-2, 3, 6, 2, 15)
diff(x)
## [1] 5 3 -4 13
cumsum(diff(x))
## [1] 5 8 4 17
cumsum(c(-2, diff(x))) # recreates x
## [1] -2 3 6 2 15</pre>
```

Thanks to **diff**, we can compute the daily changes to the EUR/AUD forex rates; see Figure 2.4.

## 2.4.5 Aggregating

The above functions form the basis for some popular summary statistics<sup>8</sup> (sample aggregates), such as:

- mean(x) gives the arithmetic mean, sum(x)/length(x),
- var(x) yields the (unbiased) sample variance,  $sum((x-mean(x))^2)/(length(x)-1)$ ,
- **sd**(x) is the standard deviation, **sqrt**(**var**(x)),

<sup>&</sup>lt;sup>8</sup> Actually, **var** and **median**, amongst others, are defined by the **stats** package, but this one is automatically loaded by default, so let us not make a fuss about it now.

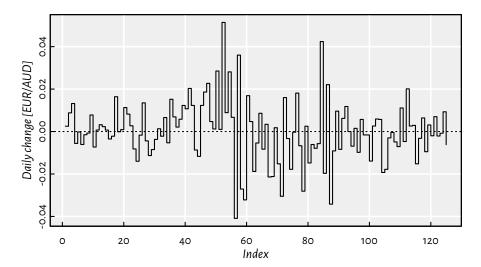


Figure 2.4: Iterated differences of the exchange rates (non-missing values only)

median(x) computes the sample median, i.e., the middle value in the sorted version of x.

For instance9:

```
x <- runif(1000)
c(min(x), mean(x), median(x), max(x), sd(x))
## [1] 0.00046535 0.49727780 0.48995025 0.99940453 0.28748391</pre>
```

**Exercise 2.8** Let x be any vector of length n with positive elements. Compute its geometric and harmonic mean, which are given by, respectively,

$$\sqrt[n]{\prod_{i=1}^{n} x_i} = e^{\frac{1}{n} \sum_{i=1}^{n} \log x_i} \quad and \quad \frac{n}{\sum_{i=1}^{n} \frac{1}{x_i}}.$$

When solving exercises like this one, it does not matter on what data you apply these functions (see, however, Section 9.3.4 for discussion). We are being abstract in the sense that the  $\mathbf{x}$  vector can be anything: from the one that features very accurate financial predictions that will help minimise inequality and make this world less miserable, through the data you have been collecting for the last ten years in relation to your definitely-super-important PhD research, whatever your company asked you to crunch today, to something related to the hobby project that you enjoy doing after hours. Therefore, just test the above on something like " $\mathbf{x} < -\mathbf{runif}(10)$ ", and move on.

All the aforementioned functions return a missing value if any of the input elements is

<sup>&</sup>lt;sup>9</sup> min, median, and max are special cases of quantile, which we will discuss much further (Section 4.4.3). It is because it returns a named vector.

unavailable. Luckily, they are equipped with the na.rm parameter, on behalf of which we can request the removal of NAs.

**Note** In the documentation, we read that the usage of some of the aforementioned functions is like sum(..., na.rm=FALSE). prod, min, and max are defined similarly. They accept any number of input vectors: each of them can be of arbitrary length. Therefore, min(1, 2, 3), min(c(1, 2, 3)) as well as min(c(1, 2), 3) all return the same result.

However, we can also read that we have **mean**(x, trim=0, na.rm=FALSE, ...). This time, only one vector can be aggregated, and any further arguments (except trim and na.rm) are ignored.

The extra flexibility (which we do not have to rely upon, ever) of the former group is due to their being associative operations: it holds, e.g., (2+3)+4=2+(3+4). Hence, the operations can be performed in any order, in any group. Also, note that they are more primitive operations: it is **mean** that is based on **sum**, not vice versa.

#### 2.5 Exercises

**Exercise 2.9** *Answer the following questions:* 

- What is the meaning of the dot-dot-dot parameter in the definition of the c function?
- We say that the **round** function is vectorised; what does that mean?
- What is wrong with a call to c(sqrt(1), sqrt(2), sqrt(3))?
- What do we mean by saying that multiplication operates element-by-element?
- How does the recycling rule work when applying `+`?
- How to (and why) set the seed of the pseudorandom number generator?
- What is the difference between NA\_real\_ and NaN?
- How are default arguments specified in the manual of, e.g., the **round** function?
- Is a call to rep(times=4, x=1:5)" equivalent to rep(4, 1:5)?
- List a few ways to generate a sequence like (-1, -0.75, -0.5, ..., 0.75, 1).

- Is "-3:5" the same as "-(3:5)"? What about the precedence of operators in expressions such as "2^3/4\*5^6", "5\*6+4/17%%8", and "1+-2^3:4-1"?
- If x is a numeric vector of length n (for some  $n \ge 0$ ), how many values will **sample**(x) output?
- Does **scan** support reading directly from compressed archives, e.g., .csv.gz files?

When in doubt, refer back to the material discussed in this chapter and/or the R manual.

**Exercise 2.10** The following code generates an example graph of arcsine and arccosine, whose preparation – thanks to vectorisation – is quite straightforward.

```
x <- seq(-1, 1, length.out=11) # increase length.out for a smoother curve
plot(x, asin(x),  # asin() computed for 11 points
    type="l",  # lines
    ylim=c(-pi/2, pi),  # y axis limits like c(y_min, y_max)
    ylab="asin(x), acos(x)") # y axis label
lines(x, acos(x), col="red", lty="dashed") # adds to the current plot
legend("topright", c("asin(x)", "acos(x)"),
    lty=c("solid", "dashed"), col=c("black", "red"), bg="white")</pre>
```

Inspired by the above, plot the following functions:  $|\sin x^2|$ ,  $|\sin |x|$ ,  $|\sin |x|$ , and  $1/(1 + e^{-x})$ . Recall that the documentation of **plot** can be viewed by calling **help**("plot.default").

**Exercise 2.11** It can be shown that:

$$4\sum_{i=1}^{n} \frac{(-1)^{i+1}}{2i-1} = 4\left(\frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \cdots\right)$$

slowly converges to  $\pi$  as n approaches  $\infty$ . Compute the above for n=1,000,000 and n=1,000,000,000 using the vectorised functions and operators discussed in this chapter, making use of the recycling rule as much as possible.

**Exercise 2.12** *Let* x *and* y *be two vectors of identical lengths* n, *say:* 

```
x <- rnorm(100)
y <- 2*x+10+rnorm(100, 0, 0.5)
```

Compute the Pearson linear correlation coefficient given by:

$$r = \frac{\sum_{i=1}^{n} \left( x_i - \frac{1}{n} \sum_{j=1}^{n} x_j \right) \left( y_i - \frac{1}{n} \sum_{j=1}^{n} y_j \right)}{\sqrt{\sum_{i=1}^{n} \left( x_i - \frac{1}{n} \sum_{j=1}^{n} x_j \right)^2} \sqrt{\sum_{i=1}^{n} \left( y_i - \frac{1}{n} \sum_{j=1}^{n} y_j \right)^2}}.$$

To make sure you have come up with a correct implementation, compare your result to a call to the built-in cor(x, y).

**Exercise 2.13** (\*) Find an R package providing a function to compute moving (rolling) averages and medians of a given vector. Apply them on the EUR/AUD currency exchange data. Draw thus obtained smoothened versions of the time series.

**Exercise 2.14** (\*\*) Compute the k-moving average using a call to convolve(..., type="filter"). In the next chapter, we will study operations that involve logical values.

# Logical vectors

### 3.1 Creating logical vectors

R defines three(!) logical constants: TRUE, FALSE, and NA, which represent "yes", "no", and "???", respectively. Each of them, when instantiated, is an atomic vector of length one.

Some of the functions we introduced in the previous chapter can be used to generate logical vectors as well:

```
c(TRUE, FALSE, FALSE, NA, TRUE, FALSE)
## [1] TRUE FALSE FALSE NA TRUE FALSE
rep(c(TRUE, FALSE, NA), each=2)
## [1] TRUE TRUE FALSE FALSE NA NA
sample(c(TRUE, FALSE), 10, replace=TRUE, prob=c(0.8, 0.2))
## [1] TRUE TRUE TRUE FALSE FALSE TRUE TRUE FALSE TRUE TRUE
```

**Note** By default, "T" is a synonym for TRUE and "F" stands for FALSE. However, these are not reserved keywords and can be reassigned to any other values. Therefore, we advise against relying on them: they are not used throughout the course of this course.

Also, notice that the logical missing value is spelled simply as "NA" and not "NA\_logical\_". Both the logical "NA" and the numeric "NA\_real\_" are, for the sake of our mental well-being, both *printed* as "NA" on the R console. This, however, does not mean they are identical; see Section 4.1 for discussion.

### 3.2 Comparing elements

## 3.2.1 Vectorised relational operators

Logical vectors frequently come into being as a result of various testing activities.

In particular, the binary operators:

• `<` (less than),

- - `<=` (less than or equal),
  - `>` (greater than),
  - `>=` (greater than or equal)
  - `==` (equal),
  - `!=` (not equal),

compare the corresponding elements of two numeric vectors and output a logical vector.

```
1 < 3
## [1] TRUE
c(1, 2, 3, 4) == c(2, 2, 3, 8)
## [1] FALSE TRUE TRUE FALSE
1:10 <= 10:1
## [1] TRUE TRUE TRUE TRUE FALSE FALSE FALSE FALSE
```

Thus, they operate in an elementwise manner. Moreover, the recycling rule is applied if necessary:

```
3 < 1:5 \# c(3, 3, 3, 3, 3) < c(1, 2, 3, 4, 5)
## [1] FALSE FALSE FALSE TRUE TRUE
c(1, 4) == 1:4 \# c(1, 4, 1, 4) == c(1, 2, 3, 4)
## [1] TRUE FALSE FALSE TRUE
```

Therefore, we can say that they are vectorised in the same manner as the arithmetic operators `+`, `\*`, etc.; compare Section 2.4.1.

#### Testing for NA, NaN, and Inf 3.2.2

Comparisons against missing values and not-numbers yield NAs. Therefore, instead of the incorrect  $x == NA_reals_or x == NaN$ , testing for missingness should rather be performed via a call to the vectorised is.na function.

```
is.na(c(NA_real_, Inf, -Inf, NaN, -1, 0, 1))
## [1] TRUE FALSE FALSE TRUE FALSE FALSE
is.nan(c(NA_real_, Inf, -Inf, NaN, -1, 0, 1))
## [1] FALSE FALSE TRUE FALSE FALSE
is.na(c(TRUE, FALSE, NA, TRUE)) # works for logical vectors, too
## [1] FALSE FALSE TRUE FALSE
```

Moreover, is.finite is noteworthy because it returns FALSE on Infs, NA\_real\_s and NaNs.

```
is.finite(c(NA_real_, Inf, -Inf, NaN, -1, 0, 1))
## [1] FALSE FALSE FALSE TRUE TRUE TRUE
```

See also the more specific is.nan and is.infinite.

### 3.2.3 Dealing with round-off errors (\*)

In mathematics, real numbers are merely an idealisation. In practice, however, it is impossible to store them with infinite precision (think  $\pi=3.1415926535897932384626433...$ ) computer memory is limited, and our time is precious.

Therefore, a widely agreed-upon consensus had to be reached. In R, we rely on the so-called *double-precision floating point format*. The *floating point* means that the numbers can be both small (close to zero) and large:  $\pm 2.23 \times 10^{-308}$  and  $\pm 1.79 \times 10^{308}$  are both acceptable.

#### Note

These two are quite distant from each other.

Every numeric value takes 8 bytes (or, equivalently, 64 bits) of memory. We are, however, able to store only *about* 15-17 decimal digits:

```
print(0.1234567890123456789012345678901234, digits=22) # 22 is max
## [1] 0.1234567890123456773699
```

which limits the precision of our computations. The *about* part is – unfortunately – due to the numbers' being written in the computer-friendly *binary*, not the human-aligned *decimal* base. This can lead to some unexpected outcomes.

#### In particular:

• 0.1 cannot be represented exactly because it cannot be written as a finite series of reciprocals of powers of 2 (it holds  $0.1 = 2^{-4} + 2^{-5} + 2^{-8} + 2^{-9} + ...$ ). This leads to surprising results such as:

```
0.1 + 0.1 + 0.1 == 0.3
## [1] FALSE
```

Despite the fact that what follows does not *show* anything suspicious:

```
c(0.1, 0.1 + 0.1 + 0.1, 0.3)
## [1] 0.1 0.3 0.3
```

Printing involves rounding. In the above context, it is misleading. Actually, we experience something more like:

```
print(c(0.1, 0.1 + 0.1 + 0.1, 0.3), digits=22)
## [1] 0.1000000000000055511 0.30000000000000444089
## [3] 0.29999999999999888978
```

• All integers between  $-2^{53}$  and  $2^{53}$  all stored exactly: this is good news. However, the next integer is beyond the representable range:

```
2^53 + 1 == 2^53
## [1] TRUE
```

• The above suggests that, more generally, the order of operations may matter. In particular, the associativity property may be violated when dealing with numbers of different orders of magnitude:

```
2^53 + 2^-53 - 2^53 - 2^-53 # should be == 0.0
## [1] -1.1102e-16
```

• Some numbers may just be just too large, too small, or too close to zero to be represented exactly:

**Important** The double-precision floating point format (IEEE 754) is not specific to R. It is used by most other computing environments, including Python and C++.

For discussion, see [31, 34, 39] ([30] can be of particular interest to the general statistical/data analysis audience).

Can we do anything about these issues?

First, when dealing with integers of a *reasonable* order of magnitude (a frequent case where we are dealing various resource or case IDs in our datasets), rest assured that we are safe: their comparison, addition, subtraction, and multiplication are always precise.

In all other cases (including applying other operations on integers, e.g., division or

**sqrt**), we need to be very careful with comparisons, especially involving testing for equality, `==`.

The sole fact that  $\sin \pi = 0$ , mathematically speaking, does not mean that we should expect that:

```
sin(pi) == 0
## [1] FALSE
```

Instead, they are so close to each other that we can *treat the difference between them as negligible*. Thus, in practice, instead of testing if x = y, we will be considering:

- |x y| (absolute error) or
- $\frac{|x-y|}{|y|}$  (relative error; which takes the order of magnitude of the numbers into account but obviously cannot be applied if y is very close to 0),

and determining if these are less than some assumed error margin,  $\varepsilon>0$ , say,  $10^{-8}$  or  $2^{-26}$ .

For example:

```
abs(sin(pi) - 0) < 2^-26
## [1] TRUE
```

**Note** Rounding can sometimes have a similar effect as testing for almost equality in terms of the absolute error.

```
round(sin(pi), 8) == 0
## [1] TRUE
```

**Important** Our recommendations are valid for the most popular applications of R, i.e., statistical and, more generally, scientific computing<sup>1</sup>. The datasets we handle on a daily basis do not represent accurate measurements themselves. Bah, the World itself is far from ideal! Therefore, we do not have to lose sleep over our not being able to precisely pinpoint the *exact* solution.

<sup>&</sup>lt;sup>1</sup> However, in financial applications, we had rather rely on base-10 numbers (compare the problem with 0.1 above). There are some libraries implementing higher precision floating-point numbers or even interval arithmetic that keeps track of error propagation operation chains.

### 3.3 Logical operations

#### 3.3.1 Vectorised logical operators

The relational operators such as `==` and `>` accept only *two* arguments. Their chaining is forbidden. A test that we would mathematically write as  $0 \le x \le 1$  (or  $x \in [0,1]$ ) cannot be expressed as "0<=x<=1" in R.

Therefore, we need a way to combine two logical conditions so as to be able to state that " $x \ge 0$  and, at the same time,  $x \le 1$ ".

In such situations, the following logical operators and functions come in handy:

- `!` (not, negation; unary),
- `&` (and, conjunction; are both predicates true?),
- `|` (or, alternation; is at least one true?),
- **xor** (exclusive-or, exclusive disjunction, either-or; is one and only one of the predicates true?).

They again act elementwisely and implement the recycling rule if necessary (and applicable).

```
x <- c(-10, -1, -0.25, 0, 0.5, 1, 5, 100)
(x >= 0) & (x <= 1)
## [1] FALSE FALSE FALSE TRUE TRUE TRUE FALSE FALSE
(x < 0) | (x > 1)
## [1] TRUE TRUE TRUE FALSE FALSE TRUE TRUE
!((x < 0) | (x > 1))
## [1] FALSE FALSE FALSE TRUE TRUE FALSE FALSE
xor(x >= -1, x <= 1)
## [1] TRUE FALSE FALSE FALSE FALSE FALSE TRUE TRUE</pre>
```

**Important** The vectorised `&` and `|` operators should not be confused with their scalar, short-circuit counterparts, `&&` and `||`; see Section 8.1.4.

### 3.3.2 Operator precedence revisited

The operators introduced in this chapter have lower precedence than the arithmetic ones. In particular, the binary `+` and `-`. Calling help("Syntax") reveals that we can extend our listing from Section 2.4.3 as follows:

```
1. `<-` (right-to-left; least binding),
```

```
2. `|`,
```

```
    3. `&`,
    4. `!` (unary),
    5. `<`,`>`,`<=`,`>=`,`==`, and `!=`,
    6. `+` and `-`,
    7. `*` and `/`,
    8. ...
```

### 3.3.3 Dealing with missingness

Operations involving missing values follow the principles of the Łukasiewicz's three-valued logic, which is based on common sense. For instance, "NA | TRUE" is TRUE because or needs at least one argument to be TRUE to generate such a result. On the other hand, "NA | FALSE" is NA, because the result would be different depending on what we substituted NA for.

Let us take a moment to contemplate the operations' *truth tables* for all the possible combinations of inputs:

```
u <- c(TRUE, FALSE, NA, TRUE, FALSE, NA, TRUE, FALSE, NA)
v <- c(TRUE, TRUE, TRUE, FALSE, FALSE, NA,
                                                    NA)
## [1] FALSE TRUE NA FALSE TRUE NA FALSE TRUE
                                                    NA
u & v
## [1] TRUE FALSE NA FALSE FALSE NA FALSE
                                                    NA
u | v
## [1] TRUE TRUE TRUE TRUE FALSE
                                   NA TRUE
                                              NA
                                                    NA
xor(u, v)
## [1] FALSE TRUE
                   NA TRUE FALSE
                                              NA
                                   NA
                                         NA
                                                    NA
```

## 3.3.4 Aggregating with all, any, and sum

Just like in the case of numeric vectors, we can summarise the contents of logical sequences.

**all** tests whether every element in a logical vector is equal to TRUE. **any** determines if there exists an element that is TRUE.

```
x <- runif(10000)
all(x <= 0.2)  # are all values in x <= 0.2?
## [1] FALSE
any(x <= 0.2)  # is there at least one element in x that is <= 0.2?
## [1] TRUE</pre>
```

the latter, as we have said above, is itself vectorised: it does *not* test whether a vector *as a whole* is equal to another one.

```
z <- c(1, 2, 3)
z == 1:3  # elementwise equal
## [1] TRUE TRUE TRUE
all(z == 1:3)  # elementwise equal summarised
## [1] TRUE</pre>
```

However, let us keep in mind the warning about the testing for *exact* equality of floating-point numbers stated in Section 3.2.3. Sometimes, considering absolute or relative errors might be more appropriate.

```
z <- sin((0:10)*pi) # sin(0), sin(pi), sin(2*pi), ..., sin(10*pi)
all(z == 0.0) # danger zone! please don't...
## [1] FALSE
all(abs(z - 0.0) < 1e-9) # are the absolute errors negligible?
## [1] TRUE</pre>
```

We can also call **sum** on a logical vector. Taking into account that it interprets TRUE as numeric 1 and FALSE as 0 (more on this in Section 4.1), it will give us the number of elements equal to TRUE.

```
sum(x \le 0.2) # how many elements in x are \le 0.2?
## [1] 1998
```

Also, by computing sum(x)/length(x), we can obtain the proportion (fraction) of values equal to TRUE in x. Equivalently:

```
mean(x <= 0.2) # proportion of elements <= 0.2
## [1] 0.1998
```

Naturally, we *expect*  $mean(runif(n) \le 0.2)$ " to be equal to 0.2 (20%), but with randomness, we can never be sure.

### 3.3.5 Simplifying predicates

Each aspiring programmer needs to become fluent with the rules governing the transformations of logical conditions, for example, that the negation of "(x >= 0) & (x < 1)" is equivalent to " $(x < 0) \mid (x >= 1)$ ".

Each such rule is called a *tautology*. Here are some of them:

- !(!p) is equivalent to p (double negation),
- !(p & q) holds if and only if !p | !q (De Morgan's law),
- !(p | q) is !p & !q (another De Morgan's law),

• all(p) is equivalent to !any(!p).

Various combinations thereof are, of course, possible. Some further simplifications are enabled by other properties of the binary operations:

- commutativity (symmetry), e.g., a + b = b + a, a \* b = b \* a,
- associativity, e.g., (a + b) + c = a + (b + c),  $\max(\max(a, b), c) = \max(a, \max(b, c))$ ,
- distributivity, e.g., a \* b + a \* c = a \* (b + c), min(max(a,b), max(a,c)) = max(a, min(b,c)),

and relations, including:

• transitivity, e.g., if  $a \le b$  and  $b \le c$  then surely  $a \le c$ .

**Exercise 3.1** Assuming that a, b, and c are numeric vectors, simplify the following expressions:

- !(b>a & b<c),
- !(a>=b & b>=c & a>=c),
- a>b & a<c | a<c & a>d,
- a>b | a<=b,</li>
- a<=b & a>c | a>b & a<=c,
- a<=b & (a>c | a>b) & a<=c,
- !all(a > b & b < c).

## 3.4 Choosing elements with ifelse

The **ifelse** function is a vectorised version of the scalar **if**...**else** conditional statement, which we will do without for as long as until Chapter 8.

It allows us to select an element from either one or another vector based on some logical condition.

A call to **ifelse**(l, t, f), where l is a logical vector, returns a vector y such that:

$$y_i = \begin{cases} t_i & \text{if } l_i \text{ is TRUE,} \\ f_i & \text{if } l_i \text{ is FALSE.} \end{cases}$$

In other words, the i-th element of the result vector is equal to  $t_i$  if  $l_i$  is TRUE and to  $f_i$  otherwise.

For example:

```
(z <- rnorm(6)) # example vector

## [1] -0.560476 -0.230177 1.558708 0.070508 0.129288 1.715065

ifelse(z >= 0, z, -z) # like abs(z)

## [1] 0.560476 0.230177 1.558708 0.070508 0.129288 1.715065
```

or:

```
(x <- rnorm(6)) # example vector
## [1] 0.46092 -1.26506 -0.68685 -0.44566 1.22408 0.35981
(y <- rnorm(6)) # example vector
## [1] 0.40077 0.11068 -0.55584 1.78691 0.49785 -1.96662
ifelse(x >= y, x, y) # like pmax(x, y)
## [1] 0.46092 0.11068 -0.55584 1.78691 1.22408 0.35981
```

By now, we should not be surprised that the recycling rule is fired up if necessary:

```
ifelse(x > 0, x^2, 0) # squares of positive xs and 0 otherwise
## [1] 0.21244 0.00000 0.00000 0.00000 1.49838 0.12947
```

**Note** All arguments are evaluated in their entirety before deciding on which elements are selected. Therefore, the following call will generate a warning:

```
ifelse(z >= 0, log(z), NA_real_)
## Warning in log(z): NaNs produced
## [1] NA NA 0.44386 -2.65202 -2.04571 0.53945
```

This is because, with log(z), we compute the logarithms of negative values anyway. To fix this, we can write:

```
log(ifelse(z >= 0, z, NA_real_))
## [1] NA NA 0.44386 -2.65202 -2.04571 0.53945
```

The calls to **ifelse** can naturally be nested in the case where we yearn for an **if...else if...else**-type expression.

**Example 3.2** A version of pmax(pmax(x, y), z) can be written as:

```
ifelse(x >= y,
    ifelse(z >= x, z, x),
    ifelse(z >= y, z, y)
)
## [1] 0.46092 0.11068 1.55871 1.78691 1.22408 1.71506
```

However, determining the three intermediate logical vectors is not necessary; we can save one call to `>=` by introducing an auxiliary variable:

```
xy <- ifelse(x >= y, x, y)
ifelse(z >= xy, z, xy)
## [1] 0.46092 0.11068 1.55871 1.78691 1.22408 1.71506
```

**Exercise 3.3** Figure 3.1 depicts a realisation of the mixture Z = 0.2X + 0.8Y of two normal distributions  $X \sim N(-2, 0.5)$  and  $Y \sim N(3, 1)$ .

```
n <- 100000
z <- ifelse(runif(n) <= 0.2, rnorm(n, -2, 0.5), rnorm(n, 3, 1))
hist(z, breaks=101, probability=TRUE, main="", col="white")</pre>
```

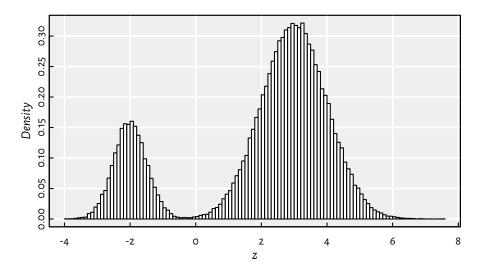


Figure 3.1: A mixture of two Gaussians generated with ifelse

In other words, we generated a variate from the normal distribution that has the expected value of -2 with probability 20%, and from the one with the expectation of 3 otherwise.

Inspired by the above, generate the following Gaussian mixtures:

```
• \frac{2}{3}X + \frac{1}{3}Y, where X \sim N(100, 16) and Y \sim N(116, 8),
```

• 
$$0.3X + 0.4Y + 0.3Z$$
, where  $X \sim N(-10, 2)$ ,  $Y \sim N(0, 2)$ , and  $Z \sim N(10, 2)$ .

(\*) On a side note, knowing that if X follows N(0,1), then the scaled-shifted  $\sigma X + \mu$  is distributed  $N(\mu, \sigma)$ , the above can be equivalently written as:

```
w <- (runif(n) <= 0.2)
z <- rnorm(n, 0, 1)*ifelse(w, 0.5, 1) + ifelse(w, -2, 3)</pre>
```

#### 3.5 Exercises

**Exercise 3.4** Answer the following questions:

- Why the statement "The Earth is flat or the smallpox vaccine is proven effective" is obviously true?
- What is the difference between NA and NA\_real\_?
- Why is "FALSE & NA" equal to FALSE, but "TRUE & NA" is NA?
- Why has "ifelse(x>=0, sqrt(x), NA\_real\_)" a tendency to generate warnings and how
  to rewrite it so as to prevent that from happening?
- What is the interpretation of "mean(x >= 0 & x <= 1)"?
- For some integer x and y, how to verify whether 0 < x < 100, 0 < y < 100, and x < y, all at the same time?
- Mathematically, for all real x, y > 0, it holds  $\log xy = \log x + \log y$ . Why then "all( $\log(x*y) = \log(x) + \log(y)$ )" can sometimes return FALSE? How to fix this?
- Is "x/y/z" always equal to "x/(y/z)"? How to fix this?
- What is the purpose of very specific functions such as log1p and expm1 (see their help page)
  and many others listed in, e.g., the GNU GSL library [27]? Is our referring to them a violation
  of the beloved "let us be minimalist" approach?
- If we know that x may be subject to error, how to test whether x > 0 in a robust manner?
- Is "y<-5" the same as "y <- 5" or rather "y < -5"?

**Exercise 3.5** What is the difference between **all** and **isTRUE**? What about `==`, **identical**, and **all.equal**? Is the last one properly vectorised?

**Exercise 3.6** Compute the cross-entropy loss between a numeric vector p with values in the interval (0,1) and a logical vector y, both of length n (you can generate them randomly or manually, it does not matter, it is just an exercise):

$$\mathcal{L}(\boldsymbol{p},\boldsymbol{y}) = \frac{1}{n} \sum_{i=1}^{n} \ell_i,$$

where

$$\ell_i = \left\{ \begin{array}{ll} -\log p_i & \text{if } y_i \text{ is TRUE ,} \\ -\log (1-p_i) & \text{if } y_i \text{ is FALSE .} \end{array} \right.$$

Interpretation: in classification problems,  $y_i \in \{FALSE, TRUE\}$  denotes the true class of the i-th object (say, whether the i-th hospital patient is symptomatic) and  $p_i \in (0,1)$  a machine learning algorithm's confidence that i belongs to class TRUE (e.g., how sure a decision tree model is that the corresponding person is unwell). Ideally, if  $y_i$  is TRUE,  $p_i$  should be close to 1 and to 0 otherwise. The cross-entropy loss quantifies by how much a classifier differs from the omniscient one. The use of the logarithm penalises strong beliefs in the wrong answer.

By the way, if we have solved any of the exercises encountered so far by referring to **if** statements, **for** loops, vector indexing like x[...], or any external R package, we recommend to go back and rewrite our code. Let us keep it simple (effective, readable) by using the *base* R's vectorised operations that we have introduced.

# Lists and attributes

After two brain-teasing chapters, it is time to cool it down a little. In this more technical part, we will introduce lists, which serve as universal containers for R objects of any size and type. Moreover, we will also show that each R object can be equipped with a number of optional attributes, thanks to which we will not only be able to label elements in any vector but also introduce new complex data types such as matrices and data frames later.

### 4.1 Type hierarchy and conversion

So far, we have been dealing with three types of atomic vectors:

- 1. logical (Chapter 3),
- 2. numeric (Chapter 2),
- 3. character (which we have barely touched upon yet, but rest assured that they will be covered in detail very soon; see Chapter 6).

To determine the type of an object programmatically, we can call the **typeof** function.

```
typeof(c(1, 2, 3))
## [1] "double"
typeof(c(TRUE, FALSE, TRUE, NA))
## [1] "logical"
typeof(c("spam", "spam", "bacon", "gluten-free spam"))
## [1] "character"
```

It turns out that we can easily convert between these types, either on our explicit demand (*type casting*) or on-the-fly (*coercion*, when we perform an operation that expects something different from the kind of input it was fed with).

**Note** (\*) Numeric vectors are reported as being either of the type double (double-precision floating-point numbers) or integer (32-bit; it is a subset of double); see Section 6.4.1. In most practical cases, this is a technical detail that we can safely ignore; compare also the **mode** function.

### 4.1.1 Explicit type casting

We can use functions such as as.logical, as.numeric, and as.character to coerce (convert) given objects to the corresponding types.

```
as.numeric(c(TRUE, FALSE, NA, TRUE, NA, FALSE))

## [1] 1 0 NA 1 NA 0

as.logical(c(-2, -1, 0, 1, 2, 3, NA_real_, -Inf, NaN))

## [1] TRUE TRUE FALSE TRUE TRUE TRUE NA TRUE NA
```

**Important** It is easily seen that the rules are:

- TRUE → 1,
- FALSE → O,
- NA → NA real ,

#### and:

- 0 → FALSE,
- NA\_real\_ and NaN → NA,
- anything else → TRUE.

The distinction between zero and non-zero is commonly applied in other programming languages as well.

Moreover, in the case of the conversion involving character strings, we have:

```
as.character(c(TRUE, FALSE, NA, TRUE, NA, FALSE))
## [1] "TRUE" "FALSE" NA "TRUE" NA
                                            "FALSE"
as.character(c(-2, -1, 0, 1, 2, 3, NA_real_, -Inf, NaN))
           "-1" "0"
                         "1"
                                "2" "3" NA "-Inf" "NaN"
## [1] "-2"
as.logical(c("TRUE", "True", "true", "T",
            "FALSE", "False", "false", "F",
            "anything other than these", NA_character_))
## [1] TRUE TRUE TRUE TRUE FALSE FALSE FALSE
as.numeric(c("0", "-1.23e4", "pi", "2+2", "NaN", "-Inf", NA_character_))
## Warning: NAs introduced by coercion
## [1]
           0 -12300
                       NA
                                   NaN
                                         -Inf
                                                  NA
```

### 4.1.2 Implicit conversion (coercion)

Recall that we referred to the three vector types as *atomic* ones: they can only be used to store elements of the *same type*.

If we make an attempt at composing an object of mixed types with c, the common type

will be determined in such a way that storing the data is done without information loss:

Hence, we see that logical is the most specialise of the tree, whereas character is the most general.

**Note** The logical NA is converted to NA\_real\_ and NA\_character\_ in the above examples. R users tend to rely on implicit type conversion when they write **c**(1, 2, NA, 4) instead of the more explicit **c**(1, 2, NA\_real\_, 4). In most cases, this is fine.

However, occasionally, it will be wiser to be more unequivocal. For instance, rep(NA\_real\_, 1e9) pre-allocates a long numeric vector instead of a logical one.

Some functions that expect vectors of specific types can apply coercion by themselves (or act as if they do so):

```
c(NA, FALSE, TRUE) + 10 # implicit conversion logical -> numeric
## [1] NA 10 11
c(-1, 0, 1) & TRUE # implicit conversion numeric -> logical
## [1] TRUE FALSE TRUE
sum(c(TRUE, TRUE, FALSE, TRUE, FALSE)) # same as sum(as.numeric(...))
## [1] 3
cumsum(c(TRUE, TRUE, FALSE, TRUE, FALSE))
## [1] 1 2 2 3 3
cummin(c(TRUE, TRUE, FALSE, TRUE, FALSE))
## [1] 1 1 0 0 0
```

**Exercise 4.1** In one of the previous exercises, we computed the cross-entropy loss between a logical vector  $\mathbf{y} \in \{0,1\}^n$  and a numeric vector  $\mathbf{p} \in (0,1)^n$ . This measure can be equivalently defined as:

$$\mathcal{L}(\boldsymbol{p}, \boldsymbol{y}) = -\frac{1}{n} \left( \sum_{i=1}^{n} y_i \log(p_i) + (1 - y_i) \log(1 - p_i) \right).$$

Implement the above formula (using vectorised operations, but not relying on **ifelse** this time) and compute the cross-entropy loss between, say, "y <- sample(c(FALSE, TRUE), n)" and "p <- runif(n)" for some n. Note how seamlessly we are translating between FALSE/TRUEs and O/1s in the above equation (in particular, where we let  $1 - y_i$  mean the logical negation of  $y_i$ ).

#### 4.2 Lists

Lists are generalised vectors. They can be comprised of R objects of any kind, also other lists. This is why we classify them as recursive (and not atomic) objects. They are especially useful wherever there is a need to handle some multitude as a single entity.

#### 4.2.1 Creating lists

The most straightforward way to create a list is by means of the **list** function:

```
list(1, 2, 3)
## [[1]]
## [1] 1
##
## [[2]]
## [1] 2
##
## [[3]]
## [1] 3
```

Notice that the above is not the same as "c(1, 2, 3)". We got a sequence that wraps three numeric vectors, each of length one. Also, how overly talkative R is when printing out lists!

```
list(c(1, 2, 3), 4, c(TRUE, FALSE, FALSE, NA, TRUE), "and so forth")
## [[1]]
## [1] 1 2 3
##
## [[2]]
## [1] 4
##
## [[3]]
## [1] TRUE FALSE FALSE NA TRUE
##
## [[4]]
## [1] "and so forth"
list(list(c(TRUE, FALSE, NA, TRUE), letters), runif(5)) # a list of lists
## [[1]]
## [[1]][[1]]
## [1] TRUE FALSE NA TRUE
##
## [[1]][[2]]
  [1] "a" "b" "c" "d" "e" "f" "g" "h" "i" "j" "k" "l" "m" "n" "o" "p" "a"
## [18] "r" "s" "t" "u" "v" "w" "x" "v" "z"
```

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```
##
##
[[2]]
## [1] 0.28758 0.78831 0.40898 0.88302 0.94047
```

However, the **str** function can be used to print R objects in a more concise fashion:

```
str(list(list(c(TRUE, FALSE, NA, TRUE), letters), runif(5)))
## List of 2
## $ :List of 2
## ..$ : logi [1:4] TRUE FALSE NA TRUE
## ..$ : chr [1:26] "a" "b" "c" "d" ...
## $ : num [1:5] 0.288 0.788 0.409 0.883 0.94
```

**Note** In Section 4.1, we said that the **c** function, when fed with arguments of mixed types, tries to determine the common type that retains the sense of data. If coercion to an atomic vector is not possible, the result will be a list.

```
c(1, "two", identity) # `identity` is an object of the type "function"
## [[1]]
## [1] 1
##
## [[2]]
## [1] "two"
##
## [[3]]
## function (x)
## x
## <environment: namespace:base>
```

Thus, the **c** function can also be used to concatenate lists:

```
c(list(1), list(2), list(3)) # 3 lists -> 1 list
## [[1]]
## [1] 1
##
## [[2]]
## [1] 2
##
## [[3]]
## [1] 3
```

Lists can be repeated using **rep**:

```
rep(list(1:11, LETTERS), 2)

## [[1]]

## [1] 1 2 3 4 5 6 7 8 9 10 11

##

## [[2]]

## [1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q"

## [18] "R" "S" "T" "U" "V" "W" "X" "Y" "Z"

##

## [[4]]

## [1] 1 2 3 4 5 6 7 8 9 10 11

##

## [[4]]

## [1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q"

## [18] "R" "S" "T" "U" "V" "W" "X" "Y" "Z"
```

### 4.2.2 Coercing to and from lists

The conversion of an atomic vector to a list of length-1 vectors can be done via a call to as.list:

```
as.list(c(1, 2, 3)) # vector of length 3 -> list of 3 length-1 vectors
## [[1]]
## [1] 1
##
## [[2]]
## [1] 2
##
## [[3]]
## [1] 3
```

Unfortunately, calling, say, **as.numeric** on a list will result in an error (even if it is comprised of numeric vectors only). We can try to flatten it to an atomic sequence by calling **unlist**:

```
unlist(list(1, 2), list(3, list(4:8)), 9))
## [1] 1 2 3 4 5 6 7 8 9
unlist(list(1, 2), list(3, list(4:8)), "spam"))
## [1] "1" "2" "3" "4" "5" "6" "7" "8" "spam"
```

**Note** (\*) Chapter 11 will mention the **simplify2array** function, which generalises **unlist** in a way that can sometimes result in a matrix.

#### 4.3 **NULL**

The NULL object (the one and only object of the type "NULL") can be used as a placeholder for any other R object or designate the absence of such.

```
list(NULL, NULL, month.name)
## [[1]]
## NULL
##
## [[2]]
## NULL
##
## [[3]]
## [1] "January"
                                            "April" "May"
                    "February"
                                "March"
## [6] "June"
                    "July"
                                "August"
                                            "September" "October"
## [11] "November" "December"
```

NULL is different from a vector of length zero because the latter has a type.

However, NULL sometimes *behaves* as a O-length vector. In particular, **length**(NULL) returns O. Also, **c** called with no arguments returns NULL.

Testing for NULL-ness can be done with a call to is.null.

**Important** NULL is not the same as NA (or it is other-typed variants). The latter can be emplaced in an atomic vector.

```
c(1, NA, 3, NULL, 5) # NULL behaves as a 0-length vector here
## [1] 1 NA 3 5
```

They both have very distinct semantics (no value vs a missing value).

Later we will see that some functions return NULL, invisibly, because they actually have nothing interesting to yield. This is the case of **print** or **plot**, which are called because of their side effects (printing and plotting).

Also, in some contexts, replacing content with NULL (e.g., when subsetting a list) will actually result in its removal.

# 4.4 Object attributes

Lists can be used to wrap many objects and form a single, ordered collection thereof.

Attributes, on the other hand, give means to inject some *extra* data into an object of any type (except NULL).

Attributes are (unordered) key=value pairs, where key is a single string, and value is any R object except NULL. They can be introduced by calling, amongst others<sup>1</sup>, the **structure** function:

```
x_simple <- 1:10
x <- structure(
    x_simple, # the object to be equipped with attributes
    attribute1="value1",
    attribute2=c(6, 100, 324)
)</pre>
```

#### 4.4.1 Developing perceptual indifference to most attributes

Let us see how the above x is reported on the console:

```
print(x)
## [1] 1 2 3 4 5 6 7 8 9 10
## attr(,"attribute1")
## [1] "value1"
## attr(,"attribute2")
## [1] 6 100 324
```

The object of concern, "1:10", was displayed first. We need to get used to that. Most of the time, we suggest to treat the "attr..." parts of the display as if they were printed in tiny font.

Equipping an object with attributes does not change its very nature (see, however, Chapter 10 for some exceptions). For example, the above x, despite featuring some extra data (metadata), is still treated as an ordinary sequence of numbers by most functions:

```
sum(x) # the same as sum(1:10), sum() does not care about any attributes
## [1] 55
typeof(x) # just a numeric vector, but with some perks
## [1] "integer"
```

**Important** Attributes are generally ignored by most functions unless they have specifically been programmed to pay attention to them.

<sup>&</sup>lt;sup>1</sup> Other ways include the replacement versions of the attr and attributes functions; see Section 9.4.6.

#### 4.4.2 But there are some use cases

Some R functions add attributes to the return value to sneak extra information that *might* be useful, just in case.

For instance, **na.omit**, whose main aim is to remove missing values from an atomic vector, yields:

```
y <- c(10, 20, NA, 40, 50, NA, 70)
(y_na_free <- na.omit(y))
## [1] 10 20 40 50 70
## attr(,"na.action")
## [1] 3 6
## attr(,"class")
## [1] "omit"</pre>
```

We can enjoy the NA-free version of y in any further computations:

```
mean(y_na_free)
## [1] 38
```

However, the na.action attribute (we ignore the class part until Chapter 10) tells us where the missing observations were:

```
attr(y_na_free, "na.action") # read the attribute value
## [1] 3 6
## attr(,"class")
## [1] "omit"
```

As another example, **gregexpr** can be used to search for a given pattern in a character vector (for more details, see Chapter 6):

```
needle <- "spam|gluten" # pattern to search for: spam OR gluten
haystack <- c("spam, spam, bacon, and gluten-free spam", "spammer") # text
(pos <- gregexpr(needle, haystack))</pre>
## [[1]]
## [1] 1 7 24 36
## attr(,"match.length")
## [1] 4 4 6 4
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
##
## [[2]]
## [1] 1
## attr(,"match.length")
## [1] 4
```

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```
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
```

We sought all occurrences of the pattern within two character strings. As their number may vary from string to string, wrapping the results in a list was a good design choice. Each list element gives the starting positions where matches can be found (there are four and one match(es), respectively).

Each vector of positions also features its own match.length attribute (amongst others), in case we need it.

**Exercise 4.2** Create a list with EUR/AUD, EUR/GBP, and EUR/USD exchange rates read from the euraud-\*.csv, eurgbp-\*.csv, and eurusd-\*.csv files in our data repository<sup>2</sup>. Each of its three elements should be a numeric vector storing the currency exchange rates. Furthermore, equip them with currency\_from, currency\_to, date\_from, and date\_to attributes, for example:

```
## [1] NA 1.6006 1.6031 NA NA 1.6119 1.6251 1.6195 1.6193 1.6132
## [11] NA NA 1.6117 1.6110 1.6188 1.6115 1.6122 NA
## attr(,"currency_from")
## [1] "EUR"
## attr(,"currency_to")
## [1] "AUD"
## attr(,"date_from")
## [1] "2020-01-01"
## attr(,"date_to")
## [1] "2020-06-30"
```

Such additional information could be stored in a few separate variables (other vectors), but then it would not be as convenient to use as the above representation.

# 4.4.3 Special attributes

Attributes have great potential which is somewhat wasted by R users due to their rarely knowing:

- that attributes exist (pessimistic scenario) or
- how to handle them (realistic scenario).

But we now know.

What is more, some attributes have been predestined to play a fundamental role in R. Namely, the most prevalent amongst the *special attributes* are:

<sup>&</sup>lt;sup>2</sup> https://github.com/gagolews/teaching-data/tree/master/marek

- names, row.names, and dimnames are used to label the elements of atomic and generic vectors (see below), and also rows and columns in matrices (Chapter 11) and data frames (Chapter 12),
- dim allows for turning flat vectors into matrices and other tensors (Chapter 11),
- levels labels the underlying integer codes in factor objects (Section 10.3.2),
- class can be used to bring forth new complex data structures based on basic types (Chapter 10).

#### We call them special because:

- they cannot be assigned arbitrary values; for instance, we will soon see that names
  can only be mapped to a character vector of the length equal to that of the sequence
  it is labelling,
- they can be accessed via designated functions, e.g., names, class, dim, dimnames, levels, etc.,
- they are widely recognised by many base and third-party R functions.

However, in spite of the above, special attributes can still be managed as any other (ordinary) ones.

**Exercise 4.3** comment is perhaps the most rarely used special attribute. Create an object (whatever) equipped with the comment attribute. Verify that assigning to it anything other than a character vector leads to an error. Read its value by calling the **comment** function. Display the object equipped with this attribute. Note that the **print** function ignores its existence whatsoever: this is how special it is.

**Important** (\*) The accessor functions such as names or class might return meaningful values, even if the corresponding attribute is not set explicitly; see, e.g., Section 11.1.5 for an example.

# 4.4.4 Labelling vector elements with the names attribute

A special attribute called names can be used to label the elements of atomic vectors and lists.

The labels may improve the expressivity and readability of our code and data.

**Exercise 4.4** Verify that the above x is still an ordinary numeric vector by calling **typeof** and **sum** on it.

Let us stress that we can ignore the names attribute whatsoever. If we apply any opera-

tion discussed in Chapter 2, we will still garner the same result no matter if such extra information is present or not.

It is just the **print** function that changed its behaviour slightly (it is a special attribute, after all). Instead of reporting:

```
## [1] 13 2 6
## attr(,"names")
## [1] "spam" "sausage" "celery"
```

we got a nicely formatted table-like display. Non-special attributes are still printed in a standard way.

```
## spam sausage celery
## 13 2 6
## attr(,"additional_attribute")
## [1] 1 2 3 4 5 6 7 8 9 10
```

**Note** Chapter 5 will also mention that some operations (such as indexing) can gain extra features in the presence of the names attribute.

This attribute can be read by calling:

```
attr(x, "names") # just like any other attribute
## [1] "spam" "sausage" "celery"
names(x) # because it is so special
## [1] "spam" "sausage" "celery"
```

Named vectors can be easily created with the c and list functions as well:

```
c(a=1, b=2)
## a b
## 1 2
list(a=1, b=2)
## $a
## [1] 1
##
## $b
## [1] 2
c(a=c(x=1, y=2), b=3, c=c(z=4)) # this is smart
## a.x a.y b c.z
## 1 2 3 4
```

Let us contemplate how a named list is printed on the console. Again, it is still a list, but with some extras.

**Exercise 4.5** A whole lot of functions return named vectors. Evaluate the following expressions and read the corresponding pages in the documentation:

- quantile(runif(100)),
- hist(runif(100), plot=FALSE),
- options (take note of the digits, scipen, max.print, and width options),
- capabilities.

**Note** (\*) Most of the time, lists are used merely as *containers* for other R objects. This is a boring yet essential role. However, let us just mention here that each data frame is, in fact, a generic vector (see Chapter 12). Each column corresponds to a named list element:

```
(df <- head(iris)) # some data frame</pre>
    Sepal.Length Sepal.Width Petal.Length Petal.Width Species
              5.1
## 1
                          3.5
                                       1.4
                                                   0.2 setosa
              4.9
## 2
                          3.0
                                       1.4
                                                   0.2 setosa
## 3
              4.7
                          3.2
                                       1.3
                                                   0.2 setosa
## 4
              4.6
                          3.1
                                       1.5
                                                   0.2 setosa
## 5
              5.0
                          3.6
                                       1.4
                                                   0.2 setosa
## 6
              5.4
                          3.9
                                       1.7
                                                   0.4 setosa
typeof(df) # it is just a list (with extras that'll be discussed later)
## [1] "list"
unclass(df) # how it is represented exactly (without the extras)
## $Sepal.Length
## [1] 5.1 4.9 4.7 4.6 5.0 5.4
##
## $Sepal.Width
## [1] 3.5 3.0 3.2 3.1 3.6 3.9
## $Petal.Length
## [1] 1.4 1.4 1.3 1.5 1.4 1.7
## $Petal.Width
## [1] 0.2 0.2 0.2 0.2 0.2 0.4
##
## $Species
## [1] setosa setosa setosa setosa setosa
## Levels: setosa versicolor virginica
## attr(,"row.names")
## [1] 1 2 3 4 5 6
```

Therefore, the functions we discuss in this chapter are of use in the processing of such structured data as well.

### 4.4.5 Altering and removing attributes

We know that a single attribute can be read by calling **attr**. Their whole list is generated with a call to **attributes**.

```
(x <- structure(c("some", "object"), names=c("X", "Y"),</pre>
    attribute1="value1", attribute2="value2", attribute3="value3"))
##
     "some" "object"
##
## attr(,"attribute1")
## [1] "value1"
## attr(, "attribute2")
## [1] "value2"
## attr(,"attribute3")
## [1] "value3"
attr(x, "attribute1") # reads a single attribute, returns NULL if unset
## [1] "value1"
attributes(x) # returns a named list with all attributes of an object
## $names
## [1] "X" "Y"
##
## $attribute1
## [1] "value1"
##
## $attribute2
## [1] "value2"
##
## $attribute3
## [1] "value3"
```

We can alter an attribute's value or add further attributes by referring to the **structure** function once again. Moreover, setting an attribute's value to NULL gets rid of it completely.

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```
## attr(,"attribute4")
## [1] "added"
```

As far as the names attribute is concerned, we may generate an un-named copy of an object by calling:

```
unname(x)
## [1] "some" "object"
## attr(,"attribute1")
## [1] "value1"
## attr(,"attribute2")
## [1] "value2"
## attr(,"attribute3")
## [1] "value3"
```

In Section 9.4.6, we will discuss the so-called *replacement functions*. They will enable us to modify or remove an object's attribute by calling "attr(x, "some\_attribute") <-new\_value".

Moreover, Section 5.5 highlights that certain operations (such as vector indexing, elementwise arithmetic operations, and coercion) might not preserve all attributes of the objects that were given as their inputs.

#### 4.5 Exercises

**Exercise 4.6** *Answer the following.* 

- That is the meaning of "c(TRUE, FALSE) \* 1:10"?
- What does "**sum(as.logical**(x))" compute when x is a numeric vector?
- We said that atomic vectors of the type character are the most general ones. Therefore, is
   "as.numeric(as.character(x))" the same as "as.numeric(x)", regardless of the type of
   x?
- What is the meaning of "as.logical(x+y)" if x and y are logical vectors? What about "as.logical(x\*y)", "as.logical(1-x)", and "as.logical(x!=y)"?
- Let x be a named numeric vector, e.g., "x <- quantile(runif(100))". What is the result of "2\*x", "mean(x)", and round(x, 2)?</li>
- What is the meaning of x == NULL?
- Give two ways to create a named character vector.
- Give two ways (discussed above; there are more) to remove the names attribute from an object.

**Exercise 4.7** There are a few peculiarities when joining or coercing lists. Compare the results generated by the following pairs of expressions:

```
# 1)
as.character(list(list(1, 2), list(3, list(4)), 5))
as.character(unlist(list(list(1, 2), list(3, list(4)), 5)))
# 2)
as.numeric(list(list(1, 2), list(3, list(4)), 5))
as.numeric(unlist(list(list(1, 2), list(3, list(4)), 5)))
# 3)
unlist(list(list(1, 2), sd))
list(1, 2, sd)
# 4)
c(list(c(1, 2), 3), 4, 5)
c(list(c(1, 2), 3), c(4, 5))
```

**Exercise 4.8** Given numeric vectors x, y, z, and w, how to combine x, y, and list(z, w) so as to obtain list(x, y, z, w)? More generally, given a set of atomic vectors and lists of atomic vectors, how to combine them to get a single list that features all atomic vectors as its elements (not a list of atomic vectors and lists, not atomic vectors unwound, etc.)?

**Exercise 4.9** What is the meaning of the following when x is a logical vector?

- cummin(x) and cummin(!x),
- cummax(x) and cummax(!x),
- cumsum(x) and cumsum(!x),
- cumprod(x) and cumprod(!x).

**Exercise 4.10** readRDS allows for serialising R objects and writing their snapshots to disk so that they can be later restored very quickly via a call to saveRDS. Verify whether this function preserves object attributes.

See also **dput** and **dget** which work with objects' textual representation in the form executable R code.

Exercise 4.11 (\*) Use jsonlite::fromJSON to read a JSON file in the form of a named list.

In the extremely unlikely event of us finding the current chapter boring, let us rejoice: some of the exercises and remarks that we will encounter in the next part – devoted to vector indexing – will definitely be deliciously stimulating!

# Vector indexing

We now know plenty of ways to process vectors in their entirety, but how to extract and replace their specific parts? We will be collectively referring to such activities as indexing. This is because they are often performed through the index operator, `[`.

#### 5.1 head and tail

Let us begin with something more lightweight, though. The **head** function can be used to fetch a few elements from the beginning of a vector.

```
x <- 1:10
head(x) # head(x, 6)
## [1] 1 2 3 4 5 6
head(x, 3) # get the first three
## [1] 1 2 3
head(x, -3) # skip the last three
## [1] 1 2 3 4 5 6 7</pre>
```

Similarly, tail extracts a few elements from the end of a sequence.

```
tail(x) # tail(x, 6)
## [1] 5 6 7 8 9 10
tail(x, 3) # get the last three
## [1] 8 9 10
tail(x, -3) # skip the first three
## [1] 4 5 6 7 8 9 10
```

Both functions work on lists, too<sup>1</sup>. They are useful, e.g., when we wish to preview the contents of a *big* object.

<sup>&</sup>lt;sup>1</sup> head and tail are actually S3 generics defined in the utils package. We will be able to call them on matrices and data frames as well; see Chapter 10.

### 5.2 Subsetting and extracting from vectors

Given a vector x, "x[i]" returns its subset comprised of elements indicated by the indexer i, which can be a *single* vector of:

- nonnegative integers (gives the positions of elements to retrieve),
- negative integers (gives the positions to omit),
- logical values (states whether the corresponding element should be fetched or skipped),
- character strings (locates the elements with specific names).

#### 5.2.1 Nonnegative indexes

Consider the following example vectors:

```
(x <- seq(10, 100, 10))
## [1] 10 20 30 40 50 60 70 80 90 100
(y <- list(1, 11:12, 21:23))
## [[1]]
## [1] 1
##
## [[2]]
## [1] 11 12
##
## [[3]]
## [1] 21 22 23</pre>
```

The first element in a vector is at index 1. Hence:

```
x[1]  # the first element
## [1] 10
x[length(x)]  # the last element
## [1] 100
```

**Important** We might have wondered why "[1]" is being displayed each time we print out an atomic vector on the console:

```
print((1:51)*10)
## [1] 10 20 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170
## [18] 180 190 200 210 220 230 240 250 260 270 280 290 300 310 320 330 340
## [35] 350 360 370 380 390 400 410 420 430 440 450 460 470 480 490 500 510
```

It is merely a visual hint indicating which vector element we output first in each line.

Vectorisation is a universal feature of R. It comes as no surprise that the indexer can also be of length greater than one.

```
x[c(1, length(x))] # the first and the last
## [1] 10 100
x[1:3] # the first three
## [1] 10 20 30
```

Take note of some boundary cases:

```
x[c(1, 2, 1, 0, 3, NA_real_, 1, 11)] # repeated, 0, missing, out of bound
## [1] 10 20 10 30 NA 10 NA
x[c()] # indexing by an empty vector
## numeric(0)
```

**Important** Subsetting with `[` yields an object of the same type.

When applied on lists, the index operator always returns a list as well, even if we ask for a single element:

```
y[2] # a list that includes the 2nd element
## [[1]]
## [1] 11 12
y[c(1, 3)] # not the same as x[1, 3] (a different story)
## [[1]]
## [1] 1
##
## [[2]]
## [1] 21 22 23
```

If we wish to *extract* a component, i.e., to dig into what is inside a list at a specific location, we can refer to `[[`:

```
y[[2]] # extract the 2nd element
## [1] 11 12
```

This is exactly why R displays "[[1]]", "[[2]]", etc. when printing out lists on the console.

Note Calling "x[[i]]" on an atomic vector, where i is a single value, has almost<sup>2</sup>

<sup>&</sup>lt;sup>2</sup> See also Section 5.5 for the discussion on the preservation of object attributes.

the same effect as "x[i]". However, `[[` generates an error if the subscript is out of bounds.

**Note** (\*) `[[` also supports multiple indexers.

```
y[[c(1, 3)]] ## Error in y[[c(1, 3)]]: subscript out of bounds
```

Its meaning is different from y[c(1, 3)], though; we are about to extract a single value, remember? Here, indexing is applied *recursively*. Namely, the above is equivalent to y[[1]][[3]] – we got an error because y[[1]] is of a length smaller than three.

More examples:

```
y[[c(3, 1)]] # y[[3]][[1]]
## [1] 21
list(list(7))[[c(1, 1)]] # 7, not list(7)
## [1] 7
```

**Important** Let us reflect on the operators' behaviour in the case of nonexistent items:

```
c(1, 2, 3)[4]

## [1] NA

list(1, 2, 3)[4]

## [[1]]

## NULL

c(1, 2, 3)[[4]]

## Error in c(1, 2, 3)[[4]]: subscript out of bounds

list(1, 2, 3)[[4]]

## Error in list(1, 2, 3)[[4]]: subscript out of bounds
```

### 5.2.2 Negative indexes

The indexer can also be a vector of negative integers. This way, we can *exclude* the elements at given positions:

```
y[-1] # all but the first
## [[1]]
## [1] 11 12
##
## [[2]]
## [1] 21 22 23
```

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```
x[-(1:3)]

## [1] 40 50 60 70 80 90 100

x[-c(1, 0, 2, 1, 1, 8:100)] # 0, repeated, out of bound indexes

## [1] 30 40 50 60 70
```

**Note** Negative and positive indexes cannot be mixed.

```
x[-1:3] # recall that -1:3 == (-1):3
## Error in x[-1:3]: only 0's may be mixed with negative subscripts
```

Also, NA indexes are not allowed amongst negative ones.

### 5.2.3 Logical indexer

A vector can also be subsetted by means of a logical vector. If they both are of identical lengths, the consecutive elements in the latter indicate whether the corresponding elements of the indexed vector are supposed to be selected (TRUE) or omitted (FALSE).

```
# 1*** 2 3 4 5*** 6*** 7 8*** 9? 10***

X[c(TRUE, FALSE, FALSE, TRUE, TRUE, FALSE, TRUE, NA, TRUE)]

## [1] 10 50 60 80 NA 100
```

In other words, x[l], where l is a logical vector, returns all x[i] with i such that l[i] is TRUE. Above, we extracted the elements at indexes 1, 5, 6, 8, and 10.

**Important** Let us be careful: if the element selector is NA, the selected element will be set to a missing value (for atomic vectors) or NULL (for lists).

```
c("one", "two", "three")[c(NA, TRUE, FALSE)]
## [1] NA    "two"
list("one", "two", "three")[c(NA, TRUE, FALSE)]
## [[1]]
## NULL
##
## [[2]]
## [1] "two"
```

This, lamentably, comes with no warning, which might be problematic when indexers are generated programmatically.

As a remedy, we sometimes pass the logical indexer to the **which** function first. It returns the indexes of the elements equal to TRUE, ignoring the missing ones.

```
which(c(NA, TRUE, FALSE))
## [1] 2
c("one", "two", "three")[which(c(NA, TRUE, FALSE))]
## [1] "two"
```

Recall that in Chapter 3, we discussed ample vectorised operations that generate logical vectors. Anything that yields a logical vector of the same length as x can be passed as an indexer.

```
x > 60  # yes, it is a perfect indexer candidate
## [1] FALSE FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE
x[x > 60]  # select elements in x that are greater than 60
## [1] 70 80 90 100
x[x < 30 | 70 < x]  # elements not between 30 and 70
## [1] 10 20 80 90 100
x[x < mean(x)]  # elements smaller than the mean
## [1] 10 20 30 40 50
x[x^2 > 77777 | log10(x) <= 1.6]  # indexing via a transformed version of x
## [1] 10 20 30 90 100
(z <- round(runif(length(x)), 2))  # ten pseudorandom numbers
## [1] 0.29 0.79 0.41 0.88 0.94 0.05 0.53 0.89 0.55 0.46
x[z <= 0.5]  # indexing based on z, not x - not a problem
## [1] 10 30 60 100</pre>
```

The indexer is always evaluated first and then passed to the subsetting operation. The index operator does not care how an indexer is generated.

Furthermore, the recycling rule is applied when necessary:

```
x[c(FALSE, TRUE)] # every second element
## [1] 20 40 60 80 100
y[c(TRUE, FALSE)] # interestingly, there is no warning here
## [[1]]
## [1] 1
##
## [[2]]
## [1] 21 22 23
```

**Exercise 5.1** Consider a simple database about six people, their favourite dishes, and birth years.

```
name <- c("Graham", "John", "Terry", "Eric", "Michael", "Terry")
food <- c("bacon", "spam", "spam", "eggs", "spam", "beans")
year <- c( 1941, 1939, 1942, 1943, 1943, 1940 )
```

The consecutive elements in different vectors correspond to each other, e.g., Graham was born in 1941, and his go-to food was bacon.

- List the names of people born in 1941 or 1942.
- List the names of those who like spam.
- List the names of those who like spam and were born after 1940.
- Compute the average birth year of the lovers of spam.
- Give the average age, in 1969, of those who didn't find spam utmostly delicious.

The answers to the above must be provided programmatically, i.e., we do not just write "Fric" and "Graham". The code must be generic enough so that it works in the case of any other database of this kind, no matter its size.

**Exercise 5.2** Remove missing values from a given vector without referring to the **na.omit** function.

#### 5.2.4 Character indexer

If a vector is equipped with the names attribute, such as this one:

```
x <- structure(x, names=letters[1:10]) # add names
print(x)
## a b c d e f g h i j
## 10 20 30 40 50 60 70 80 90 100</pre>
```

These labels can be referred to for the purpose of extracting the elements. To do this, we use an indexer that is a character vector:

```
x[c("a", "f", "a", "g", "z")]
## a f a g <NA>
## 10 60 10 70 NA
```

**Important** We have said that special object attributes add *extra* functionality on top of the existing ones. Therefore, indexing by means of positive, negative, and logical vectors is still available:

```
x[1:3]
## a b c
## 10 20 30
x[-(1:5)]
## f g h i j
## 60 70 80 90 100
x[x > 70]
## h i j
## 80 90 100
```

Lists can also be subsetted this way.

```
(y <- structure(y, names=c("first", "second", "third")))</pre>
## $first
## [1] 1
##
## $second
## [1] 11 12
##
## $third
## [1] 21 22 23
y[c("first", "second")]
## $first
## [1] 1
##
## $second
## [1] 11 12
y["third"]
           # result is a list
## $third
## [1] 21 22 23
y[["third"]] # result is the specific element unwrapped
## [1] 21 22 23
```

**Important** Labels do not have to be unique. When we have repeated names, the first matching element is extracted:

```
structure(1:3, names=c("a", "b", "a"))["a"]
## a
## 1
```

There is no direct way to select all *but* given names, just like with negative integer indexers. For a workaround, see Section 5.4.1.

**Exercise 5.3** Rewrite the solution to the above spam-lovers exercise, assuming that we have the three features wrapped inside a list: (notice that Steve has now joined the group; hello, Steve):

```
(people <- list(
                                            "Michael", "Terry", "Steve"),
   Name=c("Graham", "John", "Terry", "Eric",
   Food=c("bacon", "spam", "spam",
                                           "spam",
                                  "eggs",
                                                      "beans", "spam"),
   Year=c( 1941, 1939, 1942,
                                           1943.
                                                       1940,
                                                               NA real )
                                    1943.
))
## $Name
                                            "Michael" "Terry"
## [1] "Graham" "John" "Terry"
                                   "Eric"
                                                               "Steve"
```

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```
##
## $Food
## [1] "bacon" "spam" "spam" "eggs" "spam" "beans" "spam"
##
## $Year
## [1] 1941 1939 1942 1943 1943 1940 NA
```

Do not refer to name, food, and year directly. Instead, use the full people[["Name"]] etc. accessors. There is no need to pout: it is just a tiny bit of extra work.

### 5.3 Replacing elements

#### 5.3.1 Modifying atomic vectors

There are also *replacement* versions of the above indexing schemes. They allow us to substitute some new content for the old one.

```
(x <- 1:12)
## [1] 1 2 3 4 5 6 7 8 9 10 11 12
x[length(x)] <- 42 # modify the last element
print(x)
## [1] 1 2 3 4 5 6 7 8 9 10 11 42</pre>
```

The principles of vectorisation, recycling rule, and implicit coercion are all in place:

```
x[c(TRUE, FALSE)] <- c("a", "b", "c")
print(x)
## [1] "a" "2" "b" "4" "c" "6" "a" "8" "b" "10" "c" "42"
```

Long story long: first, to ensure that the new content can be poured into the old wineskin, R needed to convert the numeric vector to a character one; compare Section 4.1. Then, every second element therein, a total of six items, was replaced by a recycled version of the replacement sequence of length 3. Finally, the name "x" was rebound to such a brought-forth object and the previous one became forgotten.

**Note** For more details on replacement functions in general, see Section 9.4.6. Such operations alter the state of the object they are called on (quite a rare behaviour in functional languages).

**Exercise 5.4** Replace missing values in a given numeric vector with the arithmetic mean of well-defined observations therein.

#### **Modifying lists** 5.3.2

List contents can be altered as well. For modifying individual elements, the safest option is to use the replacement version of the `[[` operator:

```
y <- list(a=1, b=1:2, c=1:3)
y[[1]] < -100:110
y[["c"]] <- -y[["c"]]
print(y)
## $a
## [1] 100 101 102 103 104 105 106 107 108 109 110
##
## $b
## [1] 1 2
##
## $c
## [1] -1 -2 -3
```

The replacement version of `[` modifies a whole sub-list:

```
y[1:3] <- list(1, c("a", "b", "c"), c(TRUE, FALSE))
print(y)
## $a
## [1] 1
##
## $b
## [1] "a" "b" "c"
##
## $c
## [1] TRUE FALSE
```

#### Moreover:

```
y[1] <- list(1:10) # replace 1 element with 1 object
y[-1] <- 10:11  # replace 2 elements with 2 vectors of length 1
print(y)
## $a
## [1] 1 2 3 4 5 6 7 8 9 10
##
## $b
## [1] 10
##
## $c
## [1] 11
```

**Note** Let idx be a vector of positive indexes of elements to be modified. Overall, calling "y[idx] <- z" behaves as if we wrote:

```
    y[[idx[1]]] <- z[[1]],</li>
    y[[idx[2]]] <- z[[2]],</li>
    y[[idx[3]]] <- z[[3]],</li>
    and so forth.
```

Furthermore, z (but not idx) will be recycled if necessary, i.e., we take z[[j % length(z)]] for consecutive js from 1 to the length of idx.

#### **Exercise 5.5** *Reflect upon the results of the following expressions:*

```
y[1] <- c("a", "b", "c"),</li>
y[[1]] <- c("a", "b", "c"),</li>
y[[1]] <- list(c("a", "b", "c")),</li>
y[1:3] <- c("a", "b", "c"),</li>
y[1:3] <- list(c("a", "b", "c")),</li>
y[1:3] <- list("a", "b", "c")),</li>
y[1:3] <- list("a"),</li>
y[c(1, 2, 1)] <- c("a", "b", "c"),</li>
```

**Important** Setting a list item to NULL removes it from the list completely.

```
y <- list(1, 2, 3, 4)
y[1] <- NULL  # removes the 1st element (i.e., 1)
y[[1]] <- NULL  # removes the 1st element (i.e., now 2)
y[1] <- list(NULL) # sets the 1st element (i.e., now 3) to NULL
print(y)
## [[1]]
## NULL
##
## [[2]]
## [1] 4</pre>
```

The same notation convention is used for dropping object attributes; see Section 9.4.6.

# 5.3.3 Inserting new elements

New elements can be pushed at the end of the vector quite easily<sup>3</sup>.

<sup>&</sup>lt;sup>3</sup> And often cheaply; see Section 8.3.5 for some performance notes. Still, a warning can be generated on each size extension if the "check.bounds" flag is set; see help("options").

```
(x <- 1:5)
## [1] 1 2 3 4 5
x[length(x)+1] <- 6 # insert at the end
print(x)
## [1] 1 2 3 4 5 6
x[10] <- 10 # insert at the end but add more items
print(x)
## [1] 1 2 3 4 5 6 NA NA NA 10</pre>
```

The elements to be inserted can be named as well:

Note that x was not equipped with the names attribute before. The unlabelled elements were assigned blank labels (empty strings).

**Note** It is not possible to insert new elements at the beginning or in the middle of a sequence, at least not with the index operator. By writing "x[3:4] <- 1:5" we do not replace two elements in the middle with five other ones. However, we can always use the **c** function to slice parts of the vector and intertwine them with some new content:

```
x <- seq(10, 100, 10)
x <- c(x[1:2], 1:5, x[5:7])
print(x)
## [1] 10 20 1 2 3 4 5 50 60 70</pre>
```

# 5.4 Functions related to indexing

Let us review some operations which pinpoint interesting elements in a vector (or functions based on these).

## 5.4.1 Matching of elements in another vector

We know that the `==` operator acts in an elementwise manner. It compares each element in a vector on the left-hand side to the *corresponding* element in a vector on the

right side. Thus, missing values and the recycling rule aside, if z <- (x == y), then z[i] is TRUE if and only if x[i] == y[i].

The `%in%` operator<sup>4</sup> is vectorised differently: it checks whether each element on the left-hand side matches *one of* the elements on the right. Given z <- (x %in% y), z[i] is TRUE whenever x[i] == y[j] for some j.

```
c("spam", "bacon", "spam", "eggs", "spam") %in% c("eggs", "spam", "ham")
## [1] TRUE FALSE TRUE TRUE TRUE
```

**Example 5.6** Here is how we can remove the elements of a vector that have been assigned specified labels.

```
(x <- structure(1:12, names=month.abb)) # example vector
## Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
## 1 2 3 4 5 6 7 8 9 10 11 12
x[!(names(x) %in% c("Jan", "May", "Sep", "Oct"))] # get rid of some elements
## Feb Mar Apr Jun Jul Aug Nov Dec
## 2 3 4 6 7 8 11 12</pre>
```

More generally, match(x, y) gives us the index of the element in y that matches each x[i].

```
match(c("spam", "bacon", "spam", "eggs", "spam"), c("eggs", "spam", "ham"))
## [1] 2 NA 2 1 2
match(month.abb, c("Jan", "May", "Sep", "Oct")) # is the month on the list?
## [1] 1 NA NA NA 2 NA NA NA 3 4 NA NA
match(c("Jan", "May", "Sep", "Oct"), month.abb) # which month is it?
## [1] 1 5 9 10
```

NA\_real\_ denotes (by default) a no-match.

**Exercise 5.7** Check out the documentation of `**%in%**` to see how this operator is reduced to a call to **match**. Also, verify that it treats missing values as well-defined ones.

If the elements in y are not unique, the smallest index j such that x[i] == y[j] is returned. Therefore, for example, match(TRUE, l) can be used to fetch the index of the first occurrence of a positive value in a logical vector l.

```
(x <- round(runif(10), 2)) # example vector

## [1] 0.29 0.79 0.41 0.88 0.94 0.05 0.53 0.89 0.55 0.46

match(TRUE, x>0.8) # index of the first value > 0.8 (from the left)

## [1] 4
```

<sup>&</sup>lt;sup>4</sup> A fantastic name; see Section 9.4.5.

### 5.4.2 Assigning numbers into intervals

**findInterval** can come in handy where the assigning of numeric values into real intervals is needed. Namely, z <- **findInterval**(x, y) for increasing y gives z[i] being the index j such that x[i] is between y[j] (by default, inclusive) and y[j+1] (by default, exclusive).

For example, a sequence of five knots  $y = (-\infty, 0.25, 0.5, 0.75, \infty)$  splits the real line into the following four intervals:

$$[-\infty, 0.25)$$
  $[0.25, 0.5)$   $[0.5, 0.75)$   $[0.75, \infty)$ 

Hence, for instance:

```
findInterval(c(0, 0.2, 0.25, 0.4, 0.66, 1), c(-Inf, 0.25, 0.5, 0.75, Inf))
## [1] 1 1 2 2 3 4
```

**Exercise 5.8** Refer to the manual of **findInterval** to verify the function's behaviour when we do not include  $\pm \infty$  as endpoints and how to make  $\infty$  classified as a member of the fourth interval.

**Exercise 5.9** Using a call to **findInterval**, write a statement that generates a logical vector whose *i*-th element indicates whether x[i] is in the interval [0.25, 0.5]. Was this easier to write than an expression involving `<=` and `>=`?

### 5.4.3 Splitting vectors into subgroups

**split**(x, z) can take the output of **match** or **findInterval** (and many other operations) and divide the elements in a vector x into subgroups corresponding to identical zs.

For instance, we can assign people into groups determined by their favourite dish:

```
name <- c("Graham", "John", "Terry", "Eric", "Michael", "Terry")</pre>
food <- c("bacon", "spam", "spam", "eggs", "spam",</pre>
                                                          "beans")
split(name, food) # group names with respect to food
## $bacon
## [1] "Graham"
##
## $beans
## [1] "Terry"
##
## $eggs
## [1] "Eric"
##
## $spam
## [1] "John"
                 "Terry" "Michael"
```

The result is a named list with labels determined by the unique elements in the second vector.

Another example: here are some numbers pigeonholed into the four previously mentioned intervals:

```
x <- c(0, 0.2, 0.25, 0.4, 0.66, 1)
split(x, findInterval(x, c(-Inf, 0.25, 0.5, 0.75, Inf)))
## $`1`
## [1] 0.0 0.2
##
## $`2`
## [1] 0.25 0.40
##
## $`3`
## [1] 0.66
##
## $`4`
## [1] 1</pre>
```

Missing values in the second argument will result in the corresponding values' in the first argument being ignored. Also, unsurprisingly, the recycling rule is applied when necessary.

