

# מעבדה בחישוב בטוח בענן 203.4850

## Laboratory in Secure Computation in the Cloud

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Project Topic:

Privacy-preserving machine learning  
SVM inference on FHE encrypted data

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## Background

### Privacy preserving machine learning (PPML)

- **Machine learning**
  - Huge success, training data required, more data higher accuracy
  - Example: deep learning, support vector machines (**SVM**)
  - Privacy threats
- **Privacy preserving machine learning**
  - Utilize secure computation techniques to
  - execute machine learning inference and training,
  - without revealing information on the input beyond the output.

### Fully homomorphic encryption (FHE)

- **FHE** is a conceptually simple secure computation technique:
  - Encryption scheme that allows manipulating ciphertexts (aka, homomorphic evaluation) to produce a ciphertext for a function  $f$  on the underlying message  $m_1, \dots, m_n$ .
  - FHE is specified by four algorithms (**KeyGen**, **Enc**, **Dec**, **Eval**).
  - Standard security and correctness are required.
  - Eval is required to be correct in the sense that, given  $f$  and  $c_1 \leftarrow \text{Enc}_{pk}(m_1), \dots, c_n \leftarrow \text{Enc}_{pk}(m_n)$ , it holds that  $c \leftarrow \text{Eval}_{pk}(f, c_1, \dots, c_n)$  is a ciphertext so that
$$\text{Dec}_{sk}(c) = f(c_1, \dots, c_n)$$
- Useful for **secure outsourcing** supporting protection of data-in-use:
  - Offline: data owner (client) produces keys  $(sk, pk)$ , publishes  $pk$ , encrypts data and upload to cloud server
  - Online:
    - Client sends function  $f$  to the server, plus any additional encrypted or cleartext data as needed
    - server homomorphically evaluate  $f$  on ciphertexts to produce the result ciphertext  $c$ , and sends  $c$  to client
    - client decrypts  $c$  to obtain output
  - Advantages:
    - client's online complexity:

- time to encrypt and decrypt
  - independent of complexity of  $f$
  - server's time polynomial in complexity of  $f$
  - privacy for data owner (client) guaranteed
- **Model of computation:** Computation  $f$  is specified as an **arithmetic circuit**
  - Arithmetic circuits are circuits with gate for Addition and Multiplication operations only
  - $+, \times$  are in a field  $F$ , where  $F$  may be:
    - a finite field, eg  $+ \bmod p, \times \bmod p$ , or
    - (approximate) real numbers
  - Fact:  $(+, \times)$  is complete in the sense that it can compute any  $f$  with no more than a polynomial overhead.
  - Complexity is governed essentially by:
    - **$\times$ -depth** of the circuit, ie, number of multiplication operations along longest path from root to leaf
    - Total **number of multiplication** operations
    - **Depth** = longest path from root to leaf (counting all gates, not just multiplication)
    - **Size** = number of gates in circuit ( $+$  and  $\times$ )
- **Challenges** in designing FHE-friendly algorithms:
  - Low level programming (specifying program as a circuit) may be challenging
  - No branching
  - Worst-case input run-time always
- **Complexity** goals: design circuits that are
  - shallow (ie low  $\times$ -depth), and
  - use few multiplications
  - have “reasonable” (total) depth and size
- Examples:
  - How to compute *sign* function?
  - How to compute greater than operator?

## Project description – SVM inference on FHE encrypted data

### Your Tasks

#### 1) Train SVM model on cleartext data.

- a. Which **training data** to use?

E.g.: life sound signals <https://research.google.com/audioset>

- b. What's the inference goal?

Single class inference; e.g. identify dog bark

- c. What tools to use for training?

See resources below for an initial list of available tools

- d. Which kernels to use?

check accuracy with various common kernels

choose best accuracy vs. performance tradeoff

Hint: polynomial kernels of low degree polynomial achieve

better performance on FHE encrypted data than high degree polynomials

(can you explain why?)