We can also split x into groups defined by a combination of levels of two or more variables z1, z2, etc., by calling **split**(x, **list**(z1, z2, ...)).

**Example 5.10** The built-in ToothGrowth is a named list (with some extra attributes that make us rather call it a data frame; see Chapter 12) that represents the results of an experimental study involving 60 guinea pigs. The experiment's aim was to measure the effect of different vitamin C supplement types and doses on the growth of the rodents' teeth lengths:

```
ToothGrowth <- as.list(ToothGrowth) # it is a list, but with extra attribs
ToothGrowth[["supp"]] <- as.character(ToothGrowth[["supp"]]) # was: factor
print(ToothGrowth)
## $len
## [1] 4.2 11.5 7.3 5.8 6.4 10.0 11.2 11.2 5.2 7.0 16.5 16.5 15.2 17.3
## [15] 22.5 17.3 13.6 14.5 18.8 15.5 23.6 18.5 33.9 25.5 26.4 32.5 26.7 21.5
## [29] 23.3 29.5 15.2 21.5 17.6 9.7 14.5 10.0 8.2 9.4 16.5 9.7 19.7 23.3
## [43] 23.6 26.4 20.0 25.2 25.8 21.2 14.5 27.3 25.5 26.4 22.4 24.5 24.8 30.9
## [57] 26.4 27.3 29.4 23.0
##
## $supp
## [57] "OJ" "OJ" "OJ" "OJ"
##
## $dose
```

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We can split len with respect to the combinations of supp and dose (also called interactions) by calling:

```
split(ToothGrowth[["len"]], ToothGrowth[c("supp", "dose")], sep=" ")
## $0J 0.5
  [1] 15.2 21.5 17.6 9.7 14.5 10.0 8.2 9.4 16.5 9.7
##
## $VC 0.5
   [1] 4.2 11.5 7.3 5.8 6.4 10.0 11.2 11.2 5.2 7.0
##
## $0J 1
   [1] 19.7 23.3 23.6 26.4 20.0 25.2 25.8 21.2 14.5 27.3
##
## $VC 1
   [1] 16.5 16.5 15.2 17.3 22.5 17.3 13.6 14.5 18.8 15.5
##
## $0J 2
   [1] 25.5 26.4 22.4 24.5 24.8 30.9 26.4 27.3 29.4 23.0
##
##
## $VC 2
## [1] 23.6 18.5 33.9 25.5 26.4 32.5 26.7 21.5 23.3 29.5
```

Other synonyms are, of course, possible, e.g., **split**(ToothGrowth[[1]], ToothGrowth[-1]) and **split**(ToothGrowth[[1]], **list**(ToothGrowth[[2]], ToothGrowth[[3]])). We recommend meditating upon our conscious use of double vs single square brackets here.

Functions such as Map (Section 7.2) will enable us to compute any summary statistics within groups (e.g., the within-group averages like with "SELECT AVG(len) FROM ToothGrowth GROUP BY supp, dose" in SQL). We are in no hurry. However, as an appetiser, let us feed the boxplot function with a list of vectors; see Figure 5.1.

```
boxplot(split(ToothGrowth[["len"]], ToothGrowth[c("supp", "dose")], sep="_"))
```

**Note** unsplit can be used to revoke the effects of split. Later, we will get used to calling unsplit(Map(some\_transformation, split(x, z)), z) to modify the values in x independently in each group defined by z (e.g., standardise the variables within each class separately).

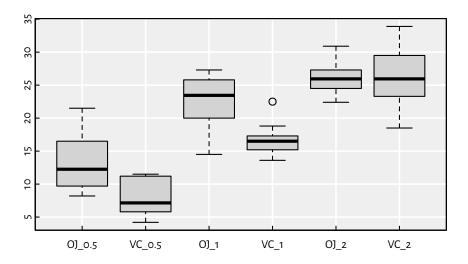


Figure 5.1: Box-and-whisker plots of len split by supp and dose (the ToothGrowth dataset)

### 5.4.4 Ordering elements

The **order** function finds the ordering permutation of a given vector, i.e., a sequence of indexes that leads to a sorted version thereof.

```
x <- c(1024, 7, 42, 666, 0, 32787)
(o <- order(x)) # the ordering permutation of x
## [1] 5 2 3 4 1 6
x[o] # ordered version of x
## [1] 0 7 42 666 1024 32787</pre>
```

Note that o[1] is the index of the smallest element in x, o[2] is the position of the second smallest, ..., and o[length(o)] is the index of the greatest value. Hence, e.g., x[o[1]] is equivalent to min(x).

Another example:

```
x <- c("b", "a", "abs", "bass", "aaargh", "aaargh", "aaaargh")
(o <- order(x))
## [1] 2 7 5 6 3 1 4
x[o]
## [1] "a" "aaaargh" "aaargh" "abs" "b" "bass"</pre>
```

Here, as x is a character vector, the ordering is lexicographical (like in a dictionary), because this is exactly how  $\le$  on strings works.

**Note** The ordering permutation that **order** returns is unique (that is why we call it *the* permutation), even for inputs containing duplicated elements. Owing to the use of a *stable* sorting algorithm, ties (repeated elements) will be listed in the order of occurrence.

```
order(c(10, 20, 40, 10, 10, 30, 20, 10, 10))
## [1] 1 4 5 8 9 2 7 6 3
```

Above we have, e.g., five 10s at positions 1, 4, 5, 6, 9. These five indexes are guaranteed to be listed in this very order.

Ordering can also be performed in a nonincreasing manner:

```
x[order(x, decreasing=TRUE)]
## [1] "bass" "b" "abs" "aargh" "aaargh" "aaaargh" "a"
```

**Note** A call to sort(x) is equivalent to x[order(x)], but the former function can be faster in some scenarios. For instance, one of its arguments can induce a *partially* sorted vector which can be helpful if we only seek a few order statistics (e.g., the seven smallest values). Speed is rarely a bottleneck in the case of sorting (when it is, we have a problem!). This is why we will not bother ourselves with such topics until the last part of this pleasant book. Currently, we aim at expanding the repertoire of our skills and abilities so that we can implement anything we can think of (rapid prototyping with the least footprint).

**Exercise 5.11** is.unsorted(x) can be used to determine if the elements in a given vector are... not sorted with respect to `<=`. Write an R expression that generates the same result by referring to the order function. Also, assuming that x is numeric, do the same by means of a call to diff.

**Note** Looking at **help**("order"), we see that it also accepts one or more arguments via the dot-dot-dot parameter, "...". This way, we can sort a vector with respect to many criteria. If there are ties (equal observations) in the first variable, they will be resolved by the order of elements in the second variable. This is most useful for rearranging rows of a data frame, which we will exercise in Chapter 12.

```
x <- c( 10, 20, 30, 40, 50, 60)
y1 <- c("a", "b", "a", "a", "b", "b")
y2 <- c("w", "w", "v", "u", "v")
x[order(y1)]
## [1] 10 30 40 20 50 60
x[order(y2)]
## [1] 40 50 30 60 10 20
x[order(y1, y2)]</pre>
```

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```
## [1] 40 30 10 50 60 20
x[order(y2, y1)]
## [1] 40 50 30 60 10 20
```

**Note** (\*) Calling **order** on a permutation (a vector that is an arbitrary arrangement of *n* consecutive natural numbers) determines its *inverse*.

```
x <- c(10, 30, 40, 20, 10, 10, 50, 30)
order(x)
## [1] 1 5 6 4 2 8 3 7
order(order(x)) # inverse of the above permutation
## [1] 1 5 7 4 2 3 8 6
(x[order(x)])[order(order(x))] # we get x again
## [1] 10 30 40 20 10 10 50 30</pre>
```

Note that order(order(x)) can be considered as a way to rank all the elements in x. For instance, the third value in x, 40, is assigned rank 7: it is the seventh smallest value in this vector. This breaks the ties on a first-come-first-served basis. But we can also write:

```
order(order(x, runif(length(x)))) # ranks with ties broken at random
## [1] 2 5 7 4 3 1 8 6
```

For different variations of these, see the rank function.

**Exercise 5.12** Recall that sample(x) returns a pseudorandom permutation of elements of a given vector unless x is a single positive number. Write an expression that always yields a proper rearrangement, regardless of the size of x.

# 5.4.5 Identifying duplicates

Whether any element in a vector was already listed in the previous part of the sequence can be verified by calling:

```
x <- c(10, 20, 30, 20, 40, 50, 50, 50, 20, 20, 60)

duplicated(x)

## [1] FALSE FALSE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE FALSE
```

This can be used to remove repeated observations; see also **unique**. This function returns a value that is not guaranteed to be sorted (unlike in some other languages/libraries).

**Exercise 5.13** What can be the use case of a call to match(x, unique(x))?

**Exercise 5.14** Given two named lists x and y, which we treat as key-value pairs, determine their set-theoretic union (with respect to the keys), for example:

```
x <- list(a=1, b=2)
y <- list(c=3, a=4)
z <- ...to.do... # combine x and y
str(z)
## List of 3
## $ a: num 4
## $ b: num 2
## $ c: num 3</pre>
```

## 5.4.6 Counting index occurrences

**tabulate** takes a vector of values from a set of small positive integers (e.g., indexes) and determines their number of occurrences:

```
x <- c(2, 4, 6, 2, 2, 2, 3, 6, 6, 3)
tabulate(x)
## [1] 0 4 2 1 0 3</pre>
```

In other words, there are 0 ones, 4 twos, ..., and 3 sixes.

**Exercise 5.15** Using a call to **tabulate** (amongst others), return a named vector with the number of occurrences of each unique element in a character vector. For example:

```
y <- c("a", "b", "a", "c", "a", "d", "e", "e", "g", "g", "c", "c", "g")
result <- ...to.do...
print(result)
## a b c d e g
## 3 1 3 1 2 3</pre>
```

## 5.5 Preserving and losing attributes

As attributes are conceived as extra data, it is up to a function's authors what they will decide to do with them. Generally, it is safe to assume that much thought has been put into the design of base R functions. Oftentimes, they behave quite reasonably. This is why we are going to spend some time now exploring their approaches to the handling of attributes.

Namely, for functions and operators that aim at transforming vectors passed as their inputs, the assumed strategy may be to:

· ignore the input attributes completely,

- equip the output object with the same set of attributes, or
- take care only of some special attributes, such as names, if that makes sense.

Below we explore some common patterns; see also Section 1.3 in [62].

#### 5.5.1 C

First, **c** drops<sup>5</sup> all attributes except names:

```
(x <- structure(1:4, names=c("a", "b", "c", "d"), attrib1="<3"))
## a b c d
## 1 2 3 4
## attr(,"attrib1")
## [1] "<3"
c(x) # only `names` are preserved
## a b c d
## 1 2 3 4</pre>
```

We can therefore end up calling this function chiefly for this nice side effect. Also, recall that unname drops the labels.

```
unname(x)
## [1] 1 2 3 4
## attr(,"attrib1")
## [1] "<3"</pre>
```

#### 5.5.2 as.something

**as.vector**, **as.numeric**, and similar drop all attributes in the case where the output is an atomic vector, but it might not necessarily do so in other cases (because they are S3 generics; see Chapter 10).

```
as.vector(x) # drops all attributes if x is atomic
## [1] 1 2 3 4
```

## 5.5.3 Subsetting

Subsetting with `[` (except where the indexer is not given) drops all attributes but names (as well as dim and dimnames; see Chapter 11), which is adjusted accordingly:

```
x[1]  # subset of labels
## a
## 1
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```

<sup>&</sup>lt;sup>5</sup> To be precise, we mean the default S3 method of **c** here; compare Section 10.2.4.

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```
x[[1]] # this always drops the labels
## [1] 1
```

The replacement version of the index operator can be used to modify the values in an existing vector whilst preserving all the attributes. In particular, skipping the indexer will allow us to replace all the elements:

```
y <- x
y[] <- c("u", "v") # note that c("u", "v") has no attributes at all
print(y)
## a b c d
## "u" "v" "u" "v"
## attr(,"attrib1")
## [1] "<3"
```

#### 5.5.4 Vectorised functions

Vectorised unary functions tend to copy all the attributes.

```
round(x)
## a b c d
## 1 2 3 4
## attr(,"attrib1")
## [1] "<3"
```

Binary operations are expected to get the attributes from the longer input. If they are of equal sizes, the first argument preferred to the second.

```
y <- structure(c(1, 10), names=c("f", "g"), attrib1=":|", attrib2=":0")</pre>
y * x # x is longer
## a b c d
## 1 20 3 40
## attr(,"attrib1")
## [1] "<3"
y[c("h", "i")] <- c(100, 1000) # add two new elements at the end
v * x
        g h
    f
## 1 20 300 4000
## attr(,"attrib1")
## [1] ":/"
## attr(,"attrib2")
## [1] ":0"
x * y
     a b c d
##
## 1 20 300 4000
```

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```
## attr(,"attrib1")
## [1] "<3"
## attr(,"attrib2")
## [1] ":0"</pre>
```

Also, refer to Section 9.4.6 for a way to copy all the attributes from one object to another.

**Important** Even in base R, the above rules are not enforced strictly. We consider them inconsistencies that should be, for the time being, treated as features (with which we need to learn to live as they have not been fixed for years, but hope springs eternal).

As far as third-party extension packages are concerned, suffice it to say that a lot of R programmers do not know what attributes are at all! It is always best to refer to the documentation, perform some experiments, and/or manually ensure the preservation of the data we care about.

**Exercise 5.16** Check what attributes are preserved by **ifelse**.

#### 5.6 Exercises

**Exercise 5.17** Answer the following questions (contemplate first, then use R to find the answer):

- What is the result of "x[c()]?" Is it the same as "x[]"?
- Is "x[c(1, 1, 1)]" equivalent to "x[1]"?
- Is "x[1]" equivalent to "x["1"]"?
- Is "x[c(-1, -1, -1)]" equivalent to "x[-1]"?
- What does "x[c(0, 1, 2, NA)]" do?
- What does "x[0]" return?
- What does "x[1, 2, 3]" do?
- What about "x[c(0, -1, -2)]" and "x[c(-1, -2, NA)]"?
- Why "x[NA]" is so significantly different from "x[c(1, NA)]"?
- What is "x[c(FALSE, TRUE, 2)]"?
- What will we obtain by calling "x[x<min(x)]"?</li>
- What about "x[length(x)+1]"?
- Why "x[min(y)]" is probably a mistake? What could it mean? How can it be fixed?

- Why cannot we mix indexes of different types and write "x[c(1, "b", "c", 4)]"? Or can we?
- Why would we call "as.vector(na.omit(x))" instead of just na.omit(x)?
- What is the difference between **sort** and **order**?
- What is the type and the length of the object returned by a call to "split(a, u)"? What about "split(a, c(u, v))"?
- How to get rid of the seventh element from a list of ten elements?
- How to get rid of the seventh, eight, and ninth elements from a list with ten elements?
- How to get rid of the seventh element from an atomic vector of ten elements?
- If y is a list, by how many elements "y[c(length(y)+1, length(y)+1, length(y)+1)]
   list(1, 2, 3)" will extend it?
- What is the difference between "x[x>0]" and "x[which(x>0)]"?

**Exercise 5.18** If x is an atomic vector of length n, "x[5:n]" obviously extracts everything from the fifth element to the end. Does it, though? Check what happens when x is of length less than five, including 0. List different ways to correct this expression so that it makes (some) sense in the case of shorter vectors.

**Exercise 5.19** Similarly, "x[length(x) + 1 - 5:1]" is supposed to return the last five elements in x. Propose a few alternatives that are correct also for short xs.

**Exercise 5.20** Given a numeric vector, fetch its five largest elements. Ensure the code works for vectors of length less than five.

**Exercise 5.21** We can compute a trimmed mean of some x by setting the trim argument to the **mean** function. Compute a similar robust estimator of location – the p-winsorised mean,  $p \in [0,0.5]$  defined as the arithmetic mean of all elements in x clipped to the  $[Q_p,Q_{1-p}]$  interval, where  $Q_p$  is the vector's p-quantile; see **quantile**. For example, if x is (8,5,2,9,7,4,6,1,3), we have  $Q_{0.25} = 3$  and  $Q_{0.75} = 7$  and hence the 0.25-winsorised mean will be equal to the arithmetic mean of (7,5,3,7,7,4,6,3,3).

**Exercise 5.22** Let x and y be two vectors of the same length, n, and no ties. Compute the Spearman rank correlation coefficient given by:

$$\varrho(\mathbf{x}, \mathbf{y}) = 1 - \frac{6\sum_{i=1}^{n} d_i^2}{n(n^2 - 1)},$$

where  $d_i = r_i - s_i$ , i = 1, ..., n, and  $r_i$  and  $s_i$  denote the rank of  $x_i$  and  $y_i$ , respectively. See also the built-in **cor**.

**Exercise 5.23** (\*) Given two vectors x and y of the same length n, a call to approx(x, y, ...) can be used to interpolate linearly between the points  $(x_1, y_1), (x_2, y_2), ..., (x_n, y_n)$ . We can use it whenever we wish to generate new ys for previously unobserved xs (somewhere "inbetween" the data we already have). Moreover, spline(x, y, ...) can perform a cubic spline interpolation, which is smoother; see Figure 5.2.

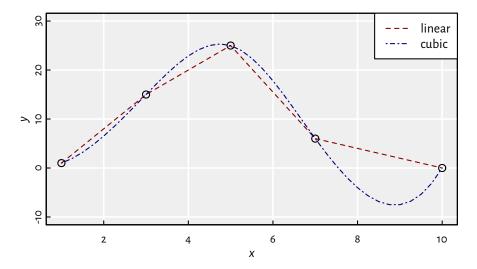


Figure 5.2: Piecewise linear and cubic spline interpolation

Using a call to one of the above, perform the missing data imputation in the euraud-20200101-20200630.  $csv^6$ , e.g., the blanks in (0.60, 0.62, NA, 0.64, NA, NA, 0.58) should be filled so as to obtain (0.60, 0.62, 0.63, 0.64, 0.62, 0.60, 0.58).

**Exercise 5.24** Given some  $1 \le from \le to \le n$ , use **findInterval** to generate a logical vector of length n with TRUE elements only at indexes between from and to, inclusive.

**Exercise 5.25** Implement expressions that yield the same results as calls to which, which.min, which.max, and rev functions. What is the difference between x[x>y] and x[which(x>y)]? What about which.min(x) vs which(x == min(x))?

**Exercise 5.26** Given two equal-length vectors x and y, fetch the value from the former that corresponds to the smallest value in the latter. Write three versions of such an expression, each dealing with potential ties in y differently, for example:

<sup>&</sup>lt;sup>6</sup> https://github.com/gagolews/teaching-data/raw/master/marek/euraud-20200101-20200630.csv

```
x <- c("a", "b", "c", "d", "e", "f")
y <- c( 3, 1, 2, 1, 1, 4)
```

should choose either the first ("b"), last ("e"), or random ("b", "d", "e" with equal probability) element from x fulfilling the above property. Make sure your code works for x being of the type character or numeric as well as an empty vector.

**Exercise 5.27** Implement an expression that yields the same result as duplicated(x) for a numeric vector x, but using diff and order.

**Exercise 5.28** Based on match and unique, implement your versions of union(x, y), intersect(x, y), setdiff(x, y), is.element(x, y), and setequal(x, y) for x and y being nonempty numeric vectors.

# Character vectors

Text is a universal, portable, economical, and efficient means of interacting between humans and computers as well as exchanging data between programs or APIs. This book is 99% made of text. And, wow, how much valuable knowledge is in it, innit?

## 6.1 Creating character vectors

## 6.1.1 Inputting individual strings

Specific character strings are delimited either by a pair of double or single quotes (apostrophes).

```
"a string"
## [1] "a string"
'another string' # and, of course, neither 'like this" nor "like this'
## [1] "another string"
```

The only difference between these two is that we cannot directly include, e.g., an apostrophe in a single quote-delimited string. On the other hand, "'tis good ol' spam" and 'I "love" bacon' are both okay.

However, to embrace characters whose inclusion might otherwise be difficult or impossible, we may always employ the so-called *escape sequences*.

R uses the backslash, "\", as the escape character, in particular:

- \" inputs the double quote character,
- \' single quote,
- \\ backslash,
- \n new line.

```
(x <- "I \"love\" bacon\n\\\"/")
## [1] "I \"love\" bacon\n\\\"/"</pre>
```

The **print** function (which was implicitly called to display the above object) does not reveal the special meaning of the escape sequences. Instead, **print** outputs strings in

the same way that we ourselves would follow when inputting them. The number of characters in x is 18, and not 23:

```
nchar(x)
## [1] 18
```

To display the string as-it-really-is, we call:

```
cat(x)
## I "love" bacon
## \"/
```

Raw character constants, where the backslash character's special meaning is disabled, can be entered using the notation like  $\Gamma''(...)'', \Gamma'''[...]'', \Gamma'''[...]'', \Gamma'''[...]'', \Gamma''''$ . These can be useful when inputting regular expressions (see below).

```
x <- r"(spam\n\\\"maps)"
print(x)
## [1] "spam\|n\\\\"maps"
cat(x)
## spam\n\\\"maps</pre>
```

... and, of course, the string version of the missing value marker is "NA\_character\_".

**Note** (\*) Some output devices may support the following codes that control the position of the caret (text cursor):

- \b backspace (move cursor one column to the left),
- $\t$  tab (advance to the next tab stop, e.g., a multiply of 8),
- \r carriage return (move to the beginning of the current line).

```
cat("abc\bd\tef\rg\nhij")
## gbd ef
## hij
```

These can be used on unbuffered outputs (see, e.g., help("stderr")) to display the status of the current operation (a simple "animated" progress bar, the print-out of the ETA, or the percentage of work completed).

Further, certain terminals can also understand the ECMA-48/ANSI-X3.64 escape sequences<sup>1</sup> of the form "\u001b[..." to control further the cursor's position, text colour, and even style. For example, "\u001b[1;31m" outputs bold red text and "\u001b[0m" resets the settings to default. Give, e.g., "cat("\u001b[1;31mspam\u001b[0m")" or "cat("\u001b[5;36m\u001b[Abacon\u001b[Espam\u001b[0m")" a try.

<sup>1</sup> https://en.wikipedia.org/wiki/ANSI\_escape\_code

**Note** (\*) The Unicode standard 15.0 (version dated September 2022) defines over 149 186 characters, i.a., letters from different scripts, mathematical symbols, and emojis. Each is assigned a unique numeric identifier; see the Unicode Character Code Charts<sup>2</sup>. For example, the *inverted exclamation mark* (see the Latin-1 Supplement section therein) has been mapped to hexadecimal code OxA1 (or 161 decimally). Knowing this magic number allows us to specify a Unicode code point using one of the following escape sequences:

- \uxxxx codes using four hexadecimal digits,
- \Uxxxxxxx codes using eight hexadecimal digits.

#### For instance:

```
cat("!\u00a1!\U000000a1!")
## !;!;!
```

All R installations allow for working with Unicode strings (more precisely, UTF-8: a super-encoding that is native to most UNIX-like boxes, including GNU/Linux and m\*\*OS). Other operating systems may use some 8-bit encoding as the system one (e.g., latin1 or cp1252), but they can be mixed with Unicode seamlessly. See help("Encoding"), help("iconv"), and [26] for discussion.

Nevertheless, certain output devices (web browsers, LaTeX renderers, text terminals) might be unable to display every possible Unicode character, e.g., due to some fonts' being missing. However, as far as the processing of character data is concerned, this does not matter: R does it with its eyes closed.

For example, in the PDF version<sup>3</sup> of this adorable book, none of the following Unicode glyphs are correctly displayed, because yours cordially did not care about installing appropriate fonts in his XeLaTeX distribution. However, its HTML variant<sup>4</sup>, generated from the same source files as the former, will likely be rendered by the kind reader's web browser as intended.

```
cat("\U0001f642\u2665\u0bb8\U0001f923\U0001f60d\u2307")
## 000000
```

# 6.1.2 Many strings, one object

Less trivial character vectors (meaning, of length greater than one) can be constructed by means of, e.g.,  $\mathbf{c}$  or  $\mathbf{rep}^5$ .

<sup>&</sup>lt;sup>2</sup> https://www.unicode.org/charts/

<sup>3</sup> https://deepr.gagolewski.com/deepr.pdf

<sup>4</sup> https://deepr.gagolewski.com

<sup>&</sup>lt;sup>5</sup> Internally, there is a string cache (a hash table). Multiple clones of the same string do not occupy more RAM than necessary.

```
(x <- c(rep("spam", 3), "bacon", NA_character_, "spam"))
## [1] "spam" "spam" "bacon" NA "spam"</pre>
```

Thus, a character vector is, in fact, a sequence of sequences of characters. As usual, the total number of strings can be fetched, via the **length** function. However, the length of each string may be read with the vectorised **nchar**.

```
length(x) # how many strings?
## [1] 6
nchar(x) # the number of code points in each string
## [1] 4 4 4 5 NA 4
```

#### 6.1.3 Concatenating character vectors

paste can be used to concatenate (join) the corresponding elements of two or more character vectors:

```
paste(c("a", "b", "c"), c("1", "2", "3")) # sep=" " by default
## [1] "a 1" "b 2" "c 3"
paste(c("a", "b", "c"), c("1", "2", "3"), sep="") # see also paste0
## [1] "a1" "b2" "c3"
```

The function is deeply vectorised:

```
paste(c("a", "b", "c"), 1:6, c("!", "?")) # implicit coercion of numbers
## [1] "a 1 !" "b 2 ?" "c 3 !" "a 4 ?" "b 5 !" "c 6 ?"
```

We can also collapse (flatten, aggregate) a sequence of strings into a single string:

```
paste(c("a", "b", "c", "d"), collapse=",")
## [1] "a,b,c,d"
paste(c("a", "b", "c", "d"), 1:2, sep="", collapse="")
## [1] "a1b2c1d2"
```

Unfortunately (perhaps for the so-called convenience), **paste** treats missing values differently from most other vectorised functions:

```
paste(c("A", NA_character_, "B"), "!", sep="")
## [1] "A!" "NA!" "B!"
```

## 6.1.4 Formatting objects

Strings can also come into being by turning other R objects into text. For example, the quite customisable (see Chapter 10) **format** function can be used to pretty-print data in dynamically generated reports.

```
x <- c(123456.789, -pi, NaN)
format(x)
## [1] "123456.7890" " -3.1416" " NaN"
cat(format(x, digits=8, scientific=FALSE, drop0trailing=TRUE), sep="\n")
## 123456.789
## -3.1415927
## NaN</pre>
```

Moreover, **sprintf** is a workhorse for turning possibly many atomic vectors into strings. The numbers' precision, strings' widths and justification, etc., can be fully controlled. Its first argument is a format string; special escape sequences starting with the per cent sign, "%", serve as placeholders for the actual values. For instance, "%s" is meant to be replaced with a corresponding string and "%f" with a floating point value. Additional options are available, e.g., "%10.2f" is a number that, when converted to text, will occupy ten text columns<sup>6</sup>, with two decimal digits of precision. Also, e.g., "%1\$s", "%2\$s", ... will insert the 1st, 2nd, ... argument as text.

```
sprintf("%.5f", pi)
## [1] "3.14159"
sprintf("%s%s", "a", c("X", "Y", "Z")) # like paste(...)
## [1] "aX" "aY" "aZ"
sprintf("key=%s, value=%.1f", c("spam", "eggs"), c(100000, 0))
## [1] "key=spam, value=100000.0" "key=eggs, value=0.0"
sprintf("%.*f", 1:5, pi) # variable precision
## [1] "3.1" "3.14" "3.142" "3.1416" "3.14159"
sprintf("%1$s, %2$s, %1$s, and %1$s", "spam", "bacon") # numbered argument
## [1] "spam, bacon, spam, and spam"
```

See help("sprintf") for more details. I recommend. Marek Gagolewski.

# 6.1.5 Reading text data from files

Given a raw text file, **readLines** can load it into memory to represent it as a character vector, with each line stored in a separate string.

<sup>&</sup>lt;sup>6</sup> This is only true for 8-bit native encodings; see also **sprintf** from the **stringx** package, which takes the text width and not the number of bytes into account.

I DEEP

```
(continued from previous page)
```

```
## [5] ""
## [6] "*Good* datasets are actually hard to find!"
```

writeLines is its counterpart. There is also an option to read or write parts of files at a time, which we mention in Section 8.3.5. Also, cat(..., append=TRUE) can be used to create a text file incrementally.

## 6.2 Pattern searching

## 6.2.1 Comparing whole strings

We have already reviewed a couple of ways to compare strings as a whole. For instance, the `==` operator implements elementwise testing:

```
c("spam", "spam", "bacon", "eggs") == c("spam", "eggs") # recycling rule
## [1] TRUE FALSE FALSE TRUE
```

In Section 5.4.1, we introduced the **match** function and its derivative, the `**%in%**` operator. They are vectorised in a different way:

```
match(c("spam", "spam", "bacon", "eggs"), c("spam", "eggs"))
## [1] 1 1 NA 2
c("spam", "spam", "bacon", "eggs") %in% c("spam", "eggs")
## [1] TRUE TRUE FALSE TRUE
```

**Note** match relies on simple, bytewise comparisons of the corresponding code points. It might not be valid in, for example, natural language processing activities; compare [18]. In particular, the German word *groß* is not deemed equal to *gross*, although we expect that should be the case, at least in a German language setting. Moreover, in the rare situations where we read Unicode-unnormalised data (say, not in the NFC form; see [17]), canonically equivalent strings may be considered different.

## 6.2.2 Partial matching

When only a consideration of the initial part of each string is required, we can call:

```
startsWith(c("s", "spam", "spamtastic", "spontaneous", "spoon"), "spam")
## [1] FALSE TRUE TRUE FALSE FALSE
```

Both the above and **endsWith** are applied elementwisely in case of many search prefixes/suffixes, just like in `==`.

Partial matching of strings can be performed with **charmatch**, which is a each-vs-all version of **startsWith**:

Note that 0 designates that there was an ambiguity in matching a string to a given table.

**Note** (\*) Section 9.5.7 discusses the very-advanced match.arg, which is frequently called from within other R functions to assist in selecting an argument from a range of possible choices. Furthermore, Section 9.4.2 and Section 15.4.4 mention the (discouraged) partial matching of list labels and argument names in function calls.

## 6.2.3 Matching anywhere within a string

Fixed patterns can also be searched for anywhere within character strings using grepl:

```
x <- c("spam", "y spammite spam", "yummy SPAM", "sram")
grepl("spam", x, fixed=TRUE) # fixed patterns, as opposed to regexes below
## [1] TRUE TRUE FALSE FALSE</pre>
```

**Important** The order of arguments is like **grepl**(needle, haystack), not the other way around. Also, this function is not vectorised with respect to the first argument.

**Exercise 6.1** Determine how the calls to grep(y, x, value=FALSE) and grep(y, x, value=TRUE) can be implemented based on grepl and other operations we are already familiar with.

**Note** As a curiosity, **agrepl** performs *approximate* matching based on Levenshtein's edit distance, which can account for a small number of "typos".

```
agrepl("spam", x)
## [1] TRUE TRUE FALSE TRUE
agrepl("ham", x, ignore.case=TRUE)
## [1] TRUE TRUE TRUE TRUE
```

## Using regular expressions (\*)

Setting perl=TRUE allows for identifying occurrences of patterns specified by the PCRE2 regular expressions (regexes).

```
grepl("^spam", x, perl=TRUE) # strings that begin with `spam`
## [1] TRUE FALSE FALSE FALSE
grepl("(?i)^spam|spam$", x, perl=TRUE) # begin or end; case ignored
## [1] TRUE TRUE TRUE FALSE
```

Note For more details on regular expressions in general, see, e.g., [23]. The ultimate reference for PCRE2 pattern syntax is the man<sup>7</sup> page pcre2pattern(3). R also gives access to ERE-like TRE library (see help("regex")), which is the default one. However, we discourage its use because it is feature-poorer.

**Exercise 6.2** The **list.files** function generates the list of file names in a given directory that match a given regular expression. For instance, the following gives all CSV files in some directory.

```
list.files("../../Projects/teaching-data/r/", r"(\.csv$)") # or "\\.csv$"
## [1] "air_quality_1973.csv" "anscombe.csv"
                                                  "iris.csv"
## [4] "titanic.csv"
                             "tooth_growth.csv"
                                                "trees.csv"
## [7] "world_phones.csv"
```

Write a single regular expression that matches file names ending with ".csv" or ".csv.gz". Also, write a regex that matches CSV files whose names do not begin with "eurusd".

#### Locating pattern occurrences 6.2.5

regexpr finds the first occurrence of a pattern in each string:

```
regexpr("spam", x, fixed=TRUE)
## [1] 1 3 -1 -1
## attr(,"match.length")
## [1] 4 4 -1 -1
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
```

In particular, there is a pattern occurrence starting at the 3th code point of the 2nd string in x. Moreover, the last string has no pattern match (denoted with -1).

The match. length attribute is generally more informative when searching with regular expressions.

To locate all the matches, i.e., globally, we use **gregexpr**:

<sup>&</sup>lt;sup>7</sup> http://www.pcre.org/current/doc/html/pcre2pattern.html

```
# `spam` followed by 0 or more letters, case insensitively
gregexpr("(?i)spam\\p{L}*", x, perl=TRUE)
## [[1]]
## [1] 1
## attr(,"match.length")
## [1] 4
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
##
## [[2]]
## [1] 3 12
## attr(,"match.length")
## [1] 8 4
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
##
## [[3]]
## [1] 7
## attr(,"match.length")
## [1] 4
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
##
## [[4]]
## [1] -1
## attr(,"match.length")
## [1] -1
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
```

As we noted in Section 4.4.2, wrapping the results in a list was a clever choice, as the number of matches can obviously vary between strings.

In Section 7.2, we will look at the Map function, which, along with substring introduced below, can aid in getting the most out of such data. Meanwhile, let us just mention that regmatches extracts the matching substrings:

```
regmatches(x, gregexpr("(?i)spam\\p{L}*", x, perl=TRUE))
## [[1]]
## [1] "spam"
##
## [[2]]
## [1] "spammite" "spam"
##
## [[3]]
## [1] "SPAM"
##
## [[4]]
## character(0)
```

**Note** (\*) Let us consider what happens when a regular expression contains parenthesised subexpressions (capture groups).

```
r <- "(?<basename>[^. ]+)\\.(?<extension>[^ ]*)"
```

The above regex consists of two such parts. The first one is labelled "basename". It comprises several arbitrary characters except for the space and the dot. The second group, named "extension", is a substring consisting of anything but the space. A dot separates these two groups.

Such a pattern can be used for unpacking space-delimited lists of file names.

```
z <- "dataset.csv.gz something_else.txt spam"</pre>
regexpr(r, z, perl=TRUE)
## [1] 1
## attr(,"match.length")
## [1] 14
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
## attr(,"capture.start")
       basename extension
##
          1
## [1,]
## attr(,"capture.length")
      basename extension
## [1,] 7
## attr(,"capture.names")
## [1] "basename" "extension"
gregexpr(r, z, perl=TRUE)
## [[1]]
## [1] 1 16
```

(continued from previous page)

```
## attr(,"match.length")
## [1] 14 18
## attr(,"index.type")
## [1] "chars"
## attr(,"useBytes")
## [1] TRUE
## attr(,"capture.start")
    basename extension
## [1,]
             1
## [2,] 16
                      31
## attr(,"capture.length")
## basename extension
## [1,]
            7
## [2,]
                       .3
             14
## attr(,"capture.names")
## [1] "basename" "extension"
```

The capture.\* attributes give us access to the matches to the individual capture groups, i.e., the basename and the extension.

**Exercise 6.3** (\*) Check out the difference between the results generated by **regexec** and **regexpr** as well as **gregexec** and **gregexpr**.

## 6.2.6 Replacing pattern occurrences

**sub** and **gsub** can replace first and all, respectively, matches to a pattern:

**Note** (\*) If a regex features some capture groups, matches thereto can be mentioned not only in the pattern itself but also in the replacement string:

```
gsub("(\\p{L})\\p{L}\\1", "\\1", "aha egg gag NaN spam", perl=TRUE)
## [1] "a egg g N spam"
```

The above matches in the following order: a letter (it is a capture group), another letter, and the former letter again. Each such palindrome of length three is replaced with just the repeated letter.

this function converts wildcards such as file???. \* or \*.csv to regular expressions that can be passed to, e.g., list.files.

#### 6.2.7 Splitting strings into tokens

**strsplit** divides each string in a character vector into chunks. This time, though, the search pattern specifying the token delimiter is given as the second argument:

```
strsplit(c("spam;spam;eggs;;bacon", "spam"), ";", fixed=TRUE)
## [[1]]
## [1] "spam" "spam" "eggs" "" "bacon"
##
## [[2]]
## [1] "spam"
```

## 6.3 Other string operations

## 6.3.1 Extracting substrings

substring extracts parts of strings between given character position ranges.

```
substring("spammity spam", 1, 4) # from 1st to 4th character
## [1] "spam"
substring("spammity spam", 10) # from 10th to end
## [1] "spam"
substring("spammity spam", c(1, 10), c(4, 14)) # vectorisation
## [1] "spam" "spam"
substring(c("spammity spam", "bacon and eggs"), 1, c(4, 5))
## [1] "spam" "bacon"
```

**Note** There is also a replacement (compare Section 9.4.6) version of the above:

```
x <- "spam, spam, bacon, and spam"
substring(x, 7, 11) <- "eggs"
print(x)
## [1] "spam, eggs, bacon, and spam"</pre>
```

Unfortunately, the number of characters in the replacement string should not exceed the length of the part being substituted (try "chickpeas" instead of "eggs"). However, substring replacement can be written as a composition of substring extraction and concatenation:

```
paste(substring(x, 1, 6), "chickpeas", substring(x, 11), sep="")
## [1] "spam, chickpeas, bacon, and spam"
```

**Exercise 6.5** Take the output generated by **regexpr** and apply **substring** to extract the pattern occurrences. If there is no match in some string, the corresponding output should be NA.

#### 6.3.2 Translating characters

**tolower** and **toupper** can be used to convert between lower and upper case:

```
toupper("spam")
## [1] "SPAM"
```

**Note** Like many other string operations in base R, these functions perform very simple character substitutions. They might not be valid in natural language processing tasks. For instance, *groß* is **not** converted to *GROSS*, the correct case folding in German.

Moreover, chartr translates individual characters:

```
chartr("\\", "/", "c:\\windows\\system\\cmd.exe") # chartr(old, new, x)
## [1] "c:/windows/system/cmd.exe"
chartr("([S", ")]*", ":( :S :[")
## [1] ":) :* :]"
```

In the first line, we replace each backslash with a slash. The second example replaces "(", "[", and "S" with ")", "]", and "\*", respectively.

## 6.3.3 Ordering strings

We have previously mentioned that operators and functions such as `<`, `>=`, sort, order, rank, and xtfrm<sup>8</sup> are based on the lexicographic ordering of strings.

```
sort(c("chłodny", "hardy", "chladný", "hladný"))
## [1] "chladný" "chłodny" "hardy" "hladný"
```

It is worth noting that the ordering depends on the currently selected locale; see **Sys. getlocale**("LC\_COLLATE"). For instance, in the Slovak language setting, we would obtain "hardy" < "hladný" < "chłodny".

**Note** Many "structured" data items can be displayed or transmitted as human-readable strings. In particular, we know that **as.numeric** can convert a string to a

<sup>&</sup>lt;sup>8</sup> See Section 12.3.1 for a use case.

number. Moreover, Section 10.3.1 will discuss date-time objects such as "1970-01-01 00:00:00 GMT". We will be processing them with specialised functions such as **strptime** and **strftime**.

**Important** (\*) Many string operations in base R are not necessarily portable. The **stringx** package defines drop-in, "fixed" replacements therefor. They are based on the International Components for Unicode (ICU<sup>9</sup>) library, a de facto standard for processing Unicode text, and the R package **stringi**; see [26].

```
# call install.packages("stringx") first
suppressPackageStartupMessages(library("stringx")) # load the package
sort(c("chłodny", "hardy", "chladný", "hladný"), locale="sk_SK")
## [1] "hardy" "hladný" "chladný" "chłodny"
toupper("gro\u00DF") # compare base::toupper("gro\u00DF")
## [1] "GROSS"
detach("package:stringx") # unload the package
```

# 6.4 Other atomic vector types (\*)

We have discussed four vector types: logical, double, character, and list (the latter being a generic-recursive vector). To get the complete picture of the sequence-like types in R, let us briefly mention integer, complex, and raw atomic types so that we are not surprised when we encounter them.

## 6.4.1 Integer vectors (\*)

Integer scalars can be input manually by using the L suffix:

```
(x <- c(1L, 2L, -1L, NA_integer_)) # looks like numeric
## [1] 1 2 -1 NA
typeof(x) # but is integer
## [1] "integer"</pre>
```

Some functions return them in a few contexts<sup>10</sup>:

<sup>9</sup> https://icu.unicode.org/

<sup>&</sup>lt;sup>10</sup> Actually, 1:10 returns an integer vector in a compact (ALTREP, see [51]) form; compare the results of the call to ".Internal(inspect(1:10))" and ".Internal(inspect(seq(1, 10, 1)))". This way, the whole vector does not have to be allocated. This saves memory and time. At the R level, though, it behaves as any other integer (numeric) sequence.

```
typeof(1:10) # seq(1, 10) as well, but not seq(1, 10, 1)
## [1] "integer"
as.integer(c(-1.1, 0, 1.9, 2.1)) # truncate/round towards 0
## [1] -1 0 1 2
```

In most expressions, integer vectors behave like numeric ones. They are silently coerced to double if need be. Therefore, there is no real practical reason to distinguish between them (they are of *internal* interest, e.g., when writing C/C++ extensions; see Chapter 14). For example:

```
1L/2L # like 1/2 == 1.0/2.0
## [1] 0.5
```

**Note** (\*) R integers are 32-bit signed types. The double type can store more integers than them (with the maximal contiguously representable integer being  $2^{53}$  vs  $2^{31} - 1$  in the former case; see Section 3.2.3):

```
as.integer(2^31-1) + 1L  # 32-bit integer overflow
## Warning in as.integer(2^31 - 1) + 1L: NAs produced by integer overflow
## [1] NA
as.integer(2^31-1) + 1 == 2^31 # integer+double == double - OK
## [1] TRUE
(2^53 - 1) + 1 == 2^53 # OK
## [1] TRUE
(2^53 + 1) - 1 == 2^53 # lost due to FP rounding, left result is 2^53 - 1
## [1] FALSE
```

**Note** Since R 3.0, there is support for vectors longer than  $2^{31}-1$  elements. As there are no 64-bit integers in R, these are indexed by doubles anyway (as we have been doing all this time). Interestingly, x[1.9] is the same as x[1], and x[-1.9] means x[-1] (a truncation of the fractional part). This is why the notation like x[length(x)\*0.2] works regardless of whether the length of x is a multiple of 5 or not, which is neat.

## 6.4.2 Raw vectors (\*)

Vectors of the type raw can store bytes, i.e., unsigned 8-bit integers, whose range is 0–255 (there are no raw NAs). For example:

```
as.raw(c(-1, 0, 1, 2, 0xc0, 254, 255, 256, NA))
## Warning: out-of-range values treated as 0 in coercion to raw
## [1] 00 00 01 02 c0 fe ff 00 00
```

They are displayed as two-digit hexadecimal (base-16) numbers. We may enter such numbers using the "0x" prefix.

Only a few functions deal with such vectors: e.g., readBin, charToRaw, and rawToChar.

## 6.4.3 Complex vectors (\*)

We can also play with vectors of the type complex, with "1i" representing the imaginary unit,  $\sqrt{-1}$ . Complex numbers appear in quite a few engineering or scientific applications, e.g., in physics, electronics, or signal processing. They are (at least: ought to be) part of introductory subjects or textbooks in university-level mathematics, including the statistics/machine learning-oriented ones, because of their heavy use of numerical computing; see e.g., [19, 29].

```
c(0, 1i, pi+pi*1i, NA_complex_)
## [1] 0.0000+0.0000i 0.0000+1.0000i 3.1416+3.1416i NA
```

Apart from the basic operators, mathematical and aggregation functions, procedures like **fft**, **solve**, **qr**, or **svd** can be fed with or produce such data. For more details, see **help**("complex") and some matrix examples in Chapter 11.

#### 6.5 Exercises

Exercises marked with (\*) might require tinkering with regular expressions or third-party R packages.

**Exercise 6.6** *Answer the following questions:* 

- How many characters are there in the string "ab\n\\\t\\\\""? What about "-{ab\n\\\\t\\\\""?
- What is the result of calling "paste(NA, 1:5, collapse="")"?
- What is the meaning of the following **sprintf** format strings: "%s", "%20s", "%-20s", "%f", "%g", "%e", "%5f", "%5.2f%", "%.2f", "%0+5f", and "[%+-5.2f]"?
- What is the difference between **regexpr** and **gregexpr**? What does "g" in the latter name stand for?
- What is the result of a call to "grepl(c("spam", "spammity spam", "aubergines"), "spam")"?
- Is it always the case that ""Aaron" < "Zorro""?
- Why "x < 10" and "x < 10" may return different results?
- If x is a character vector, is "x == x" always equal to TRUE?

- If x and y are character vectors of lengths n and m, respectively, what is the length of the output of "match(x, y)"?
- If x is a named vector, why is there a difference between "x[NA]" and " $x[NA\_character\_]$ "?
- What is the difference between "x == y" and "x % in% y"?

**Exercise 6.7** Let x, y, and z be atomic vectors and a and b be single strings. Generate the same results as "pastena(x, collapse=b)", "pastena(x, y, sep=a)", "pastena(x, y, z, sep=a)", "pastena(x, y, z, sep=a)", "pastena(x, y, z, sep=a)", "pastena(x, y, z, sep=a)", assuming that pastena is a version of paste (which we do not have) that handles missing data in a way consistent with most other functions.

**Exercise 6.8** Based on **list.files** and **glob2rx**, generate the list of all PDFs on your computer. Then, using **file.size** filter out the files smaller than 10 MiB.

**Exercise 6.9** Read a text file that stores a long paragraph of some banal prose. Concatenate all the lines to form a single, long string. Using **strwrap** and **cat**, output the paragraph on the console, nicely formatted to fit an aesthetic width, say, 60 text columns.

**Exercise 6.10** (\*) Implement your own simplified version of basename and dirname.

**Exercise 6.11** (\*) Implement an operation similar to **trimus** using the functions introduced in this chapter.

**Exercise 6.12** (\*) Write a regex that extracts all words from each string in a given character vector.

**Exercise 6.13** (\*) Write a regex that extracts, from each string in a character vector, all:

- integers numbers (signed or unsigned),
- floating-point numbers,
- numbers of any kind (including those in scientific notation),
- #hashtags,
- email@address.es,
- hyperlinks of the form http://... and https://....

**Exercise 6.14** (\*) What do 42i, 42L, and 0x42 stand for?

Exercise 6.15 (\*) Check out stri\_sort in the stringi package (or sort.character in stringx) for a way to obtain an ordering like "a1" < "a2" < "a10" < "a11" < "a100".

**Exercise 6.16** (\*) In **sprintf**, the formatter "%20s" means that if a string is less than 20 bytes long, the remaining bytes will be replaced with spaces. Only for ASCII characters (English letters, digits, some punctuation marks, etc.), it is true that one character is represented by 1 byte. Other Unicode code points can take up between 2 and 4 bytes.

```
cat(sprintf("...%6s..", c("abc", "1!<", "aßc", "qß@")), sep="\n") # aligned?
## .. abc..
## .. 1!<..</pre>
```

(continues on next page)

```
## .. aßc..
## ..qße..
```

Use the **stri\_pad** function from the **stringi** package to align the strings aesthetically. Alternatively, check out **sprintf** from **stringx**.

**Exercise 6.17** (\*) Implement an operation similar to **stri\_pad** from **stringi** using the functions introduced in this chapter.

# **Functions**

R is a *functional language* where functions play first fiddle. Each action we perform reduces itself to a call to some function or a combination thereof.

So far, we have been tinkering with dozens of available functions which are part of base R, with only a few exceptions. They constitute the essential vocabulary that everyone *must* be able to speak fluently.

Any operation, be it **sum**, **sqrt**, or **paste**, when fed with a number of arguments, generates some (hopefully fruitful) return value.

```
sum(1:10) # invoking `sum` on a specific argument
## [1] 55
```

From a user's perspective, each function is merely a tool. To achieve a goal at hand, we do not have to care about what is going on under its hood, i.e., how the inputs are being transformed so that, after a couple of nanoseconds or hours, we can relish what has been yielded. This is very convenient: all we need to know is the function's specification which can be stated, for example, informally, in plain Polish or Malay, on its help page.

In this chapter, we will learn how to write our *own* functions. Using this skill is a good development practice when we expect that some operations are to be executed many times but perhaps on different data.

Also, some R functions are meant to invoke other functions, for instance, on every element in a list or every section of a data frame grouped by a qualitative variable. Thus, it is advisable to learn how we can specify a custom operation to be propagated thereover.

## **Example 7.1** Given some objects (whatever):

```
x1 <- runif(16)
x2 <- runif(32)
x3 <- runif(64)
```

when we want to apply the same action on different data, say, compute the root mean square, instead of retyping almost identical expressions (or a bunch of them) over and over again:

```
sqrt(mean(x1^2))
## [1] 0.6545
```

I DEEP

(continued from previous page)

```
sqrt(mean(x2^2)) # the same second time - borderline okay
## [1] 0.56203
sqrt(mean(x3^2)) # tedious, barbarous, and error-prone
## [1] 0.57206
```

we can generalise the operation to any object like x:

```
rms <-
                         # bound what follows to name `rms`
   function(x)
                         # a function that takes one parameter, `x`
        sqrt(mean(x^2)) # expression to transform the input to yield output
```

and then reuse it on different concrete data instances:

```
rms(x1)
## [1] 0.6545
rms(x2)
## [1] 0.56203
rms(x3)
## [1] 0.57206
```

or even combine it with other function calls:

```
rms(sqrt(c(x1, x2, x3)))^2
## [1] 0.50824
```

Does writing your own functions equal reinventing the wheel? Can everything be found online these days (including on Stack Overflow, GitHub, or CRAN)?

Luckily, it is not the case. Otherwise, data analysts', researchers', and developers' lives would be monotonous, dreary, and uninspiring. Plus, sometimes it is much quicker to write a function from scratch than to get through the whole garbage dump from where, only occasionally, we can dig out some pearls. Not to mention the selfeducative side: we become better programmers by crunching those exercises. We are advocating for minimalism here, remember?

This and many other vital issues in function design will be reflected upon in Chapter

## 7.1 Creating and invoking functions

#### 7.1.1 Anonymous functions

Functions are usually created through the following notation:

```
function(args) body
```

First, args is a (possibly empty) list of comma-separated parameter names which are supposed to act as input variables.

Second, body is a *single* R expression that will be evaluated when the function is called. The value this expression yields will constitute the function's output.

For example, here is a definition of a function that takes no inputs and generates a constant output:

```
function() 1
## function() 1
```

We thus created a *function* object. However, it disappeared immediately thereafter, as we have not used it at all.

Any function, say,  $\mathbf{f}$  can be invoked, i.e., evaluated on concrete data, using the notation  $\mathbf{f}(\arg 1, \ldots, \arg n)$ , where " $\arg 1, \ldots, \arg n$ " are the arguments to be passed to  $\mathbf{f}$ .

```
(function() 1)() # invoking f like f(); here, no arguments are expected
## [1] 1
```

Only now have we obtained a return value.

**Note** (\*) Calling **typeof** on a function object will report "closure" (for user-defined functions), "builtin", or "primitive" (for some built-in, base ones), for the reasons that we explain in more detail in Section 9.5.3:

```
typeof(function() 1)
## [1] "closure"
```

#### 7.1.2 Named functions

Function objects can be bound with names so that they can be referred to multiple times:

<sup>&</sup>lt;sup>1</sup> In short: each function consists of a list of formal arguments, a body, an possibly (if it is a closure) an enclosing environment.

```
one <- function() 1 # one <- (function() 1)</pre>
```

We created an object named **one** (we use bold font to indicate that it is of the type function because functions are so crucial in R). We are very familiar with such a notation, as not since yesterday we are used to writing "x < 1", etc.

Invoking **one**, which can be done by writing **one**(), will yield a return value:

```
one() # (function() 1)()
## [1] 1
```

This output can be used in further computations, for instance:

```
0:2 - one() # 0:2 - (function() 1)(), i.e., 0:2 - 1
## [1] -1 0 1
```

## 7.1.3 Passing arguments to functions

Functions with no arguments are kind of boring, thus let us distil a more highbrowed operation:

```
concat <- function(x, y) paste(x, y, sep="")</pre>
```

Here we have created a mapping whose aim is to concatenate two objects using a specialised call to **paste**. Yours faithfully pleads guilty to multiplying entities needlessly because it *should* not be a problem for anyone to write **paste**(x, y, sep="") each time. Yet, 'tis merely an illustration.

The **concat** function has two *parameters*, "x" and "y". Hence, calling it will require the provision of two *arguments*, which we put within round brackets and separate from each other by commas.

```
u <- 1:5
concat("spam", u) # i.e., concat(x="spam", y=1:5)
## [1] "spam1" "spam2" "spam3" "spam4" "spam5"</pre>
```

**Important** Notice the distinction: *parameters* (*formal arguments*) are abstract, general, or symbolic; "something, anything that will be put in place of x when the function is invoked". Contrastingly, *arguments* (*actual parameters*) are concrete, specific, and real.

During the above call, x in the function's body is precisely "spam" and nothing else. Also, the u object from the caller's environment can be accessed via y in **concat**. Most of the time (yet, see Section 16.3), it is best to think of the function as being fed not with u per se but the value that u is bound to, i.e., "1:5".

Also:

```
x <- 1:5
y <- "spam"
concat(y, x) # concat(x="spam", y=1:5)
## [1] "spam1" "spam2" "spam3" "spam4" "spam5"</pre>
```

This call is still equivalent to concat(x=y, y=x). The argument x is assigned the value of y from the calling environment, "spam". Yes, one x is not the same as the other x, and which is unambiguously defined by the context. Understanding and being able to manipulate such abstractions is basic logic and common sense that everyone should master.

**Exercise 7.2** Write a function **standardise** that takes a numeric vector x as argument and returns its standardised version, i.e., from each element in x, subtract the sample arithmetic mean and then divide it by the standard deviation.

**Note** Recall from Section 2.1.3 that, syntactically speaking, the following are perfectly valid alternatives to the positionally-matched call **concat**("spam", u); see Section 15.4.4 for more details.

```
concat(x="spam", y=u)
concat(y=u, x="spam")
concat("spam", y=u)
concat(u, x="spam")
concat(x="spam", u)
concat(y=u, "spam")
```

However, we recommend to avoid the last two for the sake of the readers' sanity. It is best to provide positionally-matched arguments before the keyword-based ones.

Also, in Section 10.5, we will introduce the (overused) forward-pipe operator, `|>`, which enables the above to be written as ""spam" |> concat(u)".

# 7.1.4 Grouping expressions with curly braces, `{`

We have been informed that a function's body is a *single* R expression whose evaluated value is passed to the user as its output. This may sound restrictive and in contrast with what we have experienced so far. Rarely are we faced with such simple computing tasks, and we have already seen R functions performing quite sophisticated operations.

It turns out that, grammatically, a single R expression can be arbitrarily complex (Chapter 15); we can use curly braces to group many calls that are to be evaluated one after another.

For instance:

```
{
    cat("first expression\n")
    cat("second expression\n")
    # ...
    cat("last expression\n")
}
## first expression
## second expression
## last expression
```

We used four spaces to visually indent the constituents for greater readability (some developers prefer tabs over spaces, others find two or three spaces more urbane, but we do not). This single (compound) expression can now play a role of a function's body.

**Important** The last expression evaluated in a curly-braces delimited block will be considered its output value.

```
x <- {
    1
    2
    3 # <--- last expression: will be taken as the output value
}
print(x)
## [1] 3</pre>
```

**Note** (\*) The above code block can also be written more concisely by replacing newlines with semicolons, although with perhaps some loss in readability:

```
{1; 2; 3}
## [1] 3
```

Section 9.4 will give a few more details about `{`.

**Example 7.3** Here is a version of the above **concat** function, which takes care of a more Chapter 2-style missing values' propagation:

```
concat <- function(a, b)
{
    z <- paste(a, b, sep="")
    z[is.na(a) | is.na(b)] <- NA_character_
    z # last expression in the block - return value
}</pre>
```

Example calls:

```
concat("a", 1:3)
## [1] "a1" "a2" "a3"
concat(NA_character_, 1:3)
## [1] NA NA NA
concat(1:6, c("a", NA_character_, "c"))
## [1] "1a" NA "3c" "4a" NA "6c"
```

Let us appreciate the fact that we could keep the code brief thanks to **paste** and `**I**` implementing the recycling rule.

**Exercise 7.4** Write a function **normalise** that takes a numeric vector x and returns its version shifted and scaled to the [0,1] interval. To do so, subtract the sample minimum from each element, and then divide it by the range, i.e., the difference between the maximum and the minimum. Avoid computing min(x) twice.

**Exercise 7.5** Write a function that applies the robust standardisation of a numeric vector: subtract the median and divide it by the median absolute deviation, 1.4826 times the median of the absolute differences between the values and their median.

**Note** R is an open-source (free, libre) project. Users are not only encouraged to run the software for whatever purpose, but also study and modify its source code without any restrictions. This applies both to functions that we have authored ourselves:

```
print(concat)
## function(a, b)
## {
##     z <- paste(a, b, sep="")
##     z[is.na(a) | is.na(b)] <- NA_character_
##     z # last expression in the block - return value
## }</pre>
```

and to the routines that are part of base R or any other extension packages:

Nevertheless, some functionality might be implemented in compiled programming languages such as C, C++, or Fortran; notice a call to .Internal in the source code of paste, .Primitive in list, or .Call in runif. Therefore, we will sometimes have to dig a bit deeper to access the underlying source code; see Chapter 14 for more details.

# 7.2 Functional programming

R is a *functional* programming language. As such, it shares several common features with other languages that emphasise the role of function manipulation in software development (e.g., Common Lisp, Scheme, OCaml, Haskell, Clojure, F#). Let us explore them now.

## 7.2.1 Functions are objects

R functions were given the right to a *fair go*; they are what we refer to as *first-class citizens*. In other words, our interaction with them is not limited to their invocation; we treat them as any other language object.

• They can be stored inside list objects:

```
list(identity, NROW, sum) # a list storing three functions
## [[1]]
## function (x)
## x
## <environment: namespace:base>
##
## [[2]]
## function (x)
## if (length(d <- dim(x))) d[1L] else length(x)
## <environment: namespace:base>
##
## [[3]]
## function (..., na.rm = FALSE) .Primitive("sum")
```

This is possible owing to the fact that lists, as we recall, can embrace R objects of any kind,

• They can be created and then called inside another function's body:

```
euclidean_distance <- function(x, y)
{
    square <- function(z) z^2 # auxiliary/internal/helper function
    sqrt(sum(square(x-y))) # square root of the sum of squares
}
euclidean_distance(c(0, 1), c(1, 0)) # example call
## [1] 1.4142</pre>
```

This is why we tend to classify functions as representatives of *recursive* types (compare **is.recursive**).

• They can be passed as arguments to other operations:

```
# Replaces missing values with a given aggregate
# of all non-missing elements:
fill_na <- function(x, filler_fun)
{
    missing_ones <- is.na(x) # otherwise, we'd call is.na twice
    replacement_value <- filler_fun(x[!missing_ones])
    x[missing_ones] <- replacement_value
    x
}
fill_na(c(0, NA_real_, NA_real_, 2, 3, 7, NA_real_), mean)
## [1] 0 3 3 2 3 7 3
fill_na(c(0, NA_real_, NA_real_, 2, 3, 7, NA_real_), median)
## [1] 0.0 2.5 2.5 2.0 3.0 7.0 2.5</pre>
```

We call these higher-order functions.

**Note** More advanced techniques, which we will discuss in the third part of the book, will let the functions be:

- returned as other function's outputs,
- · equipped with auxiliary data,
- generated programmatically on the fly,
- modified at runtime.

Below we review the most basic higher-order functions, including do.call and Map.

# 7.2.2 Calling on precomputed arguments with do.call

Notation like f(arg1, ..., argn) has no monopoly over how we are supposed to call a function on a specific sequence of comma-delimited arguments. The list of actual parameters does not have to be hardcoded.

Here is an alternative. We can first prepare a number of objects to be passed as **f**'s inputs, wrap them in a list l, and then invoke **do.call(f,** l) to get the same result.

```
do.call(cbind, words) # column-bind; returns a matrix (explained later)
       Γ,17
             Γ,27
                          Γ,37
## [1,] "spam" "buckwheat" "ham"
                        "spam"
## [2,] "bacon" "quinoa"
## [3,] "eggs" "barley"
                          "spam"
do.call(rbind, words) # row-bind (explained later)
                 [,2]
## [1,] "spam"
                 "bacon" "eggs"
## [2,] "buckwheat" "quinoa" "barley"
## [3,] "ham" "spam"
                           "spam"
```

The length and content of the list passed as the second argument of do.call can be arbitrary (possibly unknown at the time of writing the code). See Section 12.1.2 for more use cases, e.g., ways to concatenate a list of data frames (perhaps produced by some complex chain of commands) into a single data frame.

If elements of the list are named, they will be matched to the corresponding keyword arguments.

```
x <- 2^{(seq(-2, 2, length.out=101))}
plot_opts <- list(col="red", lty="dashed", type="l")</pre>
do.call(plot, c(list(x, log2(x), xlab="x", ylab="log2(x)"), plot_opts))
## (plot display suppressed)
```

Notice that, e.g., plot\_opts can now be reused in further calls to graphics functions. This is very convenient as it avoids repetitions.

## Common higher-order functions

There is an important class of higher-order functions that allow us to apply custom operations on consecutive elements of sequences without relying on loop-like statements, at least explicitly. They can be found in all functional programming languages (e.g., Lisp, Haskell, Scala) and have been ported to various add-on libraries (functools in Python, more recent versions of the C++ Standard Library, etc.) or frameworks (Apache Spark and the like). Their presence reflects the obvious truth that some operations occur more frequently than others.

In particular:

- Map calls a function on each element of a sequence in order to transform:
  - their individual components (just like sqrt, round, or the unary `!` operator in R), or
  - the corresponding elements of many sequences so as to vectorise a given operation elementwisely (compare the binary `+` or paste),
- Reduce (also called accumulate) applies a binary operation to combine consecutive

elements in a sequence, e.g., to generate the aggregates, like, totally (compare sum, prod, all, max) or cumulatively (compare cumsum, cummin),

- Filter creates a subset of a sequence that is comprised of elements that enjoy a given property (which we typically achieve in R by means of the `[` operator),
- **Find** locates the first element that fulfils some logical condition (compare **which**), and so forth.

Below we will only focus on the Map function. The inspection of the remaining ones is left as an exercise. This is because, oftentimes, we can be better off with their more R-ish versions (e.g., using the subsetting operator, `[`).

## 7.2.4 Vectorising functions with Map

In data-centric computing, we are frequently faced with tasks that involve processing each element in a sequence independently, one after another. Such use cases can benefit from vectorised operations like those discussed in Chapter 2, Chapter 3, and Chapter 6.

Unfortunately, most of the functions that we introduced so far cannot be applied on lists. For instance, if we try calling **sqrt** on a list, we will get an error, even if it is a list of numeric vectors only. One way to compute the square root of all elements would be to invoke **sqrt(unlist(...))**. It is a go-to approach if we wish to treat all the list's elements as one sequence. However, this comes at the price of losing the list's structure.

We also discussed some operations that are not vectorised with respect to all their arguments, even though they could have been designed this way, e.g., grepl.

The Map function<sup>2</sup> applies an operation on each element in a vector or the corresponding elements in a number of vectors. In many situations, it may be used as a more elegant alternative to for loops that we will introduce in the next chapter.

First<sup>3</sup>, a call to Map(f, x) yields a list whose *i*-th element is equal to f(x[[i]]) (recall that [[x]]) works on atomic vectors too).

For example:

<sup>&</sup>lt;sup>2</sup> Yes, the author is aware that **Map** was implemented using the slightly more primitive **mapply** but we are not fond of the latter function's having the SIMPLIFY argument set to TRUE by default.

<sup>&</sup>lt;sup>3</sup> This use case scenario can also be programmed using lapply; lapply(x, f, ...) is equivalent to Map(f, x, MoreArgs=list(...)).

```
## $x1
## [1] 1.0000 1.4142 1.7321
##
## $x2
## [1] 0.00000 0.50000 0.70711 0.86603 1.00000
##
## $x3
## [1] 1 0 NA 0 0 1 NA
Map(length, x)
## $x1
## [1] 3
##
## $x2
## [1] 5
##
## $x3
## [1] 7
unlist(Map(mean, x)) # compute three aggregates, convert to an atomic vector
## x1 x2 x3
## 2.0 0.5 NA
Map(function(n) round(runif(n, -1, 1), 1), c(2, 4, 6)) # x is atomic now
## [[1]]
## [1] 0.4 0.8
##
## [[2]]
## [1] 0.5 0.8 -0.1 -0.7
##
## [[3]]
## [1] -0.3 0.0 0.5 1.0 -0.9 -0.7
```

Next, we can vectorise a given function over several parameters. A call to, e.g., Map(f, x, y, z) results in a list whose *i*-th element is equal to f(x[[i]], y[[i]], z[[i]]). Like in the case of, e.g., **paste**, the recycling rule will be applied if necessary.

For example, the following generates **list(seq(1, 6), seq(11, 13), seq(21, 29))**:

```
Map(seq, c(1, 11, 21), c(6, 13, 29))

## [[1]]

## [1] 1 2 3 4 5 6

##

## [[2]]

## [1] 11 12 13

##

## [[3]]

## [1] 21 22 23 24 25 26 27 28 29
```

Moreover, we can get list(seq(1, 40, length.out=10), seq(11, 40, length.out=5), seq(21, 40, length.out=10), seq(31, 40, length.out=5)) by calling:

```
Map(seq, c(1, 11, 21, 31), 40, length.out=c(10, 5))
## [[1]]
## [1] 1.0000 5.3333 9.6667 14.0000 18.3333 22.6667 27.0000 31.3333
## [9] 35.6667 40.0000
##
## [[2]]
## [1] 11.00 18.25 25.50 32.75 40.00
##
## [[3]]
## [1] 21.000 23.111 25.222 27.333 29.444 31.556 33.667 35.778 37.889 40.000
##
## [[4]]
## [1] 31.00 33.25 35.50 37.75 40.00
```

**Note** If we have some additional arguments to be passed to the function applied (which it does not have to be vectorised over), we can wrap them inside a separate list and toss it via the MoreArgs argument (à la do.call).

```
unlist(Map(mean, x, MoreArgs=list(na.rm=TRUE))) # mean(..., na.rm=TRUE)
## x1 x2 x3
## 2.0 0.5 0.4
```

Alternatively, we can always construct a custom anonymous function:

```
unlist(Map(function(xi) mean(xi, na.rm=TRUE), x))
## x1 x2 x3
## 2.0 0.5 0.4
```

**Exercise 7.6** Here is an example list of files (see our teaching data repository<sup>4</sup>) with daily Forex rates:

```
file_names <- c(
    "euraud-20200101-20200630.csv",
    "eurgbp-20200101-20200630.csv",
    "eurusd-20200101-20200630.csv"
)
```

Call **Map** to read each dataset with **scan** and determine each series' minimal, mean, and maximal value.

**Exercise 7.7** Implement your version of the **Filter** function based on a call to **Map**.

<sup>&</sup>lt;sup>4</sup> https://github.com/gagolews/teaching-data/tree/master/marek

## 7.3 Accessing third-party functions

When we indulge in the writing of a software piece, a few questions naturally arise. Is the problem we are facing fairly complex? Has it already been successfully addressed in its entirety? If not, can it, or its parts, be split into manageable chunks? Can it be constructed based on some readily available nontrivial components?

A smart developer is independent but knows when to stand on the shoulders to cry on. Let us explore some ways to reuse the existing function libraries.

## 7.3.1 Using R packages

Most contributed R extensions come in the form of the so-called *add-on packages*, which can include:

- reusable code (e.g., new functions),
- data (which we can exercise on),
- documentation (manuals, vignettes, etc.);

see Section 9.3.2 for more and [59] for all the details.

Most packages are published in the moderated repository that is part of the *Comprehensive R Archive Network* (CRAN<sup>5</sup>). However, there are also other popular sources such as Bioconductor<sup>6</sup> which specialises in bioinformatics.

We call **install.packages**("pkg") to fetch a package **pkg** from a repository (CRAN by default; see, however, the repos argument).

A call to **library**("pkg") loads an indicated package and makes the exported objects available to the user (i.e., attaches it to the search path; see Section 16.2.6).

For instance, in one of the previous chapters, we have mentioned the **gsl** package:

```
# call install.packages("gsl") first
library("gsl") # load the package
poch(10, 3:6) # calls gsl_sf_poch() from GNU GSL
## [1] 1320 17160 240240 3603600
```

Here, **poch** is an object exported by package **gsl**. If we did not call **library**("gsl"), trying to access the former would result in an error.

We could also have accessed the above function without attaching it to the search path using the **pkg**::object syntax, i.e., **gsl**::poch.

**Exercise 7.8** Use the **find** function to determine which packages define **mean**, **var**, **find**, and **Map**. Recall from Section 1.4 where such information can be found in these objects' manual pages.

<sup>5</sup> https://cloud.r-project.org/

<sup>6</sup> https://bioconductor.org/

**Note** For more information about any R extension, call <code>help(package="pkg")</code>. Also, it is advisable to visit the package's CRAN entry at an address like <code>https://CRAN.R-project.org/package=pkg</code> to access some additional information (e.g., vignettes; see also <code>vignette(package="pkg"))</code>. Why waste our time and energy by querying a web search engine that will lead us to some (usually low-quality) middleman when we can acquire authoritative knowledge directly from the source?

Moreover, it is worth exploring various CRAN Task Views<sup>7</sup> that group the packages into topics such as *Genetics*, *Graphics*, and *Optimisation*. They are curated by experts in their relevant fields.

**Important** Frequently, R packages are written in their respective authors' free time, many of whom are volunteers/public servants/enthusiasts who are neither paid for doing this nor it is part of the so-called *their job*. You can show appreciation for their generosity by, e.g., spreading the word about their software by citing them in publications (see **citation**(package="pkg")), talking about them during lunchtime, or mentioning them in (un)social media. You can also help them improve the existing code base by reporting bugs, polishing documentation, proposing new features, or cleaning up the redundant fragments of their APIs. Some readers will become one of them someday (when they come up with something valuable for our community).

#### Default packages

The always-on package **base** is a must-have. It provides us with the most crucial functions (vector addition, **c**, **Map**, **library**). Certain other packages are also loaded by default:

```
getOption("defaultPackages")
## [1] "datasets" "utils" "grDevices" "graphics" "stats"
## [6] "methods"
```

Although this list can technically be changed<sup>8</sup>, in this book we assume that the above are always attached, because it is reasonable to do so. This is why in Section 2.4.5, there was no need to call, for example, **library**("stats") before referring to the **var** and **sd** functions.

On a side note, grDevices and graphics will be discussed in Chapter 13. methods will be mentioned in Section 11.5. datasets brings a few example R objects on which we can exercise our skills. On the other hand, the functions from utils, graphics, and stats already appeared here and there.

<sup>&</sup>lt;sup>7</sup> https://cloud.r-project.org/web/views/

<sup>&</sup>lt;sup>8</sup> (\*) R is greatly configurable: we can have custom ~/.Renviron and ~/.Rprofile files that are processed on R's startup; see help("Startup").

## Source vs binary packages (\*)

R is a free and open project. Therefore, its packages are published primarily in the source form. This way, anyone can study how they work and improve them or reuse parts thereof in different projects.

If we call **install.packages**("path", repos=NULL, type="source"), we should be able to install a package from sources: path can either be pinpointing a directory or a source tarball (see **help**("untar"), most often as a compressed pkg\_version.tar.gz file).

Note that type="source" is the default unless one is on W\*\*\*\*ws or some m\*\*OS boxes; see **getOption**("pkgType"). This is because these two might require additional build tools to be present in the system, especially if a package features C, C++, or Fortran code; see Chapter 14 and Section C.3 of [61]:

- Rtools<sup>9</sup> on W\*\*\*\*ws,
- Xcode Command Line Tools<sup>10</sup> on m\*\*OS.

Because these systems are less developer-oriented, as a courtesy to their users, CRAN also distributes the platform-specific binary versions of the packages (.zip or .tgz files). install.packages will try to fetch them by default.

**Example 7.9** GitLab and GitHub are quite popular hosting platforms. It is very easy to fetch a package's source directly from them. At the time of writing this, the relevant links were, respectively:

- https://gitlab.com/user/repo/-/archive/branch/repo-branch.zip
- https://github.com/user/repo/archive/branch.zip

For example, to download the contents of the master branch in the repository rpackagedemo owned by gagolews, we can call:

```
f <- tempfile() # temporary file name - download destination
download.file("https://github.com/gagolews/rpackagedemo/archive/master.zip",
    destfile=f)</pre>
```

*Next, the contents can be extracted with* **unzip**:

```
t <- tempdir() # temporary directory to extract the files to
(d <- unzip(f, exdir=t)) # returns extracted file paths</pre>
```

The path where the files were extracted can be passed to **install.packages**:

```
install.packages(dirname(d)[1], repos=NULL, type="source")
file.remove(c(f, d)) # clean up
```

**Exercise 7.10** Use the **git2r** package to clone the **git** repository located at https://github.com/

<sup>9</sup> https://cran.r-project.org/bin/windows/Rtools/

<sup>10</sup> https://developer.apple.com/xcode/resources/

gagolews/rpackagedemo.git and install the package published therein from the current R session.

## 7.3.2 Managing dependencies (\*)

The currently-installed add-on packages may be upgraded to their most recent versions available on CRAN (or other indicated repository) by calling **update.packages**.

As a general rule, the more experienced developers we become, the less excited we get about the *new*. Sure, bug fixes and some well-thought-of additional features are usually welcome. Still, just we wait until someone updates the package API for the n-th time,  $n \ge 2$ , which will break our program that used to work flawlessly for so long.

Hence, when designing software projects (see Chapter 9 for more details), we must ask ourselves the ultimate question: do we really need to import that package with lots of dependencies from which we will just use only about 3–5 functions? Wouldn't it be better to write our own version of some functionality (and learn something new, exercise our brain, etc.), or call a mature terminal-based tool?

Otherwise, as all the historical versions of all the packages are archived on CRAN<sup>11</sup>, some software dependency management can easily be conducted by storing different releases of packages in different directories (only one version of a package can be loaded at a time though). This way, we can create an isolated environment for the addons.

To fetch the locations where packages are sought (in this very order), call:

```
.libPaths()
## [1] "/home/gagolews/R/x86_64-pc-linux-gnu-library/4.3"
## [2] "/usr/local/lib/R/site-library"
## [3] "/usr/lib/R/site-library"
## [4] "/usr/lib/R/library"
```

The same function can be used to add new folders to the search path; see also the environment variable R\_LIBS\_USER (e.g., help("Sys.setenv")). The install.packages function will honour them as target directories; see its lib parameter for more details.

Moreover, the packages may deposit some auxiliary data on the user's machine. Therefore, it might be worthwhile to set the following directories (via the corresponding environment variables) relative to the current project:

```
tools::R_user_dir("pkg", "data") # R_USER_DATA_DIR
## [1] "/home/gagolews/.local/share/R/pkg"
tools::R_user_dir("pkg", "config") # R_USER_CONFIG_DIR
## [1] "/home/gagolews/.config/R/pkg"
tools::R_user_dir("pkg", "cache") # R_USER_CACHE_DIR
## [1] "/home/gagolews/.cache/R/pkg"
```

<sup>11</sup> https://cran.r-project.org/src/contrib/Archive/

## 7.3.3 Calling external programs

Many tasks can naturally be accomplished by calling external programs. Such an approach is particularly natural on UNIX-like systems, which classically follow modular, minimalist design patterns. There are many tools at a developer's hand and each tool is specialised at solving a single, well-defined problem.

Apart from the many standard UNIX commands<sup>12</sup>, we can consider, for example:

- pandoc<sup>13</sup> converts documents between markup formats, e.g., Markdown, reStructuredText, LaTeX, LibreOffice Writer, EPUB;
- pdflatex, xelatex, and lualatex compile LaTeX documents to PDF;
- **convert** (from **ImageMagick**<sup>14</sup>) applies various operations on bitmap graphics (scaling, cropping, conversion between formats);
- graphviz<sup>15</sup> and PlantUML<sup>16</sup> can be used to create various graphs and diagrams;
- jupyter-nbconvert converts Jupyter<sup>17</sup> notebooks (see Section 1.2.5) to other formats such as LaTeX, HTML, Markdown, etc.;
- python, perl, ... can be called to perform tasks that can be expressed more easily in languages other than R;

and so forth.

The good news is that R can not only be called from the system shell (in an interactive or batch mode; see Section 1.2). It can also serve well as a glue language.

The **system2** function can be used to invoke any system command. Communication between such programs can be done using, e.g., intermediate text, JSON, CSV, XML, or any other files. The stdin, stdout, and stderr arguments can control the redirection of the standard I/O streams.

```
system2("pandoc", "-s input.md -o output.html")
system2("bash", "-c 'for i in `seq 1 2 10`; do echo $i; done'", stdout=TRUE)
## [1] "1" "3" "5" "7" "9"
system2("python3", "-", stdout=TRUE,
    input=c(
    "import numpy as np",
    "print(repr(np.arange(5)))"
    ))
## [1] "array([0, 1, 2, 3, 4])"
```

On a side note, the current working directory can be read and changed through a call

<sup>12</sup> https://en.wikipedia.org/wiki/List\_of\_Unix\_commands

<sup>13</sup> https://pandoc.org/

<sup>14</sup> https://imagemagick.org/

<sup>15</sup> https://graphviz.org/

<sup>16</sup> https://plantuml.com/

<sup>17</sup> https://jupyter.org/

to **getwd** and **setwd**, respectively. It is the directory where the current R session was started.

**Important** Relying on **system2** assumes that the commands it refers to are available on the target platform. Hence, it might not be portable unless additional assumptions are made (e.g., that a user runs some UNIX-like system and that certain libraries are installed therein). We strongly recommend GNU/Linux or FreeBSD for both software development and production use, as they are free, open, developer-friendly, user-loving, reliable, ethical, and sustainable.

## 7.3.4 A note on interfacing C, C++, Python, Java, etc. (\*)

Most stand-alone data processing algorithms are implemented in compiled, slightly lower-level programming languages. This usually makes them faster and more reusable in other environments. For instance, an industry-standard library is often written in very portable C, C++, or Fortran and has some bindings available for easier access from within R, Python, Julia, etc. This is the case with FFTW, LIBSVM, mlpack, OpenBLAS, ICU, and GNU GSL, amongst many others.

For basic ways to interact with such compiled code, see Chapter 14.

Also, the **rJava** package can dynamically create JVM objects and access their fields and methods. Similarly, **reticulate** can be used to access Python objects, including **numpy** arrays and **pandas** data frames (but see also the **rpy2** package for Python).

**Important** We should not feel obliged to use R in all the parts of a data processing pipeline. Some activities can be expressed more naturally in other languages/environments (e.g., parse raw data and create an SQL database in Python but visualise it in R). We can use other tools as the glue language (including R, Python, or Bash) to steer the data flow in the right direction.

#### 7.4 Exercises

**Exercise 7.11** *Answer the following questions:* 

- What is the result of "x <-2; x <- function(x)  $x^2$ ; x(x)?
- How to write a function that returns two objects?
- What is a higher-order function?
- What are the use cases of do.call?
- Why a call to **Map** is not necessary in the expression "**Map(paste**, x, y, z)"?

- What is the difference between Map(mean, x, na.rm=TRUE) and Map(mean, x, More-Args=list(na.rm=TRUE))?
- What do we mean when we write stringx::sprintf?
- How to get access to the vignettes (tutorials, FAQs, etc.) of the data.table and dplyr packages? Why perhaps 95% of R users would just googleit, and what is sub-optimal about this strategy?
- What is the difference between a source and a binary package?
- How to update the **base** package?
- How to ensure that we will always run an R session with only specific versions of a set of packages?

**Exercise 7.12** Write a function that computes the Gini index of a vector of positive integers x, which, assuming  $x_1 \le x_2 \le ... \le x_n$ , is equal to:

$$G(x_1, \dots, x_n) = \frac{\sum_{i=1}^{n} (n-2i+1)x_i}{(n-1)\sum_{i=1}^{n} x_i}.$$

**Exercise 7.13** Implement a function between(x, a, b) that verifies whether each element in x is in the [a, b] interval. Return a logical vector of the same length as x. Ensure the function is correctly vectorised with respect to all the arguments and handles missing data correctly.

**Exercise 7.14** Write your version of the strrep function called dup.

```
dup <- ...to.do...
dup(c("a", "b", "c"), c(1, 3, 5))
## [1] "a"  "bbb"  "ccccc"
dup("a", 1:3)
## [1] "a"  "aa"  "aaa"
dup(c("a", "b", "c"), 4)
## [1] "aaaa"  "bbbb"  "cccc"</pre>
```

**Exercise 7.15** Given a list x, generate its sublist with all the elements equal to NULL removed.

**Exercise 7.16** *Implement your version of the built-in sequence function.* 

**Exercise 7.17** Using Map, how can we generate window indexes like:

```
## [[1]]
## [1] 1 2 3
##
## [[2]]
## [1] 2 3 4
##
## [[3]]
## [1] 3 4 5
##
```

(continued from previous page)

```
## [[4]]
## [1] 4 5 6
```

Write a function **windows**(k, n) that yields k index windows with elements between 1 and n (the above example is for k = 3 and k = 6).

**Exercise 7.18** Implement a function movstat(f, x, k) that computes, using Map, a given aggregate f of each k consecutive elements in x. For instance:

```
movstat <- ...to.do...

x <- c(1, 3, 5, 10, 25, -25) # example data

movstat(mean, x, 3) # 3-moving mean

## [1] 3.0000 6.0000 13.3333 3.3333

movstat(median, x, 3) # 3-moving median

## [1] 3.0000 6.0000 13.3333 3.3333
```

**Exercise 7.19** Write a function to extract all q-grams,  $q \ge 1$ , from a given character vector. Return a list of character vectors. For example, 2-grams (bigrams) in "abcd" are: "ab", "bc", "cd".

**Exercise 7.20** Recode a character vector with a small number of distinct values to a vector where each unique code is assigned a positive integer from 1 to k. Example calls and the corresponding expected results:

```
recode <- ...to.do...

recode(c("a", "a", "a", "b", "b"))

## [1] 1 1 1 2 2

recode(c("x", "z", "y", "x", "y", "x"))

## [1] 1 3 2 1 2 1
```

**Exercise 7.21** Implement a function that returns the number of occurrences of each unique element in a given atomic vector. The return value should be a numeric vector equipped with a names attribute.

```
count <- ...to.do...
count(c(5, 5, 5, 5, 42, 42, 954))
##    5    42   954
##    4    2    1
count(c("x", "z", "y", "x", "y", "x", "w", "x", "y", NA_character_))
##    w    x    y    z   <NA>
##    1    5    3    1    1
```

Hint: use match and tabulate.

**Exercise 7.22** Implement a function that extends upon the built-in **duplicated**, indicating which occurrence (starting from the beginning of the vector) of a repeated value a given value constitutes.

```
duplicatedn <- ...to.do...
duplicatedn(c("a", "a", "b", "b"))
## [1] 1 2 3 1 2
duplicatedn(c("x", "z", "y", "x", "y", "x", "w", "x", "x", "y", "z"))
## [1] 1 1 1 2 2 3 1 4 5 3 2</pre>
```

**Exercise 7.23** Based on a call to **Map**, implement a function  $my_split$  such that, given a vector x and an atomic vector y of the same length as x,  $my_split(x, y)$  yields the same result as split(x, y).

**Exercise 7.24** Extend  $my_split$  to handle the second argument being a list of the form list(y1, y2, ...) representing the product of many levels. If the ys are of different lengths, apply the recycling rule.

**Exercise 7.25** Implement  $my_unsplit$  being your version of the built-in unsplit. Ensure it holds  $my_unsplit(split(x, g), g) == x$ for x and g of the same lengths.

**Exercise 7.26** Write a function that takes as arguments: (a) an integer n, (b) a numeric vector x of length k and no duplicated elements, (c) a vector of probabilities p of length k. Verify that  $p_i \geq 0$  for all i and  $\sum_{i=1}^k p_i \approx 1$ . Based on a random number generator from the uniform distribution on the unit interval, generate n independent realisations of a random variable X such that  $\Pr(X = x_i) = p_i$  for  $i = 1, \ldots, k$ . Hint: to obtain a single value:

- 1. generate  $u \in [0, 1]$ ,
- 2. find  $m \in \{1, ..., k\}$  such that  $u \in \left(\sum_{j=1}^{m-1} p_j, \sum_{j=1}^m p_j\right)$ ,
- 3. the result is then  $x_m$ .

**Exercise 7.27** Write a function that takes as arguments: (a) an increasingly sorted vector x of length n, (b) any vector y of length n, (c) a vector z of length k and elements in  $[x_1, x_n)$ . Let f be the piecewise linear spline that interpolates the points  $(x_1, y_1), \ldots, (x_n, y_n)$ . Return a vector w of length k such that  $w_i = f(z_i)$ .

**Exercise 7.28** (\*) Write functions **dpareto**, **ppareto**, **qpareto**, and **rpareto** that implement the basic functions related to the Pareto distribution; compare Section 2.3.4.

# Flow of execution

The **ifelse** and **Map** functions are potent. However, they allow us to process only the *consecutive* elements in a vector.

Thus, let us (finally!) discuss different ways to alter a program's control flow manually, based on some criterion, and to evaluate the same expression many times, but perhaps on different data. Before proceeding any further, let us, however, contemplate the fact that we have managed to do without them for such a long time, despite the fact that the data processing exercises we learnt to solve were far from trivial.

#### 8.1 Conditional evaluation

Life is full of surprises, so it would be nice if we could adapt to whatever the circumstances are going to be.

The following evaluates a given expression if and only if a logical condition is true.

```
if (condition) expression
```

When performing some other\_expression is preferred rather than doing nothing in the case of the condition's being false, we can write:

```
if (condition) expression else other_expression
```

For instance:

```
(x <- runif(1)) # to spice things up
## [1] 0.28758
if (x > 0.5) cat("head") else cat("tail")
## tail
```

Many expressions can, of course, be grouped with curly braces, `{`.

```
if (x > 0.5) {
    cat("head")
    x <- 1</pre>
```

(continues on next page)

(continued from previous page)

```
} else {
   cat("tail")
    x <- 0
}
## tail
print(x)
## [1] 0
```

Important At the top level, we should not put a new line before else. Otherwise, we will get an error like Error: unexpected 'else' in "else". This is because the interpreter enthusiastically executes the statements read line by line as soon as it regards them as stand-alone expressions. In this case, we first get an if without else, and then, separately, a dangling **else** without the preceding **if**.

This does not happen when a conditional statement is part of an expression group because the latter is read in its entirety.

```
function (x)
{ # opening bracket - start
   if (x > 0.5)
        cat("head")
                      # not dandling, because {...} is read as a whole
   else
        cat("tail")
} # closing bracket - expression ends
```

As an exercise, try removing the curly braces and see what happens.

#### Return value 8.1.1

`if` is a function (compare Section 9.4). Hence, it has a return value: the result of evaluating the conditional expression.

```
(x <- runif(1))
## [1] 0.28758
y <- if (x > 0.5) "head" # no else
print(y)
## NULL
y <- if (x > 0.5) "head" else "tail"
print(y)
## [1] "tail"
```

This is particularly useful when a call to `if` is the last expression in the code block constituting a function's body.

```
mint <- function(x)
{
    if (x > 0.5) # the last expression (actually, the only one)
        "head" # this can be the return value...
    else
        "tail" # or this one, depending on the condition
}

mint(x)
## [1] "tail"
unlist(Map(mint, runif(5)))
## [1] "tail" "head" "tail" "head" "head"
```

**Example 8.1** Add-on packages can be loaded using **requireNamespace**. Contrary to **library**, the former does not fail when a package is not available. Also, it does not attach it to the search path; see Section 16.2.6.

Instead, it returns a logical value indicating if the package is available for use. This can be helpful inside other functions where the availability of some additional features depends on the user environment's configuration:

```
process_data <- function(x)
{
    if (requireNamespace("some_extension_package", quietly=TRUE))
        some_extension_package::very_fast_method(x)
    else
        normal_method(x)
}</pre>
```

#### 8.1.2 Nested ifs

If more than two test cases are possible, i.e., when we need to go beyond either condition or !condition, then we can use the following construction:

```
if (a) {
    expression_a
} else if (b) {
    expression_b
} else if (c) {
    expression_c
} else {
    expression_else
}
```

This evaluates all conditions a, b, ... (in this order) until the first positive case is found and then executes the corresponding expression.

It is worth stressing that the above is nothing else than a series of nested **if** statements but written in a more readable<sup>1</sup> manner:

```
if (a) {
    expression_a
} else {
    if (b) {
     expression_b
    } else {
        if (c) {
            expression_c
        } else {
            expression_else
        }
    }
}
```

**Exercise 8.2** Write a function named **sign** that determines if a given numeric value is "positive", "negative", or "zero".

#### 8.1.3 Condition: Either TRUE or FALSE

**if** expects a condition that is a single, well-defined logical value, either TRUE or FALSE. Thence, problems may arise when this is not the case.

If the condition is of length not equal to one, we get an error:

```
if (c(TRUE, FALSE)) cat("spam")
## Error in if (c(TRUE, FALSE)) cat("spam"): the condition has length > 1
if (logical(0)) cat("bacon")
## Error in if (logical(0)) cat("bacon"): argument is of length zero
```

We cannot pass a missing value either:

```
if (NA) cat("ham")
## Error in if (NA) cat("ham"): missing value where TRUE/FALSE needed
```

**Important** If we think that we are immune to writing code violating the above constraints, just we wait until the condition becomes a function of data for which there is no sanity-checking in place.

<sup>&</sup>lt;sup>1</sup> (\*) Somewhat related is the **switch** function which relies on the lazy evaluation of its arguments (Chapter 17). Still, it can always be replaced by a series of **if**s.

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```
mint(0.25)
## [1] "T"
mint(runif(5))
## Error in if (x > 0.5) "H" else "T": the condition has length > 1
mint(log(rnorm(1))) # not obvious, only triggered sometimes
## Warning in log(rnorm(1)): NaNs produced
## Error in if (x > 0.5) "H" else "T": missing value where TRUE/FALSE needed
```

In Chapter 9, we will be particularly interested in ways to ensure input data integrity so that situations such as above will either fail gracefully or succeed bombastically.

Here, we should probably ensure that x is a single finite numeric value. Alternatively, we can test whether all(x > 0.5, na.rm=TRUE).

Interestingly, objects other that logical are accepted: they will be coerced if needed.

```
x <- 1:5
if (length(x)) # i.e., length(x) != 0, but way less readable
    cat("length is not zero")
## length is not zero</pre>
```

Recall that coercion of numeric to logical yields FALSE if and only if the original value is zero.

#### 8.1.4 Short-circuit evaluation

Especially for formulating logical conditions in **if** and **while** (see below), we have the *scalar* `||` (alternative) and `&&` (conjunction) operators.

```
FALSE || TRUE

## [1] TRUE

NA || TRUE

## [1] TRUE
```

Contrary to their vectorised counterparts (`|` and `&`), the scalar operators are lazy (Chapter 17) in the sense that they evaluate the first operand and then determine if the computing of the second one is necessary (because, e.g., FALSE && whatever is always FALSE anyway).

Therefore,

```
if (a && b) expression
```

is equivalent to:

```
if (a) {
   if (b) { # compute b only if a is TRUE
        expression
    }
}
```

and:

```
if (a || b)
    expression
```

corresponds to:

```
if (a) {
   expression
} else if (b) { # compute b only if a is FALSE
   expression
}
```

For instance, "is.vector(x) && length(x) > 0 && x[[1]] > 0" is a safe test that takes into account that "x[[1]]" has only the desired meaning for objects that are not nonempty vectors.

Some other examples:

```
{cat("spam"); FALSE} || {cat("ham"); TRUE} || {cat("cherries"); FALSE}
## spamham
## [1] TRUE
{cat("spam"); TRUE} && {cat("ham"); FALSE} && {cat("cherries"); TRUE}
## spamham
## [1] FALSE
```

Recall that the expressions within the curly braces are evaluated one after another and that the result is determined by the last value in the series.

**Exercise 8.3** Study the source code of **isTRUE** and **isFALSE** and determine if these functions could be useful in formulating the conditions within the if expressions.

#### **Exception handling** 8.2

Exceptions are exceptional, but they may happen and break things. For instance, when the internet connection drops while we try to download a file, an optimisation algorithm fails to converge, we just have a bug in our code, or:

```
read.csv("/path/to/a/file/that/does/not/exist")
## Warning in file(file, "rt"): cannot open file '/path/to/a/file/that/does/
## not/exist': No such file or directory
## Error in file(file, "rt"): cannot open the connection
```

Three types of *conditions* are frequently observed:

- errors they stop the flow of execution,
- warnings not critical, but can be turned into errors (see warn in option),
- messages they transmit some diagnostic information.

They can be manually triggered using the **stop**, warning, and message functions.

Errors (but warnings too) can be handled by means of the **tryCatch** function, amongst others.

```
tryCatch({
                     # block of expressions to execute, until an error occurs
        cat("a\n")
        stop("b")
                     # error - breaks the linear control flow
        cat("c\n")
   },
   error = function(e) { # executed immediately upon an error
        cat(sprintf("error: %s\n", e[["message"]]))
   }.
    finally = { # always executed at the end, regardless of error occurrence
        cat("finally!\n")
   }
)
## a
## error: b
## finally!
```

The two other conditions can be ignored by calling **suppressWarnings** and **suppress-Messages**.

```
log(-1)
## Warning in log(-1): NaNs produced
## [1] NaN
suppressWarnings(log(-1)) # yeah, yeah, we know what we're doing
## [1] NaN
```

**Exercise 8.4** At the time of writing of this book, the **data.table** package emits a message upon attachment. Call **suppressMessages** to silence it. However, consecutive calls to **library** do not reload an already loaded package. Therefore, the message will only be seen once per R session.

Related functions include **stopifnot** discussed in Section 9.2 and **on.exit** mentioned in Section 17.4; see Section 9.3.4 for some code debugging tips.

#### Repeated evaluation 8.3

And now for something completely different... time for the elephant in the room!

We have been able to do without loops so far (and will be quite all right in the second part of the book, too), because many data processing tasks can be written in terms of vectorised operations such as `+`, sqrt, sum, `[`, Map, and Reduce. Oftentimes, compared to their loop-based counterparts, they are more readable and efficient. We will explore this in the exercises below.

However, at times, using an explicit while or for loop might be the only natural way of solving a problem, for instance, when processing chunks of data streams. Also, an explicitly "looped" algorithm may occasionally have better<sup>2</sup> time or memory complexity.

#### while 8.3.1

if considers a given logical condition and thus determines whether to execute a given statement. On the other hand,

```
while (condition) # single TRUE or FALSE, as in `if`
   expression
```

evaluates a given expression as long as the logical condition is true. Therefore, it is advisable to make the condition dependent upon some variable that the expression can modify.

```
i <- 1
while (i <= 3) {
    cat(sprintf("%d, ", i))
    i < -i + 1
}
## 1, 2, 3,
```

Nested loops are possible, too:

```
i <- 1
while (i <= 2) {
    i <- 1
    while (j <= 3) {
        cat(sprintf("%d %d, ", i, j))
        i < -i + 1
    cat("\n")
```

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<sup>&</sup>lt;sup>2</sup> In such cases, it will often benefit from a rewrite in C or C++; see Chapter 14.

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```
i <- i + 1
}
## 1 1, 1 2, 1 3,
## 2 1, 2 2, 2 3,
```

**Example 8.5** Implement a simple linear congruential pseudorandom number generator that, given some seed  $X_0 \in [0, m)$ , outputs a sequence  $(X_1, X_2, ...)$  defined by:

$$X_i = (aX_{i-1} + c) \mod m,$$

with, e.g., a = 75, c = 74, and  $m = 2^{16} + 1$  (here, mod is the division reminder, `%\`). This generator has poor statistical properties and its use in practice is discouraged. In particular, after some number of operations k, we will find a cycle such that  $X_k = X_1, X_{k+1} = X_2, ...$ 

#### 8.3.2 for

The for-each loop:

```
for (name in vector)
  expression
```

takes each element, from the beginning to the end, in a given vector, assigns it some name, and evaluates the expression.

Example:

```
fridge <- c("spam", "spam", "bacon", "eggs")
for (food in fridge)
    cat(sprintf("%s, ", food))
## spam, spam, bacon, eggs,</pre>
```

Another example:

```
for (i in 1:length(fridge)) # better: seq_along(fridge), see below
    cat(sprintf("%s, ", fridge[i]))
## spam, spam, bacon, eggs,
```

One more:

```
for (i in 1:2) {
    for (j in 1:3)
        cat(sprintf("%d %d, ", i, j))
    cat("\n")
}
## 1 1, 1 2, 1 3,
## 2 1, 2 2, 2 3,
```

The iterator still exists after the loop's watch has ended:

```
print(i)
## [1] 2
print(j)
## [1] 3
```

#### Important Writing:

```
for (i in 1:length(x))
    print(x[i])
```

is not necessarily safe, because if x is an empty vector, then:

```
x <- logical(0)
for (i in 1:length(x)) print(x[i])
## [1] NA
## logical(0)</pre>
```

Recall from Chapter 5 that x[1] tries to access an out-of-bounds element here, and x[0] returns nothing.

We generally suggest replacing 1: length(x) with  $seq_along(x)$  or  $seq_len(length(x))$ . wherever possible.

**Note** The model **for** loop above is roughly equivalent to:

```
name <- NULL
tmp_vector <- vector
tmp_iter <- 1
while (tmp_iter <= length(tmp_vector)) {
    name <- tmp_vector[[tmp_iter]]
    expression
    tmp_iter <- tmp_iter + 1
}</pre>
```

Note that the tmp\_vector is determined before the loop itself. Hence, any changes to the vector will not influence the execution flow. Also, the loop can be applied on lists as well due to the use of `[[`.

**Example 8.6** Let x be a list and f be a function. The following code generates the same result as Map(f, x):

```
n <- length(x)

(continues on next page)
```

(continued from previous page)

```
ret <- vector("list", n) # a new list of length `n`
for (i in seq_len(n))
    ret[[i]] <- f(x[[i]])</pre>
```

**Example 8.7** Let x and y be two lists and f be a function. Here is the most basic version of Map(f, x, y).

```
nx <- length(x)
ny <- length(y)
n <- max(nx, ny)
ret <- vector("list", n)
for (i in seq_len(n))
    ret[[i]] <- f(x[[((i-1)%%nx)+1]], y[[((i-1)%%ny)+1]])</pre>
```

Note that x and y might be of different lengths. Feel free to upgrade the above code by adding a warning like the longer argument is not a multiple of the length of the shorter one. Also, rewrite it without using the modulo operator, `%\cdot`.

#### 8.3.3 break and next

**break** can be used to escape the current loop. **next** skips the remaining expressions and advances to the next iteration (where the testing of the logical condition occurs).

Here is a rather random example:

```
x <- runif(1000)
s <- 0
for (e in x) {
    if (e > 0.1)
        next
    print(e)
    if (e < 0.01)
        break
    s <- s + e
}
## [1] 0.045556
## [1] 0.04206
## [1] 0.024614
## [1] 0.045831
## [1] 0.094841
## [1] 0.00062477
print(s)
## [1] 0.2529
```

Computes the sum of the elements in x that are less than or equal to 0.1 from the beginning, stopping at the first element less than 0.01.

We have used a frequently occurring design pattern:

```
for (e in x) {
    if (condition)
        next

many_statements...
}
```

which is equivalent to:

```
for (e in x) {
    if (!condition) {
        many_statements...
    }
}
```

but which avoids introducing a nested block of expressions.

**Note** (\*) There is a third loop type,

```
repeat expression
```

which is a shorthand for

```
while (TRUE)
expression
```

i.e., it is a possibly infinite loop. Such loops are valuable when implementing situations such as *do-stuff-until-a-thing-happens*, e.g., when we want to execute a command at least once.

```
i <- 1
repeat { # while (TRUE)
    # simulate dice casting until we throw "1"
    if (runif(1) < 1/6) break # not an infinite loop after all
    i <- i+1
}
print(i)
## [1] 6</pre>
```

```
j <- 1
while (j <= 10) {
    if (j %% 2 == 0) next
    print(j)
    j <- j + 1
}</pre>
```

#### **Exercise 8.9** What about this one?

#### 8.3.4 return

**return**, when called from within a function, immediately yields a specified value and goes back to the caller.

For example, here is a simple recursive function that flattens a given list:

```
my_unlist <- function(x)
{
    if (is.atomic(x))
        return(x)

# so if we are here, x is definitely not atomic
    out <- NULL
    for (e in x)
        out <- c(out, my_unlist(e))

    out # or return(out); it's the last expression anyway, so not necessary
}

my_unlist(list(list(list(1, 2), 3), list(4, list(5, list(6, 7:10)))))
## [1] 1 2 3 4 5 6 7 8 9 10</pre>
```

**return** is a function: the round brackets are obligatory.

# 8.3.5 A note on time and space complexity of algorithms (\*)

Analysis of algorithms can give us a rough estimate of their run times or memory consumption as a function of the input data size, especially for *big* data (e.g., [14, 40]).

In scientific computing and data science, we often deal with vectors (sequences) or matrices/data frames (tabular data). Therefore, we might be interested in determining how many *primitive operations* need to be performed as a function of their length n or the number of rows n and columns m, respectively.

For instance, the O (Big-Oh) notation can express the upper bounds for time/resource consumption in asymptotic cases. For instance, we say that the time complexity is  $O(n^2)$ , if for large n, the number of operations to perform will be proportional to at most the square of the vector size (more precisely, there exists m and C>0 such that for all n>m, the number of operations is  $\leq Cn^2$ ).

Therefore, if we have two algorithms that solve the same task, one that has  $O(n^2)$  time complexity, and other of  $O(n^3)$ , it is better to choose the former because for large problem sizes, we expect it to be faster.

Moreover, whether time grows proportionally to  $\log n$ ,  $\sqrt{n}$ , n,  $n \log n$ ,  $n^2$ ,  $n^3$ , or  $2^n$ , can be informative in predicting how big the data can be if we have a fixed deadline or not too much space left on the disk.

**Exercise 8.10** The **hclust** function determines a hierarchical clustering of a dataset. It is fed with an object that stores the distance between all the pairs of input points. There are n(n-1)/2 (i.e.,  $O(n^2)$ ) unique point pairs for any given n. One numeric scalar (double type) takes 8 bytes of storage. If you have 16 GB of RAM, what is the largest dataset that you can cluster on your machine using this function?

Oftentimes, we can learn about the time or memory complexity of the functions we use from their documentation; see, e.g., help("findInterval").

**Example 8.11** A course in data structures in algorithms, which this one is not, will give us plenty of opportunities to implement many algorithms ourselves. This way, we can gain a lot of insights and intuitions.

For instance, this is a O(n)-time algorithm:

```
for (i in seq_len(n))
  expression
```

and this is one runs in  $O(n^2)$  time:

```
for (i in seq_len(n))
  for (j in seq_len(n))
      expression
```

as long as, of course, the expression is rather primitive (e.g., operations on scalar variables).

R is a very expressive language. Hence, quite complex and lengthy operations can look pretty innocent. After all, it is a glue language for rapid prototyping.

For example:

```
for (i in seq_len(n))
    for (j in seq_len(n))
    z <- z + x[[i]] + y[[j]]</pre>
```

can be seen as  $O(n^3)$  if each element in the lists x and y as well as z itself are atomic vectors of length n.

Similarly,

```
Map(mean, x)
```

is  $O(n^2)$  if x is a list of n atomic vectors, each of length n.

**Note** A quite common statistical scenario involves generating a data buffer of a fixed size:

```
ret <- c()
for (i in n)
    ret[[i]] <- generate_data(i) # here: ret[[length(ret)+1]] <- ...</pre>
```

This notation, however, involves growing the ret array in each iteration. Luckily, since R version 3.4.0, each such size extension has amortised O(1) time because some more memory is internally reserved for its prospective growth (dynamic arrays; see, e.g., Chapter 17 of [14]).

However, it would still be better to pre-allocate the output vector and grant it the desired final size already upon creation. We can construct vectors of specific lengths and types in an efficient way (more efficient than with rep) by calling:

```
numeric(3)
## [1] 0 0 0
numeric(0)
## numeric(0)
logical(5)
## [1] FALSE FALSE FALSE FALSE
character(2)
## [1] "" ""
vector("numeric", 8)
## [1] 0 0 0 0 0 0 0 0
vector("list", 2)
## [[1]]
## NULL
##
## [[2]]
## NULL
```

**Note** Not all data fit into memory, but it does not mean that we should start installing Apache Hadoop and Spark immediately. Some datasets can be processed on a chunkby-chunk basis.

R enables data stream handling (some can be of infinite length) through file connections, for example:

Many functions support reading from/writing to already established connections of different types, e.g., **file**, **gzfile**, **textConnection**, batch-by-batch.

A frequent scenario involves reading a very large CSV, JSON, or XML file only by thousands of lines/records at a time, parsing and cleansing them, and exporting them to SQL databases (which we will exercise in Chapter 12).

#### 8.4 Exercises

From now on, we must stay alert. Many, if not all, of the following tasks, can still be implemented without the explicit use of the R loops but based only on the operations covered in the previous chapters. If this is the case, try implementing both the looped and loop-free versions. Use microbenchmark::microbenchmark or proc.time to compare their run times<sup>3</sup>.

## **Exercise 8.12** Answer the following questions:

- Let x be a numeric vector. When does if(x > 0) ... yield a warning? When does it give an error? How to prevent this?
- What is the dangling **else**?
- What happens if you put if as the last expression in a curly braces block within a function's body?
- Why do we say that `&&` and `//` are lazy? What are their use cases?
- What is the difference between `&&` and `&`?
- Can while always be replaced with for? What about the other way around?
- What is wrong with "return (1+2)\*3"?

<sup>&</sup>lt;sup>3</sup> It might be the case that a **for**-based solution is faster (e.g., for larger objects) because of the use of a more efficient algorithm. Such cases will benefit from a rewrite in C or C++ (Chapter 14).

**Exercise 8.13** Verify which of the following can be safely used as logical conditions in **if** statements. If that is not the case for all x, y, ..., determine the additional conditions that must be imposed to make them valid.

```
x == 0,
x[y] > 0,
any(x>0),
match(x, y),
any(x %in% y).
```

**Exercise 8.14** What can go wrong in the following code chunk, depending on the type and form of x? Consider as many scenarios as possible.

```
count <- 0
for (i in 1:length(x))
    if (x[i] > 0)
        count <- count + 1</pre>
```

**Exercise 8.15** Implement  $shift_left(x, n)$  and  $shift_right(x, n)$ . The former function gets rid of the first n observations in x and adds n missing values at the end of the resulting vector, e.g.,  $shift_left(c(1, 2, 3, 4, 5), 2)$  is c(3, 4, 5, NA, NA). On the other hand,  $shift_right(c(1, 2, 3, 4, 5), 2)$  is c(NA, NA, 1, 2, 3).

**Exercise 8.16** Implement your version of diff.

**Exercise 8.17** Write a function that determines the longest ascending trend in a given numeric vector, i.e., the length of the longest subsequence of consecutive increasing elements. For example, the input c(1, 2, 3, 2, 1, 2, 3, 4, 3) should yield 4.

**Exercise 8.18** Implement the functions that round down and round up each element in a numeric vector to a number of decimal digits.

This concludes the first part of this magnificent book.

Part II

Deeper

# Designing functions

In Chapter 7, we learnt how to write our own functions. This skill is vital to enforcing the good development practice of avoiding code repetition: running the same command sequence on different data.

This chapter is devoted to designing such reusable modules to make them easier to use, test, and maintain. We also provide some more technical details, which were not of the highest importance upon our first exposure to this topic but are crucial to our better understanding of how R works.

## 9.1 Principles of sustainable design

Fine design is more art than science. As usual in real life, we will need to make many compromises. This is because improving things with regard to one criterion sometimes makes them worse with respect to other aspects¹ (also those that we are not aware of). Also, not everything that counts can and will be counted. Below are some observations, ideas, and food for thought.

#### 9.1.1 To write or abstain

Functions we write ourselves can often be considered merely creative combinations of the building blocks available in base R or a few high-quality add-on packages<sup>2</sup>. Some are simpler than others. Thus, there is a question if a new operation should be introduced at all: whether we are faced with the case of multiplying entities without necessity.

On the one hand, the DRY (don't repeat yourself) principle tells us that the most frequently used (say, at least three times) code chunks should be generalised in the form of a new function. As far as complex operations are concerned, this is definitely a correct approach.

On the other hand, not every generalisation is necessarily welcome. Let us say we are tired of writing g(f(x)) for the n-th time,  $n \ge 2$ . Why don't we introduce h defined

<sup>&</sup>lt;sup>1</sup> Compare the notion of Pareto efficiency.

<sup>&</sup>lt;sup>2</sup> If some nontrivial operation is missing, we can always implement it at the Clanguage level; see Chapter 14.

as a combination of **g** and **f**? This might *seem* like a clever idea, but let us not take it for granted: being tired might be an indication of our body and mind needing a rest; being lazy can be a call for more self-discipline (not an overly popular word these days, but still, an endearing trait).

**Example 9.1** paste0 is a specialised version of paste, but has the sep argument hardcoded to an empty string.

- Even if this might be the most often applied use case, is the introduction of a new function justifiable? Is it so hard to write "paste=""" each time?
- Would changing paste's default argument be better? That, of course, would harm backward
  compatibility, but what strategies could we apply to make the transition as smooth as possible?
- Would it be better to introduce a new version of paste with sep defaulting to "", and inform
  the users that the old version is deprecated and to be removed in, say, two years? (or maybe
  one year is better? or five?)

**Example 9.2** In R 4.0, **deparse1** has been introduced: it is merely a combination of **deparse** (see below) and **paste**:

```
print(deparse1)
## function (expr, collapse = " ", width.cutoff = 500L, ...)
## paste(deparse(expr, width.cutoff, ...), collapse = collapse)
## <environment: namespace:base>
```

Let us say this covers 90% of use cases: was introducing it a justified idea then? What if that number was 99%?

Overall, more functions contribute to information overload. We do not want our users to be overwhelmed by too many choices. Luckily, nothing is cemented once and for all. Had we made bad design choices resulting in our API's being bloated, we could always clean up those that no longer spark joy.

# 9.1.2 To pamper or challenge

Think about the kind of audience we would like to serve: is it our team only, students, professionals, certain client groups, etc.? Do they have mathematical, programming, engineering, or scientific background? Not everything appropriate for one cohort will be valuable for another. And not everything pleasing some now will benefit them in the long run: people (their skills, attitudes, etc.) change.

**Example 9.3** Assume we are writing a friendly and inclusive package for novices who would like

to grasp the basics of data analysis as quickly<sup>3</sup> as possible. Without much effort, it would enable them to solve 80–95% of the most common, easy problems.

Think of introducing the students to a function that returns the five largest observations in a given vector. Let us call it **nlargest**: so pleasant to use. It makes the students feel empowered quickly.

Still, when faced with the remaining 5–20% of tasks, they will have to learn another, more advanced, generic, and powerful tool anyway (in our case, the base R itself). Are they determined and skilled enough to do that? Time will tell. The least we can do is to be explicit about it.

Recall that it took us some time to arrive at **order** and subsetting via `[`. Assuming that we read this book from the beginning to the end and solve all the exercises, which we should, we are now able to implement the said **nlargest** (and lots of other functions) ourselves, using a single line of code. This will also pay off in many scenarios that we will be facing in the future, e.g., when we consider matrices and data frames.

Yes, everyone will be reinventing their own **nlargest** this way. But this constitutes a great exercise: by our being too nice, some might have lost an opportunity to learn a new, more universal skill.

Although most users would love to minimise the effort put into all their activities, ultimately, they sometimes need to learn new things. Let us thus not be afraid to teach them stuff.

Furthermore, we do not want to discourage experts (or experts to-be) by presenting them with overly simplified solutions that keep their hands tied when something more ambitious needs to be done.

#### 9.1.3 To build or reuse

In the short term, the *fail-fast* philosophy encourages us to build our applications using prefabricated components. This is fantastic at the early stage of its life cycle. If we build something really simple or whose purpose is merely to illustrate an idea, educate, or show off how "awesome" we are, let us be explicit about it so that other users do not feel obliged to treat our product (exercise) seriously.

In the (not so likely, probabilistically speaking) event of its becoming successful, we are expected to start thinking about the project's long-term stability and sustainability. After all, relying on third-party functions, packages, or programs makes our software projects less... independent. This may be problematic because:

• the dependencies might not be available on every platform or may behave differently across various system configurations,

<sup>&</sup>lt;sup>3</sup> We will leave the reflection on whether this is at all feasible for another time.

This strategy is employed by many companies (and drug dealers): make the introductory experience super-smooth and fun. At the same time, do not allow your users to become independent too easily. Instead, make them rely on your product lines/proprietary solutions/payable services etc.

The free software movement, with its do-it-yourself approach, emphasises users' becoming autonomous. This does not contradict the user-friendliness (but that many open-source projects could benefit from becoming less exclusive is a different story, and this book tries to make a change in this area).

- they may be huge (and can depend on other external software too),
- their APIs may be altered, which could result in our project's not working anymore.
- their functionality can change, which can lead to some unexpected behaviours.

Hence, it might be better to rewrite some parts from scratch on our own.

**Exercise 9.4** Identify some R packages on CRAN with many dependencies. See what functions they import from other packages. How often is it just a few lines of code?

The UNIX philosophy emphasises building and using minimalist yet nontrivial, single-purpose, high-quality pieces of software that can work as parts of more complex pipelines. R serves as a glue language quite well.

In the long run, some of our software projects might converge to such a tool. Thus, we might have to standardise our API (e.g., make it available from the command line; Section 1.2) so that the users of other languages can benefit from our work.

**Important** If our project is merely a modified interface/front-end to a standalone program developed by others, we should be humble about it. We should strive to ensure we are not the ones who get all the credit for other people's work.

Also, we must clearly state how the original tools can be used to achieve the same goals, e.g., when working from the command line.

# 9.2 Managing data flow

A function, most of the time, can and should be treated as a black box: its callers do not have to care what it hides inside. After all, they are supposed to *use* it: given some *inputs*, they expect well-defined *outputs* (explained in very detail in the function's manual; see Section 9.3.2).

# 9.2.1 Checking input data integrity and argument handling

A function takes R objects of any kind as arguments, but it does not mean feeding it with every- or any-thing is healthy for its guts.

When designing functions, it is best to handle the inputs in a manner similar to base R's behaviour. This will make our contributions easier to work with.

Lamentably, base R functions frequently do not process arguments of a similar *kind* fully consistently. Such variability might be due to many reasons and, in essence, is not necessarily bad. Usually, there might be many possible behaviours and choosing one over another will make a few users unhappy anyway. Some choices might not be

optimal, but they are for historical compatibility (e.g., with S). Of course, it might also happen (but the probability is low) that there is a bug or something is poorly designed.

This is why it is better to keep the vocabulary quite restricted Even if there are exceptions to the general rules, with fewer functions, they are easier to remember. We advocate for such minimalism in this book.

Consider the following case study, illustrating that even the extremely simple scenario dealing with a single positive integer is not necessarily straightforward.

**Exercise 9.5** In mathematical notation, we usually denote the number of objects in a collection with the famous "n".

It is implicitly assumed that such n is a single natural number (although whether this includes 0 or not should be specified at some point). The functions runif, sample, seq, rep, strrep, and class::knn take it as arguments. But nothing prevents their users from trying to challenge them by passing:

- 2.5, -1, 0, 1-1e-16 (non-positive numbers, non-integers);
- NA\_real\_, Inf (not finite);
- 1:5 (not of length 1; after all, there are no scalars in R)
- numeric(0) (an empty vector);
- TRUE, NA, c(TRUE, FALSE, NA), "1", c("1", "2", "3") (non-numeric, but coercible to);
- list(1), list(1, 2, 3), list(1:3, 4) (non-atomic);
- "spam" (utter nonsense);
- as.matrix(1), factor(7), factor(c(3, 4, 2, 3)), etc. (compound types; see Chapter 10).

Read the aforementioned functions' reference manuals and call them on different inputs. Notice how differently they handle such atypical arguments.

Sometimes we will rely on other functions to check data integrity for us.

**Example 9.6** Let us consider the following function that generates n pseudorandom numbers from the unit interval rounded to d decimal digits. We strongly believe or hope (good faith and high competence assumption) that its authors knew what they were doing when they wrote:

```
round_rand <- function(n, d)
{
    x <- runif(n) # runif will check if `n` makes sense
    round(x, d) # round will determine the appropriateness of `d`
}</pre>
```

What constitutes correct n and d and how the function behaves when not provided with positive integers is determined by the two underlying functions, **runif** and **round**:

```
round_rand(4, 1) # the expected use case
## [1] 0.3 0.8 0.4 0.9
round_rand(4.8, 1.9) # 4, 2
## [1] 0.94 0.05 0.53 0.89
round_rand(4, NA)
## [1] NA NA NA NA
round_rand(0, 1)
## numeric(0)
```

Many such design choices can be defended if they are well thought-out and adequately documented. Some programmers will opt for high uniformity/compatibility across numerous tools, but there are cases where some exceptions/diversity do more good than harm.

Yet, the functions we write might be part of a more complicated data flow pipeline. It might happen that some other function generates a value that we did not expect (because of a bug therein or because we did not study its manual). The problem starts when this unthinkable value is used as input to our function. In our case, this would correspond to the said *n*'s or *d*'s being determined programmatically.

**Example 9.7** Continuing the previous example, the following might be somewhat challenging with regard to our being flexible and open-minded:

```
round_rand(c(100, 42, 63, 30), 1) # length(c(...)), 1)
## [1] 0.7 0.6 0.1 0.9
round_rand("4", 1) # as.numeric(...), 1
## [1] 0.2 0.0 0.3 1.0
```

Sure, it is quite convenient. Nevertheless, it might lead to problems that are hard to diagnose.

Also, note the not so informative error messages in cases like:

```
round rand(NA, 1)
## Error in runif(n): invalid arguments
round_rand(4, "1")
## Error in round(x, d): non-numeric argument to mathematical function
```

Hence, some defensive design mechanisms are not a bad idea, especially if they lead to generating an informative error message.

Important stopifnot gives a convenient means to assert the enjoyment of our expectations about a function's arguments (or some intermediate values). A call to stopi**fnot**(cond1, cond2, ...) is more or less equivalent to:

```
if (!(is.logical(cond1) && !any(is.na(cond1)) && all(cond1)))
    stop("`cond1` are not all TRUE")
if (!(is.logical(cond2) && !any(is.na(cond2)) && all(cond2)))
```

(continues on next page)

```
stop("`cond2` are not all TRUE")
...
```

Thus, if all the elements in the given logical vectors are TRUE, nothing happens. We can move on safely.

### **Example 9.8** We can rewrite the above function as follows:

```
round_rand2 <- function(n, d)</pre>
₹
    stopifnot(
        is.numeric(n), length(n) == 1,
        is.finite(n), n > 0, n == floor(n),
        is.numeric(d), length(d) == 1,
        is.finite(d), d > 0, d == floor(d)
   x <- runif(n) # runif will check if n makes sense
    round(x, d) # round will determine the appropriateness of d
}
round_rand2(5, 1)
## [1] 0.7 0.7 0.5 0.6 0.3
round_rand2(5.4, 1)
## Error in round_rand2(5.4, 1): n == floor(n) is not TRUE
round rand2(5, "1")
## Error in round_rand2(5, "1"): is.numeric(d) is not TRUE
```

This implements the strictest test for "a single positive integer" possible. In the case of any violation of the underlying condition, we get a very informative error message.

### **Example 9.9** At other times, we might be interested in the argument checking like:

```
if (!is.numeric(n))
    n <- as.numeric(n)
if (length(n) > 1) {
    warning("only the first element will be used")
    n <- n[1]
}
n <- floor(n)
stopifnot(is.finite(n), n > 0)
```

This way, "4" and c(4.9, 100) will all be accepted as  $4^4$ .

We see that there is always a tension between being generous/flexible and precise/restrictive. Also, because of their particular use cases, for some functions, it will

<sup>&</sup>lt;sup>4</sup> We rely on the S<sub>3</sub> generics is.numeric and as.numeric here; see Section 10.4.

be better to behave differently than the others. Too much uniformity is as bad as chaos. We are expected to rely on common sense, but adding lightweight foolproof mechanisms is always welcome.

It is our duty to be explicit about all the assumptions we make or exceptions we allow (by writing comprehensive documentation; see Section 9.3.2).

We will revisit this topic in Section 10.4.

**Note** Example exercises related to improving the consistency of base R's argument handling in different domains include the **vctrs** and **stringx** packages<sup>5</sup>. Can these contributions be justified?

**Exercise 9.10** Reflect on how you would act in the following scenarios (and how base R and other packages or languages you know deal with them):

- a vectorised mathematical function (empty vectors? non-numeric inputs? what if it is
  equipped with the names attribute? what if it has other ones?);
- an aggregation function (what about missing values? empty vectors?);
- a function vectorised with regard to two arguments (elementwise vectorisation? recycling rule? only scalar vs vector or vector vs vector of the same length allowed? what if one argument is a row vector and the other is a column vector);
- a function vectorised with respect to all arguments (really all? maybe some exceptions are necessary?);
- a function vectorised with respect to the first argument but not the second (why such a restriction? when?).

Find a few functions that match each case.

# 9.2.2 Putting outputs into context

The functions we write do not exist in a vacuum. We should put them into a much broader context: how will they be combined with other tools?

As a general rule, our functions are expected to generate outputs of a *predictable* kind. This way, we can easily deduce what will happen in the code chunks that utilise them.

**Example 9.11** Some base R functions do not adhere to this rule for the sake of (questionable) users' convenience. We will meet a few of them in Chapter 11 and Chapter 12. In particular, **sapply** and the underlying **simplify2array**, can return a list, an atomic vector, or a matrix.

```
simplify2array(list(1, 3:4))  # list
## [[1]]
## [1] 1
(continues on next page)
```

<sup>&</sup>lt;sup>5</sup> Yours truly is the author of the latter and thus is guilty of multiplying entities beyond necessity.

Further, the index operator with drop=TRUE, which is the default, may output an atomic vector. However, it may as well yield a matrix or a data frame.

We proclaim that the default functions' behaviour should be to return the object of the most generic kind possible (if there are other options). Then:

- either we equip the function with a further argument which must be explicitly set if we *really* wish to simplify the output,
- or we ask the user to call a simplifier explicitly after the function call. In this case, if the simplifier cannot neaten the object, it should probably fail by issuing an error or at least try to apply some brute force solution (e.g., "fill the gaps" somehow itself, preferably with a warning).

#### Example 9.12 For instance:

```
as.numeric(A[1:2, ]) # always returns a vector
## [1] 1 2 4 5
stringi::stri_list2matrix(list(1, 3:4)) # fills the gaps with NAs
## [,1] [,2]
## [1,] "1" "3"
## [2,] NA "4"
```

Ideally, a function is expected to perform one (and only one) well-defined task. If a function tends to generate objects of different kinds, depending on the arguments provided, it might be better to write two functions instead.

**Exercise 9.13** Functions such as rep, seq, and sample do not perform a single task. Or do they?

**Note** (\*) In a purely functional programming language, we can assume the so-called *referential transparency*: a call to a *pure function* can always safely be replaced with the value it is supposed to generate. If this is true, then for the same set of argument values, the output is always the same. Furthermore, there are no side effects. In R, it is not exactly the case:

- a call can introduce/modify/delete variables in other environments (see Chapter 16), e.g., the state of the random number generator,
- due to lazy evaluation, functions are free to interpret the argument *forms* (passed expressions, i.e., not only: values) in whatever way they like (see Section 9.5.7, Section 12.3.9, and Section 17.5),
- printing, plotting, file reading, and database access have apparent consequences with regard to the state of some external resources.

**Important** Each function must return some value, but there are several instances (e.g., plotting, printing), where this does not make sense.

In such a case, we may consider returning **invisible**(NULL), a NULL whose *first* printing will be suppressed.

Compare the following:

```
(function() NULL)() # anonymous function, called instantly
## NULL
(function() invisible(NULL))() # printing suppressed
x <- (function() invisible(NULL))()
print(x) # no longer invisible
## NULL</pre>
```

Take a look at the return value of the built-on cat.

# 9.3 Organising and maintaining functions

#### 9.3.1 Function libraries

Definitions of frequently-used functions or datasets can be emplaced in separate source files (.R extension) for further reference.

Such libraries can be executed by calling:

```
source("path_to_file.R")
```

**Exercise 9.14** Create a source file (script) named mylib.R, where you define a function called *nlargest* which returns a few largest elements in a given atomic vector.

From within another script, call **source**("mylib.R") (note that relative paths refer to the current working directory; (compare Section 2.1.6). Then, write a few lines of code where you test **nlargest** on some example inputs.

### 9.3.2 Writing R packages (\*)

When a function library grows substantially, or when there is a need for equipping it with the relevant manual pages<sup>6</sup> (Section 9.3.2) or compiled code (Chapter 14), turning it into an R package (Section 7.3.1) might be worth considering. This is the case even if it is only for our own or small team's purpose.

**Important** You *do not have to* publish your package on CRAN<sup>7</sup>. Many users are tempted to submit whatever they have been tinkering around with for a while. Have mercy on the busy CRAN maintainers and do not contribute to the information overload unless you have come up with something potentially of service for other R users (make it less about you and more about the community; thank you in advance). R packages can always be hosted on and installed from, for instance, GitLab or GitHub.

### Package structure (\*)

A source package is merely a directory containing some special files and subdirectories:

- DESCRIPTION a text file that gives the name of the package, its version, authors, dependencies upon other packages, license, etc.;
- NAMESPACE a text file containing directives stating which objects are to be exported so that they are available to the package users and which names are to be imported from other packages;

<sup>&</sup>lt;sup>6</sup> This should read: i.e., always.

<sup>&</sup>lt;sup>7</sup> And always consult the CRAN Repository Policy at https://cran.r-project.org/web/packages/policies.html.

- R a directory with R scripts (.R files), which define, e.g., functions, example datasets, etc.;
- man a directory with R documentation files (.Rd), describing at least all the exported objects; see Section 9.3.2;
- src optional; compiled code, see Chapter 14;
- tests optional; tests to run on the package check, see Section 9.3.4.

See Section 1 in [59] for more details and other options. We do not need to repeat the information from the official manual as all readers can read it themselves.

**Exercise 9.15** Inspect the source code of the example package available for download from https: //github.com/gagolews/rpackagedemo/.

### Building and installing (\*)

Recall from Section 7.3.1 that a source package can be built and installed by calling:

```
install.packages("pkg_directory", repos=NULL, type="source")
```

Then it can be used as any other R package (Section 7.3.1). In particular, it can be loaded and attached to the search path (Section 16.2.6) via a call to:

```
library("pkg")
```

This makes all the objects marked as exportable in its NAMESPACE file available to the user; see also Section 16.3.5.

**Exercise 9.16** Create your own package **mypkg** featuring the solutions to the exercises you have solved whilst studying the material in the previous chapters. When in doubt, refer to the official manual [59].

**Note** (\*) The building and installing of packages also be done from the command line:

```
R CMD build pkg_directory # creates a distributable source tarball (.tar.gz)
R CMD INSTALL pkg-version.tar.gz
R CMD INSTALL --build pkg_directory
```

Also, some users could potentially benefit from creating their own Makefiles that help automate the processes of building, testing, checking, etc.

### Documenting R packages (\*)

Documenting functions and commenting code thoroughly is critical, even if we just write for ourselves. Most programmers sooner or later will notice that they find it hard to determine what a piece of code is doing after they take a break from it. In some sense, we always write for external audiences, which includes our future selves.

The help system is one of the stronger assets of the R environment. By far, we most likely have interacted with many documentation pages and got a general idea of what constitutes an informative documentation piece.

From the technical side, R Documentation (.Rd) files are located in the man subdirectory of a source package. All exported objects (e.g., functions) should be described clearly. Additional topics can be covered too.

During the package installation, the .Rd files are converted to various output formats, e.g., HTML or plain text, and displayed upon a call to the well-known **help** function.

Documentation files use a LaTeX-like syntax, which looks quite obscure to an untrained eye. The relevant commands are explained in very detail in Section 2 of Writing R Extensions [59].

**Note** The process of writing .Rd files by hand might be tedious, especially keeping track of the changes to the \usage and \arguments commands. Rarely do we recommend the use of third-party packages because base R facilities are usually sufficient. But **roxygen2** might be worth a try because it makes the developers' lives easier. Most importantly, it allows the documentation to be specified alongside the functions' definitions, which is much more natural.

**Exercise 9.17** Add a few manual pages to your example R package.

# 9.3.3 Writing standalone programs (\*\*)

Section 7.3.3 mentioned how to call external programs using system2.

On UNIX-like operating systems, it is easy to turn our R scripts into standalone tools that can be run from the shell. We already touched upon this topic in Section 1.2.3.

The **commandArgs** function returns the list of arguments passed from the command line to our script in the form of a character vector. Whatever we do with them is up to us. Moreover, **q** can terminate a script, yielding any integer return code. By convention, anything other than 0 indicates an error.

**Example 9.18** Say we have the following script named test file in the current directory:

```
#!/bin/env -S Rscript --vanilla

argv <- commandArgs(trailingOnly=TRUE)
cat("commandArgs:\n")
print(argv)

if (length(argv) == 0) {
    cat("Usage: testfiles file1 file2 ...\n")
    q(save="no", status=1) # exit with code 1
}</pre>
```

```
if (!all(file.exists(argv))) {
    cat("Some files do not exist.\n")
    q(save="no", status=2) # exit with code 2
}
cat("All files exist.\n")
# exits with code 0 (success)
```

Example interactions with this program from the UNIX-like terminal (bash):

```
chmod u+x testfiles # add permission to execute
./testfiles
## commandAras:
## character(0)
## Usage: testfiles file1 file2 ...
./testfiles spanish_inquisition
## commandArgs:
## [1] "spanish_inquisition"
## Some files do not exist.
./testfiles spam bacon eggs spam
## commandArgs:
## [1] "spam" "bacon" "eggs" "spam"
## All files exist.
```

The stdin, stdout, and stderr represent the always-open connections mapped to the standard input ("keyboard"), and normal and error output. They can be read from or written to using functions such as scan or cat.

During run time, we can redirect stdout and stderr to different files or even strings using sink.

# 9.3.4 Assuring quality code

Below we mention some good development practices related to maintaining quality code. This is an important topic, but writing about them is tedious to the same extent that reading about them is boring because it is the more-artistic part of software engineering. After all, they are some heuristics that are learnt best by observing and mimicking what the others are doing (and hence the exercises below will encourage us to do so).

### Managing changes and working collaboratively

We are recommended to employ some source code version control system, such as **git**, to keep track of the changes made to the software.

**Note** It is worth investing time and effort to learn how to use **git** from the command line; see https://git-scm.com/doc.

There are a few hosting providers for **git** repositories, with GitLab and GitHub being particularly popular among open-source software developers. They support working collaboratively on the projects and are equipped with additional tools for reporting bugs, suggesting feature requests, etc.

**Exercise 9.19** Find where the source code of your favourite R packages or other open-source projects is hosted. Explore the corresponding repositories, feature trackers, wikis, discussion boards, etc. Each community is different and is governed by varied, sometimes contrasting guidelines: after all, we come from all corners of the world.

### Test-driven development and continuous integration

It is often hygienic to include some principles of test-driven development when writing own functions.

**Exercise 9.20** Assume that, for some reason, we were asked to write a function to compute the root mean square (quadratic mean) of a given numeric vector. Before implementing the actual routine, we need to reflect upon what we want to achieve, especially how we want our function to behave in certain boundary cases.

**stopifnot** gives simple means to ensure a given assertion is fulfilled. If that is the case, it will move forward quietly.

*Let us say we have come up with the following set of expectations:* 

```
stopifnot(all.equal(rms(1), 1))
stopifnot(all.equal(rms(1:100), 58.16786054171151931769))
stopifnot(all.equal(rms(rep(pi, 10)), pi))
stopifnot(all.equal(rms(numeric(0)), 0))
```

Write a function **rms** that fulfils the above assertions.

**Exercise 9.21** Implement your version of the **sample** function (assuming replace=TRUE), using calls to **runif**. Start by writing a few unit tests.

A couple of R packages support writing and executing unit tests, including **testthat**, **tinytest**, **RUnit**, or **realtest**. However, in the most typical use cases, relying on **stopi-fnot** is powerful enough.

**Exercise 9.22** (\*) Consult the Writing R Extensions manual [59] about where and how to include unit tests in your example package.

**Note** (\*) R includes a built-in mechanism to check a couple of code quality areas: running R CMD check pkg\_directory from the command line (preferably using the most recent version of R) can suggest several improvements.

Also, it is possible to use various continuous integration techniques that are automatically triggered when pushing changes to our software repositories; see GitLab CI or GitHub Actions. For instance, running a package build, install, and check process is possible upon every **git** commit. Also, CRAN features some continuous integration services, including checking the package on various platforms.

### Debugging

For all his life, the current author has been debugging his programs primarily by manually printing the state of the suspicious variables (**printf** and the like) in different code areas. Hahaha lololol, so old school. Yet, weirdly efficient.

R has an interactive debugger; see the **browser** function. Also, refer to Section 9 of [63] for more details.

Some IDEs (e.g., **RStudio**) support this feature, too; see their corresponding documentation

### **Profiling**

Typically, a program spends a relatively long time executing only a small portion of code. The **Rprof** function can be a helpful tool to identify which chunks might need a rewrite, for instance, using a compiled language (Chapter 14).

Please remember, though, that bottlenecks are not only formed by using algorithms with high computational complexity, but also data input and output (such as reading files from disk, printing messages on the console, querying Web APIs, etc.).

# 9.4 Special functions: Syntactic sugar

Some functions, such as `\*`, are somewhat special. They can be referred to using an alternative syntax which, for some reason, most of us accepted as the default one. Below we will reveal, amongst others, that "5 \* 9" reduces to an ordinary function *call*:

```
`*`(5, 9) # a call to `*` with 2 arguments, equivalent to 5 * 9
## [1] 45
```

#### 9.4.1 A note on backticks

In Section 2.2, we have mentioned that we can assign (as in `<-`) syntactically valid names to our objects. Most identifiers comprised of letters, digits, dots, and underscores can be used directly in R code.

Nevertheless, it is possible to label our objects however we like: not syntactically valid

(nonstandard) identifiers just need to be enclosed in backticks (back quotes, grave accents):

```
`42 a quite peculiar name :0 lollolll` <- c(a=1, `b c`=2, `42`=3, `!`=4)
1/(1+exp(-`42 a quite peculiar name :0 lollolll`))
## a b c 42 !
## 0.73106 0.88080 0.95257 0.98201
```

Of course, such names are less convenient. However, backticks let us refer to them in any context.

### 9.4.2 Dollar, `\$` (\*)

The dollar operator, `\$`, can be an alternative accessor to a single element in a named list<sup>8</sup>.

If the label is a syntactically valid name, then x\$label does the same job as x[["label"]] (saving five keystrokes: such a burden!).

```
x <-- list(spam="a", eggs="b", `eggs and spam`="c", best.spam.ever="d")
x$eggs
## [1] "b"
x$best.spam.ever # recall that a dot has no special meaning in most contexts
## [1] "d"</pre>
```

Nonstandard names must still be enclosed in backticks:

```
x$`eggs and spam` # x[["eggs and spam"]] is okay as usual
## [1] "c"
```

We are minimalist by design here. Thence, we will avoid this operator, as it does not increase the expressive power of our function repertoire. Also, it works on neither atomic vectors nor matrices.

Furthermore, it does not work with names that are generated programmatically:

```
what <- "spam"
x$what # the same as x[["what"]] - we don't want this
## NULL
x[[what]] # works fine
## [1] "a"</pre>
```

The support for the *partial matching* of element names has been added to provide the users working in quick-and-dirty, interactive programming sessions with some relief in the case where they find the typing of the whole label extremely problematic:

<sup>&</sup>lt;sup>8</sup> And hence also from data frames.

```
x$s
## Warning in x$s: partial match of 's' to 'spam'
## [1] "a"
```

#### Compare:

```
x[["s"]] # no warning here...
## NULL
x[["s", exact=FALSE]]
## [1] "a"
```

It is generally a bad programming practice, because the result depends on the names of other items in x (which might change later) and can decrease code readability. The only reason why we obtained a warning message was because this book enforces the options(warnPartialMatchDollar=TRUE) setting, which, sadly, is not the default.

Note the behaviour on an ambiguous partial match:

```
x$egg # ambiguous resolution
## NUI I
```

as well as on an element assignment:

```
x$s <- "e"
str(x)
## List of 5
## $ spam
                 : chr "a"
               : chr "b"
## $ eggs
## $ eggs and spam : chr "c"
## $ best.spam.ever: chr "d"
## $ s
                 : chr "e"
```

This did not modify spam: it added a new element, s.

# 9.4.3 Curly braces, `{`

A block of statements grouped with curly braces, `{`, corresponds to a function call. When we write:

```
{
    print(TRUE)
    cat("two")
    3
## [1] TRUE
## two
## [1] 3
```

The parser translates it to a call to:

```
`{`(print(TRUE), cat("two"), 3)
## [1] TRUE
## two
## [1] 3
```

When the above is executed, every argument, one by one, is evaluated. Then, the last value is returned as the result of that call.

#### 9.4.4 `if`

**if** is a function, too. As mentioned in Section 8.1, it returns the value corresponding to the expression that is evaluated conditionally. Hence, we may write:

```
if (runif(1) < 0.5) "head" else "tail"
## [1] "head"</pre>
```

but also:

```
`if`(runif(1) < 0.5, "head", "tail")
## [1] "head"</pre>
```

**Note** A call like `if` (test, what\_if\_true, what\_if\_false) can only work correctly because of the lazy evaluation of function arguments; see Chapter 17.

On a side note, while, for, repeat can also be called that way, but they return invisible(NULL).

### 9.4.5 Operators are functions

# Calling built-in operators as functions

Every arithmetic, logical, and relational operator is translated to a call to the corresponding function. For instance:

```
`<`(`+`(`*`(`-`(3), 4)), 5) # 2+(-3)*4 < 5
## [1] TRUE
```

Also, x[i] is equivalent to `[`(x, i) and x[[i]] maps to `[[`(x, i).

Knowing this will not only enable us to manipulate unevaluated R code (Chapter 15) or access the corresponding manual pages (see, e.g., help("[")), but also write some expressions more concisely. For instance,

```
x <- list(1:5, 11:17, 21:23)
```

```
unlist(Map(`[`, x, 1)) # 1 is a further argument passed to `[`
## [1] 1 11 21
```

is equivalent to a call to Map(function(e) e[1], x).

**Note** Unsurprisingly, the assignment operator, `<-`, is also a function. It returns the assigned value invisibly.

Knowing that `<-` binds right to left (compare help("Syntax")), this is why the expression "a <- b <- 1" results in both a and b being assigned 1: it is equivalent to "`<-`("a", `<-`("b", 1))" and "`<- `("b", 1)" returns 1.

Owing to the pass-by-value semantics (Section 9.5.1), we can also expect that we will always be assigning a *copy* of the value on the right-hand side (with the exception of environments; Chapter 16).

```
x <- 1:6
y <- x # makes a copy (but delayed, on demand, for performance reasons)
y[c(TRUE, FALSE)] <- NA_real_ # modify every 2nd element
print(y)
## [1] NA 2 NA 4 NA 6
print(x) # state of x has not changed - x and y are different objects
## [1] 1 2 3 4 5 6</pre>
```

This is especially worth pointing out to Python (amongst others) programmers, where the above assignment would mean that x and y both refer to the same (shared) object in the computer's memory.

However, with no harm done to semantics, copying x is postponed until absolutely necessary (Section 16.1.4). This is efficient both time- and memory-wise.

#### Creating own binary operators

We can also introduce our own binary operators named like `myopname\*`:

```
`%:)%` <- function(e1, e2) (e1+e2)/2
5 %:)% 1:10
## [1] 3.0 3.5 4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5
```

Recall that `%%` and `%/%` are built-in operators denoting division remainder and integer division. Also, in Chapter 11, we will learn about `%\*%`, which implements matrix multiplication.

**Note** Chapter 10 notes that most existing operators can be overloaded for objects of different types.

### 9.4.6 Replacement functions

Functions generally do not change the state of their arguments. However, there is some syntactic sugar that allows us to replace objects or their parts with new content. We call them *replacement functions*.

For instance, three of the following calls *replace* the input x with its modified version:

```
x <- 1:5 # example input
x[3] <- 0 # replace the 3rd element with 0
length(x) <- 7 # "replace" length
names(x) <- LETTERS[seq_along(x)] # replace the names attribute
print(x) # `x` is now different
## A B C D E F G
## 1 2 0 4 5 NA NA</pre>
```

### Creating replacement functions

A replacement function is a mapping named like `name<-` with at least two parameters:

- x (the object to be modified),
- ... (possible further arguments),
- value (as the last parameter; the object on the right-hand side of the `<-` operator).

We will most often interact with *existing* replacement functions, not create our own ones. But knowing how to do the latter is vital to understanding this language feature.

For example:

```
`add<-` <- function(x, where=TRUE, value)
{
    x[where] <- x[where] + value
    x # the modified object that will replace the original one
}</pre>
```

The above aims to add some value to a subset of the input vector x (by default, to each element therein) and return its altered version that will replace the object it has been called upon.

```
y <- 1:5  # example vector
add(y) <- 10  # calls `add<- `(y, value=10)
print(y)  # y has changed
## [1] 11 12 13 14 15
add(y, 3) <- 1000  # calls `add<- `(y, 3, value=1000)
print(y)  # y has changed again
## [1] 11 12 1013 14 15</pre>
```

We see that calling "add(y, w) <- v" works as if we have called "y <- add <- (y, w, value=v)".

**Note** (\*) According to [63], a call "add(y, 3) <- 1000" is a syntactic sugar precisely for:

```
`*tmp*` <- y # temporary substitution
y <- `add<-`(`*tmp*`, 3, value=1000)
rm("*tmp*") # remove the named object from the current scope</pre>
```

This has at least two implications. First, in the unlikely event that a variable `\*tmp\*` existed before the call to the replacement function, it will be no more, it will cease to be. It will be an ex-variable. Second, the temporary substitution guarantees that y must exist before the call (a function's body does not have to refer to all the arguments passed; because of lazy evaluation, see Chapter 17, we could get away with it otherwise).

### Substituting parts of vectors

The replacement versions of the subsetting operators are named as follows:

- `[<-` is used in substitutions like "x[i] <- value",
- `[[<-` is called when we perform "x[[i]] <- value",
- `\$<-` is used whilst calling "x\$i <- value".

Here is a use case:

```
x <- 1:5
`[<-`(x, c(3, 5), NA_real_) # returns a new object
## [1] 1 2 NA 4 NA
print(x) # does not change the original input
## [1] 1 2 3 4 5</pre>
```

On a side note, `length<-` can be used to expand or shorten a given vector by calling "length(x) <- new\_length"; see also Section 5.3.3.

```
x <- 1:5
x[7] <- 7
length(x) <- 10
print(x)
## [1] 1 2 3 4 5 NA 7 NA NA NA
length(x) <- 3
print(x)
## [1] 1 2 3</pre>
```

Although, semantically speaking, calling `[<-` results in the creation of a new vector (a modified version of the original one), we may luckily expect some performance optimisations behind the scenes.

**Exercise 9.23** Write a function `**extend<-**`, which pushes new elements at the end of a given vector, modifying it in place.

```
`extend<-` <- function(x, value) ...to.do...
```

Example use:

```
x <- 1
extend(x) <- 2  # push 2 at the back
extend(x) <- 3:10  # add 3, 4, ..., 10
print(x)
## [1] 1 2 3 4 5 6 7 8 9 10</pre>
```

#### Replacing attributes

There are many replacement functions to reset object attributes (Section 4.4). In particular, each special attribute has its replacement procedure, e.g., `names<-`, `class<-`, `dim<-`, `levels<-`, etc.

```
x <- 1:3
names(x) <- c("a", "b", "c") # change the `names` attribute
print(x) # x has been altered
## a b c
## 1 2 3</pre>
```

Individual (arbitrary, including non-special ones) attributes can be set using `attr<-`, and all of them can be established via a single call to `attributes<-`.

```
x <- "spam"
attributes(x) <- list(shape="oval", smell="meaty")
attributes(x) <- c(attributes(x), taste="umami")
attr(x, "colour") <- "rose"
print(x)
## [1] "spam"
## attr(, "shape")
## [1] "oval"
## attr(, "smell")
## [1] "meaty"
## attr(, "taste")
## [1] "umami"
## attr(, "colour")
## [1] "rose"</pre>
```

Also, setting an attribute to NULL results, by convention, in its removal:

```
print(x)
## [1] "spam"
## attr(,"shape")
## [1] "oval"
## attr(,"smell")
## [1] "meaty"
## attr(,"colour")
## [1] "rose"
attributes(x) <- NULL # remove all
print(x)
## [1] "spam"</pre>
```

Which can be worthwhile in contexts such as:

```
x <- structure(c(a=1, b=2, c=3), some_attrib="value")
y <- `attributes<-`(x, NULL)</pre>
```

Here, x retains its attributes, and y is a version of x with metadata removed.

### Compositions of replacement functions

Updating only selected names like:

```
x <- c(a=1, b=2, c=3)
names(x)[2] <- "spam"
print(x)
## a spam c
## 1 2 3</pre>
```

is possible due to the fact that "names(x)[i] <-v" is equivalent to:

```
old_names <- names(x)
new_names <- `[<-`(old_names, i, value=v)
x <- `names<-`(x, value=new_names)</pre>
```

**Important** More generally, a composition of replacement calls "g(f(x, a), b) <- y" yields a result equivalent to "x <- f<-(x, a, value=g-(f(x, a), b, value=y))". Both f and f<- need to be defined, but having g is not necessary.

**Exercise 9.24** (\*) What is " $h(g(f(x, a), b), c) \leftarrow y$ " equivalent to?

**Exercise 9.25** Write a (convenient!) function `recode<-` which replaces specific elements in a character vector with some other ones, allowing the following interface:

```
`recode<-` <- function(x, value) ...to.do...

(continues on next page)
```

```
x <- c("spam", "bacon", "eggs", "spam", "eggs")
recode(x) <- c(eggs="best spam", bacon="yummy spam")
print(x)
## [1] "spam" "yummy spam" "best spam" "spam" "best spam"</pre>
```

We see that the named character vector gives a few from="to" pairs, e.g., all eggs are to be replaced by best spam.