#### 2) Design an arithmetic circuit for computing SVM inference with the SVM model you trained.

- a. Correctness: is your circuit always producing identical results to cleartext inference?

If not, how do they differ?

What's the effect on accuracy?

- b. Complexity: What's the complexity of your circuit ( $\times$ -depth, #mult, depth and size)?

#### 3) Implement inference with your SVM model on FHE encrypted data

- a. Use SEAL library for homomorphic encryption

Note: you must choose whether to work of reals (CKKS) or finite field (FV)

- b. Use your arithmetic circuit as the inference algorithm.

#### 4) Evaluate and optimize: Test your implementation for accuracy and performance.

Can you improve your solution to have better performance or accuracy?

**5) Write a report and documentations**

- a. Report should be in English, written using Latex, and in academic writing style and level
- b. Writing tips (search for more online!)
  - i. Write top-down, motivate each topic before dwelling into details,
  - ii. Each writing unit (report, section, paragraph, etc) should start with a concise sentence explaining its role: what are you going to discuss in this unit? And end with a concise sentence summarizing what your discussed.
  - iii. Write with a natural logical flow to keep reader engaged and comprehending.
- c. Report should include the following sections:
  - i. introduction (concise background, summary and impact of your work),
  - ii. background,
  - iii. your algorithm design,
  - iv. your implementation details,
  - v. your empirical evaluation
  - vi. conclusions
- d. In addition, give documentations and test files to your 1) cleartext training and 2) FHE inference work, with easy to use sample files

**6) Submit: report + code (source files, test and demo files, benchmarks, documentation).**

## Further details: architecture for SVM inference on encrypted data

### Offline:

- Server trains SVM model on cleartext data
- Client generates  $(pk, sk)$ , sends  $pk$  to server.

### Online:

- Client encrypts a data sample  $c \leftarrow \text{Enc}_{pk}(x)$ , and sends the corresponding ciphertexts  $c$  to server
- Server homomorphically evaluates the SVM model on the encrypted data sample  $c$  to produce an encrypted inference outcome  $c'$ , and send  $c'$  to client
- Client decrypts  $c'$  to obtain the inference result.

## Further details: evaluation and optimization

### Accuracy

- Cleartext model evaluation:  
How good is your model? Use standard model evaluation methods to answer.  
E.g. use cross validation, summarize rates of false positive and false negative, summarized in a Confusion map.
- FHE inference vs. cleartext:  
Is the inference result the same as when evaluating the model on cleartext data?

### Performance

- Time of inference on encrypted data: What's the run time (total and in each part)? What's the overhead over cleartext data? What are the bottlenecks?
- Communication complexity: bandwidth (how many bytes are transmitted)?

### Optimization

- Can performance be improved?
- Can accuracy be improved
- Is there a conflict between accuracy and performance? If so, what's your recommended "sweet point"?

## General guidelines

- **You are responsible** for the management of your time, progress, and meetings with me, to ensure the successful completion of your project. Note: report writing typically takes a long time; do take this under consideration when planning your time.
- **Meeting** weekly / every other week to update and discuss is highly recommended.
  - If you're stuck, this could help show a path to examine
  - If you tend to procrastinate, meeting gives you a deadline
  - Even if you think you're doing great – you might unknowingly be off the right path – a meeting can help examine your current situation and give feedback.
- **Excelling students are invited to discuss with me opportunities in my research group**
  - BSc project, MSc project/thesis, PhD thesis
  - Interesting & challenging research projects
  - Stipend (MILGA) may be possible

## Resources (initial list, search for further resources!)

- SEAL FHE library <https://www.microsoft.com/en-us/research/project/microsoft-seal/>
- SVM tutorial (theory, concise) <https://web.mit.edu/zoya/www/SVM.pdf>
- SVM tutorial (useful libraries links) <https://scikit-learn.org/stable/modules/svm.html>
- Training data: life sound signals <https://research.google.com/audioset>
- Research papers on privacy preserving machine learning with FHE