Now, determine which calls are equivalent to the following:

```
x <- c(a=1, b=2, c=3)
recode(names(x)) <- c(c="z", b="y") # or equivalently = ... ?
print(x)
## a y z
## 1 2 3
y <- list(c("spam", "bacon", "spam"), c("spam", "eggs", "cauliflower"))
recode(y[[2]]) <- c(cauliflower="broccoli") # or = ... ?
print(y)
## [[1]]
## [1] "spam" "bacon" "spam"
##
## [[2]]
## [1] "spam" "eggs" "broccoli"</pre>
```

**Exercise 9.26** (\*) Consider the `recode<-` function from the previous exercise.

Here is an example matrix with the dimnames attribute whose names attribute is set (more details in Chapter 11):

```
(x <- Titanic["Crew", "Male", , ])</pre>
##
         Survived
## Age
          No Yes
## Child
            0 0
    Adult 670 192
recode(names(dimnames(x))) <- c(Age="age", Survived="survived")</pre>
print(x)
##
        survived
## age
          No Yes
   Child 0 0
##
##
   Adult 670 192
```

This changes the x object. For each of the following subtasks, write a single call that alters names(dimnames(x)) without modifying x in place but returning a recoded copy of:

```
    names(dimnames(x)),
```

```
    dimnames(x)),
```

X.

**Exercise 9.27** (\*) Consider the `recode<-` function once again but now let an example object be a data frame featuring a column of the factor class:

```
x <- iris[c(1, 2, 51, 101), ]
recode(levels(x[["Species"]])) <- c(</pre>
    setosa="SET", versicolor="VER", virginica="VIR"
)
print(x)
       Sepal.Length Sepal.Width Petal.Length Petal.Width Species
                5.1
                                           1.4
                                                        0.2
## 1
                             3.5
## 2
                4.9
                             3.0
                                           1.4
                                                        0.2
                                                                SET
## 51
                 7.0
                                           4.7
                                                        1.4
                             3.2
                                                                VER
## 101
                 6.3
                             3.3
                                           6.0
                                                        2.5
                                                                 VIR
```

How to change levels(x[["Species"]]) and return an altered copy of:

```
• levels(x[["Species"]]),
```

- x[["Species"]],
- x

without modifying x in place?

# 9.5 Arguments and local variables

# 9.5.1 Pass by "value"

As a general rule, functions cannot change the state of their arguments<sup>9</sup>. We can think of them as being passed by *value*, i.e., as if their copy was made.

```
test_change <- function(y)
{
    y[1] <- 7
    y
}

x <- 1:5
test_change(x)
## [1] 7 2 3 4 5</pre>
```

(continues on next page)

<sup>&</sup>lt;sup>9</sup> With the exception of objects of the type environment, which are passed by reference; see Chapter 16. Also, the fact that we have access to unevaluated R expressions can cause further deviations to this rule (see below).

```
print(x) # same
## [1] 1 2 3 4 5
```

If the above were not the case, the state of x would have changed after the call.

### 9.5.2 Variable scope

Function arguments and any other variables we create inside a function's body are *relative* to each call to that function.

Both x and z are local variables. They only live whilst our function is being executed. The former temporarily *masks*<sup>10</sup> the object of the same name from the caller's context.

**Important** It is a good development practice to refrain from referring to objects not created within the current function, especially to "global" variables. We can always pass an object as an argument explicitly.

**Note** It is a function call as such, not curly braces per se that form a local scope.

Writing " $x \leftarrow \{ y \leftarrow 1; y + 1 \}$ ", y is not an auxiliary variable; it is an ordinary named object created alongside x.

On the other hand, in "x <- (function() { z <- 1; z + 1 })()", z will not be available thereafter.

<sup>&</sup>lt;sup>10</sup> Chapter 16 discusses this topic in-depth: objects are bound to their names within environments. Moreover, R uses lexical (static) scoping, which is not necessarily intuitive, especially taking into account that a function's environment can always be changed.

### 9.5.3 Closures (\*)

Most user-defined functions are, in fact, representatives of the so-called *closures*; see Section 16.3.2 and [1]. They not only consist of an R expression to evaluate but also can carry some auxiliary data.

For instance, given two equal-length numeric vectors x and y, a call to **approxfun**(x, y) returns a *function* that linearly interpolates between the consecutive points  $(x_1, y_1)$ ,  $(x_2, y_2)$ , and so forth, so that a corresponding y can be determined for any x.

```
x <- seq(0, 1, length.out=11)
f1 <- approxfun(x, x^2)
f2 <- approxfun(x, x^3)
f1(0.75) # check that it is quite close to the true 0.75^2
## [1] 0.565
f2(0.75) # compare with 0.75^3
## [1] 0.4275</pre>
```

Inspecting, however, the source codes of the above functions:

```
print(f1)
## function (v)
## .approxfun(x, y, v, method, yleft, yright, f, na.rm)
## <environment: 0x5633bb894f70>
print(f2)
## function (v)
## .approxfun(x, y, v, method, yleft, yright, f, na.rm)
## <environment: 0x5633ba9daeb0>
```

we might wonder how they can produce different results: it is evident that they are identical. It turns out, however, that they internally store some additional data that is referred to upon their calls:

```
environment(f1)[["y"]]
## [1] 0.00 0.01 0.04 0.09 0.16 0.25 0.36 0.49 0.64 0.81 1.00
environment(f2)[["y"]]
## [1] 0.000 0.001 0.008 0.027 0.064 0.125 0.216 0.343 0.512 0.729 1.000
```

We will explore this and many more in detail in the third part of this book.

# 9.5.4 Default arguments

We have already mentioned above that when designing functions performing complex tasks we will sometimes be faced with a design problem: how to find a sweet spot between being generous/mindful of the diverse needs of our users and making the API neither overwhelming nor oversimplistic.

We know that it is best if a function performs a single well-specified task. Moreover,

it is nice if it also allows its behaviour to be tweaked if one wishes to do so. The use of *default arguments* can facilitate this principle.

For instance, **log** computes logarithms, by default, the natural ones.

```
log(2.718) # the same as log(2.78, base=exp(1)) - default base
## [1] 0.9999
log(4, base=2) # different base
## [1] 2
```

**Exercise 9.28** Study the documentation of the following functions and note the default values they define: **round**, **hist**, **grep**, and **download**. **file**.

We can easily define our own functions equipped with such recommended settings:

```
test_default <- function(x=1) x

test_default()  # use default
## [1] 1
test_default(2)  # use something else
## [1] 2</pre>
```

Most often, default arguments are just constants, e.g., 1. Generally, though, they can be any R expressions: also ones that include a reference to other arguments passed to the same function; see Section 17.2.

Default arguments most often appear at the end of the parameter list, but see Section 9.4.6 (on replacement functions) for a well-justified exception.

# 9.5.5 Lazy vs eager evaluation

In some languages, function arguments are always evaluated prior to a call. In R, though, they are only computed when actually needed. We call it *lazy* or *delayed* evaluation. Recall that in Section 8.1.4, we introduced the short-circuit evaluation operators `||` (or) and `&&` (and). They can do their job precisely thanks to this mechanism.

**Example 9.29** *In the following example, we do not use the function's argument at all:* 

```
lazy_test1 <- function(x) 1 # x not used at all
lazy_test1({cat("and now for something completely different!"); 7})
## [1] 1</pre>
```

Otherwise, we would see a message being printed out on the console.

**Example 9.30** *Next, let us use x amidst other expressions in the body:* 

```
lazy_test2 <- function(x)
{</pre>
```

(continues on next page)

```
cat("it's...")
   y <- x+x # using x twice
   cat(" a man with two noses")
}
lazy_test2({cat("and now for something completely different!"); 7})
## it's... and now for something completely different! a man with two noses
## [1] 14
```

An argument is evaluated once, and its value is stored for further reference. If that were not the case, we would see two messages like and now....

We will elaborate on this in Chapter 17.

#### Ellipsis, `...` 9.5.6

Let us start with an exercise.

**Exercise 9.31** Notice the presence of `...` in the parameter list of c, list, structure, cbind, rbind, cat, Map (and the underlying mapply), lapply (a specialised version of Map), optimise, optim, uniroot, integrate, outer, aggregate. What purpose does it serve, according to these functions' manual pages?

We can create a variadic function by placing a dot-dot-dot (ellipsis; see help("dots")), `. ..., somewhere in its parameter list. The ellipsis serves as a placeholder for all objects passed to the function but not matched by any formal (named) parameters.

The easiest way to process arguments passed via `...` programmatically (see also Section 17.3) is by redirecting them to list.

```
test_dots <- function(...)</pre>
    list(...)
test_dots(1, a=2)
## [[1]]
## [1] 1
##
## $a
## [1] 2
```

Such a list can be processed just like... any other R list. What we can do with these arguments is only limited by our creativity (in particular, recall from Section 7.2.2 the very powerful do.call function). Still, there are two primary use cases of the ellipsis 11:

create a new object by combining an arbitrary number of other objects:

<sup>&</sup>lt;sup>11</sup> Which is somewhat similar to Python's \*args and \*\*kwargs in a function's parameter list.

```
c(1, 2, 3) # 3 arguments
## [1] 1 2 3
c(1:5, 6:7) # 2 arguments
## [1] 1 2 3 4 5 6 7
structure("spam") # 0 additional arguments
## [1] "spam"
structure("spam", color="rose", taste="umami") # 2 further arguments
## [1] "spam"
## attr(,"color")
## [1] "rose"
## attr(,"taste")
## [1] "umami"
cbind(1:2, 3:4)
## \[ \, 1 \] \[ \, 2 \]
## [1,] 1 3
## [2,]
         2
cbind(1:2, 3:4, 5:6, 7:8)
## [,1] [,2] [,3] [,4]
## [1,] 1 3 5 7
## [2,] 2 4 6 8
sum(1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 42)
## [1] 108
```

• pass further arguments (as-is) to other methods:

**Example 9.32** The documentation of **lapply** (let us call **help**("lapply") now) states that this function is defined as **lapply**(X, FUN, ...). Here, the ellipsis is a placeholder for a number of optional arguments that can be passed to **FUN**. Hence, if we denote the i-th element of a vector X by X[[i]], calling **lapply**(X, FUN, ...) will return a list whose i-th element will be equal to **FUN**(X[[i]], ...).

**Exercise 9.33** Using a single call to **lapply**, generate a list with three numeric vectors of lengths 3, 9, and 7, respectively, drawn from the uniform distribution on the unit interval. Then, upgrade your code to get numbers sampled from the interval [-1, 1].

### 9.5.7 Metaprogramming (\*)

In the third part of this book, we will learn that we can access the expressions passed as functions' arguments programmatically. In particular, a call to the composition of **deparse** and **substitute** can convert them to a character vector:

```
test_deparse_substitute <- function(x)
    deparse(substitute(x))

test_deparse_substitute(testing+1+2+3)
## [1] "testing + 1 + 2 + 3"
test_deparse_substitute(spam & spam^2 & bacon | grilled(spam))
## [1] "spam & spam^2 & bacon | grilled(spam)"</pre>
```

**Exercise 9.34** Check out the y-axis label generated by **plot.default**((1:100)^2). Inspect its source code. Notice a call to the two aforementioned functions.

Similarly, call **shapiro.test(log(rlnorm(100)))** and take note of the data: field.

A function is free to do with such an expression whatever it likes. For instance, it can modify the expression and then evaluate it in a very different context. Such a language feature allows certain operations to be expressed much more compactly. In theory, it is a potent tool. Unfortunately, it is easy to find many practical examples where it was over/misused and made learning or using R confusing.

**Example 9.35** (\*) The built-in **subset** and **transform** use metaprogramming techniques to specify basic data frame transformations (see Section 12.3.9 and Section 17.5). For instance:

```
transform(
    subset(
        Sepal.Length>=7.7 & Sepal.Width >= 3.0,
        select=c(Species, Sepal.Length:Sepal.Width)
    ),
    Sepal.Length.mm=Sepal.Length/10
)
##
         Species Sepal.Length Sepal.Width Sepal.Length.mm
                          7.7
## 118 virainica
                                       3.8
                                                      0.77
## 132 virginica
                          7.9
                                       3.8
                                                      0.79
## 136 virginica
                           7.7
                                       3.0
                                                       0.77
```

None of the arguments (except iris) makes sense outside of the function call contexts. In particular, neither Sepal. Length nor Sepal. Width variables exist.

The two functions took the liberty to interpret the arguments passed how they felt. They created their own virtual reality within our well-defined world. The reader must refer to their documentation to discover the meaning of such special syntax.

manual page of **prop.test**, we read that the alternative parameter defaults to **c**("two. sided", "less", "greater") but that "two.sided" is actually the default one.

If we call **print(prop.test)**, we will find the code line responsible for this behaviour: "alternative <- **match.arg**(alternative)". Consider the following example:

```
test_match_arg <- function(x=c("a", "b", "c")) match.arg(x)

test_match_arg()  # missing argument - choose 1st
## [1] "a"
test_match_arg("c")  # one of the predefined options
## [1] "c"
test_match_arg("d")  # unexpected setting
## Error in match.arg(x): 'arg' should be one of "a", "b", "c"</pre>
```

In this setting, match.arg only allows an actual parameter from a given set of choices but selects the first option if the argument is missing.

Unfortunately, we have to learn this behaviour by heart because looking at the above source code gives us no clue about this being possible. If such an expression was normally evaluated, we would use either the default argument or whatever the user passed as x (but then the function would not know the range of possible choices). A call to "match.arg(x, c("a", "b", "c"))" could guarantee the desired functionality and would be much more readable. Instead, metaprogramming techniques allowed match.arg to access the enclosing function's default argument list without explicitly referring to them.

One may ask: why is it so? The only sensible answer to this will be "because its programmer decided it must be this way". Let us contemplate this for a while. In cases like these, we are not dealing with some base R language design choice that we might like or dislike, but which we should just accept as an inherent feature. Instead, we are struggling intellectually because of some programmer's (mis)use (in good faith...) of R's flexibility itself. They have introduced a slang/dialect on top of our mother tongue, whose meaning is valid only within this function. Blame the middleman, not the environment, please.

This is why we generally advocate for avoiding relying on metaprogramming-based techniques wherever possible. We shall elaborate on this in the third part of this book.

#### 9.6 Exercises

**Exercise 9.36** Answer the following questions:

• Will "stopifnot(1)" stop? What about "stopifnot(NA)", "stopifnot(TRUE, FALSE)", and "stopifnot(c(TRUE, TRUE, NA))"?

- What does the `if` function return?
- Does `attributes<-`(x, NULL) modify x?</li>
- When can we be interested in calling `[` and `[<-` as functions (and not as operators) directly?
- How to define our own binary operator? Can it have some default arguments?
- What are the main use cases of `...`?
- What is wrong with transform, subset, and match.arg?
- When a call like "f(-1, do\_something\_that\_takes\_a\_million\_years())" does not necessarily have to be a bad idea?
- What is the difference between "names(x)[1] <- "new name" and "names(x[1]) <- "new</li> name""?
- What might be the form of x if it is legit to call it like x[[c(1, 2)]]()()()[[1]]()()?

**Exercise 9.37** What is the return value of a call to "f(list(1, 2, 3))"?

```
f <- function(x)</pre>
    for (e in x) {
         print(e)
    }
}
```

Is it NULL, invisible(NULL), x[[length(x)]], or invisible(x[[length(x)]])?

**Exercise 9.38** The split function also has its replacement version. Study its documentation to learn how it works.

**Exercise 9.39** A call to **ls**(envir=baseenv()) returns all objects defined in the base package (see Chapter 16). List the names corresponding to some replacement functions.

**Important** Apply the principle of test-driven development when solving the remaining exercises (or those you have skipped intentionally).

**Exercise 9.40** Implement your version of the **Position** and **Find** functions. Evaluation should stop as soon as the first element fulfilling a given predicate has been found.

**Exercise 9.41** Implement your version of the **Reduce** function.

**Exercise 9.42** Write a function slide(f, x, k, ...) which returns a list y of size **length**(x)-k+1 such that y[[i]] = f(x[i:(i+k-1)], ...)

```
unlist(slide(sum, 1:5, 1))
## [1] 1 2 3 4 5
unlist(slide(sum, 1:5, 3))
                                                                    (continues on next page)
```

```
## [1] 6 9 12
unlist(slide(sum, 1:5, 5))
## [1] 15
```

**Exercise 9.43** Using **slide** defined above, write another function that counts how many increasing pairs of numbers are featured in a given numeric vector. For instance, in c(0, 2, 1, 0, 1, 6, 0), there are three such pairs: (0, 2), (0, 1), (1, 6).

**Exercise 9.44** (\*) Write your version of **tools**::package\_dependencies with reverse=TRUE based on information extracted by calling utils::available.packages.

**Exercise 9.45** (\*\*) Write a standalone program (that can be run from the system shell) that computes the total size of all the files in given directories given as the script's arguments (via **commandArgs**).

# S3 classes

Let x be a randomly generated matrix with 1 000 000 rows and 1 000 columns, y be a data frame with results from the latest survey indicating that things are not the way most people (no matter the side of the many political spectra) think they are, and and z be another matrix, this time with many zeroes.

Human brain is not capable of dealing with too much information which is too specific. This is why we have a natural tendency to group different entities based on their similarities so as to form some more abstract classes thereof.

Also, many of us are inherently lazy. Thus, oftentimes we will take shortcuts to minimise energy (at a price to be paid later).

Printing out a matrix, a data frame, and a time series are all instances of the displaying of things, although they undoubtedly differ in detail.

By now, we probably have forgotten which objects are hidden behind x, y, and z. Being able to simply call "**print**(y)" without having to recall that, yes, y is a data frame, might seem quite appealing.

This chapter introduces the so-called S3 classes [13], which provide a lightweight object-oriented programming (OOP) approach for automated dispatching of calls to *generics* of the type "print(y)" to concrete *methods* such as "print.data.frame(y)", based on the *class* of the object they are invoked upon.

S3 classes in their essence are beautifully simple<sup>1</sup>. They are inspired<sup>2</sup> by the well-thought-through concepts present in other functional programming languages (such as the Common Lisp Object System; see below). Ultimately, those *generics* and *methods* are ordinary R functions (Chapter 7) and *classes* are merely additional object attributes (Section 4.4).

Of course, this does not mean that wrapping our heads around them will be effortless. However, unlike other "class systems"<sup>3</sup>, S<sub>3</sub> is ubiquitous in R programming. Suffice it

<sup>&</sup>lt;sup>1</sup> However, some classes, even the built-in ones described here, can be poorly designed (some crucial methods might be missing, they can be not well-interoperable with other classes, etc.). Do not blame this messenger. Remember that the R environment is still very reliable. Also, there are cases where changing the current behaviour in one place could lead to undesirable consequences elsewhere.

<sup>&</sup>lt;sup>2</sup> They were built on top of the ordinary ("old S") R. Hence, they have certain limitations that we discuss in the sequel: classes cannot be formally defined (often we will use named lists for representing objects, and we know we cannot be any more flexible than this), and the dispatching can only be based on the class of one of the arguments (usually the first one, but, e.g., binary operators take both types into account).

<sup>&</sup>lt;sup>3</sup> Other class systems may give an impression that they are alien implants that were forcefully added to

to say that factors, matrices, and data frames discussed in the following chapters are quite straightforward, S3-based extensions of the concepts we introduce below.

#### Object type vs class 10.1

Recall that **typeof** (introduced in Section 4.1) returns the *internal* type of any R object. So far, the basic types we covered were mostly atomic and generic vectors (compare Figure 1 in the Preface).

```
typeof(NULL)
## [1] "NULL"
typeof(c(TRUE, FALSE, NA))
## [1] "logical"
typeof(c(1, 2, 3, NA_real_))
## [1] "double"
typeof(c("a", "b", NA_character_))
## [1] "character"
typeof(list(list(1, 2, 3), LETTERS))
## [1] "list"
typeof(function(x) x)
## [1] "closure"
```

The number of admissible types is small<sup>4</sup>, but they open the world of endless possibilities<sup>5</sup>. We will learn that they provide a basis for more complex data structures. This is thanks to the fact that they can be equipped with arbitrary attributes (Section 4.4).

Most compound types constructed using the mechanisms discussed in this chapter<sup>6</sup> only pretend they are something different from what they actually are. Still, they do their job very well most of the time. By knowing what is under their hood, we will demystify them and become able to manipulate their state outside of the prescribed use cases.

**Important** Setting the class attribute might make some objects behave differently in certain scenarios.

**Example 10.1** Let us consider two identical objects equipped with different class attributes.

our language to solve a specific, rather narrow class of problems; e.g., S4 (Section 11.5), reference classes (Section 16.1.5), and other ones proposed by third-party packages.

<sup>&</sup>lt;sup>4</sup> Their list is hardcoded at the Clanguage level; compare the list of SEXPTYPEs in [62] and see also Chapter

<sup>&</sup>lt;sup>5</sup> In particular, sec:xptr mentions externalptrs which are simply pointers to memory allocated on the heap, so these might be any instances of C structs or C++ classes, etc. This makes R a very extensible lan-

<sup>&</sup>lt;sup>6</sup> But there is more: see the S4 and reference class systems discussed in Section 11.5 and Section 16.1.5.

```
xt <- structure(123, class="POSIXct") # POSIX calendar time
xd <- structure(123, class="Date")</pre>
```

Both objects are represented using numeric vectors:

```
c(typeof(xt), typeof(xd))
## [1] "double" "double"
```

However, when printed, they are decoded quite differently:

```
print(xt)
## [1] "1970-01-01 10:02:03 AEST"
print(xd)
## [1] "1970-05-04"
```

In the former case, 123 is understood as the number of seconds since the so-called UNIX epoch, 1970-01-01T00:00:00+0000. The latter is deciphered as the number of days since the said timestamp.

Hence, we expect that there exists some underlying mechanism that calls a version of **print** dependent on an object's virtual class.

That this only relies on the class attribute, which might be set, unset, or reset quite freely, is emphasised below.

```
attr(xt, "class") <- "Date" # change class from POSIXct to Date
print(xt) # same 123, but now interpreted as Date
## [1] "1970-05-04"
as.numeric(xt) # drops all attributes
## [1] 123
unclass(xd) # drops the class attribute; `attr<-`(xd, "class", NULL)
## [1] 123</pre>
```

We are having so much fun that one more illustration can only increase our joy.

#### **Example 10.2** *Consider an example data frame:*

It is an object of the following class (an object whose class attribute is set to):

```
attr(x, "class")
## [1] "data.frame"
```

Some may say, and they are absolutely right, that we have not covered data frames yet. After all, they are the topic of Chapter 12, which is still ahead of us. However, from the current perspective, we should know that R data frames are merely lists (Chapter 4) of vectors of the same lengths equipped with names and row. names attributes.

```
typeof(x)
## [1] "list"
attr(x, "class") <- NULL # or x <- unclass(x)</pre>
print(x)
## $Sepal.Length
## [1] 5.1 4.9 4.7
##
## $Sepal.Width
## [1] 3.5 3.0 3.2
## attr(,"row.names")
## [1] 1 2 3
```

**Important** Revealing how x is *actually* represented, enables us to process it (although perhaps not in the most convenient or efficient manner) using the extensive skill set that we have already<sup>7</sup> developed by studying the material covered in the previous part of our book (including solving all the exercises). This can be particularly worthwhile, especially bearing in mind that some (built-in or third-party) data types are not particularly well-designed.

Let us underline again that attributes are simple additions to R objects. However, as we said in Section 4.4.3, certain attributes are special, and class is one of them.

In particular, we can set class to be only a character vector (possibly of length greater than one; see Section 10.2.5).

```
x <- 12345
attr(x, "class") <- 1 # character vectors only
## Error in attr(x, "class") <- 1: attempt to set invalid 'class' attribute
```

Furthermore, the class function can read the value of the class attribute. Its replacement version is also available.

```
class(x) <- "Date" # set; the same as attr(x, "class") <- "Date"</pre>
class(x) # get; the same as attr(x, "class")
## [1] "Date"
```

**Important** The class function always yields a value, even if the corresponding at-

<sup>&</sup>lt;sup>7</sup> For instance, consider once again the example from Section 5.4.3 that applies the **split** function on a data frame reduced to a list.

tribute is not set. We call it an *implicit* class. Compare the following and the outputs generated by **typeof**:

```
class(NULL) # no `class` set, because NULL cannot have attributes at all
## [1] "NULL"
class(c(TRUE, FALSE, NA)) # no attributes, so class is implicit (= typeof)
## [1] "logical"
class(c(1, 2, 3, NA_real_)) # typeof yields "double"
## [1] "numeric"
class(c("a", "b", NA_character_))
## [1] "character"
class(list(list(1, 2, 3), LETTERS))
## [1] "list"
class(function(x) x) # typeof yields "closure"
## [1] "function"
```

Also, Chapter 11 will explain that any object equipped with the dim attribute also has an implicit class:

```
(x <- as.matrix(c(1, 2, 3)))
## [,1]
## [1,] 1
## [2,] 2
## [3,] 3
attributes(x) # `class` is not amongst the attributes
## $dim
## [1] 3 1
class(x) # implicit class
## [1] "matrix" "array"
typeof(x) # it is still a numeric vector (under the hood)
## [1] "double"</pre>
```

## 10.2 Generics and method dispatching

## 10.2.1 Generics, default, and custom methods

Let us inspect the source code of the **print** function:

```
print(print) # sic!
## function (x, ...)
## UseMethod("print")
## <environment: namespace:base>
```

Any function like the above we will call from now on a *generic* (*S3 generic*, from S version 3). Its only job is to invoke **UseMethod**("print"). It dispatches the control flow to another function, referred to as a *method*, based on the class of the first argument.

**Important** Even though it cannot be implied by reading the above source code, all arguments passed to the generic will also be available in the dispatched method.

For example, let us define an object of the class categorical (a name that we have just come up with; we could have called it cat, CATEGORICAL, or SpanishInquisition as well), which will be our own version of the famous built-in factor type that we discuss later.

```
x <- structure(
    c(1, 3, 2, 1, 1, 1, 3),
    levels=c("a", "b", "c"),
    class="categorical"
)</pre>
```

We assume that such an object is a sequence of small positive integers (codes). It is equipped with a character vector of length no less than the maximum of the said integers, stored as its levels attribute. For example, the first category will be used to decipher the meaning of code "1". Hence, the above vector represents a sequence a, c, b, a, a, a, a, c.

We have not defined any special method for printing objects of the categorical class. Hence, when we call **print**, the *default* (fallback) method will be called:

```
print(x)
## [1] 1 3 2 1 1 1 3
## attr(,"levels")
## [1] "a" "b" "c"
## attr(,"class")
## [1] "categorical"
```

It is the standard function for displaying numeric vectors that we are all well familiar with. Its name is print.default, and we can always call it directly:

```
print.default(x) # the default print method
## [1] 1 3 2 1 1 1 3
## attr(,"levels")

(continues on next page)
```

<sup>&</sup>lt;sup>8</sup> Some functions can have a version of **UseMethod** hidden at the C language level (internally); see Section 10.2.3.

<sup>&</sup>lt;sup>9</sup> This uses quite an obscure hack. It should also be noted that **UseMethod** heavily relies on metaprogramming (compare Chapter 17). Therefore, we do not consider it an ordinary function call. For instance, it can only be called inside a function's body. Also, once called, it does not return to the generic. Before dispatching to a particular method, it creates a couple of hidden variables which give more detail on the operation conveyed, e.g., `.Generic` or `.Class`; see help("UseMethod") and Section 5 in [63].

(continued from previous page)

```
## [1] "a" "b" "c"
## attr(,"class")
## [1] "categorical"
```

However, we can introduce our own method for printing categorical objects. Its name must precisely be **print.categorical**:

```
print.categorical <- function(x, ...)
{
    x_character <- attr(x, "levels")[unclass(x)]
    print(x_character) # calls `print.default`
    cat(sprintf("Categories: %s\n",
        paste(attr(x, "levels"), collapse=", ")))
    invisible(x) # this is what all print methods do; see help("print")
}</pre>
```

Now, calling **print** automatically dispatches the control flow to the above method:

```
print(x)
## [1] "a" "c" "b" "a" "a" "a" "c"
## Categories: a, b, c
```

Of course, the default method can still be called; calling **print.default**(x) directly will output the same result as before.

**Note print.categorical** has been equipped with the dot-dot attribute because the generic **print** had one too. We are expected to ensure consistency ourselves<sup>10</sup>.

## 10.2.2 Creating own generics

Introducing new S3 generics is as straightforward as defining a function that calls UseMethod.

For instance, here is a dispatcher which allows for creating new objects of the categorical class based on other objects:

```
as.categorical <- function(x, ...)
UseMethod("as.categorical") # synonym: UseMethod("as.categorical", x)</pre>
```

We always need to define the default method:

<sup>&</sup>lt;sup>10</sup> In particular, checking S3 generic/method consistency is part of R package check.

```
x <- as.character(x)
xu <- unique(sort(x)) # drops NAs
structure(
    match(x, xu),
    class="categorical",
    levels=xu
)
}</pre>
```

Testing:

```
as.categorical(c("a", "c", "a", "a", "d", "c"))

## [1] "a" "c" "a" "d" "c"

## Categories: a, c, d

as.categorical(c(3, 6, 4, NA, 9, 9, 6, NA, 3))

## [1] "3" "6" "4" NA "9" "9" "6" NA "3"

## Categories: 3, 4, 6, 9
```

Here, **print.categorical** was invoked twice. The above is quite flexible already: it relies on the *generic* (Section 10.2.3) **as.character**, which handles a wide variety of data types.

**Example 10.3** For instance, we might want to forbid the conversion from lists because this does not necessarily make sense:

```
as.categorical.list <- function(x, ...)
    stop("conversion of lists to categorical is not supported")</pre>
```

The users can always be instructed in the method's documentation that they are solely responsible for an explicit conversion of list objects to something different prior to a call to **as.categorical**. Whether this was a justified design choice, time will tell.

**Example 10.4** The default method deals with logical vectors perfectly fine:

```
as.categorical(c(TRUE, FALSE, NA, NA, FALSE)) # as.categorical.default
## [1] "TRUE" "FALSE" NA NA "FALSE"
## Categories: FALSE, TRUE
```

However, we might still want to introduce uts specialised version because we know a slightly more efficient algorithm (and we have nothing better to do) based on the fact that FALSE and TRUE converted to numeric yield 0 and 1, respectively:

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```
x + 1, # only 1, 2, and NAs will be generated
    class="categorical",
    levels=c("FALSE", "TRUE")
)
```

It yields the same result but is slightly faster:

```
as.categorical(c(TRUE, FALSE, NA, NA, FALSE)) # as.categorical.logical
## [1] "TRUE" "FALSE" NA NA "FALSE"
## Categories: FALSE, TRUE
```

We performed some argument validation at the beginning: a user is always able to call a method directly on an R object of any kind (which is a good thing; see Section 10.2.4). In other words, there is no guarantee that the argument x must be of type logical.

### 10.2.3 Built-in generics

Many functions and operators we have introduced so far are, in fact, S3 generics: print, head, `[`, `+`, `<=`, as.character, as.list, round, log, sum, c, and na.omit, to name a few.

Some of them might not even call **UseMethod** explicitly; dispatching can be done internally at the C language level<sup>11</sup>. Overall, generating the list of all S3 generics is somewhat tricky<sup>12</sup>. Luckily, at least the internal ones are enumerated in **help**("InternalMethods") and **help**("groupGeneric").

**Example 10.5** Let us overload the **as.character** method. The default one does not make much sense for the objects of our custom type:

```
as.character(x)
## [1] "1" "3" "2" "1" "1" "3"
```

So:

```
as.character.categorical <- function(x, ...)
attr(x, "levels")[unclass(x)]</pre>
```

And now:

<sup>&</sup>lt;sup>11</sup> This is quite unfortunate because it decreases transparency. We need to look this information up somewhere in the documentation (instead of simply inspecting a function's source code; see, e.g., cbind). Also, it allows for some methods to be hardcoded at the C language level too, and thus be unoverloadable. However, some of such design choices can somewhat be defended as they increase execution speed or memory consumption. Overall, we are not particularly happy about them.

<sup>&</sup>lt;sup>12</sup> See also .knownS3Generics and .S3\_methods\_table, which are related to the advanced topics we will cover in Section 16.3.6.

```
as.character(x)
## [1] "a" "c" "b" "a" "a" "a" "c"
```

**Exercise 10.6** Overload the **unique** and **rep** methods for objects of the class categorical.

**Example 10.7** New types ought to be designed carefully. For instance, if we forget to consider overloading the to-numeric converter, we might end up with some users being puzzled<sup>13</sup> when they see:

```
(x \leftarrow as.categorical(c(4, 9, 100, 9, 9, 100, 42, 666, 4)))
            "9" "100" "9" "9" "100" "42" "666" "4"
## [1] "4"
## Categories: 100, 4, 42, 666, 9
as.double(x) # as.double.default(x)
## [1] 2 5 1 5 5 1 3 4 2
```

Hence, we might want to introduce:

```
as.double.categorical <- function(x, ...)</pre>
ſ
    # as.double.default(as.character.categorical(x))
    as.double(as.character(x))
}
```

Which now yields:

```
as.double(x) # as.double.categorical(x)
## [1]
            9 100
                       9 100 42 666
```

**Note** We can still use unclass to fetch the codes:

```
unclass(x)
## [1] 2 5 1 5 5 1 3 4 2
## attr(,"levels")
## [1] "100" "4" "42" "666" "9"
```

It is because the above returns a class-free object, which is now guaranteed to be processed by the default methods (**print**, subsetting, **as.character**, etc.).

Exercise 10.8 What would happen if we used as.numeric instead of unclass in print. categorical and as.character.categorical?

<sup>13</sup> It is a different story if this is our conscious design choice and if we really want this behaviour. If we document it thoroughly (see how help("factor") discusses the behaviour of a to-numeric conversion), only a user's ignorance will there be to blame when they still are confused about it. Remember that we can never make an API totally foolproof and that there will always be someone to challenge/stress-test our ideas. Bad design is always wrong, but being overprotective also has its cons. Choose your audience wisely.

**Exercise 10.9** Update the above methods so that we can also create named objects of the class categorical (i.e., equipped with the names attribute).

**Exercise 10.10** The levels of x are sorted lexicographically, not numerically. Introduce a single method that would make the above code (when rerun without any alterations) generate a more natural result.

### 10.2.4 First-argument dispatch and calling S3 methods directly

With S3, the dispatching is done most often based on the class of only one<sup>14</sup> argument: by default, the first one from the parameter list.

For example, the **c** function is a generic that dispatches on the first argument's class. Let us overload it for categorical objects. In other words, let us create a function dispatched by the generic when called on a series of objects whose first element is of the said class.

```
c.categorical <- function(...)
  as.categorical(
    unlist(
        lapply(list(...), as.character)
    )
)</pre>
```

It converts each argument to a character vector (relying on the generic as.character to take care of the details). It works because unlist converts a list of such atomic vectors to a single sequence of strings.

Calling **c** with the first argument being of the class categorical dispatches to the above method:

```
x <- c(9, 5, 7, 7, 2)
xc <- as.categorical(x)
c(xc, x) # c.categorical
## [1] "9" "5" "7" "7" "2" "9" "5" "7" "7" "2"
## Categories: 2, 5, 7, 9</pre>
```

However, if the first argument is, say, unclassed, the default method will be consulted:

```
c(x, xc) # default c
## [1] 9 5 7 7 2 4 2 3 3 1
```

This method ignores the class attribute and sees xc as it is, a barebone numeric vector:

<sup>&</sup>lt;sup>14</sup> There are many exceptions to this rule. They were made for the (debatable) sake of the R users' convenience. In particular, in Section 12.1.2 we mention that **cbind** and **rbind** will dispatch to the data. frame method if at least one argument is a data frame (and others are unclassed). Binary operators dispatch on the type of both operands; see Section 10.2.6. Furthermore, it is worth noting that the S4 class system (Section 11.5) allows for dispatching based on the classes many arguments.

```
`attributes<-`(xc, NULL) # the underlying codes
## [1] 4 2 3 3 1</pre>
```

It is not a bug. It is a well-documented (and now explained) behaviour. After all, compound types (classed objects) are merely emulated through the basic ones.

**Important** In most cases, S3 methods can be called directly to get the desired outcome:

```
c.categorical(x, xc) # force a call to the specific method
## [1] "9" "5" "7" "2" "9" "5" "7" "2"
## Categories: 2, 5, 7, 9
```

We said in most cases because some methods can be:

- hardcoded at the C language level (for instance, there is no c.default defined at all<sup>15</sup>),
- hidden (defined in a package's namespace but not exported); see Section 16.3.6,
- overloaded as a group; see Section 10.2.6 and help("groupGeneric").

**Example 10.11** Just for fun, let us find a partition of the iris dataset into three clusters using the k-means algorithm:

```
res <- kmeans(iris[-5], centers=3, nstart=10)
print(res)
## K-means clustering with 3 clusters of sizes 50, 62, 38
## Cluster means:
##
   Sepal.Length Sepal.Width Petal.Length Petal.Width
                       1.4620
## 1
       5.0060
               3.4280
                               0.2460
## 2
       5.9016
              2.7484
                       4.3935
                               1.4339
## 3
       6.8500
              3.0737
                       5.7421
                               2.0711
##
## Clustering vector:
[ reached getOption("max.print") -- omitted 51 entries ]
##
## Within cluster sum of squares by cluster:
```

<sup>(</sup>continues on next page)

<sup>&</sup>lt;sup>15</sup> Dispatching to internal methods can also be done... internally. For instance, overloading `<.character` (or Compare.character; see below) will have no effect unless the base `<` is replaced with a custom one that makes an explicit call to UseMethod. Most often, we can expect that the built-in types (e.g., atomic vectors), factors, data frames, and matrices and other arrays might be treated specially.

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```
## [1] 15.151 39.821 23.879
## (between_SS / total_SS = 88.4 %)
##
## Available components:
##
## [1] "cluster" "centers" "totss" "withinss"
## [5] "tot.withinss" "betweenss" "size" "iter"
## [9] "ifault"
```

The above is an object of the class:

```
class(res)
## [1] "kmeans"
```

which, in fact, is a:

```
typeof(res)
## [1] "list"
```

The underlying list looks like:

```
unclass(res)
## $cluster
## [ reached getOption("max.print") -- omitted 51 entries ]
##
## $centers
## Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1
      5.0060
             3.4280
                     1.4620
                             0.2460
## 2
      5.9016
             2.7484
                     4.3935
                            1.4339
      6.8500 3.0737 5.7421
## 3
                            2.0711
##
## $totss
## [1] 681.37
##
## $withinss
## [1] 15.151 39.821 23.879
##
## $tot.withinss
## [1] 78.851
##
## $betweenss
## [1] 602.52
```

(continued from previous page)

```
##
## $size
## [1] 50 62 38
##
## $iter
## [1] 2
##
## $ifault
## [1] 0
```

We already know that the above was displayed in a fancy way only because there is a print method overloaded for objects of the kmeans class.

But is there?

```
print.kmeans
## Error in eval(expr, envir, enclos): object 'print.kmeans' not found
```

Even though the method is hidden (internal) in the stats package's namespace, from Section 16.3.6 we will learn that it can be accessed by calling **getS3method("print", "kmeans")** or referring to **stats**:::**print.kmeans** (note the triple colon).

#### 10.2.5 Multi-class-ness

The class attribute can be instantiated as a character vector of any length. For example:

```
(t1 <- Sys.time())
## [1] "2023-05-03 16:43:06 AEST"
(t2 <- strptime("2021-08-15T12:59:59+1000", "%Y-%m-%dT%H:%M:%S%z"))
## [1] "2021-08-15 12:59:59"
```

Let us inspect the classes of these two objects:

```
class(t1)
## [1] "POSIXct" "POSIXt"
class(t2)
## [1] "POSIXlt" "POSIXt"
```

Section 10.3.1 will discuss date-time classes in more detail. It will highlight that the former is represented as a numeric vector, while the latter is a list. Thus, these two should primarily be seen as instances of two distinct types.

However, both of them have a lot in common. Hence, it was a wise design choice to allow them to be seen also as the representatives of the same generic category of POSIX time objects.

**Important** When calling a generic function  $^{16}$  **f** on an object x of the classes  $^{17}$  class 1, class 2, ..., class 8 (in this order), **UseMethod** (f, x) dispatches to the method determined as follows:

- 1. if **f.class1** is available 18, call it;
- 2. otherwise, if **f.class2** is available, call this one;
- 3. ...;
- 4. otherwise, if **f.classK** is available, invoke it;
- 5. otherwise, refer to the fallback f.default.

**Example 10.12** There is a method **diff** for objects of the class POSIXt featuring a statement:

```
r <- if (inherits(x, "POSIXlt")) as.POSIXct(x) else x
```

This way, we can process both POSIXct and POSIXlt instances using the same procedure.

Let us see no magic in this simple scheme. It is nothing more than what we described above: a way to determine which method to call for a particular R object. It can be used as a mechanism to mimic the idea of inheritance in object-oriented programming languages. However, the S3 system does not allow for defining classes in any formal manner.

For example, we cannot say that objects of the class POSIXct inherit from POSIXt. Neither can we say that each object of the class POSIXct is also an instance of POSIXt. The class attribute can still be set arbitrarily on a per-object basis. We can create ones whose class is simply POSIXct (without the POSIXt part) or even c("POSIXt", "POSIXct") (in this order).

**Note** In any method, it is possible to call the method corresponding to the next class by calling **NextMethod**.

For instance, if we are in **f.class1**, a call to **NextMethod**(f) will try invoking **f.class2**. If such a method does not exist, further methods in the search chain will be tried, falling back to the default method if necessary. An example will be given below.

## 10.2.6 Operator overloading

Operators are ordinary functions (Section 9.4.5). Even though what follows can partially be implied by what we have said above, as usual in R, there will be some oddities.

<sup>&</sup>lt;sup>16</sup> The case of binary operators is handled differently; see Section 10.2.6.

<sup>&</sup>lt;sup>17</sup> **UseMethod** dispatches on the implicit class as determined by the **class** function. Note that the class attribute does not necessarily have to be set in order for **class** to return a sensible answer.

<sup>&</sup>lt;sup>18</sup> For more details on S3 method lookup; see Section 16.3.6.

For example, let us overload the index operator for objects of the class categorical. Looking at **help**("["), we see that the default method has two arguments: x (the categorical object being sliced) and i (the indexer). Ours will have the same interface then:

```
`[.categorical` <- function(x, i)
{
    structure(
        unclass(x)[i], # `[`(unclass(x), i)
        class="categorical",
        levels=attr(x, "levels") # the same levels as input
    )
}</pre>
```

However, the default S3 method, `[.default`, is hardcoded at the C language level. Therefore, we cannot refer to it directly. We have to call unclass instead. Alternatively, we can also call NextMethod:

```
`[.categorical` <- function(x, i)
{
    structure(
        NextMethod("["), # call default method, passing `x` and `i`
        class="categorical",
        levels=attr(x, "levels") # the same levels as input
    )
}</pre>
```

We can also introduce the replacement version of this operator:

```
`[<-.categorical` <- function(x, i, value)
{
    levels <- attr(x, "levels")</pre>
    value <- match(value, levels) # integer codes corresponding to levels
    structure(
        NextMethod("[<-"), # call default method, passing `x`, `i`, `values`
        class="categorical",
        levels=levels # same levels as input
    )
    # # or, equivalently:
    # structure(
          `[<-`(unclass(x), i, value=match(value, attr(x, "levels"))),
          class="categorical",
          levels=attr(x, "levels")
    # )
}
```

#### Testing:

```
x <- as.categorical(c(3, 6, 4, NA, 9, 9, 6, NA, 3))
x[1:4]
## [1] "3" "6" "4" NA
## Categories: 3, 4, 6, 9
x[1:4] <- c("6", "7")
print(x)
## [1] "6" NA "6" NA "9" "9" "6" NA "3"
## Categories: 3, 4, 6, 9</pre>
```

Notice how we handled the case of nonexistent levels and that the recycling rule has been automagically inherited (amongst other features) from the default index operator.

**Exercise 10.13** Do these two operators preserve the names attribute of x? Is indexing with negative integers or logical vectors supported as well? Why is that/is that not the case?

Furthermore, let us overload the `==` operator. Assume<sup>19</sup> that we would like two categorical objects to be compared based on the actual labels they encode, in an elementwise manner:

```
`==.categorical` <- function(e1, e2)
    as.character(e1) == as.character(e2)</pre>
```

We are feeling lucky: by not performing any type checking, we rely on the particular **as.character** methods corresponding to the types of e1 and e2. Also, assuming that **as.character** always<sup>20</sup> returns a character object, we dispatch to the default method for `==` (which handles atomic vectors).

#### Some examples:

```
as.categorical(c(1, 3, 5, 1)) == as.categorical(c(1, 3, 1, 1))
## [1] TRUE TRUE FALSE TRUE
as.categorical(c(1, 3, 5, 1)) == c(1, 3, 1, 1)
## [1] TRUE TRUE FALSE TRUE
c(1, 3, 5, 1) == as.categorical(c(1, 3, 1, 1))
## [1] TRUE TRUE FALSE TRUE
```

**Important** In the case of binary operators, dispatching is done based on the classes of both arguments. In all three example calls above, we call `==.categorical`, regardless of whether the classed object is the first or the second operand.

<sup>&</sup>lt;sup>19</sup> There are, of course, many possible ways to implement the `==` operator for the discussed objects. For instance, it may return either a single TRUE or FALSE depending on if two objects are identical (although probably overloading all.equal would be a better idea). We could also compare the corresponding underlying integer codes instead of the labels, etc.

<sup>&</sup>lt;sup>20</sup> Which, of course, does not have to be the case; it is merely an assumption based on our belief in the common sense of other developers.

If two operands are classed, and different methods are overloaded for both, a warning will be generated, and the default internal method will be called.

```
`==.A` <- function(e1, e2) "A"

`==.B` <- function(e1, e2) "B"

structure(c(1, 2, 3), class="A") == structure(c(2, NA, 3), class="B")

## Warning: Incompatible methods ("==.A", "==.B") for "=="

## [1] FALSE NA TRUE</pre>
```

**Note** (\*) By defining a single **Ops** method, we can define the meaning of all binary operators at once.

```
Ops.categorical <- function(e1, e2)
{
   if (!(.Generic %in% c("<", ">", "<=", ">=", "==", "!=")))
      stop(sprintf("%s not defined for 'categorical' objects", .Generic))
   e1 <- as.character(e1)
   e2 <- as.character(e2)
   NextMethod(.Generic) # dispatch to the default method (for character)
}
as.categorical(c(1, 3, 5, 1)) > c(1, 2, 4, 2)
## [1] FALSE TRUE TRUE FALSE
```

Here . Generic is a variable representing the name of the operator (generic) being invoked; see sec:use-method.

Other group generics are: Summary (including functions such as min, sum, and all), Math (abs, log, round, etc.), and Complex (e.g., Re, Im); see help("groupGeneric") for more details.

Sometimes we must rely on **registerS3method** to force R to recognise a custom method related to such generics.

#### 10.3 Common built-in S3 classes

Let us discuss some noteworthy built-in classes, including those representing datetime information and factors (ordered or not).

Classes for representing tabular data will be dealt with in separate parts of this text-book, owing to their importance and ubiquity. Namely, matrices and other arrays are covered in Chapter 11, and data frames are discussed in Chapter 12.

Inspecting other<sup>21</sup> interesting classes is left as a simple exercise for the kind reader.

#### 10.3.1 Date, time, etc.

The Date class can be used to represent... dates.

```
(x <- c(Sys.Date(), as.Date(c("1969-12-31", "1970-01-01", "2023-02-29"))))
## [1] "2023-05-03" "1969-12-31" "1970-01-01" NA
class(x)
## [1] "Date"</pre>
```

Complex types are built upon basic ones; underneath, what we deal with is:

```
typeof(x)
## [1] "double"
unclass(x)
## [1] 19480 -1 0 NA
```

which is the number of days since the *UNIX epoch*, 1970-01-01T00:00:00+0000 (midnight GMT/UTC).

The POSIXct (calendar time) class can be used to represent date-time objects:

```
(x <- Sys.time())
## [1] "2023-05-03 16:43:07 AEST"
class(x)
## [1] "POSIXct" "POSIXt"
typeof(x)
## [1] "double"
unclass(x)
## [1] 1683096187</pre>
```

Underneath, it is the number of seconds since the UNIX epoch. By default, whilst printing, the current default timezone is used (see **Sys.timezone**). However, such objects can be equipped with the tzone attribute.

```
structure(1, class=c("POSIXct", "POSIXt")) # using current default timezone
## [1] "1970-01-01 10:00:01 AEST"
structure(1, class=c("POSIXct", "POSIXt"), tzone="UTC")
## [1] "1970-01-01 00:00:01 UTC"
```

In both cases, the time is 1 second after the beginning of the UNIX epoch. On the author's PC, the former is displayed in the current local timezone, though.

**Exercise 10.14** Use **ISOdatetime** to inspect how midnights are displayed in different timezones.

 $<sup>^{21}</sup>$  unique(.S3\_methods\_table[, 2]) generates an (incomprehensive) approximation to the list of available classes.

The POSIXLt (local time) class is represented using a list of atomic vectors<sup>22</sup>.

```
(x <- as.POSIXlt(c(a="1970-01-01 00:00:00", b="2030-12-31 23:59:59")))
##
## "1970-01-01 00:00:00 AEST" "2030-12-31 23:59:59 AEDT"
class(x)
## [1] "POSIXlt" "POSIXt"
typeof(x)
## [1] "list"
str(unclass(x)) # calling str instead of print to make display more compact
## List of 11
## $ sec : num [1:2] 0 59
## $ min : int [1:2] 0 59
## $ hour : int [1:2] 0 23
## $ mday : int [1:2] 1 31
## $ mon : int [1:2] 0 11
## $ year : Named int [1:2] 70 130
## ..- attr(*, "names")= chr [1:2] "a" "b"
## $ wday : int [1:2] 4 2
## $ yday : int [1:2] 0 364
## $ isdst : int [1:2] 0 1
## $ zone : chr [1:2] "AEST" "AEDT"
## $ gmtoff: int [1:2] NA NA
## - attr(*, "tzone")= chr [1:3] "" "AEST" "AEDT"
## - attr(*, "balanced")= logi TRUE
```

**Exercise 10.15** Read about the meaning of each named element, especially mon and year; see **help**("DateTimeClasses").

The manual states that POSIXIt is supposedly *closer to human-readable forms* than POSIXct, but it is a matter of taste. Some R functions return the former, and some yield the latter type.

**Exercise 10.16** The two main functions for date formatting and parsing, **strftime** and **strptime**, use special field formatters (similar to **sprintf**). Read about them in the R manual. What type of inputs do they accept? What outputs do they produce?

There are several methods overloaded for objects of the said classes. In fact, the first call in this section already involved the use of **c.Date**.

**Exercise 10.17** Play around with the overloaded versions of **seq**, **rep**, and **as.character**.

A specific number of days or seconds can be added to or subtracted from a date or time, respectively. However, `-` (see also **diff**) can also be applied on two date-time objects, which yields an object of the class difftime.

<sup>&</sup>lt;sup>22</sup> Which was inspired by struct tm in C's <time.h>.

```
Sys.Date() - (Sys.Date() - 1)
## Time difference of 1 days
Sys.time() - (Sys.time() - 1)
## Time difference of 1 secs
```

**Exercise 10.18** Check out how objects of the class difftime are internally represented.

Applying other arithmetic operations on date-time objects yields an error. Because date-time objects are just numbers, they can be compared to each other using binary operators<sup>23</sup>. Also, methods such as **sort** and **order**<sup>24</sup> could be applied on them.

**Exercise 10.19** Check out the **stringx** package, which replaces the base R date-time processing functions with their more portable counterparts.

**Exercise 10.20** proc. time can be used to measure the time to execute a given expression:

```
t0 <- proc.time() # timer start
# ... to do - something time-consuming ...
sum(runif(1e7)) # whatever, just testing
## [1] 4999488
print(proc.time() - t0) # elapsed time
## user system elapsed
## 0.255 0.013 0.267</pre>
```

The function returns an object of the class proc\_time. Inspect how it is represented internally.

#### 10.3.2 Factors

The factor class is often used to represent categorical (qualitative) data, e.g., species, groups, types. In fact, categorical (the example class that we played with above) was inspired by the built-in factor.

```
(x <- c("spam", "spam", "bacon", "sausage", "spam", "bacon"))
## [1] "spam" "spam" "bacon" "sausage" "spam" "bacon"
(f <- factor(x))
## [1] spam spam bacon sausage spam bacon
## Levels: bacon sausage spam</pre>
```

Note how factors are printed. There are no double quote characters around the labels. The list of levels is given at the end.

Internally, such objects are represented as integer vectors (Section 6.4.1) with elements between 1 and k. They are equipped with the special (as in Section 4.4.3) levels attribute, which is a character vector of length  $k^{25}$ .

<sup>&</sup>lt;sup>23</sup> The overloaded group generic **Ops** prevents us from adding or multiplying two dates and defines the meaning of the relational operators. As an exercise, check out its source code.

<sup>&</sup>lt;sup>24</sup> See an exercise below on the use of xtfrm.

<sup>&</sup>lt;sup>25</sup> [63] states: Factors are currently implemented using an integer array to specify the actual levels and a second array

```
class(f)
## [1] "factor"
typeof(f)
## [1] "integer"
unclass(f)
## [1] 3 3 1 2 3 1
## attr(,"levels")
## [1] "bacon" "sausage" "spam"
attr(f, "levels") # also: levels(f)
## [1] "bacon" "sausage" "spam"
```

Factors are often used instead of character vectors defined over a small number of unique labels<sup>26</sup>, where there is a need to manipulate their levels easily.

```
attr(f, "levels") <- c("a", "b", "c") # also levels(f) <- c(....new...)
print(f)
## [1] c c a b c a
## Levels: a b c
```

The underlying codes remain the same.

Certain operations on vectors of small integers are relatively easy to implement, especially those concerning element grouping: splitting, counting, and plotting (e.g., Figure 13.17). It is because the integer codes can naturally be used whilst indexing other vectors. Section 5.4 mentioned a few functions related to this, such as match, split, findInterval, and tabulate. Specifically, the latter can be implemented like "for each i, increase count[factor codes[i]] by one".

**Exercise 10.21** Study the source code of the **factor** function. Note the use of **as.character**, unique, order, and match.

**Exercise 10.22** Implement a simplified version of table based on tabulate. It should work for objects of the class factor and return a named numeric vector.

Exercise 10.23 Implement your version of cut based on findInterval.

**Important** The as.numeric method has not been overloaded for factors. Therefore, when we call the generic, the default method is used: it returns the underlying integer codes as-is. This can surprise unaware users when they play with factors that feature levels consisting of strings representing integer numbers:

```
(g <- factor(c(11, 15, 16, 11, 13, 4, 15))) # converts numbers to strings
                                                                  (continues on next page)
```

of names that are mapped to the integers. Rather unfortunately users often make use of the implementation in order to make some calculations easier. This, however, is an implementation issue and is not guaranteed to hold in all implementations of R. Still, fortunately, this has been a de facto standard for factors for a very long time.

<sup>&</sup>lt;sup>26</sup> Recall that there is a global (internal) string cache. Hence, having many duplicated strings is not an issue, memory-use-wisely.

(continued from previous page)

```
## [1] 11 15 16 11 13 4 15
## Levels: 4 11 13 15 16
as.numeric(g) # the underlying codes
## [1] 2 4 5 2 3 1 4
as.numeric(as.character(g)) # to get the numbers en-coded
## [1] 11 15 16 11 13 4 15
```

Unfortunately, support for factors is often hardcoded at the C language level, which will make this class behave less predictably (from the R perspective). In particular, the manual overloading of methods for factor objects might have no effect.

**Important** If f is a factor, then x[f] does not behave like x[as.character(f)] (indexing by labels, using the names attribute). Instead, we get x[as.numeric(f)] (the underlying codes will determine the positions).

```
h <- factor(c("a", "b", "a", "c", "a", "c"))

levels(h)[h] # the same as c("a", "b", "c")[c(1, 2, 1, 3, 1, 3)]

## [1] "a" "b" "a" "c" "a" "c"

c(b="x", c="y", a="z")[h] # names are not used whilst indexing

## b c b a b a

## "x" "y" "x" "z" "x" "z"

c(b="x", c="y", a="z")[as.character(h)] # names are used now

## a b a c a c

## "z" "x" "z" "y" "z" "y"
```

More often than not, indexing by factors will happen "accidentally", leaving us slightly puzzled. In particular, factors look much like character vectors when they are featured in data frames:

```
(df <- data.frame(A=c("x", "y", "z"), B=factor(c("x", "y", "z"))))
## A B
## 1 x x
## 2 y y
## 3 z z
class(df[["A"]])
## [1] "character"
class(df[["B"]])
## [1] "factor"</pre>
```

(\*) Up until R 4.0, many functions (including data.frame and read.csv) had the string-sAsFactors option (see help("options")) set to TRUE, which resulted in all character vectors' being automatically converted to factors when, e.g., creating data frames (compare Chapter 12). Luckily, this is no longer the case, but they can still be en-

countered sporadically: for instance, the built-in iris dataset has the fifth column of the class:

```
class(iris[["Species"]])
## [1] "factor"
```

**Important** Be careful when combining factors and not-factors:

```
x <- factor(c("A", "B", "A"))
c(x, "C")
## [1] "1" "2" "1" "C"
c(x, factor("C"))
## [1] A B A C
## Levels: A B C</pre>
```

**Exercise 10.24** When subsetting a factor object, the result will inherit the levels attribute asis:

```
f[c(1, 2)] # drop=FALSE
## [1] c c
## Levels: a b c
```

However:

```
f[c(1, 2), drop=TRUE]
## [1] c c
## Levels: c
```

Implement your version of the **droplevels** function, which removes the unused attributes.

**Exercise 10.25** The replacement version of the index operator does not automatically add new levels to the modified object:

```
x <- factor(c("A", "B", "A"))
`[<-`(x, 4, value="C")  # like in x[4] <- "C"
## Warning in `[<-.factor`(x, 4, value = "C"): invalid factor level, NA
## generated
## [1] A B A <NA>
## Levels: A B
```

Implement your version of `[<-.factor]`, which is capable of doing so.

#### 10.3.3 Ordered factors

When creating factors, we can enforce a particular ordering and the number of levels:

```
x <- c("spam", "spam", "bacon", "sausage", "spam", "bacon")
factor(x, levels=c("eggs", "bacon", "sausage", "spam"))
## [1] spam spam bacon sausage spam bacon
## Levels: eggs bacon sausage spam</pre>
```

If we want the arrangement of the levels to define a linear ordering relation over the set of labels, we can call:

```
(f <- factor(x, levels=c("eggs", "bacon", "sausage", "spam"), ordered=TRUE))
## [1] spam spam bacon sausage spam bacon
## Levels: eggs < bacon < sausage < spam
class(f)
## [1] "ordered" "factor"</pre>
```

It yields an ordered factor, which enables comparisons like:

```
f[f >= "bacon"] # what's not worse than bacon?
## [1] spam spam bacon sausage spam bacon
## Levels: eggs < bacon < sausage < spam</pre>
```

How is that possible? Well, based on information provided in this chapter, it will come as no surprise that it is because... someone has implemented a relational operator for objects of the class ordered.

## 10.3.4 Formulae (\*)

Formulae are created using the `~` operator. Some R users employ them to specify widely-conceived *statistical models* in functions such as <code>lm</code> (e.g., linear regression), <code>glm</code> (generalised linear models: logistic regression etc.), <code>aov</code> (analysis of variance), <code>wilcox.test</code> (the two-sample Mann–Whitney–Wilcoxon test), <code>aggregate</code> (computing aggregates within data groups), <code>boxplot</code> (box-and-whisker plots for a variable split by a combination of factors), or <code>plot</code> (scatter plots); see also Chapter 11 in [53].

For instance, they can be used to describe symbolic relationships such as:

- "y as a linear combination of x1, x2, and x3",
- "y grouped/split by a combination of x1 and x2",

where y, x1, etc., are, for example, column names in some data frame.

Formulae are interpreted by the corresponding functions, and not the R language itself. Thus, programmers are free to assign them any meaning. As their syntax is quite esoteric, beginners might find them confusing. Hence, we will discuss them much later: in Section 17.6.

Luckily, the use of formulae can usually quite easily be avoided<sup>27</sup>.

 $<sup>^{27}</sup>$  For example,  $\mathbf{lm.fit}$  can be used instead of  $\mathbf{lm}$ . It is slightly more difficult to learn, but it has the added

## 10.4 Argument checking revisited

Recall that anything can be passed as a function's input. Here are some additions to the topic we touched upon in Section 9.2.1.

Compound objects are internally represented merely through basic types (such as numeric vectors, lists, or combinations thereof) and attributes. However, unless we really know better (which, by the way, this book is all about), we recommend relying on the hopefully well-thought-out methods developed by the designer of the class.

Ideally, when checking arguments passed to a function, determining if an object is of a desired type should be solely done by means of the generics like is.class. If that is not the case, a call to as.class may be used to ensure we will deal with an object of the desired type.

If a conversion is impossible, either because a specific method is unavailable or because its designer decided that this must be the case, whatever the consequences are is not necessarily our problem anymore.

We should explain to the user that the input type assurance is done via this very mechanism. In case they get any surprising results, they are expected to check/redefine the underlying is.class or as.class themselves.

This scheme is not watertight, and there will be users complaining that they get *unexpected* or *confusing* (in their opinion) outputs. With infinitely many potential types, however, we cannot respond to every possible situation.

**Example 10.26** As an illustration, here is a function that counts the number of occurrences of items in a numerised (digitised?) version of a given object:

```
numtable <- function(x)
{
    if (!is.numeric(x)) x <- as.numeric(x) # two generics!

    u <- unique(x)
    structure(
        tabulate(match(x, u)),
        names=as.character(u)
    )
}</pre>
```

Let us assume that the user has been informed (in the corresponding documentation page) that x must be a numeric vector (as in is.numeric) or an object coercible to (by means of as.numeric).

The callers will be stress-testing our function in many different ways:

benefit of ensuring the user knows that the emergence of all model variables is not magical (especially the nonlinear/mixed effect terms).

```
numtable(c(1, 3, 5, 5, 1, 5))
## 1 3 5
## 2 1 3
```

It is an intended behaviour.

```
numtable(c("1", "3", "5", "5", "1", "5"))
## 1 3 5
## 2 1 3
```

It makes sense, too: a character vector consisting of number-strings has been fed on input.

```
numtable(c("a", "e", "z", "a", "z"))
## Warning in numtable(c("a", "e", "z", "z", "a", "z")): NAs introduced by
## coercion
## <NA>
## 6
```

Does the output make no sense? Of course, it does. They have just passed something not easily coercible to a numeric vector. Notice the warning that suggests there is something wrong. The users need to correct their possible mistakes by themselves.

```
numtable(list(1, 2, 3:10, 2))
## Error in numtable(list(1, 2, 3:10, 2)): 'list' object cannot be coerced to
## type 'double'
```

Again, it makes sense. "But I think that this function should apply **unlist** automatically..." Well, if you want such behaviour, why don't you call **numtable(unlist(...))** yourself? It is not so difficult.

```
numtable(factor(c(1, 3, 5, 5, 1, 5)))
## 1 2 3
## 2 1 3
```

Is this confusing? No, this is a well-documented behaviour of **as.numeric** on objects of the type factor (designed by another developer). A user is expected to know that in this case, **as.character** should be called first (but we can remind them about it in the documentation).

Of course, sometimes users might discover bugs or unexpected behaviours, especially related to boundary cases we have not been considerate enough to inspect. We are, of course, the ones to blame for the following:

```
numtable(numeric(0)) # bug: this should be corrected
## <NA>
## 0
```

## 10.5 (Over)using the forward-pipe operator, `|>`(\*)

The object-oriented programming paradigm is utile when we wish to define a new data type, perhaps even a hierarchy of types. Many development teams find it an efficient tool to organise larger pieces of software. Yet, in the broad data science and numerical computing domains, we are often the consumers of object orientation rather than class designers.

Thanks to the discussed method dispatch mechanism, our language is easily extensible. Something that mimics a new data type can easily be introduced. Most importantly, methods can be added or removed during run-time, e.g., when importing external packages.

However, R is still a functional programming language, where functions are not just first-class citizens: they are privileged. Of course, there are some inherent limitations stemming from the ingenious simplicity of S3: method dispatch is usually based only on the type of the first function argument, classes cannot be defined formally (but see Section 11.5), and there is no real encapsulation (we cannot actually hide data from a user<sup>28</sup>). However, overall the whole concept has proven quite versatile.

In functional programming, the emphasis is on operations (verbs), not data (nouns). It leads to a very readable syntax. For example, assuming that **square**, x, and y are sensibly defined, the mean squared error can be written as:

#### mean(square(x-y))

It is very user-centric. However, when implementing more complex data processing pipelines, a programmer thinks: "first, I need to do this, then I need to do that, and afterwards...". When they write it down, there can be some pressing of Home and End keys necessary. It should not be a problem for most programmers.

#### finally(thereafter(then(first(x))))

However, some people are inherently lazy, always complaining, or compulsively trying to "optimise" things.

**Example 10.27** Base R is extremely flexible. We can introduce new vocabulary as we please. In Chapter 12, we will study an example where we define:

<sup>&</sup>lt;sup>28</sup> Which can be good, right?

<sup>&</sup>lt;sup>29</sup> Do not get yours truly wrong, improving things is generally good. Nevertheless, in the long run, as a compulsive habit ("this is what (some) stakeholders want", "we need to be agile and responsive", etc.), it is not really sustainable (also for the environment!). Less is better, even though slightly more challenging. By introducing a new, parallel syntax, we duplicate the existing features. We cause some divide in the community: some users will be introduced to the system through the new interface and not know the old one, and others will have to learn the new syntax to be able to communicate with the former group. We also introduce a whole new set of issues (how to make the new functions interoperable with each other seamlessly, etc.).

- group\_by (a function that splits a data frame with respect to a combination of levels in given named columns and returns a list of data frames with class list\_dfs),
- aggregate.list\_dfs (which applies a given aggregation function on each column of each data frame in a given list), and
- mean.list\_dfs (a specialised version of the former that calls mean).

The specifics do not matter now. Let us just consider the notation we use when the operations are chained:

```
# select a few rows and columns from the `iris` data frame:
iris_subset <- iris[51:150, c("Sepal.Width", "Petal.Length", "Species")]
# compute the averages of all variables grouped by Species:
mean(group_by(iris_subset, "Species"))
## Species x Mean
## 1 versicolor Sepal.Width 2.770
## 2 versicolor Petal.Length 4.260
## 3 virginica Sepal.Width 2.974
## 4 virginica Petal.Length 5.552</pre>
```

It is quite readable. We compute the mean in groups defined by Species in a subset of the iris data frame. All verbs appear on the left-hand side of the expression, with the last (the most important?) operation being listed first.

By the way, self-explanatory variable names and rich comments are priceless.

In more traditional object-oriented programming languages, either the method list is sealed inside<sup>30</sup> the class' definition (like in C++), or some peculiar patches must be applied to inject a method (like in Python)<sup>31</sup>. There, it is *the objects* that are *told* what to do. They are treated as black boxes.

Some popular languages rely on message-passing syntax, where operations are propagated (and written) left-to-right instead of inside-out. For instance, in C++ and Python (amongst many others), "obj.method1().method2()" means "call method1 on obj and then call method2 on the result.

```
x |> f() |> g(y) |> h()
(x-y) |> square() |> mean()
```

is equivalent, respectively, to:

 $<sup>^{30}</sup>$  When methods are parts of particular classes, there can be a lot of duplicated code. Functional OOP can be more developer-friendly as we can implement all methods related to roughly the same functionality in one spot.

<sup>&</sup>lt;sup>31</sup> See also the concept of extension methods in C# or Kotlin or, to some extent, class inheritance.

<sup>32</sup> It was inspired by `|` in Bash and `|>@` in F# and Julia (which are part of the language specification). Also, there is a `%>%` operator (and related ones) in the R package magrittr.

```
h(g(f(x), y))
mean(square(x-y))
```

This syntax is developer-centric. It emphasises the order in which the operations are executed, something that could always be achieved with the function-centric form and perhaps a few auxiliary variables.

The placeholder `\_` can be used on the right-hand side of the pipe operator (only once) to indicate that the left-hand side must be matched to a specific named argument of the function to be called. Otherwise, the left side always gets passed as the first argument.

Therefore, the two following expressions are equivalent:

```
x |> median() |> `-`(e1=x, e2=_) |> abs() |> median()
median(abs(x-median(x)))
```

**Example 10.28** In the above example, a pipe operator version of the iris aggregation exercise would look like:

```
iris_subset |> group_by("Species") |> mean()
```

Expressions on the right-hand side of the pipe operator must always be proper calls. Therefore, the use of round brackets is obligatory. Thus, when passing anonymous functions, we must write:

```
runif(10) |> (function(x) mean((x-mean(x))^2))() # note the "()" at the end
## [1] 0.078184
```

Peculiarly, in R 4.1.0, a "shorthand" notation for creating functions was introduced. We can save seven keystrokes and write "(...) expr" instead of "function(...) expr".

```
runif(10) |> ((x) mean((x-mean(x))^2))() # again: "()" at the end
## [1] 0.078184
```

There is nothing that cannot be achieved without the pipe operator. As this book is minimalist by design, we will be refraining<sup>33</sup> ourselves from using it.

**Note** When writing code interactively, we may sometimes benefit from using the rightward `->` operator. Suffice it to say that "name <- value" and "value -> name" are synonymous.

This way, we can write some lengthy code, store the result in an intermediate variable, and then continue to the next line (possibly referring to that auxiliary value more than once). In the long run, multiplying entities without necessity is unsustainable.

<sup>&</sup>lt;sup>33</sup> Which some readers would name an *uncool* (old-school) approach, but we do not care. Remember that the functional syntax is the native one. We have to be able to understand it anyway.

For instance:

```
runif(10) -> .; mean((.-mean(.))^2)
## [1] 0.078184
```

or:

`.` is as valid a variable name as any other one.

#### 10.6 Exercises

**Exercise 10.29** *Answer the following questions:* 

- How to display the source code of the default methods for **head** and **tail**?
- Can there be, at the same time, one object of the class c("A", "B") and another one of the class c("B", "A")?
- If f is a factor, what are the relationships between as.character(f), as.numeric(f), as.character(as.numeric(f)), and as.numeric(as.character(f))?
- If x is a named vector and f is a factor, is x[f] equivalent to x[as.character(f)] or rather x[as.numeric(f)]?

Exercise 10.30 A user calls:

```
plot(x, y, col="red", ylim=c(1, max(x)), log="y")
```

where x and y are numeric vectors. Consult **help**("plot") for the meaning of the ylim and log arguments. Was that straightforward?

**Exercise 10.31** Explain why the two following calls yield significantly different results and present a workaround:

```
c(Sys.Date(), "1970-01-01")
## [1] "2023-05-03" "1970-01-01"

(continues on next page)
```

```
c("1970-01-01", Sys.Date())
## [1] "1970-01-01" "19480"
```

**Exercise 10.32** Write methods **head** and **tail** for our example categorical class.

**Exercise 10.33** (\*) Write an R package that defines S3 class categorical. Add a few methods for this class. Note the need to use the S3method directive in the NAMESPACE file; see [59].

Exercise 10.34 Inspect the result of a call to binom. test (79, 100). Find the method responsible for such objects' pretty printing.

**Exercise 10.35** Inspect the result of a call to rle(c(1, 1, 1, 4, 3, 3, 3, 3, 3, 2, 2)). Find the method responsible for such objects' pretty printing.

**Exercise 10.36** Read more about the connection class. In particular, see the Value section in help("connections").

**Exercise 10.37** Read about the subsetting operators overloaded for the package\_version class; see help("numeric version").

**Exercise 10.38** There are **xtfrm** methods overloaded for classes such as numeric\_version, difftime, Date, and factor. Find out how they work and where they might be of service (especially in relation to **order** and **sort**; see also Section 12.3.1).

**Exercise 10.39** Give an example where split(x, list(y1, y2)) (with default arguments) will fail to generate the correct result.

**Exercise 10.40** Write a function that determines the mode, i.e., the most frequently occurring value in a given object of the class factor. If the mode is not unique, return a randomly chosen one (each with the same probability).

**Exercise 10.41** *Implement your version of the gl function.* 

**Exercise 10.42** Check out which built-in date-time functions the **stringx** package replaces with more portable ones.

# Matrices and other arrays

When we equip an atomic or generic vector with the dimattribute, it automatically becomes an object of the S3 class array. In particular, two-dimensional arrays (primary S3 class matrix) allow us to represent tabular data where items are aligned into rows and columns:

```
structure(1:6, dim=c(2, 3)) # a matrix with 2 rows and 3 columns
     [,1] [,2] [,3]
## [1,]
        1 3 5
## [2,]
        2
              4
```

Combined with the fact that there are many built-in functions overloaded for the matrix class, we have just opened up a whole world of new possibilities. We explore them in this chapter.

In particular, we discuss how to perform basic algebraic operations such as matrix multiplication, transpose, finding eigenvalues, and performing various decompositions. We also cover data wrangling operations such as array subsetting and columnand rowwise aggregation.

**Important** Oftentimes, a numeric matrix with *n* rows and *m* columns is used to represent *n* points (samples) in an *m*-dimensional space (with *m* numeric features or variables),  $\mathbb{R}^m$ .

Furthermore, in the next chapter, we will introduce data frames: matrix-like objects whose columns can be of any (not necessarily the same) type.

## 11.1 Creating arrays

### 11.1.1 matrix and array

A matrix can be conveniently created using the matrix function.

```
(A <- matrix(1:6, byrow=TRUE, nrow=2))
       [,1] [,2] [,3]
```

```
## [1,]
## [2,1
                5
```

The above converted an atomic vector of length six into a matrix with two rows. The number of columns was determined automatically (ncol=3 could have been passed to get the same result).

**Important** By default, the elements of the input vector are read columnwisely:

```
matrix(1:6, ncol=3) # byrow=FALSE
     [,1] [,2] [,3]
## [1,]
      1 3 5
## [2,]
       2
           4
```

A matrix can be equipped with dimension names, being a list of two character vectors of appropriate sizes, labelling each row and column in this order:

```
matrix(1:6, byrow=TRUE, nrow=2, dimnames=list(c("x", "y"), c("a", "b", "c")))
## abc
## x 1 2 3
## v 4 5 6
```

Alternatively, to create a matrix, we can use the array function, which requires the number of rows and columns to be specified explicitly.

```
array(1:6, dim=c(2, 3))
## [,1] [,2] [,3]
## [1,] 1 3 5
## [2,1
       2
            4
```

The elements are consumed in a column-major manner.

Arrays of dimensionality other than 2 are also possible. Here is a one-dimensional array. When printed, it is indistinguishable from an atomic vector (but the class attribute is still set to array):

```
array(1:6, dim=6)
## [1] 1 2 3 4 5 6
```

And now for something completely different: a three-dimensional array of size  $3\times4\times2$ :

```
array(1:24, dim=c(3, 4, 2))
## , , 1
##
       [,1] [,2] [,3] [,4]
##
```

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```
## [1,] 1 4 7 10

## [2,] 2 5 8 11

## [3,] 3 6 9 12

##

## , , 2

##

## [,1] [,2] [,3] [,4]

## [1,] 13 16 19 22

## [2,] 14 17 20 23

## [3,] 15 18 21 24
```

which can be thought of as two matrices of size  $3 \times 4$  (because how else can we print out a 3D object on a 2D console?).

The array function can be fed with the dimnames argument too. For instance, the above three-dimensional hypertable would require a list of three character vectors of sizes 3, 4, and 2, respectively.

**Exercise 11.1** The readers are encouraged to try out themselves that 10-dimensional arrays are also possible.

### 11.1.2 Promoting and stacking vectors

We can promote an ordinary vector to a column vector, i.e., a matrix with one column, by calling:

```
as.matrix(1:2)
## [,1]
## [1,] 1
## [2,] 2
cbind(1:2)
## [,1]
## [1,] 1
## [2,] 2
```

and to a row vector:

```
t(1:3) # transpose

## [,1] [,2] [,3]

## [1,] 1 2 3

rbind(1:3)

## [,1] [,2] [,3]

## [1,] 1 2 3
```

Actually, **cbind** and **rbind** stand for column- and row-bind; they allow multiple vectors and matrices to be stacked one after/below another:

and so forth.

Unfortunately, the *generalised* recycling rule is not implemented in full:

```
cbind(1:4, 5:8, cbind(9:10, 11)) # different from cbind(1:4, 5:8, 9:10, 11)
## Warning in cbind(1:4, 5:8, cbind(9:10, 11)): number of rows of result is
## not a multiple of vector length (arg 1)
## [,1] [,2] [,3] [,4]
## [1,] 1 5 9 11
## [2,] 2 6 10 11
```

The first two arguments are of length four.

## 11.1.3 Simplifying lists

**simplify2array** is an extension of the **unlist** function. Given a list of atomic vectors, each of length one, it will return a flat atomic vector. However, if a list of equisized vectors of greater lengths is given, these will be converted to a matrix.

```
simplify2array(list(1, 11, 21)) # each of length 1
## [1] 1 11 21
simplify2array(list(1:3, 11:13, 21:23, 31:33)) # each of length 3
## [,1] [,2] [,3] [,4]
## [1,] 1 11 21 31
## [2,] 2 12 22 32
## [3,] 3 13 23 33
simplify2array(list(1, 11:12, 21:23)) # no can do
## [[1]]
## [1] 1
```

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```
## [[2]]
## [1] 11 12
##
## [[3]]
## [1] 21 22 23
```

In the second example, each vector becomes a separate column of the resulting matrix<sup>1</sup>.

See Section 12.3.7 for a few more examples.

**Example 11.2** Quite a few functions call the above automatically (compare the simplify or SIMPLIFY (sic!) argument in **sapply**, **tapply**, **mapply**, **replicate**, etc.).

For instance:

Take note of what constitutes the columns of the return matrix.

**Exercise 11.3** Inspect the behaviour of **as.matrix** on list arguments. Write your version of **simplify2array** named **as.matrix.list** that always returns a matrix. If a list of non-equisized vectors is given, fill the missing cells with NAs.

**Important** Sometimes a call to **do.call(cbind,** x)) might be a better idea than a referral to **simplify2array**. Provided that x is a list of atomic vectors, it *always* returns a matrix: shorter vectors are recycled (which might be welcome, but not necessarily).

```
do.call(cbind, list(a=c(u=1), b=c(v=2, w=3), c=c(i=4, j=5, k=6)))
## Warning in (function (..., deparse.level = 1) : number of rows of result
## is not a multiple of vector length (arg 2)
## a b c
## i 1 2 4
## j 1 3 5
## k 1 2 6
```

### **Example 11.4** Consider a named toy list of numeric vectors:

<sup>&</sup>lt;sup>1</sup> Which can easily be explained by the fact that matrix elements are stored in a columnwise order.

```
x <- list(a=runif(10), b=rnorm(15))</pre>
```

Compare the results generated by **sapply** (which calls **simplify2array**):

```
sapply(x, function(e) c(Mean=mean(e)))
## a.Mean b.Mean
## 0.57825 0.12431
sapply(x, function(e) c(Min=min(e), Max=max(e)))
## a b
## Min 0.045556 -1.9666
## Max 0.940467 1.7869
```

with its version based on do.call and cbind:

Notice that **sapply** may return an atomic vector with somewhat surprising names.

### 11.1.4 Beyond numeric arrays

Arrays built upon atomic vectors other than numeric ones are possible too. For instance, we will later stress that comparisons featuring matrices are performed elementwisely, which results in logical matrices:

```
A >= 3
## [,1] [,2] [,3]
## [1,] FALSE FALSE TRUE
## [2,] TRUE TRUE TRUE
```

Furthermore, matrices of character strings can be useful too:

```
matrix(strrep(LETTERS[1:6], 1:6), ncol=3)
## [,1] [,2] [,3]
## [1,] "A" "CCC" "EEEEE"
## [2,] "BB" "DDDD" "FFFFFF"
```

And, of course, complex matrices:

```
A + 1i

## [,1] [,2] [,3]

## [1,] 1+1i 2+1i 3+1i

## [2,] 4+1i 5+1i 6+1i
```

We are not limited to *atomic* vectors: lists can be a basis for arrays as well:

```
matrix(list(1, 11:21, "A", list(1, 2, 3)), nrow=2)
## [,1] [,2]
## [1,] 1 "A"
## [2,] integer,11 list,3
```

Some elements are not displayed correctly, but they are still there.

### 11.1.5 Internal representation

An object of the S3 class array is an atomic vector or a list equipped with the dims attribute being a vector of nonnegative integers. Interestingly, we do not have to set the class attribute explicitly: the accessor function **class** will return an implicit<sup>2</sup> class anyway (compare Section 4.4.3).

```
class(1) # atomic vector
## [1] "numeric"
class(structure(1, dim=rep(1, 1))) # 1D array (vector)
## [1] "array"
class(structure(1, dim=rep(1, 2))) # 2D array (matrix)
## [1] "matrix" "array"
class(structure(1, dim=rep(1, 3))) # 3D array
## [1] "array"
```

Note that a two-dimensional array is additionally of the matrix class.

Optional dimension names are represented by means of the dimnames attribute, which is a list of d character vectors, where d is the array's dimensionality.

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<sup>&</sup>lt;sup>2</sup> Calling unclass on a matrix has no effect.

```
## [[2]]
## [1] "A" "B" "C"
```

**Important** Internally, elements in an array are always stored in the columnwise (column-major, Fortran) order:

```
as.numeric(A) # drop all attributes to reveal the underlying numeric vector
## [1] 1 2 3 4 5 6
```

Setting byrow=TRUE in a call to the matrix only affects the order in which this function reads a given source vector, not the column/row-majorness.

```
(B <- matrix(1:6, ncol=3, byrow=TRUE))
## [,1] [,2] [,3]
## [1,] 1 2 3
## [2,] 4 5 6
as.numeric(B)
## [1] 1 4 2 5 3 6
```

The two said special attributes can be modified through the replacement functions `dim<-` and `dimnames<-` (and, of course, `attr<-` as well). In particular, changing dim does not alter the underlying atomic vector; it only affects how other functions, including the corresponding **print** method, interpret their placement on a virtual grid:

```
`dim<-`(A, c(3, 2)) # not the same as transpose of A
## [,1] [,2]
## [1,] 1 4
       2
## [2,]
## [3,] 3 6
```

We obtained a different view of the same flat data vector. Also, the dimnames attribute was dropped because its size became incompatible with the newly requested dimensionality.

Exercise 11.5 Study the source code of the nrow, NROW, ncol, NCOL, rownames, row.names, and colnames functions.

Interestingly, for one-dimensional arrays, the names function returns a reasonable value (based on the dimnames attribute, which is a list featuring one character vector), despite the names attribute's not being set.

What is more, dimnames itself can be named:

```
names(dimnames(A)) <- c("ROWS", "COLUMNS")</pre>
print(A)
```

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```
## COLUMNS
## ROWS A B C
## a 1 3 5
## b 2 4 6
```

It is still a numeric matrix, but the presentation thereof is slightly prettified.

**Exercise 11.6 outer** applies an elementwisely vectorised function on each pair of elements from two vectors, forming a two-dimensional result grid. Based on two calls to **rep**, implement it yourself.

Some examples:

```
outer(c(x=1, y=10, z=100), c(a=1, b=2, c=3, d=4), "*") # multiplication
## a b c d
## x 1 2 3 4
## y 10 20 30 40
## z 100 200 300 400
outer(c("A", "B"), 1:8, paste, sep="-") # concatenate strings
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## [1,] "A-1" "A-2" "A-3" "A-4" "A-5" "A-6" "A-7" "A-8"
## [2,] "B-1" "B-2" "B-3" "B-4" "B-5" "B-6" "B-7" "B-8"
```

**Exercise 11.7** Show how match(y, z) can be implemented with outer. Is its time and memory complexity optimal, though?

**Exercise 11.8 table** creates a contingency matrix/array that counts the number of unique pairs of corresponding elements from one or more vectors of equal lengths. Implement its one- and two-argument version based on **tabulate**.

For example:

```
tips <- read.csv(paste0("https://github.com/gagolews/teaching-data/raw/",
    "master/other/tips.csv"), comment.char="#") # a data.frame (list)
table(tips[["day"]])
##
   Fri Sat Sun Thur
            76 62
         87
table(tips[["smoker"]], tips[["day"]])
##
##
        Fri Sat Sun Thur
##
   No 4 45 57
                      45
   Yes 15 42 19
##
                      17
```

#### Array indexing 11.2

Array subsetting can be performed by means of an overloaded<sup>3</sup> [` method, which we will usually provide with many indexers: two in the matrix case; see help("[").

Throughout this section, we refer to the two following example matrices:

```
(A <- matrix(1:12, byrow=TRUE, nrow=3))
## [,1] [,2] [,3] [,4]
## [1,] 1 2 3 4
## [2,] 5
            6 7 8
## [3,] 9 10 11 12
B <- A
dimnames(B) <- list(</pre>
   c("a", "b", "c"), # row labels
   c("x", "y", "z", "w") # column labels
)
В
## x y z w
## a 1 2 3 4
## b 5 6 7 8
## c 9 10 11 12
```

Subsetting higher-dimensional arrays will be covered at the end.

## Arrays are built upon basic vectors

Subsetting based on one indexer (as in Chapter 5) will refer to the underlying flat vector.

For instance:

```
A[6]
## [1] 10
```

It is the element in the third row, second column. Recall that values are stored in the column-major order.

## Selecting individual elements

Mathematically, we say that our example  $3 \times 4$  real matrix  $\mathbf{A} \in \mathbb{R}^{3 \times 4}$  is like:

$$\mathbf{A} = \left[ \begin{array}{cccc} a_{1,1} & a_{1,2} & a_{1,3} & a_{1,4} \\ a_{2,1} & a_{2,2} & a_{2,3} & a_{2,4} \\ a_{3,1} & a_{3,2} & a_{3,3} & a_{3,4} \end{array} \right] = \left[ \begin{array}{cccc} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{array} \right].$$

<sup>&</sup>lt;sup>3</sup> Hidden deeply at the C language level.

Matrix elements are aligned in a two-dimensional grid. They are organised into rows and columns. Hence, we can pinpoint a cell using two indexes:  $a_{i,j}$  refers to the i-th row and the j-th column.

Similarly in R:

```
A[3, 2] # 3rd row, 2nd column
## [1] 10
B["c", "y"] # using dimnames == B[3, 2]
## [1] 10
```

#### 11.2.3 Selecting rows and columns

Some textbooks, and we are fond of this notation here as well, mark with  $\mathbf{a}_{i,\cdot}$  a vector that consists of all the elements in the *i*-th row and with  $\mathbf{a}_{\cdot,i}$  all items in the *j*-th column.

In R, these will correspond to one of the indexers being left out.

```
A[3,] # 3rd row

## [1] 9 10 11 12

A[, 2] # 2nd column

## [1] 2 6 10

B["c",] # or B[3,]

## x y z w

## 9 10 11 12

B[, "y"] # or B[, 2]

## a b c

## 2 6 10
```

Let us stress that A[1], A[1, ], and A[, 1] have all different meanings. Also, we see that the results' dimnames are adjusted accordingly; see also unname, which can take care of them once and for all.

**Exercise 11.9** Use **duplicated** to remove repeating rows in a given numeric matrix (see also **unique**).

## 11.2.4 Dropping dimensions

Extracting an individual element or a single row/column from a matrix yields an atomic vector. If the dim attribute consists of 1s only, it will be removed whatsoever.

In order to obtain proper row and column vectors, we can request the preservation of the dimensionality of the output object (and, more precisely, the length of dim) by passing drop=FALSE to `[`.

```
A[1, 2, drop=FALSE] # 1st row, 2nd columns
## [,1]
## [1,] 2
```

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```
A[1, , drop=FALSE] # 1st row
## [,1] [,2] [,3] [,4]
## [1,] 1 2 3 4
A[ , 2, drop=FALSE] # 2nd column
## [,1]
## [1,] 2
## [2,] 6
## [3,] 10
```

Important Unfortunately, the drop argument defaults to TRUE. Many bugs could be avoided otherwise, primarily when the indexers are generated programmatically.

See also the **drop** function, which removes the dimensions with only one level.

Note For list-based matrices, we can also use a multi-argument version of `[[` to extract the individual elements.

```
C <- matrix(list(1, 11:12, 21:23, 31:34), nrow=2)</pre>
C[1, 2] # for `[`, input type is the same as the output type, hence a list
## [[1]]
## [1] 21 22 23
C[1, 2, drop=FALSE]
      [,1]
## [1,] integer,3
C[[1, 2]] # extract
## [1] 21 22 23
```

## 11.2.5 Selecting submatrices

Indexing based on two vectors, both of length two or more, extracts a sub-block of a given matrix:

```
A[1:2, c(1, 2, 4)] # rows 1 and 2, columns 1, 2, and 4
## [,1] [,2] [,3]
## [1,] 1 2 4
## [2,] 5
            6
B[c("a", "b"), -3]
## x y w
## a 1 2 4
## b 5 6 8
```

Note again that drop=TRUE is the default, which affects the behaviour if one of the indexers is a scalar.

```
A[c(1, 3), 3]

## [1] 3 11

A[c(1, 3), 3, drop=FALSE]

## [,1]

## [1,] 3

## [2,] 11
```

**Exercise 11.10** Overload the **split** function for the matrix class so that, given a matrix with n rows and an object of the class factor of length n (or a list of such objects), a list of n matrices is returned. For example:

## 11.2.6 Selecting elements based on logical vectors

Logical vectors can also be used as indexers, with consequences that are not hard to guess:

```
A[c(TRUE, FALSE, TRUE), -1] # select 1st and 3rd row, all but 1st column

## [,1] [,2] [,3]

## [1,] 4 7 10

## [2,] 6 9 12

B[B[, "x"]>1 & B[, "x"]<=9, ] # all rows where x is in (1, 9]

## x y z w

## b 5 6 7 8

## c 9 10 11 12

A[2, colMeans(A)>6, drop=FALSE] # 2nd row of the columns with means > 6

## [,1] [,2]

## [1,] 8 11
```

**Note** Section 11.3 notes that comparisons involving matrices are performed in an elementwise manner, for example:

Such logical matrices can be used to index other matrices of the same size. Such indexing always yields a (flat) vector:

```
A[A>7]
## [1] 8 9 10 11 12
```

It is nothing else than the single-indexer subsetting involving two flat vectors (a numeric and a logical one); the dim attributes are not considered here.

Exercise 11.11 Implement your versions of max.col, lower.tri, and upper.tri.

#### 11.2.7 Selecting based on two-column numeric matrices

We can also index a matrix A with a two-column matrix of positive integers I, for instance:

```
(I <- cbind(
   c(1, 3, 2, 1, 2),
   c(2, 3, 2, 1, 4)
))
     [,1] [,2]
##
## [1,]
         1
## [2,]
         3
## [3,]
        2
             2
       1
## [4,]
             1
## [5,]
         2
              4
```

Now A[I] gives easy access to:

```
A[I[1, 1], I[1, 2]],A[I[2, 1], I[2, 2]],A[I[3, 1], I[3, 2]],
```

and so forth. In other words, each row of I gives the coordinates of the elements to extract.

```
A[I]
## [1] 4 9 5 1 11
```

This is exactly A[1, 2], A[3, 3], A[2, 2], A[1, 1], A[2, 4]. The result is always a flat vector.

**Note** which can also return a list of index matrices:

Moreover, arrayInd can be used to convert flat indexes to multidimensional ones.

**Exercise 11.12** Implement your version of **arrayInd** and a function performing the inverse operation.

**Exercise 11.13** Write your version of diag.

#### 11.2.8 Higher-dimensional arrays

For *d*-dimensional arrays, indexing can involve up to *d* indexes. It is particularly valuable for arrays with the dimnames attribute set representing contingency tables over a Cartesian product of multiple factors. The built-in **datasets**::Titanic object is an example of this:

```
str(dimnames(Titanic)) # for reference (note that dimnames are named)
## List of 4
## $ Class : chr [1:4] "1st" "2nd" "3rd" "Crew"
## $ Sex : chr [1:2] "Male" "Female"
## $ Age : chr [1:2] "Child" "Adult"
## $ Survived: chr [1:2] "No" "Yes"
Titanic["Crew", "Male", "Adult", "Yes"]
## [1] 192
```

gives the number of adult male crew members who survived the accident. Also:

```
Titanic["Crew", , "Adult", ]

## Survived

## Sex No Yes

## Male 670 192

## Female 3 20
```

and so on.

**Exercise 11.14** Check if the above four-dimensional array can be indexed using matrices with four columns.

### 11.2.9 Replacing elements

There is also a multidimensional version of the replacement subsetting function, `[<-`.

Generally, subsetting drops all attributes except names, dim, and dimnames (unless it does not make sense otherwise). The replacement variant of the index operator modifies vector values but generally preserves all the attributes.

This enables transforming matrix elements like:

Take note of the preservation of dim and dimnames.

**Exercise 11.15** Given a character matrix with entities that can be interpreted as numbers like:

```
(X <- rbind(x=c(a="1", b="2"), y=c("3", "4")))
## a b
## x "1" "2"
## y "3" "4"
```

convert it to a numeric matrix with a single line of code. Preserve all attributes.

## 11.3 Common operations

#### 11.3.1 Matrix transpose

The matrix transpose, mathematically denoted with  $\mathbf{A}^T$ , is available via a call to  $\mathbf{t}$ :

```
(A <- matrix(1:6, byrow=TRUE, nrow=2))

## [,1] [,2] [,3]

## [1,] 1 2 3

## [2,] 4 5 6

t(A)

## [,1] [,2]

## [1,] 1 4

## [2,] 2 5

## [3,] 3 6
```

Hence, if  $\mathbf{B} = \mathbf{A}^T$ , then it is a matrix such that  $b_{i,j} = a_{j,i}$ . In other words, in the transposed matrix, rows become columns, and columns become rows.

For higher-dimensional arrays, a generalised transpose can be achieved with **aperm** (try permuting the dimensions of Titanic). Also, the conjugate transpose of a complex matrix  $\mathbf{A}$  is done via  $\mathbf{Conj}(\mathbf{t}(A))$ .

#### 11.3.2 Vectorised mathematical functions

Vectorised functions such as **sqrt**, **abs**, **round**, **log**, **exp**, **cos**, **sin**, etc., operate on each array element<sup>4</sup>.

```
A <- matrix(1/(1:6), nrow=2)
round(A, 2)  # rounds every element in A

## [,1] [,2] [,3]

## [1,]  1.0  0.33  0.20

## [2,]  0.5  0.25  0.17
```

**Exercise 11.16** Using a single call to **matplot**, which accepts the y argument to be a matrix, draw a plot of  $\sin(x)$ ,  $\cos(x)$ ,  $|\sin(x)|$ , and  $|\cos(x)|$  for  $x \in [-2\pi, 6\pi]$ .

## 11.3.3 Aggregating rows and columns

When we call an aggregation function on an array, it will reduce all elements to a single number:

```
(A <- matrix(1:12, byrow=TRUE, nrow=3))

## [,1] [,2] [,3] [,4]

## [1,] 1 2 3 4

## [2,] 5 6 7 8

## [3,] 9 10 11 12

mean(A)

## [1] 6.5
```

 $<sup>^4</sup>$  They are simply applied on each element of the underlying flat vector. Section 5.5 mentioned that unary functions preserve all attributes of their inputs, hence also dim and dimnames.

The apply function may be used to summarise individual rows or columns in a matrix:

- apply(A, 1, f) applies a given function f on each row of a matrix A;
- apply(A, 2, f) applies f on each column of A.

For instance:

```
apply(A, 1, mean) # synonym: rowMeans(A)
## [1] 2.5 6.5 10.5
apply(A, 2, mean) # synonym: colMeans(A)
## [1] 5 6 7 8
```

The function being applied does not have to return a single number:

Take note of the columnwise order of the output values.

apply works on higher-dimensional arrays:

```
apply(Titanic, 1, mean) # 1st dimension - Class
## 1st 2nd 3rd Crew
## 40.625 35.625 88.250 110.625
apply(Titanic, c(1, 3), mean) # w.r.t. Class (1st) and Age (3rd)
## Age
## Class Child Adult
## 1st 1.50 79.75
## 2nd 6.00 65.25
## 3rd 19.75 156.75
## Crew 0.00 221.25
```

## 11.3.4 Binary operators

In Section 5.5, we stated that binary elementwise operations, such as addition or multiplication, preserve the attributes of the longer input or both (with the first argument preferred to the second) if they are of equal sizes.

Taking into account that:

an array is simply a flat vector equipped with the dim attribute, and

• we refer to the respective *default* methods when applying binary operators allows us to deduce how `+`, `<=`, `&`, etc. behave in several different contexts.

**Array-Array.** First, let us note what happens when we operate on two arrays of identical dimensionalities.

```
(A <- rbind(c(1, 10, 100), c(-1, -10, -100)))
## [,1] [,2] [,3]
## [1,] 1 10 100
## [2,] -1 -10 -100
(B <- matrix(1:6, byrow=TRUE, nrow=2))
## [,1] [,2] [,3]
## [1,] 1 2 3
## [2,] 4 5 6
A + B # elementwise addition
## [,1] [,2] [,3]
## [1,] 2 12 103
## [2,]
        3 -5 -94
A * B # elementwise multiplication (not: algebraic matrix multiply)
## [,1] [,2] [,3]
## [1,] 1 20 300
## [2,] -4 -50 -600
```

They are simply the addition and multiplication of the corresponding elements of two given matrices.

**Array-Scalar**. Second, we can apply scalar-matrix operations:

```
(-1)*B

## [,1] [,2] [,3]

## [1,] -1 -2 -3

## [2,] -4 -5 -6

A^2

## [,1] [,2] [,3]

## [1,] 1 100 10000

## [2,] 1 100 10000
```

They multiplied each element in B by -1 and squared every element in A, respectively. The behaviour of relational operators is similar:

```
A >= 1 & A <= 100

## [,1] [,2] [,3]

## [1,] TRUE TRUE TRUE

## [2,] FALSE FALSE FALSE
```

**Array-Vector**. Next, based on the recycling rule and the fact that elements are ordered columnwisely, we get that:

```
B * c(10, 100)

## [,1] [,2] [,3]

## [1,] 10 20 30

## [2,] 400 500 600
```

It multiplied every element in the first *row* by 10 and each element in the second row by 100.

If we wish to multiply each element in the first, second, ..., etc. *column* by the first, second, ..., etc. value in a vector, we should *not* call:

```
B * c(1, 100, 1000)

## [,1] [,2] [,3]

## [1,] 1 2000 300

## [2,] 400 5 6000
```

but rather:

```
t(t(B) * c(1, 100, 1000))

## [,1] [,2] [,3]

## [1,] 1 200 3000

## [2,] 4 500 6000
```

or:

```
t(apply(B, 1, `*`, c(1, 100, 1000)))

## [,1] [,2] [,3]

## [1,] 1 200 3000

## [2,] 4 500 6000
```

**Exercise 11.17** Write a function that standardises the values in each column of a given matrix: for each column, from every element, subtract the mean and then divide it by the standard deviation. Try to do it in a few different ways, including via a call to **apply**, **sweep**, **scale**, or based solely on arithmetic operators.

**Note** Some sanity checks are done on the dimattributes, so not every configuration is possible. Notice the following peculiarities:

```
getOption("error")
## NULL
A + t(B) # dim==c(2, 3) vs dim==c(3, 2)
## Error in A + t(B): non-conformable arrays
A * cbind(1, 10, 100) # this is too good to be true
## Error in A * cbind(1, 10, 100): non-conformable arrays

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```

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```
A * rbind(1, 10) # but A * c(1, 10) works...

## Error in A * rbind(1, 10): non-conformable arrays

A + 1:12

## Error in eval(expr, envir, enclos): dims [product 6] do not match the

## length of object [12]

A + 1:5 # partial recycling is okay

## Warning in A + 1:5: longer object length is not a multiple of shorter

## object length

## [1,1] [2,2] [3]

## [1,1] 2 13 105

## [2,1] 1 -6 -99
```

## 11.4 Numerical matrix algebra (\*)

Many data analysis and machine learning algorithms, in their essence, involve quite simple matrix algebra and numerical mathematics. Suffice it to say that anyone serious about data science and scientific computing should learn the necessary theory; see, for example, [29] and [30].

R is a convenient interface to the well-tested and stable algorithms from, amongst others, LAPACK and BLAS<sup>5</sup>. Below we mention only a few of them. Many third-party packages feature hundreds of algorithms tackling differential equations, constrained and unconstrained optimisation, etc. Exploring the relevant CRAN Task Views<sup>6</sup> can give a comprehensive overview.

## 11.4.1 Matrix multiplication

`\*` performs elementwise multiplication. For what we call (algebraic) matrix multiplication, we use the `%\*%` operator.

Here is a quick refresher from a basic linear algebra course. The matrix multiplication can only be performed on two matrices of *compatible sizes*: the number of columns in the left matrix must match the number of rows in the right operand.

Given  $\mathbf{A} \in \mathbb{R}^{n \times p}$  and  $\mathbf{B} \in \mathbb{R}^{p \times m}$ , their multiply is a matrix  $\mathbf{C} = \mathbf{A}\mathbf{B} \in \mathbb{R}^{n \times m}$  such that  $c_{i,j}$  is the dot product of the *i*-th row in  $\mathbf{A}$  and the *j*-th column in  $\mathbf{B}$ :

$$c_{i,j} = \mathbf{a}_{i,\cdot} \cdot \mathbf{b}_{\cdot,j} = \sum_{k=1}^{p} a_{i,k} b_{k,j},$$

<sup>&</sup>lt;sup>5</sup> (\*) We can select the underlying implementation of **BLAS** at R's compile time; see Section A.3 in [61]. Some of them are faster than others.

<sup>6</sup> https://cran.r-project.org/web/views/

for i = 1, ..., n and j = 1, ..., m.

For instance:

```
(A <- rbind(c(1, 1, 1), c(-1, 1, 0)))

## [,1] [,2] [,3]

## [1,] 1 1 1

## [2,] -1 1 0

(B <- rbind(c(3, -1), c(1, 2), c(6, 1))))

## [1,] 3 -1

## [2,] 1 2

## [3,] 6 1

A %*% B

## [,1] [,2]

## [1,] 10 2

## [2,] -2 3
```

**Note** When applying `%\*%` on one or more flat vectors, their dimensionality will be promoted automatically to make the operation possible. However,  $\mathbf{c}(a, b)$  %\*%  $\mathbf{c}(c, d)$  gives a scalar ac + bd, and not a  $2 \times 2$  matrix.

Further, crossprod(A, B) yields  $A^TB$  and tcrossprod(A, B) determines  $AB^T$  more efficiently than relying on `%\*%`. We can omit the second argument and get  $A^TA$  and AA, respectively.

```
crossprod(c(1, 1)) # Euclidean norm squared
       \lceil, 1\rceil
## [1,]
          2
crossprod(c(1, 1), c(-1, 1)) # dot product of two vectors
       [,17
##
## [1,]
crossprod(A) # same as t(A) %*% A, i.e., dot products of all column pairs
## [,1] [,2] [,3]
## \[ 1. \] 2 0 1
## [2,] 0
             2
                  1
## [3,]
         1
             1
```

Recall that if the dot product of two vectors equals 0, we say that they are orthogonal (perpendicular).

**Exercise 11.18** (\*) Write your versions of **cov** and **cor**: functions to compute the covariance and correlation matrices. Make use of the fact that the former can be determined with **crossprod** based on a centred version of an input matrix.

## 11.4.2 Solving systems of linear equations

The **solve** function can be used to solve m systems of n linear equations of the form  $\mathbf{A}\mathbf{X} = \mathbf{B}$ , where  $\mathbf{A} \in \mathbb{R}^{n \times n}$  and  $\mathbf{X}, \mathbf{B} \in \mathbb{R}^{n \times m}$  (via the LU decomposition with partial pivoting and row interchanges).

#### 11.4.3 Norms and metrics

Given an  $n \times m$  matrix **A**, calling **norm**(A, "1"), **norm**(A, "2"), and **norm**(A, "I"), we can compute the operator norms:

$$\begin{array}{lcl} \|\mathbf{A}\|_1 & = & \max_{j=1,\dots,m} \sum_{i=1}^n |a_{i,j}|, \\ \|\mathbf{A}\|_2 & = & \sigma_1(\mathbf{A}) = \sup_{\mathbf{0} \neq \mathbf{x} \in \mathbb{R}^m} \frac{\|\mathbf{A}\mathbf{x}\|_2}{\|\mathbf{x}\|_2} \\ \|\mathbf{A}\|_I & = & \max_{i=1,\dots,n} \sum_{j=1}^m |a_{i,j}|, \end{array}$$

where  $\sigma_1$  gives the largest singular value (see below).

Also, passing "F" as the second argument yields the Frobenius norm,  $\|\mathbf{A}\|_F = \sqrt{\sum_{i=1}^n \sum_{j=1}^m a_{i,j}^2}$ , and "M" computes the max norm,  $\|\mathbf{A}\|_M = \max_{i=1,\dots,m\atop j=1,\dots,m} |a_{i,j}|$ .

If **A** is a column vector, then  $\|\mathbf{A}\|_F$  and  $\|\mathbf{A}\|_2$  are equivalent. They are referred to as the Euclidean norm. Moreover,  $\|\mathbf{A}\|_M = \|\mathbf{A}\|_I$  give the supremum norm and outputs  $\|\mathbf{A}\|_1$  the Manhattan (taxicab) one.

**Exercise 11.19** Given an  $n \times m$  matrix **A** representing m vectors in  $\mathbb{R}^n$ , normalise each column so that you obtain m unit vectors, i.e., whose Euclidean norm equals 1.

Further, **dist** determines all pairwise distances between a set of n vectors in  $\mathbb{R}^m$ , written as an  $n \times m$  matrix.

For example, let us consider three vectors in  $\mathbb{R}^2$ :

From that, we see that the distance between the first and the third vector is ca. 1.41421. Euclidean, maximum, Manhattan, and Canberra distances/metrics are available, amongst others.

**Exercise 11.20** dist returns an object of S3 class dist. Inspect how it is represented.

**Example 11.21** adist implements a couple of string metrics. For example:

```
x <- c("spam", "bacon", "eggs", "spa", "spams", "legs")
names(x) < -x
(d \leftarrow adist(x))
##
        spam bacon eggs spa spams legs
                 5
                     4
## spam
                        1
## bacon
           5
                0
                        5
                               5
                                    5
## eggs
                5
                               4
## spa
          1
                 5
                     4
                          0
                               2
                                    4
## spams
                 5
                                    4
## legs
```

gives the Levenshtein distances between each pair of strings. In particular, we need two edit operations (character insertions, deletions, or replacements) to turn "eggs" into "legs" (add l and remove g).

**Example 11.22** Objects of the class dist can be used to perform hierarchical clusterings of datasets. For example:

```
h <- hclust(as.dist(d), method="average") # see also: plot(h, labels=x)
cutree(h, 3)
## spam bacon eggs spa spams legs
## 1 2 3 1 1 3</pre>
```

yields a grouping into 3 clusters determined by the average linkage ("legs" and "eggs" are grouped together, "spam", "spam", "spams" form another cluster, and "bacon" is a singleton).

## 11.4.4 Eigenvalues and eigenvectors

**eigen** returns a sequence of eigenvalues  $(\lambda_1, \dots, \lambda_n)$  (ordered nondecreasingly w.r.t.  $|\lambda_i|$ ) and a matrix **V** whose columns define the corresponding eigenvectors (scaled to unit length) of a given matrix **X**. To recall, by definition, it holds that  $\mathbf{X}\mathbf{v}_{\cdot,i} = \lambda_i \mathbf{v}_{\cdot,i}$ .

Here are the eigenvalues and the corresponding eigenvectors of an example matrix (defining rotation in 2D by  $\pi/3$ ):

```
(R <- rbind(c(cos(pi/3), -sin(pi/3)), c(sin(pi/3), cos(pi/3))))
## [,1] [,2]
## [1,] 0.50000 -0.86603
## [2,] 0.86603 0.50000
eigen(R)
## eigen() decomposition
## $values
## [1] 0.5+0.86603i 0.5-0.86603i
##
## $vectors
## [,1] [,2]</pre>
```

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```
## [1,] 0.70711+0.00000i 0.70711+0.00000i
## [2,] 0.00000-0.70711i 0.00000+0.70711i
```

**Example 11.23** Consider a pseudorandom sample from a bivariate<sup>7</sup> normal distribution; see Figure 11.1.

```
Z <- matrix(rnorm(2000), ncol=2) # independent N(0, 1)
Z <- Z %*% rbind(c(1, 0), c(0, sqrt(5))) # scaling
Z <- Z %*% R # rotation
Z <- t(c(10, -5) + t(Z)) # translation
plot(Z, asp=1)</pre>
```

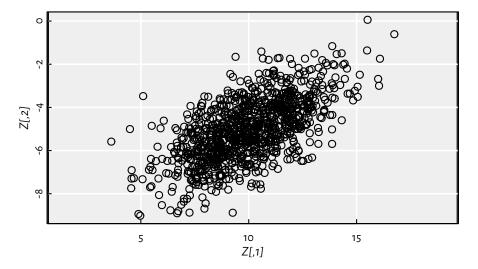


Figure 11.1: Example bivariate normal sample

It is known that eigenvectors of the covariance matrix correspond to the principal components of the original dataset. Furthermore, the eigenvalues give the variance explained by them.

```
eigen(cov(Z))
## eigen() decomposition
## $values
## [1] 5.18609 0.98386
##
## $vectors
## [,1] [,2]
```

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 $<sup>^7</sup>$  For drawing random samples from any multivariate distribution, refer to the theory of copulas, e.g., [45]. There are a few R packages on CRAN that implement the most popular models.

```
## [1,] -0.86715 0.49804
## [2,] -0.49804 -0.86715
```

this roughly corresponds to the principal directions  $[\sin(\pi/3), \cos(\pi/3)]$  and the theretoorthogonal  $[\cos(\pi/3), -\sin(\pi/3)]$  with variances of 5 and 1, respectively. Still, this method of performing a PCA is not particularly numerically stable; see below for an alternative.

### 11.4.5 QR decomposition

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We say that a real  $n \times m$  matrix  $\mathbf{Q}$ ,  $n \ge m$ , is orthogonal whenever  $\mathbf{Q}^T \mathbf{Q} = \mathbf{I}$  (identity matrix). This is equivalent to  $\mathbf{Q}$ 's being orthogonal unit vectors (if  $\mathbf{Q}$  is a square matrix, then  $\mathbf{Q}^T = \mathbf{Q}^{-1}$  if and only if  $\mathbf{Q}^T \mathbf{Q} = \mathbf{Q} \mathbf{Q}^T = \mathbf{I}$ ).

Let **A** be a real<sup>8</sup>  $n \times m$  matrix with  $n \ge m$ . Then **A** = **QR** is its QR decomposition (in the so-called narrow form), if **Q** is an orthogonal  $n \times m$  matrix and **R** is an upper triangular  $m \times m$  one.

The qr function returns an object of S3 class qr from which we can extract the two components; see the qr.Q and qr.R functions.

**Example 11.24** Let **X** be an  $n \times m$  data matrix, representing n points in  $\mathbb{R}^m$ , and a vector  $\mathbf{y} \in \mathbb{R}^n$  of the desired outputs corresponding to each input. For fitting a linear model  $\mathbf{x}^T \boldsymbol{\theta}$ , where  $\boldsymbol{\theta}$  is a vector of m parameters, we can use the method of least squares, which minimises

$$\mathcal{L}(\boldsymbol{\theta}) = \sum_{i=1}^{n} \left(\mathbf{x}_{i,\cdot}^{T} \boldsymbol{\theta} - y_{i}\right)^{2} = \|\mathbf{X}\boldsymbol{\theta} - \mathbf{y}\|_{2}^{2}$$

It might be shown that if  $\mathbf{X} = \mathbf{Q}\mathbf{R}$ , then  $\boldsymbol{\theta} = (\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^T\mathbf{y} = \mathbf{R}^{-1}\mathbf{Q}^T\mathbf{y}$ , which can conveniently be determined via a call to **qr.coef**.

In particular, we can fit a simple linear regression model y = ax + b by considering  $\mathbf{X} = [x, 1]$  and  $\boldsymbol{\theta} = [a, b]$ , for example (see Figure 11.2):

 $<sup>^8</sup>$  **A** can also be a complex matrix, which results in its QR decomposition's being such that **Q** is a unitary matrix.

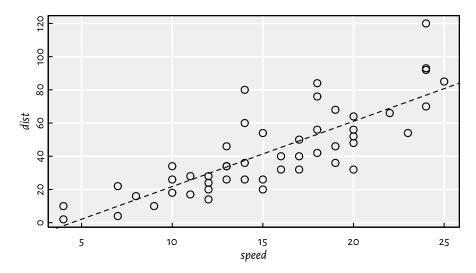


Figure 11.2: The built-in cars dataset and the fitted regression line

**solve** with one argument determines the inverse of a given matrix. The fitted model is y = 3.93241x - 17.5791.

The same approach is used by **Im.fit**, the workhorse behind the **Im** method accepting an R formula (which some readers might be familiar with; compare Section 17.6).

## 11.4.6 SVD decomposition

Given a real  $n \times m$  matrix **X**, its singular value decomposition (SVD) is given by **X** =  $\mathbf{U}\mathbf{D}\mathbf{V}^T$ , where **D** is a  $p \times p$  diagonal matrix (featuring the so-called singular values of **X**,  $d_{1,1} \ge ... \ge d_{p,p} \ge 0$ ,  $p = \min\{n, m\}$ ), and **U** and **V** are orthogonal matrices of dimension  $n \times p$  and  $m \times p$ , respectively.

**svd** may not only be used to determine the solution to linear regression but also to perform the principal component analysis. Namely,  $\mathbf{V}$  gives the eigenvectors of  $\mathbf{X}^T\mathbf{X}$ . Assuming that  $\mathbf{X}$  is centred at 0, the latter is precisely its scaled covariance matrix.

**Example 11.25** Continuing the PCA example above, we can determine the principal directions also by calling:

<sup>&</sup>lt;sup>9</sup> As the pseudoinverse  $\mathbf{X}^+ = \left(\mathbf{X}^T\mathbf{X}\right)^{-1}\mathbf{X}^T = \mathbf{V}\mathbf{D}^+\mathbf{U}^T = \mathbf{R}^{-1}\mathbf{Q}^T$ , with  $\mathbf{X}^+\mathbf{X} = \mathbf{I}$ . Here  $\mathbf{D}^+$  is a transposed version of  $\mathbf{D}$  featuring the reciprocals of its non-zero elements.

<sup>&</sup>lt;sup>10</sup> See the source code of **getS3method**("prcomp", "default").

```
Zc <- apply(Z, 2, function(x) x-mean(x)) # centred version of Z

svd(Zc)[["v"]]

## [,1] [,2]

## [1,] -0.86715 0.49804

## [2,] -0.49804 -0.86715
```

## 11.5 S4 classes (\*)

The concept of the S3-style object-oriented programming is based on a brilliantly simple idea (see Chapter 10): calling a generic  $\mathbf{f}(x)$  dispatches automatically to a method  $\mathbf{f.class\_of\_x}(x)$  or  $\mathbf{f.default}(x)$  in the case where the former does not exist. Naturally, it has some inherent limitations:

- classes cannot be formally defined; the class attribute may be assigned arbitrarily onto any object<sup>11</sup>,
- argument dispatch is performed only<sup>12</sup> with regard to one data type<sup>13</sup>.

In most cases, and with an appropriate level of mindfulness, this is not a problem at all. However, it is a typical condition of programmers who come to our world from more mainstream languages (e.g., C++; yours truly included) until they appreciate the true beauty of R's being somewhat different. Before they fully develop such an acquired taste, though, they grow restless as "R is not a real object-oriented system because it lacks polymorphism, encapsulation, formal inheritance, and so on, and something must be done about it". The truth is that it had not had to, but with high probability, it would have anyway in one way or another.

And so the fourth version of the S language was introduced in 1998 (see [9]). It brought a new object-oriented system, which we are used to referring to as S4. Its R version has been implemented in the methods package. Below we discuss it briefly; for more details, see help("Classes\_Details") and help("Methods\_Details") as well as [10] and [11].

**Note** (\*) S4 was loosely inspired by the Common Lisp Object System (with its defclass, defmethod, etc.; see, e.g., [20]). In the current author's opinion, the S4 system is somewhat of an afterthought. Due to appendages like this, R seems like a patch-

<sup>&</sup>lt;sup>11</sup> A partial solution to this could involve defining a method like **validate.class\_name**, which is called frequently and which checks whether a given object enjoys some desired constraints.

<sup>&</sup>lt;sup>12</sup> Although there are functions featuring some workarounds (see, e.g., cbind, which dispatches to cbind. data.frame if one argument is a data frame and the remaining ones are vectors or matrices). Also, we said in the previous chapter that binary operators consider the classes of both operands.

<sup>&</sup>lt;sup>13</sup> Hypothetically, we can imagine an OOP system relying on methods named like method.class\_name1. class\_name2 where dispatching is based on two argument types. It would be beautiful, but it is not the case in R.

work language; suffice it to say that it was not the last attempt to do a somewhat more real OOP in the overall functional R: the story will resume in Section 16.1.5.

The main problem with all the OOP approaches is that each of them is *parallel* to S3 which never lost its popularity and is still at the very core of our language. We are thus covering them for the sake of completeness because that's what must be done. After all, with non-zero probability, the reader will sooner or later come across such objects (e.g., below, we explain the meaning of a notation like x@slot). Also, yours truly rebelliously suggests taking statements such as "for new projects, it is recommended to use the more flexible and robust S4 scheme provided in the methods package" (see help("UseMethod")) with a pinch of salt.

### 11.5.1 Defining S4 classes

An S4 class can formally be registered through a call to **setClass**. For instance:

```
library("methods") # in the case where it is not auto-loaded
setClass("categorical", slots=c(data="integer", levels="character"))
```

defines a class named categorical. It has two slots: data and levels being integer and character vectors, respectively. This notation is already quite peculiar. There is no assignment suggesting that we have introduced something novel.

An object of the above class can be instantiated by calling **new**:

```
z <- new("categorical", data=c(1L, 2L, 2L, 1L, 1L), levels=c("a", "b"))
print(z)
## An object of class "categorical"
## Slot "data":
## [1] 1 2 2 1 1
##
## Slot "levels":
## [1] "a" "b"</pre>
```

That z is of the recently-introduced class can be verified as follows:

```
is(z, "categorical")
## [1] TRUE
class(z) # also: attr(z, "class")
## [1] "categorical"
## attr(,"package")
## [1] ".GlobalEnv"
```

**Important** Some R packages require the **methods** package only for the sake of being able to access the handy **is** function. It does not mean they are defining new S4 classes.

**Note** S4 objects are marked as being of the following basic type:

```
typeof(z)
## [1] "S4"
```

See Section 1.12 in [62] for technical details on how they are internally represented. In particular, in our case, all the slots are simply stored as object attributes:

```
attributes(z)
## $data
## [1] 1 2 2 1 1
##
## $levels
## [1] "a" "b"
##
## $class
## [1] "categorical"
## attr(,"package")
## [1] ".GlobalEnv"
```

#### Accessing slots 11.5.2

Reading or writing slot contents can be done via the `@` operator and the slot function or their replacement versions.

```
z@data # or slot(z, "data")
## [1] 1 2 2 1 1
z@levels <- c("A", "B")</pre>
```

**Note** The `@` operator can only be used on S4 objects, and some sanity checks are automatically performed:

```
z@unknown <- "spam"
## Error in (function (cl, name, valueClass) : 'unknown' is not a slot in
      class "categorical"
z@data <- "spam"
## Error in (function (cl, name, valueClass) : assignment of an object of
##
      class "character" is not valid for @'data' in an object of class
       "categorical"; is(value, "integer") is not TRUE
##
```

## 11.5.3 Defining methods

For the S4 counterparts of the S3 generics (Section 10.2), see **help**("setGeneric"). Luckily, there is an reasonable degree of interoperability between the S3 and S4 systems.

Let us start by introducing a new method for the well-known as.character generic. Instead of defining as.character.categorical, we need to register a new routine with setMethod.

```
setMethod(
    "as.character",  # name of the generic
    "categorical",  # class of 1st arg; or: signature=c(x="categorical")
    function(x, ...)  # method definition
        x@levels[x@data]
)
```

Testing:

```
as.character(z)
## [1] "A" "B" "B" "A" "A"
```

**show** is the S4 counterpart of **print**:

Interestingly, it is involved automatically upon a call to print:

```
print(z) # calls `show` for `categorical`
## [1] "A" "B" "A" "A"
## Categories: A, B
```

Methods that dispatch on the type of multiple arguments are also possible, for example:

```
(continued from previous page)
```

```
function (x, f, drop=FALSE, ...)
        split(x, as.character(f), drop=drop, ...)
)
```

allows the first argument to be of any type (like a default method), and:

```
setMethod(
    "split",
    c(x="matrix", f="categorical"),
    function (x, f, drop=FALSE, ...)
        lapply(
            split(seq\_len(NROW(x)), f, drop=drop, ...), # calls the above
            function(i) x[i, , drop=FALSE])
)
```

is a version tailored for matrices. Testing:

```
A <- matrix(1:35, nrow=5) # whatever
split(A, z) # matrix, categorical
## $A
     [,1] [,2] [,3] [,4] [,5] [,6] [,7]
##
## [1,7
        1
            6 11 16 21 26 31
## [2,]
            9 14 19 24
                            29
       4
                                 34
## [3,] 5 10 15 20 25 30 35
##
## $B
  [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## [1,] 2 7 12 17 22 27 32
## [2,]
       3
            8
                13 18 23
                             28
                                 33
split(1:5, z) # ANY, categorical
## $A
## [1] 1 4 5
##
## $B
## [1] 2 3
```

**Exercise 11.26** Overload the `[` operator for the categorical class.

## Defining constructors

We can also overload the initialize method, which is automatically called by new:

```
setMethod(
    "initialize", # class name
    "categorical", # method name
                                                                   (continues on next page)
```

(continued from previous page)

```
function(.Object, x)
{  # the method itself
    x <- as.character(x) # see above
    xu <- unique(sort(x)) # drops NAs

    .Object@data <- match(x, xu)
    .Object@levels <- xu

    .Object # return value - a modified object
}
</pre>
```

This allows for constructing new objects of the class categorical based on an object like x above, for instance:

```
w <- new("categorical", c("a", "c", "a", "a", "d", "c"))
print(w)
## [1] "a" "c" "a" "a" "d" "c"
## Categories: a, c, d</pre>
```

We have not set the two slots directly. They were automatically taken care of by **initialize** (note the American spelling).

**Exercise 11.27** Set up a validating method for our class; see **help**("setValidity").

#### 11.5.5 Inheritance

New S4 classes can be derived from existing ones, for instance:

```
setClass("binary", contains="categorical")
```

is a child class inhering all slots from its parent. We can, for example, overload the initialisation method for it:

#### Testing:

```
new("binary", c(TRUE, FALSE, TRUE, FALSE, NA, TRUE))
## [1] "1" "0" "1" "0" NA "1"
## Categories: 0, 1
```

We still used the **show** method of the parent class.

## 11.5.6 A note on the Matrix package

The Matrix package is perhaps the most widely known showcase of the S4 object orientation (and that is the reason why we cover S4 in this very chapter). It defines classes and methods for dense and sparse matrices, including rectangular, symmetric, triangular, band, and diagonal ones.

For instance, large graph (e.g., in network sciences) or preference (e.g., in recommender systems) data can be represented using sparse matrices (those which feature many os; after all, it is extremely more common for two vertices in a network *not* to be joined by an edge than to be connected).

#### For example:

It created a real diagonal matrix. Moreover:

```
B <- as(A, "sparseMatrix")
B[1, 2] <- 7
B[4, 1] <- 42
print(B)
## 5 x 5 sparse Matrix of class "dgCMatrix"
##
## [1,] 1 7 . . .
## [2,] . 2 . . .
## [3,] . . 3 . .
## [4,] 42 . . 4 .
## [5,] . . . . 5</pre>
```

yields a general sparse real matrix in the CRC (compressed, sparse, column-oriented) format.

For more information on the package, see vignette(package="Matrix").

#### 11.6 Exercises

**Exercise 11.28** Let X be a matrix with dimnames set, e.g.:

Explain (in your own words) the meaning of the following expressions involving matrix subsetting. Note that not each of them is valid.

```
    X[1, ],
```

- X[, 3],
- X[, 3, drop=FALSE],
- X[3],
- X[, "a"],
- X[, c("a", "b", "c")],
- X[, -2],
- X[X[,1] > 5, ],
- X[X[,1]>5, c("a", "b", "c")],
- X[X[,1]>=5 & X[,1]<=10, ],
- X[X[,1]>=5 & X[,1]<=10, c("a", "b", "c")],
- X[, c(1, "b", "d")].

**Exercise 11.29** Assuming that X is an array, what are the differences between the following indexing schemes?

```
    X["1", ] vs X[1, ],
```

- X[, "a", "b", "c"] vs X["a", "b", "c"] vs X[, c("a", "b", "c")] vs X[c("a", "b", "c")],
- X[1] vs X[, 1] vs X[1, ],
- X[X>0] vs X[X>0, ] vs X[, X>0],

- X[X[, 1]>0] vs X[X[, 1]>0,] vs X[,X[,1]>0],
- X[X[, 1]>5, X[1, ]<10] vs X[X[1, ]>5, X[, 1]<10].

**Exercise 11.30** *Give a few ways to create a matrix like:* 

```
## [,1] [,2]

## [1,] 1 1

## [2,] 1 2

## [3,] 1 3

## [4,] 2 1

## [5,] 2 2

## [6,] 2 3
```

and one like:

```
[,1] [,2] [,3]
    [1, 7]
##
   [2,]
##
   [3, 7]
##
   \lceil 4, \rceil 1
                2
##
   [5,7] 1
##
   [6,] 1
##
                      2
   [7,]
##
   [8,]
   [9,]
## [10,]
## [11,]
                      1
## [12,]
```

**Exercise 11.31** For a given real  $n \times m$  matrix  $\mathbf{X}$ , determine the bounding hyperrectangle of thusly encoded n input points in an m-dimensional space. Return a  $2 \times m$  matrix  $\mathbf{B}$  with  $b_{1,j} = \min_i x_{i,j}$  and  $b_{2,j} = \max_i x_{i,j}$ .

**Exercise 11.32** Let  $\mathbf{t}$  be a vector of n integers in  $\{1, \dots, k\}$ . Write a function to one-hot-encode each  $t_i$ : return a 0–1 matrix  $\mathbf{R}$  of size  $n \times k$  such that  $r_{i,j} = 1$  if and only if  $j = t_i$ . For example, if  $\mathbf{t} = [1, 2, 3, 2, 4]$  and k = 4, then:

$$\mathbf{R} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right].$$

On a side note, such a representation is beneficial when solving, e.g., a multiclass classification problem by means of k binary classifiers.

Then, write another function, but this time setting  $r_{i,j} = 1$  if and only if  $j \ge t_i$ , e.g.:

$$R = \left[ \begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{array} \right].$$

**Important** Kind reminder: as usual, try to solve all the exercises without using explicit **for** and **while** loops (provided that it is possible).

**Exercise 11.33** Given an  $n \times k$  real matrix, apply the softmax function on each row, i.e., map  $x_{i,j}$  to  $\frac{\exp(x_{i,j})}{\sum_{l=1}^k \exp(x_{i,l})}$ . Then, one-hot decode the values in each row, i.e., find the column number with the greatest value. Return a vector of size n with elements in  $\{1,\ldots,k\}$ .

**Exercise 11.34** Assume that an  $n \times m$  real matrix  $\mathbf{X}$  represents n points in  $\mathbb{R}^m$ . Write a function (but do not refer to dist) that determines the pairwise distances between all the n points and a given  $\mathbf{y} \in \mathbb{R}^m$ . Return a vector  $\mathbf{d}$  of length n with  $d_i = \|\mathbf{x}_{i.} - \mathbf{y}\|_2$ .

**Exercise 11.35** Let X and Y be two real-valued matrices of sizes  $n \times m$  and  $k \times m$ , respectively, representing two sets of points in  $\mathbb{R}^m$ . Return an integer vector  $\mathbf{r}$  of length k such that  $r_i$  indicates the index of the point in X with the least distance to (the closest to) the i-th point in Y, i.e.,  $r_i = \arg\min_i \|\mathbf{x}_{i,\cdot} - \mathbf{y}_{i,\cdot}\|_2$ .

**Exercise 11.36** Write your version of the built-in **utils**::combn.

**Exercise 11.37** Time series are vectors or matrices of the class ts equipped with the tspattribute, amongst others. Refer to **help**("ts") for more information about how they are represented and what S3 methods have been overloaded for them.

**Exercise 11.38** (\*) Numeric matrices can be stored in a CSV file, amongst others. Usually, we will be loading them via *read.csv*, which returns a data frame (see Chapter 12), for example:

```
X <- as.matrix(read.csv(
    paste0(
        "https://github.com/gagolews/teaching-data/",
        "raw/master/marek/eurxxx-20200101-20200630.csv"
    ),
    comment.char="#",
    sep=","
))</pre>
```

Write a function **read\_numeric\_matrix**(file\_name, comment, sep) which is based on a few calls to **scan** instead. Use **file** to establish a file connection so that you can ignore the comment lines and fetch the column names before reading the actual numeric values.

Exercise 11.39 (\*) Using readBin, read the t10k-images-idx3-ubyte.gz from the MNIST

database homepage<sup>14</sup>. The output object should be a three-dimensional,  $10000 \times 28 \times 28$  array with real elements between 0 and 255. Refer to the File Formats section therein for more details.

**Exercise 11.40** (\*\*) Circular convolution of discrete-valued multidimensional signals can be performed by means of **fft** and matrix multiplication, whereas affine transformations require only the latter. Apply various image transformations such as sharpening, shearing, and rotating on the MNIST digits and plot the results using the **image** function.

**Exercise 11.41** (\*) Using constrOptim, find the minimum of the Constrained Betts Function  $f(x_1, x_2) = 0.01x_1^2 + x_2^2 - 100$  with linear constraints  $2 \le x_1 \le 50$ ,  $-50 \le x_2 \le 50$ , and  $10x_1 \ge 10 + x_2$ . (\*\*) Also, use **solve.QP** from the **quadprog** package to find the minimum.

<sup>14</sup> https://web.archive.org/web/20211107114045/http://yann.lecun.com/exdb/mnist/

# Data frames

Most matrices are built on top of atomic vectors. Hence, they only allow items of the same type to be arranged into rows and columns. Data frames (objects of S3 class data. frame, first introduced in [13]), on the other hand, are collections of vectors of the same lengths or matrices with identical row counts, hence allowing to represent structured data of possibly heterogeneous types. For instance:

```
class(iris) # `iris` is an example built-in data frame
## [1] "data.frame"
iris[c(1, 51, 101), ] # 3 chosen rows from `iris`
       Sepal.Lenath Sepal.Width Petal.Lenath Petal.Width
                                                             Species
## 1
                5.1
                            3.5
                                          1.4
                                                      0.2
                                                              setosa
## 51
                            3.2
                                          4.7
                                                      1.4 versicolor
                7.0
                                          6.0
                                                      2.5 virginica
## 101
                6.3
                            3.3
```

It is a mix of numeric and factor-type data.

The good news is that not only are data frames built upon named lists (e.g., to extract a column, we can refer to `[[`), but also many functions recognise them to be matrix-like (e.g., to select specific rows and columns, two indexes can be passed to `[` like in the example above). Hence, it will soon turn out that we already know a lot about how to perform basic data wrangling activities, even if we do not fully realise it now.

**Important** Some readers will approach this chapter biased by what they know from elsewhere, including their experience with some popular third-party packages for data frame processing. The art is to filter out that information as noise (for the time being, at least). We will show how robust base R vocabulary is and how much can be implied from the material covered in the preceding chapters.

Yes, this book is like a breathtaking thriller/drama/love story: it is meant to be read from the beginning to the end. Please go back to the start of this comprehensive course if you happened to pop in here by accident or driven by "but I need to know *now*". Good morning.

<sup>&</sup>lt;sup>1</sup> We are already highly skilled in dealing with unstructured data and turning them into something that is much more regular: the numerous functions that we have covered in the first part of this book, allow us to extract meaningful data from text, handle missing values, engineer features, and so forth.

#### Creating data frames 12.1

#### data.frame and as.data.frame 12.1.1

Most frequently, data frames are based on a series of logical, numeric, or characters vectors of identical lengths. In such a scenario, the data.frame function is particularly worthwhile.

```
(x <- data.frame(</pre>
   a=c(TRUE, FALSE),
   b=1:6,
   c=runif(6),
   d=c("spam", "spam", "eggs")
))
        ab c
##
## 1 TRUE 1 0.77437 spam
## 2 FALSE 2 0.19722 spam
## 3 TRUE 3 0.97801 eggs
## 4 FALSE 4 0.20133 spam
## 5 TRUE 5 0.36124 spam
## 6 FALSE 6 0.74261 eggs
```

The shorter vectors were recycled. We can verify that the diverse column types were retained and no coercion was made, by calling:

```
str(x)
## 'data.frame': 6 obs. of 4 variables:
## $ a: logi TRUE FALSE TRUE FALSE TRUE FALSE
## $ b: int 123456
## $ c: num 0.774 0.197 0.978 0.201 0.361 ...
## $ d: chr "spam" "spam" "eggs" "spam" ...
```

We can also fetch the class of each column directly by calling (compare Section 12.3):

```
sapply(x, class) # the same as unlist(Map(class, x))
                                  C
    "logical" "integer" "numeric" "character"
```

Important For many reasons (see, e.g., Section 12.1.5 and Section 12.1.6), we recommend having the type of each column always checked, e.g., by calling the str function.

Many objects, such as matrices, can easily be coerced to data frames using particular as.data.frame methods.

Here is an example matrix:

Let us convert it to a data frame:

```
as.data.frame(A)  # as.data.frame.matrix

## u v

## 1 1 4

## 2 2 5

## 3 3 6
```

Note that a matrix with no row labels is printed slightly differently than a data frame with (as it will soon turn out) the default row.names.

Named lists are amongst other candidates for a meaningful conversion. Consider an example list where each element is a vector of the same length as the other ones:

```
(l <- Map(
   function(x) {
       c(Min=min(x), Median=median(x), Mean=mean(x), Max=max(x))
   split(iris[["Sepal.Length"]], iris[["Species"]])
))
## $setosa
    Min Median Mean Max
## 4.300 5.000 5.006 5.800
##
## $versicolor
    Min Median Mean
                       Max
## 4.900 5.900 5.936 7.000
##
## $virginica
     Min Median Mean
##
                         Max
## 4.900 6.500 6.588
                       7.900
```

Each list element will be turned into a separate column:

```
as.data.frame(l) # as.data.frame.list
         setosa versicolor virginica
## Min
          4.300
                    4.900
                             4.900
## Median 5.000
                     5.900
                               6.500
          5.006
                              6.588
## Mean
                     5.936
## Max
          5.800
                     7.000
                               7.900
```

Sadly, as.data.frame.list is not particularly fond of lists of vectors of incompatible lengths:

```
as.data.frame(list(a=1, b=11:12, c=21:23))
## Error in (function (..., row.names = NULL, check.rows = FALSE, check.names
## = TRUE, : arguments imply differing number of rows: 1, 2, 3
```

The above vectors could have been recycled with a warning. But they were not.

```
as.data.frame(list(a=1:4, b=11:12, c=21)) # recycling rule okay
## a b c
## 1 1 11 21
## 2 2 12 21
## 3 3 11 21
## 4 4 12 21
```

The method for the S3 class table (mentioned in Chapter 11) can be helpful as well. Here is an example contingency table together with its *unstacked* version.

```
(t <- table(mtcars[["vs"]], mtcars[["cyl"]]))</pre>
##
##
       4 6 8
    0 1 3 14
##
    1 10 4 0
##
as.data.frame(t) # as.data.frame.table; see the stringsAsFactors note below!
    Var1 Var2 Freq
## 1
      0
            4
                 1
## 2
       1
            4
                10
## 3
       0
            6
                .3
## 4
      1
            6
                4
## 5
       0
            8
               14
## 6
       1
                 0
```

as.data.frame.table is so handy that we might want to call it directly on any array. This way, we can convert it from the so-called wide format to the long one; see Section 12.3.6 for more details.

**Note** The above method is based on **expand.grid**, which determines all combinations of a given series of vectors.

```
expand.grid(1:2, c("a", "b", "c")) # see the stringsAsFactors note below!
##
     Var1 Var2
## 1
       1
## 2
## 3
            Ь
       1
## 4
      2
            Ь
## 5
      1
            C
## 6
       2
```

Overall, many classes of objects can be included<sup>2</sup> in a data frame; the popular choices include Date, POSIXct, and factor. It is worth noting that the data.frame function calls the corresponding as.data.frame method. Also, format is used whilst printing the columns.

**Example 12.1** Here are two custom methods for what we would like to call from now on an S3 class spam:

```
as.data.frame.spam <- function(x, ...)
    structure(
        list(x),
        class="data.frame",
        row.names=seq_along(x)
    )
format.spam <- function(x, ...)
    paste0("*", x, "*")</pre>
```

Testing data frame creation and printing:

```
data.frame(
    a=structure(c("a", "b", "c"), class="spam"),
    b=factor(c("spam", "bacon", "spam")),
    c=Sys.Date()+1:3
)
##    a    b    c
## 1 *a* spam 2023-05-04
## 2 *b* bacon 2023-05-05
## 3 *c* spam 2023-05-06
```

#### 12.1.2 cbind.data.frame and rbind.data.frame

There are data frame-specific versions of **cbind** or **rbind** (which we discussed in the context of stacking matrices; Section 11.1.2). They are used quite eagerly:

<sup>&</sup>lt;sup>2</sup> The attributes of objects stored as matrix columns will generally be preserved (even if they are not displayed by **print**; see **str** though).

**help**("cbind") states that they will be referred to if at least<sup>3</sup> one of its arguments is a data frame, and the other arguments are atomic vectors or lists (possibly with the dim attribute).

For example:

```
x <- iris[c(1, 51, 101), c("Sepal.Length", "Species")] # whatever
cbind(Yummy=c(TRUE, FALSE, TRUE), x)
## Yummy Sepal.Length Species
## 1 TRUE 5.1 setosa
## 51 FALSE 7.0 versicolor
## 101 TRUE 6.3 virginica</pre>
```

It added a new column to a data frame x. Moreover:

```
rbind(x, list(42, "virginica"))
## Sepal.Length Species
## 1     5.1     setosa
## 51     7.0 versicolor
## 101     6.3 virginica
## 11     42.0 virginica
```

It added a new row. Note that columns are of different types. Hence, the values to row-bind were provided as a generic vector. The list can also be named. It can consist of vectors of length greater than one, given in any order:

```
rbind(x, list(
    Species=c("virginica", "setosa"),
    Sepal.Length=c(42, 7)
))
##
       Sepal.Length
                       Species
## 1
                5.1
                         setosa
## 51
                7.0 versicolor
## 101
                6.3 virginica
## 11
               42.0 virainica
                7.0
## 2
                         setosa
```

Sometimes a direct referral to these methods will be necessary. Consider an example list of atomic vectors:

```
x <- list(a=1:3, b=11:13, c=21:23)
```

First, we call the generic, which dispatches to the default method:

<sup>&</sup>lt;sup>3</sup> This is a clear violation of the rule that an S3 generic dispatches on the type of only one argument (usually: the first). It is an exception made for the sake of the questionable user *convenience*. Also, note that there is no **cbind.default** method available: it is hardcoded at the C language level.

If we want to ensure we garner a data frame as a result, we need to write:

```
do.call(cbind.data.frame, x)
## a b c
## 1 1 11 21
## 2 2 12 22
## 3 3 13 23
```

This is particularly useful for fetching outputs from Map and its friends, which are wrapped inside a list. For instance:

```
l <- unname(Map(</pre>
    function(x) list(
        Sepal.Length=mean(x[["Sepal.Length"]]),
        Sepal.Width=mean(x[["Sepal.Width"]]),
        Species=x[["Species"]][1]
    split(iris, iris[["Species"]]) # split.data.frame; see below
))
str(l)
## List of 3
## $ :List of 3
   ..$ Sepal.Length: num 5.01
##
   ..$ Sepal.Width : num 3.43
   ..$ Species : Factor w/ 3 levels "setosa", "versicolor",..: 1
##
## $ :List of 3
   ..$ Sepal.Length: num 5.94
##
##
   ..$ Sepal.Width : num 2.77
## ..$ Species
                   : Factor w/ 3 levels "setosa", "versicolor",... 2
## $ :List of 3
    ..$ Sepal.Length: num 6.59
##
   ..$ Sepal.Width : num 2.97
##
##
     ..$ Species : Factor w/ 3 levels "setosa", "versicolor",...: 3
```

It is nothing more than a fancy way to obtain an illustrative list, which we may now turn into a data frame by calling:

```
do.call(rbind.data.frame, l)
## Sepal.Length Sepal.Width Species
## 1 5.006 3.428 setosa
(continues on next page)
```

```
## 2
                         2.770 versicolor
            5.936
## 3
            6.588
                         2.974 virginica
```

On the other hand, **do.call**(rbind, l) does not return an amiable object type:

```
do.call(rbind, l)
##
        Sepal.Length Sepal.Width Species
## [1,] 5.006
                    3.428
                                 setosa
## [2,] 5.936
                    2.77
                                 versicolor
## [3,] 6.588
                     2.974
                                 virainica
```

Despite the pretty face, it is a matrix... over a list:

```
str(do.call(rbind, l))
## List of 9
## $ : num 5.01
## $ : num 5.94
## $ : num 6.59
## $ : num 3.43
## $ : num 2.77
## $ : num 2.97
## $ : Factor w/ 3 levels "setosa", "versicolor",..: 1
## $ : Factor w/ 3 levels "setosa", "versicolor",...: 2
## $ : Factor w/ 3 levels "setosa", "versicolor",..: 3
## - attr(*, "dim")= int [1:2] 3 3
## - attr(*, "dimnames")=List of 2
   ..$ : NULL
##
     ..$: chr [1:3] "Sepal.Length" "Sepal.Width" "Species"
##
```

# 12.1.3 Reading data frames

Structured data can be imported from external sources, such as CSV/TSV (comma/tabseparated values) or HDF5 files, relational databases supporting SQL (see Section 12.1.4), web APIs (e.g., through the curl and jsonlite packages), spreadsheets [60], and so on.

In particular, read.csv and the like fetch data from plain text files consisting of records, where commas, semicolons, tabs, etc. separate the fields.

For instance:

```
x <- data.frame(a=runif(3), b=c(TRUE, FALSE, TRUE)) # example data frame
f <- tempfile() # temporary file name</pre>
write.csv(x, f, row.names=FALSE) # export
```

It created a CSV file that looks like:

```
cat(readLines(f), sep="\n") # print file contents
## "a", "b"
## 0.287577520124614, TRUE
## 0.788305135443807, FALSE
## 0.4089769218117, TRUE
```

The above can be read by calling:

```
read.csv(f)

## a b

## 1 0.28758 TRUE

## 2 0.78831 FALSE

## 3 0.40898 TRUE
```

**Exercise 12.2** Check out **help**("read.table") for a long list of tunable parameters, especially: sep, dec, quote, header, comment.char, and row.names. Further, note that reading from compressed files is supported directly.

**Important** CSV is the most portable and user-friendly format for exchanging matrix-like objects between different programs and computing languages (Python, Julia, LibreOffice Calc, etc.). Such files can be opened in any text editor.

**Note** As mentioned in Section 8.3.5, we can process data frames on a chunk-by-chunk basis, This is beneficial especially when data do not fit into memory (compare the nrows argument to **read.csv**).

# 12.1.4 Interfacing relational databases and querying with SQL (\*)

The **DBI** package provides a universal interface for particular database management systems whose drivers are implemented in additional add-ons such as **RSQLite**, **RMariabB**, **RPostgreSQL**, etc., or, more generally, **RODBC** or **odbc**. For more details, see Section 4 of [60].

**Example 12.3** Let us play with an in-memory (volatile) instance of an SQLite database.

```
library("DBI")
con <- dbConnect(RSQLite::SQLite(), ":memory:")</pre>
```

It returned an object representing a database connection which we can refer to in further communication.

An easy way to create a database table is to call:

```
dbWriteTable(con, "mtcars", mtcars) # `mtcars` is a toy built-in data frame
```

Alternatively, dbExecute could have been called to send SQL statements such as CREATE TABLE ... followed by a series of INSERT INTO ....

Some data retrieval can now follow:

```
dbGetQuery(con,
   SELECT cyl, vs, AVG(mpg) AS mpg_ave, AVG(hp) AS hp_ave
   FROM mtcars
   GROUP BY cyl, vs
")
##
   cyl vs mpg_ave hp_ave
## 1 4 0 26.000 91.00
## 2 4 1 26.730 81.80
## 3 6 0 20.567 131.67
## 4 6 1 19.125 115.25
## 5 8 0 15.100 209.21
```

It gave us an ordinary R data frame. We can process it in the same fashion as any other object of this kind.

At the end, the database connection must be closed.

```
dbDisconnect(con)
```

**Exercise 12.4** Database passwords must never be stored in plain text files, let alone in R scripts in version-controlled repositories. Consider a few ways to fetch credentials programmatically:

- using environment variables (see help("Sys.getenv")),
- using the keyring package,
- calling system2 (Section 7.3.3) to retrieve it from the system keyring (e.g., the keyring package for Python provides a platform-independent command-line utility).

#### Strings as factors? 12.1.5

The following is so critical that we devote a separate section to discuss it so we always remain vigilant (such is life: maintaining some level of mindfulness is often a good idea).

Important Some functions related to data frames automatically convert character vectors to factors. This behaviour is frequently controlled by the stringsAsFactors argument.

This is particularly problematic because, when printed, factor and character columns look identical:

```
(x <- data.frame(a=factor(c("U", "V")), b=c("U", "V")))
## a b
## 1 U U
## 2 V V</pre>
```

We recall from Section 10.3.2 that factors can be nasty. For example, passing factors as indexers in `[` or converting them with as.numeric might give counterintuitive (for the uninformed) results. Also, when we want to extend factors by previously unobserved data, new levels must manually be added. This can cause some unexpected behaviour in contexts such as:

Therefore, always having the data types checked is a praiseworthy habit. For instance:

```
str(x)
## 'data.frame': 2 obs. of 2 variables:
## $ a: Factor w/ 2 levels "U", "V": 1 2
## $ b: chr "U" "V"
```

Before R 4.0, some functions, including data.frame and read.csv had the stringsAs-Factors argument defaulting to TRUE. It is no longer the case for many of them.

However, exceptions to this rule still exist, e.g., including as.data.frame.table and expand.grid. Besides, some built-in example data frames have factor-typed columns inherited from the old days, e.g.:

```
class(iris[["Species"]])
## [1] "factor"
```

We observe that the Species column in iris is not of the type character. Thence, adding a new variety might be oblique:

```
iris2 <- iris[c(1, 51, 101), ] # example subset
levels(iris2[["Species"]]) <- c(levels(iris2[["Species"]]), "croatica")</pre>
rbind(iris2, c(6, 3, 3, 2, "croatica"))
      Sepal.Length Sepal.Width Petal.Length Petal.Width
##
                                                          Species
## 1
               5.1
                          3.5
                                       1.4
                                                    0.2
                                                           setosa
## 51
                 7
                          3.2
                                       4.7
                                                   1.4 versicolor
## 101
               6.3
                           3.3
                                                    2.5 virginica
                                          6
                                                         croatica
## 4
```

Alternatively, we could have simply converted the Species column to the type character.

### 12.1.6 Internal representation

Objects of S3 class data.frame are built upon lists of vectors of the same length or matrices with identical row counts. Such lists define their consecutive columns. Apart from class, they must be equipped with the following special attributes:

- names a character vector (as usual in any named list) labelling the columns or their groups,
- row.names a character or integer vector with no duplicates nor missing values, doing what is advertised.

Therefore, a data frame can be created from scratch by calling, for example:

```
structure(
    list(a=11:13, b=21:23), # sets the `names` attribute already
    row.names=1:3,
    class="data.frame"
)
## a b
## 1 11 21
## 2 12 22
## 3 13 23
```

Here is a data frame based on a length-5 list, a matrix with five rows, and a length-5 numeric vector with some fancy row names on top:

```
structure(
   list(
       a=list(1, 1:2, 1:3, numeric(0), -(4:1)),
       b=cbind(u=11:15, v=21:25),
       c=runif(5)
   ),
   row.names=c("spam", "bacon", "eggs", "ham", "aubergine"),
   class="data.frame"
)
##
                         a b.u b.v c
                        1 11 21 0.28758
## spam
## bacon
                    1, 2 12 22 0.78831
## eggs
                  1, 2, 3 13 23 0.40898
## ham
                            14 24 0.88302
## aubergine -4, -3, -2, -1 15 25 0.94047
```

In general, the columns of the type list can contain anything, e.g., other lists or R

functions. Including atomic vectors of varying lengths, just like above, allows for creating something à la *ragged arrays* – a pretty handy scenario.

The issue with matrix entries, on the other hand, is that they appear as if they were many. Still, as it will turn out in the sequel, they are often treated as a single complex column, e.g., by the index operator (see Section 12.2). Therefore, from this perspective, the above data frame has three columns, not four. Such compound columns can be output by **aggregate** (see Section 12.3), amongst others. They are valuable in certain contexts: the *column groups* can be easily accessed as a whole and batch-processed in the same way.

**Important** Unfortunately, data frames with list or matrix columns cannot be normally created with the **data.frame** nor **cbind** functions. This might explain why they are less popular. This behaviour is dictated by the underlying **as.data.frame** methods, which they both call. As a curiosity, see **help**("I"), though.

**Exercise 12.5** Verify that if a data frame has a matrix column, the matrix does not need to have any column names (the second dimnames).

The names and row.names attributes are special in the sense of Section 4.4.3. In particular, they can be accessed or modified by the corresponding functions.

It is worth noting that <code>row.names(df)</code> always returns a character vector, even when <code>attr(df, "row.names")</code> is an integer vector. Further, calling "<code>row.names(df) <- NULL"</code> will reset<sup>4</sup> this attribute to the most commonly desired case of consecutive natural numbers, for example:

```
(x \leftarrow iris[c(1, 51, 101), ]) # comes with some sad row names
##
       Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                              Species
## 1
                5.1
                            3.5
                                          1.4
                                                               setosa
## 51
                7.0
                            3.2
                                          4.7
                                                      1.4 versicolor
## 101
                6.3
                            3.3
                                          6.0
                                                      2.5 virginica
row.names(x) <- NULL # reset to seq_len(NROW(x))</pre>
     Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                           Species
## 1
              5.1
                          3.5
                                        1.4
                                                             setosa
## 2
              7.0
                          3.2
                                        4.7
                                                    1.4 versicolor
              6.3
                                                    2.5 virginica
## 3
                          3.3
                                        6.0
```

**Exercise 12.6** What is the name of the replacement version of the row. names method for the data. frame class?

Exercise 12.7 Implement your version of expand.grid.

<sup>4 `</sup>attr<-`(df, "row.names") does not feature the same sanity checks as `row.names<-`(df) does. For instance, it is easy to corrupt a data frame by setting too short a row.names attribute.

**Exercise 12.8** Write a version of **xtabs** that does not rely on a formula interface (compare Section 10.3.4). Allow three parameters: a data frame, the name of the "counts" column, and the names of the cross-classifying variables. Hence,  $my_xtabs(x, "Freq", c("Var1", "Var2"))$  should be equivalent to **xtabs**(Freq~Var1+Var2, x).

# 12.2 Data frame subsetting

#### 12.2.1 Data frames are lists

Data frames are named lists, where each element represents an individual column. Therefore<sup>5</sup>, **length** yields the number of columns and **names** gives their respective labels.

Let us play with the following data frame:

```
(x <- data.frame(</pre>
   a=runif(6),
   b=rnorm(6),
   c=LETTERS[1:6],
   d1=c(FALSE, TRUE, FALSE, NA, FALSE, NA),
   d2=c(FALSE, TRUE, FALSE, TRUE, FALSE, TRUE)
))
##
                     b c
                            d1
                                   12
## 1 0.287578 0.070508 A FALSE FALSE
## 2 0.788305 0.129288 B TRUE TRUE
## 3 0.408977 1.715065 C FALSE FALSE
## 4 0.883017 0.460916 D
                            NA TRUF
## 5 0.940467 -1.265061 E FALSE FALSE
## 6 0.045556 -0.686853 F
                           NA TRUE
typeof(x) # each data frame is a list
## [1] "list"
length(x) # the number of columns
## [1] 5
names(x)
         # column labels
## [1] "a" "b" "c" "d1" "d2"
```

The one-argument versions of extract and index operators behave as expected. `[[` fetches (looks inside) the contents of a given column:

<sup>&</sup>lt;sup>5</sup> This is a strong word. This implication relies on an implicit assumption that the primitive functions **length** and **names** have not been contaminated by treating data frames differently than named lists. Luckily, that is indeed not the case. Although we have the index operators specially overloaded for the data.frame class, they behave quite reasonably. As we will see, they allow for a mix of list- and matrix-like behaviours.

```
x[["a"]] # or x[[1]]
## [1] 0.287578 0.788305 0.408977 0.883017 0.940467 0.045556
```

`[` returns a data frame (a list with extras) comprised of the specified elements:

```
x["a"] # or x[1]
##
## 1 0.287578
## 2 0.788305
## 3 0.408977
## 4 0.883017
## 5 0.940467
## 6 0.045556
x[c(TRUE, TRUE, FALSE, TRUE, FALSE)]
## a
                   b d1
## 1 0.287578 0.070508 FALSE
## 2 0.788305 0.129288 TRUE
## 3 0.408977 1.715065 FALSE
## 4 0.883017 0.460916 NA
## 5 0.940467 -1.265061 FALSE
## 6 0.045556 -0.686853 NA
```

Just like with lists, the replacement versions of the said operators can be used to add new or replace existing columns.

```
y <- head(x, 1) # for a more compact display
y[["a"]] <- round(y[["a"]], 1) # replaces the column with new content
y[["b"]] <- NULL # removes the column, like, totally
y[["e"]] <- 10*y[["a"]]^2 # adds a new column at the end
print(y)
## a c d1 d2 e
## 1 0.3 A FALSE FALSE 0.9
```

**Example 12.9** Some spam for thought to show how much we already know. Here are a few common use cases of indexing using some popular vectorised functions.

```
y <- head(x, 1) # example data frame (more compact display)
```

Move the column a to the end:

Remove the columns a and c:

```
y[-match(c("a", "c"), names(y))]
## b d1 d2
## 1 0.070508 FALSE FALSE
```

Select all columns between a and c:

```
y[match("a", names(y)):match("c", names(y))]
## a bc
## 1 0.28758 0.070508 A
```

Fetch the columns with names starting with d:

```
y[grep("^d", names(y))]
## d1 d2
## 1 FALSE FALSE
```

Change the name of column c to z:

```
names(y)[names(y) == "c"] <- "z"
print(y)
##
            b z d1 d2
## 1 0.28758 0.070508 A FALSE FALSE
```

Change names: d2 to u and d1 to v:

```
names(y)[match(c("d2", "d1"), names(y))] <- c("v", "u")
print(y)
##
              bz u
## 1 0.28758 0.070508 A FALSE FALSE
```

**Note** Some R users might prefer the `\$` operator over `[[`, but we do not. By default, the former supports partial matching of column names which might be appealing when R is used interactively. Nonetheless, it does not work on matrices nor it allows for programmatically generated names. It is also trickier to use on not syntactically valid labels; compare Section 9.4.1.

**Exercise 12.10** Write a function names\_replace that changes the names of columns based on a translation table given in a from=to fashion, for instance:

```
names\_replace <- function(x, ...) ...to.do...
x <- data.frame(a=1, b=2, c=3)
names_replace(x, c="new_c", a="new_a")
## new_a b new_c
## 1 1 2
```

#### 12.2.2 Data frames are matrix-like

Data frames can be considered "generalised" matrices. They store data of any kind (possibly mixed) organised in a tabular fashion. Some functions mentioned in the previous chapter will be overloaded for the data frame case. These include: dim (despite the lack of the dim attribute), NROW, NCOL, and dimnames (which is, of course, based on row.names and names).

For example:

```
(x <- data.frame(</pre>
    a=runif(6),
    b=rnorm(6),
    c=LETTERS[1:6],
    d1=c(FALSE, TRUE, FALSE, NA, FALSE, NA),
    d2=c(FALSE, TRUE, FALSE, TRUE, FALSE, TRUE)
))
##
                      b c
                             d1
## 1 0.287578 0.070508 A FALSE FALSE
## 2 0.788305 0.129288 B TRUE TRUE
## 3 0.408977 1.715065 C FALSE FALSE
## 4 0.883017 0.460916 D
                            NA TRUE
## 5 0.940467 -1.265061 E FALSE FALSE
## 6 0.045556 -0.686853 F NA TRUE
dim(x) # the number of rows and columns
## [1] 6 5
dimnames(x) # it is not a matrix, but a matrix-like object
## [[1]]
## [1] "1" "2" "3" "4" "5" "6"
##
## [[2]]
## [1] "a" "b" "c" "d1" "d2"
```

In addition to the list-like behaviour, which only allows for dealing with particular columns or groups thereof, the `[` operator was also equipped with the ability to take two indexers:

```
x[1:2,] # first two rows

## a b c d1 d2

## 1 0.28758 0.070508 A FALSE FALSE

## 2 0.78831 0.129288 B TRUE TRUE

x[x[["a"]] >= 0.3 & x[["a"]] <= 0.8, -2] # or use x[, "a"]

## a c d1 d2

## 2 0.78831 B TRUE TRUE

## 3 0.40898 C FALSE FALSE
```

Recall the drop argument to `[` and its effects on matrix indexing. In the current case, its behaviour will be similar with regard to the operations on individual columns:

```
x[, 1]  # synonym: x[[1]], because drop=TRUE

## [1] 0.287578 0.788305 0.408977 0.883017 0.940467 0.045556

x[, 1, drop=FALSE] # synonym: x[1]

## a

## 1 0.287578

## 2 0.788305

## 3 0.408977

## 4 0.883017

## 5 0.940467

## 6 0.045556
```

When we extract a single row and more than one column, drop does not apply. It is because columns (unlike in matrices) can potentially be of different types:

```
x[1, 1:2] # two numeric columns but the result is still a numeric
## a b
## 1 0.28758 0.070508
```

#### However:

```
x[1, 1]
## [1] 0.28758
x[1, 1, drop=FALSE]
## a
## 1 0.28758
```

**Note** Once again, let us take note of logical indexing featuring missing values:

```
x[x[["d1"]], ]
##
                    Ь
                            d1
## 2
       0.78831 0.12929
                       B TRUE TRUE
## NA
           NA
                  NA <NA>
                            NA
## NA.1
           NA
                  NA <NA> NA
x[which(x[["d1"]]), ] # drops missing values
                b c d1 d2
##
         а
## 2 0.78831 0.12929 B TRUE TRUE
```

The default behaviour is consistent with many other R functions: it explicitly indicates that something is missing (we are selecting a "don't know"; hence, the result is "don't know" as well). Regretfully, this comes with no warning. As we rarely manually check missing values in the outputs, our absent-mindedness can lead to code bugs.

By far, we might have already noted that the index operator adjusts (not: resets) the row.names attribute. For instance:

It is a version of x comprised of only the top three values in the u column. Indexing by means of character vectors will refer to row.names and names:

This is not the same as "xs[5, c("a", "b")]", even though row.names is formally an integer vector here.

**Note** If a data frame features a matrix, we need to use the index/extract operator twice in order to access a specific sub-column:

In other words, neither "x[["Sepal.Length.Min"]]" nor "x[, "Sepal.Length.Min"]" works.

Regarding the replacement version of the index operator, it is a quite flexible tool. It allows the new content to be a vector, a data frame, a list, or even a matrix.

**Exercise 12.11** Write two replacement functions<sup>6</sup>. First, **set\_row\_names** which replaces the row.names of a data frame with the contents of a specific column, for example:

```
(x <- aggregate(iris[1], iris[5], mean)) # some data frame
## Species Sepal.Length
## 1 setosa 5.006
## 2 versicolor 5.936
(continues on next page)</pre>
```

<sup>6 (\*)</sup> Compare pandas.DataFrame.set\_index and pandas.DataFrame.reset\_index in Python.

```
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```

```
## 3 virginica
                      6.588
set_row_names(x) <- "Species"</pre>
print(x)
##
             Sepal.Length
## setosa
                    5.006
## versicolor
                    5.936
## virginica
                     6.588
```

Second, reset\_row\_names which converts row.names to a standalone column of a given name, for instance:

```
reset_row_names(x) <- "Type"</pre>
print(x)
## Sepal.Length
                      Type
          5.006
## 1
                    setosa
## 2
          5.936 versicolor
## 3
          6.588 virginica
```

These two functions may be handy as they allow for writing "x[something, ]" instead of "x[x[["column"]] %**in**% something, ]".

#### **Common operations** 12.3

Below we review the most commonly applied operations related to data frame wrangling. We have a few dedicated functions or methods overloaded for the data. frame class. However, we have already mastered the necessary skills to deal with such objects through our hard work: in particular, by solving all the exercises listed in the preceding chapters. Let us repeat: data frames are just lists exhibiting matrix-like behaviour.

# 12.3.1 Ordering rows

Ordering rows in a data frame with respect to different criteria can be easily achieved through the **order** function and the two-argument version of `[`.

For instance, here are the top six cars in terms of the time (in seconds) to complete a 402-metre race:

```
mtcars6 <- mtcars[order(mtcars[["qsec"]])[1:6], ]</pre>
mtcars6[["model"]] <- row.names(mtcars6)</pre>
row.names(mtcars6) <- NULL</pre>
print(mtcars6)
```

(continues on next page)

```
##
      mpg cyl disp hp drat
                              wt qsec vs am gear carb
                                                                model
## 1 15.8
              351 264 4.22 3.17 14.50
                                        0
                                           1
                                                5
                                                     4 Ford Pantera L
## 2 15.0
              301 335 3.54 3.57 14.60
                                                5
                                                        Maserati Bora
## 3 13.3
              350 245 3.73 3.84 15.41
                                                3
                                                           Camaro Z28
## 4 19.7
            6 145 175 3.62 2.77 15.50 0
                                                5
                                                         Ferrari Dino
## 5 14.3
            8 360 245 3.21 3.57 15.84 0
                                                3
                                                           Duster 360
                                           0
## 6 21.0
              160 110 3.90 2.62 16.46 0
                                                            Mazda RX4
```

**order** uses a stable sorting algorithm. Therefore, any sorting with respect to a different criterion will not break the *relative* ordering of qsec in row groups with ties:

```
mtcars6[order(mtcars6[["cyl"]]), ]
     mpg cyl disp hp drat wt gsec vs am gear carb
                                                              model
            6 145 175 3.62 2.77 15.50
## 4 19.7
                                               5
                                                   6
                                                       Ferrari Dino
## 6 21.0
             160 110 3.90 2.62 16.46 0
                                                          Mazda RX4
## 1 15.8
           8 351 264 4.22 3.17 14.50 0 1
                                              5
                                                   4 Ford Pantera L
## 2 15.0
           8 301 335 3.54 3.57 14.60 0 1
                                               5
                                                      Maserati Bora
## 3 13.3
           8 350 245 3.73 3.84 15.41
                                      0 0
                                               3
                                                         Camaro Z28
## 5 14.3
              360 245 3.21 3.57 15.84
                                               3
                                                         Duster 360
```

**Example 12.12** Notice the difference between ordering by cyl and gear vs gear and cyl:

```
mtcars6[order(mtcars6[["cyl"]], mtcars6[["gear"]]), ]
      mpg cyl disp hp drat wt qsec vs am gear carb
                                                             model
          6 160 110 3.90 2.62 16.46 0 1
                                                         Mazda RX4
## 6 21.0
## 4 19.7
           6 145 175 3.62 2.77 15.50 0
                                                   6
                                                      Ferrari Dino
## 3 13.3
           8 350 245 3.73 3.84 15.41 0 0
                                              3
                                                         Camaro Z28
                                                   4
## 5 14.3
           8 360 245 3.21 3.57 15.84 0 0
                                              3
                                                   4
                                                        Duster 360
## 1 15.8
           8 351 264 4.22 3.17 14.50 0 1
                                              5
                                                   4 Ford Pantera L
           8 301 335 3.54 3.57 14.60 0 1
## 2 15.0
                                              5
                                                   8
                                                     Maserati Bora
mtcars6[order(mtcars6[["gear"]], mtcars6[["cyl"]]), ]
     mpa cvl disp hp drat wt qsec vs am gear carb
                                                             model
           8 350 245 3.73 3.84 15.41
## 3 13.3
                                                        Camaro Z28
## 5 14.3
           8 360 245 3.21 3.57 15.84
                                              3
                                        0
                                                        Duster 360
## 6 21.0
           6 160 110 3.90 2.62 16.46 0 1
                                              4
                                                   4
                                                         Mazda RX4
           6 145 175 3.62 2.77 15.50 0 1
## 4 19.7
                                              5
                                                       Ferrari Dino
## 1 15.8
           8 351 264 4.22 3.17 14.50 0 1
                                              5
                                                   4 Ford Pantera L
## 2 15.0
           8 301 335 3.54 3.57 14.60 0
                                              5
                                                   8 Maserati Bora
```

**Note** Mixing increasing and decreasing ordering is tricky as the decreasing argument to **order** currently does not accept multiple flags in all the contexts. Perhaps the easiest way to change the ordering direction is to use the unary minus operator on the column(s) to be sorted decreasingly.

```
mtcars6[order(mtcars6[["gear"]], -mtcars6[["cyl"]]), ]
     mpg cyl disp hp drat wt gsec vs am gear carb
                                                             mode1
## 3 13.3
           8 350 245 3.73 3.84 15.41
                                              3
                                                  4
                                                        Camaro Z28
## 5 14.3
             360 245 3.21 3.57 15.84
                                              3
                                                  4
                                                        Duster 360
## 6 21.0
           6 160 110 3.90 2.62 16.46 0 1
                                                         Mazda RX4
                                              4
                                                  4
## 1 15.8
         8 351 264 4.22 3.17 14.50 0 1
                                              5
                                                 4 Ford Pantera L
           8 301 335 3.54 3.57 14.60 0 1
## 2 15.0
                                              5
                                                  8 Maserati Bora
## 4 19.7
           6 145 175 3.62 2.77 15.50 0 1
                                              5
                                                       Ferrari Dino
```

For factor and character columns, xtfrm can convert them to sort keys first.

```
mtcars6[order(mtcars6[["cyl"]], -xtfrm(mtcars6[["model"]])), ]
##
     mpg cyl disp hp drat wt gsec vs am gear carb
                                                            model
## 6 21.0
         6 160 110 3.90 2.62 16.46 0 1
                                                  4
                                                        Mazda RX4
## 4 19.7
           6 145 175 3.62 2.77 15.50 0 1
                                             5
                                                  6
                                                     Ferrari Dino
## 2 15.0 8 301 335 3.54 3.57 14.60 0 1
                                             5
                                                  8 Maserati Bora
## 1 15.8 8 351 264 4.22 3.17 14.50 0 1
                                             5
                                                  4 Ford Pantera L
## 5 14.3 8 360 245 3.21 3.57 15.84 0 0
                                             3
                                                  4
                                                       Duster 360
## 3 13.3
           8 350 245 3.73 3.84 15.41 0 0
                                             3
                                                       Camaro Z28
```

Both of the above behave like decreasing=c(FALSE, TRUE).

**Exercise 12.13** Write a method **sort.data.frame** that orders a data frame with respect to a given set of columns.

```
sort.data.frame <- function(x, decreasing=FALSE, cols) ...to.do...</pre>
sort(mtcars6, cols=c("cyl", "model"))
     mpg cyl disp hp drat wt gsec vs am gear carb
                                                             mode1
## 4 19.7
         6 145 175 3.62 2.77 15.50 0 1
                                             5
                                                  6
                                                     Ferrari Dino
## 6 21.0
           6 160 110 3.90 2.62 16.46 0 1
                                             4
                                                  4
                                                         Mazda RX4
## 3 13.3 8 350 245 3.73 3.84 15.41 0 0
                                             3
                                                        Camaro Z28
                                                  4
## 5 14.3 8 360 245 3.21 3.57 15.84 0 0
                                             .3
                                                        Duster 360
## 1 15.8 8 351 264 4.22 3.17 14.50 0 1
                                             5
                                                  4 Ford Pantera L
## 2 15.0
           8 301 335 3.54 3.57 14.60 0 1
                                             5
                                                  8 Maserati Bora
```

Unfortunately, that decreasing must be of length one and be placed as the second method argument is imposed by the **sort** S3 generic.

# 12.3.2 Handling duplicated rows

**duplicated**, **anyDuplicated**, and **unique** have methods overloaded for the data.frame class. They can be used to indicate, get rid of, or replace the repeating rows.

```
sum(duplicated(iris)) # how many duplicated rows are there?
## [1] 1
(continues on next page)
```

### 12.3.3 Joining (merging) data frames

The **merge** function can perform the JOIN operation that some readers might know from SQL<sup>7</sup>. It matches the items in the columns that two given data frames somewhat share and then returns their combination.

**Example 12.14** Two calls to <code>merge</code> could be used to match data on programmers (each identified by <code>developer\_id</code> and giving such details as their name, location, main skill, etc.) with the information about the open-source projects (each identified by <code>project\_id</code> and informing us about its title, scope, web site, and so forth) they are engaged in (based on a third data frame featuring <code>developer\_id</code> and <code>project\_id</code> pairs).

As a simple illustration, consider the two following objects:

```
A <- data.frame(
    u=c("b0", "b1", "b2", "b3"),
    v=c("a0", "a1", "a2", "a3")
)

B <- data.frame(
    v=c("a0", "a2", "a2", "a4"),
    w=c("c0", "c1", "c2", "c3")
)</pre>
```

The two *common* columns, i.e., storing data of similar nature (a-something strings), are both named v.

First, the *inner* (*natural*) *join*, where we list only the matching pairs:

```
merge(A, B) # x=A, y=B, by="v", all.x=FALSE, all.y=FALSE

## v u w

## 1 a0 b0 c0

## 2 a2 b2 c1

## 3 a2 b2 c2
```

The common column (or, more generally, columns) is included only once in the result.

<sup>&</sup>lt;sup>7</sup> JOIN is the reverse operation to data normalisation known from the relational database theory. It reduces data redundancy and increases their integrity. What data scientists need for succeeding with their daily activities (analysis, visualisation, processing) is sometimes the opposite of what the art of data management focuses on (efficient collection and storage). The readers are encouraged to learn about various normalisation forms from, e.g., [16] or any other course covering this topic.

The *left join* guarantees that all elements in the first data frame will be included in the result:

```
merge(A, B, all.x=TRUE) # by="v", all.y=FALSE

## v u w

## 1 a0 b0 c0

## 2 a1 b1 <NA>

## 3 a2 b2 c1

## 4 a2 b2 c2

## 5 a3 b3 <NA>
```

The right join includes all records in the second argument:

```
merge(A, B, all.y=TRUE) # by="v", all.x=FALSE

## v u w

## 1 a0 b0 c0

## 2 a2 b2 c1

## 3 a2 b2 c2

## 4 a4 <NA> c3
```

The *full outer join* is their set-theoretic union:

**Exercise 12.15** Show how match (Section 5.4.1) can be used to implement a very basic version of merge.

# 12.3.4 Aggregating and transforming columns

Let us discuss how to perform data aggregation or engineer features. Although we already know how to access individual columns with `[` and process them using the many vectorised functions, we still have something interesting to add about the said matter.

It would be tempting to try implementing such operations with **apply**. Unfortunately, currently, this function coerces its argument to a matrix. Hence, we should refrain from applying it on data frames whose columns are of mixed types<sup>8</sup>.

However, taking into account that data frames are special lists, we can always call Map and its relatives.

<sup>&</sup>lt;sup>8</sup> Due to this, storing data as matrix columns inside data frames is not such a bad idea.

### **Example 12.16** Given an example data frame:

```
(iris sample <- iris[sample(NROW(iris), 6), ])</pre>
       Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                              Species
                             3.5
                                          1.5
## 28
                5.2
                                                       0.2
                                                               setosa
## 80
                5.7
                             2.6
                                          3.5
                                                       1.0 versicolor
                6.3
                             3.3
                                          6.0
                                                       2.5 virginica
## 101
                             3.2
## 111
                6.5
                                          5.1
                                                       2.0 virginica
## 137
                6.3
                             3.4
                                          5.6
                                                       2.4 virginica
## 133
                6.4
                             2.8
                                          5.6
                                                       2.2 virginica
```

To get the class of each column, we can call:

```
sapply(iris_sample, class) # or unlist(Map(class, iris))
## Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## "numeric" "numeric" "numeric" "factor"
```

*Next, here is a way to compute some aggregates of the numeric columns:* 

or:

```
sapply(iris_sample[sapply(iris_sample, is.numeric)], mean)
## Sepal.Length Sepal.Width Petal.Length Petal.Width
## 6.0667 3.1333 4.5500 1.7167
```

We can also fetch more than a single summary of each column:

```
as.data.frame(Map(
    function(x) c(Min=min(x), Max=max(x)),
    Filter(is.numeric, iris sample)
))
       Sepal.Length Sepal.Width Petal.Length Petal.Width
##
## Min
                5.2
                            2.6
                                          1.5
                                                       0.2
## Max
                6.5
                             3.5
                                          6.0
                                                       2.5
```

or:

```
sapply(iris_sample[sapply(iris_sample, is.numeric)], quantile, c(0, 1))
## Sepal.Length Sepal.Width Petal.Length Petal.Width
## 0% 5.2 2.6 1.5 0.2
## 100% 6.5 3.5 6.0 2.5
```

The latter called **simplify2array** automatically. Thus, the result is a matrix.

```
iris_sample[] <- Map(function(x) {</pre>
    if (!is.numeric(x)) x else (x-mean(x))/sd(x)
}, iris_sample)
print(iris_sample)
       Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                           Species
                                               -1.65318
          -1.70405
                                   -1.76004
## 28
                       1.03024
                                                            setosa
## 80
          -0.72094
                      -1.49854
                                   -0.60591
                                               -0.78117 versicolor
## 101
          0.45878
                      0.46829
                                    0.83674
                                                0.85384 virginica
## 111
          0.85202
                       0.18732
                                    0.31738
                                                0.30884 virginica
                                                0.74484 virginica
## 137
           0.45878
                      0.74927
                                    0.60591
                                                0.52684 virainica
           0.65540
                      -0.93659
                                    0.60591
## 133
```

## 12.3.5 Handling missing values

The **is.na** method for objects of the class data.frame returns a logical matrix of the same dimensionality<sup>9</sup>, indicating whether the corresponding items are missing or not. Of course, this function can still be called on individual columns as well.

Further, na.omit can be used to get rid of rows with missing values.

**Exercise 12.17** Given a data frame, use is. na and other functions such as apply or approx to:

- 1. remove all rows that feature at least one missing value,
- 2. remove all rows that only consist of missing values,
- 3. remove all columns that feature at least one missing value,
- 4. for each column, replace all missing values with the column averages,
- 5. for each column, replace all missing values with values that linearly interpolate between the preceding and succeeding well-defined observations (of use in time series), e.g., the blanks in c(0.60, 0.62, NA, 0.64, NA, NA, 0.58) should be filled to obtain c(0.60, 0.62, 0.63, 0.64, 0.62, 0.60, 0.58).

## 12.3.6 Reshaping data frames

Consider an example matrix:

(continues on next page)

<sup>&</sup>lt;sup>9</sup> Provided that a data frame does not feature a matrix column.

```
names(dimnames(A)) <- c("Row", "Col")
print(A)
## Col
## Row u v
## X 0.29 0.88
## Y 0.79 0.94
## Z 0.41 0.05</pre>
```

The as.data.frame method for the table class can be called directly on any array:

It is an instance of array *reshaping*. More precisely, we call it *stacking*: we converted from a *wide* (okay, in this example, not so wide, as we have only two columns) to a *long* format.

This can be also achieved by means of the **reshape** function which is more flexible and operates directly on data frames (but is harder to use):

```
(df <- `names<-`(
   data.frame(row.names(A), A, row.names=NULL),
   c("Row", "Col.u", "Col.v")))
   Row Col.u Col.v
## 1 X 0.29 0.88
## 2 Y 0.79 0.94
      Z 0.41 0.05
(stacked <- reshape(df, varying=2:3, direction="long"))</pre>
     Row time Col id
## 1.u X
            u 0.29 1
## 2.u Y u 0.79 2
## 3.u Z
           u 0.41 3
## 1.v X v 0.88 1
## 2.v Y v 0.94 2
## 3.v Z
            v 0.05 3
```

Maybe the default column names are not superb, but we can adjust them manually afterwards.

The reverse operation is called *unstacking*:

```
reshape(stacked, idvar="Row", timevar="time", drop="id", direction="wide")

## Row Col.u Col.v

## 1.u X 0.29 0.88

## 2.u Y 0.79 0.94

## 3.u Z 0.41 0.05
```

Exercise 12.18 Given a named numeric vector, convert it to a data frame with two columns, for instance:

```
convert <- function(x) ...to.do...
x <- c(spam=42, eggs=7, bacon=3)
convert(x)
## key value
## 1 spam 42
## 2 eggs 7
## 3 bacon 3</pre>
```

**Exercise 12.19** Reshape (stack) the built-in WorldPhones dataset. Then, reshape (unstack) the stacked WorldPhones dataset. Further, unstack the stacked set but first remove<sup>10</sup> five random rows from it and then randomly permute all the remaining rows. Fill in the missing entries with NAs.

**Exercise 12.20** Implement a basic version of **as.data.frame.table** manually (using **rep** etc.). Also, write a function **as.table.data.frame** that implements its reverse. Make sure both functions are compatible with each other.

**Exercise 12.21** The built-in Titanic is a four-dimensional array. Convert it to a long data frame.

**Exercise 12.22** Perform what follows on the data frame defined below:

- 1. convert the second column from character to a list of character vectors (split at ", ");
- 2. extract the first elements from each of the vectors;
- 3. extract the last elements:
- 4. (\*) unstack the data frame;
- 5. (\*) stack it back to a data frame featuring a list;
- 6. convert the list back to a character column (concatenate with ", " as separator).

```
(x <- data.frame(
    name=c("Kat", "Ron", "Jo", "Mary"),
    food=c("buckwheat", "spam,bacon,spam", "", "eggs,spam,spam,lollipops")
))
## name food

(continues on next page)</pre>
```

<sup>&</sup>lt;sup>10</sup> The original dataset can be thought of as representing a fully crossed design experiment (all combinations of two grouping variables are present). Its truncated version is like an incomplete cross-design.

```
## 1 Kat buckwheat
## 2 Ron spam,bacon,spam
## 3 Jo
## 4 Mary eggs,spam,spam,lollipops
```

**Exercise 12.23** Write a function that converts all matrix-based columns in a given data frame to separate atomic columns. Also, write a function that does the opposite: one that groups all columns with similar prefixes and turns them into matrices.

## 12.3.7 Aggregating data in groups

We can straightforwardly apply various transforms on data groups determined by a factor-like variable or a combination thereof thanks to the **split.data.frame** method, which returns a list of data frames.

For example:

```
x <- data.frame(</pre>
    a=c( 10.
                    20,
                           30,
                                   40.
                                           50),
    u=c("spam", "spam", "eggs", "spam", "eggs"),
                   2,
           1,
                           1,
                                    1,
split(x, x["u"]) # i.e., split.data.frame(x, x["u"]) or x[["u"]]
## $eggs
## a u v
## 3 30 eggs 1
## 5 50 eggs 1
##
## $spam
    а
          u v
## 1 10 spam 1
## 2 20 spam 2
## 4 40 spam 1
```

It split x with respect to the u column, which served as the grouping variable. On the other hand:

```
split(x, x[c("u", "v")]) # sep="."
## $eggs.1
## a u v
## 3 30 eggs 1
## 5 50 eggs 1
##
## $spam.1
## a u v
```

(continues on next page)

```
## 1 10 spam 1
## 4 40 spam 1
##
## $eggs.2
## [1] a u v
## <0 rows> (or 0-length row.names)
##
## $spam.2
## a u v
## 2 20 spam 2
```

It partitioned with respect to a combination of two factor-like sequences. A nonexistent level pair (eggs, 2) resulted in an empty data frame.

**Exercise 12.24** split.data.frame (when called explicitly) can also be used to break a matrix into a list of matrices (rowwisely). Given a matrix, perform its train-test split: allocate, say, 70% of the rows at random into one matrix and the remaining 30% into another.

If we need to aggregate grouped data in numeric columns, **sapply** is quite convenient. To recall, it is a combination of **lapply** (one-vector version of **Map**) and **simplify2array** (Section 11.1.3).

```
sapply(split(iris[1:2], iris[5]), sapply, mean)
## setosa versicolor virginica
## Sepal.Length 5.006 5.936 6.588
## Sepal.Width 3.428 2.770 2.974
```

If the function to apply returns more than a single value, **sapply** will not return too informative a result: the list of matrices converted to a matrix will not have the row. names argument set. As a workaround, we either call **simplify2array** explicitly or pass simplify="array" to **sapply**:

```
(res <- sapply(
   split(iris[1:2], iris[5]),
   sapply,
   function(x) c(Min=min(x), Max=max(x)),
   simplify="array"
)) # or simplify2array(lapply or Map etc.)
## , , setosa
##
      Sepal.Length Sepal.Width
##
              4.3
## Min
                         2.3
## Max
              5.8
                          4.4
##
## , , versicolor
##
```

```
Sepal.Length Sepal.Width
##
## Min
               4.9
                           2.0
                7.0
## Max
                           3.4
##
## , , virginica
##
##
       Sepal.Length Sepal.Width
## Min
                4.9
                            2.2
                7.9
## Max
                            3.8
```

It yielded a three-dimensional array, which is particularly handy if we now wish to access specific results by name:

```
res[, "Sepal.Length", "setosa"]
## Min Max
## 4.3 5.8
```

Also, the previously mentioned as.data.frame.table method works on it like a charm (up to the column names):

```
as.data.frame.table(res)
     Var1
                 Var2
##
                           Var3 Freq
## 1 Min Sepal.Length setosa 4.3
## 2 Max Sepal.Length
                        setosa 5.8
## 3 Min Sepal.Width
                        setosa 2.3
## 4 Max Sepal.Width
                        setosa 4.4
## 5 Min Sepal.Length versicolor 4.9
## 6 Max Sepal.Length versicolor 7.0
## 7 Min Sepal.Width versicolor 2.0
## 8 Max Sepal.Width versicolor 3.4
## 9 Min Sepal.Length virginica 4.9
## 10 Max Sepal.Length virginica 7.9
## 11 Min Sepal.Width virainica 2.2
## 12 Max Sepal.Width virginica 3.8
```

**Note** If the grouping (by) variable is a list of two or more factors, the combined levels will be concatenated to a single string:

```
as.data.frame.table(as.array(sapply(
    split(ToothGrowth["len"], ToothGrowth[c("supp", "dose")]),
    sapply,
    mean
)))
## Var1 Freq
```

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```
(continued from previous page)
```

```
## 1 0J.0.5.len 13.23

## 2 VC.0.5.len 7.98

## 3 0J.1.len 22.70

## 4 VC.1.len 16.77

## 5 0J.2.len 26.06

## 6 VC.2.len 26.14
```

Also, the name of the aggregated column (len) has been included. This behaviour yields a result that may be deemed convenient in some contexts but not necessarily so in others.

**Exercise 12.25** Many aggregation functions are idempotent, which means that when they are fed with a vector with all the elements being identical, the result is exactly that unique element: min, mean, median, and max behave this way.

Overload the **mean** and **median** methods for character vectors and factors. They should return NA when fed with a sequence where not all elements are the same. Otherwise, they are expected to output the unique value.

```
mean.character <- function(x, na.rm=FALSE, ...) ...to.do...
mean.factor <- function(x, na.rm=FALSE, ...) ...to.do...</pre>
```

This way, we can also aggregate the grouping variables conveniently:

The built-in **aggregate** method can assist us in when a single function is to be applied on all columns in a data frame.

```
aggregate(iris[-5], iris[5], mean) # not: ...[[5]]
        Species Sepal.Length Sepal.Width Petal.Length Petal.Width
##
                      5.006
                                  3.428
                                                1.462
                                                            0.246
## 2 versicolor
                      5.936
                                   2.770
                                                4.260
                                                            1.326
                      6.588
                                   2.974
                                                5.552
                                                            2.026
## 3 virginica
aggregate(ToothGrowth["len"], ToothGrowth[c("supp", "dose")], mean)
    supp dose
```

(continues on next page)

The second argument, by, must be list-like (this includes data frames). Neither a factor nor an atomic vector are acceptable. Also, if the function being applied returns many values, they will be wrapped into a matrix column:

```
(x <- aggregate(iris[2], iris[5], function(x) c(Min=min(x), Max=max(x))))</pre>
        Species Sepal.Width.Min Sepal.Width.Max
## 1
         setosa
                            2.3
                                            4.4
## 2 versicolor
                           2.0
                                            3.4
## 3 virginica
                           2.2
                                            3.8
class(x[["Sepal.Width"]])
## [1] "matrix" "array"
x[["Sepal.Width"]] # not: Sepal.Width.Max, etc.
       Min Max
## [1,] 2.3 4.4
## [2,] 2.0 3.4
## [3, ] 2.2 3.8
```

It is actually handy because by referring to x[["Sepal.Width"]], we have access to all the stats for this column. Further, if many columns are being aggregated simultaneously, we can process all the summaries in the same way.

**Exercise 12.26** Check out the built-in **by** function, which supports some basic split-apply-bind use cases. Note the particularly peculiar behaviour of the **print** method for the by class.

The most flexible scenario involves applying a custom function returning any set of aggregates in the form of a list and then row-binding the results to obtain a data frame.

**Example 12.27** The following implements an R version of what we would express in SQL as:

```
SELECT supp, dose, AVG(len) AS ave_len, COUNT(*) AS count
FROM ToothGrowth
GROUP BY supp, dose
```

Ad rem:

II DEEPER

(continued from previous page)

```
dose=df[1, "dose"],
       ave_len=mean(df[["len"]]),
       count=NROW(df)
   )
))
##
         supp dose ave_len count
## 0J.0.5
         OJ 0.5 13.23
## VC.0.5 VC 0.5
                    7.98
                             10
## 0J.1
           OJ 1.0
                     22.70
                             10
## VC.1
          VC 1.0 16.77
                             10
## 0J.2
           OJ 2.0 26.06
                             10
## VC.2
           VC 2.0
                    26.14
                             10
```

**Example 12.28** As an exercise, let us study a function that takes a named list x (can be a data frame) and a sequence of col=f pairs and applies the function f (or each function from a list of functions f) on the named element col in x:

```
napply \leftarrow function(x, ...)
{
    fs <- list(...)
    stopifnot(is.list(x), !is.null(names(x)))
    stopifnot(all(names(fs) %in% names(x)))
    do.call(
        c, # concatenates lists
        lapply(
            structure(seq_along(fs), names=names(fs)),
            function(i)
            { # always returns a list
                y <- x[[ names(fs)[i] ]]</pre>
                 if (is.function(fs[[i]]))
                     list(fs[[i]](y))
                else
                     lapply(fs[[i]], function(f) f(y))
            }
        )
    )
}
```

For example:

```
first <- function(x, ...) head(x, n=1L, ...) # we use it below
napply(ToothGrowth,
    supp=first, dose=first, len=list(ave=mean, count=length)
)
## $supp
                                                                 (continues on next page)
```

```
## [1] VC
## Levels: OJ VC
##
## $dose
## [1] 0.5
##
## $len.ave
## [1] 18.813
##
## $len.count
## [1] 60
```

applies **first** on both ToothGrowth[["supp"]] and ToothGrowth[["dose"]] as well as **mean** and **length** on ToothGrowth[["len"]]. List names are there for a more dramatic effect.

And now:

```
do.call(
   rbind.data.frame,
   lapply(
       split(ToothGrowth, ToothGrowth[c("supp", "dose")]),
       napply,
       supp=first, dose=first, len=list(ave=mean, count=length)
   )
)
##
         supp dose len.ave len.count
## 0J.0.5 0J 0.5 13.23
                                10
## VC.0.5 VC 0.5
                    7.98
                                10
## 0J.1 0J 1.0 22.70
                                10
## VC.1
         VC 1.0 16.77
                                10
## 0J.2
         OJ 2.0 26.06
                                10
## VC.2
         VC 2.0
                   26.14
                                10
```

or even:

```
aaaggg <- function(x, by, ...)
    do.call(rbind.data.frame, lapply(split(x, x[by]), napply, ...))</pre>
```

so that:

This brings fun back to R programming in the sad times when many things are given to us on a plate.

By the way, the above has not been tested thoroughly. It is a proof of concept. As usual, testing, debugging, and extending are left as an exercise for the reader.

**Example 12.29** Section 10.5 considered an example where we used our own **group\_by** function and an aggregation method overloaded for the object's class it returns.

Here is the function that splits a data frame into a list of data frames with respect to a combination of levels in given named columns:

```
group_by <- function(df, by)
{
    stopifnot(is.character(by), is.data.frame(df))
    df <- droplevels(df) # in case there are factors with empty levels
    structure(
        split(df, df[names(df) %in% by]),
        class="list_dfs",
        by=by
    )
}</pre>
```

The next function applies a set of aggregates on every column of each data frame in a given list (two nested *lapply*s plus some cosmetic additions):

```
aggregate.list_dfs <- function(x, FUN, ...)</pre>
{
    aggregates <- lapply(x, function(df) {
        is by <- names(df) %in% attr(x, "by")
        res <- lapply(df[!is_by], FUN, ...)
        res mat <- do.call(rbind, res)
        if (is.null(dimnames(res_mat)[[2]]))
            dimnames(res_mat)[[2]] <- paste0("f", seq_len(NCOL(res_mat)))</pre>
        cbind(
            `row.names<-`(df[1, is_by, drop=FALSE], NULL),
            x=row.names(res_mat),
            `row.names<-`(res_mat, NULL)
        )
    })
    combined_aggregates <- do.call(rbind.data.frame, aggregates)</pre>
    `row.names<-`(combined_aggregates, NULL)
}
aggregate(group_by(ToothGrowth, c("supp", "dose")), range)
     supp dose x f1 f2
     OJ 0.5 len 8.2 21.5
## 1
       VC 0.5 len 4.2 11.5
## 2
## 3
       OJ 1.0 len 14.5 27.3
                                                               (continues on next page)
```

```
## 4  VC 1.0 len 13.6 22.5
## 5  OJ 2.0 len 22.4 30.9
## 6  VC 2.0 len 18.5 33.9
```

We really want our API to be bloated. Hence, let us introduce a convenience function, which is a specialised version of the above:

## 12.3.8 Transforming data in groups

Some variables will sometimes need to be transformed relative to what is happening in a dataset's subsets. This is the case, e.g., where we decide that missing values should be replaced by the corresponding within-group averages or want to compute the relative ranks or z-scores.

If the loss of the original ordering of rows is not an issue, the standard split-apply-bind will suffice.

An example data frame:

```
(x <- data.frame(
    a=c( 10,  1,  NA,  NA,  NA,  4),
    b=c( -1,  10,  40,  30,  1,  20),
    c=runif(6),
    d=c("v", "u", "u", "v", "u")
))
##    a    b     c  d
## 1 10 -1 0.52811 v
## 2    1 10 0.89242 u
## 3 NA 40 0.55144 u
## 4 NA 30 0.45661 u
## 5 NA    1 0.95683 v
## 6    4 20 0.45333 u</pre>
```

Some operations:

And now:

```
do.call(rbind.data.frame, lapply(
    split(x, x["d"]),
    function(df) {
        df[["a"]] <- fill_na(df[["a"]])</pre>
        df[["b"]] <- rank(df[["b"]])</pre>
        df[["c"]] <- standardise(df[["c"]])</pre>
        df
    }
))
##
          a b
                      c d
## u.2 1.0 1 1.46357 u
## u.3 2.5 4 -0.17823 u
## u.4 2.5 3 -0.63478 u
## u.6 4.0 2 -0.65057 u
## v.1 10.0 1 -0.70711 v
## v.5 10.0 2 0.70711 v
```

Only the *relative* ordering of rows within groups has been retained. Overall, the rows are in a different order.

If this is an issue, we can use the **unsplit** function:

```
unsplit(
    lapply(
        split(x, x["d"]),
        function(df) {
            df[["a"]] <- fill_na(df[["a"]])</pre>
            df[["b"]] <- rank(df[["b"]])</pre>
            df[["c"]] <- standardise(df[["c"]])</pre>
            df
        }
    ),
    x["d"]
)
        a b
## 1 10.0 1 -0.70711 v
## 2 1.0 1 1.46357 u
## 3 2.5 4 -0.17823 u
## 4 2.5 3 -0.63478 u
## 5 10.0 2 0.70711 v
## 6 4.0 2 -0.65057 u
```

**Exercise 12.30** Show how we can do the above also via the replacement version of **split**.

**Example 12.31** Reverting to the previous ordering can be done manually too. It is because the

split operation behaves as if we first ordered the data frame with respect to the grouping variable(s) (using a stable sorting algorithm).

Here is some transformation of a sample data frame split by a combination of two factors:

```
(x <- `row.names<-`(ToothGrowth[sample(NROW(ToothGrowth), 10), ], NULL))</pre>
##
       len supp dose
## 1
     23.0
           OJ 2.0
## 2 23.3
            OJ 1.0
## 3 29.4
           OJ 2.0
            OJ 1.0
## 4 14.5
## 5 11.2 VC 0.5
## 6 20.0 OJ 1.0
## 7 24.5
           OJ 2.0
## 8 10.0 OJ 0.5
## 9
      9.4
           OJ 0.5
## 10 7.0
           VC 0.5
(y <- do.call(rbind.data.frame, lapply(</pre>
    split(x, x[c("dose", "supp")]), # two grouping variables
   function(df) {
       df[["len"]] <- df[["len"]] * 100^df[["dose"]] * # whatever
            ifelse(df[["supp"]] == "0J", -1, 1)
                                                       # do not overthink it
       df
)))
##
                len supp dose
## 0.5.0J.8
               -100
                      OJ 0.5
## 0.5.0J.9
                -94
                      OJ 0.5
## 1.0J.2
              -2330
                      OJ 1.0
## 1.0J.4
                      OJ 1.0
              -1450
## 1.0J.6
              -2000
                      OJ 1.0
## 2.0J.1
                      OJ 2.0
            -230000
## 2.0J.3
            -294000 OJ 2.0
## 2.0J.7
            -245000
                      OJ 2.0
## 0.5.VC.5
                      VC
                          0.5
                112
## 0.5.VC.10
                 70
                      VC 0.5
```

Section 5.4.4 mentioned that by calling **order**, we can determine the inverse of a given permutation. Hence, we can call:

```
y[order(order(x[["supp"]], x[["dose"]])), ] # not: dose, supp
##
                  len supp dose
                       OJ 2.0
## 2.0J.1
             -230000
## 1.0J.2
               -2330
                       OJ 1.0
## 2.0J.3
             -294000
                       OJ 2.0
## 1.0J.4
                       OJ 1.0
               -1450
## 0.5.VC.5
                 112
                       VC 0.5
                                                               (continues on next page)
```

```
## 1.0J.6
               -2000
                          1.0
                       OJ
## 2.0J.7
             -245000
                       OJ 2.0
## 0.5.0J.8
                -100
                       OJ 0.5
## 0.5.0J.9
                 - 94
                       OJ 0.5
## 0.5.VC.10
                  70
                       VC 0.5
```

Additionally, we can manually restore the original row.names, et voilà.

## 12.3.9 Metaprogramming-based techniques (\*)

Section 9.5.7 mentioned that R is equipped with the ability to write programs that manipulate unevaluated expressions. As a consequence, some functions provide us with convenient<sup>II</sup> interfaces to a few common operations. These include **transform**, {commandsubset, with, and basically every procedure accepting a formula. The popular **data.table** and **dplyr** packages also fall into this class (Section 12.3.10).

However, we have already noted that each method must be studied separately. It can arbitrarily interpret the *form* of the passed arguments without taking into account their *real* meaning. Hence, we avoid<sup>12</sup> them in this course, as we can do perfectly without them.

Withal, they are thought-provoking on their own. Furthermore, they are quite popular in other users' code. This is why they deserve an honourable mention. Learning them in more detail is left to the kind reader as an optional exercise.

**Example 12.32** For instance, let us consider an example call to the **subset** function:

```
subset(iris, Sepal.Length>7.5, -(Sepal.Width:Petal.Width))
       Sepal.Length
##
                      Species
## 106
                7.6 virginica
                7.7 virginica
## 118
                7.7 virginica
## 119
## 123
                7.7 virginica
                7.9 virainica
## 132
                7.7 virginica
## 136
```

Neither Sepal.Length>7.5 nor - (Sepal.Width: Petal.Width) make sense as standalone R expressions because we have not defined the named variables used therein:

<sup>&</sup>lt;sup>11</sup> Furthermore, some third-party packages can sometimes be faster and more memory efficient (on larger datasets), as is usually the case with more specialised tools. However, in many daily programming contexts, the speed of the data wrangling operations is not often an issue. Remember that we always have SQL-supporting relational databases at our disposal.

<sup>&</sup>lt;sup>12</sup> We are not alone in our calling to refrain from using them. help("subset") warns (and help("transform") quite similarly): This is a convenience function intended for use interactively. For programming, it is better to use the standard subsetting functions like `[`, and in particular the nonstandard evaluation of argument subset can have unanticipated consequences. The same in help("with"): For interactive use, this is very effective and nice to read. For programming however, i.e., in one's functions, more care is needed, and typically one should refrain from using with, as, e.g., variables in data may accidentally override local variables.

```
Sepal.Length>7.5 # utter nonsense

## Error in eval(expr, envir, enclos): object 'Sepal.Length' not found
-(Sepal.Width:Petal.Width) # gibberish

## Error in eval(expr, envir, enclos): object 'Sepal.Width' not found
```

Only from **help**("subset") we can learn that this tool generously decides that the second expression plays the role of a row selector. Moreover, the third one removes all the columns between the two given ones.

In our course, we pay attention to developing transferable skills. Assuming that R is not the only language we are going to learn during our long and happy lives, it is much more likely that in the next environment, we will be writing something more of the more basic form instead:

```
between <- function(x, from, to) (which(from == x):which(to == x))
iris[iris[["Sepal.Length"]]>7.5,
    -between(names(iris), "Sepal.Width", "Petal.Width")]
##
      Sepal.Length Species
## 106
                7.6 virginica
                7.7 virginica
## 118
                7.7 virginica
## 119
## 123
                7.7 virginica
## 132
                7.9 virginica
## 136
                7.7 virginica
```

Let us stress again that this is a book on how to become a great chef who proudly uses sustainably-sourced produce, not how to order ultra-processed food from DeliverNoodlesQuickly.com.

**Example 12.33** transform can be used to add, modify, and remove columns in a data frame with the possibility of referring to existing features as if they were ordinary variables:

```
head(transform(mtcars, log hp=log(hp), am=2*am-1, hp=NULL))
##
                    mpg cyl disp drat wt gsec vs am gear carb log hp
## Mazda RX4
                   21.0
                         6 160 3.90 2.620 16.46 0 1
                                                            4 4.7005
                         6 160 3.90 2.875 17.02 0 1
## Mazda RX4 Wag
                   21.0
                                                        4
                                                            4 4.7005
## Datsun 710
                   22.8 4 108 3.85 2.320 18.61 1 1
                                                        4
                                                            1 4.5326
                  21.4 6 258 3.08 3.215 19.44 1 -1
## Hornet 4 Drive
                                                       3
                                                            1 4.7005
## Hornet Sportabout 18.7 8 360 3.15 3.440 17.02 0 -1
                                                        3
                                                            2 5.1648
                         6 225 2.76 3.460 20.22 1 -1
## Valiant
                   18.1
```

Similarly, **attach** adds any named list to the search path (see Section 16.2.6) so that the columns can be accessed by name. Nevertheless, we cannot alter their contents. As an alternative, **with** and **within** may be referred to if writing df[["..."]] each time is so difficult for us (it should not be):

```
rm(list=c("mpg", "hp", "vs", "qsec"))
})
##
                    cvl disp drat
                                         am gear carb fuel_economy log_hp
                                     wt
                      6 160 3.90 2.620 yes
## Mazda RX4
                                               4
                                                    4
                                                            11.190 4.7005
## Mazda RX4 Wag
                      6 160 3.90 2.875 yes
                                               4
                                                            11.190 4.7005
## Datsun 710
                      4 108 3.85 2.320 yes
                                                            10.307 4.5326
                                               4
                                                   1
## Hornet 4 Drive
                     6 258 3.08 3.215
                                               3
                                                            10.981 4.7005
## Hornet Sportabout
                      8 360 3.15 3.440
                                               3
                                                    2
                                                            12.567 5.1648
                                         по
                      6 225 2.76 3.460
## Valiant
                                                            12.983 4.6540
                                               3
```

**Example 12.34** As mentioned in Section 10.3.4 (see Section 17.6 for more details), formulae are special objects that consist of two unevaluated expressions separated by a tilde ( $\sim$ ).

Functions can support formulae and do what they please with them, but a popular approach is to allow them to express "something grouped by something else" or "one thing as a function of other things".

```
do.call(rbind.data.frame, lapply(split(ToothGrowth, ~supp+dose), head, 1))
          len supp dose
## 0J.0.5 15.2
                OJ 0.5
## VC.0.5 4.2
                VC 0.5
## 0J.1
         19.7
              OJ 1.0
## VC.1 16.5
              VC 1.0
## OJ.2
         25.5
                OJ 2.0
## VC.2
         23.6
              VC 2.0
aggregate(cbind(mpg, log_hp=log(hp))~am:cyl, mtcars, mean)
              mpg log hp
    am cyl
## 1
         4 22.900 4.4186
## 2 1
         4 28.075 4.3709
        6 19.125 4.7447
## 3
    1 6 20.567 4.8552
## 4
## 5
    0 8 15,050 5,2553
## 6 1 8 15.400 5.6950
head(model.frame(mpg+hp\sim log(hp)+I(1/qsec), mtcars))
##
                   mpq + hp loq(hp)
                                     I(1/qsec)
## Mazda RX4
                      131.0 4.7005 0.060753....
## Mazda RX4 Wag
                      131.0 4.7005 0.058754....
## Datsun 710
                      115.8 4.5326 0.053734....
## Hornet 4 Drive
                      131.4 4.7005 0.051440....
## Hornet Sportabout
                      193.7 5.1648 0.058754....
## Valiant
                       123.1 4.6540 0.049455....
```

If these seem esoteric, it is because that is precisely the case. We need to consult the corresponding functions' manuals to understand what they do. And, as we do not recommend their use by beginner programmers, we will not explain them here.

**Exercise 12.35** In the last example, the peculiar printing of the last column is due to which method's being overloaded?

In the third part of this book, we will return to these functions as they will serve as an amusing illustration of how to implement our own procedures that rely on metaprogramming techniques.

### 12.3.10 A note on the dplyr (tidyverse) and data. table packages (\*)

The popular third-party packages **data.table** and **dplyr** implement the most common data frame wrangling procedures. Some operations may be much faster for larger datasets.

They both introduce an entirely new API for the operations we already know well how to perform. Furthermore, they are heavily based on metaprogramming (lazy evaluation). A nice way to learn them is by solving some of the exercises listed below.

**dplyr** is part of a vast system of interdependent packages called **tidyverse**, which tend to do things their own way. They became quite invasive over the last few years.

Still, R programmers ought to remember that they are *able* to do without them. What is more, they also *need* to rely on other solutions when processing other prominent data structures is required, e.g., of fancy lists and matrices. Base R always comes first as the most fundamental layer.

Important Some functions we may find helpful (annoyingly to base R users) return objects of the class tibble (tbl\_df) (e.g., haven::read.xpt that reads SAS data files). However, these are, in fact, subclasses of data.frame. We can always use as.data.frame to get our favourite objects back.

Also, we cannot stress enough that it is SQL that we recommend learning as perhaps the most powerful interface to more considerable amounts of data. It will give us the skills that can be used later in other programming environments.

Base R (and its predecessor, S) has long ago proven to be a versatile tool for rapid prototyping, calling specialised procedures written in C or Java, and wrangling data that fit into memory. For larger problems, techniques for working with batches of data, sampling methods, or aggregating data stored elsewhere are often the way to go, especially when building machine learning models or visualisation<sup>13</sup> is required. Usually, the most recent data will be stored in normalised databases, and we will need to join a few tables to fetch something interesting from the perspective of the current analysis context.

<sup>&</sup>lt;sup>13</sup> For example, drawing a scatter plot of one billion points makes little sense. It may result in unreadable images of large file sizes. They first need to be sampled or summarised somehow (e.g., binned); see Chapter 13.

#### 12.4 Exercises

**Exercise 12.36** *Answer the following questions:* 

- What attributes a data frame must be equipped with?
- If row. names is an integer vector, how to access rows labelled 1, 7, and 42?
- How to create a data frame that features a column that is a list of character vectors of different lengths?
- How to create a data frame that includes a matrix column?
- How to convert all numeric columns in a data frame to a numeric matrix?
- Assuming that x is an atomic vector, what is the difference between "as.data.frame(x)" vs "as.data.frame(as.list(x))" vs "as.data.frame(list(a=x))" vs "data.frame(a=x)"?

**Exercise 12.37** Assuming that x is a data frame, what is the meaning of/difference between the following:

- "x["u"]" vs "x[["u"]]" vs "x[, "u"]"?
- "x["u"][1]" vs "x[["u"]][1]" vs "x[1, "u"]" vs "x[1, "u", drop=FALSE]"?
- "x[which(x[[1]] > 0), ]" vs "x[x[[1]] > 0, ]"?
- "x[grep("^foo", names(x))]"?

**Exercise 12.38** Assume we have a data frame with columns named like: ID (character), checked (logical, possibly with missing values), category (factor), x0, ... x9 (ten separate numeric columns), y0, ... y9 (ten separate numeric columns), coords (numeric matrix with two columns named lat and long), and features (list of character vectors of different lengths).

- How to extract the rows where checked is TRUE?
- How to extract a subset comprised only of ID and x-something columns?
- How to extract the rows for which ID is like three letters and then five digits (e.g., XYZ12345)?
- How to select all the numeric columns in one go?
- Assuming that the IDs are like three letters and then five digits, how to add two columns: ID3 (the letters) and ID5 (the five digits)?
- How to get rid of all the columns between x3 and y7?
- How to check where both lat and long in coords are positive?
- How to add the row indicating the number of features?
- How to extract the rows where "spam" is amongst the features?
- How to convert it to a long data frame with two columns: ID and feature (individual strings)?

- How to change the name of the ID column to id?
- How to make the y-foo columns appear before the x-bar ones?
- How to order the rows with respect to checked (FALSE first, then TRUE) and IDs (decreasingly)?
- How to remove rows with duplicate IDs?
- How to determine how many entries correspond to each category?
- How to compute the average lat and long in each category?
- How to compute the average lat and long for each category and checked combined?

**Exercise 12.39** Consider the flights<sup>14</sup> dataset. Give some ways to select all rows between March and October (regardless of the year).

**Exercise 12.40** In this task, you will be working with a version of a dataset on 70k+ Melbourne trees (urban fores  $t^{15}$ ).

- 1. Load the downloaded dataset by calling the **read.csv** function.
- 2. Fetch the IDs (Com. ID) and trunk diameters (Diameter. Breast. Height) of five horse chestnuts with the smallest diameters at breast height. The output data frame must be sorted with respect to Diameter. Breast. Height, decreasingly.
- 3. Create a new data frame that gives the number of trees planted each year.
- 4. Compute the average age (in years, based on Year . Planted; using **aggregate**) of the trees of genera (each genus separately): Eucalyptus, Platanus, Ficus, Acer, and Quercus. Depict the sorted data with **barplot**.

**Exercise 12.41** (\*) Consider the historic data dumps of https://travel.stackexchange.com/available here<sup>16</sup>. Export the CSV files located therein to an SQLite database. Then, write some R code that corresponds to the following SQL queries (use **dbGetQuery** to verify your results):

```
SELECT

Users.DisplayName,
Users.Age,
Users.Location,
SUM(Posts.FavoriteCount) AS FavoriteTotal,
Posts.Title AS MostFavoriteQuestion,
MAX(Posts.FavoriteCount) AS MostFavoriteQuestionLikes
FROM Posts
JOIN Users ON Users.Id=Posts.OwnerUserId
WHERE Posts.PostTypeId=1
GROUP BY OwnerUserId

(continues on next page)
```

<sup>14</sup> https://github.com/gagolews/teaching-data/blob/master/other/flights.csv

<sup>15</sup> https://github.com/gagolews/teaching-data/raw/master/marek/urban\_forest.csv.gz

<sup>16</sup> https://github.com/gagolews/teaching-data/tree/master/travel\_stackexchange\_com\_2017

ORDER BY FavoriteTotal DESC LIMIT 10 --- 2) **SELECT** Posts. ID, Posts. Title, Posts2.PositiveAnswerCount FROM Posts JOIN ( SELECT Posts.ParentID, COUNT(\*) AS PositiveAnswerCount WHERE Posts.PostTypeID=2 AND Posts.Score>0 **GROUP BY** Posts.ParentID ) AS Posts2 ON Posts. ID=Posts2. ParentID ORDER BY Posts2. PositiveAnswerCount DESC LIMIT 10 --- 3) **SELECT** Posts. Title. UpVotesPerYear. Year, MAX(UpVotesPerYear.Count) AS Count FROM ( SELECT PostId, COUNT(\*) AS Count, STRFTIME('%Y', Votes.CreationDate) AS Year FROM Votes WHERE VoteTypeId=2 GROUP BY PostId, Year ) AS UpVotesPerYear JOIN Posts ON Posts.Id=UpVotesPerYear.PostId WHERE Posts.PostTypeId=1 GROUP BY Year --- 4) SELECT Questions. Id, Questions. Title, BestAnswers.MaxScore, Posts. Score AS AcceptedScore, BestAnswers.MaxScore-Posts.Score AS Difference FROM (

(continued from previous page)

```
SELECT Id, ParentId, MAX(Score) AS MaxScore
        FROM Posts
        WHERE PostTypeId==2
        GROUP BY ParentId
    ) AS BestAnswers
JOIN (
        SELECT * FROM Posts
        WHERE PostTypeId==1
    ) AS Questions
    ON Questions. Id=BestAnswers. ParentId
JOIN Posts ON Questions. Accepted Answer Id=Posts. Id
WHERE Difference>50
ORDER BY Difference DESC
--- 5)
SELECT
    Posts. Title.
    CmtTotScr.CommentsTotalScore
FROM (
        SELECT
            PostID,
            UserID,
            SUM(Score) AS CommentsTotalScore
        FROM Comments
        GROUP BY PostID, UserID
) AS CmtTotScr
JOIN Posts ON Posts.ID=CmtTotScr.PostID
    AND Posts.OwnerUserId=CmtTotScr.UserID
WHERE Posts.PostTypeId=1
ORDER BY CmtTotScr.CommentsTotalScore DESC
LIMIT 10
--- 6)
SELECT DISTINCT
    Users. Id.
    Users.DisplayName,
    Users.Reputation,
    Users.Age,
    Users.Location
FROM (
        SELECT
            Name, UserID
        FROM Badges
        WHERE Name IN (
            SELECT
                Name
```

```
FROM Badges
            WHERE Class=1
            GROUP BY Name
            HAVING COUNT(*) BETWEEN 2 AND 10
        AND Class=1
    ) AS ValuableBadges
JOIN Users ON ValuableBadges.UserId=Users.Id
--- 7)
SELECT
    Posts. Title,
    VotesByAge2.OldVotes
FROM Posts
JOIN (
    SELECT
        PostId,
        MAX(CASE WHEN VoteDate = 'new' THEN Total ELSE @ END) NewVotes,
        MAX(CASE WHEN VoteDate = 'old' THEN Total ELSE @ END) OldVotes,
        SUM(Total) AS Votes
    FROM (
        SELECT
            PostId,
            CASE STRFTIME('%Y', CreationDate)
                WHEN '2017' THEN 'new'
                WHEN '2016' THEN 'new'
                ELSE 'old'
                END VoteDate,
            COUNT(*) AS Total
        FROM Votes
        WHERE VoteTypeId=2
        GROUP BY PostId, VoteDate
    ) AS VotesByAge
    GROUP BY VotesByAge.PostId
    HAVING NewVotes=0
) AS VotesByAge2 ON VotesByAge2.PostId=Posts.ID
WHERE Posts.PostTypeId=1
ORDER BY VotesByAge2.OldVotes DESC
LIMIT 10
```

**Exercise 12.42** (\*) Generate a CSV file featuring some random data arranged in a few columns of a size at least two times larger than your available RAM. Then, export the CSV file to an SQLite database. Use file connections (Section 8.3.5) and the nrow argument to **read.table** to be able to process it on a chunk-by-chunk basis.

Determine whether setting colclasses in **read. table** speeds up the reading of large CSV files significantly or not.

**Exercise 12.43** (\*) Export the whole XML data dump of StackOverflow<sup>17</sup> published at https://archive.org/details/stackexchange (see also https://data.stackexchange.com/) to an SQLite database.

<sup>17</sup> https://stackoverflow.com

# Graphics

The R Project homepage advertises our free software as an *environment for statistical computing and graphics*. Hence, had we not dealt with the latter use case, our course would have been incomplete.

R is nowadays equipped with the two following independent (incompatible, yet coexisting) systems for graphics generation; see Figure 13.1.

- 1. The (historically) newer one, **grid** (e.g., [44]), is very flexible but might seem quite complicated. Some readers might have come across the **lattice** [49] and **ggplot2** [54, 57] packages before. They are built on top of **grid**.
- 2. On the other hand, its traditional (S-style) counterpart, *base* **graphics** (e.g., [7]), is much easier to master. It still gives their users complete control over drawing processes. It is simple, fast, and minimalist, which makes it very attractive from the perspective of this course's philosophy.

This is why we only cover the second system here.

**Note** All figures in this book were generated using **graphics** and its dependants. They are sufficiently aesthetic, aren't they? Form precedes essence.

# 13.1 Graphics primitives

In **graphics**, we do not choose from a superfluity of virtual objects to be placed on an abstract canvas, letting some algorithm decide how and when to delineate them. We *just draw*. To do so, we call functions that plot the following *graphics primitives* (see, e.g., [35, 41]):

- plotting symbols (e.g., pixels, circles, stars) of different shapes and colours,
- line segments of different styles (e.g., solid, dashed, dotted),
- polygons (optionally filled),
- text (using available fonts),
- raster images (bitmaps; if the output device supports it).

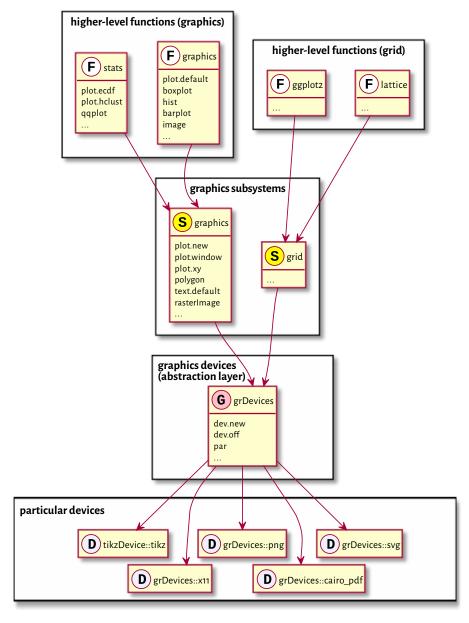


Figure 13.1: Relation between the graphics subsystems

That's it. It will turn out that *all* other shapes (smooth curves, circles) might be easily approximated using the above.

**Example 13.1** Figure 13.2 depicts some graphics primitives, which we plotted using the following program. We will detail the meaning of all the functions in the next sections.

```
par(mar=rep(0.5, 4)) # small plot margins (bottom, left, top, right)
plot.new() # start a new plot
plot.window(c(0, 6), c(0, 2), asp=1) # x range: 0-6, y: 0-2; proportional
x \leftarrow c(0, 0, NA, 1, 2, 3, 4, 4, 5, 6)
y < -c(0, 2, NA, 2, 1, 2, 2, 1, 0.25, 0)
points(x[-(1:6)], y[-(1:6)]) # symbols
lines(x, y) # line segments
text(c(0, 6), c(0, 2), c("(0, 0)", "(6, 2)"), col="red") # two text labels
rasterImage(
    matrix(c(1, 0, # 2x3 pixel "image"; 0=black, 1=red
             0, 1,
             0, 0), byrow=TRUE, ncol=2),
    5, 0.5, 6, 2, # position: xleft, ybottom, xright, ytop
    interpolate=FALSE
polygon(
    c(4, 5, 5.5,
                  4), # x coordinates of the vertices
    c(0, 0, 1, 0.75), # y coordinates
    lty="dotted", # border style
    col="#ffff0044" # fill colour: semi-transparent yellow
)
```

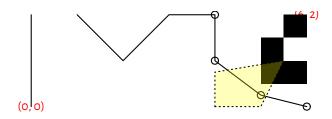


Figure 13.2: Graphics primitives: plotting symbols, line segments, polygons, text labels, and bitmaps; Objects are added one after another, with newer ones drawn over the already existing shapes

**Important** In **graphics**, most of the function calls have immediate effects. Objects are drawn on the active plot one by one, and their state cannot be modified later.

Of course, in practice, we do not always have to be so low-level. There are many builtin functions that implement the most popular chart types: histograms, bar plots, dendrograms, etc. They are expected to suit our basic needs. We will review them in Section 13.3.

The more basic routines we discuss next will still be of service for fine-tuning our figures and adding further details. But, if the prefabricated components are not what we are after, we will be able to create any drawing from scratch.

### 13.1.1 Symbols (points)

The **points** function can draw a series of plotting symbols (by default, circles) on the two-dimensional plot region relative to the user coordinate system.

We specify the points' coordinates using the x and y arguments (two vectors of equal lengths; no recycling). Alternatively, we may give a matrix or a data frame with two columns: its first column (regardless of how and if it is named) defines the abscissae, and the second column determines the ordinates.

This function allows each point to be plotted differently if this is what we desire. Thus, it is ideal for drawing scatter plots, possibly for grouped data (see Figure 13.17 below). It is vectorised with respect to, amongst others, the col (colour; see Section 13.2.1), cex (scale, defaults to 1), and pch (plotting character or symbol, defaults to 1, i.e., a circle) arguments.

**Example 13.2** Figure 13.3 gives an overview of the plotting symbols available. The most often used ones are:

- NA\_integer\_ no symbol,
- 0, ..., 14 and 15, ..., 18 unfilled and filled symbols, respectively;
- 19, ..., 25 filled symbols with a border of width Lwd; for codes 21–25, the fill colour is controlled separately by the bg parameter,
- ". " a tiny point (a "pixel"),
- "a", "1", etc. a single character (not all Unicode characters are available); strings longer than one will be truncated.

|          | 0        | Δ  | +  | ×  | $\Diamond$ | $\nabla$ |          | *        |
|----------|----------|----|----|----|------------|----------|----------|----------|
| 0        | 1        | 2  | 3  | 4  | 5          | 6        | 7        | 8        |
| $\Phi$   | <b>⊕</b> | ΧX | Ħ  | 8  |            |          | •        | <b>A</b> |
| 9        | 10       | 11 | 12 | 13 | 14         | 15       | 16       | 17       |
| <b>♦</b> | •        | •  | 0  |    | <b>\Q</b>  | Δ        | $\nabla$ |          |
| 18       | 19       | 20 | 21 | 22 | 23         | 24       | 25       | 26       |
| Α        | В        | a  | Ь  | S  | *          | !        |          |          |

Figure 13.3: Plotting characters and symbols (pch)

#### 13.1.2 Line segments

**lines** can be used to draw connected line segments whose mid- and endpoints are given in a similar manner as in the **points** function. A series of segments can be interrupted by defining an endpoint whose coordinate is a missing value; compare Figure 13.2.

Actually, **points** and **lines** are wrappers around the same function, **plot.xy**, which we usually do not call directly. Their type arguments determine the object to draw; the only difference is that the former uses type="p" whilst the latter relies on type="l" by default. Changing these to type="b" (both) or type="o" (overplot) will give their combination. Moreover, type="s" and type="S" results in step functions (with post- and pre-increments, respectively), and type="h" draws bar plot-like vertical lines. See Figure 13.4 for an illustration (implement something similar yourself as an exercise).

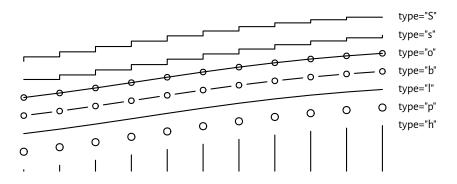


Figure 13.4: Different type argument settings in **lines** or **points** 

The col argument controls the line colour (see Section 13.2.1), and lwd determines the line width (1 by default). Six named line types (lty) are available, which can also be specified via their respective numeric identifiers, lty=1, ..., lty=6; see Figure 13.5 (implementing a similar plot is left as an exercise). Additionally, custom dashes can be defined using strings of up to 8 (hexadecimal) digits. Consecutive digits give the lengths of the dashes and blanks. For instance, lty="1343" yields a dash of length 1,

followed by a space of length 3, then a segment of length 4, followed by a blank of length 3. The whole sequence will be recycled for as long as necessary.

Figure 13.5: Line types (lty)

**Example 13.3 lines** can be used for plotting empirical cumulative distribution functions (we will suggest it as an exercise later), regression models (e.g., lines, splines of different degrees), time series, and any other mathematical functions, even when they are smooth and curvy. The naked eye cannot tell the difference between a densely sampled piecewise linear approximation of an object and its original version.

The code below illustrates this (sad for the high-hearted idealists) truth using the sine function; see Figure 13.6.

```
ns <- c(seq(3, 25, by=2), 50, 100)
par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, length(ns)*pi), c(-1, 1))
for (i in seq_along(ns)) {
    x <- seq((i-1)*pi, i*pi, length.out=ns[i])
    lines(x, sin(x))
    text((i-0.5)*pi, 0, ns[i], cex=0.89)
}</pre>
```



Figure 13.6: Sampling more densely gives the illusion of smoothness

**Exercise 13.4** Implement your version of the **segments** function using a call to **lines**.

**Exercise 13.5** (\*) Implement a simplified version of the **arrows** function, where the length of edges of the arrowhead is given in user coordinates (and not inches; you will be equipped with skills to achieve this later; see Section 13.2.5). Use the ljoin and lend arguments (see **help**("par") for admissible values) to change the line end and join styles (from the default rounded caps).

### 13.1.3 Polygons

**polygon** draws a polygon with a border of specified colour and line type (border, lty, lwd). If the col argument is not missing, the polygon is filled (or hatched; cf. the density and angle arguments).

**Example 13.6** To demo the above function, let us draw a few regular (equilateral and equiangular) polygons; see Figure 13.7. By increasing the number of sides, we can obtain an approximation to a circle.

```
regular_poly <- function(x0, y0, r, n=101, ...)
{
    theta <- seq(0, 2*pi, length.out=n+1)[-1]
    polygon(x0+r*cos(theta), y0+r*sin(theta), ...)
}

par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, 9.5), c(-1, 1), asp=1)
    regular_poly(1, 0, 1, n=3)
    regular_poly(3.5, 0, 1, n=7, density=15, angle=45, col="tan", border="red")
    regular_poly(6, 0, 1, n=10, density=8, angle=-60, lty=3, lwd=2)
    regular_poly(8.5, 0, 1, n=100, border="brown", col="lightyellow")
```

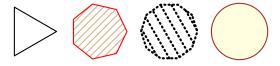


Figure 13.7: Regular polygons drawn using polygon

Note the asp=1 argument to the **plot.window** function (which we detail below) that guarantees the same scaling of the x- and y-axes. This way, the circle looks like one and not an oval.

Notice that the last vertex adjoins the first one. Also, if we are absent-minded (or particularly creative), we can produce self-intersecting or otherwise degenerate shapes.

**Exercise 13.7** *Implement your version of the rect function using a call to polygon.* 

#### 13.1.4 Text

A call to **text**, draws arbitrary strings (newlines and tabs are allowed) centred at the specified points. Moreover, by setting the pos argument, the labels may be placed below, to the left of, etc., the pivots. Some further position adjustments are also possible (adj, offset); see Figure 13.8.

col specifies the colour, cex affects the size, and srt changes the rotation of the text.

On many default graphics devices, we have little control over the font face used: font family can be chosen using family ("sans", "serif", "mono"), and font can be used to



Figure 13.8: The positioning of text with **text** (the plotting symbols were added for reference)

select the normal variant (1), bold (2), italic (3), or bold italic (4). See, however, Section 13.2.7 for some workarounds.

**Note** (\*) There is some limited support for basic mathematical symbols and formulae. It relies on some quirky syntax that we enter using unevaluated R expressions (Chapter 15). Still, it should be enough to meet our most basic needs. For instance, passing "quote(beta[i]^j)" as the labels argument to text, will output " $\beta_i^j$ ". See help("plotmath") for more details.

For more sophisticated mathematical typesetting, see the **tikzDevice** graphics device mentioned in Section 13.2.7. It outputs plot specifications that can be rendered by the LaTeX typesetting system.

## 13.1.5 Raster images (bitmaps) (\*)

Most output devices support drawing raster images encoded in the form of bitmaps, i.e., matrices whose elements represent pixels (see Figure 13.2 for an example).

Raster images are helpful for drawing heat maps or backgrounds of contour plots; see Section 13.3.4.

**Example 13.8** Optionally, bilinear interpolation can be applied if the drawing area is larger than the bitmap size, and we would like to smoothen the colour transitions out. Figure 13.9 presents a very stretched  $4 \times 3$  pixel image, with and without interpolation.



Figure 13.9: Example bitmaps drawn with rasterImage: with (left) and without (right) colour interpolation

### 13.2 Graphics settings

**par** can be used to query and modify (as long as they are not read-only) many graphics settings.

For instance, we have several parameters related to the current page or device settings, e.g., the plot's margins (see Section 13.2.2) or user coordinates (see Section 13.2.3).

Moreover, values of some of the parameters set via **par** may be taken by a few functions<sup>1</sup> as settings to use by default. This is the case of, e.g., col, pch, lty in the **points** and **lines** function.

**Exercise 13.9** Study the following (pseudo)code.

```
lines(x, y) # use the default `lty`, i.e., par("lty") == "solid"

old_settings <- par(lty="dashed") # change setting, save old for reference
lines(x, y) # use the default `lty`, i.e., par("lty") == "dashed"
lines(x, y, lty=3) # use the given `lty`
lines(x, y) # lty="dashed"
par(old_settings) # restore previous settings
lines(x, y) # lty="solid"</pre>
```

The reference list of available parameters is given in **help**("par"). Below we discuss the most noteworthy ones.

#### 13.2.1 Colours

Many functions allow specifying colours of the plotted objects or their parts; compare, e.g., col and border arguments to **polygon**, or col and bg to **points**.

There are a few ways to specify colours (see the *Colour Specification* section in **help**("par") for more details).

• A "colour name" string, being one of the 657 predefined tags known to the **colours** function:

<sup>&</sup>lt;sup>1</sup> Unfortunately, it is not as straightforward as that. For instance, **polygon** is unaffected by the col setting, **axis** uses col.axis instead, etc. We should always consult the documentation.

• An "#rrggbb" string, specifying a position in the RGB<sup>2</sup> colour space; three series of hexadecimal numbers of two digits each, i.e., between  $oo_{hex} = 0$  (off) and  $FF_{hex} = 255$  (full on), giving the intensity of the red, green, and blue channels<sup>3</sup>.

In practice, the **col2rgb** and **rgb** functions can be used to convert between the decimal and hexadecimal representations:

```
C <- c("black", "red", "green", "blue", "cyan", "magenta",</pre>
    "yellow", "grey", "lightgrey", "pink") # example colours
(Cmat <- structure(col2rgb(C), dimnames=list(c("R", "G", "B"), C)))</pre>
    black red green blue cyan magenta yellow grey lightgrey pink
                                                          211 255
## R
         0 255
                   0
                        0
                             0
                                   255
                                          255 190
## G
                 255
                          255
                                          255 190
                                                          211 192
                   0 255 255
                                   255
                                            0 190
## B
                                                          211 203
structure(rgb(Cmat[1, ], Cmat[2, ], Cmat[3, ], maxColorValue=255),
    names=C)
##
       black
                   red
                           green
                                      blue
                                                cyan
                                                       magenta
                                                                   vellow
## "#000000" "#FF0000" "#00FF00" "#000FF" "#00FFFF" "#FF00FF" "#FFF00"
        grey lightgrey
                            pink
## "#BEBEBE" "#D3D3D3" "#FFC0CB"
```

• An "#rrggbbaa" string, like above, but with the added alpha channel (two additional hexadecimal digits): from  $oo_{hex} = 0$  denoting fully transparent, to  $FF_{hex} = 255$  indicating fully visible ("lit") colour; see Figure 13.2 for an example.

Semi-transparency (translucency) can significantly enhance the expressivity of our data visualisations; see Figure 13.18 and Figure 13.19.

• An integer index, selecting an item from the *current palette* (with recycling), which we can get or set by a call to **palette**. Moreover, 0 identifies the background colour, **par**("bg").

Integer colour specifiers are particularly valuable when plotting data in groups, as defined by factors. The underlying integer level codes can be mapped to consecutive colours from any palette; see Figure 13.17 below for an example.

**Example 13.10** We recommend memorising the colours in the default palette:

<sup>&</sup>lt;sup>2</sup> https://en.wikipedia.org/wiki/RGB\_color\_model

<sup>&</sup>lt;sup>3</sup> From school, we probably know the *subtractive* CMY (cyan, magenta, yellow) model, where we obtain, e.g., a green colour by using blue-ish and yellow crayons (subtracting certain wavelengths from white light). The RGB model, on the other hand, corresponds to the three photoreceptor/cone cells in the retinas of the human eyes. Nonetheless, it is *additive* and, therefore, less intuitive: total darkness emerges when we emit no light, yellow emerges when mixing red and green beams, etc.

```
palette() # default palette
## [1] "#000000F0" "#DF536BF0" "#61D04FF0" "#2297E6F0" "#28E2E5F0"
## [6] "#CD0BBCF0" "#F5C710F0" "#999999F0"
```

These are<sup>4</sup>, in order: black, red, green, blue, cyan, magenta, yellow, and grey; see<sup>5</sup> Figure 13.10 for an illustration.

```
k \leftarrow length(palette())

par(mar=rep(0.5, 4)); plot.new(); plot.window(c(0, k+1), c(0, 1))

points(1:k, rep(0.5, k), col=1:k, pch=16, cex=3)

text(1:k, 0.5, palette(), pos=rep(c(1, 3), length.out=k), col=1:k, offset=1)

text(1:k, 0.5, 1:k, pos=rep(c(3, 1), length.out=k), col=1:k, offset=1)
```



Figure 13.10: The default colour palette

Choosing usable colours requires some talents that most programmers lack. Therefore, we will find ourselves relying on the built-in colour sets. palette.pals and hcl. pals return the names of the available *discrete* (qualitative) palettes. Then, palette. colors and hcl.colors (note the American spelling) can generate a given number of colours from a particular named set.

Continuous (quantitative) palettes are also available, see rainbow, heat.colors, terrain. colors, topo.colors, cm.colors, and gray.colors. They transition smoothly between some predefined pivot colours, e.g., from blue through green to brown (like in a topographic map with elevation colouring). They may be of use, e.g., when drawing contour plots; compare Figure 13.27.

**Exercise 13.11** Create a demo of the aforementioned built-in palettes in a similar (or nicer) style to that in Figure 13.11.

## 13.2.2 Plot margins and clipping regions

A device (page) region represents a single plot window, one raster image file, or a page in a PDF document (see Section 13.2.7 for more information on graphics devices). As we will learn from Section 13.2.6, it is capable of holding many figures.

<sup>&</sup>lt;sup>4</sup> Actually, red-ish, green-ish, etc. The choice is more aesthetic than when pure red, green, etc. was used (before R 4.0.0). It is also expected to be more friendly to people who have some colour vision deficiencies (roughly every 1 in 12 men (8%) and 1 in 200 women (0.5%), especially in the red-green or blue-yellow spectrum; see [46] for more details).

<sup>&</sup>lt;sup>5</sup> The readers of the printed version of this book should know that its online version displays this figure (and all others) in full colour. See you there.

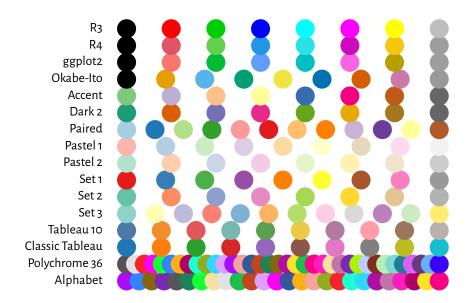


Figure 13.11: Qualitative colour palettes in **palette.pals**; R4 is the default one, as seen in Figure 13.10

Usually, however, we draw *one figure per page*. In such a case, the device region is divided into the following parts:

- 1) *outer margins*, which can be set using, e.g., the oma graphics parameter (in text lines, based on the height of the default font); by default, they equal to 0;
- 2) figure region:
  - a) inner (plot) margins, by default mar=c(5.1, 4.1, 4.1, 2.1) text lines (bottom, left, top, right, respectively); this is where we usually emplace the figure title, axes labels, etc.
  - b) plot region, where we draw graphics primitives positioned relative to the user coordinates.

**Note** Typically, all drawings are *clipped* to the plot region, but this can be changed with the xpd parameter; see also the **clip** function that allows clipping to an arbitrary rectangle.

**Example 13.12** Figure 13.12 shows the default page layout. In the code chunk below, note the use of mtext to print a text line in the inner margins, box to draw a rectangle around the plot or figure region, axis to add the two axes (labels and tick marks), and title to add some descriptive labels.

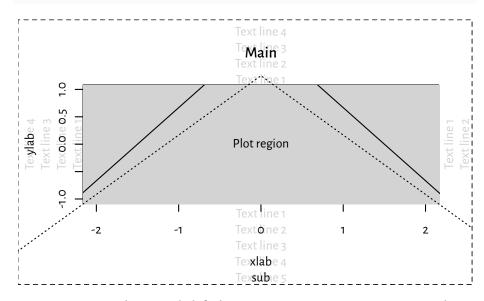


Figure 13.12: Figure layout with default inner (mar=c(5.1, 4.1, 4.1, 2.1)) text lines) and outer (ma=c(0, 0, 0, 0)) margins; We see that a lot of space is wasted and hence some tweaking might be necessary to suit our needs better; Note the clipping of the solid line to the plot region

#### 13.2.3 User coordinates

**plot.window** can be used to set the user coordinates. It accepts the following parameters:

• xlim, ylim – vectors of length two giving the minimal and maximal ranges on the

respective axes; by default, they are extended by 4% in each direction (for aesthetic reasons; see, e.g., Figure 13.12), but see the xaxs and yaxs graphics parameters;

- asp aspect ratio (y/x); defaults to NA, i.e., no adjustment; use asp=1 for circles to look like ones, and not ovals;
- log switches logarithmic scaling on particular axes: "" (none; default), "x", "y", or "xy".

**Example 13.13** The graphics parameter us r can be used to read (and set) the extremes of the user coordinates in the form  $(x_1, x_2, y_1, y_2)$ .

```
plot.new()
plot.window(c(-1, 1), c(1, 1000), log="y", yaxs="i")
par("usr")
## [1] -1.08   1.08   0.00   3.00
```

Indeed, the x-axis range was extended by 4% in each direction. We have turned this behaviour off for the y-axis, which uses the base-10 logarithmic scale. In this case, its actual range is  $10^{\text{par}("usr")[3:4]}$ , because  $\log_{10} 1 = 0$  and  $\log_{10} 1000 = 3$ .

**Exercise 13.14** Implement your version of the abline function.

#### 13.2.4 Axes

Even though axes (labels and tick marks) can be drawn manually using the aforementioned graphics primitives, it is usually too tedious a work.

This is why we tend to rely on the axis function, which draws the object on one of the plot sides (as usual, 1=bottom, ..., 4=right).

Once **plot.window** is called, **axTicks** can be called to guesstimate some tasteful (*round*) locations for the tick marks based on the current plot size. By default, they are based on the xaxp and yaxp graphics parameters, which give the axis ranges and the number of intervals between the tick marks.

```
plot.new(); plot.window(c(-0.9, 1.05), c(1, 11))
par("usr") # (x1, x2, y1, y2)
## [1] -0.978 1.128 0.600 11.400
par("yaxp") # (y1, y2, n)
## [1] 2 10 4
axTicks(2) # left y-axis
## [1] 2 4 6 8 10
par("xaxp") # (x1, x2, n)
## [1] -0.5 1.0 3.0
axTicks(1) # bottom x-axis
## [1] -0.5 0.0 0.5 1.0
par(xaxp=c(-0.9, 1.0, 5)) # change
```

(continues on next page)

```
axTicks(1)
## [1] -0.90 -0.52 -0.14 0.24 0.62 1.00
```

**axis** relies on the same algorithm as **axTicks**. Alternatively, we can provide our own tick locations and labels.

**Example 13.15** Most of the plots in this book use the following graphics settings (except las=1 to axis(2)); see Figure 13.13. Check out help("par"), help("axis"), etc. and tune them up to suit your needs.

```
par(mar=c(2.2, 2.2, 1.2, 0.6))
par(tcl=0.25) # the length of the tick marks (fraction of text line height)
par(mgp=c(1.1, 0.2, 0)) # axis title, axis labels, and axis line location
par(cex.main=1, font.main=2) # bold, normal size - main in title
par(cex.axis=0.8889)
par(cex.lab=1, font.lab=3) # bold italic, normal size
plot.new(); plot.window(c(0, 1), c(0, 1))
# a "grid":
rect(par("usr")[1], par("usr")[3], par("usr")[2], par("usr")[4],
    col="#00000010")
abline(v=axTicks(2), col="white", lwd=1.5, lty=1)
abline(h=seq(0, 1, length.out=4), col="white", lwd=1.5, lty=1)
# set up axes:
axis(2, at=seq(0, 1, length.out=4), c("0", "1/3", "2/3", "1"), las=1)
axis(1)
title(xlab="xlab", ylab="ylab")
box()
```

## 13.2.5 Plot dimensions (\*)

Certain sizes can be read or specified in inches (1 inch (1") is exactly 25.4 mm):

- pin plot dimensions (width, height),
- fin figure region dimensions,
- din page (device) dimensions,
- mai plot (inner) margin size,
- omi outer margins,
- cin the size of the "default" character (width, height).

If the figure is scaled, the *virtual* inch (the one reported by R) will not match the physical one (e.g., the actual size in the printed version of this book or on the computer screen).

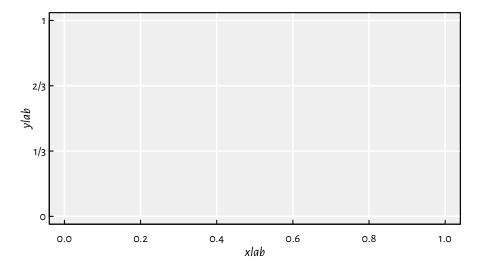


Figure 13.13: Custom axes and other settings

usr. They are automatically mapped to the *physical* device region, taking into account the page size, outer and inner margins, etc.

Knowing the above, some basic scaling can be used to convert between the user and physical sizes (in inches). It is based on the ratios (usr[2]-usr[1])/pin[1] and (usr[4]-usr[3])/pin[2]; compare the **xinch** and **yinch** functions.

**Example 13.16** (\*) Figure 13.14 shows how we can pinpoint the edges of the figure and device region in user coordinates.

**Exercise 13.17** (\*) We cannot use **mtext** to print text on the right inner margin rotated by 180 degrees compared to what we see in Figure 13.12. Write your version of this function that will allow you to do so. Hint: use **text**, the cin graphics parameter, and what you can read from Figure 13.14.

## 13.2.6 Many figures on one page (subplots)

It is possible to create many figures on one page. In such a case, each of them has its own inner margins and a plot region.

A call to par(mfrow=c(nr, nc)) or par(mfcol=c(nr, nc)) splits the page into a regular grid with nr rows and nc columns. Each invocation of plot.new starts a new figure. Consecutive figures are either placed in a rowwise manner (mfrow) or the columnwise one (mfcol). Alternatively, the mfg parameter can be used to enforce a custom order.

**Example 13.18** Figure 13.15 depicts an example page with four figures aligned on a  $2 \times 2$  grid.

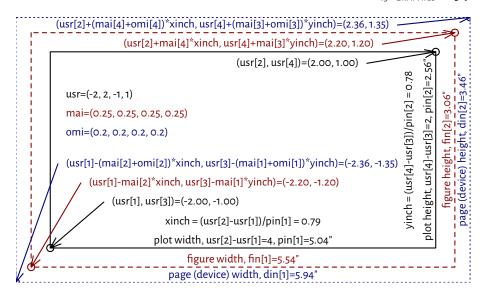


Figure 13.14: User vs device coordinates

```
par(oma=rep(1.2, 4)) # outer margins (default 0)
par(mfrow=c(2, 2)) # a 2x2 plot grid
for (i in 1:4) {
    plot.new()
    par(mar=c(3, 3, 2, 2)) # each plot can have different inner margins
    plot.window(c(i-1, i+1), c(-1, 1)) # separate user coordinates for each
    text(i, 0, sprintf("Plot region (plot %d)\n(%d, %d)", i,
        par("mfg")[1], par("mfg")[2]))
    box("figure", lty="dashed") # a box around the figure region
    box("plot") # a box around the plot region
    axis(1) # horizontal axis (bottom)
    axis(2) # vertical axis (left)
}
box("outer", lty="dotdash") # a box around the whole page
for (i in 1:4)
    mtext(sprintf("Outer margin %d", i), side=i, outer=TRUE)
```

Thanks to mfrow and mfcol, we can create a scatter plot matrix or different trellis plots. If a non-regular grid is required, we can call the slightly more sophisticated **layout** function (which is incompatible with mfrow and mfcol). Examples will follow later; see Figure 13.26 and Figure 13.24.

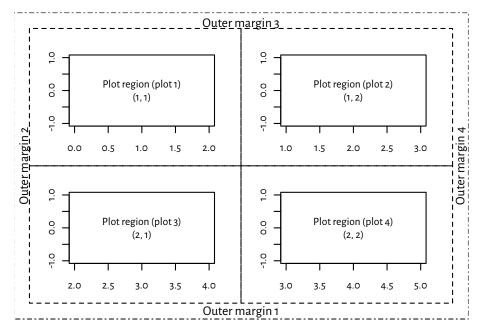


Figure 13.15: A page with four figures created using par(mfrow=c(2, 2))

Certain grid sizes might affect the mex and cex parameters and hence the default font sizes (amongst others). Refer to the documentation of par for more details.

## 13.2.7 Graphics devices

Where our plots are displayed depends on our development environment (Section 1.2). Users of JupyterLab see the plots embedded into the current notebook, consumers of RStudio display them in a dedicated Plots pane, working from the console opens a new graphics window (unless we work in a text-only environment), whereas compiling utils::Sweave or knitr markup files results in an image included in the output document.

In practice, we might be interested in exercising our creative endeavours on different devices. For instance:

```
cairo_pdf("figure.pdf", width=6, height=3.5) # open "device"
# ... calls to plotting functions...
dev.off() # save file, close device
```

This draws something in a PDF file. Similarly, a call to png or svg would create a PNG or a SVG file. In both cases, as we rely on the Cairo library, we can customise the font family by calling Cairo::CairoFonts.

uses a lossy compression method. Therefore, it is not a particularly fortunate file format for data visualisations. It does not support transparency either.

PDF is a popular choice in printed publications (e.g., articles or books).

It is worth knowing that PNG and JPEG are raster graphics formats, i.e., they store figures as bitmaps (pixel matrices). They are fast to render, but the file sizes might become immense if we want decent image quality (high resolution). Most importantly, they should not be scaled: it is best to display them at their original widths and heights.

On the other hand, SVG and PDF files store vector graphics, i.e., all primitives are described geometrically. This way, the image can be redrawn at any size and is always expected to be aesthetic. Unfortunately, scatter plots featuring millions of points will result in considerable files size and relatively slow rendition times (but there are tricks to remedy this).

Users of TeX might be interested in **tikzDevice::tikz**, which creates TikZ files that can be compiled in the form of standalone PDF files or embedded in LaTeX documents (and its variants). This allows typesetting beautiful equations using the standard "\$...\$," syntax within any R string.

A list of many built-in devices is available in help("Devices").

**Note** (\*) The opened graphics devices form a stack; calling **dev.off** will return to the last opened device (if any). See **dev.list** and other functions listed in its help page for more information.

Each device has its own graphics parameters. When opening a new device, we start with default settings in place.

Also, dev.hold and dev.flush can be used to suppress the immediate display of the plotted objects, which might increase the drawing speed on certain devices.

The current plot can be copied to another device (e.g., a PDF file) using dev.print.

**Exercise 13.19** (\*) Create an animated PNG displaying a large point sliding along the sine curve. Generate a series of video frames like in Figure 13.16. Store each frame in a separate PNG file. Then, use **ImageMagick**<sup>6</sup> (compare Section 7.3.3; or rely on some other tool) to combine these files as a single animated PNG.

## 13.3 Higher-level functions

Higher-level plotting commands call plot.new, plot.window, axis, box, title, etc., and draw many graphics primitives on behalf of the user. They provide ready-to-use im-

<sup>6</sup> https://imagemagick.org/

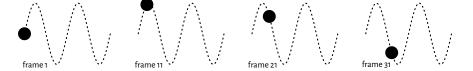


Figure 13.16: Selected frames of an example animation: they can be stored in separate files and then be combined into a single animated PNG

plementations of the most common data visualisation tools, e.g., box-and-whisker plots, histograms, pairs plots, etc.

Below we review some of them. We also show how they can be customised or even rewritten from scratch if we are not completely happy with them. They will inspire us to practice some lower-level graphics programming.

**Exercise 13.20** Check out the meaning of the ask, new, xaxt, yaxt, and ann graphics parameters and how they affect plot.new, axis, title, and so forth.

### 13.3.1 Scatter- and function plots with plot. default and matplot

The default method for the **plot** S3 generic is a convenient wrapper around **points** and **lines**.

**Example 13.21 plot** can be used to draw a scatter plot of two numeric variables, possibly grouped by another categorical variable. From Section 10.3.2 we know that a factor is represented as a vector of small natural numbers. Therefore, its underlying level codes can be used directly as col or pch specifiers; see Figure 13.17 for a demonstration. Take note of a call to the **legend** function.

```
plot(
    jitter(iris[["Sepal.Length"]]), # x (it is a numeric vector)
    jitter(iris[["Petal.Width"]]), # y (it is a numeric vector)
    col=as.numeric(iris[["Species"]]), # colours (integer codes)
    pch=as.numeric(iris[["Species"]]), # plotting symbols (integer codes)
    xlab="Sepal length",
    ylab="Petal width",
    asp=1 # y/x aspect ratio
)
legend(
    "bottomright",
    legend=levels(iris[["Species"]]),
    col=seq_along(levels(iris[["Species"]])),
    pch=seq_along(levels(iris[["Species"]])),
    bq="white"
)
```

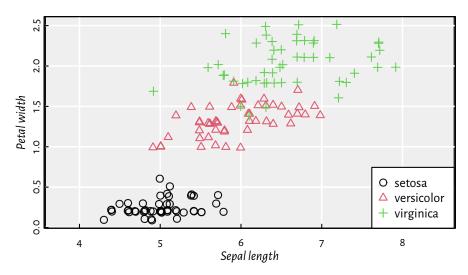


Figure 13.17: as.numeric on factors can be used to define different plotting styles for each factor level

**Exercise 13.22** Pass ann=FALSE and axes=FALSE to **plot** to suppress the addition of axes and labels. Then, draw them manually using the functions discussed in the previous section.

**Exercise 13.23** Draw a plot of the  $y = \sin x$  function using a call to **plot**. Then, call **lines** to depict  $y = \cos x$ . Add a legend. Later, do the same using a single call to **matplot**.

**Example 13.24** Semi-transparency may convey additional information. Figure 13.18 shows two scatter plots of adult females' weight vs height. If the points are fully opaque, we cannot judge the density around them. On the other hand, translucent symbols somewhat imitate the two-dimensional histograms that we depict later in Figure 13.29.

**Example 13.25** Figure 13.19 depicts the average monthly temperatures in Warsaw, Poland (a time series). Note that the translucent ribbon representing the low-high average temperature intervals was added using a call to *polygon*.

```
# Warsaw monthly temperatures, source: https://en.wikipedia.org/wiki/Warsaw high <- c( 0.6, 1.9, 6.6, 13.6, 19.5, 21.9, (continues on next page)
```

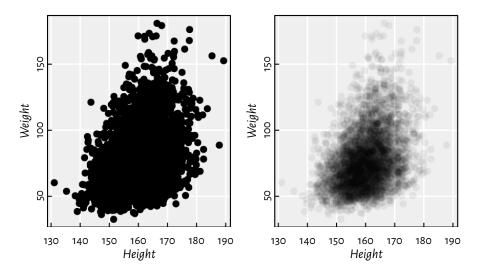


Figure 13.18: Semi-transparent symbols can give the idea of the points' distribution density

(continued from previous page)

**Example 13.26** Figure 13.20 depicts a scatter plot similar to Figure 13.18, but now with the points' hue being a function of a third variable.

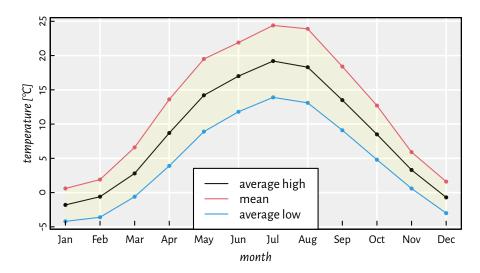


Figure 13.19: A semi-transparent ribbon was added by calling **polygon** to highlight the area between the low-high ranges (intervals)

(continued from previous page)

```
pch=16, xlab="Height", ylab="Weight")
par(mar=c(2.2, 0.6, 2.2, 0.6))
plot.new(); plot.window(c(0, 1), c(0, nlevels(zf)))
rasterImage(as.matrix(rev(col)), 0, 0, 1, nlevels(zf), interpolate=FALSE)
text(0.5, 1:nlevels(zf)-0.5, sprintf("%3.0f", midpoints(breaks)))
mtext("Waist 0", side=3)
```

**Exercise 13.27** Implement your version of the function to draw a scatter plot matrix (a pairs plot), pairs.

**Exercise 13.28 ecdf** returns an object of S3 classes  $\mathbf{c}(\text{"ecdf"}, \text{"stepfun"})$ . There are  $\mathbf{plot}$  methods overloaded for these classes. Inspect their source code. Then, inspired by this, create your own function to compute and display the empirical cumulative distribution function corresponding to a given numeric vector.

**Exercise 13.29 spline** performs cubic spline interpolation, whereas **smooth.spline** determines a smoothing spline of a given two-dimensional dataset. Plot different splines for cars[["dist"]] as a function of cars[["speed"]]. Which of these two functions is more appropriate for depicting this dataset?

# 13.3.2 Bar plots and histograms

A bar plot is drawn using a series of rectangles (i.e., some polygons) of different heights (or widths, if we request horizontal alignment).

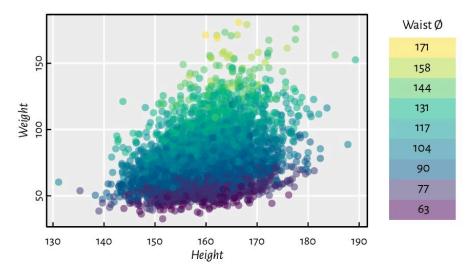


Figure 13.20: A 2D scatter plot with a third variable represented by colours

**Example 13.30** Let us visualise the dataset<sup>7</sup> listing the most frequent causes of medication errors (data are fabricated):

```
cat_med = c(
    "Unauthorised drug", "Wrong IV rate", "Wrong patient", "Dose missed",
    "Underdose", "Wrong calculation", "Wrong route", "Wrong drug",
    "Wrong time", "Technique error", "Duplicated drugs", "Overdose"
)
counts_med = c(1, 4, 53, 92, 7, 16, 27, 76, 83, 3, 9, 59)
```

A Pareto chart combines a bar plot with bars of decreasing heights with a cumulative percentage curve; see Figure 13.21. Note that **barplot** returns the midpoints of the bars and that the function sets the xaxs graphics parameter and thus does not extend the x-axis range by 4% on both sides (which does not make us happy here).

\_\_\_\_\_

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<sup>&</sup>lt;sup>7</sup> https://www.cec.health.nsw.gov.au/CEC-Academy/quality-improvement-tools/pareto-charts

(continued from previous page)

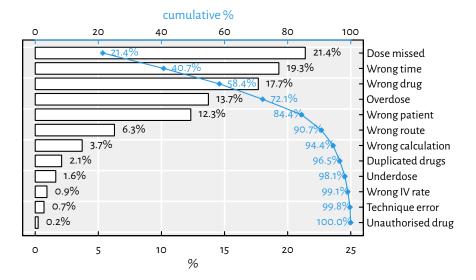


Figure 13.21: An example Pareto chart (a fancy bar plot); double axes have a general tendency to confuse the reader

**Exercise 13.31** Draw a bar plot summarising, for each passenger Class and Sex, the number of adults who did not survive the sinking of the deadliest 1912 cruise; see Figure 13.22 and the built-in Titanic dataset.

**Exercise 13.32** Implement your version of **barplot**, but where the bars are placed precisely at the positions specified by the user, e.g., allowing the bar midpoints to be consecutive integers.

We will definitely not cover the (in)famous pie charts in our book. The human brain is not very skilled at judging the relative differences between the areas of geometric objects.

Moving on: a histogram is a simple density estimator for continuous data. It can be thought of as a bar plot with bars of heights proportional to the number of observa-

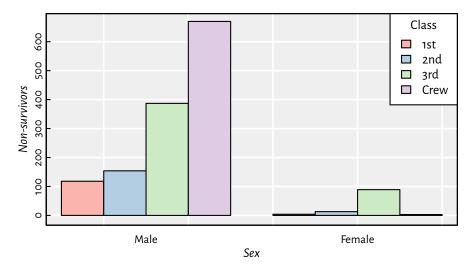


Figure 13.22: An example bar plot representing a two-way contingency table

tions falling into the corresponding disjoint intervals. Most often, there is no space between the bars to emphasise that the intervals cover the whole data range.

A histogram can be computed and drawn using the high-level function **hist**; see Figure 13.23.

```
par(mfrow=c(1, 2))
for (breaks in list("Sturges", 25)) {
    # Sturges (a heuristic) is the default; any value is merely a suggestion
    hist(iris[["Sepal.Length"]], probability=TRUE, xlab="Sepal length",
        main=NA, breaks=breaks, col="white")
    box() # weirdly we need to add it manually
}
```

**Exercise 13.33** Study the source code of **hist.default**. Note the (invisibly returned) list (of S3 class histogram). Then, study **graphics:::plot.histogram**. Implement similar functions yourself.

**Exercise 13.34** Modify your function to draw a scatter plot matrix so that it gives the histograms of the marginal distributions on its diagonal.

**Example 13.35** Using **layout** mentioned in Section 13.2.6, we can draw a scatter plot with marginal histograms; see Figure 13.24. Note that we split the page into four plots of unequal sizes, but the upper right part of the grid is unused. We use **hist** for binning only (plot=FALSE). Then, **barplot** is utilised for drawing because it gives greater control over the process (e.g., allows vertical layout).

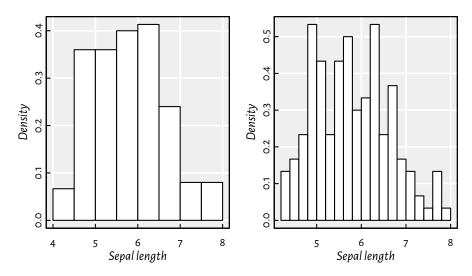


Figure 13.23: Example histograms: The same dataset, but different bin numbers

```
layout(matrix(
    c(1, 1, 1, 0, # first row: plot no. 1 of width 3 and nothing
      3, 3, 2, # three rows: square plot no. 3 and a thin but long no. 2
      3, 3, 3, 2,
      3, 3, 3, 2), nrow=4, byrow=TRUE))
par(mex=1, cex=1) # the layout function changed this!
x <- jitter(iris[["Sepal.Length"]])</pre>
y <- jitter(iris[["Sepal.Width"]])</pre>
# subplot 1
par(mar=c(0.2, 2.2, 0.6, 0.2), ann=FALSE)
hx \leftarrow hist(x, plot=FALSE, breaks=seq(min(x), max(x), length.out=20))
barplot(hx[["density"]], space=0, axes=FALSE, col="#00000011")
# subplot 2
par(mar=c(2.2, 0.2, 0.2, 0.6), ann=FALSE)
hy <- hist(y, plot=FALSE, breaks=seq(min(y), max(y), length.out=20))</pre>
barplot(hy[["density"]], space=0, axes=FALSE, horiz=TRUE, col="#00000011")
# subplot 3
par(mar=c(2.2, 2.2, 0.2, 0.2), ann=TRUE)
plot(x, y, xlab="Sepal length", ylab="Sepal width",
    xlim=range(x), ylim=range(y)) # default xlim, ylim
```

**Example 13.36** (\*) Kernel density estimators (KDEs) are another way to guesstimate the data distribution. The **density** function, for a given numeric vector, returns a list that features, amongst others, the x and y coordinates of the points that we can pass directly to the **lines** function. Below we depict the KDEs of data split into three groups; see Figure 13.25.

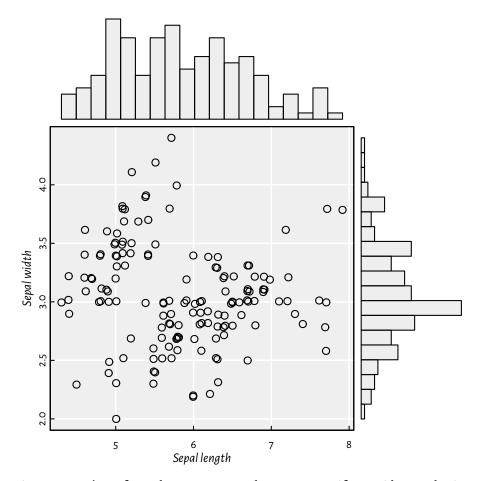


Figure 13.24: Three (four) plots on one page, but on a nonuniform grid created using layout: A scatter plot with marginal histograms

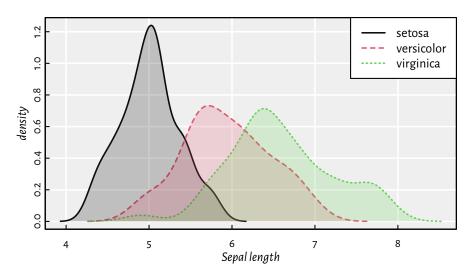


Figure 13.25: Kernel density estimators of sepal length split by species in the Iris dataset; Note the semi-transparent polygons (again)

**Exercise 13.37** (\*) Implement a function **grid\_kde**, which draws kernel density estimators for a given numeric variable split by a combination of three factor levels; see Figure 13.26 for an example.

```
grid_kde <- function(data, values, x, y, hue) ...to.do...

tips <- read.csv("~/Projects/teaching-data/other/tips.csv", comment.char="#",
    stringsAsFactors=TRUE) # see https://github.com/gagolews/teaching-data
head(tips, 3) # preview an example dataset

## total_bill tip sex smoker day time size

## 1 16.99 1.01 Female No Sun Dinner 2

## 2 10.34 1.66 Male No Sun Dinner 3

## 3 21.01 3.50 Male No Sun Dinner 3

grid_kde(tips, values="tip", x="smoker", y="time", hue="sex")</pre>
```

# 13.3.3 Box-and-whisker plots

We have already seen a chart generated by **boxplot** in Figure 5.1. Tinkering with it will give us some robust practice, which in turn shall make us perfect.

**Exercise 13.38** Modify the code generating Figure 5.1 so that:

- 1. same doses are grouped together (more space between different doses; also, on the x-axis, only unique doses are printed),
- 2. different supps have different colours (add a legend explaining them).

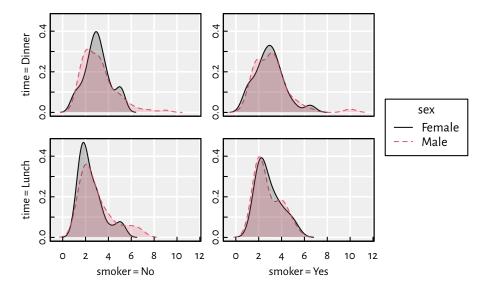


Figure 13.26: An example grid plot (also known as a trellis, panel, conditioning, or lattice plot) featuring kernel density estimators for a numeric variable (amount of tip in a US restaurant) split by a combination of three factor levels (smoker, time, sex)

**Exercise 13.39** Write a function for drawing box plots using graphics primitives.

**Exercise 13.40** (\*) Write a function for drawing violin plots. They are similar to box plots but use kernel density estimators.

**Exercise 13.41** (\*) Implement a bag plot, which is a two-dimensional version of a box plot. Use **chull** to compute the convex hull of a point set.

## 13.3.4 Contour plots and heat maps

When plotting a function of two variables like z = f(x, y), the magnitude of the z component can be expressed using colour brightness or hue.

**image** is a convenient wrapper around **rasterImage**, which can be used to draw contour plots, two-dimensional histograms, heatmaps, etc.

**Example 13.42** Figure 13.27 presents a filled contour plot of Himmelblau's function,  $f(x, y) = (x^2 + y - 11)^2 + (x + y^2 - 7)^2$ , for  $x \in [-5, 5]$  and  $y \in [-4, 4]$ . A call to **contour** adds labelled contour lines (which is actually a nontrivial operation).

```
x <- seq(-5, 5, length.out=250)
y <- seq(-4, 4, length.out=200)
z <- outer(x, y, function(xg, yg) (xg^2 + yg - 11)^2 + (xg + yg^2 - 7)^2)
image(x, y, z, col=grey(seq(1, 0, length.out=16)))
contour(x, y, z, nlevels=16, add=TRUE)</pre>
```

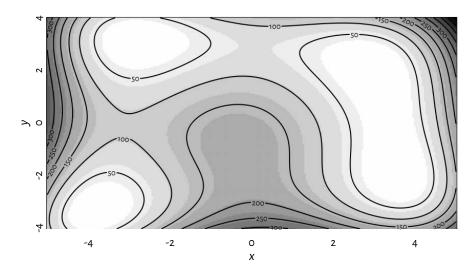


Figure 13.27: A filled contour plot of Himmelblau's function with labelled contour lines

In **image**, the number of rows in z matches the length of x, whereas the number of columns therein is equal to the size of y. This might be counterintuitive; if z is printed, the image is its 90-degree rotated version.

**Example 13.43** Figure 13.28 presents an example heatmap depicting Pearson's correlations between all pairs of variables in the nhanes dataset which we loaded some time ago.

```
0 <- c(6, 5, 1, 7, 4, 2, 3) # order of rows/cols (by similarity)
R <- cor(nhanes[o, o])
par(mar=c(2.8, 7.6, 1.2, 7.6), ann=FALSE)
image(1:NROW(R), 1:NCOL(R), R,
    ylim=c(NROW(R)+0.5, 0.5),
    zlim=c(-1, 1),
    col=hcl.colors(20, "BluGrn", rev=TRUE),
    xlab=NA, ylab=NA, asp=1, axes=FALSE)
axis(1, at=1:NROW(R), labels=dimnames(R)[[1]], las=2, line=FALSE, tick=FALSE)
axis(2, at=1:NCOL(R), labels=dimnames(R)[[2]], las=1, line=FALSE, tick=FALSE)
text(arrayInd(seq_along(R), dim(R)),
    labels=sprintf("%.2f", R),
    col=c("white", "black")[abs(R<0.8)+1],
    cex=0.89)</pre>
```

**Exercise 13.44** Check out the **heatmap** function, which uses hierarchical clustering to find an aesthetic reordering of the matrix's items.

**Example 13.45** Figure 13.29 depicts a two-dimensional histogram. It approaches the idea of reflecting the points' density quite differently from the semi-transparent symbols in Figure 13.18.

| hipcirc   | 1.00    | 0.88    | 0.94   | 0.83      | 0.24   | -0.15  | -0.44  |
|-----------|---------|---------|--------|-----------|--------|--------|--------|
| armcirc   | 0.88    | 1.00    | 0.94   | 0.82      | 0.21   | 0.12   | -0.29  |
| weight    | 0.94    | 0.94    | 1.00   | 0.92      | 0.45   | 0.16   | -0.24  |
| waistcirc | 0.83    | 0.82    | 0.92   | 1.00      | 0.63   | 0.35   | -0.00  |
| leglen    | 0.24    | 0.21    | 0.45   | 0.63      | 1.00   | 0.66   | 0.36   |
| height    | -0.15   | 0.12    | 0.16   | 0.35      | 0.66   | 1.00   | 0.80   |
| armlen    | -0.44   | -0.29   | -0.24  | -0.00     | 0.36   | 0.80   | 1.00   |
|           | hipcirc | armcirc | weight | waistcirc | leglen | height | armlen |

Figure 13.28: A correlation heatmap drawn using image

**Exercise 13.46** (\*) Implement some two-dimensional kernel density estimator and plot it using **contour**.

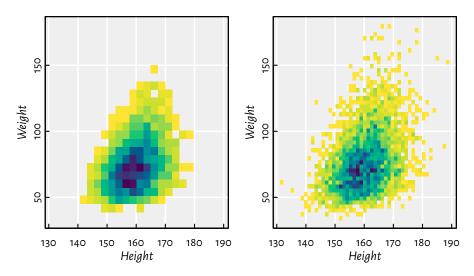


Figure 13.29: Two-dimensional histograms with different numbers of bins, where the bin count is reflected by the colour

### 13.4 Exercises

**Exercise 13.47** *Answer the following questions:* 

- Can functions from the graphics package be used to adjust the plots generated by lattice and ggplot2?
- List the most common graphics primitives.
- Can all high-level functions be implemented using low-level ones? As an example, discuss the key ingredients used in **barplot**.
- Some high-level functions discussed in this chapter feature the add parameter. What is its purpose?
- What are the admissible values of pch and lty? Also, in the default palette, what is the meaning of colours 1, 2, ..., 16? Can their meaning be changed?
- Can all graphics parameters be changed?
- What is the difference between passing xaxt="n" to plot.default vs setting it with par, and then calling plot.default?
- Which graphics parameters are set by plot.window?
- What is the meaning of the usr parameter when using the logarithmic scale on the x-axis?

- (\*) How to place a plotting symbol exactly 1 centimetre from the top-left corner of the current page (following the page's diagonal)?
- Semi-transparent polygons are nice, right?
- Can an ellipse be drawn using polygon?
- What happens when we set the graphics parameter mfrow=c(2, 2)?
- How to export the current plot to a PDF file?

**Exercise 13.48** Draw the 2022 BTC-to-USD close rates<sup>8</sup> time series. Then, add the 7- and 30-day moving averages.

(\*) Also, fit a local polynomial (moving) regression model using the Savitzky–Golay filter (see **loess**).

**Exercise 13.49** (\*) *Draw (from scratch) a candlestick plot for the 2022 BTC-to-USD rates*<sup>9</sup>.

**Exercise 13.50** (\*) Create a function to draw a normal quantile-quantile (Q-Q) plot, i.e., for inspecting whether a numeric sample might come from some normal distribution.

**Exercise 13.51** (\*) Draw a map of the world, where each country is filled with a colour whose brightness or hue is linked to its Gini index of income inequality. You can easily find the data on Wikipedia. Try to find an open dataset that gives the borders of each country as vertices of a polygon (e.g., in the form of a (geo)JSON file).

**Exercise 13.52** Next time you see a pleasant data visualisation somewhere, try to reproduce it using base *graphics*.

For further information on graphics generation in R, see, e.g., Chapter 12 in [53], [44], and [48]. In this chapter, we were only interested in *static* graphics, e.g., for use in printed publications or plain websites. Interactive plots that a user might tinker with in a web browser are a different story.

And so the second part of our course is ended.

<sup>&</sup>lt;sup>8</sup> https://github.com/gagolews/teaching-data/raw/master/marek/btcusd\_close\_2022.csv

<sup>9</sup> https://github.com/gagolews/teaching-data/raw/master/marek/btcusd\_ohlc\_2022.csv

Part III

Deepest

# $\times\!\!\times$ Interfacing compiled code (\*)

imes This chapter is under construction. Please come back later.

R is a nice *glue* language: it is perfect for implementing data wrangling pipelines, visualisation, and developing prototypes of data analysis algorithms. In other words, it makes connecting larger *building blocks* very easy. Still, for performance reasons<sup>1</sup>, we recommend moving the more computing-intensive tasks to the C, C++, or Fortran level. R works very well as a user-friendly interface to compiled code.

The definitive reference on this topic is Chapter 5 in [59].

imes This chapter is under construction. Please come back later.

<sup>&</sup>lt;sup>1</sup> A well-written, portable function library relying only on simple data structures (e.g., arrays of the type double and int) can be used in other environments, such as Python (e.g., via Cython) of Julia. Let us remember about other programmers yearning for the possibility to enjoy our cultivated algorithms.

# *Unevaluated expressions (\*)*

In this and the remaining chapters, we will learn some hocus-pocus that should only be of interest to the advanced-to-be<sup>1</sup> and open-minded R programmers who would like to understand what is going on under our language's hood. In particular, we will inspect the mechanisms behind why certain functions act differently from what we would expect them to do if a *standard* evaluation scheme was followed (compare **subset** and **transform** mentioned in Section 12.3.9).

Namely, in normal programming languages, when we write something like:

```
plot(x, exp(x))
```

the expression  $\exp(x)$ , is evaluated *first* and its value<sup>2</sup> (in this case: probably a numeric vector) is only then passed to the **plot** function as the actual parameter. Thus, if `x` was set to be  $\sec(0, 10, \end{bmatrix})$ , the above never means anything else than:

```
plot(c(0.00, 0.01, 0.02, 0.03, ...), c(1.0000, 1.0101, 1.0202, 1.0305, ...))
```

But R was heavily inspired by the S language from whom it has taken the notion of lazy arguments (Chapter 17). It is equipped with the ability to apply a set of techniques referred to as *metaprogramming* (computing on the language, reflection). With it, we can define functions that can peek outside their small world and clearly see the code fragment passed as their arguments. Having access to such *unevaluated expressions*, we can do to them whatever we please: print, modify, evaluate on different data, or ignore whatsoever.

In theory, this enables implementing many potentially helpful<sup>3</sup> beginner-friendly features and express certain requests in a more concise manner. For instance, that the y-axis labels in Figure 2.2 could be generated automatically is precisely because **plot** was able to see not only a vector like **c**(1.0000, 1.0101, 1.0202, 1.0305, ...) but also the expression that generated it, **exp**(x).

<sup>&</sup>lt;sup>1</sup> Remember that this book is supposed to be read from the beginning to the end. Also, if you have not tested yourself against all the 300-odd exercises suggested so far, please do it before proceeding with the material presented here. Only practice makes perfect, and nothing is built in a day. Give yourself time: you can always come back later.

<sup>&</sup>lt;sup>2</sup> Or a reference/pointer to an object that stores the said value.

<sup>&</sup>lt;sup>3</sup> The original authors of R (R. Ihaka and R. Gentleman), in [36], mention: "A policy of *lazy arguments* is very useful because it means that, in addition to the value of an argument, its symbolic form can be made available in the function being called. This can be very useful for specifying functions or models in symbolic form."

Nonetheless, as a form of *untamed freedom of expression*<sup>4</sup>, metaprogramming has the potential to result in chaos, confusion, and division in the user community. In particular, we can introduce a microlanguage within our language that people outside our circle will not be able to understand.

Therefore, cursed be us, for we are about to start eating from the tree of the knowledge of good and evil. But remember: with great power comes great fun (and responsibility).

# 15.1 Expressions at a glance

At the most general level, expressions (statements) in a language like R can be classified into two groups:

- simple expressions:
  - constants (e.g., 3.14, 2i, 42L, NA\_real\_, TRUE, "character string", NULL, -1.
    3e-16, 0x123abc),
  - names (symbols, identifiers),
- *compound expressions* combinations of n + 1 expressions (simple or compound) of the form:

$$(f, e_1, e_2, \dots, e_n).$$

As we will soon see, compound expressions represent a *call* to f (an *operator*) on a sequence of arguments  $e_1, e_2, \ldots, e_n$  (*operands*). It is why, equivalently, we denote them with  $f(e_1, e_2, \ldots, e_n)$ .

On the other hand, *names* such as `x`, `iris`, `sum`, and `spam` have no meaning without an explicitly stated context. This will be a topic we will explore in Chapter 16. Prior to that, we treat them as meaning-less.

Hence, for the time being, we are only interested in the *syntax* or *grammar* of our language, not the *semantics*. We are abstract in the sense that, in the expression "mean(rates)+2", neither `mean`, `x`, nor even `+` have the "usual" sense. Therefore, we should treat them as equivalent to, say, f(g(x), 2) or  $span(bacon(spanish_inquisition), 2)$ .

<sup>&</sup>lt;sup>4</sup> In the current author's opinion, R (as a whole, in the sense of R (GNUS) as a language and an environment) would be better off if an ordinary programmer was not exposed so much to functions heavily relying on metaprogramming. A healthy user can perfectly do without (and thus refrain from using) them. The fact that we call them advanced will not make us cool if we start horsing around with nonstandard evaluation. Perverse is perhaps a better label.

<sup>&</sup>lt;sup>5</sup> Which we know that we can equivalently express as "`+`(mean(rates), 2)"; see Section 9.4.5.

# 15.2 Language objects

There are three types of *language objects* in R:

- name (symbol) stores object names in the sense of simple expressions: names in Section 15.1;
- call represents unevaluated function calls in the sense of *compound expressions* above;
- expression quite confusingly, represents a *sequence* of simple or compound expressions (constants, names, or calls).

One way to create a simple or compound expression is by *quoting*, where interpreter is asked to refrain from evaluating a given command:

```
quote(spam) # name (symbol)
## spam
quote(f(x)) # call
## f(x)
quote(1+2+3*pi) # another call
## 1 + 2 + 3 * pi
```

None of the above was executed.

Single strings can be converted to names by calling:

```
as.name("spam")
## spam
```

Calls can be built programmatically by invoking:

```
call("sin", pi/2)
## sin(1.5707963267949)
```

Sometimes we had rather quote the arguments passed:

```
call("sin", quote(pi/2))
## sin(pi/2)
call("c", 1, exp(1), quote(exp(1)), pi, quote(pi))
## c(1, 2.71828182845905, exp(1), 3.14159265358979, pi)
```

Objects of the type expression can be thought of as list-like objects that consist of simple or compound expressions.

```
(exprs <- expression(1, spam, mean(x)+2))
## expression(1, spam, mean(x) + 2)</pre>
```

All arguments were quoted.

We can select or subset the individual statements using the extraction or index operators:

```
exprs[-1]
## expression(spam, mean(x) + 2)
exprs[[3]]
## mean(x) + 2
```

**Exercise 15.1** Check the type of the object returned by a call to "c(1, "two", sd, list(3, 4:5), expression(3+3))".

There is also an option to *parse* a given text fragment or a whole source file:

```
parse(text="mean(x)+2")
## expression(mean(x) + 2)
parse(text=" # two code lines (a comment to be ignored by the parser)
    x <- runif(5, -1, 1)
    print(mean(x)+2)
")
## expression(x <- runif(5, -1, 1), print(mean(x) + 2))
parse(text="2+") # syntax error - unfinished business
## Error in parse(text = "2+"): <text>:2:0: unexpected end of input 1: 2+ ^
```

**Important** The **deparse** function can be used to convert language objects to character vectors. For instance:

```
deparse(quote(mean(x+2)))
## [1] "mean(x + 2)"
```

This function has the nice side effect of tidying up the code formatting:

```
exprs <- parse(text=
"`+`(x, 2)->y; if(y>0) print(y**10|>log()) else { y<--y; print(y)}")
```

Let us print them out:

```
for (e in exprs)
    cat(deparse(e), sep="\n")
## y <- x + 2
## if (y > 0) print(log(y^10)) else {
## y <- -y
## print(y)
## }</pre>
```

**Note** Calling **class** on objects of the three aforementioned types yields name, call, and expression, whereas **typeof** returns symbol, language, and expression, respectively.

## 15.3 Calls as combinations of expressions

We have mentioned that calls (compound expressions) are combinations of simple or compound expressions of the form  $(f, e_1, ..., e_n)$ .

The first expression on the list, denoted above with f, plays a special role. It is precisely seen in the following examples:

```
as.call(expression(f, x))
## f(x)
as.call(expression(`+`, 1, x))
## 1 + x
as.call(expression(`while`, i < 10, i <- i + 1))
## while (i < 10) i <- i + 1
as.call(expression(function(x) x**2, log(exp(1))))
## (function(x) x^2)(log(exp(1)))
as.call(expression(1, x, y, z)) # utter nonsense, but syntactically valid
## 1(x, y, z)</pre>
```

Recall from Section 9.4 that operators and language constructs such as **if** and **while** are ordinary functions.

Furthermore:

```
expr <- quote(f(1+2, a=1, b=2))
length(expr)
## [1] 4
names(expr) # NULL if no arguments are named
## [1] "" "" "a" "b"</pre>
```

## 15.3.1 Browsing parse trees

Square brackets give us access to the individual expressions constituting an object of the type call. For example:

```
expr <- quote(1+x)
expr[[1]]
## `+`</pre>
(continue on next need)
```

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III DEEPEST

```
expr[2:3]
## 1(x)
```

A compound expression was defined recursively: it may consist of other compound expressions.

For instance, the following expression:

```
expr <- quote(
    while (i < 10) {
        cat("i =", i, "\n")
        i <- i+1
    }
)</pre>
```

can be rewritten using the f(...) notation like:

```
`while`(`<`(i, 10), `{`( cat("i =", i, "\n"), `<-`(i, `+`(i, 1))))
```

Equivalently, in the Polish notation (the prefix notation; (f, ...); traditionally used in Lisp), it will look like:

Thus, for example, we can dig into the sub-expressions using a series of extractions:

```
expr[[2]][[1]] # or expr[[c(2, 1)]]
## `<`
expr[[3]][[2]][[4]] # or expr[[c(3, 2, 4)]]
## [1] "\n"</pre>
```

**Example 15.2** We can even write a recursive function to traverse the whole parse tree:

```
recapply <- function(expr)

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```

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```
{
    if (is.call(expr)) lapply(expr, recapply)
    else expr
}
str(recapply(expr))
## List of 3
   $ : symbol while
   $:List of 3
##
   ..$ : symbol <
   ..$ : symbol i
    ..$ : num 10
##
##
   $ :List of 3
    ..$ : symbol {
##
##
   ..$ :List of 4
    .. ..$ : symbol cat
##
     .. ..$ : chr "i ="
##
     .. ..$ : symbol i
##
     .. ..$ : chr "\n"
##
    ..$ :List of 3
##
##
    ...$ : symbol <-
     .. ..$ : symbol i
##
##
    .. ..$ :List of 3
     .. .. ..$ : symbol +
##
    .. .. ..$ : symbol i
     .. .. ..$ : num 1
```

# 15.3.2 Manipulating calls

The R language is *homoiconic*: it can treat code as data. This includes the ability to manipulate it on the fly. This is because, just like on lists, we can freely use the replacement versions of `[` and `[[` on objects of the type call.

```
expr[[2]][[1]] <- as.name("<=")
expr[[3]] <- quote(i <- i * 2)
print(expr)
## while (i <= 10) i <- i * 2</pre>
```

We are only limited by our imagination.

# 15.4 Inspecting function definitions and arguments thereto

# 15.4.1 Getting the body and formal arguments

Consider the following definition:

```
test <- function(x, y=1)
    x+y # whatever</pre>
```

We know from the first part of this book that calling **print** on a function will reveal its source code.

It turns out that we can get access to the list of parameters in the form of a named list<sup>6</sup>:

```
formals(test)
## $x
##
##
##
##
## $y
## [1] 1
```

Note that the expressions generating the values of the default arguments are stored as ordinary list elements (for more details, see Section 17.2).

Furthermore, we can get access to the function's body:

```
body(test)
## x + y
```

It is an object of the now well-known class call. Thus, we can customise it as we please:

```
body(test)[[1]] <- as.name("*") # change from `+` to `*`
body(test) <- as.call(list(as.name("{"), quote(cat("spam")), body(test)))
test
## function (x, y = 1)
## {
## cat("spam")
## x * y
## }</pre>
```

<sup>&</sup>lt;sup>6</sup> Actually, a special internal datatype called pairlist, which is rarely seen in R; see [62] and [59] for information on how to deal with them at the C level. From this course's perspective, seeing pairlists as named lists is perfectly fine.

### 15.4.2 Getting the expression passed as an actual argument

A call to **substitute** allows us to reveal the expression used to generate a function's argument.

```
test <- function(x) substitute(x)</pre>
```

Some examples:

```
test(1)
## [1] 1
test(2+spam)
## 2 + spam
test(test(test(!!7)))
## test(test(!!7))
test() # it is not an error
```

Chapter 17 notes that arguments are evaluated only on demand (lazily): **substitute** triggers no computations. This opens the possibility to implement functions that interpret their input whichever way they like; see Section 9.5.7, Section 12.3.9, and Section 17.5 for examples.

**Example 15.3** *library* (see Section 7.3.1) allows specifying the name of the package to be loaded both in the form of a character string and a name:

```
library("gsl") # preferred
library(gsl) # discouraged - via as.character(substitute(package))
```

A user saves two keystrokes at the cost of not being able to prepare the package name programmatically before the call:

```
which_package <- "gsl"
library(which_package) # library("which_package")
## Error in library(which_package): there is no package called
## 'which_package'</pre>
```

In order to make the above possible, we need to alter the character.only argument (which defaults to FALSE):

```
library(which_package, character.only=TRUE)
```

**Exercise 15.4** It is quite common to see a call like **deparse(substitute(**arg)) or **as. character(substitute(**arg)) in many built-in functions. Study the source code of **plot. default, hist.default, prop. test, wilcox. test. default** and the aforementioned **library**. Explain why they do that. Propose a solution to achieve the same functionality without using reflection techniques.

### 15.4.3 Checking if an argument is missing

There is an easy way to check whether an argument was provided at all:

```
test <- function(x) missing(x)

test(1)
## [1] FALSE
test()
## [1] TRUE</pre>
```

**Exercise 15.5** Study the source code of **sample**, **seq.default**, **plot.default**, **matplot**, and **t.test.default**. Determine the role of a call to **missing**. Would introducing a default argument NULL and testing its value with **is.null** constitute a reasonable alternative?

### 15.4.4 Determining how a function was called

Even though this somewhat touches on the topics discussed in the two following chapters, it is worth knowing that **sys.call** can look at the call stack and determine how the current function was invoked.

Moreover, match.call takes us a step further: it returns a call with argument names matched to a function's formal parameters list.

For instance:

```
test <- function(x, y, ..., a="yes", b="no")
{
    print(sys.call()) # sys.call(0)
    print(match.call())
}

x <- "maybe"
test("spam", "bacon", "eggs", u = "ham"<"jam", b=x)
## test("spam", "bacon", "eggs", u = "ham" < "jam", b = x)
## test(x = "spam", y = "bacon", "eggs", u = "ham" < "jam", b = x)</pre>
```

Another example where we see that we can access the call stack much more deeply:

```
f <- function(x)
{
    g <- function(y)
    {
        cat("g:\n")
        print(sys.call(0))
        print(sys.call(-1)) # go back one frame
        y
    }
}</pre>
```

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```
cat("f:\n")
print(sys.call(0))
g(x+1)
}

f(1)
## f:
## f(1)
## g:
## g(x+1)
## f(1)
## f(1)
## [1] 2
```

**Note** Let us formalise the order of matching function parameters *to* the passed arguments. As described in Section 4.3 in [63], it proceeds as follows:

- keyword arguments with names matched exactly, each name matched at most once,
- 2. remaining keyword arguments, but with the partial matching of names listed before the ellipsis, `...`, each match must be unambiguous,
- 3. positional matching to the remaining parameters,
- 4. all remaining arguments (named or not) will be consumed by the ellipsis (if present).

For instance:

```
test <- function(spam, jasmine, jam, ..., option=NULL)
print(match.call())</pre>
```

#### Example calls:

```
test(1, 2, 3, 4, option="yes")
## test(spam = 1, jasmine = 2, jam = 3, 4, option = "yes")
test(1, 2, jasmine="no", sp=4, ham=7)
## Warning in test(1, 2, jasmine = "no", sp = 4, ham = 7): partial argument
## match of 'sp' to 'spam'
## Warning in match.call(definition, call, expand.dots, envir): partial
## argument match of 'sp' to 'spam'
## test(spam = 4, jasmine = "no", jam = 1, 2, ham = 7)
test(1, 2, ja=7) # ambiguous match
## Warning in test(1, 2, ja = 7): partial argument match of 'ja' to 'jasmine'
## Error in test(1, 2, ja = 7): argument 3 matches multiple formal arguments
```

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```
test(o=7) # partial matching of `option` failed - `option` is after `...`
## test(o = 7)
```

Note again that our environment uses **options**(warnPartialMatchArgs=TRUE).

**Exercise 15.6** A function can<sup>7</sup> see how it was defined by its maker. Call **sys.function** inside its body to reveal that.

Exercise 15.7 Execute "match.call(sys.function(-1), sys.call(-1))" in the g function above.

### 15.5 Exercises

**Exercise 15.8** *Answer the following questions:* 

- What is a simple expression? What is a compound expression? Give a few examples.
- What is the difference between an object of the type call and that of the type expression?
- What do formals and body return when called on a function object?
- How to test if an argument to a function was given at all? Provide a use case for such a verification.
- Give a few ways to create an unevaluated call.
- What is the purpose of **deparse(substitute(...))**? Give a few examples of functions that use this technique.
- What is the difference between sys.call and match.call?

**Exercise 15.9** Write a function that takes the dot-dot argument (Section 9.5.6). Using **match.call** (amongst others), determine the list of all the expressions passed via `...`; some might be named (just like in one of the above examples). The solution is given in Section 17.3.

**Exercise 15.10** Write a function **check\_if\_calls**(f, fun\_list) that takes another function {command}fon input. Then, it verifies if f calls any of the functions (referred to by their names) from a character vector fun\_list.

<sup>&</sup>lt;sup>7</sup> Therefore, it is possible to write a function that returns a modified version of itself.

# *Environments and evaluation (\*)*

In the first part of our book, we discussed the most crucial *basic* object types: numeric, logical, and character vectors, lists (generic vectors), and functions.

In this chapter, we introduce another basic type: *environments*. Like lists, they can be classified as recursive data structures; compare the diagram in Figure 17.2.

**Important** Each object of the type environment consists of:

- a *frame*<sup>1</sup> (Section 16.1), which stores a set of *bindings* that associate variable names with their corresponding values; it can be thought of as a container of named R objects of any type;
- a reference to an *enclosing environment*<sup>2</sup> (Section 16.2.2), which might be inspected (recursively!) when a requested named variable is not found in the current frame.

Even though we rarely interact with them directly (unless we need a hash table-like data structure with a quick by-name element lookup), they are crucial for the R interpreter itself. Namely, we shall soon see that they form the basis of the *environment model of evaluation*, which governs how expressions are computed (Section 16.2).

# 16.1 Frames: Environments as object containers

To create a new, empty environment, we can call the new.env function:

```
e1 <- new.env()
typeof(e1)
## [1] "environment"</pre>
```

In this section, we treat environments merely as containers for named objects of any kind, i.e., we deal with the *frame* part thereof.

<sup>&</sup>lt;sup>1</sup> Not to be confused with a data frame, i.e., an object (list) of S3 class data. frame; see Chapter 12.

<sup>&</sup>lt;sup>2</sup> Some also call it a *parent* environment, but we will not. We will try following the nomenclature established in Section 3.2 in [1]. Note that there is a bit of a mess in the R documentation regarding how enclosing environments are referred to.

Let us insert some elements into e1:

```
e1[["x"]] <- "x in e1"
e1[["y"]] <- 1:3
e1[["z"]] <- NULL # unlike in the case of lists, creates a new element
```

The `[[` operator provides us with a named list-like look-and-feel also in the case of element extraction:

```
e1[["x"]]
## [1] "x in e1"
e1[["spam"]] # does not exist
## NULL
(e1[["y"]] <- e1[["y"]]*10) # replace with new content
## [1] 10 20 30
```

### 16.1.1 Printing

Printing an environment leads to a quite awkward result:

```
print(e1) # same with str(e1)
## <environment: 0x561da7d7deb8>
```

It is the address where e1 is stored in the computer's memory. It can serve as the environment's unique identifier.

As we have said, these objects are of rather internal interest. Thus, such an esoteric message was perhaps a good design choice to ward off novices. However, we can easily get the list of objects stored inside the container by calling names:

```
names(e1) # but attr(e1, "names") is not set
## [1] "x" "y" "z"
```

Moreover, **length** gives the number of bindings in the frame:

```
length(e1)
## [1] 3
```

#### Environments vs named lists 16.1.2

Environment frames, in some sense, can be thought of as named lists, but the set of admissible operations is severely restricted. In particular, we cannot extract more than one element at the same time using the index operator:

```
e1[c("x", "y")] # but see the `mget` function
## Error in e1[c("x", "y")]: object of type 'environment' is not subsettable
```

nor can we refer to the elements by position:

```
e1[[1]] <- "bad key"
## Error in e1[[1]] <- "bad key": wrong args for environment subassignment
```

**Exercise 16.1** Check if **lapply** and **Map** can be applied directly on environments. Also, can we iterate over their elements using a **for** loop?

Still, named lists can be converted to environments and vice versa using as.list and as.environment.

```
as.list(e1)
## $x
## [1] "x in e1"
##
## $y
## [1] 10 20 30
##
## $z
## NULL
as.environment(list(u=42, whatever="it's not going to be printed anyway"))
## <environment: 0x561da7935538>
as.list(as.environment(list(x=1, y=2, x=3))) # no duplicates allowed
## $y
## [1] 2
##
## $x
## [1] 3
```

### 16.1.3 Hash maps: Fast element lookup by name

Environment frames are internally implemented using hash tables (hash maps; see, e.g., [14, 38]) with character string keys.

**Important** A *hash table* is a data structure that allows for a very quick<sup>3</sup> lookup and insertion of individual elements *by name*.

The above comes at a price, including what we have already observed above:

- the elements are not ordered in any particular way: they cannot be referred to via a numeric index;
- all element names must be unique.

**Note** A list may be considered a *sequence*, but an environment frame is only, in fact, a *set* (a bag) of *key-value pairs*. In most numerical computing applications, we would rather

<sup>&</sup>lt;sup>3</sup> In hash tables, element lookup, insertion, and deletion take amortised O(1) time.

store, iterate over, and process all the elements *in order*, hence the greater prevalence of the former. Lists still allow for an element lookup by name, even though this is slightly slower<sup>4</sup>. Overall, they are much more universal.

**Example 16.2** A natural use case of manually-created environment frames deals with grouping a series of objects identified by character string keys.

Consider a simple pseudocode for counting the number of occurrences of objects in a given container:

```
for (key in some_container) {
    if (!is.null(counter[["key"]]))
        counter[["key"]] <- counter[["key"]]+1
    else
        counter[["key"]] <- 1
}</pre>
```

Let us assume that some\_container is large, say, of size n, e.g., it is generated on the fly by reading some data stream. Then, the run-time of the above algorithm will depend on the data structure used. If the counter is a list, then, theoretically, the worst-case performance will be  $O(n^2)$  (if all keys are unique). On the other hand, for environments, it will be faster by one order magnitude: down to amortised O(n).

**Exercise 16.3** Implement a test function according to the above pseudocode and benchmark the two data structures using **proc.time** on some example data.

**Exercise 16.4** (\*) Determine the number of unique text lines in a huge file (assuming that the set of unique text lines fits into memory, but the file itself does not). Also, determine the five most frequently occurring text lines.

# 16.1.4 Pass-by-value, copy on demand: Not for environments

Given any object, say, x, when we issue:

```
y <- x
```

its copy<sup>5</sup> is made so that y and x are independent. In other words, any change to the state of x (or y) is not reflected in y (or x).

For instance:

<sup>&</sup>lt;sup>4</sup> Accessing elements by position (numeric index) in lists takes O(1) time. The worst-case scenario for the element lookup by name is linear with respect to the container size: when the item is not found. Also, inserting new elements at the end takes amortised O(1) time.

<sup>&</sup>lt;sup>5</sup> Delayed (on demand); see below.

(continued from previous page)

```
print(y)
## $a
## [1] 2
print(x) # not affected: `x` and `y` are independent
## $a
## [1] 1
```

The same happens with arguments that we feed to the functions:

```
mod <- function(y, key) # it is like: local_y <- passed_argument
{
    y[[key]] <- y[[key]]+1
    y
}

mod(x, "a") # returns a modified copy of `x`
## $a
## [1] 2
print(x) # not affected
## $a
## [1] 1</pre>
```

We can thus say that R applies the pass-by-value strategy here.

**Important** Environments are the only<sup>6</sup> objects that follow the assign- and pass-by-reference strategies.

In other words, if we perform:

```
x <- as.environment(x)
y <- x</pre>
```

then the names x and y are bound with the same object in the computer's memory:

```
print(x)
## <environment: 0x561da6b66ab8>
print(y)
## <environment: 0x561da6b66ab8>
```

### Therefore:

<sup>&</sup>lt;sup>6</sup> We do not count all the tricks we can do at the C language level (Chapter 14). Also, the distinction between pass-by-value and pass-by-reference is slightly more complicated in R because of the lazy evaluation of arguments (Chapter 17). We make an idealisation for didactic purposes here.

```
y[["a"]] <- y[["a"]]+1
print(y[["a"]])
## [1] 2
print(x[["a"]]) # `x` is `y`, `y` is `x`
## [1] 2
```

The same happens when we pass an environment to a function:

```
mod(y, "a") # pass-by-reference (`y` is `x`, remember?)
## <environment: 0x561da6b66ab8>
x[["a"]]
          # `x` has changed
## [1] 3
```

Thus, any changes we make to an environment passed as an argument to a function will be visible outside the call. This minimises time and memory use in certain situations

**Note** (\*) For efficiency reasons, when we write "y <- x", a copy of `x` (unless it is an environment) is created only if it is absolutely necessary.

Here is some benchmarking of the copy-on-demand mechanism.

```
n <- 100000000 # like, a lot
```

Creation of a new large numeric vector:

```
t0 <- proc.time(); x <- numeric(n); proc.time() - t0</pre>
##
     user system elapsed
     0.853 1.993
                     2.852
##
```

Creation of a (delayed) copy:

```
proc.time() - t0
t0 <- proc.time(); y <- x;
     user system elapsed
##
##
         0
```

It was instant. Thus, we definitely did not duplicate the n data cells.

Copy-on-demand is implemented using some simple reference counting; compare sec:memory-management. We can inspect that x and y point to the same address in memory by calling:

```
.Internal(inspect(x)) # internal function - do not use it
## @7efba1134010 14 REALSXP g0c7 [REF(2)] (len=1000000000, tl=0) 0,0,0,0,...
.Internal(inspect(y))
## @7efba1134010 14 REALSXP g0c7 [REF(2)] (len=1000000000, tl=0) 0,0,0,0,...
```

The actual copying is only triggered when we try to modify x or y. This is when the objects need to be separated.

Now x and y are different objects.

```
.Internal(inspect(x))
## @7efba1134010 14 REALSXP g0c7 [MARK,REF(1)] (len=1000000000, tl=0) 0,0,...
.Internal(inspect(y))
## @7ef9c43ce010 14 REALSXP g0c7 [MARK,REF(1)] (len=1000000000, tl=0) 1,0,...
```

The elapsed time is similar to that needed to create x from scratch. Further modifications will already be quick:

### 16.1.5 A note on reference classes (\*\*)

In Section 11.5, we briefly mentioned the S4 system for object-oriented programming.

It turns out that we also have access to its variant, called *reference classes*<sup>7</sup>. It was first introduced in R version 2.12.0.

Reference classes are implemented using S4 classes, with the data part being of the type environment. This gives a more typical object-oriented experience, where methods can modify the data they act on in place.

They are theoretically interesting concepts on their own and quite appealing to package developers with C++ or Java background. Nevertheless, in the current author's opinion, such classes are alien citizens of our environment, violating its *functional* nature. Therefore, we will not be discussing them here.

A curious reader is referred to **help**("ReferenceClasses") and Chapters 9 and 11 of [11] for more details.

<sup>&</sup>lt;sup>7</sup> Some call them R5, but we will not.

#### The environment model of evaluation 16.2

In Chapter 15, we said that there are three types of expressions: constants (e.g., 1 and "spam"), names (e.g., x and spam), and calls (like f(x, 1)).

**Important** Names (symbols) have no meaning by themselves. The *meaning* of a name always depends on the context, which is specified by some environment.

Consider a simple expression merely consisting of a name, `x`:

```
expr_x <- quote(x)
```

Let us define two environments that bind the name `x` with two different constants.

```
e1 <- as.environment(list(x=1))</pre>
e2 <- as.environment(list(x="spam"))</pre>
```

An expression is evaluated within a specific environment. We can do that by calling eval:

```
eval(expr_x, envir=e1) # evaluate `x` within environment e1
## [1] 1
eval(expr_x, envir=e2) # evaluate the same `x` within environment e2
## [1] "spam"
```

The very same expression has two different meanings, depending on the context. This is quite like in the so-called real life: "I'm good" can mean "I don't need anything" but also "My virtues are plentiful". It all depends on who and when is asking, i.e., in which environment we evaluate the said sentence.

We call this the *environment model of evaluation*, a notion that R authors have borrowed from a Lisp-like language called Scheme<sup>8</sup> (see Section 3.2 in [1] and Section 6 in [63]).

# Getting the current environment (here: the global one)

By default, expressions are evaluated in the *current* environment. We can fetch it by calling:

```
sys.frame(sys.nframe()) # get the current environment
## <environment: R GlobalEnv>
```

We are working on the R console. Hence, the current one is the global environment (user

 $<sup>^8</sup>$  That is why everyone serious about R programming should add the Structure and Interpretation of Computer Programs [1] to their reading list. Also, R is not the only known marriage between statistics and Lisp-like languages; see also LISP-STAT [50].

workspace). We can access it from anywhere by calling **globalenv** or referring to the `.GlobalEnv` object.

**Example 16.5** Calling any operation, for instance<sup>9</sup>:

```
x <- "spammity spam"
```

means evaluating it within the current environment:

```
eval(quote(x <- "spammity spam"), envir=sys.frame(sys.nframe()))</pre>
```

Here, we bound the string "spammity spam" with the name  $\hat{x}$  in the current environment's frame:

```
sys.frame(sys.nframe())[["x"]] # yes, `x` is in the current environment now
## [1] "spammity spam"
globalenv()[["x"]] # because the global environment is the current one here
## [1] "spammity spam"
```

Therefore, when we now refer to `x` (from within the current environment):

```
x # eval(quote(x), envir=sys.frame(sys.nframe()))
## [1] "spammity spam"
```

precisely the above named object is fetched.

**Exercise 16.6** save.image can be used to save the current workspace, i.e., the global environment, by default, to the file named .Rdata in the current working directory. Test this function in combination with load.

**Note** Names starting with a dot are *hidden*. **ls**, a function to fetch all names registered within a given environment, does not list them by default.

```
.test <- "spam"
ls() # list all names in the current environment, i.e., the global one
## [1] "e1" "e2" "expr_x" "mod" "x" "y"</pre>
```

Compare the above with:

On a side note, `.Random.seed` stores the current pseudorandom number generator's seed; compare Section 2.1.5.

 $<sup>^{9}</sup>$  Let us, for now, take for granted that `<-` is accessible from the current context and denotes assignment.

### Enclosures, enclosures thereof, etc.

To show that there is much more to the environment model of evaluation than what we mentioned above, let us try to evaluate an expression featuring two names:

```
e2 <- as.environment(list(x="spam")) # once again (a reminder)</pre>
expr_comp <- quote(x < "eggs")</pre>
eval(expr_comp, envir=e2)
## Error in x < "eggs": could not find function "<"
```

The meaning of any constant (here, "spam") is context-independent, `x` is specified by the environment provided, but the name `<` is not mentioned therein. Hence the error.

Nonetheless, we feel that we know the meaning of `<`. It is a relational operator, obviously, isn't it? To increase the confusion, let us highlight that our experience-grounded intuition is true in the following context:

```
e3 <- new.env()
e3[["x"]] <- "bacon"
eval(expr comp, envir=e3)
## [1] TRUE
```

So where does the name `<` come from? It is neither included in e2 nor e3:

```
e2[["<"]]
## NULL
e3[["<"]]
## NULL
```

Is `<` hardcoded somewhere? Or is it also dependent on the context? Why is it visible when evaluating an expression within e3 but not in e2?

Studying<sup>10</sup> help("[[") (see the Environments section therein), we discover that e3[["<"]] is equivalent to a call to **get**("<", envir=e3, inherits=FALSE).

In help("get"), we read that if the inherits argument is set to TRUE (which is the default in **get**), then the enclosing frames of the given environment are searched as well.

Continuing the example from the previous subsection:

```
get("<", envir=e2) # inherits=TRUE</pre>
## Error in get("<", envir = e2): object '<' not found
get("<", envir=e3) # inherits=TRUE</pre>
## function (e1, e2) .Primitive("<")</pre>
```

And indeed, we see that `<` is reachable from within e3 but not e2. It means that e3

<sup>&</sup>lt;sup>10</sup> Which we should have done already a long time ago, but most likely, we did not.

*points to* another environment where further information should be sought if we the current container is left empty-handed.

**Important** The reference (pointer) to the *enclosing environment* is integral to each environment (alongside a *frame* of objects). It can be fetched and set using the **parent.env** function.

### 16.2.3 Missing names are sought in enclosing environments

To understand the idea of enclosing environments better, let us create two new environments whose enclosures are explicitly set as follows:

```
(e4 <- new.env(parent=e3))
## <environment: 0x561da73a80d0>
(e5 <- new.env(parent=e4))
## <environment: 0x561da728b4f8>
```

To verify that everything is in order, let us inspect the following:

```
print(e3) # this is the address of e3 by the way
## <environment: 0x561da7982ba8>
parent.env(e4) # e3 is the enclosing environment of e4
## <environment: 0x561da7982ba8>
parent.env(e5) # e4 is the enclosing environment of e5
## <environment: 0x561da73a80d0>
```

Also, let us bind two different objects with the name `y` in e5 and e3.

```
e5[["y"]] <- "spam"
e3[["y"]] <- function() "a function `y` in e3"
```

The current state of matters is depicted in Figure 16.1.

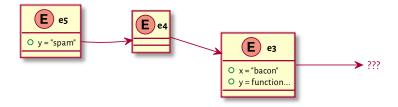


Figure 16.1: Example environments and their enclosures (original setting)

Now, let us consider a simple expression featuring the `y` name only and evaluate it in the above environments:

```
expr_y <- quote(y)
eval(expr_y, envir=e3)
## function() "a function `y` in e3"
eval(expr_y, envir=e5)
## [1] "spam"
```

No surprises yet. However, evaluating it in e4, which does not feature `y`, yields:

```
eval(expr_y, envir=e4)
## function() "a function `y` in e3"
```

It returned 'y' from e4's enclosure, e3.

Let us horse around with the enclosures of e5 and e4 so that we obtain the setting depicted in Figure 16.2:

```
parent.env(e5) <- e3</pre>
parent.env(e4) <- e5</pre>
```

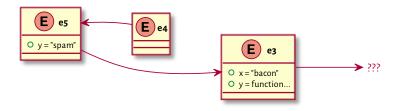


Figure 16.2: Example environments and their enclosures (after the change made)

Now evaluating `y` again in the same e4 yields a very different result:

```
eval(expr_y, envir=e4)
## [1] "spam"
```

**Important** If a name is referred to in an expression but is missing in the current environment, it will be sought in its enclosure(s).

Note There are some functions related to searching within and modifying environments which optionally (see their inherits argument) allow for continuing explorations in the enclosures until successful:

- inherits=TRUE by default:
  - exists,
  - get,

- inherits=FALSE by default:
  - assign,
  - rm (remove).

### 16.2.4 Looking for functions

Interestingly, if a name is used instead of a function to be called, the object sought is always<sup>11</sup> of the mode function.

Consider a similar expression to the above, but this time including the name `y` playing a different role:

```
expr_y2 <- quote(y()) # a call to something named `y`
eval(expr_y2, envir=e4)
## [1] "a function `y` in e3"</pre>
```

In other words, what we used here was not:

```
get("y", envir=e4)
## [1] "spam"
```

but:

```
get("y", envir=e4, mode="function")
## function() "a function `y` in e3"
```

**Note** "name()", ""name"()", and "`name`()" are synonymous. However, the first expression is acceptable only if the name is syntactically valid.

# 16.2.5 Inspecting the search path

Going back to our expression involving a relational operator:

```
expr_comp
## x < "eggs"
```

Why does the following work as expected?

```
eval(expr_comp, envir=e3)
## [1] TRUE
```

Well, we gathered all the bits to understand it now. Namely, `<` is a function that is looked up in the following way:

<sup>&</sup>lt;sup>11</sup> This is why we can write "c < -c(1, 2)" and then still be able to call c to create another vector.

```
get("<", envir=e3, inherits=TRUE, mode="function")
## function (e1, e2) .Primitive("<")</pre>
```

It was reachable from e3, which means that e3 also has an enclosing environment.

```
parent.env(e3)
## <environment: R_GlobalEnv>
```

This is our global namespace, which was the current environment when e3 was created. Still, we did not define `<` there. It means that the global environment also has an enclosure.

We can explore the whole *search* path by starting at the global environment and following the enclosures recursively.

```
ecur <- globalenv() # starting point</pre>
repeat {
    cat(pasteO(format(ecur), " (", attr(ecur, "name"), ")")) # pretty-print
    if (exists("<", envir=ecur, inherits=FALSE))</pre>
        cat(strrep(" ", 20), "`<` found here!")</pre>
    cat("\n")
    ecur <- parent.env(ecur) # advance to its enclosure
}
## <environment: R_GlobalEnv> ()
## <environment: 0x561da7bc1408> (.marekstuff)
## <environment: package:stats> (package:stats)
## <environment: package:graphics> (package:graphics)
## <environment: package:grDevices> (package:grDevices)
## <environment: package:utils> (package:utils)
## <environment: package:datasets> (package:datasets)
## <environment: package:methods> (package:methods)
## <environment: 0x561da5c55b80> (Autoloads)
                                                `<` found here!
## <environment: base> ()
## <environment: R EmptyEnv> ()
## Error in parent.env(ecur): the empty environment has no parent
```

Underneath the global environment, there is a whole list of attached packages:

- packages attached by the user (.marekstuff is used internally in the process of evaluating code in this book),
- 2. default packages (Section 7.3.1),
- 3. (\*\*) **Autoloads** (for the promises-to-load R packages; compare **help**("autoload"); it is a technicality we may safely ignore here),

- 4. the **base** package, which we can access directly by calling **baseenv**; it is where most of the *fundamental* functions from the previous chapters reside,
- 5. the *empty* environment (**emptyenv**), which is the only one followed by nothing (the loop would turn out endless otherwise).

It comes at no surprise that the `<` operator has been found in the base package.

**Note** On a side note, the reason why this operation failed:

```
e2 <- as.environment(list(x="spam")) # to recall
eval(expr_comp, envir=e2)
## Error in x < "eggs": could not find function "<"</pre>
```

is because **as.environment** sets the enclosing environment to:

```
parent.env(e2)
## <environment: R_EmptyEnv>
```

See also **list2env** which gives greater control over this (cf. its parent argument).

# 16.2.6 Attaching to and detaching from the search path

In Section 7.3.1, we mentioned that we can access the objects exported by a package without attaching them to the search path by using the **pkg::object** syntax (this loads the package if necessary).

For instance:

```
tools::toTitleCase("`tools` not attached to the search path")
## [1] "`tools` not Attached to the Search Path"
```

However:

```
toTitleCase("nope")
## Error in toTitleCase("nope"): could not find function "toTitleCase"
```

It does not work, because  ${\tt toTitleCase}$  is not reachable from the current environment.

Let us inspect the current search path (yes, there is a built-in function for that):

Writing "pkg::" might be inconvenient in the long run (for some). Thus, we can call

**library** to attach the package to the search path immediately below the global environment.

```
library("tools")
```

The search path becomes (see Figure 16.3 for an illustration):

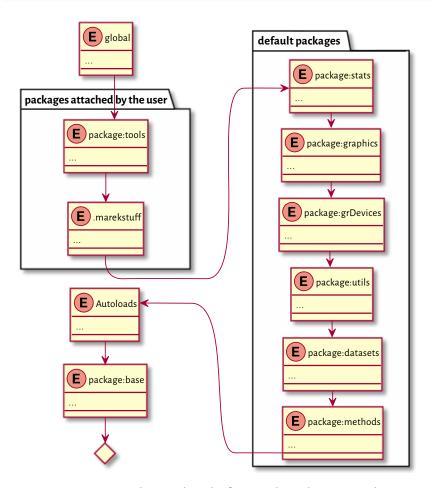


Figure 16.3: The search path after attaching the tools package

Therefore, what follows, now works as expected:

```
toTitleCase("Nobody expects the Spanish Inquisition")
## [1] "Nobody Expects the Spanish Inquisition"
```

We can use **detach**<sup>12</sup> to remove an item from the search path.

```
detach("package:tools")
"package:tools" %in% search() # not there anymore
## [1] FALSE
```

We use the "package:" prefix for the reasons that we shall describe in Section 16.3.5.

**Note** We can also plug arbitrary environments<sup>13</sup> and named lists into the search path. Recalling that data frames are built upon the latter (Section 12.1.6), some users rely on this technique to free themselves from the onerous burden of typing the object name each time its column is to be referred to:

```
attach(iris)
head(Sepal.Length) # iris[["Sepal.Length"]]
## [1] 5.1 4.9 4.7 4.6 5.0 5.4
```

Here, the iris list was converted to an environment, and the necessary enclosures were set accordingly:

```
str(parent.env(globalenv()))
## <environment: 0x561da7c5ebb0>
## - attr(*, "name")= chr "iris"
str(parent.env(parent.env(globalenv())))
## <environment: 0x561da7bc1408>
## - attr(*, "name")= chr ".marekstuff"
```

Overall, attaching data frames is discouraged, especially outside the interactive mode. Let us not be too lazy.

```
detach(iris) # such a relief
```

# 16.2.7 Masking (shadowing) objects from down under

An assignment via `<-` (and assign, by default) creates a binding in the *current* environment.

<sup>&</sup>lt;sup>12</sup> Which does not unload the package from memory, though; see unload (possibly combined with library.dynam.unload).

<sup>&</sup>lt;sup>13</sup> Or we should rather say, environment frames. When an environment is attached to the search path, it is duplicated so that the changes made to the original environment are not reflected in the copy. Then its previous enclosure is discarded. After all, we want a series of recursive calls to parent.env to form the whole search path.

Therefore, even if the name to bind exists somewhere on the search path, it will not be modified. Instead, a new name will be created.

```
expr_comp <- quote("spam" < "eggs")
eval(expr_comp)
## [1] FALSE</pre>
```

Here, we rely on `<` from the base environment. Withal, we can create an object of the same name in the current (global) context:

```
'<' <- function(e1, e2)
{
    warning("This is not the base '<', mate.")
    NA
}</pre>
```

Now we have two different functions of the same name. When we evaluate an expression within the current environment or any of its "descendants", the new name will *shadow* the base one:

```
eval(expr_comp)
## Warning in "spam" < "eggs": This is not the base `<`, mate.
## [1] NA
eval(expr_comp, envir=e5) # e5's enclosure's enclosure is the global env
## Warning in "spam" < "eggs": This is not the base `<`, mate.
## [1] NA</pre>
```

But we can still call the original function directly:

```
base::`<`(1, 2)
## [1] TRUE
```

It is also reachable from within the current environment's "ancestors":

```
eval(expr_comp, envir=as.environment("package:utils"))
## [1] FALSE
```

Before proceeding any further, let us clean up after ourselves. Otherwise, we will be asking for trouble.

```
rm("<") # removes `<` from the global environment
```

An attached package may introduce some object names that are also available elsewhere. For instance:

```
library("stringx")
## Attaching package: 'stringx'
(continues on next page)
```

```
## The following objects are masked from 'package:base': casefold, chartr,
## endsWith, gregexec, gregexpr, grep, grepl, gsub, ISOdate, ISOdatetime,
## nchar, nzchar, paste, paste0, regexec, regexpr, sprintf, startsWith,
## strftime, strptime, strrep, strsplit, strtrim, strwrap, sub, substr,
## substr<-, substring, substring<-, Sys.time, tolower, toupper, trimws,
## xtfrm, xtfrm.default</pre>
```

Therefore, in the current context, we have what follows:

```
toupper("Groß") # stringx::toupper
## [1] "GROSS"
base::toupper("Groß")
## [1] "GROß"
```

Sometimes<sup>14</sup>, we can use assign(..., inherits=TRUE) or its synonym, `<<-`, to modify the *existing* binding (without creating a new one if not necessary).

**Note** Let us attach the iris data frame (named list) to the search path again:

```
attach(iris)
Sepal.Length[1] <- 0</pre>
```

It does not modify the original iris nor its converted-to-an-environment copy that we can find in the search path. Instead, a new vector named Sepal.Length has been created in the current environment:

```
exists("Sepal.Length", envir=globalenv(), inherits=FALSE)
## [1] TRUE
```

We can verify the above statement as follows:

```
rm("Sepal.Length") # removes the one in the global environment
Sepal.Length[1] # `iris` from the search path
## [1] 5.1
iris[["Sepal.Length"]][1] # the original `iris`
## [1] 5.1
```

However, by writing:

```
Sepal.Length[1] <<- 0 # uses assign(..., inherits=TRUE)
```

We changed the state of the environment on the search path.

 $<sup>^{14}</sup>$  We normally cannot modify package namespaces. As we will mention in Section 16.3.5, they are automatically locked.

```
exists("Sepal.Length", envir=globalenv(), inherits=FALSE)
## [1] FALSE
Sepal.Length[1] # `iris` from the search path
## [1] 0
```

Yet, the original iris object is left untouched. There is no mechanism in place that would *synchronise* the original data frame and the object in the search path.

```
iris[["Sepal.Length"]][1] # the original `iris`
## [1] 5.1
```

### 16.3 Closures

So far, we have only covered the rules for evaluating *standalone* R expressions. In this section, we look at what happens *inside* the invoked functions.

### 16.3.1 Local environment

When we call a function, a new temporary environment is created. It is where all arguments<sup>15</sup> and local variables are emplaced. During the function evaluation, this environment becomes the current one. After the call, the environment ceases to exist, and we return to the previous environment from the call stack.

Consider the following function:

```
test <- function(x)
{
    print(ls()) # list object names in the current environment
    y <- x^2 # creates a new variable
    print(sys.frame(sys.nframe())) # get the ID of the current environment
    str(as.list(sys.frame(sys.nframe()))) # display its contents
}</pre>
```

First call:

```
test(2)
## [1] "x"
## <environment: 0x561da7c3b278>
## List of 2
## $ y: num 4
## $ x: num 2
```

<sup>&</sup>lt;sup>15</sup> Function arguments are initially unevaluated; see Chapter 17.

Second call:

```
test(3)
## [1] "x"
## <environment: 0x561da7fed9b8>
## List of 2
## $ y: num 9
## $ x: num 3
```

Each time, the current environment is different. This is why we do not see the `y` variable at the start of the second call. It is a brilliantly simple implementation of the storage for local variables.

# 16.3.2 Lexical scope and function closures

We were able to access the **print** function (amongst others) in the above example. This should make us wonder what the enclosing environment of that local environment is.

```
print_enclosure <- function()
    print(parent.env(sys.frame(sys.nframe())))

print_enclosure()
## <environment: R_GlobalEnv>
```

It is the global environment. Let us evaluate the same function from within another one:

```
call_print_enclosure <- function()
    print_enclosure()

call_print_enclosure()
## <environment: R_GlobalEnv>
```

It is the global environment again. If R used the so-called *dynamic scoping*, we would see the local environment of the function that invoked the one above. If this were true, we would have access to the caller's local variables from within the callee.

**Important** Objects of the type closure, i.e., user-defined<sup>16</sup> functions, consist of three components:

- a list of formal arguments (compare **formals** and Section 15.4.1);
- an expression (compare body and Section 15.4.1 again);

<sup>&</sup>lt;sup>16</sup> There are two other types of functions: a special is an internal function that does not necessarily evaluate its arguments (e.g., switch, if, or quote; compare also Chapter 17), whereas a builtin always evaluates its actual parameters, e.g., sum.

• a reference to the *associated environment* where the function might store data for further use (see **environment**).

By default, the associated environment is set to the current environment where the function was created.

A local environment created during a function's call has this associated environment as its closure.

Due to this, we say that R has lexical (static) scope.

Thence, in the above example, we have:

```
environment(print_enclosure) # print the associated environment
## <environment: R_GlobalEnv>
```

**Example 16.7** Consider the following function that prints out `x` defined outside of its scope:

```
test <- function() print(x)</pre>
```

Now:

```
x <- "x in global"
test()
## [1] "x in global"</pre>
```

printed out x from the user workspace because this is precisely the environment associated with the function.

However, setting the associated environment to a different one that also happens to define `x` will give a different result:

```
e <- new.env()
e[["x"]] <- "x in e"
environment(test) <- e
test()
## [1] "x in e"</pre>
```

# **Example 16.8** Consider the following example:

```
cat(sprintf("x = %s\n", x))
}

x <- "spam"
subtest()
environment(subtest) <- globalenv()
subtest()
}

x <- "bacon"
test()
## test: current env: <environment: 0x561da79b8c50>
## subtest: enclosing env: <environment: 0x561da79b8c50>
## x = spam
## subtest: enclosing env: <environment: R_GlobalEnv>
## x = bacon
```

Here is what happened.

- A call to test creates a local function subtest, whose associated environment is set to the local frame of the current call. It is precisely the current environment where subtest was created.
- 2. The above explains why **subtest** can access the local variable `x` inside its maker.
- 3. Then we change the environment associated with **subtest** to the global one.
- 4. In the next call to **subtest**, unsurprisingly, we gain access to  $\hat{x}$  in the user workspace.

**Note** In lexical (static) scoping, which variables a function refers to can be deduced by reading the function's body only and not how it is called in other contexts. This is the theory. Nevertheless, the fact that we can freely modify the associated environment anywhere can complicate the program analysis greatly.

If we find the rules of lexical scoping confusing, we ought to refrain from referring to objects outside of the current scope ("global" or "non-local" variables") except for the functions defined as top-level ones or coming from the external packages. It is what we have been doing so far most of the time.

# 16.3.3 Application: Function factories

As closures are functions with associated environments, and the role of environments is to store information, we can consider closures = functions + data.

We have already seen that in Section 9.5.3, where we described the approxfun function. To recall:

```
x \leftarrow seq(0, 1, length.out=11)
f1 <- approxfun(x, x^2)</pre>
print(f1)
## function (v)
## .approxfun(x, y, v, method, yleft, yright, f, na.rm)
## <environment: 0x561da7eb55e0>
```

The variables `x`, `y`, etc., that **f1**'s source code refers to, are stored inside its dedicated, associated environment:

```
ls(envir=environment(f1))
## [1] "f"
            "method" "na.rm" "x"
                                                  "yleft" "yright"
```

We are used to referring to the routines such as approxfun as function factories. They return functions whose non-local variables are stored in their associated environments.

**Example 16.9** *Consider the following function factory:* 

```
gen power <- function(p)</pre>
    function(x) x^p # p references a non-local variable
```

A call to **gen\_power** creates a local environment that defines one variable,  $\hat{p}$ , where argument's value is stored. Then, we create a function whose associated environment (remember that R uses lexical scoping) is that local one. Therefore, the reference to the non-local  $\hat{p}$  in its body will be resolved therein. This new function is returned by **gen\_power** to the caller. Normally, the local environment would be destroyed, but it is still used after the call, so it will not be garbage-collected.

Example calls:

```
(square <- gen_power(2))</pre>
## function(x) x^p
## <environment: 0x561da61f63a0>
(cube <- gen power(3))</pre>
## function(x) x^p
## <environment: 0x561da676e228>
cube(2)
## [1] 8
square(2)
## [1] 4
```

The underlying environment can, of course, be modified:

```
assign("p", 7, envir=environment(cube))
cube(2) # so much for the cube
## [1] 128
```

**Example 16.10** *Negate* is another example of a built-in function factory. Study its source code:

```
print(Negate)
## function (f)
## {
##     f <- match.fun(f)
##     function(...) !f(...)
## }
## <environment: namespace:base>
```

# **Example 16.11** *In* [36], the following example is given:

```
account <- function(total)
    list(
        balance = function() total,
        deposit = function(amount) total <<- total+amount,
        withdraw = function(amount) total <<- total-amount
)

Robert <- account(1000)
Ross <- account(500)
Robert$deposit(100)
Ross$withdraw(150)
Robert$balance()
## [1] 1100
Ross$balance()
## [1] 350</pre>
```

We can now fully understand why the above code does what it does. It somewhat resembles a class with three methods and one data field. No wonder why reference classes (Section 16.1.5) were introduced at some point: they are based on the same concept.

**Exercise 16.12** Write a function factory named **gen\_counter** which implements a simple counter that is increased by one upon each call thereto.

```
gen_counter <- function() ...to.do...
c1 <- gen_counter()
c2 <- gen_counter()
c(c1(), c1(), c2(), c1(), c2())
## [1] 1 2 1 3 2</pre>
```

Moreover, write a function that resets a given counter to zero.

```
reset_counter <- function(counter_fun) ...to.do...
reset_counter(c1)
c1()
## [1] 1</pre>
```

# 16.3.4 Accessing the calling environment

We know that the environment associated with a function is not necessarily the same as the environment from which the function was called, sometimes quite confusingly referred to as the *parent frame*.

R maintains a whole *frame stack*. The global environment is assigned the number 0. Each call to a function increases the stack by one frame, whereas returning from a call decreases the counter.

To get the current frame number, we call **sys.nframe**. This is why **sys.frame**(**sys.nframe**()) returns the current environment.

We can fetch the calling environment by referring to parent.frame() or sys. frame(sys.parent()), amongst others<sup>17</sup>.

Thanks to parent.frame, we may evaluate arbitrary expressions in (on behalf of) the calling environment. Typically, we should not be doing that. However, some built-in functions rely on this feature, hence our avid interest in it here. We will discuss a few of its use cases below.

# 16.3.5 Package namespaces (\*)

Any R package, say, pkg, defines two environments:

- namespace:pkg where all objects are defined (functions, vectors, etc.); this is the enclosing environment of all closures in the package;
- package:pkg can be attached to the search path; contains selected be objects from namespace:pkg that can be accessed by the user.

We will use our example package discussed in Section 7.3.1. Recall that it is available for download from https://github.com/gagolews/rpackagedemo/.

```
library("rpackagedemo") # https://github.com/gagolews/rpackagedemo/
## Loading required package: tools
```

Here is its DESCRIPTION file:

Package: rpackagedemo

Type: Package

Title: Just a Demo R Package

Version: 1.0.2 Date: 1970-01-01

Author: Anonymous Llama

Maintainer: Unnamed Kangaroo <roo@inthebush.au>

(continues on next page)

<sup>&</sup>lt;sup>17</sup> In **help**("sys.parent"), we read that the parent frame number, as returned by **sys.parent**(), is not necessarily equal to **sys.nframe**()-1. It is certainly true if we are at the top (global) level.

<sup>&</sup>lt;sup>18</sup> Exported using the export or exportPattern directive of the package's NAMESPACE file; see Section 1 in [59].

```
Description: Provides a function named bamboo(), just give it a shot.

License: GPL (>= 2)

Imports: stringx

Depends: tools
```

The Import and Depends fields specify which packages (apart from **base**) ours depends on. As we can see above, all items in the latter list are attached to the search path on a call to **library**.

The NAMESPACE file specifies the names imported from other packages and those that are expected to be visible to the user:

```
importFrom(stringx, sprintf)
importFrom(tools, toTitleCase)
S3method(print, koala)
S3method(print, kangaroo, .a_hidden_method_to_print_a_roo)
export(bamboo)
```

Thus, our package exports one object, a function named **bamboo** (we will discuss the S3 methods in the next section). It is included in the "package:rpackagedemo" environment attached to the search path:

```
ls(envir=as.environment("package:rpackagedemo")) # ls("package:rpackagedemo")
## [1] "bamboo"
```

Let us give it a shot:

```
bamboo("spanish inquisition") # rpackagedemo::bamboo
## G'day, Spanish Inquisition!
```

We did not expect that at all.

Let us inspect its source code:

```
print(bamboo)
## function (x = "world")
## cat(prepare_message(toTitleCase(x)))
## <environment: namespace:rpackagedemo>
```

We see a call to **toTitleCase** (most likely from **tools**, and this is indeed the case) and to **prepare\_message** which is not listed in the package's imports. We definitely cannot access it directly:

```
prepare_message
## Error in eval(expr, envir, enclos): object 'prepare_message' not found
```

It turns out that it is the package's internal function. It is thus included in the "namespace:rpackagedemo" environment.

```
(e <- environment(rpackagedemo::bamboo)) # or getNamespace("rpackagedemo")</pre>
## <environment: namespace:rpackagedemo>
ls(envir=e)
## [1] "bamboo"
                          "prepare_message" "print.koala"
```

We can get it via the `:::` operator:

```
print(rpackagedemo:::prepare_message)
## function (x)
## sprintf("G'day, %s!\n", x)
## <environment: namespace:rpackagedemo>
```

All functions defined in a package have the corresponding package namespace as their associated environment. As a consequence, bamboo can refer to prepare\_message directly.

Now, it will be educative to inspect the enclosure of "namespace: rpackagedemo":

```
(e <- parent.env(e))</pre>
## <environment: 0x561da774a6e8>
## attr(,"name")
## [1] "imports:rpackagedemo"
ls(envir=e)
## [1] "sprintf"
                    "toTitleCase"
```

It is the environment featuring the bindings to all the imported objects. This is why our package can also refer to stringx::sprintf and tools::toTitleCase.

Its enclosure is the namespace of the base package (not to be confused with "package:base"):

```
(e <- parent.env(e))</pre>
## <environment: namespace:base>
```

The next enclosure is, interestingly, the global environment:

```
(e <- parent.env(e))</pre>
## <environment: R_GlobalEnv>
```

Then, of course, the whole search path follows (Section 16.2.5); see Figure 16.4 for an illustration.

**Note** (\*\*) All environments related to packages are locked, which means that we cannot change any bindings within their frames; compare help("lockEnvironment").

In the extremely rare event of needing to patch an existing function within an already loaded package, we can call unlockBinding followed by assign to change its definition.

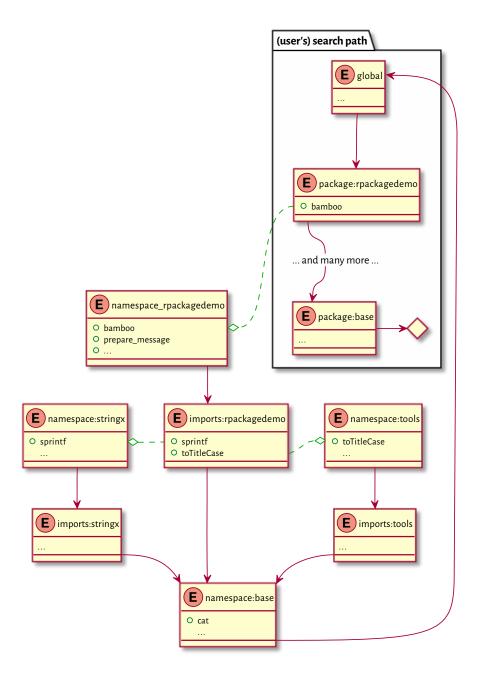


Figure 16.4: A search path for an example package; Dashed lines represent environments associated with closures, whereas solid lines denote enclosing environments; References to objects within each package are resolved inside their respective namespaces

```
new_message <- function (x) sprintf("Nobody expects %s!\n", x)</pre>
e <- getNamespace("rpackagedemo")</pre>
environment(new_message) <- e # set enclosing environment (very important!)</pre>
unlockBinding("prepare_message", e)
assign("prepare_message", new_message, e)
rm("new_message")
bamboo("the spanish inquisition")
## Nobody expects The Spanish Inquisition!
```

R is indeed a quite hackable language (except in the cases where it is not).

**Exercise 16.13** (\*\*) A function or a package might register certain functions (hooks) to be called upon various events, e.g., attaching a package to the search patch; see **help**("setHook") and help(".onAttach").

- Inspect the source code of plot.new and notice a reference to a hook named "before.plot. new". Try setting such a hook yourself (e.g., one that changes some graphics parameters discussed in Section 13.2) and see what happens upon each call to a plotting function.
- 2. Define the .onLoad, .onAttach, .onUnload, and .onDetach functions in your own R package and take note of when they are invoked.

**Exercise 16.14** (\*\*) For the purpose of this book, we have registered a custom "before.plot. new" hook that sets our favourite graphics parameters that we described in Section 13.2.4. Moreover, we modified **plot.window** slightly to obtain the white grid on a grey background, e.g., in Figure 13.13.

Apply similar hacks to the **graphics** package so that its outputs suit your taste better.

#### 16.3.6 S3 method lookup by UseMethod (\*)

Let us go back to the rpackagedemo example. Inspecting the NAMESPACE file, we see that the package defines two print methods: for printing S3 objects of the classes koala and kangaroo.

The package is attached to the search path. Therefore, we can access these methods via a call to the corresponding generic:

```
print(structure("Tiny Teddy", class="koala"))
## This is a cute koala, Tiny Teddy
print(structure("Moike", class="kangaroo"))
## This is a very naughty kangaroo, Moike
```

However, the package does not make the definitions of these S3 methods available to the user, at least not directly. It is not the first time when we have experienced such an obscuration.

In the first case, the method is simply hidden in the package namespace. It is still available under the expected name:

```
rpackagedemo:::print.koala
## function (x, ...)
## cat(sprintf("This is a cute koala, %s\n", x))
## <environment: namespace:rpackagedemo>
```

In the second case, it appears under a very different identifier:

```
rpackagedemo:::.a_hidden_method_to_print_a_roo
## function (x, ...)
## cat(sprintf("This is a very naughty kangaroo, %s\n", x))
## <environment: namespace:rpackagedemo>
```

Since the base **UseMethod** is still able to find them, we suspect there probably is a global register of all S3 methods. And this is indeed the case.

We can use getS3method to get access to what is available via UseMethod:

```
getS3method("print", "kangaroo")
## function (x, ...)
## cat(sprintf("This is a very naughty kangaroo, %s\n", x))
## <environment: namespace:rpackagedemo>
```

**Important** Overall, the search for methods is performed in two places:

 in the environment where the generic is called (the current environment); this is why defining print.kangaroo in the current scope will use this method instead of the one from the package:

```
print.kangaroo <- function(x, ...) cat("Nobody expects", x, "\n")
print(structure("the Spanish Inquisition", class="kangaroo"))
## Nobody expects the Spanish Inquisition</pre>
```

2. in the internal S3 methods table (registration database).

See **help**("UseMethod") for more details. Also, recall that in Section 10.2.3, we said that **UseMethod** is not the only way to perform method dispatching. There are also internal generics (**help**("InternalMethods")) and group generic functions (**help**("groupGeneric")).

**Exercise 16.15** (\*) Study the source code of **getS3method**. Note the reference to the base::.\_\_S3MethodsTable\_\_. object which is for R's internal use (we ought not to tinker with it directly). Moreover, study the **registerS3method** function with which we can define new S3 methods not necessarily following the **generic.classname** convention.

### 16.4 Exercises

**Exercise 16.16** Asking too many questions is not very charismatic, but challenge yourself by trying to find the answer to the following.

- What is the role of a frame in an environment?
- What is the role of an enclosing environment? How to read it or set it?
- What is the difference between a named list and an environment?
- What functions and operators work on named lists but cannot be applied on environments?
- What do we mean by saying that environments are not passed by value to R functions?
- What do we mean by saying that objects are sometimes copied on demand?
- What happens if a name listed in an expression to be evaluated is not found in the current environment?
- How and what kind of objects can we attach to the search path?
- What happens if we have two identical object names on the search path?
- What do we mean by saying that package namespaces are locked when loaded?
- What is the current environment when we evaluate an expression "on the console"?
- What is the difference between `<-` and `<<-`?
- Do packages have their own search paths?
- What is a function closure?
- What is the difference between the dynamic and the lexical scope?
- When evaluating a function, how is the enclosure of the current (local) environment determined? Is it the same as the calling environment? How to get it/them programmatically?
- How and why function factories work?
- (\*) What is the difference between the "package: pkg" and "namespace: pkg" environments?
- How do we fetch the definition of an S3 method that does not seem to be available directly via the standard accessor **generic.classname**?
- (\*) base::print.data.frame calls base::format.data.frame (directly). Will the introduction of print.data.frame in the current environment affect how data frames are printed?
- (\*) On the other hand, **base**::**format.data.frame** calls the generic **base**::**format** on all the input data frame's columns. Will the overloading of the particular methods affect how data frames are printed?

#### Exercise 16.17 Calling:

```
pkg <- available.packages()
pkg[, "Package"] # a list of the names of available packages
pkg[, "Depends"] # dependencies</pre>
```

gives the list of available packages and their dependencies. Convert the dependency lists to a list of character vectors (preferably using regular expressions; see Section 6.2.4).

Then, generate a list of reverse dependencies: what packages depend on each given package.

Use an object of the type environment (a hash table) to map the package names to numeric IDs (indexes). It will significantly speed up the whole process (compare it to a named list-based implementation).

**Exercise 16.18** According to [63], compare also Section 9.4.6, a call to:

```
add(x, f(x)) \ll v
```

translates to:

```
`*tmp*` <- get(x, envir=parent.env(), inherits=TRUE)
x <<- `add<-`(`*tmp*`, f(x), v) # note: not f(`*tmp*`)
rm(`*tmp*`)</pre>
```

Given:

```
`add<-` <- function(x, where=TRUE, value)
{
    x[where] <- x[where] + value
    x # the modified object that will replace the original one
}

y <- 1:5
f <- function() { y <- -(1:5); add(y, y==-3) <<- 1000; y }</pre>
```

Explain why the following calls yield the results they give:

```
f()
## [1] -1 -2 -3 -4 -5
print(y)
## [1] 1 2 1003 4 5
```

# Lazy evaluation (\*\*)

The ability to create, store, and manipulate unevaluated expressions so that they can be computed later is not particularly special. Many languages enjoy such *metaprogramming* (computing *on* the language, reflection) capabilities, e.g., Lisp, Scheme, Wolfram, Julia, amongst many others.

However, R inherited from its predecessor, the S language, a variation of lazy¹ (nonstrict, noneager, delayed) evaluation of function arguments. They are only computed when their *values* are first needed. As we can take the expressions used to generate them (via **substitute**; see Section 15.4.2), we shall see that we can ignore their meaning in the original (caller's) context and compute them in a very different one.

# 17.1 Evaluation of function arguments

We know that calls such as `if`(test, ifyes, ifno), `||`(mustbe, maybe), or `&&`(mustbe, maybe) do not have to evaluate all their arguments.

```
{cat(" first "); FALSE} && {cat(" second "); FALSE}
## first
## [1] FALSE
{cat(" first "); TRUE } && {cat(" Spanish Inquisition "); FALSE}
## first Spanish Inquisition
## [1] FALSE
```

We can write such functions ourselves. For instance:

```
test <- function(a, b, c) a + c  # b is unused
test({cat("spam\n"); 1}, {cat("eggs\n"); 10}, {cat("salt\n"); 100})
## spam
## salt
## [1] 101</pre>
```

The second argument was not referred to in the function's body. Therefore, it was not evaluated.

<sup>&</sup>lt;sup>1</sup> But without the memoisation of results generated by expressions, which is available, e.g., in Haskell. In other words, in an expression like c(f(x), f(x)), the call f(x) will still be performed twice.

### **Example 17.1** *Study the following very carefully.*

```
test <- function(a, b, c)
{
    cat("Arguments passed to test (expressions): \n")
    cat("a = ", deparse(substitute(a)), "\n")
    cat("b = ", deparse(substitute(b)), "\n")
    cat("c = ", deparse(substitute(c)), "\n")
    subtest <- function(x, y, z)</pre>
    ſ
        cat("Arguments passed to subtest (expressions): \n")
        cat("x = ", deparse(substitute(x)), "\n")
        cat("y = ", deparse(substitute(y)), "\n")
        cat("z = ", deparse(substitute(z)), "\n")
        cat("Using x and z... ")
        retval <- x + z # does not refer to `y`
        cat("Cheers!\n")
        retval
   }
   cat("Using c... ")
    c # force evaluation; we do not even have to be particularly creative
    subtest(a, \sim!\sim b*2 := headache \rightarrow ha@x$y, c*10) # no evaluation yet!
}
environment(test) <- new.env() # to spice things up</pre>
test(
    {testx <- "goulash"; cat("spam\n"); 1},
    {testy <- "kabanos"; cat("eggs\n"); MeAn(egGs+whatever&!!weird[stuff])},
    {testx <- "kransky"; cat("salt\n"); 100}</pre>
)
## Arguments passed to test (expressions):
            testx <- "goulash" cat("spam\n") 1 }
testy <- "kabanos" cat("eggs\n") MeAn(egGs + whatever ...
## a = {
## b = {
## c = {
            testx <- "kransky" cat("salt\n") 100 }
## Using c... salt
## Arguments passed to subtest (expressions):
## x = a
## y = `:=`(~!~b * 2, ha@x$y <<- headache)
## z = c * 10
## Using x and z... spam
## Cheers!
## [1] 1001
```

```
print(testx)
## [1] "goulash"
print(testy)
## Error in eval(expr, envir, enclos): object 'testy' not found
```

On a side note, the `~` (formula) operator will be discussed in Section 17.6. Furthermore, the `:=` operator was used in an ancient version of R for assignments. The parser still recognises it, yet now it has no associated meaning.

### **Important** We note what follows.

- Either the evaluation of an argument does not happen, or is triggered only once (in which case the result is cached).
- Evaluation is *delayed* until the very first request for the underlying value (we call it *lazy evaluation*).
- Evaluation takes place in the calling environment (parent frame).
- Fetching the expression passed as an argument using **substitute** (Section 15.4.2) or checking if an argument was provided with **missing** (Section 15.4.3) does not trigger the evaluation.
- Merely passing arguments further to another function usually does not trigger the evaluation.

We wrote *usually* because functions of the type builtin (e.g., c, list, sum, `+`, `&`, and `:`) always evaluate the arguments. There is no lazy evaluation in the case of the arguments passed to group generics; see help("groupGeneric") and Section 10.2.6. Furthermore, replacement functions' values arguments (Section 9.4.6) are computed eagerly.

**Exercise 17.2** Study the source code of **system.time** and notice the use of delayed evaluation to measure the duration of the execution of a given expression. Also, **on.exit** (Section 17.4) reacts to possible exceptions.

**Example 17.3** It turns out that the role of **substitute** is broader than just getting the expression passed as an argument. We can actually replace each occurrence of every name from a given dictionary (a named list or an environment).

For instance:

```
cat("ex =", deparse(ex), "\n")
        cat("ey =", deparse(ey), "\n")
        eval(as.call(list(substitute, ey, list(x=ex))))
   }
    subtest(spam(!x[x](x)))
}
test(eels@hovercraft)
## ex = eels@hovercraft
## ey = spam(!x[x](x))
## spam(!eels@hovercraft[eels@hovercraft](eels@hovercraft))
```

This way, we could fetch the expression passed as the x argument to the calling function and replace every occurrence of x in the expression ey.

**substitute** does not evaluate its first argument. Hence, if we called **substitute**(ey, ...), we would treat `ey` as a quoted name.

#### **Exercise 17.4** Study the source code of replicate:

```
print(replicate)
## function (n, expr, simplify = "array")
## sapply(integer(n), eval.parent(substitute(function(...) expr)),
       simplify = simplify)
##
## <environment: namespace:base>
```

**Exercise 17.5** (\*) Implement your version of the **bquote** function.

**Note** (\*) Internally, lazy evaluation of arguments is implemented using the so-called promises (compare [63]). As such, they consist of:

- an expression (which we can access by calling substitute);
- an environment where the expression is to be evaluated (once this happens, it is set to NULL);
- a cached value (computed on demand, once).

This interface is not really visible from within R, but see help("delayedAssign").

**Exercise 17.6** Inspect the definition of match.fun. Why is it called by, e.g., apply, Map, or outer?

Note that it uses **eval.parent(substitute(substitute(FUN)))** to fetch the expression representing the argument passed by the calling function (but it is probably very rarely needed there). Compare:

```
test <- function(x)
{
    subtest <- function(y)
    {
        # NOT: substitute(y)
        # NOT: eval.parent(substitute(y))
        eval.parent(substitute(substitute(y)))
    }
    subtest(x*3)
}

test(1+2)
## (1 + 2) * 3</pre>
```

# 17.2 Evaluation of default arguments

As we know from Section 9.5.4, default arguments are special expressions specified in a function's parameter list. When a function's body requires the value of an argument that the caller did not provide, the default expression will be evaluated *in the current (local) environment* of the function. It is thus different from the case of normally passed arguments, which are interpreted in the context of the calling environment.

```
x <- "banana"
test <- function(y={cat("spam\n"); x})</pre>
{
    cat(deparse(substitute(y)), "\n")
    cat("bacon\n")
    x <- "rotten potatoes"
    cat(y, y, "\n")
}
test(x)
## x
## bacon
## banana banana
test()
## {
         cat("spam\n")
                           x }
## bacon
## spam
## rotten potatoes rotten potatoes
```

```
test({cat("spam\n"); x})
## {
       cat("spam \ n") x 
## bacon
## spam
## banana banana
```

As usual, the evaluation is triggered only once, where it is explicitly requested, and only when needed.

**Example 17.7** *Consider the following example from [36]:* 

```
sumsq <- function(y, about=mean(y), na.rm=FALSE)</pre>
{
    if (na.rm)
        y <- y[!is.na(y)]</pre>
    sum((y - about)^2)
}
sumsq(c(1, NA_real_, NA_real_), na.rm=TRUE)
## [1] 0
```

The nice side effect is that the computation of the mean may take into account the removal of the missing values if requested.

However, as the idea of lazy evaluation of arguments is alien to most programmers (especially those coming from different languages), it might be better to rewrite the above using a call to missing (Section 15.4.3):

```
sumsq <- function(y, about, na.rm=FALSE)</pre>
    if (na.rm)
        y < -y/!is.na(y)
    if (missing(about))
        about <- mean(y)
    sum((y - about)^2)
}
sumsq(c(1, NA_real_, NA_real_), na.rm=TRUE)
## [1] 0
```

or better even:

```
sumsq <- function(y, about=NULL, na.rm=FALSE)</pre>
{
     if (na.rm)
         y \leftarrow y[!is.na(y)]
                                                                              (continues on next page)
```

```
if (is.null(about))
     about <- mean(y)
     sum((y - about)^2)
}
sumsq(c(1, NA_real_, NA_real_), na.rm=TRUE)
## [1] 0</pre>
```

Exercise 17.8 The default arguments to do.call, list2env, and new.env are set to parent. frame. What does that mean?

**Exercise 17.9** Study the source code of the **local** function:

```
print(local)
## function (expr, envir = new.env())
## eval.parent(substitute(eval(quote(expr), envir)))
## <environment: namespace:base>
```

# 17.3 Ellipsis, `...`, revisited

If our function features the dot-dot-dot parameter, `...`, whatever we pass through it is packed into a pairlist of promise expressions. Thus, we can relish the benefits of lazy evaluation. In particular, we can redirect all `...`-fed arguments to another call as-is.

```
test <- function(...)
{
    subtest <- function(x, ...)
    {
        cat("x = "); str(x)
        cat("... = "); str(list(...))
}

subtest(...)
}

test({cat("eggs! "); 1}, {cat("spam! "); 2}, z={cat("rice! "); 3})

## x = eggs! num 1

## ... = spam! rice! List of 2

## $ : num 2

## $ z: num 3</pre>
```

**Exercise 17.10** In the documentation of *lapply*, we read that this function is called like "*lap-*

ply(X, FUN, ...)", where `...` are optional arguments to FUN. Verify that whatever is passed via the ellipsis is evaluated only once and not on each application of FUN on the elements of X.

**Example 17.11** We know from Chapter 13 that many high-level graphics functions rely on multiple calls to more primitive functions that allow for setting a variety of parameters (e.g., via par). A common scenario is for a high-level function to submit all the passed arguments to more basic routines. Each underlying procedure can then decide by itself which items it is interested in.

```
test <- function(...)
{
    subtest1 <- function(..., a=1) c(a=a)
    subtest2 <- function(..., b=2) c(b=b)
    subtest3 <- function(..., c=3) c(c=c)

    c(subtest1(...), subtest2(...), subtest3(...))
}
test(a="A", b="B", d="D")
##    a    b    c
## "A" "B" "3"</pre>
```

Here, for instance, **subtest1** only consumes the value of `a` and ignores all the other arguments whatsoever. **plot.default** (amongst others) relies on such a design pattern.

...length() fetches the number of items passed via the ellipsis, ...names() retrieves their names (in the case they are given as keyword arguments), and ...elt(i) gives the *value* of the *i*-th element. Furthermore, ..1, ..2, and so forth are synonymous with ...elt(1), ...elt(2), etc.

```
test <- function(...)
{
    cat("length:", ...length(), "\n")
    cat("names: ", paste(...names(), collapse=", "), "\n")
    for (i in seq_len(...length()))
        cat(i, ":", ...elt(i), "\n")
    print(substitute(...elt(i)))
}

test(u={cat("honey! "); "a"}, {cat("gravy! "); "b"}, w={cat("bacon! "); "c"})
## length: 3
## names: u, , w
## honey! 1 : a
## gravy! 2 : b
## bacon! 3 : c
## ...elt(3L)</pre>
```

Note that ...elt(i) triggers the evaluation of the respective argument. Unfortu-

nately, we cannot use **substitute** to fetch the underlying expression. Instead, we can rely on **match.call** discussed in Section 15.4.4:

```
test <- function(a, b, ..., z=1)
{
    e <- match.call()[-1]
    as.list(e[!(names(e) %in% names(formals(sys.function())))])
}

str(test(1+1, 2+2, 3+3, 4+4, a=2, z=8, w=4))
## List of 4
## $ : language 2 + 2
## $ : language 3 + 3
## $ : language 4 + 4
## $ w: num 4</pre>
```

**Note** Objects passed via `...`, even if they are specified as keyword arguments, cannot be referred to by their name as if they were local variables:

```
test <- function(...) zzz
test(zzz=3)
## Error in test(zzz = 3): object 'zzz' not found</pre>
```

In other words, no assignment in the local environment is triggered.

**Exercise 17.12** Implement your version of the built-in switch function.

**Exercise 17.13** Write your version of the **stopifnot** function.

# 17.4 on.exit(\*)

**on.exit** registers an expression to be evaluated at the very end of a call, regardless of whether the function exited due to an error or not. It might be used to reset the temporarily modified graphics parameters (see **par**) and system options (**options**) or clean up the allocated resources (e.g., close all open file connections).

For instance:

```
cat("roti canai\n")
    if (reset)
        on.exit() # cancels all (replace by nothing)
    if (error)
        stop("aaarrgh!")
    cat("end\n")
    "return value"
}
test()
## roti canai
## end
## bacon
## spam
## [1] "return value"
test(reset=TRUE)
## roti canai
## end
## [1] "return value"
test(error=TRUE)
## roti canai
## Error in test(error = TRUE): aaarrgh!
## bacon
## spam
```

We can always do without on.exit, e.g., by applying proper exception handling techniques; see Section 8.2.

**Exercise 17.14** In the definition of **scan**, notice the call to:

```
on.exit(close(file))
```

Is its purpose to close the file on exit?

**Exercise 17.15** Why does **graphics**::barplot.default call the following expressions?

```
dev.hold()
opar <- if (horiz) par(xaxs="i", xpd=xpd) else par(yaxs="i", xpd=xpd)
on.exit({
    dev.flush()
    par(opar)
})
```

# 17.5 Metaprogramming and laziness in action: Examples (\*)

Due to lazy evaluation, we can define functions that allow any random gibberish as their arguments as long as they are syntactically valid R expressions. Nothing but basic decency stops us from interpreting them in any way we want. Each such function can become a microverse (a microlanguage?) by itself. This will surely confuse<sup>2</sup> our users, as they will have to analyse every procedure's behaviour separately.

In this section, we extend on our notes from Section 9.5.7 and Section 12.3.9. We look at a few built-in functions relying on metaprogramming and laziness, mostly because studying them is a good exercise. It can help extend our programming skills and deepen our understanding of the concepts discussed in this part of the book.

By no means is it an invitation to use them in practice.

Still, R's computing on the language capabilities might interest some advanced programmers (e.g., package developers).

### 17.5.1 match.arg

match.arg was mentioned in Section 9.5.7. When called normally, it matches a string against a set of possible choices, similarly to pmatch:

```
choices <- c("spam", "bacon", "eggs")
match.arg("spam", choices)
## [1] "spam"
match.arg("s", choices) # partial matching
## [1] "spam"
match.arg("eggplant", choices) # no match
## Error in match.arg("eggplant", choices): 'arg' should be one of "spam",
## "bacon", "eggs"
match.arg(choices, choices) # match first
## [1] "spam"</pre>
```

However, skipping the second argument, this function will fetch the choices from the default argument of the function it is enclosed in!

```
test <- function(x=c("spam", "bacon", "eggs"))
    match.arg(x)

test("spam")
## [1] "spam"
test("s")

(continues on next page)</pre>
```

<sup>&</sup>lt;sup>2</sup> Novices are prone to overgeneralising when they learn new material that they are still far from comfortable with. Such exceptions go against this natural coping strategy of theirs.

```
## [1] "spam"
test("eggplant")
## Error in match.arg(x): 'arg' should be one of "spam", "bacon", "eggs"
test()
## [1] "spam"
```

**Exercise 17.16** Inspect the source code and the documentation of **stats::binom.test**, which looks like:

```
function(..., alternative = c("two.sided", "less", "greater"))
{
    # ...
    alternative <- match.arg(alternative)
    # ...
}</pre>
```

Note the alternative argument and its peculiar default value.

**Exercise 17.17** Study the source code of match.arg. In particular, notice the following fragment:

```
if (missing(choices)) {
    formal.args <- formals(sys.function(sysP <- sys.parent()))
    choices <- eval(
        formal.args[[as.character(substitute(arg))]],
        envir=sys.frame(sysP)
    )
}</pre>
```

#### 17.5.2 curve

The curve function can be called, e.g., like:

```
curve(sin(1/x^2), 1/pi, 3, 1001, lty=2)
```

which results in Figure 17.1. Wait a minute... We did not define `x` as a sequence ranging between ca. 0.3 and 3!

**Exercise 17.18** Study the source code of **curve**. Take note of the following fragment of its definition:

```
function(expr, from=NULL, to=NULL, n=101, xlab="x", type="l", ...)
{
    # ...
    expr <- substitute(expr)
    ylab <- deparse(expr)</pre>
```

(continues on next page)

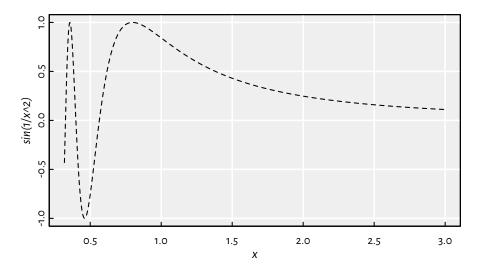


Figure 17.1: An example plot generated by calling curve

```
x <- seq.int(from, to, length.out=n)
ll <- list(x=x)
y <- eval(expr, envir=ll, enclos=parent.frame())
plot(x=x, y=y, type=type, xlab=xlab, ylab=ylab, ...)
# ...
}</pre>
```

### 17.5.3 with and within

Environments and named lists (and hence data frames) are similar (Section 16.1.2). Due to this, the envir argument to **eval** can be set to either.

Therefore, for instance:

```
eval(quote(head(Sepal.Length)), envir=iris)
## [1] 5.1 4.9 4.7 4.6 5.0 5.4
```

evaluates the given expression in something like list2env(iris, parent=parent. frame()). Thus, even though Sepal.Length is not a standalone variable, it is treated as one *inside* the iris data frame.

The enclosure is set to the calling frame. Hence, we can successfully refer to the head function located somewhere on the search path. This is somewhat similar to attach (Section 16.2.6) but without modifying the search path.

The with function does exactly the above:

```
print(with.default)
## function (data, expr, ...)
## eval(substitute(expr), data, enclos = parent.frame())
## <environment: namespace:base>
```

### Example use:

```
with(iris, {
    x <- Sepal.Length # `Sepal.Length` is in `iris`
    mean(x)
})
## [1] 5.8433</pre>
```

As we evaluate the above in the local (temporary) environment, we cannot modify the existing columns of the data frame this way. However, the within function includes a way to detect and apply any changes made.

```
within(iris, {
    Sepal.Length <- Sepal.Length/1000
    Spam <- "yum!"
}) -> iris2
head(iris2, 3)
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species Spam
## 1
           0.0051
                           3.5
                                        1.4
                                                     0.2 setosa yum!
## 2
           0.0049
                           3.0
                                        1.4
                                                     0.2 setosa yum!
## 3
           0.0047
                           3.2
                                        1.3
                                                     0.2 setosa yum!
```

#### **Exercise 17.19** Study the source code of within:

```
print(within.data.frame)
## function (data, expr, ...)
## {
       parent <- parent.frame()</pre>
##
##
        e <- evalq(environment(), data, parent)</pre>
##
        eval(substitute(expr), e)
        l <- as.list(e, all.names = TRUE)</pre>
##
        l <- l[!vapply(l, is.null, NA, USE.NAMES = FALSE)]</pre>
##
       nl <- names(l)</pre>
##
##
       del <- setdiff(names(data), nl)</pre>
       data[nl] <- l
##
       data[del] <- NULL
##
       data
##
## }
## <environment: namespace:base>
```

Note that evalq(expr, ...) is equivalent to eval(quote(expr), ...). Also, vapply(X, FUN, NA, ...) is like a call to sapply, but it guarantees that the result is a logical vector.

#### 17.5.4 transform

We can call **transform** to modify/add columns in a data frame using vectorised functions, for instance:

If we suspect that this function evaluates all expressions passed as `...` within the data frame, we are brilliantly right. Furthermore, there must be some mechanism to detect newly created variables so that new columns can be added.

### **Exercise 17.20** Study the source code of transform:

```
print(transform.data.frame)
## function (`_data`, ...)
## {
       e <- eval(substitute(list(...)), ` data`, parent.frame())</pre>
##
       tags <- names(e)
##
       inx <- match(tags, names(`_data`))</pre>
##
       matched <- !is.na(inx)</pre>
##
##
       if (any(matched)) {
            ` data`[inx[matched]] <- e[matched]
            `_data` <- data.frame(`_data`)
##
##
##
       if (!all(matched))
            do.call("data.frame", c(list(`_data`), e[!matched]))
##
##
       else ` data`
## }
## <environment: namespace:base>
```

In particular, note that `e` is a named list.

#### 17.5.5 subset

The **subset** function selects rows and columns of a data frame that meet certain criteria. For instance:

The second argument, the row selector, must definitely be evaluated within the data

frame. We expect it to reduce itself to a logical vector which then can be passed to the index operator.

The "select all columns except those between the given ones" part can be implemented by assigning each column a consecutive integer and then treating them as numeric indexes.

### **Exercise 17.21** Study the source code of **subset**:

```
print(subset.data.frame)
## function (x, subset, select, drop = FALSE, ...)
## {
##
       chkDots(...)
       r <- if (missing(subset))</pre>
##
           rep len(TRUE, nrow(x))
##
##
       else {
##
            e <- substitute(subset)</pre>
            r <- eval(e, x, parent.frame())</pre>
##
            if (!is.logical(r))
##
                stop("'subset' must be logical")
##
            r & !is.na(r)
##
##
       vars <- if (missing(select))</pre>
##
            rep_len(TRUE, ncol(x))
##
       else {
##
##
            nl <- as.list(seq_along(x))</pre>
##
            names(nl) \leftarrow names(x)
##
            eval(substitute(select), nl, parent.frame())
##
       x[r, vars, drop = drop]
##
## }
## <environment: namespace:base>
```

# A forward-pipe operator

Section 10.5 mentioned the pipe operator, \| | > \| . We can implement its simplified version manually:

```
`%>%` <- function(e1, e2)
{
    e2 <- as.list(substitute(e2))</pre>
    e2 <- as.call(c(e2[[1]], substitute(e1), e2[-1]))</pre>
    eval(e2, envir=parent.frame())
}
```

This function imputes `e1` as the first argument in a call `e2` and then evaluates the new expression.

Example calls:

```
x <- c(1, NA_real_, 2, 3, NA_real_, 5)
x %>% mean # mean(x)
## [1] NA
x %>% `-`(1) # x-1
## [1] 0 NA 1 2 NA 4
x %>% na.omit %>% mean # mean(na.omit(x))
## [1] 2.75
x %>% mean(na.rm=TRUE) # mean(x, na.rm=TRUE)
## [1] 2.75
```

Moreover, we can memorise the value of `e1` under the name, say, `.` so that it can be referred to in the right-hand side expression. This comes at the cost of forcing the evaluation of the left-hand side argument and thus losing the potential benefits of laziness, including access to the generating expression.

```
`%.>%` <- function(e1, e2)
{
    env <- list2env(list(.=e1), parent=parent.frame())
    e2 <- as.list(substitute(e2))
    e2 <- as.call(c(e2[[1]], quote(.), e2[-1]))
    eval(e2, envir=env)
}</pre>
```

This way, we can refer to the value of the left-hand side multiple times in a single call, for instance:

```
set.seed(123); runif(5) %.>% `[`(.>0.5) # x[x>0.5] with x=runif(5)
## [1] 0.78831 0.88302 0.94047
```

This is crazy, I know. I made this. Your author. One more then:

```
# x[x >= 0.5 & x <= 0.9] <- 0.5 with x=round(runif(5), 2):
set.seed(123); runif(5) %.>% round(2) %.>% `[<-`(.>=0.5 & .<=0.9, value=NA)
## [1] 0.29 NA 0.41 NA 0.94</pre>
```

I cannot wait for someone to put this operator into some new R package (it is a brilliant idea, by the way, isn't it?) and then confuse thousands of users ("What is this thing?").

## 17.5.7 Other ideas (\*\*)

Why stop ourselves here? We can create way more invasive functions that read some local variables in the calling functions (unless they are primitive; in R, there are always exceptions to general rules...).

Here is an operator, thanks to which we can select a range of columns in a data frame between two given labels:

```
`%:%` <- function(e1, e2)
{
    # get the `x` argument in the caller (hoping its `[`)
    x <- get("x", envir=sys.frame(sys.nframe()-1))</pre>
    n < - names(x)
    from <- pmatch(substitute(e1), n)</pre>
    to <- pmatch(substitute(e2), n)
    from:to
}
head(iris[, Sepal.W%:%Petal.W])
     Sepal.Width Petal.Length Petal.Width
## 1
             3.5
                           1.4
                                        0.2
## 2
             3.0
                           1.4
                                        0.2
## 3
             3.2
                           1.3
                                        0.2
             3.1
                           1.5
## 4
                                        0.2
## 5
             3.6
                           1.4
                                        0.2
             3.9
                           1.7
## 6
                                        0.4
```

This operator relies on the assumption that it is called in the expression passed as an argument to a non-primitive function which also takes a named vector `x` as an actual parameter. So ugly.

**Exercise 17.22** *Make the above more foolproof:* 

- if `%:%` is used outside of `[` or `[<-`, raise a polite error,
- allow `x` to be a matrix (is it possible?),
- prepare better for the case of less expected inputs.

**Exercise 17.23** Modify the definition of the above operator so that both:

```
iris[, -Sepal.W%:%Petal.W]
iris[, -(Sepal.W%:%Petal.W)]
```

mean "select everything except".

**Exercise 17.24** Define `%:%` for data frames so that:

- x[%:%3, ] means "select the first three rows",
- x[3%:%, ] means "select from the third to the end",
- x[-3%:%,] means "select from the third last to the end",
- x[%:%-10, ] means "select all but the last nine".

The ceiling is the limit. Just please, do not use the above in production.

## 17.6 Processing formulae, `~` (\*)

Formulae were introduced to S in the early 1990s [13]. Their original raison d'être was to specify *statistical models*; compare Section 10.3.4.

From the language perspective, they are merely unevaluated calls to the `~` (tilde) operator. When creating them, we do not even have to apply **quote** explicitly. For instance:

```
f <- (y ~ x1 + x2) # or: `~`(y, x1+x2)
mode(f)
## [1] "call"
class(f)
## [1] "formula"</pre>
```

Hence, formulae are compound objects in the sense given in Chapter 10.

Usually, formulae are equipped with an additional attribute:

```
attr(f, ".Environment")
## <environment: R_GlobalEnv>
```

**Exercise 17.25** Create a function that generates a list of formulae of the form " $y \sim x1+x2+...+xk$ ", for all possible combinations x1, x2, ..., xk (of any cardinality) of elements in a given set of xs. For instance:

```
formula_allcomb <- function(y, xs, env=parent.frame()) ...to.do...</pre>
str(formula_allcomb("len", c("supp", "dose")))
## List of 3
## $ :Class 'formula' language len ~ supp + dose
   ....- attr(*, ".Environment")=<environment: R_GlobalEnv>
## $:Class 'formula' language len ~ dose
   ....- attr(*, ".Environment")=<environment: R_GlobalEnv>
## $ :Class 'formula' language len ~ supp
   ....- attr(*, ".Environment")=<environment: R_GlobalEnv>
str(formula allcomb(
    "y",
   c("x1", "x2", "x3"),
   env=NULL
))
## List of 7
## $ :Class 'formula'
                       language y \sim x1 + x2 + x3
## $ :Class 'formula'
                        language y \sim x2 + x3
## $ :Class 'formula'
                       language y \sim x1 + x3
## $:Class 'formula' language y ~ x3
```

(continues on next page)

```
## $ :Class 'formula' language y ~ x1 + x2
## $ :Class 'formula' language v ~ x2
## $ :Class 'formula' language y ~ x1
```

As they are unevaluated expressions, functions can assign any fantastic meaning to formulae. We cannot really do anything about it. However, many functions, especially in the stats and graphics packages, rely on a call to model.frame and related routines. Thanks to this, we can at least find some behavioural patterns. In particular, help("formula") lists some typical meanings of operators that can be used in a formula.

**Example 17.26** Here are a few examples (executing the expressions below is left as an exercise).

• Draw a box-and-whisker plot for iris[["Sepal.Length"]] split by iris[["Species"]]:

```
boxplot(Sepal.Length~Species, data=iris)
```

 Draw a box plot for ToothGrowth[["len"]] split by a combination of levels in Tooth-Growth[["supp"]] and ToothGrowth[["dose"]]:

```
boxplot(len~supp:dose, data=ToothGrowth)
```

• Split the given data frame by a combination of values in two specified columns therein:

```
split(ToothGrowth, ~supp:dose)
```

• Fit a linear regression model of the form y = a + bx, where y is iris[["Sepal.Length"]] and x is iris[["Petal.Length"]]:

```
lm(Sepal.Length~Petal.Length, data=iris)
```

• Fit a linear regression model of the form z = ax + by, where z is iris[["Sepal.Length"]], x is iris[["Petal.Length"]], and y is iris[["Sepal.Width"]] (without the intercept term):

```
lm(Sepal.Length~Petal.Length+Sepal.Width+0, data=iris)
```

• Fit a linear regression model of the form z = a + bx + cy + dxy, where z is iris[["Sepal. Length"]]+e (with  $\hat{}$ e  $\hat{}$ fetched from the associated environment), and x and y are like above:

```
e <- rnorm(length(iris[["Sepal.Length"]]), 0, 0.05)</pre>
lm(I(Sepal.Length+e)~Petal.Length*Sepal.Width, data=iris)
```

• Draw scatter plots of warpbreaks[["breaks"]] vs their indexes for data grouped by a combination of warpbreaks[["wool"]] and warpbreaks[["tension"]]:

```
Index <- seq_len(NROW(warpbreaks))
coplot(breaks ~ Index | wool * tension, data=warpbreaks)</pre>
```

From the perspective of this book, which focuses on more universal aspects of the R language, formulae are not interesting enough to describe them in any more detail. However, the kind reader is now equipped with all the necessary knowledge to solve the following very educative exercises.

Exercise 17.27 Study the source code of graphics:::boxplot.formula, stats::Im, and stats:::t.test.formula and notice how they prepare and process the calls to model.frame, model.matrix, model.response, model.weights, etc.

Note that their main aim is to prepare data to be passed to **boxplot.default**, **lm.fit** (it is just a function with such a name, not an S3 method), and **t.test.default** 

**Exercise 17.28** Write a function similar to **curve**, but one that allows to specify the function to plot using a formula.

### 17.7 Exercises

**Exercise 17.29** *Answer the following questions.* 

- What is the role of promises?
- Why do we generally discourage the use of functions relying on metaprogramming?
- How are default arguments evaluated?
- Is there anything special about formulae from the language perspective?
- R evaluates function arguments lazily. Does it mean that "y[c(length(y)+1, length(y)+1, length(y)+1)] <- list(1, 2, 3)" extends a list `y` by three elements? Or are there cases where evaluation is eager?</li>

#### Exercise 17.30 Given:

```
test <- function(x, y=deparse(substitute(x)), force_first=FALSE)
{
    if (force_first) y # just force the evaluation of y here
    x <- x**2
    print(y)
}

test(1:5)
## [1] "c(1, 4, 9, 16, 25)"
test(1:5, force_first=TRUE)
## [1] "1:5"</pre>
```

Why did the two above calls yield different results?

### 17.8 Outro

Recall our first approximation to the classification of R data types that we presented in the *Preface*. To summarise what we have covered in this book, let us contemplate Figure 17.2, which gives a much broader picture.

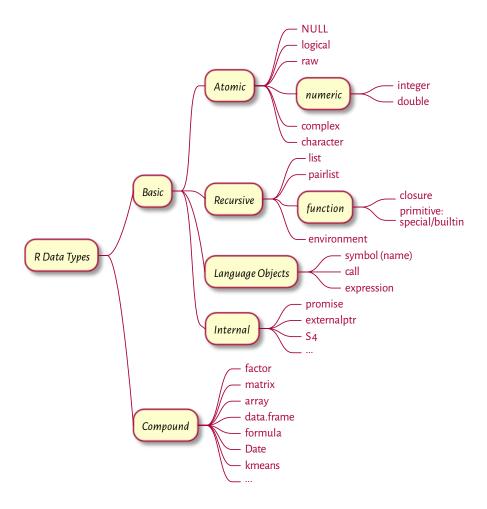


Figure 17.2: R data types

If we omitted something, it was most likely on purpose: either we can now study it on our own easily, it is not really worth our attention, or it violates our *minimalist* design principles that we explained in the *Preface*.

Now that we have reached the end of this course, we might be interested in reading the following materials:

- R Language Definition [63],
- R Internals [62],
- Writing R Extensions [59],
- R's source code available at https://cran.r-project.org/src/base/.

What is more, the NEWS files available at https://cran.r-project.org/doc/manuals/r-release/ will keep us updated with fresh features, bug fixes, and newly deprecated functionality; see also the **news** function.

Please spread the news about this book. Also, check out the other open-access textbook by yours truly, *Minimalist data wrangling with Python*<sup>3</sup> [25]. Thank you.

Good luck with your further projects!

<sup>3</sup> https://datawranglingpy.gagolewski.com/

# Changelog

The most up-to-date version of this book can be found at https://deepr.gagolewski.com/.

**Important** This book is still a work in progress. The first twelve chapters are already quite readable, but there will be more (I might be busy with other projects, though). Stay tuned.

Any bug/typos reports/fixes<sup>4</sup> are appreciated.

Below is the list of the most noteworthy changes:

- under development (vo.2.y.9xxx):
  - Minor extensions.
  - ...work ongoing...
  - TO DO: Chapter 14 (interfacing compiled code)
  - TO DO: copyediting
  - TO DO: proofreading
- **2023-04-27** (vo.2.1):
  - Chapter on graphics drafted.
- 2023-04-09 (VO.2.0):
  - New HTML theme (featuring light and dark modes).
  - Chapter on unevaluated expressions drafted.
  - Chapter on environments and evaluation drafted.
  - Chapter on lazy evaluation drafted.
- 2022-12-29 (VO.1.12):
  - First public release at https://deepr.gagolewski.com.
  - Chapters 1–12 (basic and compound types, functions, control flow, etc.)
     drafted.

<sup>4</sup> https://github.com/gagolews/deepr/issues

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- Preface drafted.
- ISBN 978-0-6455719-2-9 reserved.
- Cover.

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